MCFM v5.0

A Monte Carlo for FeMtobarn processes at Hadron Colliders

Users Guide

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Contents

1	Overview	3
2	Installation	4
3	Input parameters 3.1 Parton distributions	5
4	Runtime options	9
5	Nuclear collisions 2	20
6	6.1 Histograms	20 21 22
7	7.1 W-boson production, processes 1,6 7.2 W+ jet production, processes 11,16 7.3 W γ production, processes 12,17 7.4 W+c production, processes 13,18 7.5 W+c production ($m_c = 0$), processes 14,19 7.6 W+ $b\bar{b}$ production, processes 20,25 7.7 W+ $b\bar{b}$ production ($m_b = 0$), processes 21,26 7.8 W+2 jets production, processes 22,27 7.9 W+3 jets production, processes 23,28 7.10 W+ $b\bar{b}$ + jet production ($m_b = 0$), processes 24,29 7.11 Z-boson production, processes 31–33 7.12 Z+ jet production, processes 41–43 7.13 Z+2 jets production, processes 44 7.14 Z+3 jets production, process 45 7.15 $Z\gamma$ production, processes 48,49 7.16 $Z+b\bar{b}$ production, process 50	23 24 24 24 25 25 25 26 26 26 27 27 27 27
	7.19 $Z + c\bar{c}$ production $(m_c = 0)$, process 56	28 28 28 28

	7.20.2 WZ production, processes 71–73, 76–78	29
	7.20.3 ZZ production, processes 81–84, 86–89	29
	7.20.4 Anomalous couplings	29
7.21	WH production, processes $91,96$	30
7.22	ZH production, processes 101–103	31
7.23	Higgs production, processes 111–116	31
7.24	H+b production, processes 141–143	31
7.25	$t\bar{t}$ production with decay, processes 151 and 152	32
7.26	$t\bar{t}$ production with decay and a gluon, process 156	32
7.27	$Q\overline{Q}$ production, processes 157–159	32
7.28	$t\bar{t}$ + jet production, process 160	33
7.29	Single top production, processes 161–177	33
7.30	Wt production, processes 180–186	34
7.31	$Ht\bar{t}$ production, processes 190 and 191	35
7.32	$Zt\bar{t}$ production, processes 196 and 197	35
7.33	H+ jet production, processes $201-207$	35
7.34	Higgs production via WBF, processes 211–217	36
7.35	$\tau^+\tau^-$ production, process 221	36
	Z+Q production, processes 261–267	36
7.37	H+2 jet production, processes 271, 272	37
7.38	H+3 jet production, processes 273, 274	37
7.39	W+Q+ jet production $(Q pdf)$, processes 311–326	37
7.40	W+c+ jet production, processes 331, 336	38
7.41	Z+Q+iet production, processes 341–357	38

1 Overview

MCFM is a parton-level Monte Carlo program which gives NLO predictions for a range of processes at hadron colliders. The preferred reference to the program depends upon the process under study. The relevant papers are:

- J. M. Campbell and R. K. Ellis, "An update on vector boson pair production at hadron colliders," Phys. Rev. D **60**, 113006 (1999) [arXiv:hep-ph/9905386].
- J. M. Campbell and R. K. Ellis, "Radiative corrections to Z b anti-b production," Phys. Rev. D **62**, 114012 (2000) [arXiv:hep-ph/0006304].

- J. Campbell and R. K. Ellis,
 "Next-to-leading order corrections to W + 2jet and Z + 2jet production at hadron colliders,"
 Phys. Rev. D 65, 113007 (2002) [arXiv:hep-ph/0202176].
- J. Campbell, R. K. Ellis, F. Maltoni and S. Willenbrock, "Higgs boson production in association with a single bottom quark," Phys. Rev. D 67, 095002 (2003) [arXiv:hep-ph/0204093].
- J. Campbell, R. K. Ellis and D. L. Rainwater, "Next-to-leading order QCD predictions for W + 2jet and Z + 2jet production at the CERN LHC," Phys. Rev. D 68, 094021 (2003) [arXiv:hep-ph/0308195].
- J. Campbell, R. K. Ellis, F. Maltoni and S. Willenbrock, "Associated production of a Z boson and a single heavy-quark jet," Phys. Rev. D **69**, 074021 (2004) [arXiv:hep-ph/0312024].
- E. L. Berger and J. Campbell, "Higgs boson production in weak boson fusion at next-to-leading order," Phys. Rev. D **70**, 073011 (2004) [arXiv:hep-ph/0403194].
- J. Campbell, R. K. Ellis and F. Tramontano, "Single top production and decay at next-to-leading order," Phys. Rev. D **70**, 094012 (2004) [arXiv:hep-ph/0408158].
- J. Campbell and F. Tramontano, "Next-to-leading order corrections to W t production and decay," Nucl. Phys. B **726**, 109 (2005) [arXiv:hep-ph/0506289].

2 Installation

The tar'ed, gzip'ed and uu-encoded package may be downloaded from the MCFM home-page at http://mcfm.fnal.gov. After extracting, the source can be initialized by running the Install command and then compiled with make. The Install script may be edited prior to running, to include the locations of the CERNLIB and LHAPDF libraries, if desired. The code has been developed and tested under Redhat Linux. Please report any compilation problems under other operating systems to the authors.

The directory structure of the installation is as follows:

Paramter	Name	Input Value	Output Value determined by ewscheme			
	$(_{\tt inp})$		-1	0	1	2
G_F	Gf	1.16639×10^{-5}	input	calculated	input	input
$\alpha(M_Z)$	aemmz	1/128.89	input	input	calculated	input
$\sin^2 \theta_w$	xw	0.2312	calculated	input	calculated	input
M_W	wmass	80.419 GeV	input	calculated	input	calculated
M_Z	zmass	91.188 GeV	input	input	input	calculated
m_t	mt	172.5 GeV	calculated	input	input	input

Table 1: Different options for the scheme used to fix the electroweak parameters of the Standard Model and the corresponding default input values.

- Doc. The source for this document.
- Bin. The directory containing the executable mcfm, and various essential files notably the options file input.DAT.
- Bin/Pdfdata. The directory containing the PDF data-files.
- obj. The object files produced by the compiler.
- src. The Fortran source files in various subdirectories.

The files which it is most likely that the user will need to modify are located in src/User. It is convenient, if one wants to modify one of these files, (or any other file in the subdirectories of the src directory), to copy it first to the directory where the user has installed mcfm. The makefile will use this file in preference to the identically named file in the sub-directories of src.

3 Input parameters

MCFM now allows the user to choose between a number of schemes for defining the electroweak couplings. These choices are summarized in Table 1. The scheme is selected by modifying the value of ewscheme in src/User/mdata.f prior to compilation, which also contains the values of all input parameters (see also Table 2).

For the default scheme (ewscheme=-1), we use the effective field theory approach, which is valid for scales below the top mass. In this approach there

Parameter	Fortran name	Default value
$m_{ au}$	mtau	$1.777~\mathrm{GeV}$
$m_{ au}^2$	mtausq	$3.1577 \; \mathrm{GeV^2}$
m_c^2	mcsq	$2.25~\mathrm{GeV^2}$
m_b^2	mbsq	$17.64 \; { m GeV^2}$
$\Gamma_{ au}$	tauwidth	$2.269 \times 10^{-12} \text{ GeV}$
Γ_W	wwidth	$2.06 \mathrm{GeV}$
Γ_Z	zwidth	$2.49 \mathrm{GeV}$
V_{ud}	Vud	0.975
V_{us}	Vus	0.222
V_{ub}	Vub	0.
V_{cd}	Vcd	0.222
V_{cs}	Vcs	0.975
V_{cb}	Vcb	0.

Table 2: Default values for the remaining parameters in MCFM.

are 4 independent parameters (which we choose to be G_F , $\alpha(M_Z)$, M_W and M_Z). For further details, see Georgi [1].

For the alternative schemes (ewscheme=0,1,2) the top mass is simply an additional input parameter and there are 3 other independent parameters from the remaining 5. The variable ewscheme then performs exactly the same role as idef in MadEvent [2]. ewscheme=0 is the old MadEvent default and ewscheme=1 is the new MadEvent default, which is also the same as that used in Alpgen and LUSIFER. For processes in which the top quark is directly produced it is preferable to use the schemes (ewscheme=0,1,2), since in these schemes one can adjust the top mass to its physical value, (in src/User/mdata.f).

3.1 Parton distributions

The value of $\alpha_S(M_Z)$ is not adjustable; it is hardwired with the parton distribution. In addition, the parton distribution also specifies the number of loops that should be used in the running of α_S . The default mode of operation is to choose from a collection of modern parton distribution functions that are included with MCFM. The distributions, together with their associated $\alpha_S(M_Z)$ values, are given in Table3. For the older distributions, where the

coupling was specified by Λ this requires some calculation and/or guesswork.

