

# Application Design Using Java

Lecture 22

# SQL Injection



- Code injection technique that might destroy your database
- One of the most common Web hacking techniques
- Malicious code placed in SQL statements via Web page input
- Prevention
  - Limit permissions of the MySQL user used by the application to access the database
  - Input validation, don't trust any user input
    - Regular expressions as whitelists for structured data
    - For fixed sets of values (drop-down lists, radio buttons, etc.), determine which value is returned. The input data should match one of the offered options exactly.
  - SQL parameters
  - Stored procedures
  - Use character-escaping functions for user-supplied input

# SQL Injection Examples

- Getting access to the entire table, all rows and columns. Imagine it were a table with all users, their passwords, etc.

Executed the following SQL statement:

SELECT airport, city, country, latitude, longitude FROM advjava.airports WHERE country = "" or ""="" AND city = "" or ""=""

Enter country:

" or ""=""

Enter city:

" or ""=""

Find

Search results for country: " or ""="" and city: " or ""=""

Airport	City	Country	Latitude	Longitude
Goroka Airport	Goroka	Papua New Guinea	-6.081888634590001	145.301988291
Madang Airport	Madang	Papua New Guinea	-5.20707988739	145.789001465
Mount Hagen Kagamuga Airport	Mount Hagen	Papua New Guinea	-5.826789855957031	144.29600524902344
Nadzab Airport	Nadzab	Papua New Guinea	-6.569803	146.725977
Port Moresby Jacksons International Airport	Port Moresby	Papua New Guinea	-9.443300355834961	147.22000122070312
Wewak International Airport	Wewak	Papua New Guinea	-3.58383011818	143.660000348
Narsarsuaq Airport	Narsarsuaq	Greenland	61.1804995728	-45.4259986877
Godthaab / Nuuk Airport	Godthaab	Greenland	64.19090271	-51.6781005859
Kangerlussuaq Airport	Søndrestrøm	Greenland	67.0122218982	-50.7119031047
Thule Air Base	Thule	Greenland	76.5311965942	-68.7032012939
Akureyri Airport	Akureyri	Iceland	65.66000366210938	-18.0727005048828
Egilsstaðir Airport	Egilsstaðir	Iceland	65.2833023071289	-14.401399612426758
Hermðingur Airport	Hefn	Iceland	64.295601	-15.2272
Húsavík Airport	Húsavík	Iceland	65.952301	-17.428001
Ísafjörður Airport	Ísafjörður	Iceland	66.05809783635547	-23.13529982617198
Keflavík International Airport	Keflavík	Iceland	63.985000610352	-22.665600357056
Patrekjörður Airport	Patrekjörður	Iceland	65.555801	-23.965
Reykjavík Airport	Reykjavík	Iceland	64.1299972534	-21.9405994415
Siglufjörður Airport	Siglufjörður	Iceland	66.133301	-18.8167
Vestmannaeyjar Airport	Vestmannaeyjar	Iceland	63.42430114740094	-20.27890014684375
Sault Ste Marie Airport	Sault Ste Marie	Canada	46.48500061035156	-84.5083964140625
Winnipeg / St. Andrews Airport	Winnipeg	Canada	50.0564002991	-97.03250122070001
Halifax / CFB Shearwater Heliport	Halifax	Canada	44.6387018433	-63.489401062499994
St. Anthony Airport	St. Anthony	Canada	51.3918991089	-58.083099365200006

- Deleting the table.

Executed the following SQL statement:

SELECT airport, city, country, latitude, longitude FROM advjava.airports WHERE country = "" or ""="" AND city = "" or ""=";  
DROP TABLE `airports`;-- "

Enter country:

" or ""=""

Enter city:

" or ""="; DROP TABLE `airports`;-- "

Find

Search results for country: " or ""="" and city: " or ""="; DROP TABLE `airports`;-- "

Airport	City	Country	Latitude	Longitude
---------	------	---------	----------	-----------

SELECT \* FROM `airports`;

159 13:49:39 SELECT \* FROM `airports` LIMIT 0-1000  
SELECT \* FROM `airports`

Error Code: 1146. Table 'advjava.airports' doesn't exist

# SQL Injection Eliminated

The image displays a side-by-side comparison of Java code in an IDE, illustrating the removal of a SQL injection vulnerability. The left pane shows the original code, which concatenates user input into a SQL query. The right pane shows the patched code, which uses `PreparedStatement` and `setString` to safely handle user input. Below the code, a browser window shows the search results for a specific country and city.

**Original Code (Left Pane):**

```
String url = node.get("MySQLConnection",
"jdbc:mysql://localhost:3306/advjava?allowMultiQueries=true&useSSL=false");

Connection con = null;
StringBuffer resultTable = new StringBuffer(
"<table><tr><th>Airport</th><th>City</th><th>Country</th>" +
"<th>Latitude</th><th>Longitude</th></tr>"
);

try
{
    con = DriverManager.getConnection(url);
    String query = "SELECT airport, city, country, latitude, longitude " +
        "FROM advjava.airports WHERE country = \"" + country + "\" " +
        "AND city = \"" + city + "\"";
    try (Statement stat = con.createStatement()) {
        boolean res = stat.execute(query);
        if (res) {
            try (ResultSet rs = stat.getResultSet()) {
                System.out.println("Executed the following SQL statement:");
                System.out.println(query);
                while (rs.next()) {
                    resultTable.append("<tr><td>").append(rs.getString(1)).
                        append("</td><td>").append(rs.getString("city")).
                        append("</td><td>").append(rs.getString(3)).
                        append("</td><td>").append(rs.getDouble(4)).
                        append("</td><td>").append(rs.getDouble(5)).
                        append("</td></tr>");
                }
            }
        }
    }
    resultTable.append("</table>");
}
```

**Patched Code (Right Pane):**

```
String url = node.get("MySQLConnection",
"jdbc:mysql://localhost:3306/advjava?useSSL=false");

Connection con = null;
StringBuffer resultTable = new StringBuffer(
"<table><tr><th>Airport</th><th>City</th><th>Country</th>" +
"<th>Latitude</th><th>Longitude</th></tr>"
);

try
{
    con = DriverManager.getConnection(url);
    String query = "SELECT airport, city, country, latitude, longitude " +
        "FROM advjava.airports WHERE country = ? AND city = ?";

    try (PreparedStatement stat = con.prepareStatement(query)) {
        stat.setString(1, country);
        stat.setString(2, city);
        try (ResultSet rs = stat.executeQuery()) {
            System.out.println("Executed the following SQL statement:");
            System.out.println(query);
            while (rs.next()) {
                resultTable.append("<tr><td>").append(rs.getString(1)).
                    append("</td><td>").append(rs.getString("city")).
                    append("</td><td>").append(rs.getString(3)).
                    append("</td><td>").append(rs.getDouble(4)).
                    append("</td><td>").append(rs.getDouble(5)).
                    append("</td></tr>");
            }
        }
    }
    resultTable.append("</table>");
}
```

**Search results for country: " or ""=" and city: " or ""="**

id	airport	city	country	iata	icao	latitude	longitude	elevation
1	Goroka Airport	Goroka	Papua New Guinea	GKA	AYGA	-6.081689834590001	145.391998291	5282
2	Madang Airport	Madang	Papua New Guinea	MAG	AYMD	-5.20707988739	145.789001465	20
3	Mount Hagen Kagamuga Airport	Mount Hagen	Papua New Guinea	HGU	AYMH	-5.826789855957031	144.29600524902344	5388
4	Nadzab Airport	Nadzab	Papua New Guinea	LAE	AYNZ	-6.569803	146.725977	239
5	Port Moresby Jacksons International Airport	Port Moresby	Papua New Guinea	POM	AYPY	-9.443380355834961	147.22000122070312	146
6	Wewak International Airport	Wewak	Papua New Guinea	WWK	AYWK	-3.58383011818	143.669006348	19
7	Narsarsuaq Airport	Narsarsuaq	Greenland	UAK	BGBW	61.1604995728	-45.4259986877	112
8	Godthaab / Nuuk Airport	Godthaab	Greenland	GOH	BGGH	64.19090271	-51.6781005859	283
9	Kangerlussuaq Airport	Sondrestrom	Greenland	SFJ	BGSF	67.0122218992	-50.7116031647	165
10	Thule Air Base	Thule	Greenland	THU	BGTL	76.5311965942	-68.7032012939	251

# Designing Database Schema

The screenshot displays the MySQL Workbench interface for designing a database schema. The main window shows an EER Diagram with two tables: **Vendors** and **Products**. The **Vendors** table has columns: **vendor\_id** (INT, Primary Key), **name** (VARCHAR(255)), and **address** (VARCHAR(255)). The **Products** table has columns: **prod\_id** (INT, Primary Key), **name** (VARCHAR(255)), **color** (VARCHAR(45)), and **vendor** (INT). A foreign key relationship is established between the **vendor** column in the **Products** table and the **vendor\_id** column in the **Vendors** table, with a 1:1 cardinality.

