

Theory of Computation Coursework – ACSF375

Questions answered: A1 and B1

A1) a.

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A1) a. 1.  $x = \lfloor i(3)/2 \rfloor = 1.5 = 1$   $x = 1$  ID: ACSF375

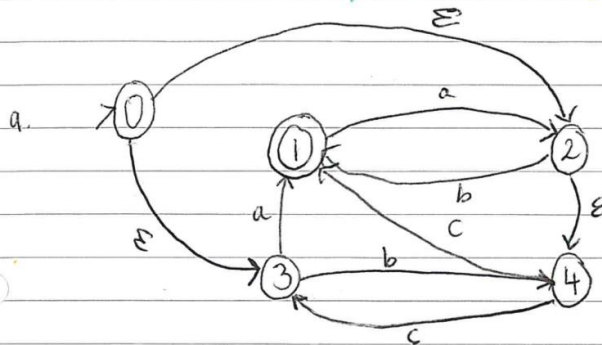
2.  $y = \lfloor x(1) + 3 \rfloor \bmod 5 = 4$   $y = 4$

3.  $z = \lfloor i(3)/5 \rfloor + 1 = 1.6 = 1$   $z = 1$   $i = 3$   $j = 7$   $k = 5$

4.  $u = \lfloor j(7)/5 \rfloor + 3 = 4.4 = 4$   $u = 4$

5.  $v = \lfloor k(5)/5 \rfloor + 1 = 2$   $v = 2$

6.  $w = 5 - v(2) = 3$   $w = 3$



A1) b.

b.) Create our transition table

State	a	b	c	ε	Initial state = 0 Accept state = 1 My empty transitions from start: 0 → 2 0 → 2 → 4 0 → 3
0	ε	ε	ε	2, 3	
1	2	ε	ε	ε	
2	ε	1	ε	4	
3	1	4	ε	ε	
4	ε	ε	1, 3	ε	

Create our new transition table:

Type of state	New state	a	b	c
Start	{0, 2, 3, 4}	{1}	{1, 4}	{1, 3}
Accept	{1}	{2, 4}	∅	∅
Accept	{1, 4}	{2, 4}	∅	{1, 3}
Accept	{1, 3}	{1, 2, 4}	{4}	∅
Accept	{2, 4}	∅	{1}	{1, 3}
Accept	{1, 2, 4}	{2, 4}	{1}	{1, 3}
Empty	{∅}	∅	∅	∅

## Renaming our states

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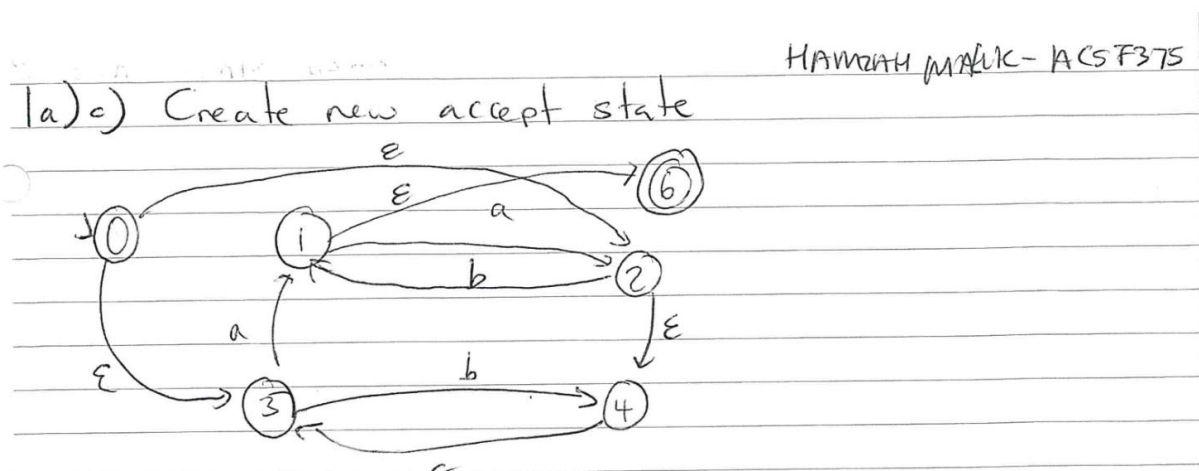
Type of state	new state	rename
Start	{0, 2, 3, 4}	{5}
Accept	{1}	{6}
Accept	{1, 4}	{7}
Accept	{1, 3}	{8}
	{2, 4}	{9}
Accept	{1, 2, 4}	{10}
	{4}	{11}
Empty	{0}	{12}

