

### III - UNIT.

#### Magnetic Sensors :-

##### INTRODUCTION :-

Magnetic sensor usually refers to a sensor that converts the magnitude and variations of a magnetic field into electric signal. (or)

Magnetic sensor that detects the magnitude of magnetism generated by a magnet or current.

##### What is magnetic sensor :-

- The sensor transducer which uses the change in magnetic field for their operation.
- used to measure the current, speed, position, & displacement.
- As the conventional sensor, magnetic sensor does not give output parameter directly.

- Signal processing is required for desired output.
- A few are being conveniently used in developing sensors. Some of these are:
  - Magnetic field sensor :- It developed following 'Ay' effect. In effect, is observed as the change in Young's modulus with magnetization.
  - Magneto-elastic sensors :- Based on the fact that in a longitudinal field, given in a ferromagnetic rod changes its magnetization.
  - Magnetic elastic sensors :- Produced using compressive stress changes magnetization or affects magnetization in some way.
  - Torque / force sensors :- 'Wiedemann effect' is used to develop the torque / force sensors.

## Magneto resistive Sensor :-

- Are developed on the basis of Thomson effect which is basically a change in resistance of specified materials with magnetic field impressed.
- ⇒ Hall effect Sensor (or) magnetogalvanic Sensors :-  
the most common and widely used type of magnetic sensor.

- They operate on the fact that a crystal carrying a current, to a magnetic field perpendicular to the direction of the current, produces a transverse voltage.

## $\Rightarrow$ Sensors and the Principle Behind:

- $\rightarrow$  In effect, the Ax effect is an outcome of magnetostriction.
- $\rightarrow$  A demagnetized ferromagnetic material.
- $\rightarrow$  When undergoes a mechanical stress.
- $\rightarrow$  It develops two types of stresses in it, namely:
  - (i) the plain mechanical elastic strain  $E_s$  and
  - (ii) the magnetoelastic strain  $E_m$ .
- $\rightarrow$  the magnetic domains by the applied stress  $S_a$ . Given.
- $\rightarrow$  the Young's modulus of the demagnetized material as

$$Y_{dm} = \frac{S_a}{E_s + E_m}$$

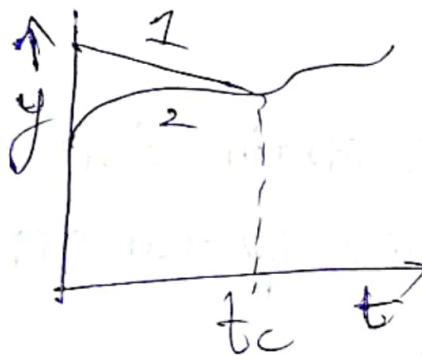
- $\rightarrow$  for a saturated sample no magneto-elastic strain is produced. no further orientation is possible.
- $\rightarrow$  And hence the ~~Young~~

Young's modulus becomes

$$Y_{sm} = \frac{S_a}{E_s}$$

where  $Y_{sm}$  is the Young's modulus of the saturated material.

