Unit - IV

Graphs: Graph Implementation Methods. Graph

Totaversal methods.
Sorting: Heap Sort, External Sorting - Model for external Sorting, Merge Sort.

Introduction to Graphs

A graph is a Collection of two Sets V and E whose "V" is a finite non-empty set of vertices and "E" is a finite non-empty set of edges.

* Vertices are nothing but the nodes in the graph.

* Two adjacent vertices are joihed by edges.

* Any graph is denoted as G= SV, Eg.

in between the

 $\frac{\mathcal{E}_{X'}}{\mathcal{E}_{X}}$ E5

9= { { V, , V, , V3, V4, V5, V3, $\{E_1, E_2, E_3, E_4, E_7, E_8, E_8\}$

Edge: An edge is a Connecting link between two vertices. Edge is also known as Arc. In the above example graph E_1 , E_2 , E_3 , E_4 , E_5 , E_6 , E_7 are known as Edges. (ie) (V_1, V_2) (V_1, V_3) (V_1, V_4) (V_2, V_3) (V_3, V_5) (V_4, V_6) (V_5, V_6)

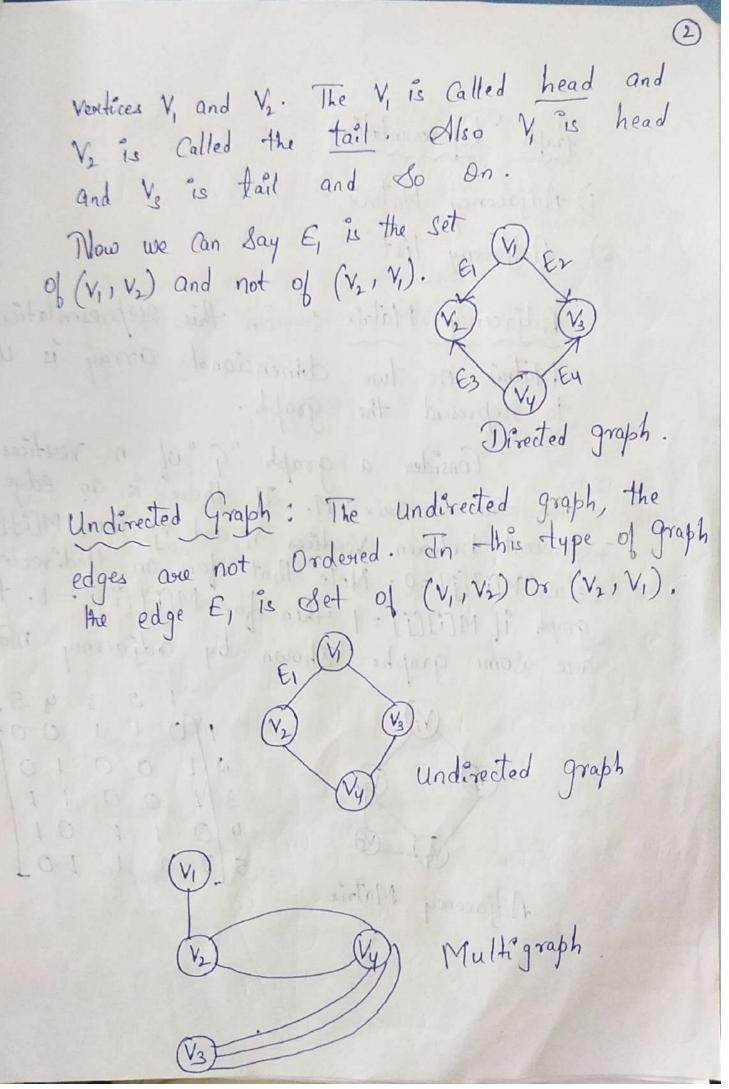
Types of Graphs

Basically graphs are of two types

O Directed graphs

Undirected graphs.

