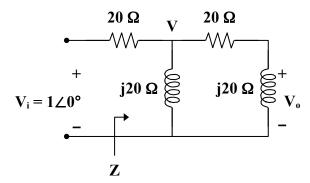
Chapter 9, Solution 74.

One such RL circuit is shown below.



We now want to show that this circuit will produce a 90° phase shift.

$$\mathbf{Z} = j20 \parallel (20 + j20) = \frac{(j20)(20 + j20)}{20 + j40} = \frac{-20 + j20}{1 + j2} = 4(1 + j3)$$

$$\mathbf{V} = \frac{\mathbf{Z}}{\mathbf{Z} + 20} \mathbf{V}_{i} = \frac{4 + j12}{24 + j12} (1 \angle 0^{\circ}) = \frac{1 + j3}{6 + j3} = \frac{1}{3} (1 + j)$$

$$\mathbf{V}_{o} = \frac{j20}{20 + j20} \mathbf{V} = \left(\frac{j}{1 + j}\right) \left(\frac{1}{3} (1 + j)\right) = \frac{j}{3} = 0.3333 \angle 90^{\circ}$$

This shows that the output leads the input by 90°.