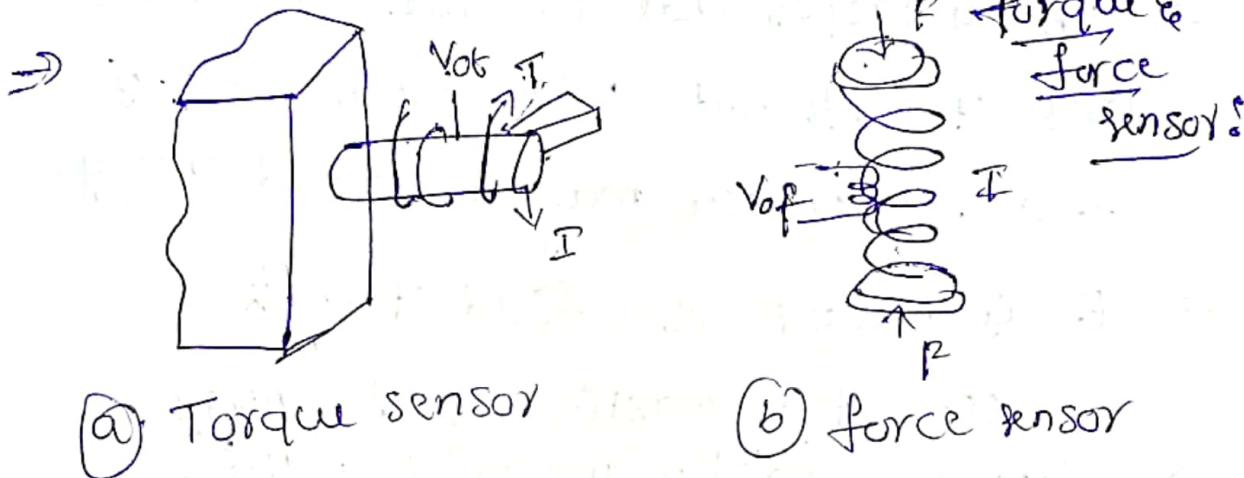
$$\frac{\Delta Y}{Y_{dm}} = \frac{Y_{sm} - Y_{dm}}{Y_{dm}} = \frac{E_m}{E_s}$$



for the material mentioned,

- In this figure varies depending on the annealing condition (temperature) of the material.
- In this figure critical temperature is  $t_c$ , which usually is close to the annealing temperature.

- Curve 1 in the figure corresponds to the magnetized state.
- Curve 2 in the nonmagnetized state.
- Change in  $\Delta V$  of about 10% can be obtained at room temperature.



- Weidemann effect is used to make torque/force sensor.
- Fix (a) & (b) with a current  $I$  passing in direction as shown in fig. And a torque produced in the rod.
- An output voltage  $V_{of}$  is obtained that gives a measure of the torque.
- In fig (a)
- In fig (b).  $V_{of}$  is the output voltage for the force in the balanced condition.

## Magnetoelastic Sensor:

Magnetoelastic sensor interactions and conversion of elastic energy  $E_s$  into magnetic energy  $E_m$  take place.

- $E_m$  is proportional to the product of field strength and polarization and often called the magnetic field energy.
- $E_s$  is product of field strength. ∵ called the elastic stress energy.
- depending on the material, there appears a crystalline energy  $E_{cryst}$ .
- An energy  $E_{ca}$  which is called the uniaxial anisotropy energy.
- The shape anisotropy energy  $E_N$  is developed.
- The magneto mechanical coupling factor  $k_{33}$  is defined as the ratio of the elastic stress · energy to the total storage energy.

$$k_{33} = \frac{E_s}{E_s + E_m + E_{cr} + E_{at} + E_N}$$

## Magnetoresistive Sensors :-

Magnetoresistive sensor uses the fact that the electrical resistance in a ferromagnetic thin film alloy is changed through an external magnetic field.

- Magnetoresistive effects are observed in metals specially in ferromagnetic types.
- It is known as anisotropic magnetoresistive effect.
- In Semiconductor, this effect is sometimes called the geometrical magnetoresistive effect.
- The effect is due to the fact that under magnetic field there occur different shifts of energy levels for electrons having negative and positive spins.

- Resulting in a change in density of states at the Fermi level.
- The current lines become longer and the resistivity increases.

### Anisotropic Magnetoresistive Sensing:

This type of magnetoresistive effect can be analyzed taking into account the complex ferromagnetic

- The Relation between the direction of magnetization and resistivity is sufficient also between the internal magnetization direction and external fields.
- If the angle between the direction of internal magnetization  $M$  and that of current in the sample  $I$  is  $\phi$  then, the resistivity is given by.