Dissected graphs: - In the directed graph the dissections are Shown on the edges. the edges between the vertices are Ordered. In this type of graph, the edge E, is in between the



the bank teller is a V all of bank and Graph Reposesentations D Adjacency Matrix Adjacency Matrix: - In this suppresentation,

Matrix or two dimensional array is Used

to suppresent the graph. Consider a graph "9" of n Vertices
and the matrix M. II there is an edge

present between Vertices You and V; then Mci][j]=1

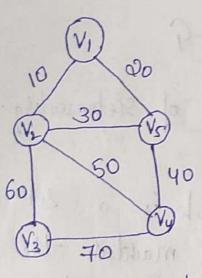
else Mci][j]=0. Note that for an Undirected

else Mci][j]=0. Note that for an Undirected graph if M(i](j]=1 then for M(j][i]=1. Here are some graphe shown by adjacency matrix. 1 2 3 4 5 1 0 1 1 0 0 2 1 0 0 1 0 3 1 0 0 1 1 5 0 0 1 1 0] Adjacency Matrix HOPE HOLD KIND

Adjacency Matrix dor Weighted graph

In the weighted graph, weights or distances are given along every edge. Hence in an adjacency matrix representation any edge which is present between Vertices V; and V; is denoted by its weight.

Hence M[i][j] = Weight of edge.



20 10 10 30 70 0 40

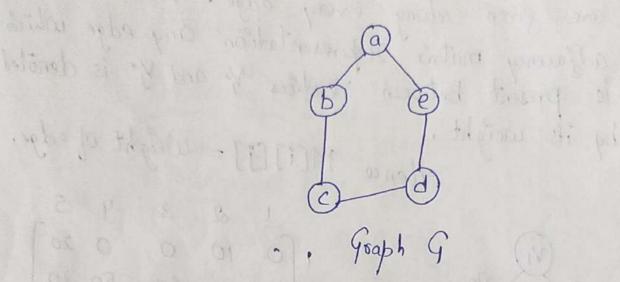
Adjacency Matrix

Adjacency matrix depresentation for Weighted graph

If there is no edge between Vi and Yo then . ishop Inputs.

M[i][j] = 0.

Adjacency list: In this Representation, a linked list is Used to Represent a graph.



There are two methods of Hepresenting graph using adjacency list.

Method 1:- The graph is a set of Vestices and edges, we will maintain the two structure dor vestices and edges respectively.

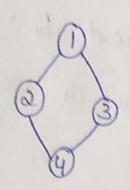
Exim graph has the nodes as a, b, c, d, e. we will mantain the liked list of these head nodes as well as the adjacent nodes.

(cont.-d]

Graph Pravorsale DBFs DFs

> BFS [Bread first Search]: - In BFS We Start Jeon Some Vertex and Jihd all the adjacent vertices of et. This Process will be Despeated for all the Vertices. So that the Vertices breadth get Printed. for Avoiding Repetition of Vertices, we maistain array of visited nodes. A queue data structure is used to store adjacent Vertices.

Implementation of BFS: - In BFs the queue "is maintained for Storning the adjacent nodes and an array 'Visited' is maintained for Keeping the track of visited nodes. The Once a Particular node is Visited it should not be Dievisited again.



Step 1: Start with Vertex 17

0 1 2 3 4

Inserted Veetext in queue and mailed the index! of Visited array by 1.

Step 2:
0 1 2 3 4

Front

Hear

of the state and the the state of

Delete 1' and pontit it. So 1'gets Ponted.

Step 3: Find adjacent Verticus of Vertex 1 and mark them as Visited, Insert those in Queue.

