Windkessel model

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This code was developed by Miodrag Bolic for the book PERVASIVE CARDIAC AND RESPIRATORY MONITORING DEVICES.

Introduction

The Windkessel model

The Windkessel model is an interpretative model that allows us to achieve the following:

Given the aortic flow and the parameters of the model, we can generate aortic and peripheral pressure signals.

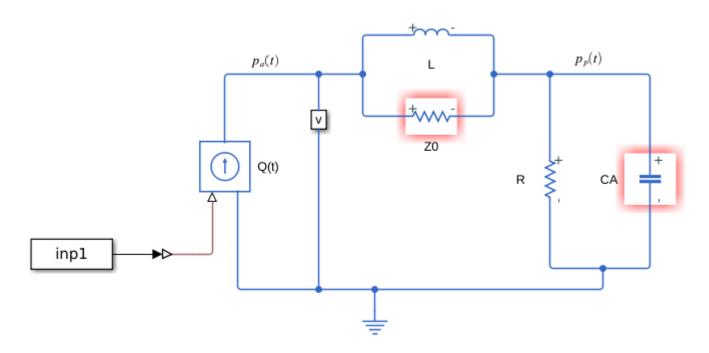
Given the aortic flow and the aortic pressure, we can estimate the values of parameters such as arterial compliance that have physiological meaning and can be interpreted.

The pressure plays the role of the voltage at different points and the blood flow of the current.

Parameters include:

- Z0 is the characteristic impedance of the artery
- R is the peripheral resistance
- CA is the arterial compliance which is the change in arterial blood volume (due to a given change in arterial blood pressure,

• L is the arterial inertance and it is defined as the change in pressure in the arterial segment versus the acceleration of the blood.

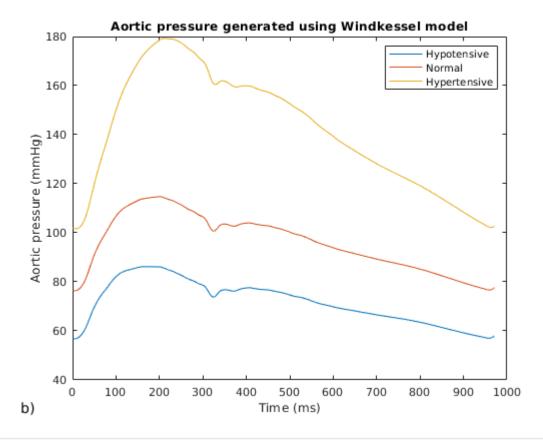


In this section Windkessel model will be presented.

