Hendrix Programming Team Reference

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Limits

As a rule of thumb, you should assume about 10^8 (= 100 million) operations per second. If you can think of a straightforward brute force solution to a problem, you should check whether it is likely to fit within the time limit; if so, go for it! Some problems are explicitly written to see if you will recognize this. If a brute force solution won't fit, the input size can help guide you to search for the right algorithm running time.

Example: suppose a problem requires you to find the length of a shortest path in a weighted graph.

- If the graph has |V| = 400 vertices, you should use Floyd-Warshall: it is the easiest to code and takes $O(V^3)$ time which should be good enough.
- If the graph has |V| = 4000 vertices, especially if it doesn't have all possible edges, you can use Dijkstra's algorithm, which is $O(E \log V)$.
- If the graph has $|V| = 10^5$ vertices, you should look for some special property of the graph which allows you to solve the problem in O(V) or $O(V \log V)$ time—for example, perhaps the graph is a tree, so you can run DFS to find a unique path and then add up the weights. An input size of 10⁵ is a common sign that you are expected to use an $O(n \lg n)$ or O(n) algorithm—it's big enough to make $O(n^2)$ too slow but not so big that the time to do I/O makes a big difference.

\overline{n}	Worst running time	Example
11	O(n!)	Generating all permutations (§9.4, page 27)
25	$O(2^n)$	Generating all subsets (§10, page 29)
100	$O(n^4)$	Some brute force algorithms
400	$O(n^3)$	Floyd-Warshall (§5.6, page 17)
10^{4}	$O(n^2)$	Testing all pairs
10^{6}	$O(n \lg n)$	BFS/DFS; sort+greedy

- bing, transportationplanning, dancerecital, prozor, rectanglesurrounding, weakvertices
- $2^{10} = 1024 \approx 10^3$
- One int is 32 bits = 4 bytes. So an array of 10⁶ ints requires < 4 MB—typical memory limit is 1 GB.
- $2 \cdot 10^9$ fits in a 32-bit int.
- $9 \cdot 10^{18}$ fits in a 64-bit long.
- If you need larger values, use BigInteger (§2.11, page 9) or just use Python (§13, page 35); see Combinatorics (§9.4, page 27).

Java Reference

2.1 Template

```
import java.util.*;
import java.math.*;

public class ClassName {
    public static void main(String[] args) {
        Scanner in = new Scanner(System.in);

        // Solution code here

        System.out.println(answer);
    }
}
```

2.2 Scanner

Scanner is relatively slow but should usually be sufficient for most purposes. If the input or output is relatively large (> 1MB) and you suspect the time taken to read or write it may be a hindrance, you can use Fast I/O (§2.14, page 9).

```
// Read a whole line up to the next newline character.
// Consumes the newline but does not include it in the
// returned String.
String line = in.nextLine();

// Read until end of input
while (in.hasNext()) {
    line = in.nextLine();
}
}
```

2.3 String

The String type can be used in Java to represent sequences of characters.

[TODO: Useful String methods: concatenation, substring, charAt, ...?] [TODO: Converting between String and char[], advantages and disadvantages of each]

battlesimulation, bing, connectthedots, itsasecret, shiritori, suffixarrayreconstruction

2.4 Arrays

[TODO: Basic array template/examples.]

falcondive, freefood, traveltheskies

2.5 ArrayList

[TODO: Basic template and examples. Useful ArrayList methods: add, get, set. Advantages/disadvantages compared to arrays.]