Visit

O 1 2 3 4 Increment front

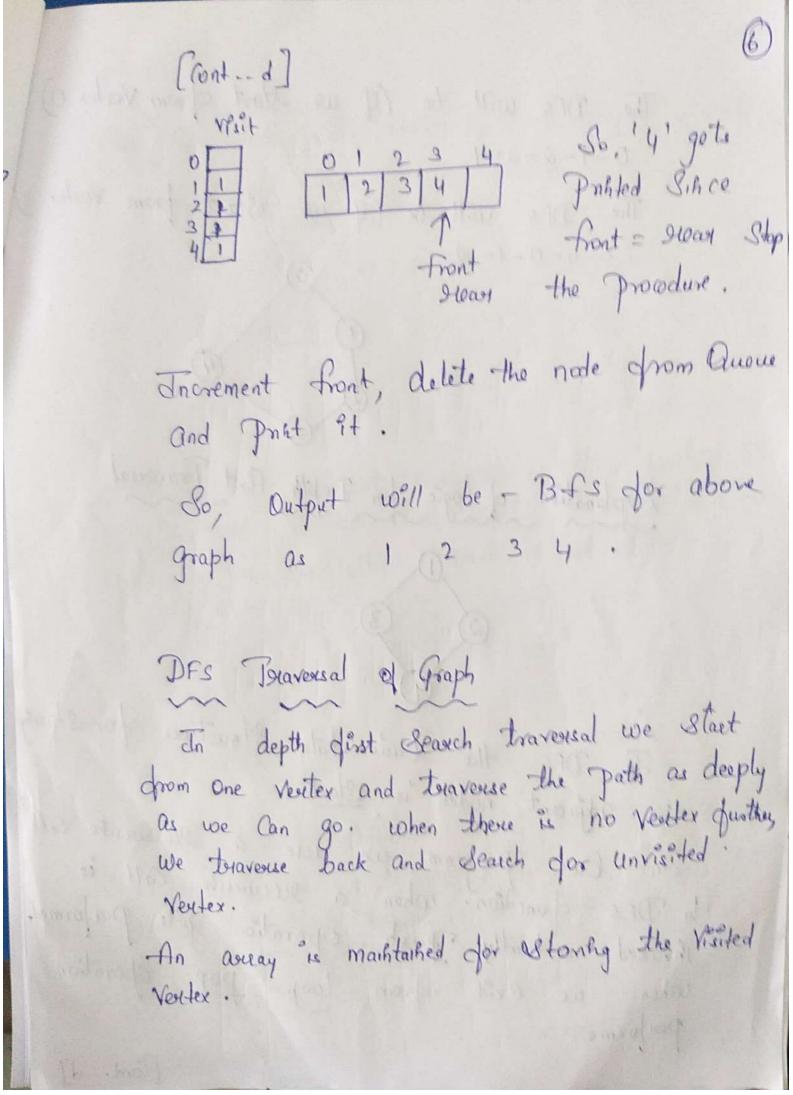
[12] 1 by 1 delete 12'

Here and

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Step 4: find deligacent to 2' and insent nodes in Queue as well as mark them as Visited Step 5: Increment front and delete the node 80 13' gets prihted Step 6: find adjacent to 13' i.e 4 Check whether it is marked as Visited. If it is marked as visited do not insert in the

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The DFS will be (if we start from Vertex 0) The DFs will be (if we start from Vertex 3) 3-4-0-1-2 doleto the male of som Encur Explanation of logic for Depth first Travousal the basic data Storicture for Storing In DES the adjacent nodes is stack. In Dur Program we use a recursible Call to DFS function. when a recursible Call is throked actually push operation gets performed. When we exit from loop pop operation Performs [Cont. ...d]

[Contd]
Step 1: Start with Veritex 1, Print it So'1' gets Printed. Mark 1 as Visited. Vesited 1 1 2 3 4 0 3
graph'g'
Step 2: find adjacent Ventex to 1, Say i.e 2'. if it is not Visited, Call Drs(a) i.e a will get inserted in the stack, mark is as visited. Visited Visited Visited O O O O O O O O O O O O O
Step 3: find adjacent to '2' i.e Vesitex 4 if it is not visited Call DFS (4) i.e, 4 will get pushed is not visited Call DFS (4) i.e, 4 will get pushed.
is not Visited Call DFS (4) 110. On to the Stack mark it as Visited. Of O Visited Stack Of O Visited Stack Of O Visited Stack