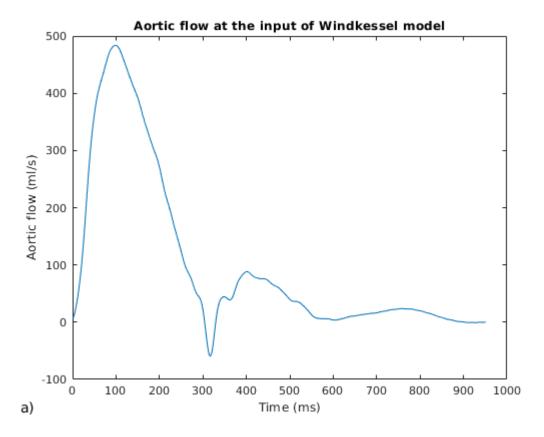
Forward modeling

```
% Modeling Case 1
load('data_17s.mat')
a=[];
fs=200;
src1=zeros(200,0);
global start_pulse_ind;
global end_pulse_ind;
start_pulse_ind=15800;
end_pulse_ind=16841;
%src1=240*ones(65,1);
inp1(:,2)=TFP(:,2); % flow
inp1(:,1)=TFP(:,1);
model_name = 'WK';
open_system(model_name)
param=[0.039 1.95 0.71 0.011; 0.043 1.5 0.95 0.015; 0.05 0.7 1.4 0.02];
%param=[3 2 0.6 0.005];
cases=['hypotensive', 'normotensive', 'hypertensive'];
figure
for level =1:3
    L = sdo.getParameterFromModel(model_name, 'L');
    L.Value=param(level,4);
    sdo.setValueInModel(model_name,L);
```

```
Z0 = sdo.getParameterFromModel(model name, 'Z0');
    Z0.Value=param(level,1);
    sdo.setValueInModel(model_name,Z0);
   R = sdo.getParameterFromModel(model_name, 'R');
   R. Value=param(level, 3);
    sdo.setValueInModel(model_name,R);
    CA = sdo.getParameterFromModel(model_name, 'CA');
    CA.Value=param(level,2);
    sdo.setValueInModel(model_name,CA);
    % Collect these parameters into a vector.
    v = [L Z0 R CA];
    simOut = sim(model_name, 'CaptureErrors', 'on');
    %figure
    %plot(simOut.simout.Time, simOut.simout.Data)
    plot(simOut.simout.Data(14000:14970))
   hold on
end
xlabel("Time (ms)")
ylabel("Aortic pressure (mmHg)")
legend({'Hypotensive', 'Normal', 'Hypertensive'})
title("Aortic pressure generated using Windkessel model")
annonation_save('b)', "Fig4.4b.jpg", SAVE_FLAG);
```



```
figure
plot(inp1(14000:14950,2))
xlabel("Time (ms)")
ylabel("Aortic flow (ml/s)")
title("Aortic flow at the input of Windkessel model")
annonation_save('a)', "Fig4.4a.jpg", SAVE_FLAG);
```



```
% hold on % plot()
```

Sensitivity analysis and fitting the model

In this section, we will load data that correspond to the flow and pressure of a hypotensive subject with low blood pressure. Then we will perform the following steps:

- 1. Sensitivity analysis to determine the initial values of the parameters for the estimation
- 2. Selection of parameters that need to be optimized.
- 3. Fitting the parameters of the model.
- 4. Determining the accuracy of the fitting since we already know the parameters for the hypotensive subject.

Sensitivity analysis

```
% Modeling Case 1 - hypotensive subject
% Sensitivity analysis
```

```
out(:,2)=TFP(:,3); % we can also ake the BP signal from the hypotensive subject above
out(:,1)=TFP(:,1);

[EvalResult, ParamValues, p] = sensitivityEvaluationWK(out)
```

ps =
 ParameterSpace with properties:

ParameterNames: {'Z0' 'CA' 'R' 'L'}

ParameterDistributions: [1×4 prob.UniformDistribution]

RankCorrelation: []

Options: [1x1 sdo.SampleOptions]

Notes: []

EvalResult = 100×1 table

	CustomReq
1	406.2856
2	1.5245e+04
3	3.5740e+03
4	1.1509e+03
5	3.1156e+03
6	7.3713e+03
7	103.7613
8	1.2459e+03
9	1.6702e+04
10	631.7304
11	3.4012e+03
12	1.4067e+04
13	4.1379e+03
14	4.3811e+03

ParamValues = 100×4 table

	Z0	CA	R	L
1	0.0365	1.8888	0.5146	0.0089
2	0.0484	1.5390	1.9386	0.0079
3	0.0533	2.2124	0.1244	0.0071
4	0.0396	0.9233	0.3962	0.0077
5	0.0496	0.7046	0.1711	0.0010
6	0.0124	2.1282	1.5687	0.0031
7	0.0206	2.0947	0.8075	0.0045
8	0.0309	0.8024	1.0483	0.0053
9	0.0135	0.5800	1.9814	0.0030

	Z0	CA	R	L
10	0.0746	1.3362	0.4713	0.0097
11	0.0256	1.5545	1.2854	0.0012
12	0.0696	0.5816	1.8808	0.0096
13	0.0781	1.7203	1.3466	0.0064
14	0.0765	0.5029	1.3375	0.0013

