

# Example: Uncertainty Quantification of a Differential Amplifier

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This code was developed by Miodrag Bolic for the book PERVASIVE CARDIAC AND RESPIRATORY MONITORING DEVICES

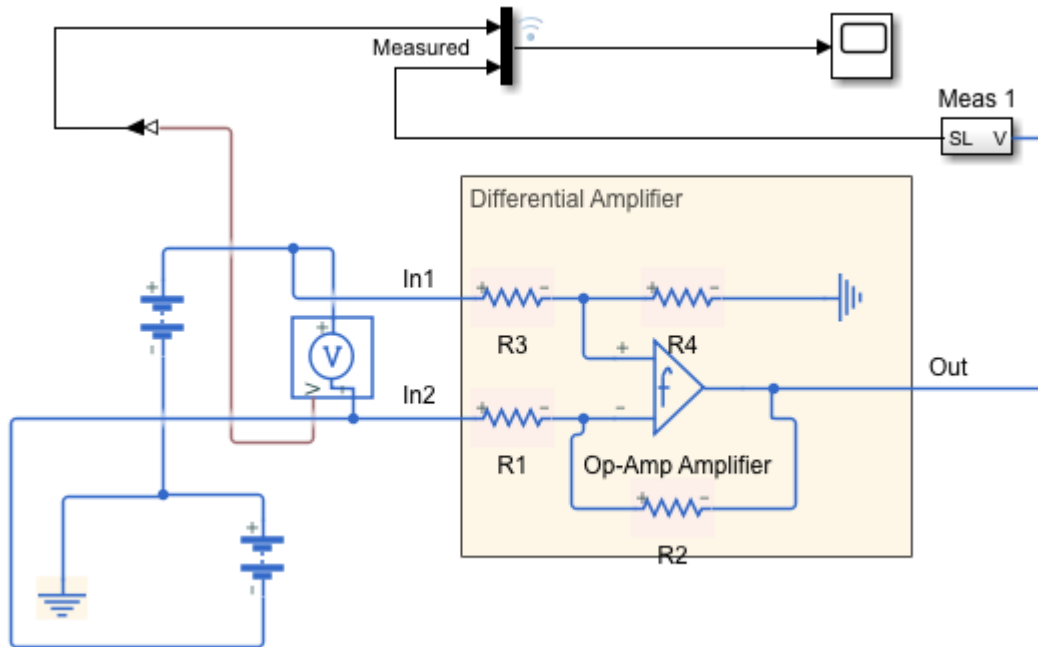
## Introduction

Resistors are commonly given with their tolerance of 0.1 %, 1 %, 2 % and so on. It is commonly assumed that the resistor values follow uniform distribution. If the tolerance is given as the variable (tol) then the values of the resistor can be sampled from the uniform distribution in the range  $[R - \text{tol}, R + \text{tol}]$ .

## Differential Amplifier

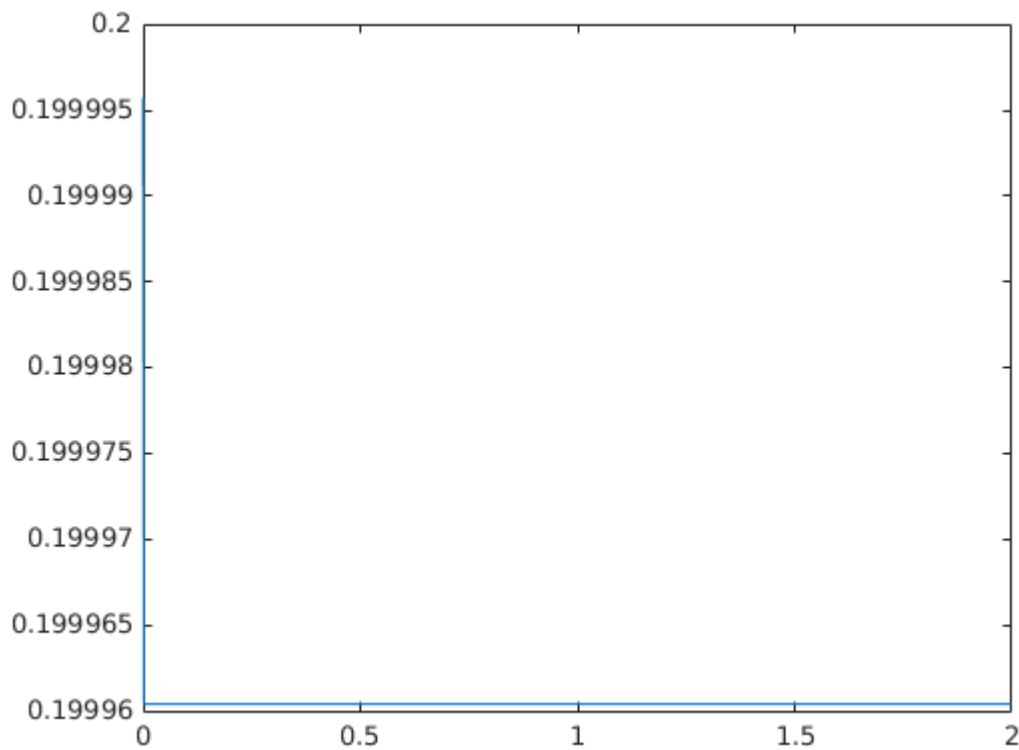
The simulation of the Differential Amplifier circuit can be seen below. Differential amplifiers amplifies the difference between the input voltages. For the selected values of resistors, the output of this circuit is 10 times larger than the difference between inputs. Resistors have the following values :  $R_1=10 \text{ k}\Omega$ ,  $R_2=100 \text{ k}\Omega$ ,  $R_3=10$