I do to they it sales I die to Btep 4: find adjacent to 14' ie Verter 3 il it is not visited Call DFs.(3) Tie 3 will be Pushed Onto the Stack mark it Visited. Misited Stack

O 1

2

1

Loop 3 will be

Popped print 13'. (a) 1) (a) 27(a) 1/6 (b) 1/6) Since all the nodes are Correct Stop the Procedure. So, Output Q DFS is 1243. Applications of Graph 1) In Computer networking Such as local Area Network (IAN], Wide Area Metworking (WAN),
internetworking. 2) In telephone Cabling graph theory is effectively used. 3) In job Scheduling Algorithms.

Depth - first Traversal

Algorithm

i) Instialize all the nodes to steady state and stack to empty
Stack to empty
State [v] = 1 (: 1 indicates Ready
State]

2) Begin with any arbitrary node 's' in graph,

Push et onto State [s] = 2 (!: 2 shdicates
waithy state]

3) Repeat through 8-tep 5 while stack is not empty

4) Pop node N of stack and mark the status of node to be Visited.

5) Push all nodes w adjacent to 11 thto Stack and mark their status as waiting.

State (W] = 2

6) If the graph Still Cortains nodes which are in steady state goto Ekp 2.

7) Petwin.

```
Lossedon P traffic displication
      Stogram
      # Include ( Stor h >
 # Include < Conio.h>
        int a [20] (20], reach [20], n;
        Void des (18th v)
In States S
        "int i;
          Heach [v]=1;
 for (i=1; i <=n; i++)
  if (a[v][i] & &! steach[i])
   Prhtf ("In o/. d?", v, i);
dfs(i); 32
 (int i, j, Count = 0;
       Printf(" | n Enter number of vertices");
 Scant (", dx, 2n);
       for(i=1; ic=n; i++) &
        for (j=1; j<=n; j++)
     a cij cij = 0; 19th
       Prohot of (" In Enter the adjacency matrix In")
          -for ( =1; i <= n; i++)
```

for (j=1; j<=n; j++) Scart (" % d", & a (i) (i)); dfs(1); Post + (1 1 2) - 1 don a word ! for (i=1; ix=n; i++) if (reach (i) Count ++; 10 man of the 3 (Count = = n) Point-f ("In Graph is Connected"); else Printf ("In Graph is not Connected"),
getch (); Advante > shutch Boreadth Fixt Praversal -Algorithm: 1) Initialize all nodes to Heady State State[V]=1 [Here V sie ponesents all nodes of graph] its state to waiting.

3) Repeat through Step 5 Until queue is not empty.

4) Remove a node N from pueue and change its Status to Visited.

(But a land)

to betranno 2 de p 1 1 1- thirt

State [N]=3.

5) Add to pueue all neighbows

Priogram for BFS (Breadth - first Search]

1hclude < Stdio.h >

int a[20] [20], 9[20], Visited (20], n, i, j, f=0,

91=-1;

Void bfs (1ht v)

{
-for (i=1; i<=n; i++)

if (a[v][i] 4 & ! visited (i])

9(++91) = i;

if (f <=91)

```
Visited (9(4)] = 1;
     bfs(9(++1));
    Void main ()
      int v;
  Poshtf (" In Giter the number of vertices:"),
  Scanf ("./.d", &n);
for (i=1; i<=n; i++)
    9[1]=0;
   Visited [i] = 0;
  Prohtf ("In Enter graph data in matrix dorm: In").
  for (i=1; ic=n; i++)
  E it's contrary to reduce it paties
   for (j=1; j<=n; j++)
32 Scart (" % d", & a(i](s]);
 Printf ("In Enter the Stauting Vertex:");
 Scanf ("/.d", &v);
```

```
bfs(v);
       Parint f(" |n The node which are swachable are: 10"),
        for (i=1; i(=n; i++)
        { Visited (i])
        Paint f ("/, d | t", i);
     else a relative attended of the state
          E Point f (" In Bfs is not possible. Not all nodes
          aue greachable ");
           bollak;
Ratter of the graph date in this form the
         Output
         Enter the number of Vertices: 4
         Enter graph data in matrix form;
         Part of the Colon the assenting see less in
```