By editing the Makefile, it is straightforward to switch to either the PDFLIB or the LHAPDF parton distribution function implementations.

To use PDFLIB, one must first set the variable CERNLIB in the makefile to point to the directory that contains libpdflib804.a and then modify PDFROUTINES to take the value PDFLIB. The parameters to choose the pdf set are then specified in Bin/input.DAT.

To use LHAPDF, one must first set the variable LHAPDFLIB in the makefile to point to the directory that contains libLHAPDF.a and then modify PDFROUTINES to take the value LHAPDF. The parameters to choose the pdf set are then provided in Bin/input.DAT - the name of the group and the integer specifying the set. MCFM expects to find the sets in a sub-directory of Bin called PDFsets, as in the LHAPDF distribution. It is easiest to simply create a symbolic link appropriately.

One may always return to the built-in distributions by resetting PDFROUTINES to take the value NATIVE in the makefile, (and recompiling).

mrs02nl	0.1197	mrs02nn	0.1154
mrs0119	0.119	mrs0117	0.117
mrs0121	0.121	${\tt mrs01_j}$	0.121
${\tt mrs}99_1$	0.1175	mrs99_2	0.1175
mrs99_3	0.1175	${\tt mrs}99_4$	0.1125
mrs99_5	0.1225	mrs99_6	0.1178
${\tt mrs}99_7$	0.1171	mrs99_8	0.1175
mrs99_9	0.1175	mrs9910	0.1175
mrs9911	0.1175	mrs9912	0.1175
mrs98z1	0.1175	mrs98z2	0.1175
mrs98z3	0.1175	mrs98z4	0.1125
mtungb1	0.109	mrs98z5	0.1225
mrs96r1	0.113	mrs96r2	0.120
mrs96r3	0.113	mrs96r4	0.120
mrs95ap	0.1127	mrs95_g	0.1148
hmrs90e	0.09838	hmrs90b	0.10796
cteq6_m	0.118	cteq6_d	0.118
cteq6_l	0.118	cteq611	0.130
cteq5hq	0.118	cteq5f3	0.106
cteq5f4	0.112	cteq5_m	0.118
cteq5_d	0.118	${\sf cteq5_l}$	0.127
cteq511	0.127	cteq5hj	0.118
cteq5m1	0.118	ctq5hq1	0.118
cteq4a5	0.122	cteq4hj	0.116
cteq41q	0.114	cteq4_m	0.116
cteq4_d	0.116	cteq4_l	0.132
cteq4a1	0.110	cteq4a2	0.113
cteq4a3	0.116	cteq4a4	0.119
cteq3_m	0.112	$cteq3_1$	0.112
cteq3_d	0.112		

Table 3: Available pdf sets and their corresponding values of $\alpha_S(M_Z)$.

Command executed	Location of input file
mcfm	input.DAT
mcfm myfile.DAT	myfile.DAT
mcfm mydir	mydir/input.DAT
mcfm mydir myfile.DAT	mydir/myfile.DAT

Table 4: Summary of command line options for running mcfm.

4 Runtime options

mcfm execution is performed in the Bin/directory, with syntax:

The executable mcfm is automatically moved to Bin by the makefile. If no command line options are given, then mcfm will default to using the file input.DAT in the current directory for choosing options¹. The different possibilities are summarized in Table 4. In addition, if a working directory mydir is specified then output files will also be produced in this directory. By using these options one may, for instance, keep all input and output files for different processes in separate directories.

Each parameter in the input file is specified by a line such as

and we will give a description of all the parameters below, together with valid and/or sensible inputs for value. Groups of parameters are separated by a blank line and a description of that section, for readability.

• file version number. This should match the version number that is printed when mcfm is executed.

 $\{ {
m blank\ line} \}$ [Flags to specify the mode in which MCFM is run]

¹Note that this is very different from previous versions of MCFM. All auxiliary input files from v3.2 and earlier have now been incorporated into a single file.

- evtgen. The default for this, and the following three parameters, is .false. and this corresponds to the usual mode of operation. It is possible to generate n-tuples instead of histograms, as well as unweighted events, for some processes. Please refer to Section 6.2 for further details.
- creatent. See above.
- skipnt. See above.
- dswhisto. See above.

$\{ blank \ line \} \\ [General options to specify the process and execution]$

- nproc. The process to be studied is given by choosing a process number, according to Table 5. $f(p_i)$ denotes a generic partonic jet.
- part. This parameter has 5 possible values, described below:
 - lord. The calculation is performed at leading order only.
 - virt. Virtual (loop) contributions to the next-to-leading order result are calculated (+counterterms to make them finite), including also the lowest order contribution.
 - real. In addition to the loop diagrams calculated by virt, the full next-to-leading order results must include contributions from diagrams involving real gluon emission (-counterterms to make them finite). Note that only the sum of the real and the virt contributions is physical.
 - tota. For simplicity, the tota option simply runs the virt and real real pieces in series before performing a sum to obtain the full next-to-leading order result. In this case, the number of points specified by ncall1 and ncall2 is automatically increased when performing the real calculation. In practice, it may be more efficient to do run the pieces separately by hand, (c.f. ncall below.
 - todk Processes 161,166,171,176,181,186 only, see sctions 7.29 and
 7.30 below.

nproc	$f(p_1) + f(p_2) \to \dots$	Order
1	$W^{+}(\to \nu(p_3) + e^{+}(p_4))$	NLO
6	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4))$	NLO
11	$W^{+}(\rightarrow \nu(p_{3}) + e^{+}(p_{4})) + f(p_{5})$	NLO
12	$W^{+}(\rightarrow \nu(p_3) + e^{+}(p_4)) + \gamma(p_5)$	NLO
13	$W^{+}(\rightarrow \nu(p_3) + e^{+}(p_4)) + \bar{c}(p_5)$	LO
14	$W^{+}(\to \nu(p_3) + e^{+}(p_4)) + \bar{c}(p_5)$ [massless]	NLO
16	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + f(p_5)$	NLO
17	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + \gamma(p_5)$	NLO
18	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + c(p_5)$	LO
19	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + c(p_5)$ [massless]	NLO
20	$W^+(\to \nu(p_3) + e^+(p_4)) + b(p_5) + \overline{b}(p_6)$ [massive]	LO
21	$W^+(\to \nu(p_3) + e^+(p_4)) + b(p_5) + \bar{b}(p_6)$	NLO
22	$W^+(\to \nu(p_3) + e^+(p_4)) + f(p_5) + f(p_6)$	NLO
23	$W^+(\to \nu(p_3) + e^+(p_4)) + f(p_5) + f(p_6) + f(p_7)$	LO
24	$W^+(\to \nu(p_3) + e^+(p_4)) + b(p_5) + \bar{b}(p_6) + f(p_7)$	LO
25	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6)$ [massive]	LO
26	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6)$	NLO
27	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + f(p_5) + f(p_6)$	NLO
28	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + f(p_5) + f(p_6) + f(p_7)$	LO
29	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6) + f(p_7)$	LO
31	$Z^0(\to e^-(p_3) + e^+(p_4))$	NLO
32	$Z^0(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4)))$	NLO
33	$Z^0(o b(p_3) + ar b(p_4))$	NLO
41	$Z^0(\to e^-(p_3) + e^+(p_4)) + f(p_5)$	NLO
42	$Z_0(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4))) - [\text{sum over } 3 \nu] + f(p_5)$	NLO
43	$Z^0(\to b(p_3) + \bar{b}(p_4)) + f(p_5)$	NLO
44	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + f(p_{5}) + f(p_{6})$	NLO
45	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + f(p_{5}) + f(p_{6}) + f(p_{7})$	LO
48	$Z^{0}(\to e^{-}(p_3) + e^{+}(p_4)) + \gamma(p_5)$	NLO
49	$Z^0(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4))) - [\text{sum over } 3 \nu] + \gamma(p_5)$	
50	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + b(p_{6})$ [massive]	LO
51	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + \bar{b}(p_{6})$	NLO
52	$Z_0(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + b(p_5) + \bar{b}(p_6)$	NLO
53	$Z^{0}(\rightarrow b(p_{3}) + \bar{b}(p_{4})) + b(p_{5}) + \bar{b}(p_{\underline{6}})$	NLO
54	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + \bar{b}(p_{6}) + f(p_{7})$	LO
56	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5}) + \bar{c}(p_{6})$	NLO

