Chapter 11, Solution 38.

For the power system in Fig. 11.67, find: (a) the average power, (b) the reactive power, (c) the power factor. Note that 220 V is an rms value.

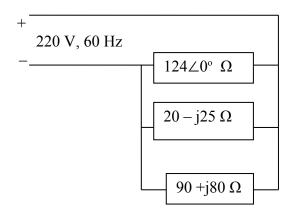


Figure 11.67 For Prob. 11.38.

Solution

$$S_{1} = \frac{V^{2}}{Z_{1}^{*}} = \frac{220^{2}}{124} = 390.32$$

$$S_{2} = \frac{V^{2}}{Z_{2}^{*}} = \frac{220^{2}}{20 + j25} = 944.4 - j1180.5$$

$$S_{3} = \frac{V^{2}}{Z_{3}^{*}} = \frac{220^{2}}{90 - j80} = 300 + j267.03$$

$$S = S_{1} + S_{2} + S_{3} = 1634.7 - j913.47 = 1872.6 < -29.196^{\circ} \text{ VA}$$
(a) $P = \text{Re}(S) = 1634.7 \text{ W}$

(b)
$$Q = Im(S) = 913.47 \text{ VA (leading)}$$

(c)
$$pf = cos (29.196^{\circ}) = 0.8732$$