Lostling

Southing: The Sorting is a technique by which we expect the list of elements to be arrange as Ascending or Descending order.

Ascending Order: The elements one Sorted in low - high Order.

Descending Order: The elements are Sorted in high - low order.

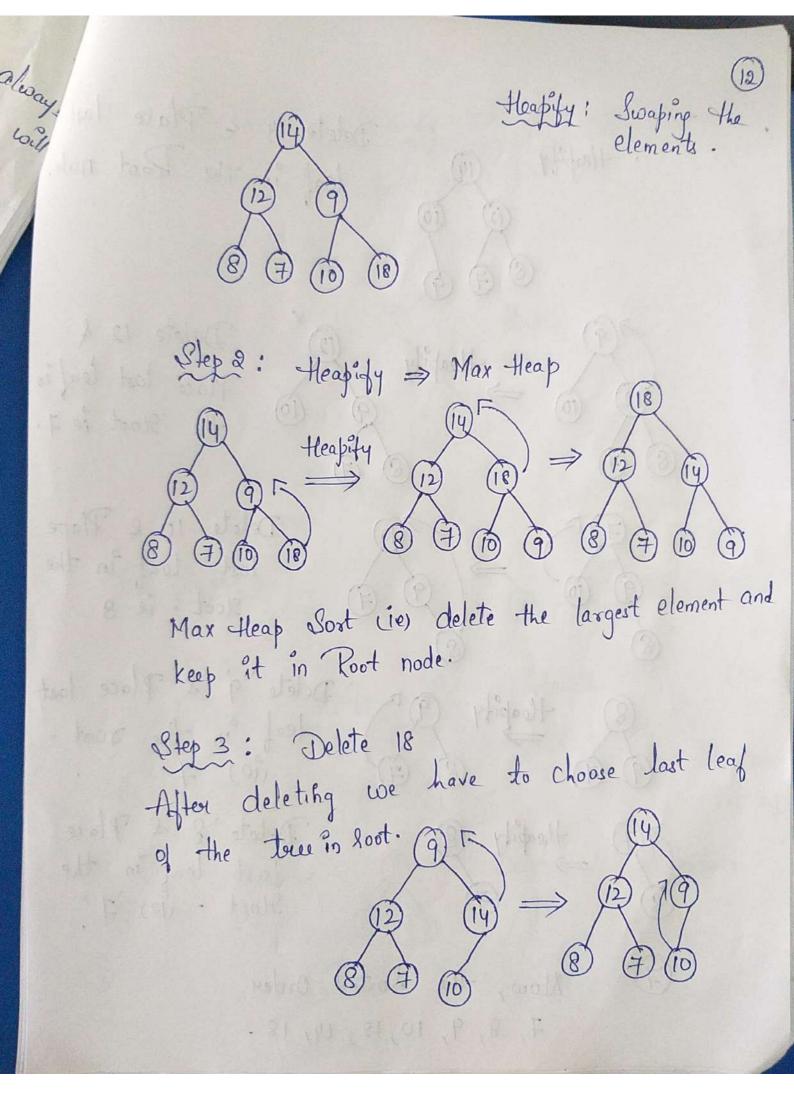
Heap Sort: Heap Sort is a Sosting method discovered by J. W. J. Williams. It works in two stages.