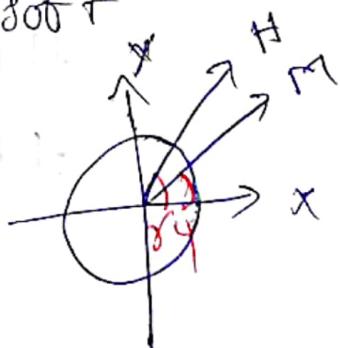
P.

$$\text{Resistivity } \rho(\phi) = \rho_x + (\rho_B - \rho_x) \cdot \cos^2 \phi$$

$\rho_x$  is the value of  $\rho$  for  $\phi = 90^\circ$

$\rho_B$  is the value of  $\rho$  for  $\phi = 0^\circ$

- Ferromagnetic materials have high internal magnetization because of exchange coupling at the quantum mechanical level.
- The electron magnetic moments parallel particularly in small areas known as domains which are separated by walls.
- Since different domains have parallelism in different directions.
- This is specially true for soft ferromagnetic materials.
- An external field  $H$ , magnetization  $M$  rotates which can be calculated by evaluating the energy density  $E$  in terms of the angle  $\varphi$  b/w  $M$  and the axis of lowest energy.



- The film can be considered to possess an elliptical shape.
- figure gives the geometry of the assumed structure.
- The major axis of the ellipse is the easy axis.
- Energy  $E$  has 3 components
  - (i) the field energy
$$E_H = -HM \cos(\gamma - \psi)$$
- (2) the anisotropy energy
- (3) the demagnetization energy.

$$H_{dx} = -N_x M \cos \psi$$

$$H_{dy} = -N_y M \sin \psi$$

## Semiconductor Magnetoresistors :-

- Semiconductor material is exposed to magnetic field. its resistance increases.
- The velocity  $v$  of a free charge carrier and the magnetic induction  $B$ .
- The Hall angle  $\Theta_H$  between the electric field  $E_H$  and the direction of the current.
- The charge in the direction of the current.
- Its rotation increases the path length of the current flow as mentioned.
- but is observed as an increase in the resistance of the material.
- The change in resistivity is proportional to the square of the component of the field perpendicular to the current vector,  $B_p^2$ .

$$\text{Thus } P_B = P_0 (1 + \rho B_p^2)$$

$\text{H.R}$  → the coefficient of magneto-resistance.

- If the magnetic field is large,  $\theta_h$  approaches  $\pi/2$  and  $P_B$ .
- It shows a linear dependence on field  $B$ .
- The semiconductor plate and magnetic field are included in the resistance ratio of the plate with and without field.

$$\frac{R_B}{R_0} = \frac{P_B}{P_0} [1 + c_a (\mu_H B)^2]$$

and for  $\theta_h \rightarrow \pi/2$

$$\frac{R_B}{R_0} \left( \frac{P_B}{P_0} \right) (c_b + c_c \mu_H B)$$

where  $c_a, c_b, c_c$

$c_a, c_b, c_c$  are factors dependent on the plate geometry.

$\mu_H$  is the Hall mobility.

- Resistance is linearly proportional to field  $B$ .

## Hall effect and Sensors :-

- Hall effect sensor is a type of sensor
- And magnitude of a magnetic field using the Hall effect.
- Hall effect sensors are also galvanomagnetic effect sensors.
- Hall effect is observed both in metals and Semiconductors.

### The Hall effect:-

- A current is sent through a very long strip
- It's homogeneous semiconductor in the x (long) direction.
- A magnetic field is applied to produce a flux density  $B_2$ ; then electric field  $E_y$  in the direction of y. which is called the Hall field.
- A voltage  $V_H$ ; called the hall voltage. is given by  $V_H = B_2 I e$ . -①

- Galvanomagnetic effects
- The Lorentz force on the charge carrier transport phenomena in condensed medium.
- The Lorentz force is expressed by

$$F = eE + e(v \times B) \quad \text{--- (2)}$$

where

$e$  is the charge of the carrier

$E$  is the electrical field

$v$  is the velocity and

$B$  is the magnetic induction.