k $\Omega$  and R4=100 k $\Omega$ . Tolerance of each resistor is 1%. For the input voltage difference of 0.2 V, the output is 2 V.



## Running Model

```
% Code to plot simulation results from Differential amplifier
% Running model for the first time
model_name = 'Diff_ampl1';
open_system(model_name);
sim(model_name)
plot(logsout_diff_amp{1}.Values.Time, logsout_diff_amp{1}.Values.Data(:,1))
```



## Making Resistor Labels Visible

find\_system can find systems, blocks, lines, ports and returns the objects in the specified system that meet the specified criteria.

set\_param will set system and block parameter values

```
SETTING_PARAM=0;
if SETTING_PARAM
    blockNames = find_system( model_name , 'Type' , 'Block' );
    for k = 1 : length( blockNames )
        set_param( blockNames{k} , 'ShowName' , 'on' );
    end;
    set_param( 'Diff_ampl1/ERef Diff Amp1' , 'ShowName' , 'off' );
    set_param( 'Diff_ampl1/ERef Diff Amp' , 'ShowName' , 'off' );
end
```

## Maximum tolerance test

Running tests and getting results for the simulation with maximum tolerance considered.

```
% Get simulation results
% Max Tolerance
set_param( 'Diff_ampl1/R1' , 'enable_R_tol' , '3' );
```

```

set_param('Diff_ampl1/R2','enable_R_tol','2');
set_param('Diff_ampl1/R3','enable_R_tol','3');
set_param('Diff_ampl1/R4','enable_R_tol','2');
sim('Diff_ampl1');
simlog_prSensorMaxTol = logcout_diff_amp.get('Pr_Signal');

```

## Minimum tolerance test

Running tests and getting results for the simulation with minimum tolerance considered.

```

% Get simulation results
% Min Tolerance
set_param('Diff_ampl1/R1','enable_R_tol','2');
set_param('Diff_ampl1/R2','enable_R_tol','3');
set_param('Diff_ampl1/R3','enable_R_tol','2');
set_param('Diff_ampl1/R4','enable_R_tol','3');
sim('Diff_ampl1');
simlog_prSensorMinTol = logcout_diff_amp.get('Pr_Signal');