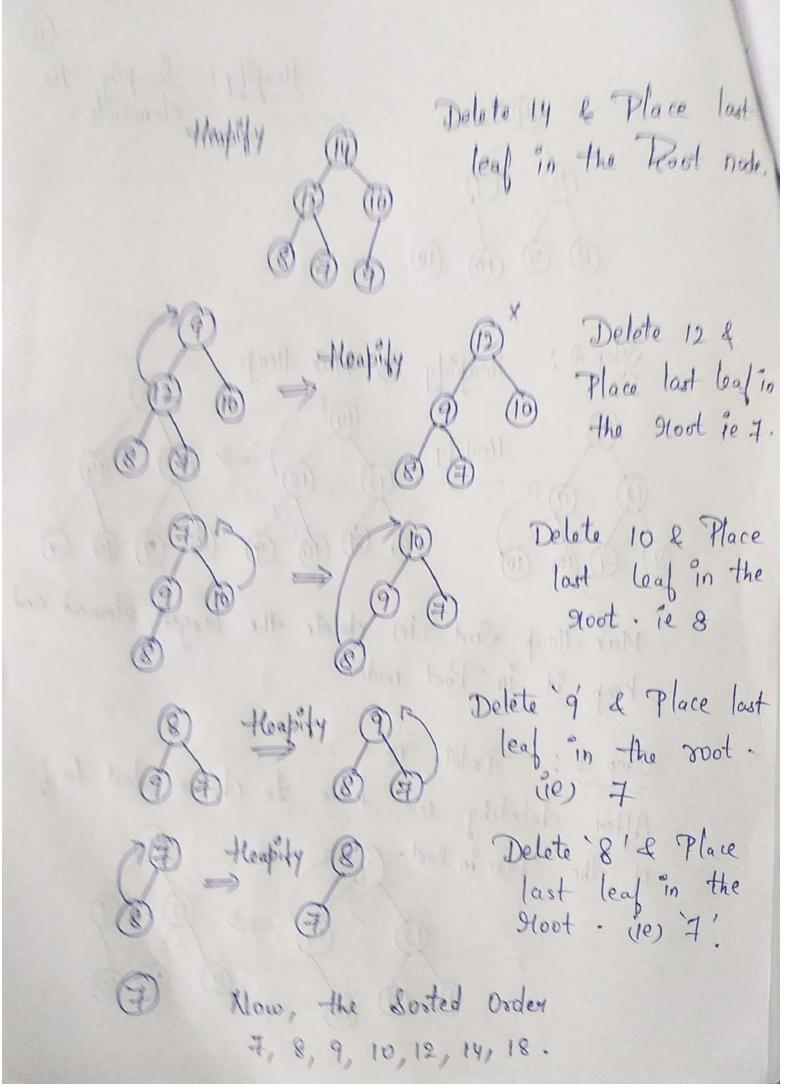
) Heap Construction

2) Deletion of Maximum key

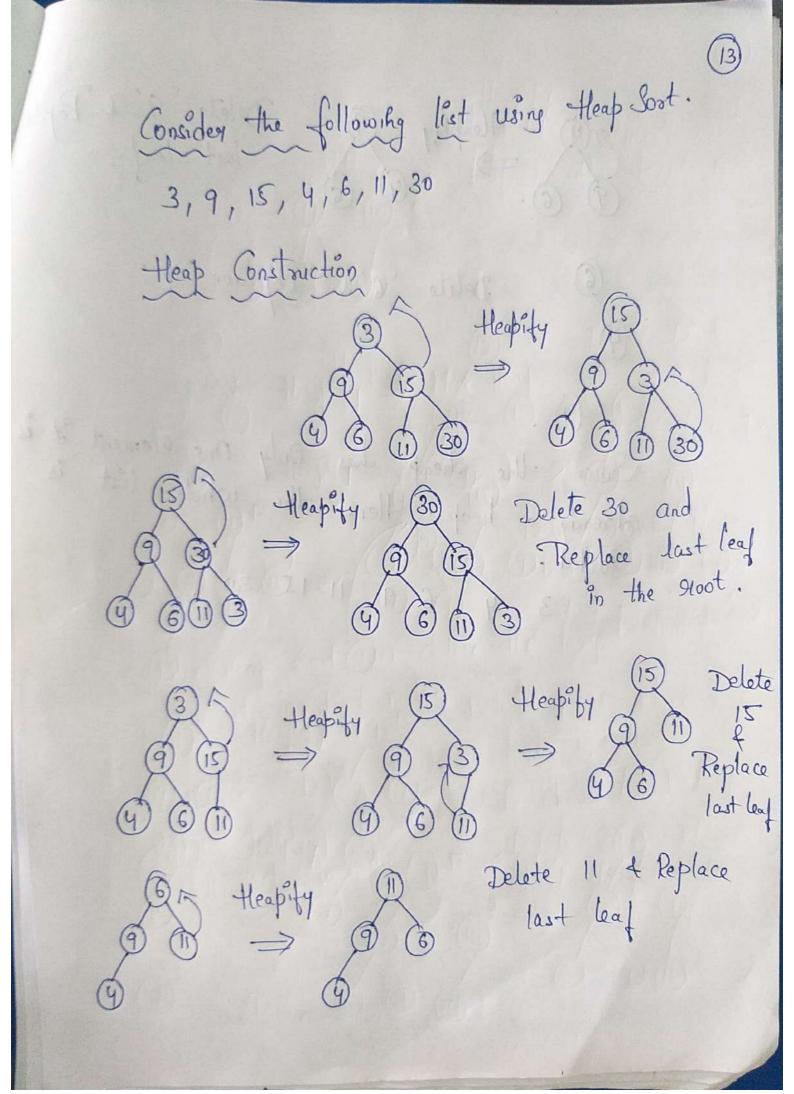
Heap Construction: first Construct a heap dor given numbers.

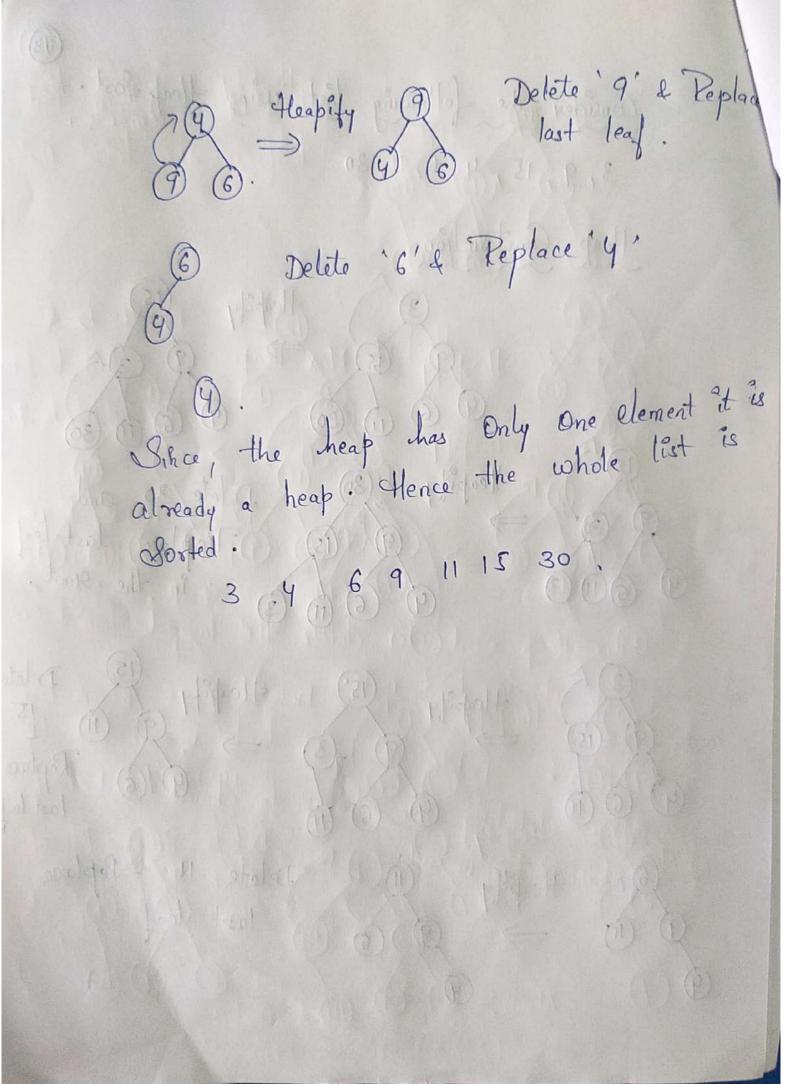
Deletion of Maximum key: Delete 900t key alway) for (n-1) times to Hemaining heap. Hence we will get the elements in decreasing order. For an array heap implementation of delete the element from heap and Jut the deleted element in the last position in away. Thus after deleting all the elements one by one, if we Collect these deleted elements in an array starting from last index of array. Heap Sort - SDeletion of Mox Key Model FE - 4moillill . T. MIT pd 1) Sost the elements using Heap Sort. 14, 12, 9, 8, 7, 10, 18. Step!: Heap Construction Hore Construct the tree as in the given Sequence.