2.6 Stack

[TODO: Example using Stack class.] [TODO: Mention balanced parentheses, DFS]

backspace, islands, pairingsocks, reservoir, restaurant, throwns, zagrade

2.7 Queue

[TODO: Queue interface, ArrayDeque class]

brexit, coconut, ferryloading4, shuffling

2.8 PriorityQueue

[TODO: Examples of using PriorityQueue. Show how to construct with custom Comparator, eg. using lambda notation] [TODO: Note lack of decreaseKey operation (Dijkstra), use remove + add, not as fast]



bank, guessthedatastructure, knigsoftheforest

2.9 Set

[TODO: HashSet, TreeSet]

2.10 Map

[TODO: HashMap, TreeMap]

2.11 BigInteger

[TODO: Examples. Useful methods, constructors (gcd, mod, base conversion!).]



basicremains

2.12 Sorting

[TODO: Basic template for implementing Comparable] [TODO: Arrays.sort, Collections.sort] [TODO: Include code for basic sorting implementations (in case it's useful to code them up explicitly so they can be enhanced with extra info): insertion sort, mergesort, quicksort)]

2.13 BitSet

[TODO: Basic examples of BitSet use.]



primesieve

2.14 Fast I/O

Typically ACM ICPC problems are designed so Scanner and System.out.println are fast enough to read and write the required input and output within the time limits. However, these are relatively slow since they are unbuffered (every single read and write happens immediately). Occasionally it can be useful to have faster I/O; indeed, some problems on Kattis cannot be solved in Java without using this. [TODO: Link to some examples.]

Be sure to call flush() at the end of your program or else some output might be lost!

```
/* Example usage:

*
    * Kattio io = new Kattio(System.in, System.out);

*
    * while (io.hasMoreTokens()) {
    * int n = io.getInt();
    * double d = io.getDouble();
    * double ans = d*n;

*
    * io.println("Answer: " + ans);
    * }
```

```
* io.flush(); // DON'T FORGET THIS LINE!
import java.util.StringTokenizer;
import java.io.BufferedReader;
import java.io.BufferedOutputStream;
import java.io.IOException;
import java.io.InputStream;
import java.io.InputStreamReader;
import java.io.PrintWriter;
import java.io.OutputStream;
class Kattio extends PrintWriter {
   public Kattio(InputStream i) {
        super(new BufferedOutputStream(System.out));
        r = new BufferedReader(new InputStreamReader(i));
   }
   public Kattio(InputStream i, OutputStream o) {
        super(new BufferedOutputStream(o));
       r = new BufferedReader(new InputStreamReader(i));
   public boolean hasMoreTokens() {
        return peekToken() != null;
   public int getInt() {
        return Integer.parseInt(nextToken());
   }
   public double getDouble() {
        return Double.parseDouble(nextToken());
   public long getLong() {
        return Long.parseLong(nextToken());
   }
   public String getWord() {
       return nextToken();
   private BufferedReader r;
   private String line;
   private StringTokenizer st;
   private String token;
   private String peekToken() {
        if (token == null)
            try {
                while (st == null || !st.hasMoreTokens()) {
                    line = r.readLine();
                    if (line == null) return null;
```

```
st = new StringTokenizer(line);
}
token = st.nextToken();
} catch (IOException e) { }
return token;
}

private String nextToken() {
   String ans = peekToken();
   token = null;
   return ans;
}
```

Data Structures

3.1 Union-find

A union-find structure can be used to keep track of a collection of disjoint sets, with the ability to quickly test whether two items are in the same set, and to quickly union two given sets into one. It is used in Kruskal's Minimum Spanning Tree algorithm (§5.7, page 17), and can also be useful on its own. find and union both take essentially constant amortized time.

drivingrange, islandhopping, kastenlauf, lostmap, minspantree, numbersetseasy, treehouses, unionfind, virtualfriends, wheresmyinternet

```
class UnionFind {
    private byte[] r; private int[] p; // rank, parent
    // Make a new union-find structure with n items in singleton sets,
    // numbered 0 .. n-1 .
    public UnionFind(int n) {
        r = new byte[n]; p = new int[n];
        for (int i = 0; i < n; i++) {
            r[i] = 0; p[i] = i;
    }
    // Return the root of the set containing v, with path compression. O(1).
    // Test whether u and v are in the same set with find(u) == find(v).
    public int find(int v) {
        return v == p[v] ? v : (p[v] = find(p[v]));
    // Union the sets containing u and v. O(1).
    public void union(int u, int v) {
        int ru = find(u), rv = find(v);
        if (ru != rv) {
                    (r[ru] > r[rv]) p[rv] = ru;
            else if (r[rv] > r[ru]) p[ru] = rv;
            else { p[ru] = rv; r[rv]++; }
        }
    }
}
```

