

Chapter 6, Solution 30.

$$v_o = \frac{1}{C} \int_0^t i dt + v_o(0)$$

For $0 < t < 1$, $i = 90t$ mA,

$$v_o = \frac{10^{-3}}{3 \times 10^{-6}} \int_0^t 90t dt + 0 = 15t^2 \text{ kV}$$
$$v_o(1) = 15 \text{ kV}$$

For $1 < t < 2$, $i = (180 - 90t)$ mA,

$$v_o = \frac{10^{-3}}{3 \times 10^{-6}} \int_1^t (180 - 90t) dt + v_o(1)$$
$$= [60t - 15t^2]_1^t + 15 \text{ kV}$$
$$= [60t - 15t^2 - (60 - 15) + 15] \text{ kV} = [60t - 15t^2 - 30] \text{ kV}$$

$$v_o(t) = \begin{cases} 15t^2 \text{ kV}, & 0 < t < 1 \\ [60t - 15t^2 - 30] \text{ kV}, & 1 < t < 2 \end{cases}$$