Type of state	New State	a	b	c
start	{5}	{6}	{7}	{8}
Accept	{6}	{9}	{12}	{12}
Accept	{7}	{9}	{12}	{8}
Accept	{8}	{10}	{11}	{12}
	{9}	{12}	{6}	{8}
Accept	{10}	{9}	{6}	{8}
	{11}	{12}	{12}	{8}
Empty	{12}	{12}	{12}	{12}

A1) c.

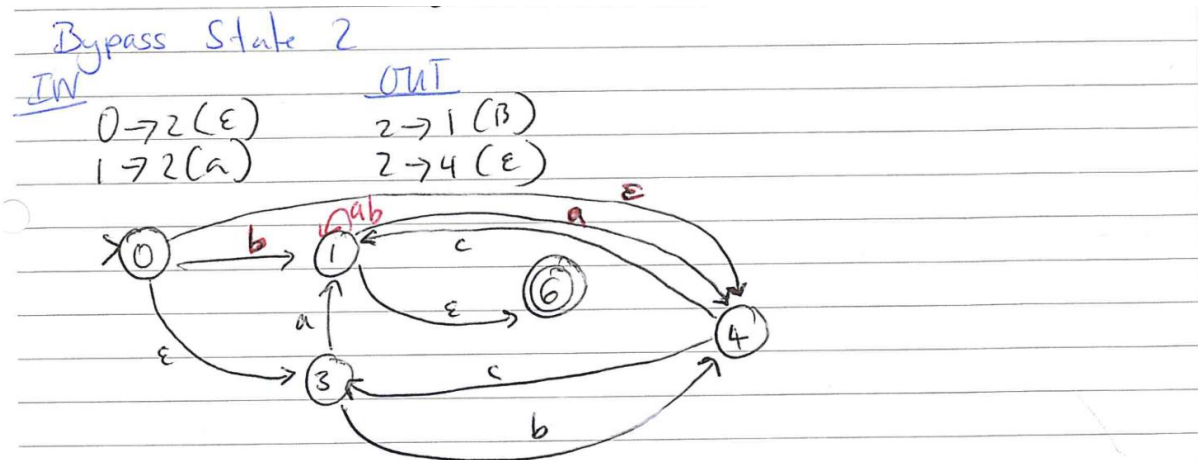
Creating a new accept state for my initial diagram.



My new accept state from my initial diagram in part a is now 6 instead of 1. Note a new start state is not needed as there are no incoming transitions from node 0.

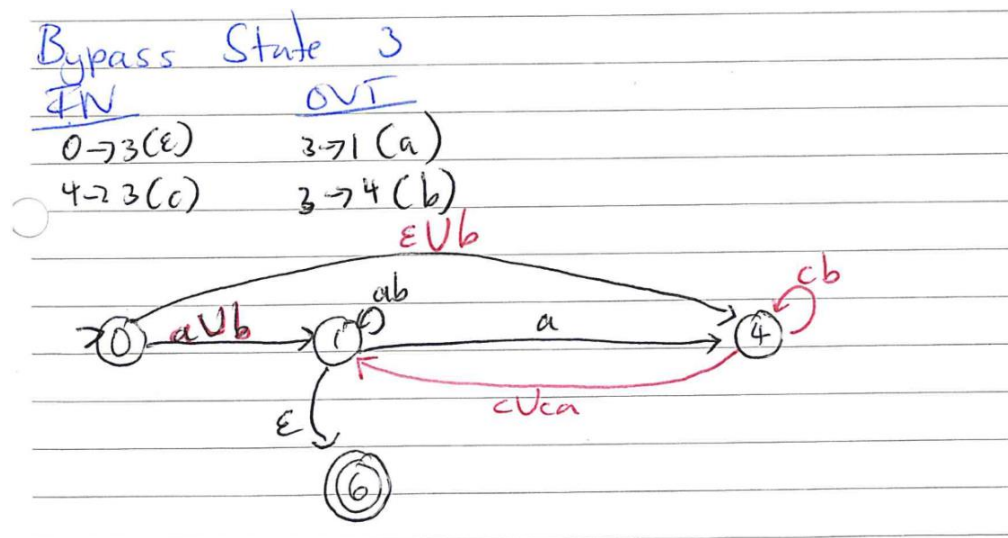
## Bypass State 2

I now bypass State 2 and label the incoming transitions and outgoing transitions. This gives a total of 2x2 transitions which means 4 new transitions – these are coloured in red in the diagram below.

