Chapter 9, Solution 29.

Given that $v_C(0) = 2\cos(155^\circ)$ V, what is the instantaneous voltage across a $2-\mu$ F capacitor when the current through it is $I = 4\sin(10^6 t + 25^\circ)$ A?

Solution

$$Z = \frac{1}{j\omega C} = \frac{1}{j(10^6)(2 \times 10^{-6})} = -j \ 0.5$$

$$V = IZ = (4 \angle 25^{\circ})(0.5 \angle -90^{\circ}) = 2 \angle -65^{\circ}$$

Therefore $v(t) = 2 \sin(10^6 t - 65\mathbb{I}) V$.