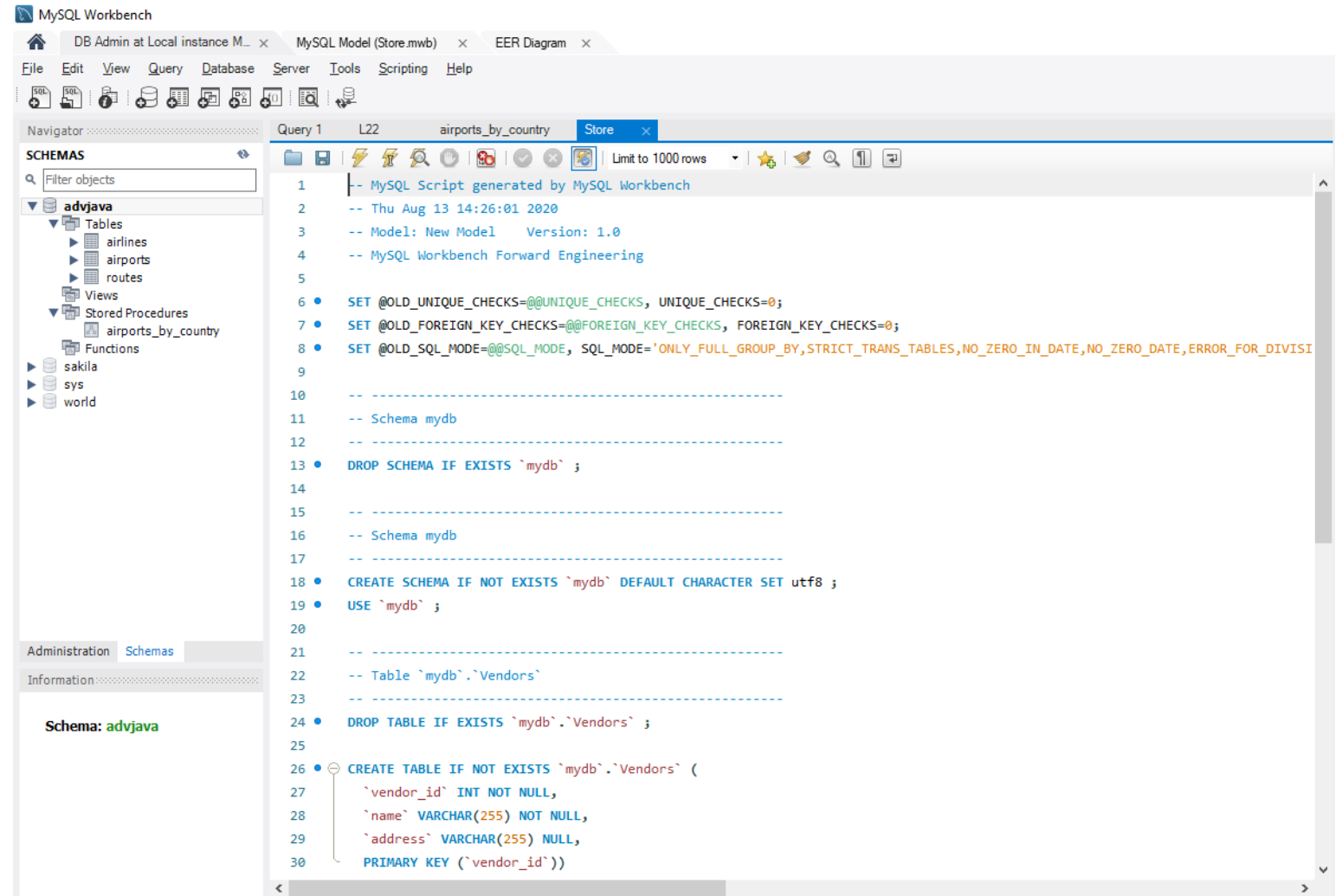
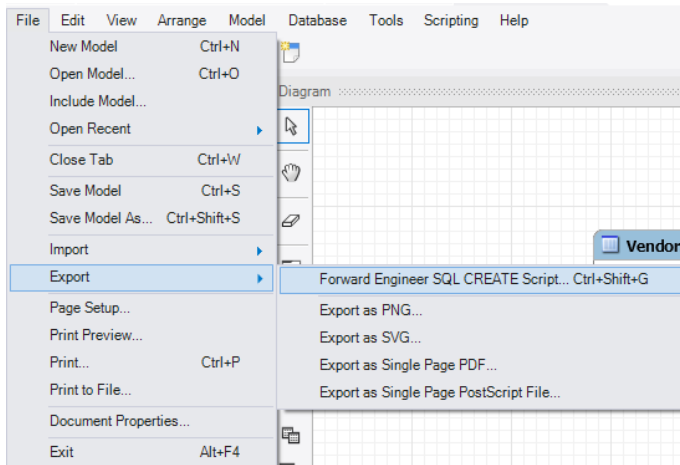
The **Products** table structure is detailed in the table structure view below:

Column Name	Datatype	PK	NN	UQ	B	UN	ZF	AI	G	Default/Expression
prod_id	INT	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	
name	VARCHAR(255)	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	
color	VARCHAR(45)	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	
vendor	INT	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	

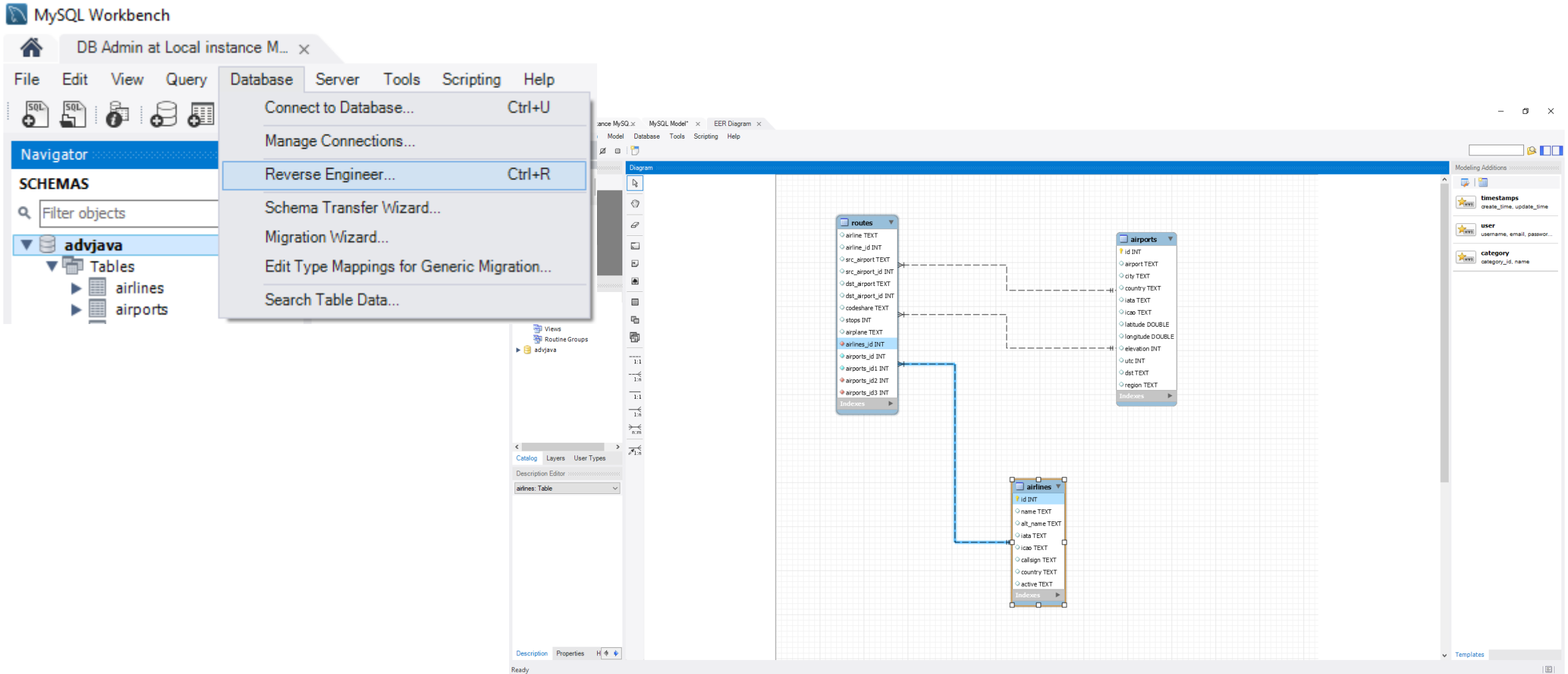
The **Products** table properties are configured as follows:

- Column Name: **vendor**
- Data Type: **INT**
- CharSet/Collation: **Default Charset**
- Comments: (Empty)
- Storage: ☐ Virtual, ☐ Stored
- Primary Key: ☐ (Not checked)
- Not Null: ☒ (Checked)
- Unique: ☐ (Not checked)
- Binary: ☐ (Not checked)
- Unsigned: ☐ (Not checked)
- Zero Fill: ☐ (Not checked)
- Auto Increment: ☐ (Not checked)
- Generated: ☐ (Not checked)

# Creating Database from Model



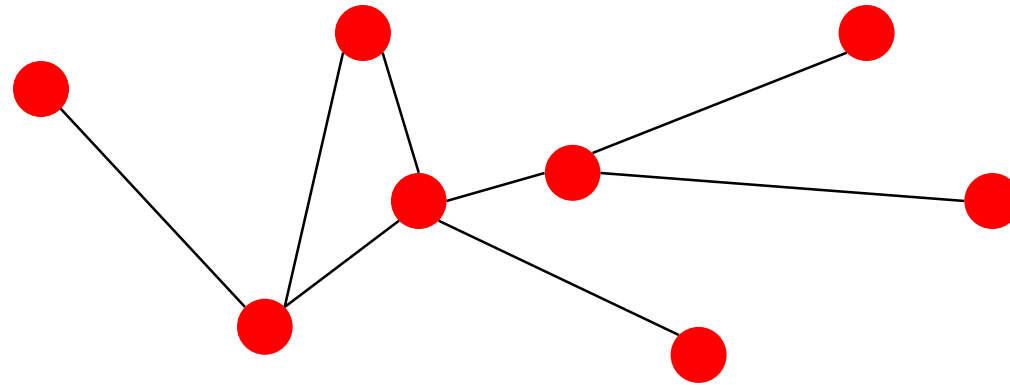
# Reverse Engineering a Database



# Networks and graphs



# COMPONENTS OF A COMPLEX SYSTEM



▪ **components:** nodes, vertices

$N$

▪ **interactions:** links, edges

$L$

▪ **system:** network, graph

$(N,L)$

## NETWORKS OR GRAPHS?

***network*** often refers to real systems

- www,
- social network
- metabolic network.