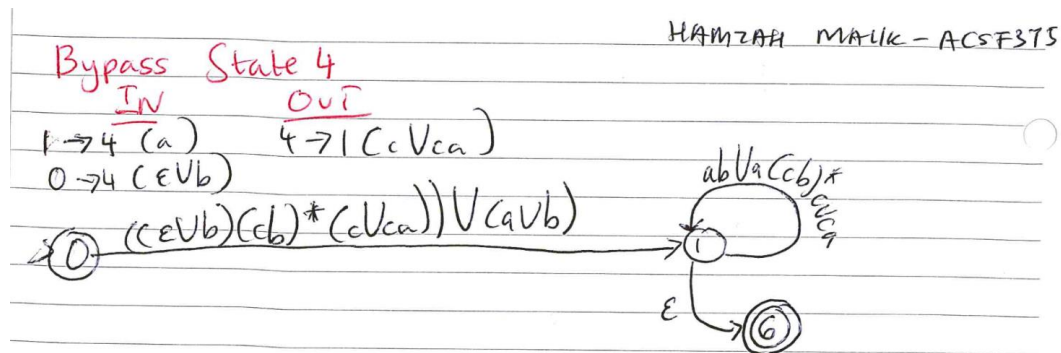


I have now chosen to bypass State 3. This also has four new transitions (2 in, 2 out) and labelled below in red.

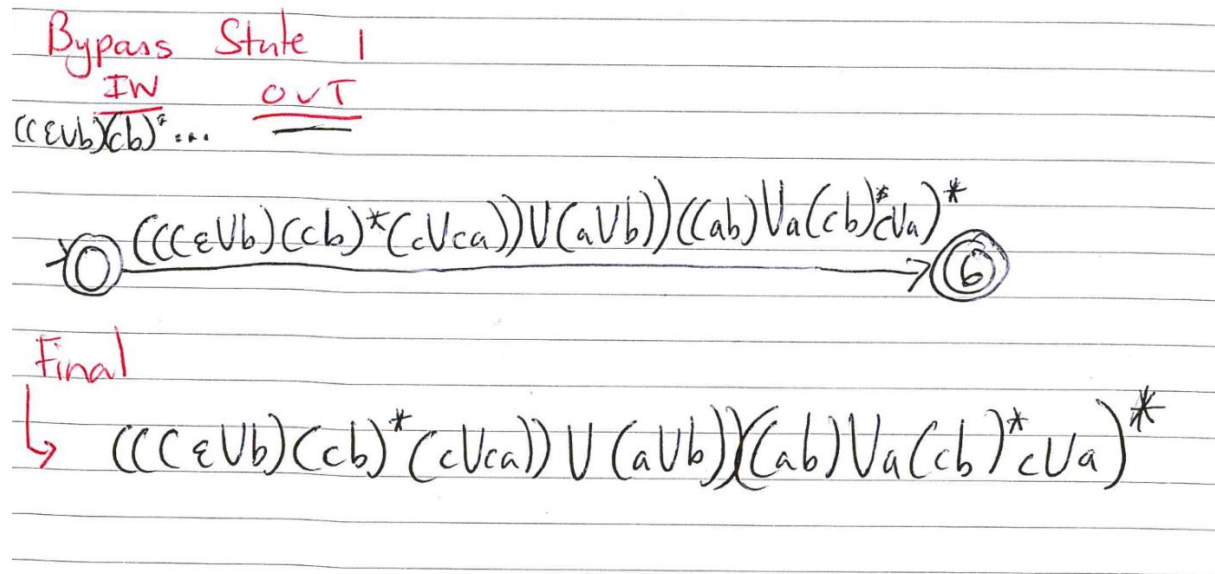
**Note:** I have applied the sum of edges to transitions where necessary.



