Chapter 6, Solution 11.

$$v = \frac{1}{C} \int_{0}^{t} i dt + v(0) = 10 + \frac{1}{4x10^{-3}} \int_{0}^{t} i(t) dt$$

For
$$0 < t < 2$$
, $i(t) = 15mA$, $V(t) = 10 + v = 10 + \frac{10^3}{4 \times 10^{-3}} \int_0^t 15 dt = 10 + 3.76t$

$$v(2) = 10 + 7.5 = 17.5$$

For
$$2 < t < 4$$
, $i(t) = -10 \text{ mA}$

$$v(t) = \frac{1}{4 \times 10^{-3}} \int_{2}^{t} i(t)dt + v(2) = -\frac{10 \times 10^{-3}}{4 \times 10^{-3}} \int_{2}^{t} dt + 17.5 = 22.5 + 2.5t$$

$$v(4)=22.5-2.5x4=12.5$$

For
$$4 < t < 6$$
, $i(t) = 0$, $v(t) = \frac{1}{4 \times 10^{-3}} \int_{2}^{t} 0 dt + v(4) = 12.5$

For 6 < t < 8, i(t) = 10 mA

$$v(t) = \frac{10x10^3}{4x10^{-3}} \int_{4}^{t} dt + v(6) = 2.5(t - 6) + 12.5 = 2.5t - 2.5$$

Hence,

$$v(t) = \begin{cases} 10 + 3.75t \, V, & 0 < t < 2s \\ 22.5 - 2.5t \, V, & 2 < t < 4s \\ 12.5 \, V, & 4 < t < 6s \\ 2.5t - 2.5 \, V, & 6 < t < 8s \end{cases}$$

which is sketched below.