Language: (Network, node, link)

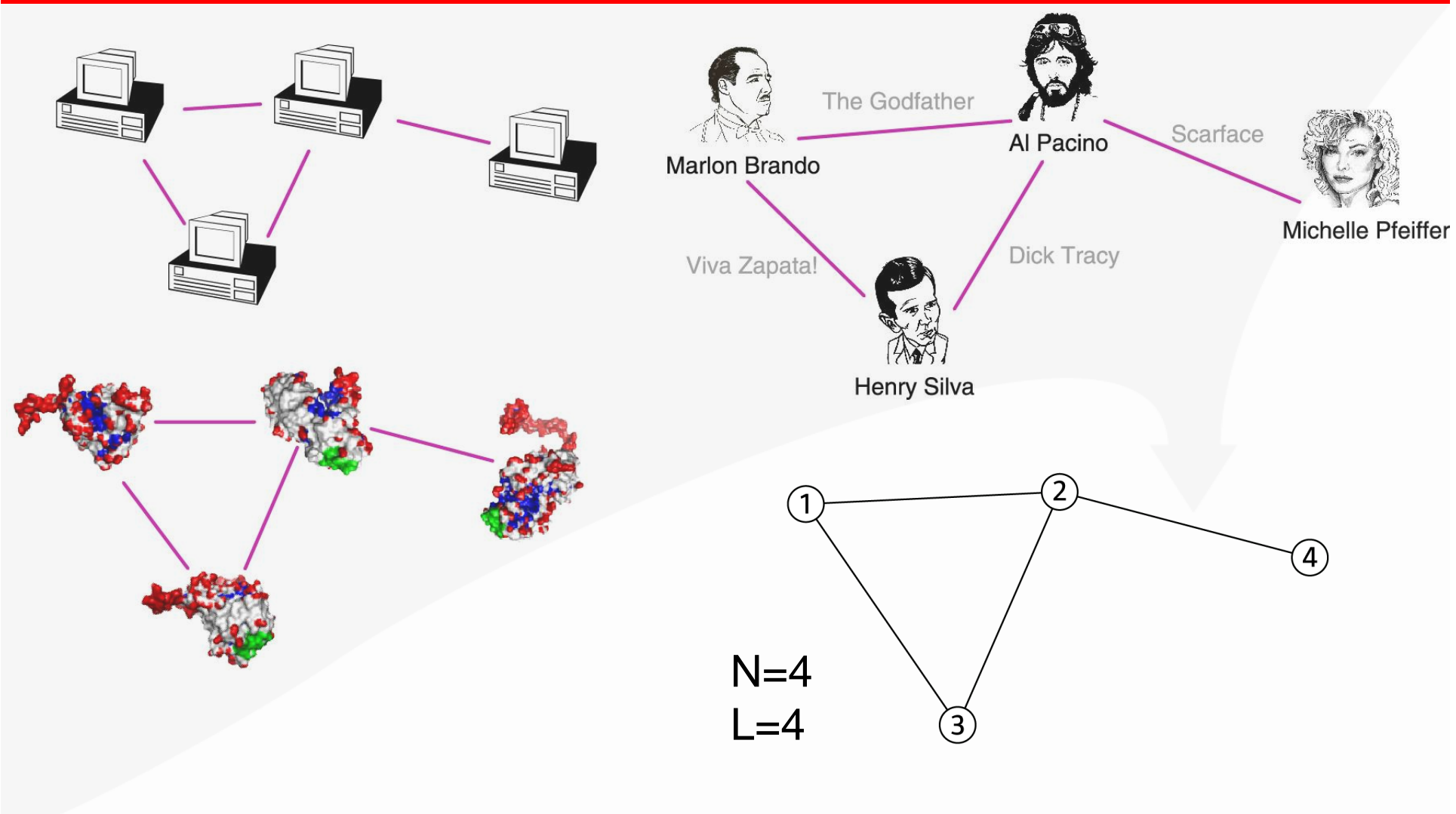
***graph***: mathematical representation of a network

- web graph,
- social graph (a Facebook term)

Language: (Graph, vertex, edge)

We will try to make this distinction whenever it is appropriate, but in most cases we will use the two terms interchangeably.

# A COMMON LANGUAGE



## CHOOSING A PROPER REPRESENTATION

The choice of the proper network representation determines our ability to use network theory successfully.

In some cases there is a unique, unambiguous representation. In other cases, the representation is by no means unique.

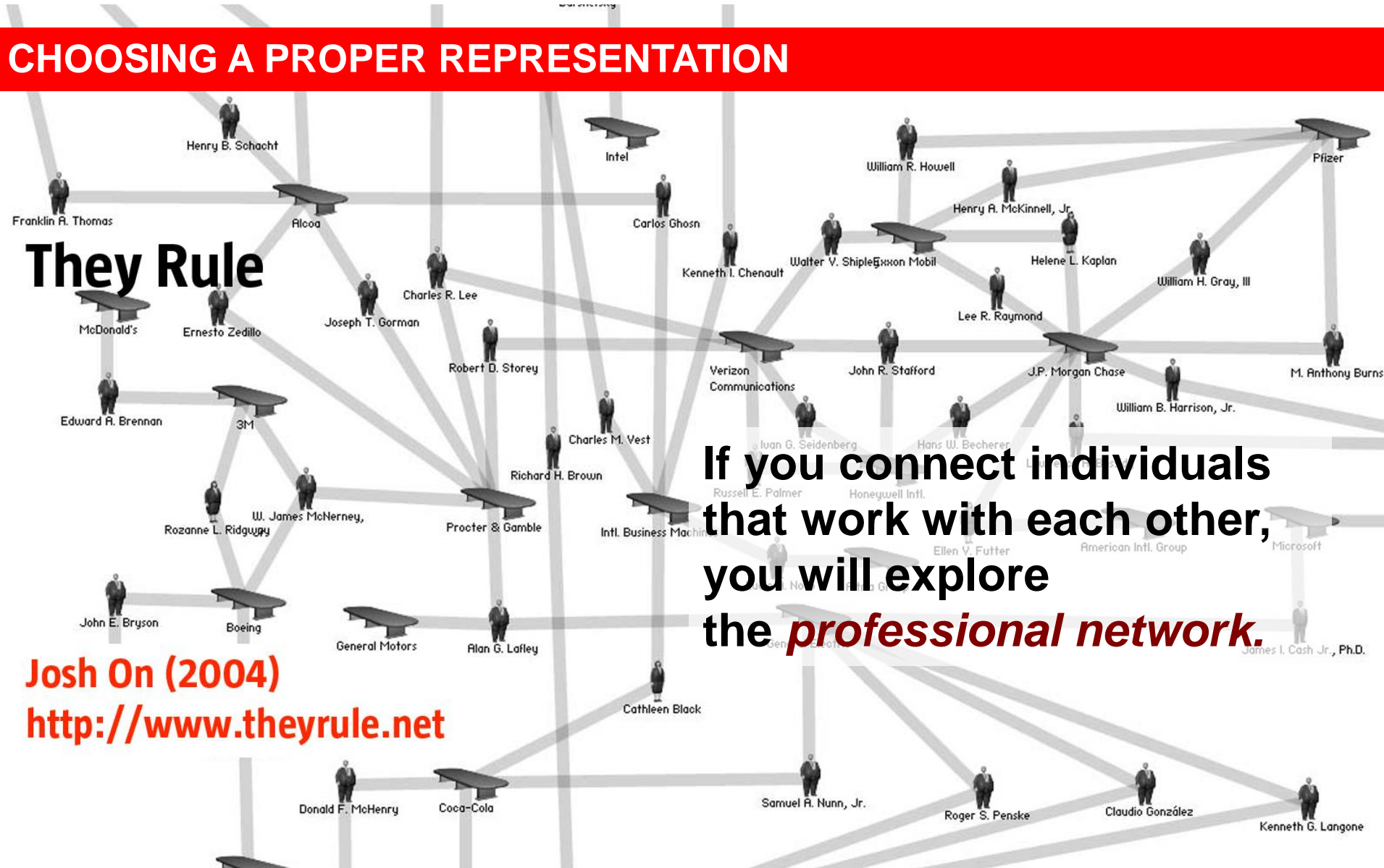
For example, the way we assign the links between a group of individuals will determine the nature of the question we can study.

## CHOOSING A PROPER REPRESENTATION

**They Rule**

Josh On (2004)  
<http://www.theyrule.net>

If you connect individuals  
that work with each other,  
you will explore  
the *professional network*.



## CHOOSING A PROPER REPRESENTATION

### The structure of adolescent romantic and sexual networks

If you connect those that have a romantic and sexual relationship, you will be exploring the *sexual networks*.