- 3.2 Heaps
- 3.3 Tries
 - **3** boggle, heritage, phonelist
- 3.4 Red-black trees
- 3.5 Segment trees
- 3.6 Fenwick trees

Search

4.0.1 Complete search

[TODO: Complete search aka brute force]

4.0.2 Binary and ternary search

[TODO: Binary search on an array; binary search on unbounded function on the integers; binary search on real interval; ternary search]

Graphs

5.1 Useful graph theory

[TODO: characterization of trees.]

5.2 Representation

[TODO: Adjacency matrix, adjacency maps. Edge objects. Implicit graphs.]

5.3 BFS

[TODO: Code for BFS with level labelling, parent map.]



5.4 DFS, SCCs, topological sorting

[TODO: Code for DFS, start/finish labelling, top sorting, Tarjan's SCC algorithm]

- 5.5 Single-source shortest paths (Dijkstra)
- 5.6 All-pairs shortest paths (Floyd-Warshall)
- 5.7 Min spanning tree (Kruskal)

5.8 Max flow

A flow network is a directed, weighted graph where the edge weights (typically integers) are thought of as representing capacities (e.g. imagine pipes of varying sizes). The max flow problem is to determine, given a flow network, the maximum possible amount of flow which can move through the network between given source and sink vertices, subject to the constraints that the flow on any edge is no greater than the capacity, and the sum of incoming flows equals outgoing flows at every vertex other than the source or sink. Flow networks can be used to model a wide variety of problems.

[TODO: Enumerate a few problem types: item assignment; max bipartite matching; min cut]

[TODO: choose directed/undirected edges carefully!]

[TODO: Requires vertices $0 \dots n-1$: either carefully keep track of which numbers are for which vertices, or use lookup tables]

5.8. MAX FLOW CHAPTER 5. GRAPHS

 \odot copsandrobbers, escapeplan, gopher2, guardianofdecency, marblestree, maxflow, mincut, paintball, waif

Dinitz' Algorithm is probably the best all-around algorithm to use for solving max flow problems in competitive programming. It takes $O(V^2E)$ in theory (although is often much faster in practice). In the special case where we are modelling a bipartite matching problem, Dinitz' Algorithm reduces to the Hopcroft-Karp algorithm which runs in $O(E\sqrt{V})$.

```
class FlowNetwork {
    private static final int INF = ~(1<<31);</pre>
    int[] level;
    boolean[] pruned;
    HashMap<Integer, HashMap<Integer, Edge>> adj;
    public FlowNetwork(int n) {
        level = new int[n];
        pruned = new boolean[n];
        adj = new HashMap<>();
        for (int i = 0; i < n; i++)
            adj.put(i, new HashMap<>());
    }
    public void addDirEdge(int u, int v, long cap) {
        if (adj.get(u).containsKey(v)) {
            adj.get(u).get(v).capacity = cap;
        } else {
            Edge e = new Edge(u, v, cap);
            Edge r = new Edge(v,u,0);
            e.setRev(r);
            adj.get(u).put(v, e);
            adj.get(v).put(u, r);
        }
    }
    // Add an UNdirected edge u<->v with a given capacity
    public void addEdge(int u, int v, long cap) {
        Edge e = new Edge(u, v, cap);
        Edge r = new Edge(v,u,cap);
        e.setRev(r);
        adj.get(u).put(v, e);
        adj.get(v).put(u, r);
    }
    public long maxFlow(int s, int t) {
        if (s == t) return INF;
        else {
            long totalFlow = 0;
            while (bfs(s,t)) totalFlow += sendFlow(s,t);
            return totalFlow;
    }
    private long sendFlow(int s, int t) {
```