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External Sorting

External Borting Process is used when the number of elements (or succords) to be Sorted age in large number, Such that all of them Cannot be accommodated in the internal memory of Computer. These deles Containing huge decords to be Ported au Stored on external Storage devices and external sorting process is applied.

The external Sorting process performs

1) Bring few succords [from external storage] into the main memory.

2) Apply internal Sort algorithm on those decords to generate "Juns".

3) Write " 9 uns." Onto the external storage devices.

4) Mesge the "Quins" generated in the Steps

5) Repeat Steps (100, 2, 3, 4 until all ours ave morged and a Single " run" which is a Sorted file of records are left ait. Consider a file Containing 1000 96 Cords. But main memory Can accommodate Only 200 9600000 at a time. Therefore, External Sorting technique is applied as follows. 1) Read the first 200 seconds from the Input file, Sort them and write them to an output morge file [Say merge A]. Read another 200 seconds, Sort them and write them to an Alternate menge file (Say menge B). [Say menge B]. 3) Again another 200 Herords are Head from shout
Ale, Sorted and written to merge fele Merge
A. Thes Process is Repeated until all Herords are read and Sorted. 1000 Records 17-10 p. 81 C Sout and write hewall on merge diles Records 201 - 400 Merge B "Records 1-200 Records 401-600 Merge-A "Rocords 601 - 800 Records 801-1000

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Examples of external Sorting algorithms

D MultiPway Meige

Bax

2) Polyphase Merge.

Multiloay Merige: A multiloay merige is an n-way merige that uses additional tapes and makes Sosting of input more Simples by minimizing the total number of passes.

let $T_{x_1}, T_{x_2}, T_{x_3}, \dots, T_{x_n},$ $T_{y_1}, T_{y_2}, T_{y_3}, \dots, T_{y_n}$ be the tapes.

Out of these In tapes, half of them will work as a shput tapes and the Other half will work as Output tapes.

Tx, 25 88 1 80 5 29 8 90 15 61 32 69 7

TX2 TXN TYN TYN

employed although of the algorithms Meorge Sorting Merge Sort Merge Sort is an external Sorting algorithm which Makes use of Secondary Storage. It uses divide and Conquer approach to Nort a given list. It desides the list into n Sublists of Gud Size Until Only One element is left in Sublist. Theo it Recursively applies merge sort on two Borted Sublists to down a Combined list. Evi- Apply Merge Sort on the following list 12, 11, 35, 19, 62, 25, 41 12 11 35 19 62 25 41 62 25 41 11 35 19 62 25 41 11 35 19