**Bearman PS, Moody J, Stovel K.**

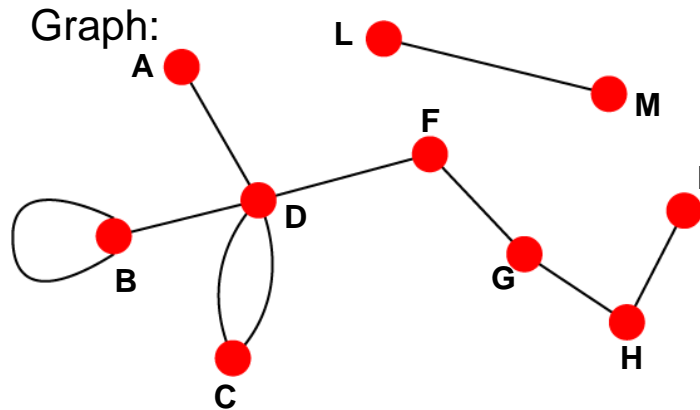
Institute for Social and Economic Research and Policy - Columbia University

<http://researchnews.osu.edu/archive/chainspix.htm>

# UNDIRECTED VS. DIRECTED NETWORKS

## Undirected

Links: undirected (*symmetrical*)



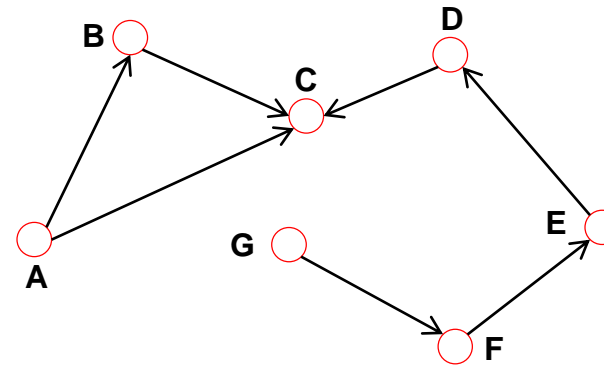
### Undirected links :

coauthorship links  
Actor network  
protein interactions

## Directed

Links: directed (*arcs*).

Digraph = directed graph:



*An undirected link is the superposition of two opposite directed links.*

### Directed links :

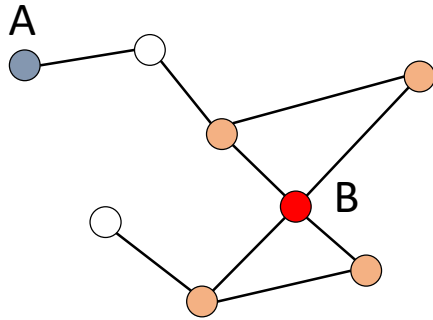
URLs on the www  
phone calls  
metabolic reactions

# Degree, Average Degree and Degree Distribution



## NODE DEGREES

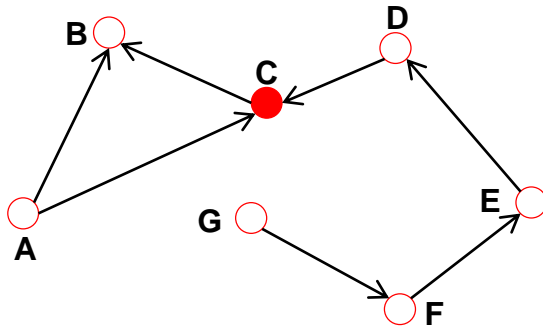
Undirected



Node degree: the number of links connected to the node.

$$k_A = 1 \quad k_B = 4$$

Directed



In *directed networks* we can define an **in-degree** and **out-degree**.

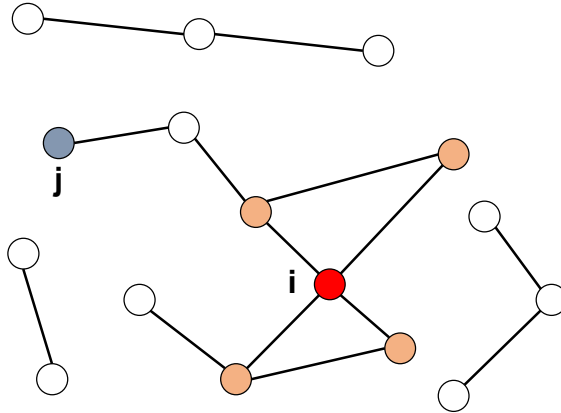
The (total) degree is the sum of in- and out-degree.

$$k_C^{in} = 2 \quad k_C^{out} = 1 \quad k_C = 3$$

**Source**: a node with  $k^{in} = 0$ ; **Sink**: a node with  $k^{out} = 0$ .

## AVERAGE DEGREE

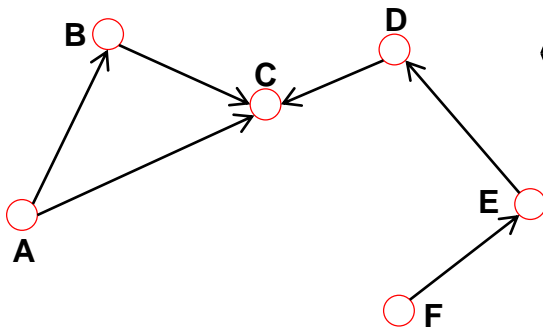
Undirected



$$\langle k \rangle \equiv \frac{1}{N} \sum_{i=1}^N k_i \quad \langle k \rangle = \frac{2L}{N}$$

N – the number of nodes in the graph

Directed



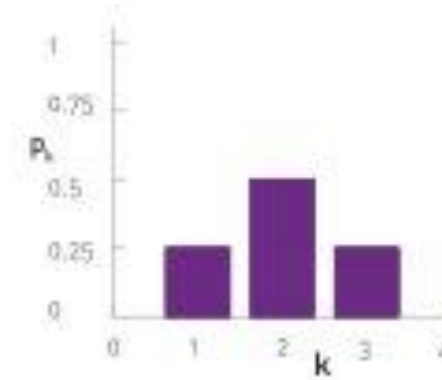
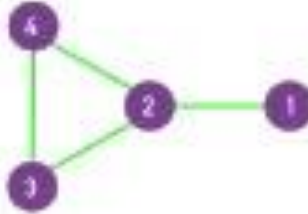
$$\langle k^{in} \rangle \equiv \frac{1}{N} \sum_{i=1}^N k_i^{in}, \quad \langle k^{out} \rangle \equiv \frac{1}{N} \sum_{i=1}^N k_i^{out}, \quad \langle k^{in} \rangle = \langle k^{out} \rangle$$

$$\langle k \rangle = \frac{L}{N}$$

# DEGREE DISTRIBUTION

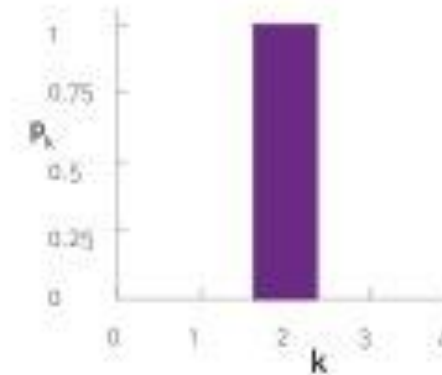
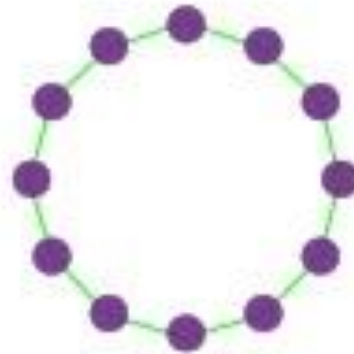
## Degree distribution