nproc	$f(p_1) + f(p_2) \rightarrow \dots$	Order
61	$W^{+}(\to \nu(p_3) + e^{+}(p_4)) + W^{-}(\to e^{-}(p_5) + \bar{\nu}(p_6))$	NLO
62	$W^{+}(\rightarrow \nu(p_{3}) + e^{+}(p_{4})) + W^{-}(\rightarrow q(p_{5}) + \bar{q}(p_{6}))$	NLO
63	$W^{+}(\to q(p_3) + \bar{q}(p_4)) + W^{-}(\to e^{-}(p_5) + \bar{\nu}(p_6))$	NLO
64	$W^{+}(\to \nu(p_3) + e^{+}(p_4)) + W^{-}(\to e^{-}(p_5) + \bar{\nu}(p_6))$ [no pol]	NLO
71	$W^+(\to \nu(p_3) + \mu^+(p_4)) + Z^0(\to e^-(p_5) + e^+(p_6))$	NLO
72	$W^{+}(\to \nu(p_3) + \mu^{+}(p_4)) + Z^{0}(\to \nu_e(p_5) + \bar{\nu}_e(p_6))$	NLO
73	$W^{+}(\to \nu(p_3) + \mu^{+}(p_4)) + Z^{0}(\to b(p_5) + \bar{b}(p_6))$	NLO
76	$W^-(\to \mu^-(p_3) + \bar{\nu}(p_4)) + Z^0(\to e^-(p_5) + e^+(p_6))$	NLO
77	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + Z^{0}(\to \nu(p_5) + \bar{\nu}(p_6))$	NLO
78	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + Z^{0}(\to b(p_5) + \bar{b}(p_6))$	NLO
81	$Z^{0}(\to \mu^{-}(p_3) + \mu^{+}(p_4)) + Z^{0}(\to e^{-}(p_5) + e^{+}(p_6))$	NLO
82	$Z^{0}(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + Z^{0}(\rightarrow e^{-}(p_5) + e^{+}(p_6))$	NLO
83	$Z^{0}(\rightarrow e^{-}(p_{5}) + e^{+}(p_{6})) + Z^{0}(\rightarrow b(p_{3}) + \bar{b}(p_{4}))$	NLO
84	$Z^{0}(\to 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + Z^{0}(\to b(p_5) + \bar{b}(p_6))$	NLO
86	$Z^{0}(\to e^{-}(p_{5}) + e^{+}(p_{6})) + Z^{0}(\to \mu^{-}(p_{3}) + \mu^{+}(p_{4})) \text{ [no } \gamma^{*}]$	NLO
87	$Z^{0}(\rightarrow e^{-}(p_{5}) + e^{+}(p_{6})) + Z^{0}(\rightarrow 3 \times (\nu(p_{3}) + \bar{\nu}(p_{4}))) \text{ [no } \gamma^{*}]$	NLO
88	$Z^{0}(\to e^{-}(p_{5}) + e^{+}(p_{6})) + Z^{0}(\to b(p_{3}) + \bar{b}(p_{4})) \text{ [no } \gamma^{*}]$	NLO
89	$Z^{0}(\to 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + Z^{0}(\to b(p_5) + \bar{b}(p_6)) \text{ [no } \gamma^*]$	NLO
91	$W^{+}(\to \nu(p_3) + e^{+}(p_4)) + H(\to b(p_5) + \bar{b}(p_6))$	NLO
96	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + H(\to b(p_5) + \bar{b}(p_6))$	NLO
101	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + H(\rightarrow b(p_{5}) + \bar{b}(p_{6}))$	NLO
102	$Z^{0}(\to 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + H(\to b(p_5) + \bar{b}(p_6))$	NLO
103	$Z^{0}(\to b(p_{3}) + \bar{b}(p_{4})) + H(\to b(p_{5}) + \bar{b}(p_{6}))$	NLO
111	$H(\rightarrow b(p_3) + \bar{b}(p_4))$	NLO
112	$H(\to \tau^-(p_3) + \tau^+(p_4))$	NLO
113	$H(\to W^+(\nu(p_3) + e^+(p_4)) + W^-(e^-(p_5) + \bar{\nu}(p_6)))$	NLO
114	$H(\to Z^0(\mu^-(p_3) + \mu^+(p_4)) + Z^0(e^-(p_5) + e^+(p_6))$	NLO
115	$H(\to Z^0(3 \times (\nu(p_3) + \bar{\nu}(p_4))) + Z^0(e^-(p_5) + e^+(p_6))$	NLO
116	$H(\to Z^0(\mu^-(p_3) + \mu^+(p_4)) + Z^0(b(p_5) + \bar{b}(p_6))$	NLO
141	$H(\to b(p_3) + \bar{b}(p_4)) + b(p_5)(+g(p_6))$	NLO
142	$H(\to b(p_3) + \bar{b}(p_4)) + \bar{b}(p_5)(+b(p_6))$	NLO
143	$H(\rightarrow b(p_3) + \bar{b}(p_4)) + b(p_5) + \bar{b}(p_6)$ [both observed]	NLO

nproc	$f(p_1) + f(p_2) \to \dots$	Order
151	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\to \bar{b}(p_6)) + e^-(p_7) + \bar{\nu}(p_8))$	LO
152	$t(\to u(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\to \bar{b}(p_6)) + q(p_7) + \bar{q}(p_8))$	LO
156	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\to \bar{\nu}(p_7) + e^-(p_8) + \bar{b}(p_6)) + g(p_9)$	LO
157	$t\bar{t}$ [for total Xsect]	NLO
158	$b\bar{b}$ [for total Xsect]	NLO
159	$car{c}$ [for total Xsect]	NLO
160	$t\bar{t} + g$ [for total Xsect]	LO
161	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + q(p_6)$ [t-channel]	NLO
162	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + q(p_6)$ [decay]	NLO
166	$\bar{t}(\to e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + q(p_6)$ [t-channel]	NLO
167	$\bar{t}(\to e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + q(p_6)$ [decay]	NLO
171	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{b}(p_6))$ [s-channel]	NLO
172	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{b}(p_6))$ [decay]	NLO
176	$\bar{t}(\to e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + b(p_6))$ [s-channel]	NLO
177	$\bar{t}(\to e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + b(p_6))$ [decay]	NLO
180	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + t(p_5)$	NLO
181	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + t(\nu(p_5) + e^+(p_6) + b(p_7))$	NLO
182	$W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + t(\nu(p_5) + e^+(p_6) + b(p_7))$ [decay]	NLO
185	$W^+(\to \nu(p_3) + e^+(p_4)) + \bar{t}(p_5)$	NLO
186	$W^+(\to \nu(p_3) + e^+(p_4)) + \bar{t}(e^-(p_5) + \bar{\nu}(p_6) + \bar{b}(p_7))$	NLO
187	$W^+(\to \nu(p_3) + e^+(p_4)) + \bar{t}(e^-(p_5) + \bar{\nu}(p_6) + \bar{b}(p_7))$ [decay]	NLO
190	$t(p_3) + \bar{t}(p_4) + H(p_5)$	LO
191	$t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7) + e^-(p_8) + \bar{b}(p_6)) + H(p_9 + p_{10})$	LO
196	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\to \bar{\nu}(p_7) + e^-(p_8) + \bar{b}(p_6)) + Z(e^-(p_9), e^+(p_{10}))$	LO
197	$t(\to \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\to \bar{\nu}(p_7) + e^-(p_8) + \bar{b}(p_6)) + Z(b(p_9), \bar{b}(p_{10}))$	LO
201	$H(\rightarrow b(p_3) + \bar{b}(p_4)) + f(p_5)$ [full mt dep.]	LO
202	$H(\to \tau^-(p_3) + \tau^+(p_4)) + f(p_5)$ [full mt dep.]	LO
203	$H(o b(p_3) + ar{b}(p_4)) + f(p_5)$	NLO
204	$H(\to \tau^-(p_3) + \tau^+(p_4)) + f(p_5)$	NLO
206	$A(\to b(p_3) + \bar{b}(p_4)) + f(p_5)$ [full mt dep.]	LO
207	$A(\to \tau^-(p_3) + \tau^+(p_4)) + f(p_5)$ [full mt dep.]	LO
211	$H(\to b(p_3) + \bar{b}(p_4)) + f(p_5) + f(p_6)$ [WBF]	NLO
212	$H(\to \tau^-(p_3) + \tau^+(p_4)) + f(p_5) + f(p_6)$ [WBF]	NLO
216	$H(\to b(p_3) + \bar{b}(p_4)) + f(p_5) + f(p_6) + f(p_7)$ [WBF+jet]	NLO
217	$H(\to \tau^-(p_3) + \tau^+(p_4)) + f(p_5) + f(p_6) + f(p_7)$ [WBF+jet]	NLO
221	$\tau^-(\to e^-(p_3) + \bar{\nu}_e(p_4) + \nu_\tau(p_5)) + \tau^+(\to \bar{\nu}_\tau(p_6) + \nu_e(p_7) + e^+(p_8))$	LO