If  $J$  is the total current density

then the carrier transport eqns is

$$J = J_0 + \mu_H [J_0 \times B] \quad \text{--- (3)}$$

→ The galvanomagnetic effects such as magnetoresistive and Hall effect can be derived from the solutions of Eq. - (3) with appropriate boundary conditions.

- ⇒ The Hall effect has varying intensity in different materials.
- ⇒ The materials for this effect are characterized by hall coefficient

which is defined as

$$h_c = -\frac{E_H}{J \times B}.$$

→ The Hall voltage can be expressed in terms of Hall coefficient  $h_c$

$$V_H = \pm h_c J_x B_z W.$$

→ The coefficient  $h_c$  is reduced if  $n_p$  and  $n_n$  are the concentrations  $\mu_p$  and  $\mu_n$  are the Hall scattering factors.

→  $\mu_p$  and  $\mu_n$  are the holes and electrons respectively, then the coefficient

is given by

$$h_c = \frac{1}{e} \frac{n_p n_p - n_n n_n (\mu_n / \mu_p)^2}{(n_p + n_n (\mu_n / \mu_p))^2}$$

→ Carrier density  $n_c$  equals  $n_p$  and  $n_n$  which is calculable from Standard caln.

$$n_c = A T^{\frac{3}{2}} \exp \left( \frac{-E_g}{2kT} \right).$$

A is coefficient

$T$  = Temperature

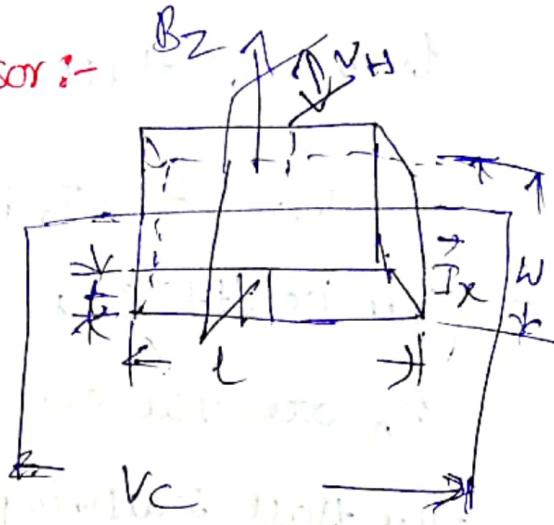
$k$  = Boltzmann constant

$E_g$  = band gap energy

The Hall effect sensor :-

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fig :- Hall sensor



In this fig : A voltage  $V_C$  across the supply electrode produce a current  $I_x$  which flows along the length and for a magnetic induction  $B_z$  across  $l \times w$  face shown in fig.

$$V_{H,i} = \frac{hc B_z I_x}{t}$$

A geometrical correction factor needs to be introduced which is defined

$$\text{as } k_g = V_H / V_{H,i}$$

$$\text{so } V_H = k_g \frac{hc B_z I_x}{t}$$

→ In large drop along the strip which may not be acceptable as a Sensor.

→ The voltage drop  $V_C$  is given by

$$V_C = R_h I_x = \left( \frac{I_x}{\mu_0 n_n} \right) \left( \frac{l}{w t} \right)$$

$V_H$  can be written as

$$V_H = - \frac{\mu_{Hn} k g B_2 V C W}{l}$$

## Inductance and eddy current sensor

→ Eddy current sensors are capable of high resolution measurement and are also referred to as inductive sensor.

→ Eddy sensor too current sensors work in magnetic fields.

→ Inductance and eddy current sensors follow the Faraday's law

of induction which is mathematically

$$\text{as } \oint E dI = - \frac{d}{dt} \iint_A B \cdot dA$$

- The voltage induced in closed turns of a coil is proportional to the time rate of change of flux linkage.
- The inductance sensors use the effect of voltage induction.
- The eddy current type use the current induced due to alternating magnetic field.
- Both these are the most useful. They are easily adapted to measure displacement, rpm, force, weight, acceleration, torque, pressure and so on.
- A voltage in proportion to a variable to be measured can be induced in a number of ways.
- (i) By varying the coupling between the two coils.