:

p(1,1) =

Name: 'Z0'
Value: 0.0500
Minimum: 0.0100
Maximum: 0.1000
Free: 1
Scale: 0.0625

Info: [1x1 struct]

p(2,1) =

Name: 'CA'
Value: 2
Minimum: 0.5000
Maximum: 3
Free: 1
Scale: 1

Info: [1x1 struct]

p(3,1) =

Name: 'R'
Value: 0.6000
Minimum: 0.1000
Maximum: 2
Free: 1
Scale: 2

Info: [1x1 struct]

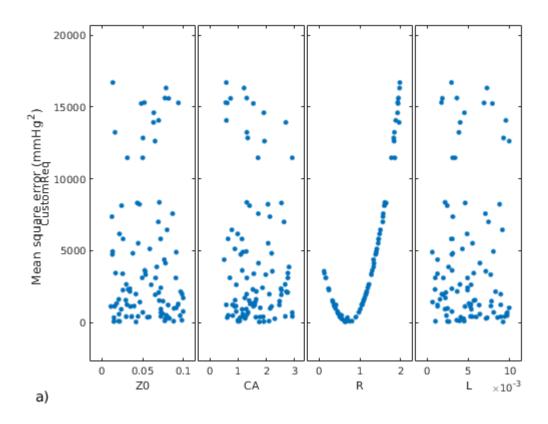
p(4,1) =

Name: 'L'
Value: 0.0050
Minimum: 5.0000e-04
Maximum: 0.0100
Free: 1
Scale: 0.0312
Info: [1x1 struct]

4x1 param.Continuous

lists of methods, superclasses

```
sdo.scatterPlot(ParamValues,EvalResult)
ylabel('Mean square error (mmHg^2)')
title("The scatter plot of mean square error vs. Windkessel parameters")
```



```
exportgraphics(gcf, "Fig4.5a.jpg", 'Resolution',600)
opts = sdo.AnalyzeOptions;
opts.Method = 'Correlation';
sensitivities = sdo.analyze(ParamValues, EvalResult, opts);
disp(sensitivities)
```

CustomReq

Z 0	-0.0040993
CA	-0.11084
R	0.81746
L	-0.0018477

Selection of parameters

```
[fval, idx_min] = min(EvalResult.CustomReq);
L.Value = ParamValues.L(idx_min);
Z0.Value = ParamValues.Z0(idx_min);
R.Value = ParamValues.R(idx_min);
CA.Value = ParamValues.CA(idx_min);
L.Minimum=L.Value/2;
L.Maximum=L.Value*1.5;
```

```
Z0.Minimum=Z0.Value/2;
Z0.Maximum=Z0.Value*1.5;

R.Minimum=R.Value/2;
R.Maximum=R.Value*1.5;

CA.Minimum=CA.Value/2;
CA.Maximum=CA.Value*1.5;
```

Optimization

```
% Selection of parameters from the sensitivity analysis to be used in the
% optimization
Exp = sdo.Experiment(model_name);
v = [L ZO R CA];
Exp = setEstimatedValues(Exp, v);  % use vector of parameters/states
Simulator = createSimulator(Exp);
% Simulator = sim(Simulator);
% Retrieve logged signal data.
% SimLog = find(Simulator.LoggedData,get_param('WK','SignalLoggingName'));
% Sig_Log = find(SimLog,'Sig');

opts = sdo.OptimizeOptions;
opts.Method = 'fmincon';
estFcn = @(v) WK_OptEvalFcn(v, Simulator, Exp,out);
vOpt = sdo.optimize(estFcn, v, opts);
```

Optimization started 14-Feb-2023 20:04:11

			max			First-order
Iter	F-count	f(x)	constrai	int	Step-size	optimality
0	9	46.7518	3	0		
1	21	26.3315)	0	0.241	1.42e+03
2	32	19.0406)	0	0.411	863
3	46	18.648	3	0	0.155	579
4	53	10.82	2	0	0.569	340
5	59	7.295)	0	0.447	110
6	70	4.43566)	0	0.363	363
7	78	2.69023	3	0	0.224	30.6
8	86	1.11433	3	0	0.19	35.7
9	94	0.657785)	0	0.0668	7.39
10	105	0.656918	3	0	0.0171	4.77
11	113	0.653798	3	0	0.00317	0.756
12	121	0.652268	3	0	0.00599	1.84
13	122	0.652268	3	0	0.000882	1.84
Local	minimum	possible. C	Constraints	sat	isfied.	

fmincon stopped because the size of the current step is less than the value of the step size tolerance and constraints are satisfied to within the value of the constraint tolerance.

