Chapter 10, Solution 4.

Compute $v_o(t)$ in the circuit of Fig. 10.53.

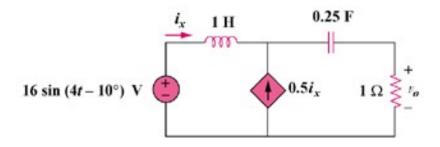
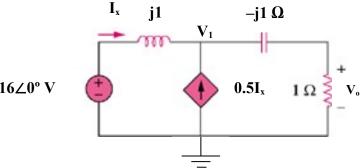


Figure 10.53 For Prob. 10.4.

Solution

Step 1. Convert the circuit into the frequency domain and solve for the node voltage, V_1 , using analysis. The find the current $I_C = V_1/[1+(1/(j4x0.25)]]$ which then produces $V_0 = 1xI_C$. Finally, convert the capacitor voltage back into the time domain.



Note that we represented $16\sin(4t-10^\circ)$ volts by $16 \angle 0^\circ$ V. That will make our calculations easier and all we have to do is to offset our answer by a -10° .

Our node equation is $[(V_1-16)/j] - (0.5I_x) + [(V_1-0)/(1-j)] = 0$. We have two unknowns, therefore we need a constraint equation. $I_x = [(16-V_1)/j] = j(V_1-16)$. Once we have V_1 , we can find $I_0 = V_1/(1-j)$ and $V_0 = 1xI_0$.

Step 2. Now all we need to do is to solve our equations.

$$[(V_1 - 16)/j] - [0.5j(V_1 - 16] + [(V_1 - 0)/(1 - j)] = [-j - j0.5 + 0.5 + j0.5]V_1 + j16 + j8 = 0 \text{ or } 1 - j0.5 + 0.5 + j0.5 = 0$$

$$[0.5-j]V_1 = -j24$$
 or $V_1 = j24/(-0.5+j) = (24\angle 90^{\circ})/(1.118\angle 116.57^{\circ}) = 21.47\angle -26.57^{\circ}$ V.

Finally,
$$I_x = V_1/(1-j) = (21.47 \angle -26.57^\circ) (0.7071 \angle 45^\circ) = 15.181 \angle 18.43^\circ$$
 A and $V_o = 1xI_o = 15.181 \angle 18.43^\circ$ V or

$$v_o(t) = 15.181\sin(4t-10^{\circ}+18.43^{\circ}) = 15.181\sin(4t-8.43^{\circ})$$
 volts.