Chapter 10, Solution 45.

Use superposition to find i(t) in the circuit of Fig. 10.90.

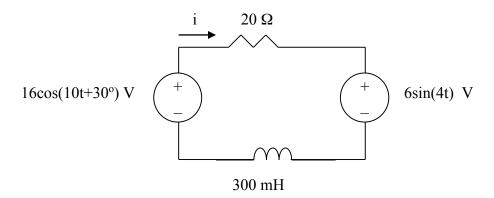
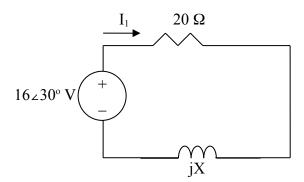


Figure 10.90 For Prob. 10.45.

Solution

Let $i = i_1 + i_2$, where i_1 and i_2 are due to $16\cos(10t + 30^\circ)$ and $6\sin4t$ sources respectively. To find i₁, consider the circuit below.

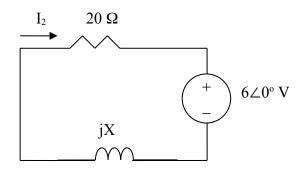


$$X = \omega L = 10x300x10^{-3} = 3$$

Type equation here.
$$I_1 = \frac{16 \angle 30^{\circ}}{20 + j3} = \frac{16 \angle 30^{\circ}}{20.22 \angle 8.53^{\circ}} = 0.7913 \angle 21.47^{\circ}$$

$$i_1(t) = 791.1\cos(10t+21.47^\circ) \text{ mA}.$$

To find i₂(t), consider the circuit below,



$$X = \omega L = 4x300x10^{-3} = 1.2$$

$$I_2 = \frac{-6 \angle 0^{\circ}}{20 + j \cdot 1.2} = \frac{6 \angle 180^{\circ}}{20.036 \angle 3.43^{\circ}} = 0.2995 \angle 176.57^{\circ} \text{ or}$$

$$i_2(t) = 299.5\sin(4t+176.57^\circ) \text{ mA}.$$

Thus,

$$i(t) = i1(t) + i2(t) = [791.1\cos(10t+21.47^{\circ}) + 299.5\sin(4t+176.57^{\circ})] \text{ mA}.$$