

Chapter 7, Solution 54.

- (a) Before $t = 0$, i is obtained by current division or

$$i(t) = \frac{4}{4+4} (2) = 1 \text{ A}$$

After $t = 0$,

$$i(t) = i(\infty) + [i(0) - i(\infty)] e^{-t/\tau}$$

$$\tau = \frac{L}{R_{eq}}, \quad R_{eq} = 4 + (4 \parallel 12) = 7 \Omega$$

$$\tau = \frac{3.5}{7} = \frac{1}{2}$$

$$i(0) = 1, \quad i(\infty) = \frac{(4 \parallel 12)}{4 + (4 \parallel 12)} (2) = \frac{3}{4+3} (2) = \frac{6}{7}$$

$$i(t) = \frac{6}{7} + \left(1 - \frac{6}{7}\right) e^{-2t}$$

$$i(t) = \frac{1}{7} (6 - e^{-2t}) \text{ A}$$

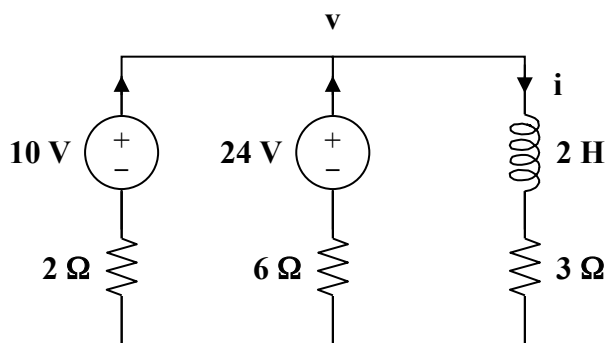
- (b) Before $t = 0$, $i(t) = \frac{10}{2+3} = 2 \text{ A}$

After $t = 0$, $R_{eq} = 3 + (6 \parallel 2) = 4.5$

$$\tau = \frac{L}{R_{eq}} = \frac{2}{4.5} = \frac{4}{9}$$

$$i(0) = 2$$

To find $i(\infty)$, consider the circuit below, at $t = \infty$ when the inductor becomes a short circuit,



$$\frac{10-v}{2} + \frac{24-v}{6} = \frac{v}{3} \longrightarrow v = 9 \quad i(\infty) = \frac{v}{3} = 3 \text{ A and } i(t) = 3 + (2-3) e^{-9t/4}$$

$$i(t) = 3 - e^{-9t/4} \text{ A}$$