## Bypassing State 4.



## Bypassing State 1



Our final regular expression from this diagram using Kleenes Theorem is:

$((\emptyset \cup b)(cb)^*(c \cup ca)) \cup (a \cup b)((ab) \cup a(cb)^*c \cup a)^*$



B1) a.

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B1) a) 1. First introduce our new start production rule.

$$\bullet S_0 \rightarrow S$$

$$\bullet S \rightarrow BDE \mid aE \mid b$$

$$\bullet B \rightarrow BC \mid \epsilon$$

$$\bullet C \rightarrow b$$

$$\bullet D \rightarrow SC \mid \epsilon$$

$$\bullet E \rightarrow BD \mid b$$

2. Now we must identify the productions that lead to null and remove these null productions.

$$\bullet B \rightarrow \epsilon \mid BC \mid C$$

$$\bullet D \rightarrow \epsilon \mid SC \mid C$$

$$\bullet E \rightarrow BD \mid B \mid D \mid \epsilon$$

$$\bullet E \rightarrow BDE \mid BD \mid BE \mid DE \mid B \mid D \mid E \mid a \mid \epsilon$$

$$\bullet S_0 \rightarrow S \mid \epsilon$$

↳ Now, we remove our null paths:

$$\bullet S_0 \rightarrow S$$

$$\bullet S \rightarrow BDE \mid aE \mid b \mid BD \mid BE \mid DE \mid B \mid D \mid E \mid a$$

$$\bullet B \rightarrow BC \mid C$$

$$\bullet C \rightarrow b$$

$$\bullet D \rightarrow SC \mid C$$

$$\bullet E \rightarrow BD \mid b \mid B \mid D$$

3. Remove unit productions  $\rightarrow$  first identify these!

- $SD \rightarrow S$
- $S \rightarrow B \mid D \mid E$
- $B \rightarrow C$
- $D \rightarrow C$
- $E \rightarrow B \mid D$

now these values are replaced.

- $SD \rightarrow BDE \mid aE \mid b \mid BD \mid BE \mid DE \mid BC \mid SC \mid a$
- $S \rightarrow BDE \mid aE \mid b \mid BD \mid BE \mid DE \mid BC \mid SC \mid a$
- $B \rightarrow BC \mid b$
- $C \rightarrow b$
- $D \rightarrow SC \mid b$
- $E \rightarrow BD \mid b \mid BC \mid SC$

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4. We have to remove the productions containing 2+ symbols.

These are:

- $SD \rightarrow BDE$
- $S \rightarrow BDE$

We introduce a new production rule for this case which we call

(Y)

$\hookrightarrow Y \rightarrow a$

This transforms our CFG to the following:

- $SD \rightarrow B \times \mid aE \mid b \mid BD \mid BE \mid DE \mid BC \mid SC \mid a$
- $S \rightarrow B \times \mid aE \mid b \mid BD \mid BE \mid DE \mid BC \mid SC \mid a$
- $B \rightarrow BC \mid b$
- $C \rightarrow b$
- $D \rightarrow SC \mid b$
- $E \rightarrow BD \mid b \mid BC \mid SC$

$\hookrightarrow Y \rightarrow DE \Rightarrow$  this is our new production rule

5. Lastly we remove our mixed productions and replace emptys removed.  
The only mixed productions are:

•  $S \rightarrow aE$

•  $S \rightarrow aE \rightarrow$  both mix terminals and non-terminals

To fix this, we introduce a new production rule for the **TERMINAL** symbol.

•  $Z \rightarrow a$

We also add an empty ( $\epsilon$ ) to  $S$  to replace the emptys removed.

