

Chapter 9, Solution 19.

$$\begin{aligned} \text{(a)} \quad 3\angle 10^\circ - 5\angle -30^\circ &= 2.954 + j0.5209 - 4.33 + j2.5 \\ &= -1.376 + j3.021 \\ &= 3.32\angle 114.49^\circ \end{aligned}$$

$$\begin{aligned} \text{Therefore,} \quad 3 \cos(20t + 10^\circ) - 5 \cos(20t - 30^\circ) \\ = \mathbf{3.32 \cos(20t + 114.49^\circ)} \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad 40\angle -90^\circ + 30\angle -45^\circ &= -j40 + 21.21 - j21.21 \\ &= 21.21 - j61.21 \\ &= 64.78\angle -70.89^\circ \end{aligned}$$

$$\text{Therefore,} \quad 40 \sin(50t) + 30 \cos(50t - 45^\circ) = \mathbf{64.78 \cos(50t - 70.89^\circ)}$$

$$\begin{aligned} \text{(c)} \quad \text{Using } \sin\alpha &= \cos(\alpha - 90^\circ), \\ 20\angle -90^\circ + 10\angle 60^\circ - 5\angle -110^\circ &= -j20 + 5 + j8.66 + 1.7101 + j4.699 \\ &= 6.7101 - j6.641 \\ &= 9.44\angle -44.7^\circ \end{aligned}$$

$$\begin{aligned} \text{Therefore,} \quad 20 \sin(400t) + 10 \cos(400t + 60^\circ) - 5 \sin(400t - 20^\circ) \\ = \mathbf{9.44 \cos(400t - 44.7^\circ)} \end{aligned}$$