nproc	$f(p_1) + f(p_2) \to \dots$	Order
261	$Z^0(\to e^-(p_3) + e^+(p_4)) + b(p_5)$	NLO
262	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5})$	NLO
263	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + \bar{b}(p_{5}) + b(p_{6})$ [1 b-tag]	NLO
264	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + \bar{c}(p_{5}) + c(p_{6})$ [1 c-tag]	NLO
266	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5})(+\bar{b}(p_{6}))$	NLO
267	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5})(+\bar{c}(p_{6}))$	NLO
271	$H(b(p_3) + \bar{b}(p_4)) + f(p_5) + f(p_6)$ [in heavy top limit]	LO
272	$H(\tau^{-}(p_3) + \tau^{+}(p_4)) + f(p_5) + f(p_6)$ [in heavy top limit]	LO
273	$H(b(p_3) + \bar{b}(p_4)) + f(p_5) + f(p_6) + f(p_7)$ [in heavy top limit]	LO
274	$H(\tau^{-}(p_3) + \tau^{+}(p_4)) + f(p_5) + f(p_6) + f(p_7)$ [in heavy top limit]	LO
311	$f(p_1) + b(p_2) \to W^+(\to \nu(p_3) + e^+(p_4)) + b(p_5) + f(p_6)$	LO
316	$f(p_1) + b(p_2) \to W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + f(p_6)$	LO
321	$f(p_1) + b(p_2) \to W^+(\to \nu(p_3) + e^+(p_4)) + c(p_5) + f(p_6)$	LO
326	$f(p_1) + b(p_2) \to W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + c(p_5) + f(p_6)$	LO
331	$W^{+}(\to \nu(p_3) + e^{+}(p_4)) + c(p_5) + f(p_6)$ [c-s interaction]	LO
336	$W^{-}(\to e^{-}(p_3) + \bar{\nu}(p_4)) + c(p_5) + f(p_6)$ [c-s interaction]	LO
341	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + f(p_{6})[+f(p_{7})]$	NLO
342	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + f(p_{6})[+b(p_{7})]$	(REAL)
346	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + f(p_{6}) + f(p_{7})$	LO
347	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + b(p_{5}) + f(p_{6}) + b(p_{7})$	LO
351	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5}) + f(p_{6})[+f(p_{7})]$	NLO
352	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5}) + f(p_{6})[+c(p_{7})]$	(REAL)
356	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5}) + f(p_{6}) + f(p_{7})$	LO
357	$Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + c(p_{5}) + f(p_{6}) + c(p_{7})$	LO
902	[Check of Volume of 2 particle phase space]	=
903	[Check of Volume of 3 particle phase space]	_
904	[Check of Volume of 4 particle phase space]	_
905	[Check of Volume of 5 particle phase space]	_
906	[Check of Volume of 6 particle phase space]	_
908	[Check of Volume of 8 particle phase space]	_
909	[Check of Volume of 4 particle massive phase space]	_
910	[Check of Volume of 3 particle (2 massive) phase space]	_

Table 5: Processes indicated by choice of the variable ${\tt nproc}.$

- runstring. When MCFM is run, it will write output to several files. The label runstring will be appended to the names of these files.
- sqrts. This is the centre-of-mass energy, \sqrt{s} of the colliding particles, measured in GeV.
- ih1, ih2. The identities of the incoming hadrons may be set with these parameters, allowing simulations for both $p\bar{p}$ (such as the Tevatron) and pp (such as the LHC). Setting ih1 equal to +1 corresponds to a proton, whilst -1 corresponds to an anti-proton. Values greater than 1000d0 represent a nuclear collision, as described in Section 5.
- hmass. For processes involving the Higgs boson, this parameter should be set equal to the putative value of M_H .
- scale. This parameter may be used to adjust the value of the renormalization scale. This is the scale at which α_S is evaluated and will typically be set to a mass scale appropriate to the process $(M_W, M_Z, M_t$ for instance). For processes involving vector bosons, setting this scale to -1d0 chooses a scale equal to the average mass of the bosons involved.
- facscale. This parameter may be used to adjust the value of the factorization scale and will typically be set to a mass scale appropriate to the process $(M_W, M_Z, M_t$ for instance). As above, setting it to -1d0 will choose an appropriate value for certain processes.
- dynamicscale When set to .true. the renormalization and factorization scales are recalculated for each event. In this case, the values of scale and facscale take on a special meaning that determines the method used to calculate the scale:
 - 1d0 : $\mu^2 = M_V^2 + p_T(V)^2$ only appropriate for processes involving a vector boson V
 - 2d0 : $\mu^2 = < p_T^{jet} >^2 -$ only appropriate for processes involving jets
 - 3d0 : $\mu^2 = \hat{s}$, the partonic centre of mass energy
 - 4d0: $\mu^2 = H_T^2$, where H_T is the scalar sum of the p_T 's of all the particles in each event

Note that care must be used when selecting this option, since not all choices are appropriate for each process.

- zerowidth. When set to .true. then all vector bosons are produced on-shell. This is appropriate for calculations of *total* cross-sections (such as when using removebr equal to .true., below). When interested in decay products of the bosons this should be set to .false..
- removebr. When set to .true. the branching ratios are removed for unstable particles such as vector bosons or top quarks. See the process notes in Section 7 below for further details.
- itmx1, itmx2. The program will perform two runs of VEGAS once for pre-conditioning and then the final run to collect the total cross-section and fill histograms. The number of sweeps for each run is given by itmx1 (pre-conditioning) and itmx2 (final). The default value for both is 10.
- ncall1, ncall2. For every sweep of VEGAS, the number of events generated will be ncall1 in the pre-conditioning stage and ncall2 in the final run. The number of events required depends upon a number of factors. The error estimate on a total cross-section will often be reasonable for a fairly small number of events, whereas accurate histograms will require a longer run. As the number of particles in the final state increases, so should the number of calls per sweep. Typically one might make trial runs with part set to lord to determine reasonable values for ncall1 and ncall2. Such values should also be appropriate for the virt piece of next-to-leading order and should probably be increased by a factor of ~ 5 for the real calculation.
- ij. This is the seed for the VEGAS integration and can be altered to give different results for otherwise identical runs.
- dryrun. The default value of this parameter is .false.. When set to .true. the pre-conditioning sweeps in the VEGAS integration are skipped, with the reported results coming from a single run, (ie itmx1 iterations of ncall1 points each)
- Qflag. This only has an effect when running a W+2 jets or Z+2 jets process. Please see section 7.8 below.

• Gflag. This only has an effect when running a W+2 jets or Z+2 jets process. Please see section 7.8 below.

{blank line} [Pdf selection]

- pdlabel. The choice of parton distribution is made by inserting the appropriate 7-character code from Table 3 here. As mentioned above, this also sets the value of $\alpha_S(M_Z)$.
- NGROUP, NSET. These integers choose the parton distribution functions to be used when using the PDFLIB package.
- LHAPDF group, LHAPDF set. These choose the parton distribution functions to be used when using the LHAPDF package the group is specified by a character string and the set by an integer. Please see http://durpdg.dur.ac.uk/lhapdf/ for further details. For appropriate PDF sets choosing a value of -1 for the set number (LHAPDF set) will perform the calculation of the PDF uncertainties (see also Section 6.1, especially the caveat regarding using non-grid PDF sets).

{blank line} [Jet definition and event cuts]

- m34min, m34max, m56min, m56max. These parameters represent a basic set of cuts that may be applied to the calculated cross-section. The only events that contribute to the cross-section will have, for example, m34min < m34 < m34max where m34 is the invariant mass of particles 3 and 4 that are specified by nproc. m34min; 0 is obligatory for processes which can involve a virtual photon, such as nproc=31.
- inclusive. This logical parameter chooses whether the calculated cross-section should be inclusive in the number of jets found at NLO. An *exclusive* cross-section contains the same number of jets at next-to-leading order as at leading order. An *inclusive* cross-section may instead contain an extra jet at NLO.
- algorithm This specifies the jet-finding algorithm that is used, and can take the values ktal (for the Run II k_T -algorithm) and cone (for a midpoint cone algorithm).

