

Chapter 9, Solution 12.

Let $\mathbf{X} = 4\angle 40^\circ$ and $\mathbf{Y} = 20\angle -30^\circ$. Evaluate the following quantities and express your results in polar form.

$$(\mathbf{X} + \mathbf{Y})/\mathbf{X}^*$$

$$(\mathbf{X} - \mathbf{Y})^*$$

$$(\mathbf{X} + \mathbf{Y})/\mathbf{X}$$

$$\mathbf{X} = 3.064 + j2.571; \mathbf{Y} = 17.321 - j10$$

$$\begin{aligned} \text{(a)} \quad (\mathbf{X} + \mathbf{Y})\mathbf{X}^* &= (20.38 - j7.429)(4\angle -40^\circ) \\ &= (21.69\angle -20.03^\circ)(4\angle -40^\circ) = 86.76\angle -60.03^\circ \\ &= \mathbf{86.76\angle -60.03^\circ} \end{aligned}$$

$$\text{(b)} \quad (\mathbf{X} - \mathbf{Y})^* = (-14.257 + j12.571)^* = \mathbf{19.41\angle -139.63^\circ}$$

$$\text{(c)} \quad (\mathbf{X} + \mathbf{Y})/\mathbf{X} = (21.69\angle -20.03^\circ)/(4\angle 40^\circ) = \mathbf{5.422\angle -60.03^\circ}$$