$P(k)$ : probability that a randomly chosen node has degree  $k$



$N_k$  = # nodes with degree  $k$

$P(k) = N_k / N$      plot



# DEGREE DISTRIBUTION

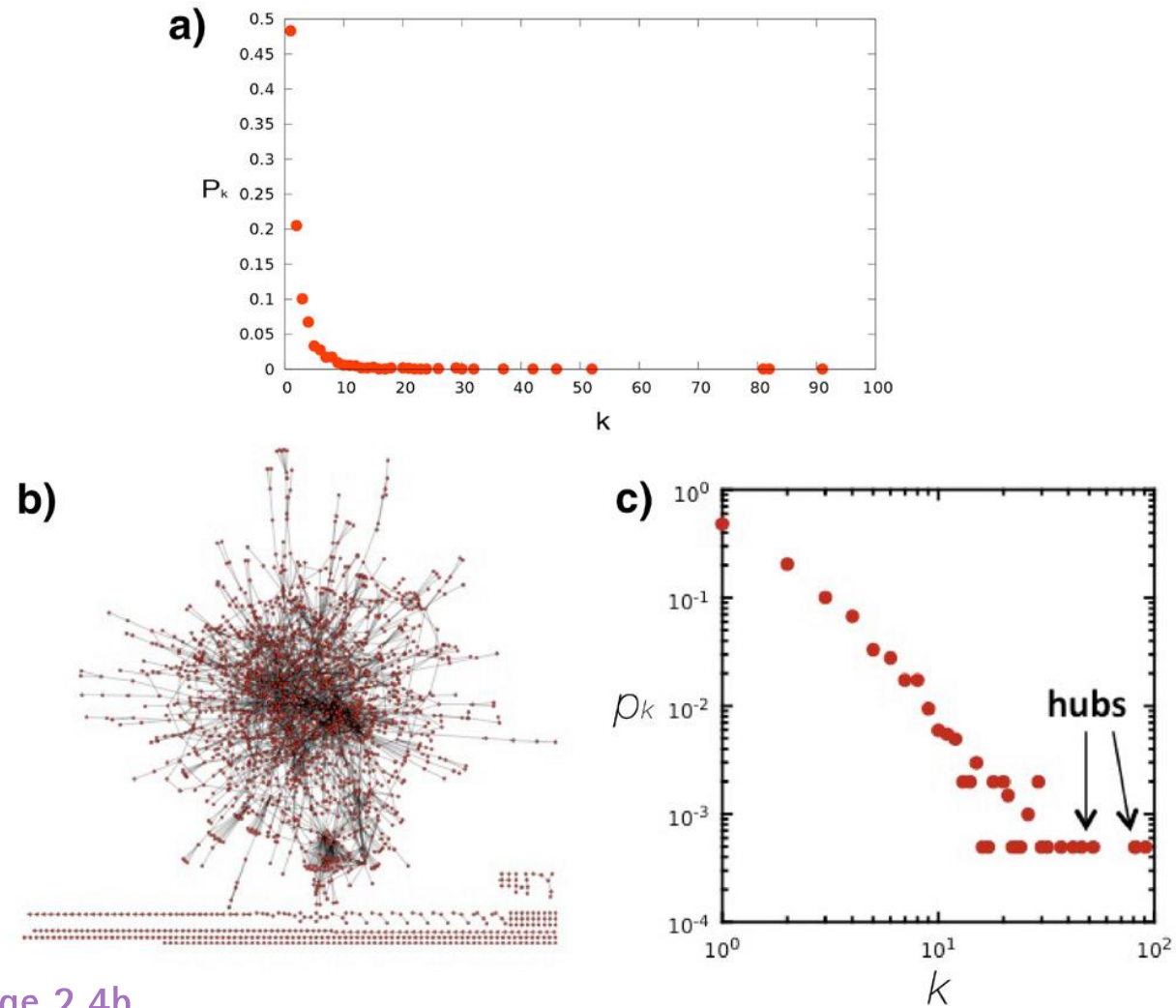
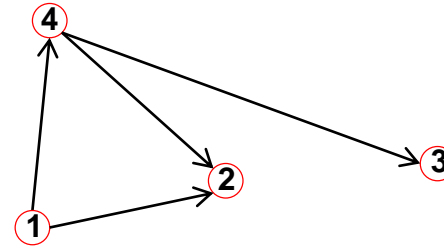
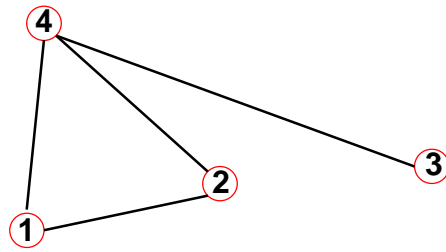


Image 2.4b

# Adjacency matrix

# ADJACENCY MATRIX



$A_{ij}=1$  if there is a link between node  $i$  and  $j$

$A_{ij}=0$  if nodes  $i$  and  $j$  are not connected to each other.

$$A_{ij} = \begin{pmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix} \quad A_{ij} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{pmatrix}$$

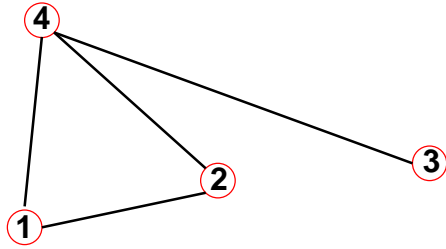
Note that for a directed graph (right) the matrix is not symmetric.

$A_{ij} = 1$  if there is a link pointing from node  $j$  and  $i$

$A_{ij} = 0$  if there is no link pointing from  $j$  to  $i$ .

# ADJACENCY MATRIX AND NODE DEGREES

Undirected



$$A_{ij} = \begin{pmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$$

$$A_{ij} = A_{ji}$$

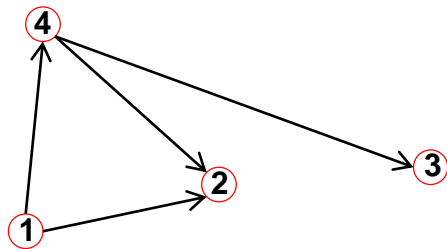
$$A_{ii} = 0$$

$$k_i = \sum_{j=1}^N A_{ij}$$

$$k_j = \sum_{i=1}^N A_{ij}$$

$$L = \frac{1}{2} \sum_{i=1}^N k_i = \frac{1}{2} \sum_{ij} A_{ij}$$

Directed



$$A_{ij} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{pmatrix}$$

$$A_{ij} \neq A_{ji}$$

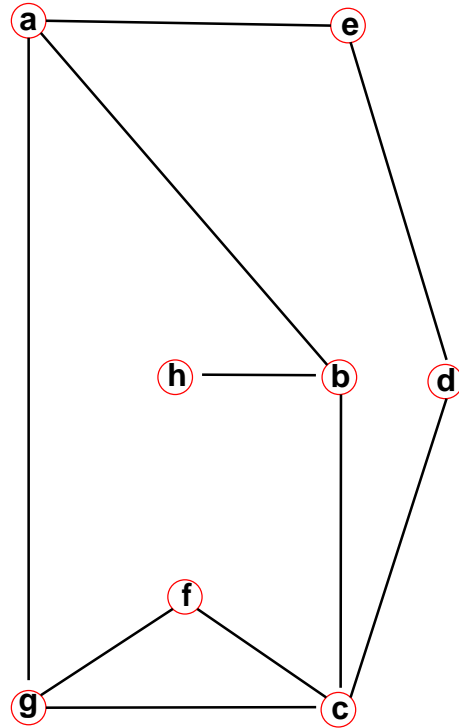
$$A_{ii} = 0$$

$$k_i^{in} = \sum_{j=1}^N A_{ij}$$

$$k_j^{out} = \sum_{i=1}^N A_{ij}$$

$$L = \sum_{i=1}^N k_i^{in} = \sum_{j=1}^N k_j^{out} = \sum_{i,j} A_{ij}$$

# ADJACENCY MATRIX



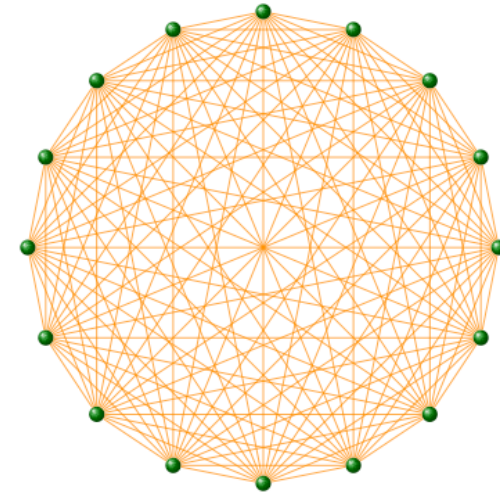
	a	b	c	d	e	f	g	h
a	0	1	0	0	1	0	1	0
b	1	0	1	0	0	0	0	1
c	0	1	0	1	0	1	1	0
d	0	0	1	0	1	0	0	0
e	1	0	0	1	0	0	0	0
f	0	0	1	0	0	0	1	0
g	1	0	1	0	0	0	0	0
h	0	1	0	0	0	0	0	0



Real networks are sparse

## COMPLETE GRAPH

The maximum number of links a network of N nodes can have is:  $L_{\max} = \binom{N}{2} = \frac{N(N-1)}{2}$



A graph with degree  $L=L_{\max}$  is called a **complete graph**, and its average degree is  $\langle k \rangle = N-1$

## REAL NETWORKS ARE SPARSE

**Most networks observed in real systems are sparse:**

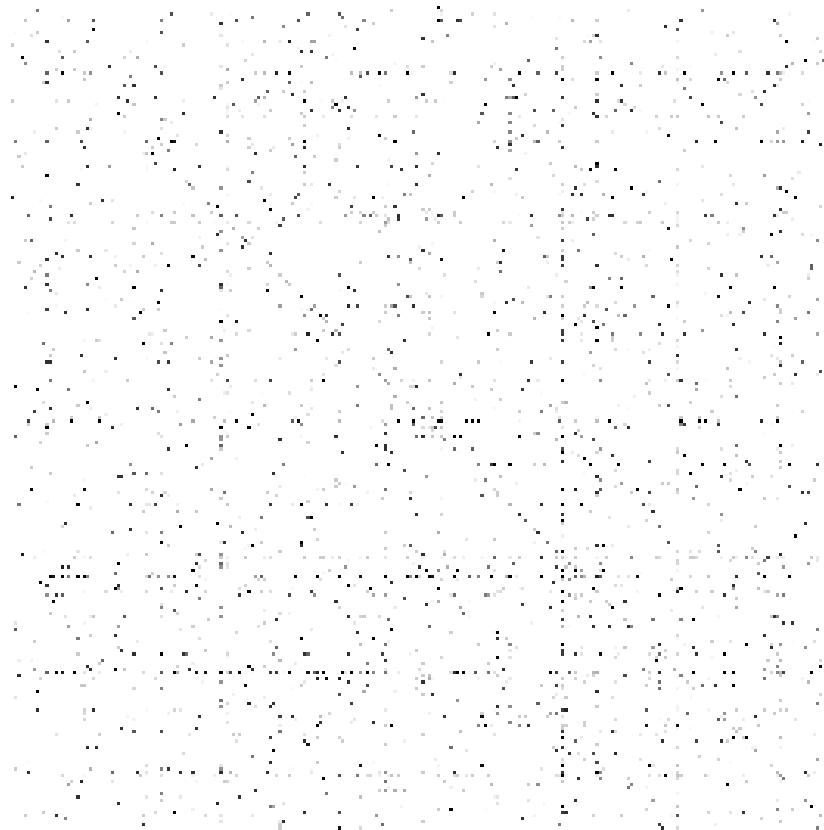
$$L \ll L_{\max}$$

or

$$\langle k \rangle \ll N-1.$$

WWW (ND Sample): $\langle k \rangle = 4.51$	$N = 325,729;$	$L = 1.4 \cdot 10^6$	$L_{\max} = 10^{12}$
Protein ( <i>S. Cerevisiae</i> ): $\langle k \rangle = 2.39$	$N = 1,870;$	$L = 4,470$	$L_{\max} = 10^7$
Coauthorship (Math): $\langle k \rangle = 3.9$	$N = 70,975;$	$L = 2 \cdot 10^5$	$L_{\max} = 3 \cdot 10^{10}$
Movie Actors: $L_{\max} = 1.8 \cdot 10^{13}$	$N = 212,250;$ $\langle k \rangle = 28.78$	$L = 6 \cdot 10^6$	