```

## Random tolerance

Generate random values of resistors assuming that their values follow the uniform distribution.

```
RANDOM_TOLERANCE=1
```

```
RANDOM_TOLERANCE = 1
```

```

if RANDOM_TOLERANCE
    for i=1:1000
        set_param('Diff_ampl1/R1','enable_R_tol','1'); % random tolerance
        set_param('Diff_ampl1/R2','enable_R_tol','1');
        set_param('Diff_ampl1/R3','enable_R_tol','1');
        set_param('Diff_ampl1/R4','enable_R_tol','1');
        set_param('Diff_ampl1/R1','tol_distribution','1'); %1 is uniform, 2 is Gaussian
        set_param('Diff_ampl1/R2','tol_distribution','1');
        set_param('Diff_ampl1/R3','tol_distribution','1');
        set_param('Diff_ampl1/R4','tol_distribution','1');
        sim('Diff_ampl1');
        simlog_param=logcout_diff_amp.get('Pr_Signal');
        param_mean(i)=mean(simlog_param.Values.Data(10:end,2));

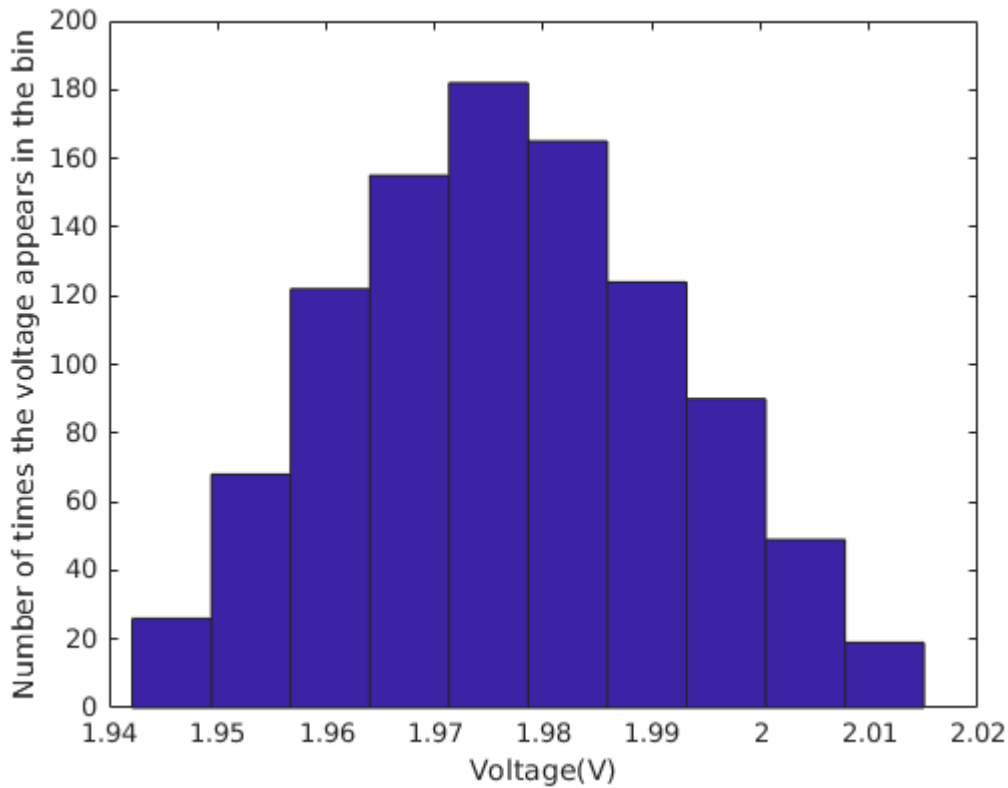
    end
    figure, histogram(param_mean,'Normalization','pdf')
    pd=fitdist(param_mean,'Normal');
    z1=1.94:0.001:2.02;
    y=pdf(pd,z1);
    hold on
    plot(z1,y)
    ci=paramci(pd,0.1) %0.05
    ci_percent=100*(ci(:,1)-2)/2

```

```

ylabel('Distribution of V_o')
xlabel('V_O(V)');
legend('Empirical distribution','Fitted normal distribution')
end

```



```

% Nominal Value
set_param('Diff_ampl1/R1','enable_R_tol','0');
set_param('Diff_ampl1/R2','enable_R_tol','0');
set_param('Diff_ampl1/R3','enable_R_tol','0');
set_param('Diff_ampl1/R4','enable_R_tol','0');

