

Chapter 6, Solution 84.

An 8-mH inductor is used in a fusion power experiment. If the current through the inductor is $i(t) = 5 \sin^2(\pi t)$ mA, $t > 0$, find the power being delivered to the inductor and the energy stored in it at $t = 0.5$ s.

Solution

$$v = L(di/dt) = 8 \times 10^{-3} \times 5 \times 2\pi \sin(\pi t) \cos(\pi t) 10^{-3} = 40\pi \sin(2\pi t) \mu\text{V}$$

$$p = vi = 40\pi \sin(2\pi t) 5 \sin^2(\pi t) 10^{-9} \text{ W, at } t=0 \text{ } p = \mathbf{0W}$$

$$w = \frac{1}{2} L i^2 = \frac{1}{2} \times 8 \times 10^{-3} \times [5 \sin^2(\pi / 2) \times 10^{-3}]^2 = 4 \times 25 \times 10^{-9} = \underline{100 \text{ nJ}}$$
$$= \mathbf{100 \text{ nJ}}$$