## ADJACENCY MATRICES ARE SPARSE

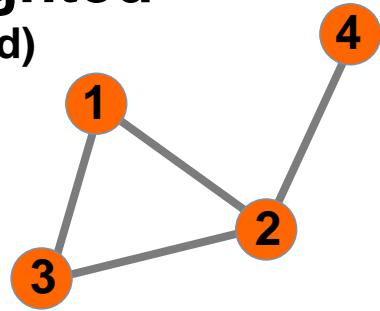


# WEIGHTED AND UNWEIGHTED NETWORKS

## WEIGHTED AND UNWEIGHTED NETWORKS

$$A_{ij} = w_{ij}$$

## Unweighted (undirected)



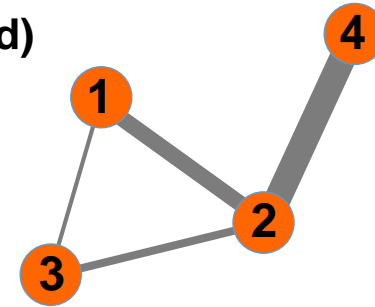
$$A_{ij} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$A_{ii} = 0 \quad A_{ij} = A_{ji}$$

$$L = \frac{1}{2} \sum_{i,j=1}^N A_{ij} \quad \langle k \rangle = \frac{2L}{N}$$

protein-protein interactions, [www](http://www)

## Weighted (undirected)



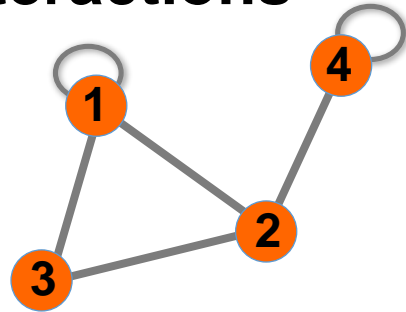
$$A_{ij} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 2 & 0.5 & 0 \\ 2 & 0 & 1 & 4 \\ 0.5 & 1 & 0 & 0 \\ 0 & 4 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$A_{ii} = 0 \quad A_{ij} = A_{ji}$$

$$L = \frac{1}{2} \sum_{i,j=1}^N \text{nonzero}(A_{ij}) \quad \langle k \rangle = \frac{2L}{N}$$

Call Graph, metabolic networks

## Self-interactions

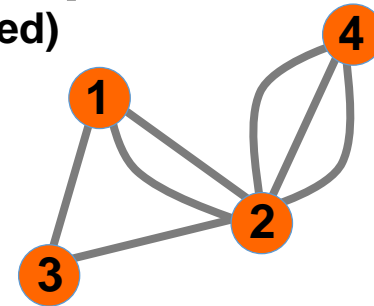


$$A_{ij} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix} \end{matrix}$$

$$L = \frac{1}{2} \sum_{i,j=1, i \neq j}^N A_{ij} + \sum_{i=1}^N A_{ii} \quad A_{ij} = A_{ji} \quad ?$$

Protein interaction network, [www](http://www)

## Multigraph (undirected)



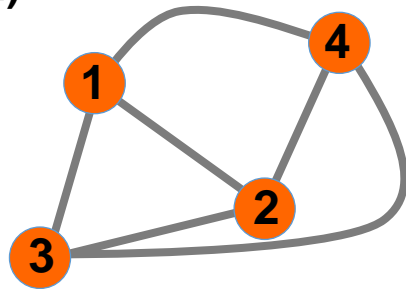
$$A_{ij} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 2 & 1 & 0 \\ 2 & 0 & 1 & 3 \\ 1 & 1 & 0 & 0 \\ 0 & 3 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$L = \frac{1}{2} \sum_{i,j=1}^N \text{nonzero}(A_{ij}) \quad A_{ii} = 0 \quad A_{ij} = A_{ji} \quad \langle k \rangle = \frac{2L}{N}$$

Social networks, collaboration networks



## Complete Graph (undirected)



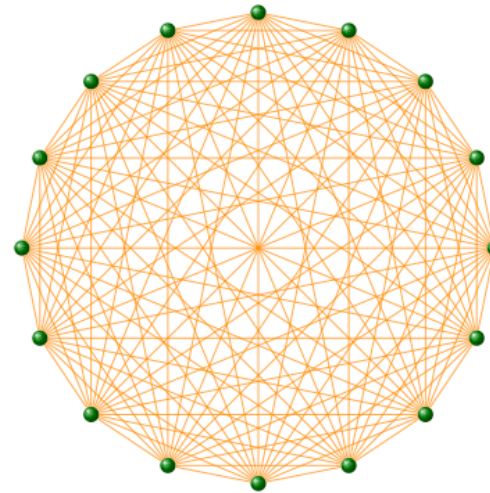
$$A_{ij} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

$$A_{ii} = 0$$

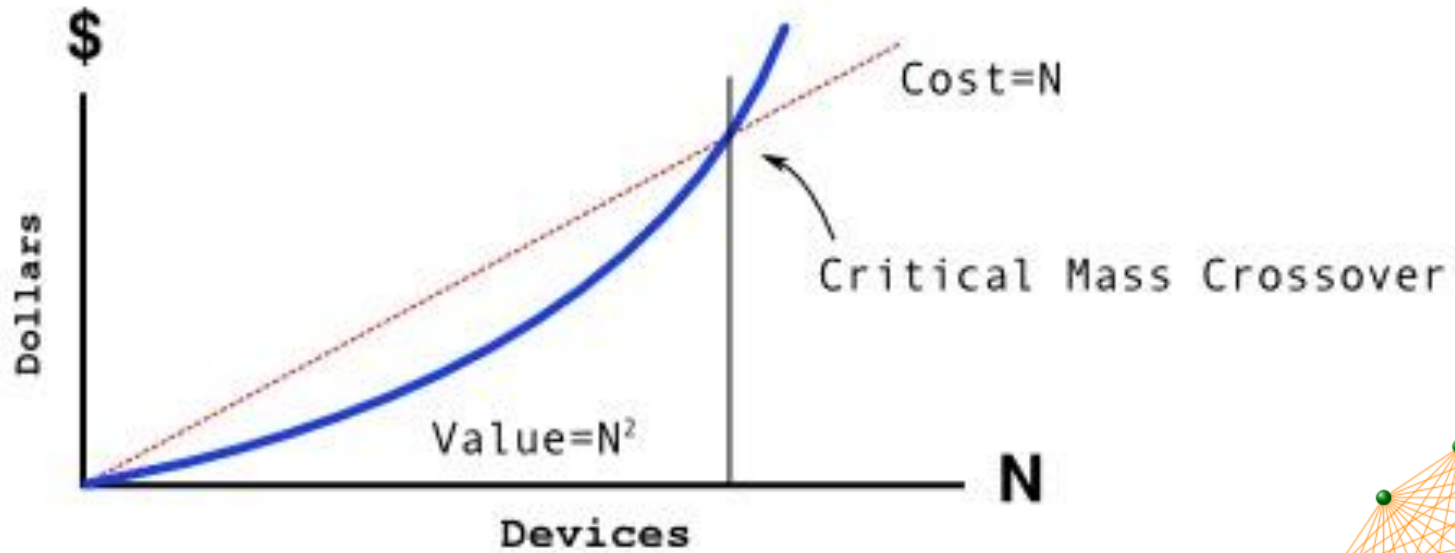
$$A_{i^1, j} = 1$$

$$L = L_{\max} = \frac{N(N-1)}{2} \quad \langle k \rangle = N-1$$

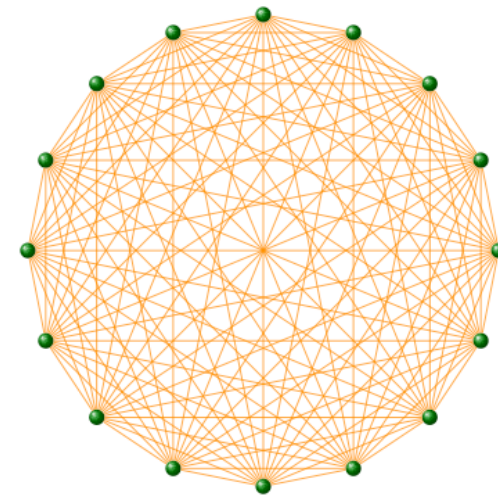
*Actor network, protein-protein interactions*