```

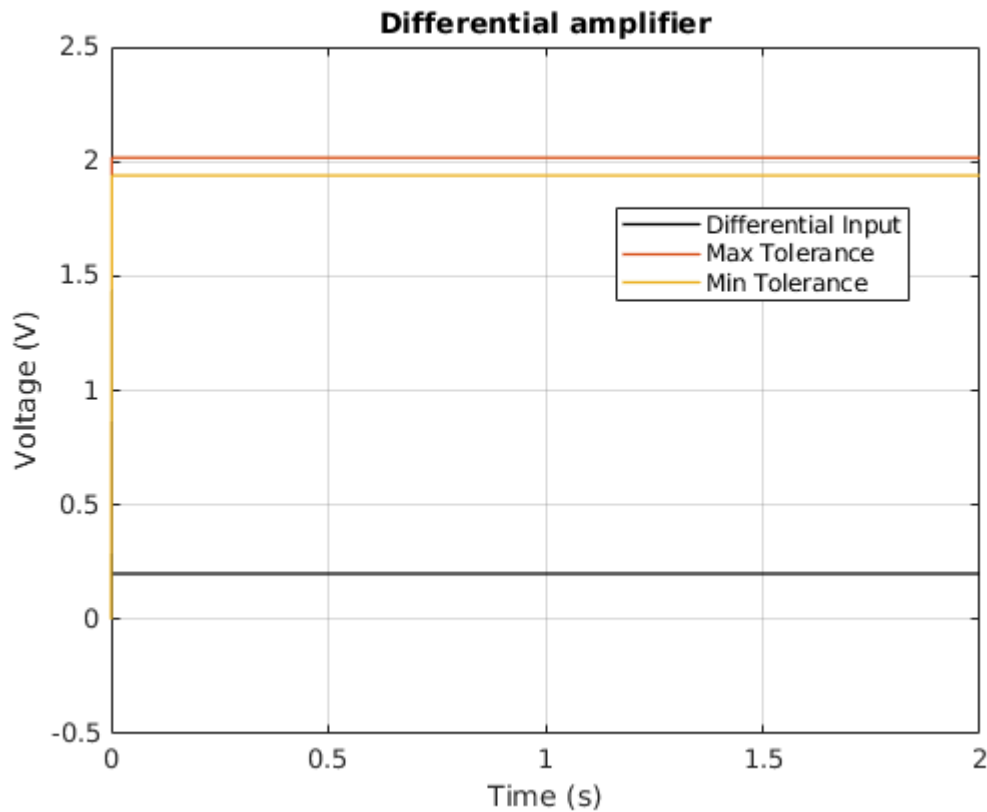
## Results

Final results for the differential input, maximum tolerance, and minimum tolerance will be plotted.

```

% Plot results
plot(simlog_prSensorMinTol.Values.Time, simlog_prSensorMinTol.Values.Data(:,1), 'k','LineWidth',2);
hold on
plot(simlog_prSensorMaxTol.Values.Time, simlog_prSensorMaxTol.Values.Data(:,2), 'b','LineWidth',2);
plot(simlog_prSensorMinTol.Values.Time, simlog_prSensorMinTol.Values.Data(:,2), 'r','LineWidth',2);
hold off
grid on
title('Differential amplifier')
ylabel('Voltage (V)')
legend({'Differential Input', 'Max Tolerance', 'Min Tolerance'}, 'Location', 'Best');
xlabel('Time (s)');

```



## Uncertainty analysis

`sdo.getParameterFromModel(modelname,paramname)` will creates an object from the Simulink model parameter that can be tuned to satisfy design requirements during optimization.

```
R1 = sdo.getParameterFromModel(model_name, 'R1');
% R1.Minimum=R1.Value*1.01;
% R1.Maximum=R1.Value*0.99;

R2 = sdo.getParameterFromModel(model_name, 'R2');
% R2.Minimum=R2.Value*1.01;
% R2.Maximum=R2.Value*0.99;

R3 = sdo.getParameterFromModel(model_name, 'R3');
% R3.Minimum=R3.Value*1.01;
% R3.Maximum=R3.Value*0.99;

R4 = sdo.getParameterFromModel(model_name, 'R4');
% R4.Minimum=R4.Value*1.01;
% R4.Maximum=R4.Value*0.99;

%V = sdo.getParameterFromModel(model_name, 'V');
% V.Minimum=V.Value*1.01;
% V.Maximum=V.Value*0.99;
```

## Identifying Type of Distribution

Distributions of uncertain parameters will be identified and if they are not specified, uniform distribution is considered.

```
v=[R1; R2; R3; R4];
ps = sdo.ParameterSpace(v);
%v=setDistribution(ps,'V',makedist('normal',V.Value, 0.005*V.Value));
R1=setDistribution(ps,'R1',makedist('normal',R1.Value, 0.005*R1.Value));
R2=setDistribution(ps,'R2',makedist('normal',R2.Value, 0.005*R2.Value));
R3=setDistribution(ps,'R3',makedist('normal',R3.Value, 0.005*R3.Value));
R4=setDistribution(ps,'R4',makedist('normal',R4.Value, 0.005*R4.Value));
```

## Generating Samples

1000 samples from the parameter space will be generated.

```
rng default; % for reproducibility
x = sdo.sample(ps, 500); % uniform sampling
%sdo.scatterPlot(x);
```

## Simulation Definition

Specify model signals to log during model simulation.

```
Simulator = sdo.SimulationTest('Diff_ampl1');

Sig_Info = Simulink.SimulationData.SignalLoggingInfo;
Sig_Info.BlockPath = 'Diff_ampl1/Meas 1';
Sig_Info.LoggingInfo.LoggingName = 'Sig';
Sig_Info.LoggingInfo.NameMode = 1;

Simulator.LoggingInfo.Signals = Sig_Info;
```

## Create Evaluation Objective Function

Create a function that is called for each combination of parameters being varied, to compute the cost.