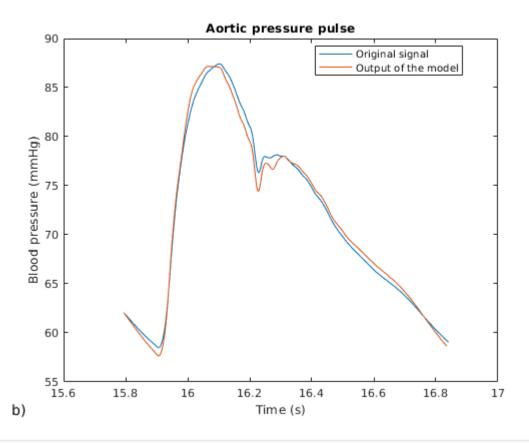
```
disp(vOpt)
```

```
Minimum: 0.0046
   Maximum: 0.0138
     Free: 1
    Scale: 0.0156
     Info: [1x1 struct]
(1,2) =
     Name: 'Z0'
    Value: 0.0386
   Minimum: 0.0209
   Maximum: 0.0628
     Free: 1
    Scale: 0.0625
     Info: [1x1 struct]
(1,3) =
     Name: 'R'
    Value: 0.7127
   Minimum: 0.3234
   Maximum: 0.9702
     Free: 1
    Scale: 1
     Info: [1x1 struct]
(1,4) =
     Name: 'CA'
    Value: 2.0364
   Minimum: 0.8742
   Maximum: 2.6226
     Free: 1
    Scale: 2
     Info: [1x1 struct]
1x4 param.Continuous
lists of methods, superclasses
%% Visualizing Result of Optimization
% Obtain the model response after estimation. Search for the
% model_residual signal in the logged simulation data.
Simulator = createSimulator(Exp);
Simulator = sim(Simulator);
plot(out(start_pulse_ind:end_pulse_ind,1), out(start_pulse_ind:end_pulse_ind,2))
hold on
```

(1,1) =

Name: 'L' Value: 0.0138

```
plot(Simulator.LoggedData.simout.Time(start_pulse_ind:end_pulse_ind), Simulator.LoggedI
xlabel('Time (s)');
ylabel('Blood pressure (mmHg)');
legend({'Original signal', 'Output of the model'},'Location','Best')
title("Aortic pressure pulse")
annonation_save('b)',"Fig4.5b.jpg", SAVE_FLAG);
```



```
function Vals = WK_OptEvalFcn(v,Simulator,Exp,out)
%WK_EVALFCN
%
% Function called at each iteration of the evaluation problem.
%
% The function is called with a set of parameter values, P, and returns
% the evaluated cost, Vals.
%
% See the sdoExampleCostFunction function and sdo.evaluate for a more
% detailed description of the function signature.
%
% Model Evaluation
%start_pulse_ind=15800;
%end_pulse_ind=16841;
global start_pulse_ind;
```

```
global end_pulse_ind;
% Simulate the model.
Exp = setEstimatedValues(Exp, v); % use vector of parameters/states
Simulator = createSimulator(Exp,Simulator);
Simulator = sim(Simulator);

% Retrieve logged signal data.
% SimLog = find(Simulator.LoggedData,get_param('WK','SignalLoggingName'));
% Sig_Log = find(SimLog,'PaSig');
PaSig=Simulator.LoggedData.simout.Data;
% Evaluate the design requirements.
Vals.F = mean((PaSig(start_pulse_ind:end_pulse_ind)-out(start_pulse_ind:end_pulse_ind,2)
end
```