- ptmin_jet, etamin_jet, etamax_jet. These specify the values of p_T^{\min} , $|\eta|^{\min}$ and $|\eta|^{\max}$ for the jets that are found by the algorithm.
- Rcut_jet. If the final state of the chosen process contains either quarks or gluons then for each event an attempt will be made to form them into jets. For this it is necessary to define the jet separation $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2}$ so that after jet combination, all jet pairs are separated by $\Delta R > \text{Rcut_jet}$.
- makecuts. If this parameter is set to .false. then no additional cuts are applied to the events and the remaining parameters in this section are ignored. Otherwise, events will be rejected according to a set of cuts that is specified below. Further options may be implemented by editing src/User/gencuts.f.
- ptmin_lepton, etamax_lepton. These specify the values of p_T^{\min} and $|y|^{\max}$ for the hardest lepton produced in the process.
- ptmin_missing. Specifies the minimum missing transverse momentum (coming from neutrinos).
- ptmin_lepton(2nd+), etamax_lepton(2nd+). These specify the values of p_T^{\min} and $|y|^{\max}$ for the remaining leptons in the process. This allows for staggered cuts where, for instance, only one lepton is required to be hard and central.
- R(jet,lept)_min. Using the definition of ΔR above, requires that all jet-lepton pairs are separated by $\Delta R > \text{R(jet,lept)}$ _min.
- R(lept,lept) min. When non-zero, all lepton-lepton pairs must be separated by $\Delta R > R(lept,lept)$ min.
- Delta_eta(jet,jet)_min. This enforces a pseudo-rapidity gap between the two hardest jets j_1 and j_2 , so that: $|\eta^{j_1} \eta^{j_2}| > \text{Delta_eta(jet,jet)_min}.$
- jets_opphem. If this parameter is set to .true., then the two hardest jets are required to lie in opposite hemispheres, $\eta^{j_1} \cdot \eta^{j_2} < 0$.
- lepbtwnjets_scheme. This integer parameter provides no additional cuts when it takes the value 0. When equal to 1 or 2, leptons are

required to lie between the two hardest jets. With the ordering $\eta^{j-} < \eta^{j+}$ for the pseudo-rapidities of jets j_1 and j_2 :

 $\begin{array}{ll} \texttt{lepbtwnjets_scheme} \ = \ 1: \ \eta^{j_-} < \eta^{\text{leptons}} < \eta^{j_+}; \\ \texttt{lepbtwnjets_scheme} \ = \ 2: \ \eta^{j_-} + \texttt{Rcut_jet} < \eta^{\text{leptons}} < \eta^{j_+} - \texttt{Rcut_jet}. \end{array}$

- ptmin_bjet, etamax_bjet. If makecuts is .true. and a process involving b-quarks is being calculated, then these can be used to specify stricter values of p_T^{\min} and $|\eta|^{\max}$ for b-jets.
- ptminphoton, etamaxphoton. These specify the values of p_T^{\min} and $|y|^{\max}$ for any photons produced.
- conephoton, coneptcut. These constitute a photon isolation cut which ensures that the amount of hadronic transverse momentum in a cone around each photon is less than a specified fraction of the photon's p_T .

$$\sum_{R < R_0} p_T^{\text{hadronic}} < f \times p_T^{photon},$$

where R_0 and f are specified by cone_photon and cone_ptcut respectively.

{blank line}
[Anomalous couplings of the W and Z]

- Delta_g1(Z). See section 7.20.
- Delta_K(Z). See section 7.20.
- Delta_K(gamma). See section 7.20.
- Lambda(Z). See section 7.20.
- Lambda (gamma). See section 7.20.
- Form-factor scale, in TeV. See section 7.20.

{blank line}
[How to resume/save a run]

- readin. If .true., the program will read in a previously saved VEGAS grid from the file specified by ingridfile.grid. Note that this, and the following 3 options, have no effect if part is set to tota (in this case, grids are automatically saved and loaded as part of the calculation).
- writeout. If .true., the program will write out the VEGAS grid at the end of the run, to the file specified by outgridfile.grid.
- ingridfile. See above.
- outgridfile. See above.

5 Nuclear collisions

It is possible to specify nuclear collisions by choosing values of ih1 and/or ih2 above 1000d0. In that case, the identity of the nucleus is specified by the atomic number and mass (Z and A respectively) as follows:

$$ih = 1000Z + A. \tag{1}$$

For example, to choose an incoming lead beam one would set ih1=+82207d0, corresponding to Z=82 and A=207. When running the program, the value of sqrts should also be changed. This must be done by hand and is not automatically taken care of by the program. The centre-of-mass energy is decreased by a factor of $\sqrt{Z/A}$ for each nuclear beam.

The nucleon PDF's are calculated by applying the correction factors of EKS98 [8] on top of the PDF set that is selected. This construction simply corrects each parton distribution by a factor that depends on the value of (x, μ) in the event. This parametrization is limited to the region $\mu < 100 \text{ GeV}$ and any value above that threshold will instead default to 100 GeV.

Note that the cross-section reported by the program at the end of the run is given per nucleon per beam. Therefore the appropriate factors of A should be applied in order to obtain the total cross section.

6 Output

In addition to the direct output of the program to stdout, after the final sweep of VEGAS the program will output two additional files. If a working

directory was specified in the command line, then these output files will be written to that directory.

The standard output will detail the iteration-by-iteration best estimate of the total cross-section, together with the accompanying error estimate. After all sweeps have been completed, a final summary line will be printed. In the npart = tota case, this last line will actually be the sum of the two separate real and virtual integrations.

The two other output files are outputname.dat and outputname.top, which contain data for various histograms associated with the calculated process. The first of these is in a raw format which may be read in by a plotting package of the user's choosing. The other file contains the histograms as a TOPDRAWER file, as well as a summary of the options file (input.DAT) in the form of comments at the beginning. The structure of outputname is as follows:

procname_part_pdlabel_scale_runstring

where procname is a label assigned by the program corresponding to the calculated process; the remaining labels are as input by the user in the file input.DAT.

The histograms are setup in the file src/User/nplotter.f. The arguments of this subroutine are p,wt,switch. p contains the momenta of all the particles (i.e. the four momenta of the leptons and jets). The order of the jets is not necessarily the order specified in process.DAT. However in the case that we have a b-quark or antiquark they are labelled by bq and ba respectively in the array jetlabel. wt is the weight of the event.

6.1 Histograms

Extra histograms may be added to the file src/User/nplotter.f in a fairly straightforward manner. Each histogram is filled by making a call to the routine bookplot and updating the histogram counter n by 1. For example:

```
call bookplot(n,tag,' eta3',eta3,wt,-5d0,5d0,0.5d0,'lin')
n=n+1
```

The first two arguments of the call should not be changed. The third argument is a string describing the plot which will be used for the title in TOPDRAWER. The fourth argument carries the variable to be plotted, which has been previously calculated. The argument wt contains the phase-space

weight and should not be changed. The last arguments tell the histogramming routine to use bins of size 0.5 which run from -5 to 5, and use a linear scale for the plot. A logarithmic scale may be used by changing the final argument to 'log'.

If the LHAPDF package is being used and the value of LHAPDF set is equal to -1, to indicate a calculation using PDF uncertainties, then errors on distributions may also be accumulated. Note that, due to limitations within the LHAPDF distribution, calculations using error PDF sets are impractical unless the grid versions of the sets are used. The grid versions are available in LHAPDF v.3 and may be identified by the .LHgrid extension in the PDFsets directory. To use the grid version, simply pass the PDF set name, including this extension, as the value of LHAPDF group in the input file.

To accumulate errors in distributions, add an extra line to nplotter.f after the call to bookplot but before the counter is incremented. For example, to calculate the PDF uncertainties on the distribution of eta3 one would simply add:

call ebookplot(n,tag,eta3,wt)

The third argument contains the variable to plot and the other entries should not be changed. The other parameters for the plot are exactly those specified on the previous line, in the call to bookplot. Since each PDF error distribution takes up quite a lot of memory during execution, there is a limit of 4 on the number of distributions with errors that can be calculated at one time. When calculating PDF uncertainties on distributions, the program will produce an additional file which contains the results for each PDF error set individually. In addition the main file will include the uncertainty limits on the distribution, which is obtained by choosing the extremal values of the weights in all PDF sets, on a bin-by-bin basis. Thus the resulting error limits are not simply described by a single PDF set.

6.2 Other output modes

As noted in the description of the input file, there are a number of other output modes which may be useful in certain situations. In particular, the ability to output n-tuples can be used to generate a large event record that can be subsequently analyzed according to the users needs. Much of the code for generating these outputs can be found in src/User/dswhbook.f; some additional work may be required, depending on the process under study.

The simplest alternative output mode is obtained by changing the flag dswhisto to .true. . In this way, the TOPDRAWER output file is replaced by the file outputname.rz which contains the histograms in HBOOK format.

To obtain the simplest n-tuple output, the flag creatent should be set to .true. In this case, each event that enters a histogram is also recorded as an n-tuple in the file outputname_batchno.rz. The batchno starts at zero and is incremented by one every one millions events. Each event is a simple row-wise n-tuple consisting of the 4-momenta of each of the final state particles $(p_x, p_y, p_z \text{ and } E, \text{ in that order})$ followed by 5 numbers representing the event weight. The first number represents the total event weight and the others, the contribution from gluon-gluon, quark-gluon (and antiquarkgluon), quark-quark (and antiquark-antiquark) and quark-antiquark initial states. Single precision is used, for economy. A simple way to analyze these n-tuples is to use the h2root command and then perform manipulations with the ROOT package. Note that these n-tuples contain no information about either the flavour or the colour of the initial or final state particles. Summation and averaging over these variables has already been performed. Furthermore, the 'events' are weighted - so are not events in the traditional event generator sense.