(ii) By changing inductance of two coils.

when a soft magnetic core is displaced inside them.

(iii) By varying magnetic flux linkage.

→ when an air gap is varied.

when the direction of magnetic polarization is changed. and so on.

→ Eddy current is produced by moving an electrical conductor in an alternating magnetic field. and its effects is utilized in the same way.

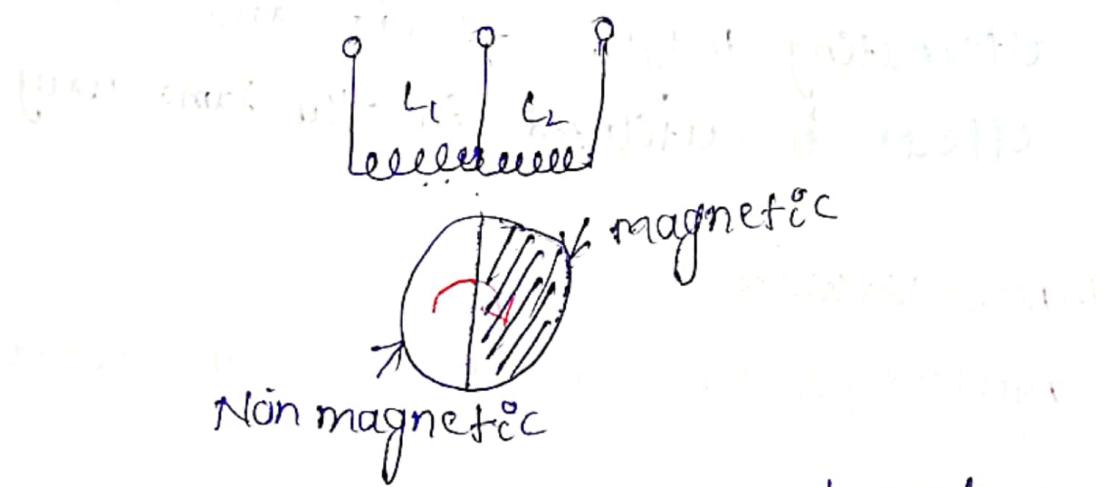
Linear Variable

Angular / Rotary movement transducers:

An angular movement such as twist or torsion of a shaft.

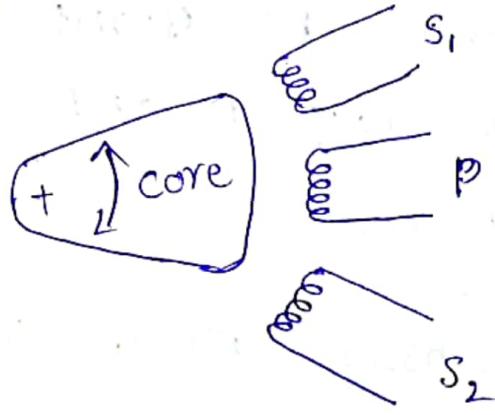
→ A section of the same may be made with half of it made of a ferromagnetic material.

- The half being made of non-magnetic material.
- Two coils are arranged.
- The inductance of the two parts.
- It depends on the amount of magnetic material in the linkage path of the coil fluxes.
- The scheme is shown in fig.



A split coil rotary transducer

Another technique for rotary motion measurement is a modified version of the LVDT as depicted in fig.



modified version of LVDT for angular movement measurement

### Synchros :-

A commonly used error detector of mechanical positions of rotating shafts in AC control systems is the synchro.

- A synchro is a type of transducer which transforms the angular position of the shaft into an electric signal.
- By changing the magnetic coupling between coils.
- As ac-excited electromechanical sensors have been developed.

→ for measurement at distant point  
It devices are adopted and are  
known as synchros.