## METCALFE'S LAW



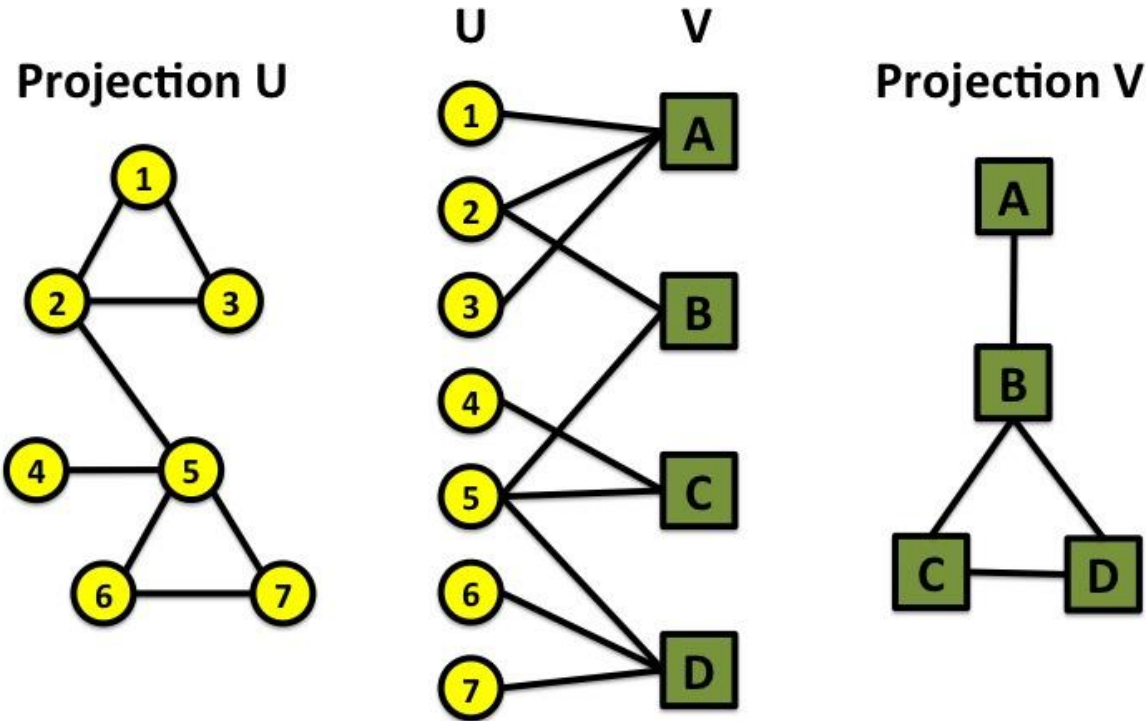
The maximum number of links a network of N nodes can have is: 
$$L_{\max} = \binom{N}{2} = \frac{N(N-1)}{2}$$



# BIPARTITE NETWORKS

# BIPARTITE GRAPHS

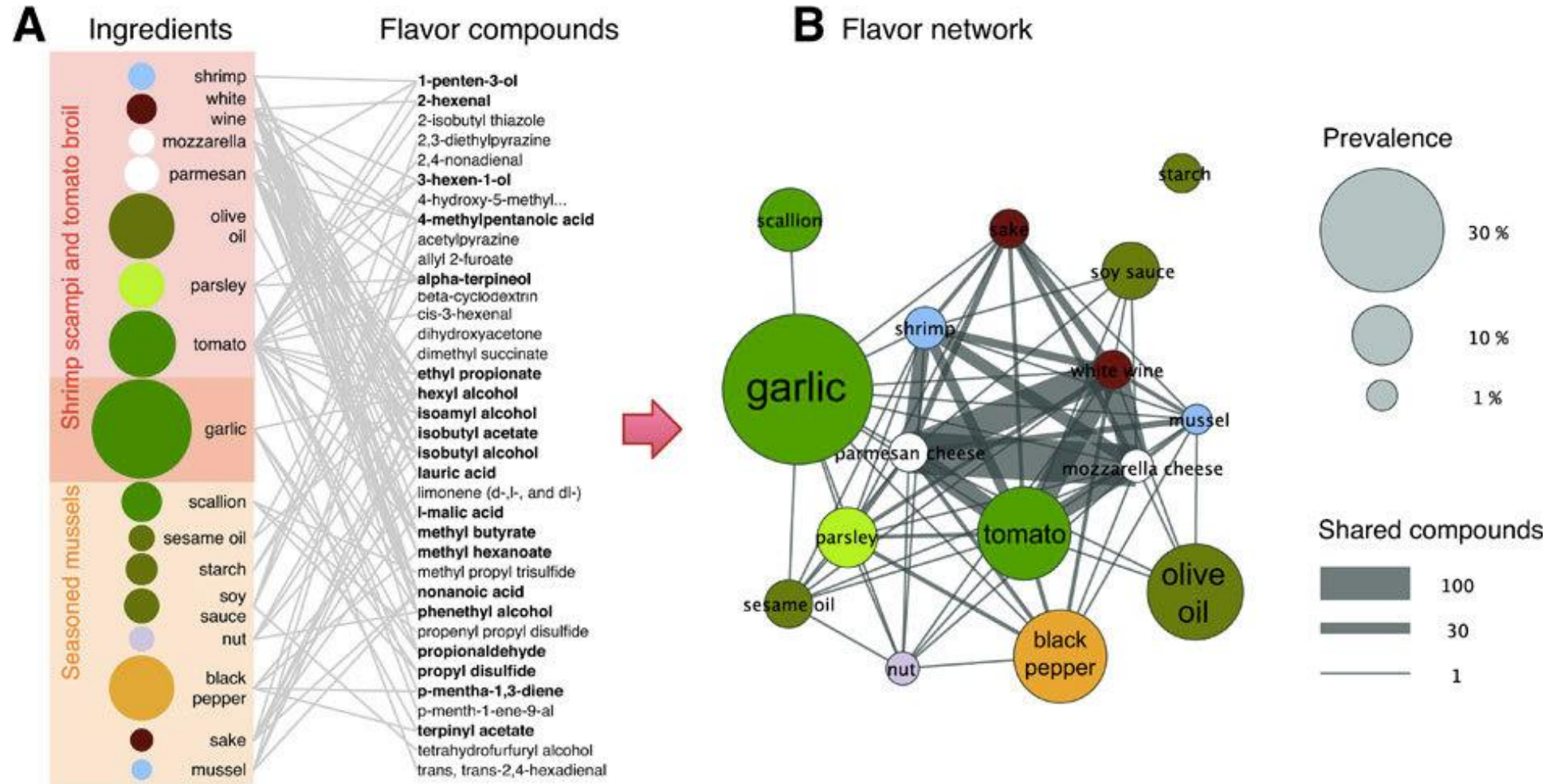
**bipartite graph** (or **bigraph**) is a [graph](#) whose nodes can be divided into two [disjoint sets](#)  $U$  and  $V$  such that every link connects a node in  $U$  to one in  $V$ ; that is,  $U$  and  $V$  are [independent sets](#).



## Examples:

Hollywood actor network  
Collaboration networks  
Disease network (diseasome)

# Ingredient-Flavor Bipartite Network



Y.-Y. Ahn, S. E. Ahnert, J. P. Bagrow, A.-L. Barabási <sup>[1]</sup> Flavor network and the principles of food pairing , Scientific Reports 196, (2011).

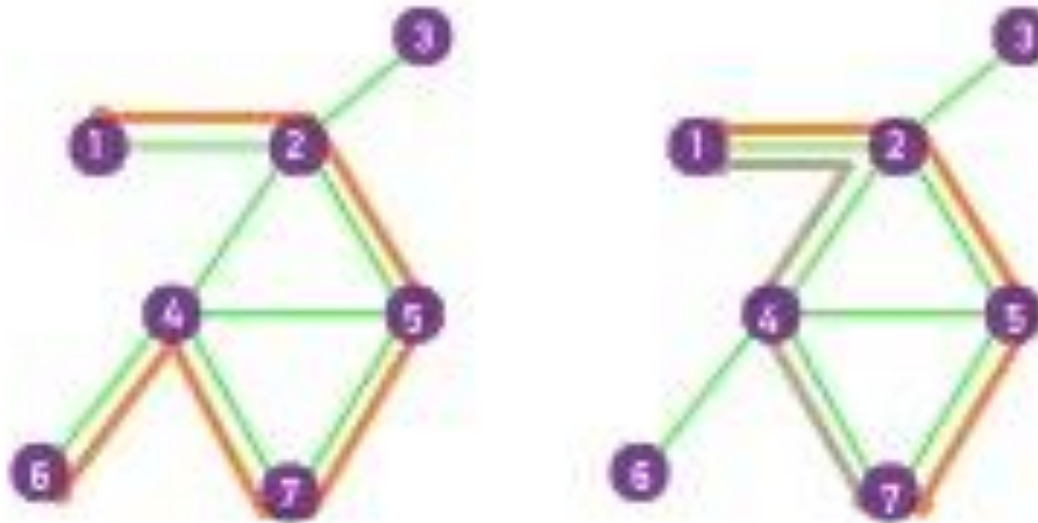
# PATHOLOGY

# PATHS

A *path* is a sequence of nodes in which each node is adjacent to the next one

$P_{i_0, i_n}$  of length  $n$  between nodes  $i_0$  and  $i_n$  is an ordered collection of  $n+1$  nodes and  $n$  links

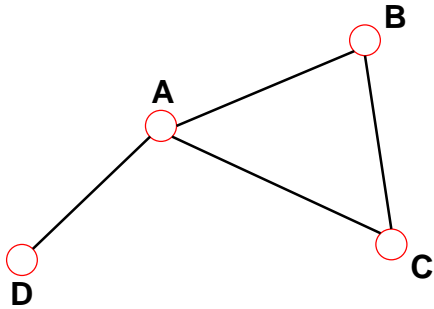
$$P_n = \{i_0, i_1, i_2, \dots, i_n\} \quad P_n = \{(i_0, i_1), (i_1, i_2), (i_2, i_3), \dots, (i_{n-1}, i_n)\}$$



- In a directed network, the path can follow only the direction of an arrow.