In order to obtain unweighted events, one must change the flag evtgen to .true. This option is only available at lowest order at present. In this mode, the program will first perform a run to obtain the maximum weight and then perform a simple unweighting procedure against this number. In this mode the program will also assign identities to the particles in the initial state, according to the relative parton-parton luminosities. The routines that handle most of the processing can be found in src/User/eventhandler.f. Much of this code was tailored to diboson production in Run II of the Tevatron, so further work by the user is almost certainly required.

7 Notes on specific processes

Note that, as of version 4.0, the version of each process described in the fileprocess.DAT includes all appropriate boson decays. This is the calculation that is described when the parameter removebr is set to .false., as indicated above.

In many cases a more simple calculation can be performed by setting this parameter to .true., in which case these decays are not performed. In the

notes below we indicate the simpler processes thus obtained. When running in this mode, the parameter zerowidth should be set to .true. also, for consistency. However in certain circumstances, for the sake of comparison, it may be useful to run with it set to .false. .

7.1 W-boson production, processes 1,6

These processes represent the production of a W boson which subsequently decays leptonically. The calculation may be performed at NLO.

When removebr is true, the W boson does not decay.

7.2 W+ jet production, processes 11,16

These processes represent the production of a W boson which subsequently decays leptonically, in association with a single jet. The calculation may be performed at NLO.

When removebr is true, the W boson does not decay.

7.3 $W\gamma$ production, processes 12,17

These processes represent the production of a W boson which subsequently decays leptonically, in association with a real photon. The calculation may be performed at NLO. Note however that the contribution in which a jet fragments into a photon is not included, so these processes are currently of limited utility.

When removebr is true, the W boson does not decay.

7.4 W + c production, processes 13,18

These processes represent the production of a W boson which subsequently decays leptonically, in association with a charm quark. This is produced at LO by an initial state which contains a strange quark and a gluon. The effect of the charm quark mass is included throughout the calculation. The calculation may be performed at LO only.

When removebr is true, the W boson does not decay.

7.5 W+c production $(m_c=0)$, processes 14,19

These processes are identical to 13 and 18 except for the fact that the charm quark mass is neglected. The calculation can currently be performed at LO only.

7.6 $W + b\bar{b}$ production, processes 20,25

These processes represent the production of a W boson which subsequently decays leptonically, in association with a $b\bar{b}$ pair. The effect of the bottom quark mass is included throughout the calculation. The calculation may be performed at LO only.

When removebr is true, the W boson does not decay.

7.7 $W + b\bar{b}$ production $(m_b = 0)$, processes 21,26

These processes are identical to 20 and 25 except for the fact that the bottom quark mass is neglected. This allows the calculation to be performed up to NLO, with currently calculated virtual matrix elements.

When removebr is true, the W boson does not decay.

7.8 W+2 jets production, processes 22,27

[For more details on this calculation, please refer to hep-ph/0202176 and hep-ph/0308195]

This process represents the production of a W boson and 2 jets, where the W boson decays leptonically. The calculation may be performed up to NLO, as detailed below.

For these processes (and also for Z+2 jet production, nproc=44) the next-to-leading order matrix elements are particularly complex and so they have been divided into two groups. The division is according to the lowest order diagrams from which they originate:

- 1. Diagrams involving two external quark lines and two external gluons, the "Gflag" contribution. The real diagrams in this case thus involve three external gluons.
- 2. Diagrams where all four external lines are quarks, the "Qflag" contribution. The real diagrams in this case involve only one gluon.

By specifying Gflag and Qflag in input.DAT one may select one of these options at a time. The full result may be obtained by straightforward addition of the two individual pieces, with no meaning attached to either piece separately. In the lowest order calculation, both of these may be set to .true. simultaneously - however this is the only case where this is possible.

When removebr is true, the W boson does not decay.

7.9 W + 3 jets production, processes 23,28

This process represents the production of a W boson and 3 jets, where the W boson decays leptonically. The calculation may be performed at LO only. When removebr is true, the W boson does not decay.

7.10 $W + b\bar{b} +$ jet production $(m_b = 0),$ processes 24,29

These processes represent the production of a W boson which subsequently decays leptonically, in association with a $b\bar{b}$ pair and an additional jet. The effect of the bottom quark mass is neglected throughout and the calculation may be performed at LO only.

When removebr is true, the W boson does not decay.

7.11 Z-boson production, processes 31–33

These processes represent the production of a Z boson which subsequently decays either into electrons (nproc=31), neutrinos (nproc=32) or bottom quarks (nproc=33). Where appropriate, the effect of a virtual photon is also included. As noted above, in these latter cases m34min > 0 is obligatory. The calculation may be performed at NLO, although the NLO calculation of process 33 does not include radiation from the bottom quarks (it is in the initial state only).

When removebr is true in process 31, the Z boson does not decay.

7.12 Z+ jet production, processes 41–43

These processes represent the production of a Z boson and a single jet, where the Z subsequently decays either into electrons (nproc=41), neutrinos (nproc=42) or bottom quarks (nproc=43). Where appropriate, the effect of a virtual photon is also included. The calculation may be performed at NLO,

although the NLO calculation of process 43 does not include radiation from the bottom quarks.

When removebr is true in process 41, the Z boson does not decay.

7.13 Z+2 jets production, process 44

[For more details on this calculation, please refer to hep-ph/0202176 and hep-ph/0308195]

This process represents the production of a Z boson and 2 jets, including also the effect of a virtual photon. The Z/γ^* decays to an e^+e^- pair. The calculation may be performed up to NLO - please see the earlier Section 7.8 for more details, especially the discussion Qflag and Gflag.

When removebr is true, the Z boson does not decay.

7.14 Z+3 jets production, process 45

This process represents the production of a Z boson and 3 jets, including also the effect of a virtual photon. The Z/γ^* decays to an e^+e^- pair. The calculation may be performed at LO only.

When removebr is true, the Z boson does not decay.

7.15 $Z\gamma$ production, processes 48,49

These processes represent the production of a Z boson (or virtual photon) in association with a real photon. The Z/γ^* subsequently decays into either an e^+e^- pair (nproc=48) or neutrinos (nproc=49). The calculation may be performed at NLO. However since the contribution of a jet fragmenting into a photon is not included, these processes are currently of limited utility.

When removebr is true in process 48, the Z boson does not decay.

7.16 $Z + b\bar{b}$ production, process 50

These processes represent the production of a Z boson (or virtual photon) which subsequently decays leptonically, in association with a $b\bar{b}$ pair. The effect of the bottom quark mass is included throughout the calculation. The calculation may be performed at LO only.

When removebr is true, the Z boson does not decay.

7.17 $Z + b\bar{b}$ production $(m_b = 0)$, processes 51–53

Process 51 is identical to 50 except for the fact that the bottom quark mass is neglected. This allows the calculation to be performed up to NLO. The other processes account for the decays into neutrinos (nproc=52) and bottom quarks (nproc=53). Note that the NLO calculation of process 53 does not currently include radiation from the bottom quarks produced in the decay.

When removebr is true in process 51, the Z boson does not decay.

7.18 $Z + b\bar{b} + \text{ jet production } (m_b = 0), \text{ process } 54$

This process represents the production of a Z boson (and virtual photon) which subsequently decays leptonically, in association with a $b\bar{b}$ pair and an additional jet. The effect of the bottom quark mass is neglected throughout and the calculation may be performed at LO only.

When removebr is true, the Z boson does not decay.

7.19 $Z + c\bar{c}$ production $(m_c = 0)$, process 56

Process 56 is the equivalent of 51, with the bottom quarks replaced by charm. Although the charm mass is neglected, the calculation contains diagrams with two gluons in the initial state and a Z coupling to the quark line – hence the dependence upon the quark flavour.

When removebr is true in process 56, the Z boson does not decay.

7.20 Di-boson production, processes 61–89

[For more details on this calculation, please refer to hep-ph/9905386]

These processes represent the production of a diboson pair V_1V_2 , where V_1 and V_2 may be either a W or Z/γ^* . All the processes in this section may be calculated at NLO, with the exception of nproc=64. There are various possibilities for the subsequent decay of the bosons, as specified in the sections below.

7.20.1 WW production, processes 61-64

For WW production, both W's can decay leptonically (nproc=61) or one may decay hadronically (nproc=62 for W^- and nproc=63 for W^+). Process

64 implements the matrix elements for the leptonic decay of both W's but where no polarization information is retained. It is included for the sake of comparison with other calculations. Note that, in processes 62 and 63, the NLO corrections do not include radiation from the hadronic decays of the W.

