

Chapter 6, Solution 31.

$$i_s(t) = \begin{cases} 30t \text{ mA}, & 0 < t < 1 \\ 30 \text{ mA}, & 1 < t < 3 \\ -75 + 15t, & 3 < t < 5 \end{cases}$$

$$C_{eq} = 4 + 6 = 10 \mu\text{F}$$

$$v = \frac{1}{C_{eq}} \int_0^t i \, dt + v(0)$$

For $0 < t < 1$,

$$v = \frac{10^{-3}}{10 \times 10^{-6}} \int_0^t 30t \, dt + 0 = 1.5t^2 \text{ kV}$$

For $1 < t < 3$,

$$\begin{aligned} v &= \frac{10^3}{10} \int_1^t 20 \, dt + v(1) = [3(t-1) + 1.5] \text{ kV} \\ &= [3t - 1.5] \text{ kV} \end{aligned}$$

For $3 < t < 5$,

$$\begin{aligned} v &= \frac{10^3}{10} \int_3^t 15(t-5) \, dt + v(3) \\ &= \left[1.5 \frac{t^2}{2} - 7.5t \right] \Big|_3^t + 7.5 \text{ kV} = [0.75t^2 - 7.5t + 23.25] \text{ kV} \end{aligned}$$

$$v(t) = \begin{cases} 1.5t^2 \text{ kV}, & 0 < t < 1 \text{ s} \\ [3t - 1.5] \text{ kV}, & 1 < t < 3 \text{ s} \\ [0.75t^2 - 7.5t + 23.25] \text{ kV}, & 3 < t < 5 \text{ s} \end{cases}$$

$$i_1 = C_1 \frac{dv}{dt} = 6 \times 10^{-6} \frac{dv}{dt}$$

$$i_1 = \begin{cases} 18t \text{ mA}, & 0 < t < 1 \text{ s} \\ 18 \text{ mA}, & 1 < t < 3 \text{ s} \\ [9t - 45] \text{ mA}, & 3 < t < 5 \text{ s} \end{cases}$$

$$i_2 = C_2 \frac{dv}{dt} = 4 \times 10^{-6} \frac{dv}{dt}$$

$$i_2 = \begin{cases} 12t \text{ mA}, & 0 < t < 1 \text{ s} \\ 12 \text{ mA}, & 1 < t < 3 \text{ s} \\ [6t - 30] \text{ mA}, & 3 < t < 5 \text{ s} \end{cases}$$