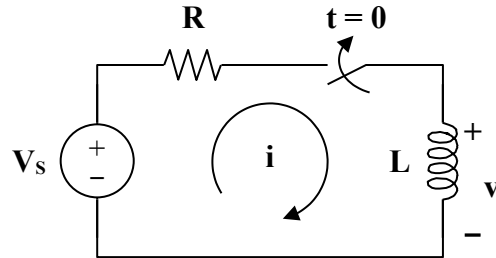


### Chapter 7, Solution 51.

Consider the circuit below.



After the switch is closed, applying KVL gives

$$V_s = Ri + L \frac{di}{dt}$$

$$\text{or} \quad L \frac{di}{dt} = -R \left( i - \frac{V_s}{R} \right)$$

$$\frac{di}{i - V_s/R} = \frac{-R}{L} dt$$

Integrating both sides,

$$\ln \left( i - \frac{V_s}{R} \right) \bigg|_{I_0}^{i(t)} = \frac{-R}{L} t$$

$$\ln \left( \frac{i - V_s/R}{I_0 - V_s/R} \right) = \frac{-t}{\tau}$$

$$\text{or} \quad \frac{i - V_s/R}{I_0 - V_s/R} = e^{-t/\tau}$$

$$i(t) = \frac{V_s}{R} + \left( I_0 - \frac{V_s}{R} \right) e^{-t/\tau}$$

which is the same as Eq. (7.60).