

Chapter 10, Solution 91.

(a) Let $V_2 =$ voltage at the noninverting terminal of the op amp
 $V_o =$ output voltage of the op amp
 $Z_p = 10 \text{ k}\Omega = R_o$
 $Z_s = R + j\omega L + \frac{1}{j\omega C}$

As in Section 10.9,

$$\frac{V_2}{V_o} = \frac{Z_p}{Z_s + Z_p} = \frac{R_o}{R + R_o + j\omega L - \frac{j}{\omega C}}$$

$$\frac{V_2}{V_o} = \frac{\omega C R_o}{\omega C (R + R_o) + j(\omega^2 LC - 1)}$$

For this to be purely real,

$$\omega_o^2 LC - 1 = 0 \rightarrow \omega_o = \frac{1}{\sqrt{LC}}$$

$$f_o = \frac{1}{2\pi \sqrt{LC}} = \frac{1}{2\pi \sqrt{(0.4 \times 10^{-3})(2 \times 10^{-9})}}$$

$$f_o = \mathbf{180 \text{ kHz}}$$

(b) At oscillation,

$$\frac{V_2}{V_o} = \frac{\omega_o C R_o}{\omega_o C (R + R_o)} = \frac{R_o}{R + R_o}$$

This must be compensated for by

$$A_v = \frac{V_o}{V_2} = 1 + \frac{80}{20} = 5$$

$$\frac{R_o}{R + R_o} = \frac{1}{5} \rightarrow R = 4 R_o = \mathbf{40 \text{ k}\Omega}$$