CHAPTER 5. GRAPHS 5.8. MAX FLOW

```
for (int i = 0; i < pruned.length; i++)</pre>
                                pruned[i] = false;
                     return sendFlowR(s, t, INF);
          }
          private long sendFlowR(int s, int t, long availableFlow) {
                      if (s == t) return availableFlow;
                     long sentFlow = 0;
                      for (Edge e : adj.get(s).values()) {
                                  if \ (e.remainingCapacity() > 0 \ \&\& \ !pruned[e.to] \ \&\& \ level[e.to] == level[s] \ + \ 1) \ \{ \ level[e.to] \ + \ 1) \ \{ \ 
                                           long flow = sendFlowR(e.to, t, Math.min(availableFlow, e.remainingCapacity()));
                                            availableFlow -= flow; sentFlow += flow;
                                            e.flow += flow; e.rev.flow -= flow;
                                            if (availableFlow == 0) break;
                      }
                      if (sentFlow == 0) pruned[s] = true;
                     return sentFlow;
          private boolean bfs(int s, int t) {
                      for (int i = 0; i < level.length; i++) level[i] = -1;</pre>
                     Queue<Integer> q = new ArrayDeque<>();
                     q.add(s); level[s] = 0;
                      while (!q.isEmpty()) {
                                 int cur = q.remove();
                                 for (Edge e : adj.get(cur).values()) {
                                            if (e.remainingCapacity() > 0 && level[e.to] == -1) {
                                                      level[e.to] = level[cur]+1;
                                                      q.add(e.to);
                                 }
                     return level[t] >= 0;
          }
}
class Edge {
          int from, to;
          long capacity, flow;
          Edge rev;
          public Edge(int from, int to, long cap) {
                      this.from = from; this.to = to; this.capacity = cap; this.flow = 0;
          public void setRev(Edge rev) { this.rev = rev; rev.rev = this; }
          public long remainingCapacity() { return capacity - flow; }
```

[TODO: Include a sample solution using a flow network]

5.9 Miscellaneous

[TODO: New virtual source/sink node trick]

Dynamic Programming

Strings

7.1 Suffix arrays

Divide & Conquer

Counting inversions 8.1



excursion, froshweek

Mathematics

- 9.1 GCD/Euclidean Algorithm
- 9.2 Fractions
- 9.3 Primes and factorization

[TODO: Basic primality testing and factorization with trial division. Sieving (primes, factors, Euler totient).]

9.4 Combinatorics

[TODO: Basic principles of combinatorics. Code for computing binomial coefficients.] [TODO: mod $10^9 + 7$.]

Remember to use long if you need an answer $mod(10^9 + 7)$ (which would fit in an int) but computing the answer requires $multiplying \mod(10^9 + 7)$.

[TODO: Heap's Algorithm for generating all permutations. See Bit Tricks for generating all subsets.] [TODO: PIE?]

Bit Tricks

[TODO: Basic bit manipulation. Using bitstrings to compactly represent sets/states. Iterating through all subsets with counter.]

[TODO: BitSet instead of array of booleans.]

Geometry

Miscellaneous

12.1 Range queries

[TODO: Monoid vs group] [TODO: Prefix sum trick] [TODO: 2D prefix sum trick with PIE] [TODO: Kadena's Algorithm for max subsequence sum] [TODO: Segment trees, Fenwick trees]

12.2 2D grids

[TODO: Discussion of implicit graphs] [TODO: Formulas for converting between pair of coordinates and single index] [TODO: Trick for listing neighbors with delta vector]

Python

Python's built-in support for arbitrary-size integers (using BigInteger in Java is a pain!) and built-in dictionaries with lightweight syntax make it attractive for certain kinds of problems.

Below is a basic template showing how to read typical contest problem input in Python:

```
import sys

if __name__ == '__main__':

    n = int(sys.stdin.readline())  # Read an int on a line by itself
    for _ in range(n):  # Do something n times

        # Read all the ints on a line into a list
        xs = map(int, sys.stdin.readline().split())

        # Read a known number of ints into variables
        p, q, r, y = map(int, sys.stdin.readline().split())
```

[TODO: Mention basic Python data structures such as set, deque, list methods]