**CNF OF OUR CFG:**

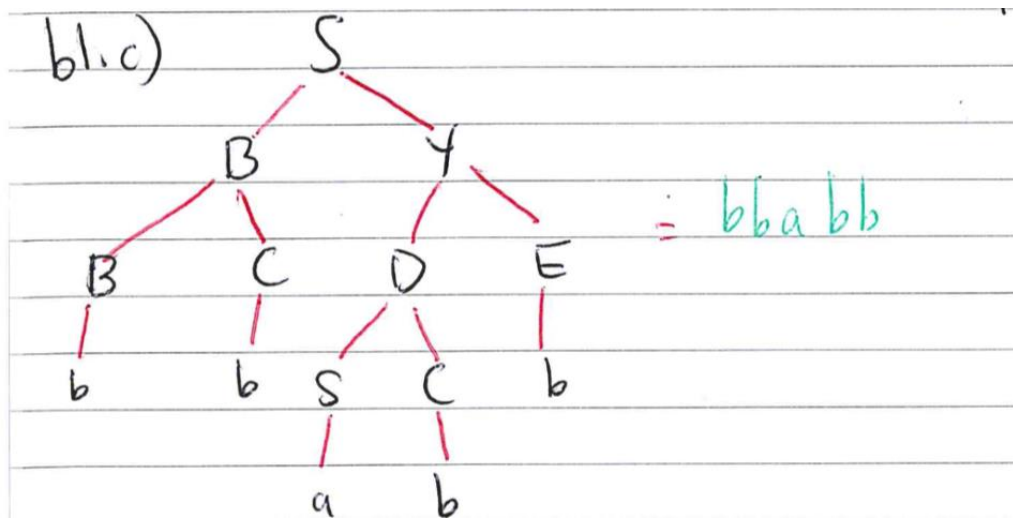
$S \rightarrow$	<del><math>BY</math></del>   $ZE$   $BD$   $BE$   $DE$   $BC$   $SC$   $a$   $b$   $\epsilon$
$S \rightarrow$	<del><math>BY</math></del>   $ZE$   $BD$   $BE$   $DE$   $BC$   $SC$   $a$   $b$
$B \rightarrow$	$BC$   $b$
$C \rightarrow$	$b$
$D \rightarrow$	$SC$   $b$
$E \rightarrow$	$BD$   $b$   $BC$   $SC$
$Y \rightarrow$	$DE$
$Z \rightarrow$	$a$

B1) b.

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$(S0, \epsilon, \epsilon), (F, S0)$	$(f, \epsilon, y), (f, DE)$
$(F, \epsilon, S0), (F, BX)$	
$(F, \epsilon, S0), (F, ZE)$	$(f, \epsilon, z), (f, a)$
$(F, \epsilon, S0), (F, BD)$	
$(F, \epsilon, S0), (F, BE)$	$(f, a, a), (f, \epsilon)$
$(F, \epsilon, S0), (F, DE)$	$(f, b, b), (f, \epsilon)$
$(F, \epsilon, S0), (F, BC)$	
$(F, \epsilon, S0), (F, SC)$	
$(F, \epsilon, S0), (F, a)$	
$(F, \epsilon, S0), (F, b)$	
$(F, \epsilon, S0), (F, \epsilon)$	
$(F, \epsilon, S), (F, BX)$	
$(F, \epsilon, S), (F, ZE)$	
$(F, \epsilon, S), (F, BD)$	
$(F, \epsilon, S), (F, BE)$	
$(F, \epsilon, S), (F, DE)$	
$(F, \epsilon, S), (F, BC)$	
$(F, \epsilon, S), (F, SC)$	
$(F, \epsilon, S), (F, a)$	
$(F, \epsilon, S), (F, b)$	
$(F, \epsilon, B), (F, BC)$	
$(F, \epsilon, B), (F, b)$	
$(F, \epsilon, C), (F, b)$	
$(F, \epsilon, D), (F, SC)$	
$(F, \epsilon, D), (F, b)$	
$(F, \epsilon, E), (F, BD)$	
$(F, \epsilon, E), (F, b)$	
$(F, \epsilon, E), (F, BC)$	
$(F, \epsilon, E), (F, SC)$	



B1) c.



B1) d.

Current State	Input Tape	Stack
S0	bbaabb	⊙
F	bbaabb	S0
F	bbaabb	BY
F	bbaabb	BCY
F	bbaabb	bCY
F	bbaabb	CY
F	bbaabb	bY
F	bbaabb	Y
F	bbaabb	DE
F	bbaabb	SCE
F	bbaabb	aCE
F	bbaabb	CE
F	bbaabb	bE
F	bbaabb	E
F	bbaabb	b
F	bbaabb	ε