When ${\tt removebr}$ is true in processes 61 and 64, the W bosons do not decay.

7.20.2 *WZ* production, processes 71–73, 76–78

For WZ production, the W is chosen to decay leptonically. The Z (or virtual photon, when appropriate) may decay into electrons (nproc=71,76), neutrinos (nproc=72,77) or a pair of bottom quarks (nproc=73,78). Note that, in processes 73 and 78, the NLO corrections do not include radiation from the bottom quarks that are produced by the Z decay.

When removebr is true in processes 71 and 76, neither the W or the Z boson decays.

7.20.3 ZZ production, processes 81–84, 86–89

For ZZ production, there are two sets of processes corresponding to the inclusion of a virtual photon when appropriate (nproc=81-84) and the case where it is neglected (nproc=86-89). Thus nproc=86-89 are really for diagnostic purposes only.

The Z's can either both decay leptonically (nproc=81,86), one can decay leptonically while the other decays into neutrinos (nproc=82,87) or bottom quarks (nproc=83,88), or one decays into neutrinos and the other into a bottom quark pair (nproc=84,89). Note that, in processes 83–84 and 88–89, the NLO corrections do not include radiation from the bottom quarks that are produced by the Z decay.

When removebr is true in processes 81 and 86, neither of the Z bosons decays.

7.20.4 Anomalous couplings

As of version 3.0, it is possible to specify anomalous trilinear couplings for the W^+W^-Z and $W^+W^-\gamma$ vertices that are relevant for WW and WZ production. To run in this mode, one must set zerowidth equal to .true. and modify the appropriate lines for the couplings in input.DAT, (see below).

The anomalous couplings appear in the Lagrangian, $\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{anom}$ as follows (where \mathcal{L}_{SM} represents the usual Standard Model Lagrangian):

$$\mathcal{L}_{anom} = ig_{WWZ} \left[\Delta g_1^Z \left(W_{\mu\nu}^* W^{\mu} Z^{\nu} - W_{\mu\nu} W^{*\mu} Z^{\nu} \right) + \Delta \kappa^Z W_{\mu}^* W_{\nu} Z^{\mu\nu} \right. \\ \left. + \frac{\lambda^Z}{M_W^2} W_{\rho\mu}^* W_{\nu}^{\mu} Z^{\nu\rho} \right] + ig_{WW\gamma} \left[\Delta \kappa^{\gamma} W_{\mu}^* W_{\nu} \gamma^{\mu\nu} + \frac{\lambda^{\gamma}}{M_W^2} W_{\rho\mu}^* W_{\nu}^{\mu} \gamma^{\nu\rho} \right],$$

where $X_{\mu\nu} \equiv \partial_{\mu}X_{\nu} - \partial_{\nu}X_{\mu}$ and the overall coupling factors are $g_{WWZ} = -e$, $g_{WW\gamma} = -e \cot \theta_w$. This is the most general Lagrangian that conserves C and P separately and electromagnetic gauge invariance requires that there is no equivalent of the Δg_1^Z term for the photon coupling.

In order to avoid a violation of unitarity, these couplings are included in MCFM only after suppression by dipole form factors,

$$\Delta g_1^Z \to \frac{\Delta g_1^Z}{(1+\hat{s}/\Lambda^2)^2}, \qquad \Delta \kappa^{Z/\gamma} \to \frac{\Delta \kappa_1^{Z/\gamma}}{(1+\hat{s}/\Lambda^2)^2}, \qquad \lambda^{Z/\gamma} \to \frac{\Delta \lambda^{Z/\gamma}}{(1+\hat{s}/\Lambda^2)^2},$$

where \hat{s} is the vector boson pair invariant mass and Λ is an additional parameter giving the scale of new physics, which should be in the TeV range. These form factors should be produced by the new physics associated with the anomalous couplings and this choice is somewhat arbitrary.

The file input.DAT contains the values of the 6 parameters which specify the anomalous couplings:

0.0d0	[Delta_g1(Z)]
0.0d0	[Delta_K(Z)]
0.0d0	[Delta_K(gamma)]
0.0d0	[Lambda(Z)]
0.0d0	[Lambda(gamma)]
2.0d0	[Form-factor scale, in TeV]

with the lines representing Δg_1^Z , $\Delta \kappa^Z$, $\Delta \kappa^\gamma$, λ^Z , λ^γ and Λ [TeV] respectively. By setting the first 5 parameters to zero, as above, one recovers the Standard Model result.

7.21 WH production, processes 91,96

These processes represent the production of a W boson which subsequently decays leptonically, in association with a Standard Model Higgs boson that

decays into a bottom quark pair. The calculation may be performed at NLO, although radiation from the bottom quarks in the decay is not included.

When removebr is true, neither the W boson nor the Higgs decays.

7.22 ZH production, processes 101–103

These processes represent the production of a Z boson (or virtual photon) in association with a Standard Model Higgs boson that decays into a bottom quark pair. The Z/γ^* subsequently decays into either an e^+e^- pair (nproc=101), neutrinos (nproc=102) or a further bottom quark pair (nproc=103). The calculation may be performed at NLO, although radiation from the bottom quarks in the decay of the Higgs (or the Z, for process 103) is not included.

When removebr is true in process 101, neither the Z boson nor the Higgs decays.

7.23 Higgs production, processes 111–116

These processes represent the production of a Standard Model Higgs boson that decays either into a bottom quark pair (nproc=111), a pair of tau's (nproc=112), a W^+W^- pair that further decays leptonically (nproc=113) or a ZZ pair. For the case of a ZZ decay, the subsequent decays can either be into a pair of muons and a pair of electrons (nproc=114), a pair of electrons and neutrinos (nproc=115) or a pair of muons and a pair of bottom quarks (nproc=116). The calculation is performed in the limit of infinite top quark mass, so that at LO the relevant diagram is the coupling of two gluons to the Higgs via a top quark loop. The calculation may be performed at NLO, although radiation from the bottom quarks in the decay of processes 111 and 116 is not included.

When removebr is true in processes 111–114, the Higgs boson does not decay.

7.24 H + b production, processes 141–143

[For more details on this calculation, please refer to hep-ph/0204093]

These processes represent the production of a Standard Model Higgs boson that decays into a pair of bottom quarks, in association with a further

bottom quark. The initial state at lowest order is a bottom quark and a gluon. The calculation may be performed at NLO, although radiation from the bottom quarks in the Higgs decay is not included.

For this process, the matrix elements are divided up into a number of different sub-processes, so the user must sum over these after performing more runs than usual. At lowest order one can proceed as normal, using nproc=141. For a NLO calculation, the sequence of runs is as follows:

- Run nproc=141 with part=virt and part=real (or, both at the same time using part=tota);
- Run nproc=142 with part=real.

The sum of these yields the cross-section with one identified *b*-quark in the final state. To calculate the contribution with two *b*-quarks in the final state, one should use nproc=143 with part=real.

When removebr is true, the Higgs boson does not decay.

7.25 $t\bar{t}$ production with decay, processes 151 and 152

These processes describe lowest order $t\bar{t}$ production including two leptonic decays $t \to bl\nu$ (process 151) and one leptonic and one hadronic decay (152). We use the matrix elements of ref. [9].

When removebr is true in process 151, the top quarks do not decay.

7.26 $t\bar{t}$ production with decay and a gluon, process 156

This process describes lowest order $t\bar{t}+g$ production including two leptonic decays $t\to bl\nu$. Zerowidth must be set to true for this case.

When removebr is true, the top quarks do not decay.

7.27 $Q\overline{Q}$ production, processes 157–159

These processes calculate the production of heavy quarks (157 for top, 158 for bottom and 159 for charm) up to NLO using the matrix elements of ref. [7]. No decays are included.

7.28 $t\bar{t}$ + jet production, process 160

This process calculates the production of top quarks and a single jet at LO, without any decay of the top quarks.

7.29 Single top production, processes 161–177

[For more details on this calculation, please refer to hep-ph/0408158]

These processes represent single top production and may be calculated up to NLO as described below.

Single top production is divided as usual into s-channel (processes 171–177) and t-channel (161–167) diagrams. Each channel includes separately the production of a top and anti-top quark, which is necessary when calculating rates at the LHC. Below we illustrate the different use of these processes by considering t-channel top production (161,162), although the procedure is the same for anti-top production (166,167) and the corresponding s-channel processes (171,172) and (176,177).

To calculate cross-sections that do not include any decay of the (anti-)top quark, one should use process 161 (or, correspondingly, 166, 171 and 176) with removebr true. The procedure is exactly the same as for any other process.