→ Synchros, as sensors are of two types.

namely (i) torque type and  
(ii) control type.

→ The general constructional features  
of a synchro are represented in fig.

→ It consists of a stator with  
three windings  $S_1$ ,  $S_2$ , and  $S_3$  separated  
by  $120^\circ$  in space and a rotor  $R$ ,

→ which is supplied with an ac.  
voltage.

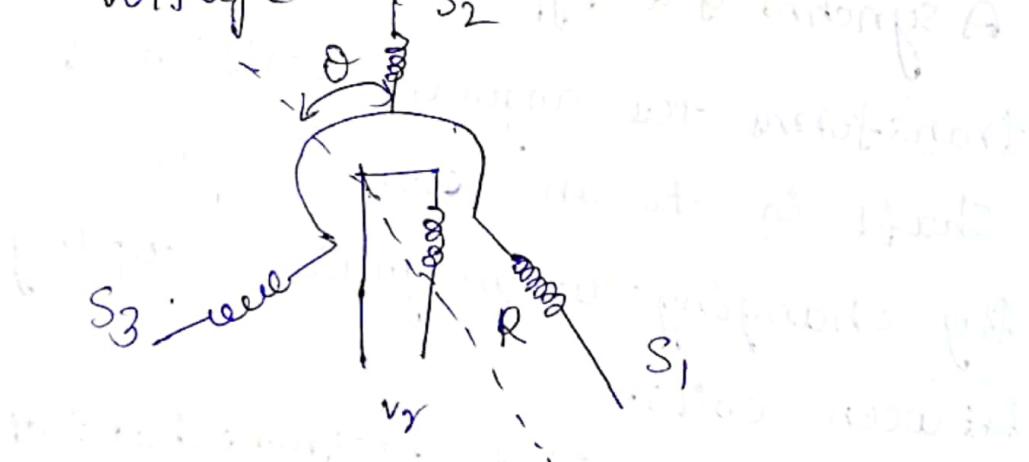


Fig: General constructional feature  
of a synchro.

