# Homework 8

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### Exercise 1: .

How many strings are there of four lower case letters that have the letter x in them?

Number of strings of length  $4 = 26^4$ 

Number of strings of length 4 other than  $x = 25^4$ 

Thus, the answer is  $26^4 - 25^4 = 66351$  strings.

# Exercise 2: .

How many strings of four decimal digits

a) do not contains the same digit twice?

$$10 * 9 * 8 * 7 = 5040$$

b)End with an even digit?

$$10^3 * 5 = 5000$$

c) Have exactly three digits that are 9s?

$$9*4 = 36$$

#### Exercise 3: .

How many license plates can be made using either three digits followed by three letters, or three letters followed by three digits?

$$9^3 * 26^3 + 26^3 * 9^3 = 2(26^3 * 9^3) = 25625808$$

#### Exercise 4: .

How many subsets of a set with 100 elements have more than one element?

All of the subset  $= 2^{100}$ 

The sub set has less than one element = 100 + 1

Thus, the answer is  $2^{100} - 100 - 1$ .

# Exercise 5: .

How many bit strings of length 10 contain either five consecutive 0s or five consecutive 1s?

let's consider 5 consecutive 1s first:

if it start at position 1, remaining digits can be both 1 and 0:  $2^5 = 32$ 

if it start at position k=2,3,4,5,6, the number at position k-1 must be o, or it will be in previous cases:  $5*2^4$ 

So the total number is  $2^5 + 5 * 2^4 = 112$ 

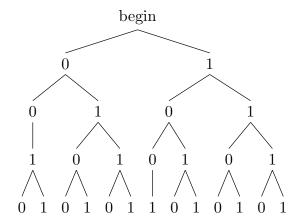
5 consecutive 0s is similar as 5 consecutive 1s, so we get another 112.

because we count 0000011111 and 1111100000 twice, we should subtract 2 from the answer.

Thus the final answer is 112 \* 2 - 2 = 222

#### Exercise 6: .

Use a tree diagram to find the number of bit strings of length four with no three consecutive 0s.



So there are 13 strings of length four with no three consecutive 0s.

## Exercise 7: .

Form a group of 13 men, 8 women, 2 boys and 4 girls.

(a) How many ways can a man, a woman, a boy and a girl be selected?

$$13 * 8 * 2 * 4 = 832$$

(b) How many ways can a male and a female be selected?

$$(13+2)*(8+4) = 180$$

(c) How many ways can a person be selected?

$$13 + 8 + 2 + 4 = 27$$

## Exercise 8: Extra Credit

How many numbers in the range 100-999 have no repeated digits? (For example, 110 and 211 have repeated 1, while 101 is OK)

$$9*9*9 = 729$$

Now how many of them are even? (be careful!).

if the first digit is even, the second is odd

$$4*5*5 = 100$$

if the first digit is even, the second is even

$$4 * 4 * 4 = 64$$

if the first digit is odd, the second is odd

$$5*4*5 = 100$$

if the first digit is odd, the second is even

$$5*5*4 = 100$$

So the total number is 100 + 64 + 100 + 100 = 364