When one wishes to calculate observables related to the decay of the top quark, removebr should be false. The LO calculation proceeds as normal. At NLO, there are two options:

- part=virt, real or tota: final state radiation is included in the production stage only
- part = todk: radiation is included in the decay of the top quark also and the final result corresponds to the sum of real and virtual diagrams. This process can only be performed at NLO with zerowidth = .true. This should be set automatically. Note that these runs automatically perform an extra integration, so will take a little longer.

The contribution from radiation in the decay may be calculated separately using process 162. This process number can be used with part=virt,real only. To ensure consistency, it is far simpler to use 161 and this is the recommended approach.

7.30 Wt production, processes 180-186

[For more details on this calculation, please refer to hep-ph/0506289]

These processes represent the production of a W boson that decays leptonically in association with a top quark. The lowest order diagram involves a gluon and a bottom quark from the PDF, with the b-quark radiating a W boson and becoming a top quark. The calculation can be performed up to NLO.

Processes 180 and 185 produce a top quark that does not decay, whilst in processes 181 and 186 the top quark decays leptonically. Consistency with the simpler processes (180,185) can be demonstrated by running process 181,186 with removebr set to true.

At next-to-leading order, the calculation includes contributions from diagrams with two gluons in the initial state, $gg \to Wtb$. The p_T of the additional b quark is vetoed according to the value of the parameter ptbjetmin which is specified in the input file. The contribution from these diagrams when the p_T of the b quark is above ptbjetmin is zero. The values of this parameter and the factorization scale (facscale) set in the input file should be chosen carefully. Appropriate values for both (in the range 30-100 GeV) are discussed in the associated paper.

When one wishes to calculate observables related to the decay of the top quark, removebr should be false. The LO calculation proceeds as normal. At NLO, there are two options:

- part=virt, real or tota: final state radiation is included in the production stage only
- part = todk: radiation is included in the decay of the top quark also and the final result corresponds to the sum of real and virtual diagrams. This process can only be performed at NLO with zerowidth = .true. This should be set automatically. Note that these runs automatically perform an extra integration, so will take a little longer.

The contribution from radiation in the decay may be calculated separately using processes 182,187. These process numbers can be used with part=virt,real only. To ensure consistency, it is far simpler to use 181,186 and this is the recommended approach.

7.31 $Ht\bar{t}$ production, processes 190 and 191

These processes represent the production of a Higgs boson in association with a pair of top quarks. The calculation can be performed at LO only.

For process 190, neither the top quarks nor the Higgs boson decays. In process 191, both the top quarks decay leptonically and the Higgs boson decays into a pair of bottom quarks. Consistency with the simpler process (190) can be demonstrated by running process 191 with removebr set to true.

7.32 $Zt\bar{t}$ production, processes 196 and 197

These processes represent the production of a Z boson in association with a pair of top quarks which both decay leptonically. In process 196 the Z boson decays into an electron pair, whilst in 197 the decay is into a bottom quark pair. The calculations can be performed at LO only.

When removebr is true in process 196, the Z boson does not decay.

7.33 H+ jet production, processes 201–207

These processes represent the production of a Higgs boson in association with a single jet, with the subsequent decay of the Higgs to either a pair of bottom quarks (processes 201,203,206) or to a pair of tau's (202,204,207).

The Higgs boson couples to a pair of gluons via a loop of heavy fermions which, in the Standard Model, is accounted for almost entirely by including the effect of the top quark alone. For processes 201,202,206,207, the matrix elements include the full dependence on the top quark mass. The calculation can only be performed at LO. However, the Higgs boson can either be the Standard Model one (processes 201,202) or a pseudoscalar (206,207).

For processes 203 and 204, the calculation is performed in the limit of infinite top quark mass, so that NLO results can be obtained. The virtual matrix elements have been implemented from refs [4] and [5]. Phenomenological results have previously been given in refs. [3],[4] and [6]. Note that the effect of radiation from the bottom quarks in process 203 is not included.

When removebr is true in processes 201,203 and 206, the Higgs boson does not decay.

7.34 Higgs production via WBF, processes 211–217

[For more details on this calculation, please refer to hep-ph/0403194]

These processes provide predictions for the production of a Higgs boson in association with two jets via weak-boson fusion (WBF). The Higgs boson subsequently decays to either a pair of bottom quarks (processes 211,216) or to a pair of tau's (212,217).

Calculations can be performed up to NLO for processes 211 and 212. In addition to this, processes 216 and 217 provide the lowest order calculation of the WBF reaction which radiates an additional jet.

When removebr is true, the Higgs boson does not decay.

7.35 $\tau^+\tau^-$ production, process 221

This process provides predictions for the production of a tau lepton pair, with subsequent leptonic decays. The calculation is available at LO only. The relevant matrix elements are adapted from the ones in ref. [9].

When removebr is true, the tau leptons do not decay.

7.36 Z+Q production, processes 261–267

[For more details on this calculation, please refer to hep-ph/0312024]

These processes represent the production of a Z boson that decays into a pair of electrons, in association with a heavy quark, Q.

For processes 261, 262, 266 and 267 the initial state at lowest order is the heavy quark and a gluon and the calculation may be performed at NLO. As for H+b production, the matrix elements are divided into two sub-processes at NLO. Thus the user must sum over these after performing more runs than usual. At lowest order one can proceed as normal, using nproc=261 (for Z+b) or nproc=262 (for Z+c). For a NLO calculation, the sequence of runs is as follows:

- Run nproc=261 (or 262) with part=virt and part=real (or, both at the same time using part=tota);
- Run nproc=266 (or 267) with part=real.

The sum of these yields the cross-section with one identified heavy quark in the final state when inclusive is set to .false. . To calculate the rate for at least one heavy quark, inclusive should be .true..

For processes 263 and 264, the calculation uses the matrix elements for the production of a Z and a heavy quark pair and demands that one of the heavy quarks is not observed. It may either lie outside the range of p_T and η required for a jet, or both quarks may be contained in the same jet. Due to the extra complexity (the calculation must retain the full dependence on the heavy quark mass), this can only be computed at LO.

When removebr is true, the Z boson does not decay.

7.37 H+2 jet production, processes 271, 272

These processes represent the production of a Standard Model Higgs boson in association with two jets. The Higgs boson subsequently decays to either a bottom quark pair (nproc=271), or a pair of tau's (nproc=272).

The matrix elements are included in the infinite top mass limit using an effective Lagrangian approach. These calculations can be performed at LO only.

When removebr is true, the Higgs boson does not decay.

7.38 H+3 jet production, processes 273, 274

These processes represent the production of a Standard Model Higgs boson in association with three jets. The Higgs boson subsequently decays to either a bottom quark pair (nproc=273), or a pair of tau's (nproc=274).

The matrix elements are included in the infinite top mass limit using an effective Lagrangian approach. These calculations can be performed at LO only.

When removebr is true, the Higgs boson does not decay.

7.39 W+Q+ jet production (Q pdf), processes 311–326

These processes represent the production of a W boson that decays leptonically, in association with a heavy quark, Q and an additional light jet. In processes 311 and 316 Q is a bottom quark, whilst processes 321 and 326 involve a charm quark.

The initial state in these processes consists of a light quark and a heavy quark, with the light quark radiating the W boson. These calculations may be performed at LO only.

When removebr is true, the W boson does not decay.

7.40 W + c + jet production, processes 331, 336

These processes represent the production of a W boson that decays leptonically, in association with a charm quark and an additional light jet.

In contrast to processes 321 and 326 described above, the initial state in this case consists of two light quarks, one of which is a strange quark which radiates the W boson. The calculation may be performed at LO only.

When removebr is true, the W boson does not decay.

7.41 Z+Q+jet production, processes 341–357

[For more details on this calculation, please refer to hep-ph/0510362]

These processes represent the production of a Z boson that decays into a pair of electrons, in association with a heavy quark, Q and an untagged jet.

For processes 341 and 351 the initial state at lowest order is the heavy quark and a gluon and the calculation may be performed at NLO. As for H+b and Z+Q production, the matrix elements are divided into two subprocesses at NLO. Thus the user must sum over these after performing more runs than usual. At lowest order one can proceed as normal, using nproc=341 (for Zbj) or nproc=351 (for Zcj). For a NLO calculation, the sequence of runs is as follows:

- Run nproc=341 (or 351) with part=virt and part=real (or, both at the same time using part=tota);
- Run nproc=342 (or 352) with part=real.

The sum of these yields the cross-section with one identified heavy quark and one untagged jet in the final state when inclusive is set to .false. . To calculate the rate for at least one heavy quark and one jet (the remaining jet may be a heavy quark, or untagged), inclusive should be .true..

Processes 346,347 and 356,357 are the lowest order processes that enter the above calculation in the real contribution. They can be computed only at LO. When removebr is true, the Z boson does not decay.

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