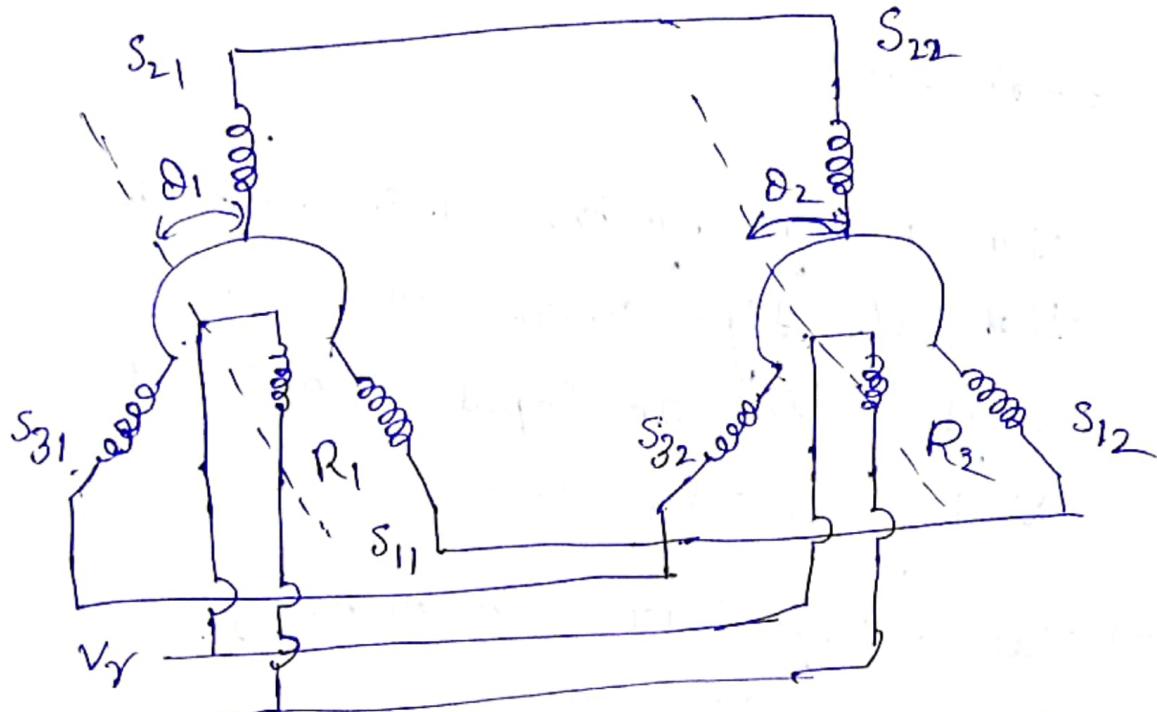


Fig:- Torque type synchro sensor.

- In magnitude and phase these windings are connected electrically to  $S_{12}$ ,  $S_{22}$  and  $S_{32}$ .
- It's same voltage with phase as in those windings of stator 1 produce a field.
- The rotor  $R_2$ , if not oriented as rotor  $R_1$ .
- If it is a receive a torque and rotation is same rotational position as that of  $R_1$ .

~~for A S~~

- for a single synchro unit such as that of fig. with the rotor angle  $\delta$  for an input sinusoidal voltage  $V_r = V_{r0} \sin \omega t$ .
- The voltage induced in windings  $S_1, S_2$ , and  $S_3$  are

$$V_{S1} = k V_{r0} \sin \omega t \cos(\delta + 120^\circ) \quad (1)$$

$$V_{S2} = k V_{r0} \sin \omega t \cos \delta \quad (2)$$

$$V_{S3} = k V_{r0} \sin \omega t \cos(\delta + 240^\circ) \quad (3)$$

where  $k$  is a constant, such as the ratio of the rotor to the stator turns. from eqn (3).

The line voltages are

$$V_{S12} = k \sqrt{3} V_{r0} \sin \omega t \sin(\delta + 240^\circ) \quad (4)$$

$$V_{S23} = k \sqrt{3} V_{r0} \sin \omega t \sin(\delta + 120^\circ) \quad (5)$$

$$V_{S31} = k \sqrt{3} V_{r0} \sin \omega t \sin \delta \quad (6)$$

→ In torque type Sensors. If it is assumed that  $\delta_1 = \delta_2$ .

→ ~~If~~ There are no unbalanced terminal Voltages.

→ The torque is approximately sinusoidal in form.

$$T = k_T \sin(\delta_1 - \delta_2) \quad \text{--- (7)}$$

→ This arrangement is known as the Synchro Control transformer.

→ The error voltage  $V_e(t)$  is proportional to the cosine of the angle between the two rotors.  $\cos(\delta_1 - \delta_2)$ .

$$V_e(t) = k' V_{ro} \sin \omega t \cos(\delta_1 - \delta_2) \quad \text{--- (8)}$$

→ If the two rotors are oriented at right angles,  $V_e(t) = 0$  and with

$$\delta_1 = 0^\circ \text{ and } \delta_2 = 90^\circ$$

If  $\delta_1 - \delta_2$  is close to  $90^\circ$ ,

then

$$V_e(t) = k' V_{ro} \sin \omega t \sin \{90^\circ - (\delta_1 - \delta_2)\}$$
$$\propto \{(\delta_1 - \delta_2) - 90^\circ\}$$

the error voltage is proportional to the angular rotational difference of the rotors. In case of synchro control transformer.

- To measure sum or differences of angles.
- The differential unit has star connected windings on both the Stator and the rotor.
- The rotor has a cylindrical structure.
- Synchro differential unit may also be used as a transmitter when its rotor is a driven one.
- Synchro torque units are used by transmitter  $S_{T_1}$  and  $S_{T_2}$  and the differential unit is used by Synchro differential receiver.