Use an anonymous function with one argument that calls Diff\_ampl\_evalFcn.

```
% evalfcn = @(P) Diff_ampl_evalFcn(P,Simulator,Requirements);
evalfcn = @(P) ComputeOutput(P,Simulator);
```

## Evaluation Options

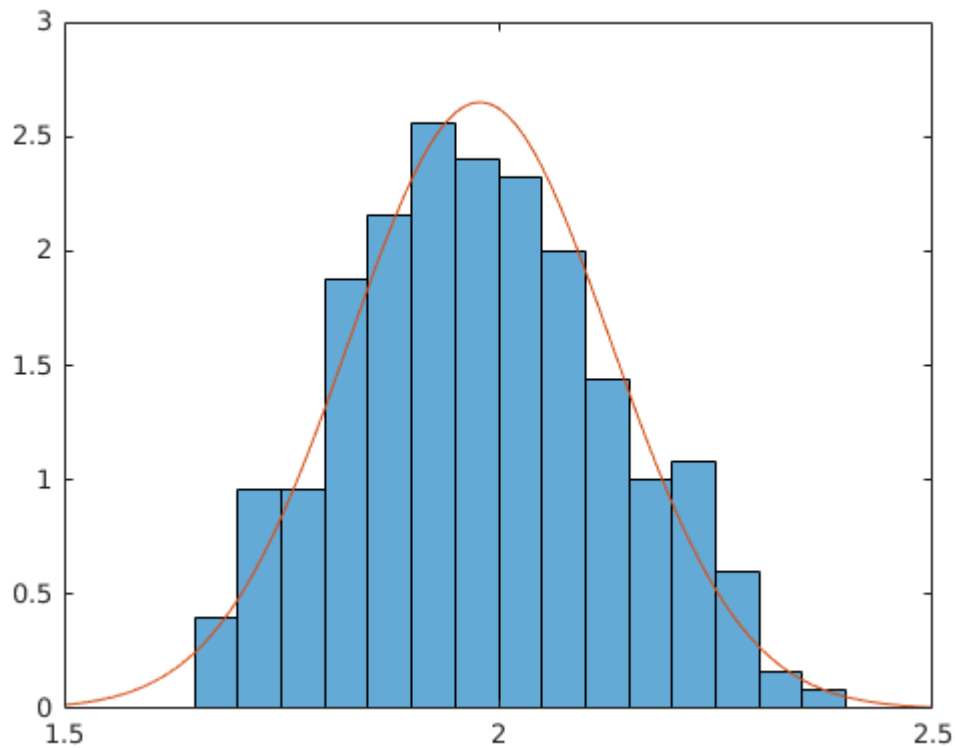
Specify evaluation options.

```
Options = sdo.EvaluateOptions;
Options.EvaluatedModel = Simulator;
```

## Compute the output of the Model

Call `sdo.evaluate` with the objective function handle, parameters to vary, parameter values, and options.

```
[EvalResult,Info] = sdo.evaluate(evalfcn,ps,x,Options);  
z=EvalResult.out;  
figure  
histogram(z,'Normalization','pdf')  
pd=fitdist(z,'Normal');  
z1=1.5:0.01:2.5;  
y=pdf(pd,z1);  
hold on  
plot(z1,y)
```



```
ci=paramci(pd,0.1);%0.05  
ci_percent=100*(ci(:,1)-2)/2;
```

-----

This function computes the mean at the output.

```
function Vals = ComputeOutput(P,Simulator)  
%DIFF_AMPL_EVALFCN  
%  
% Function called at each iteration of the evaluation problem.
```



```

%
% The function is called with a set of parameter values, P, and returns
% the evaluated cost, Vals.
%
% See the sdoExampleCostFunction function and sdo.evaluate for a more
% detailed description of the function signature.
%
% Simulate the model.
Simulator.Parameters = P;
Simulator = sim(Simulator);

% Retrieve logged signal data.
SimLog = find(Simulator.LoggedData,get_param('Diff_ampl1','SignalLoggingName'));
Sig_Log = find(SimLog,'Sig');

Vals.out=mean(Sig_Log.Values.Data(20:end));
end

```