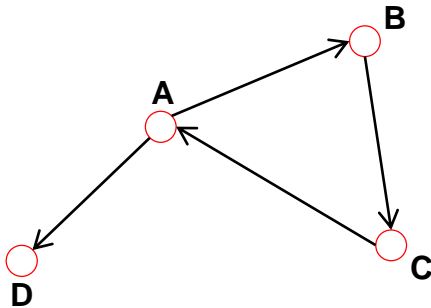
## DISTANCE IN A GRAPH

### Shortest Path, Geodesic Path



The *distance (shortest path, geodesic path)* between two nodes is defined as the number of edges along the shortest path connecting them.

\*If the two nodes are disconnected, the distance is infinity.



In **directed graphs** each path needs to follow the direction of the arrows.

Thus in a digraph the distance from node A to B (on an AB path) is generally different from the distance from node B to A (on a BCA path).



## NUMBER OF PATHS BETWEEN TWO NODES

### Adjacency Matrix

**$N_{ij}$ , number of paths between any two nodes  $i$  and  $j$ :**

**Length  $n=1$ :** If there is a link between  $i$  and  $j$ , then  $A_{ij}=1$  and  $A_{ij}=0$  otherwise.

**Length  $n=2$ :** If there is a path of length two between  $i$  and  $j$ , then  $A_{ik}A_{kj}=1$ , and  $A_{ik}A_{kj}=0$  otherwise.

The number of paths of length 2:

$$N_{ij}^{(2)} = \sum_{k=1}^N A_{ik}A_{kj} = [A^2]_{ij}$$

**Length  $n$ :** In general, if there is a path of length  $n$  between  $i$  and  $j$ , then  $A_{ik}\dots A_{lj}=1$  and  $A_{ik}\dots A_{lj}=0$  otherwise.

The number of paths of length  $n$  between  $i$  and  $j$  is\*

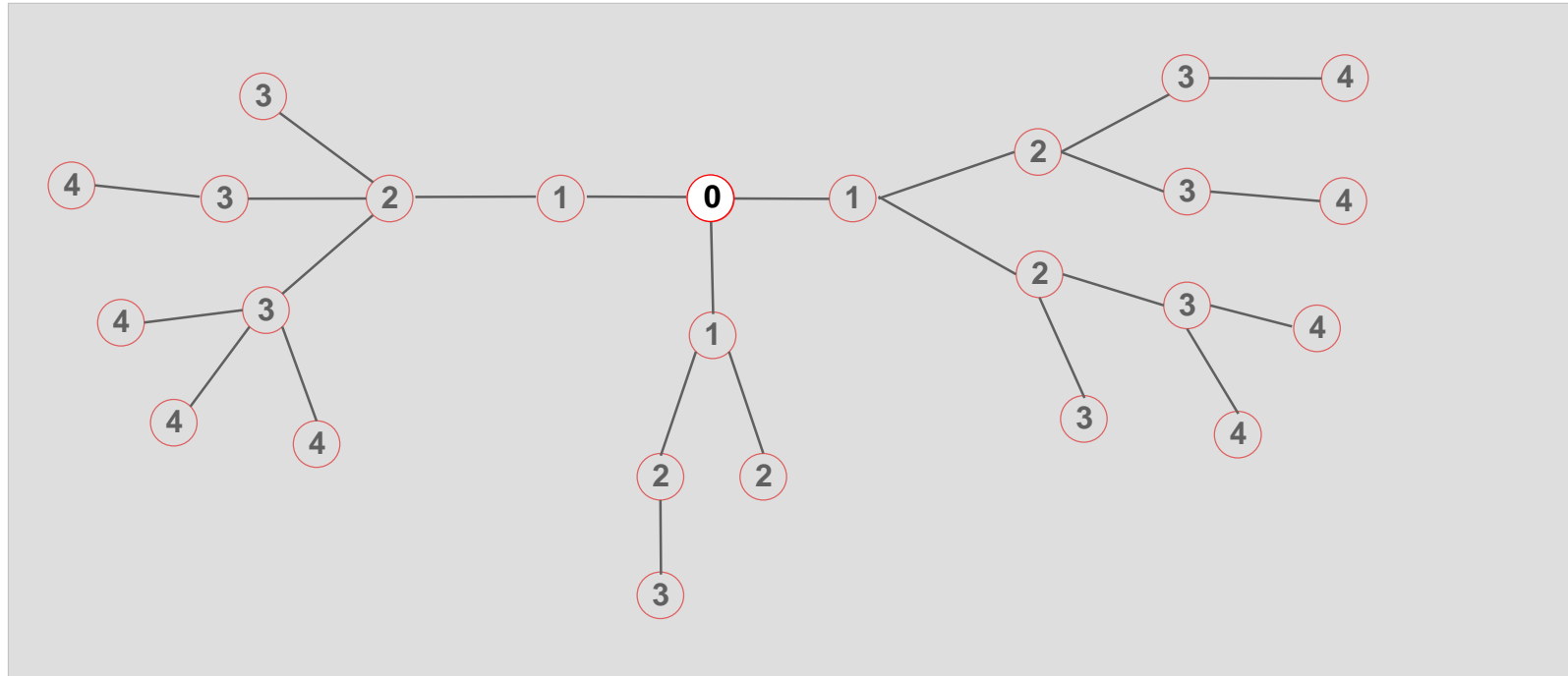
$$N_{ij}^{(n)} = [A^n]_{ij}$$

\* holds for both directed and undirected networks.

# FINDING DISTANCES: BREADTH FIRST SEARCH

Distance between node 0 and node 4:

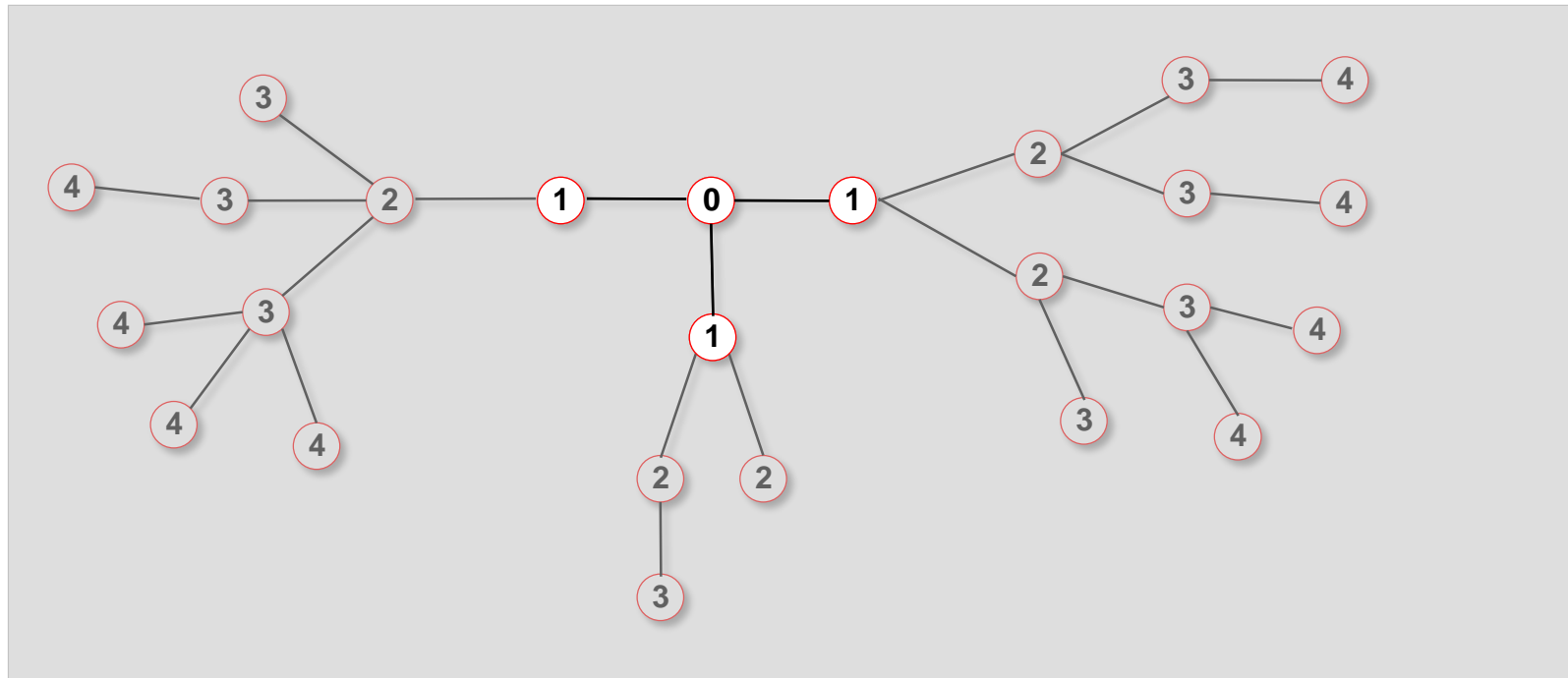
1. Start at 0.



## FINDING DISTANCES: BREADTH FIRST SEARCH

**Distance between node 0 and node 4:**

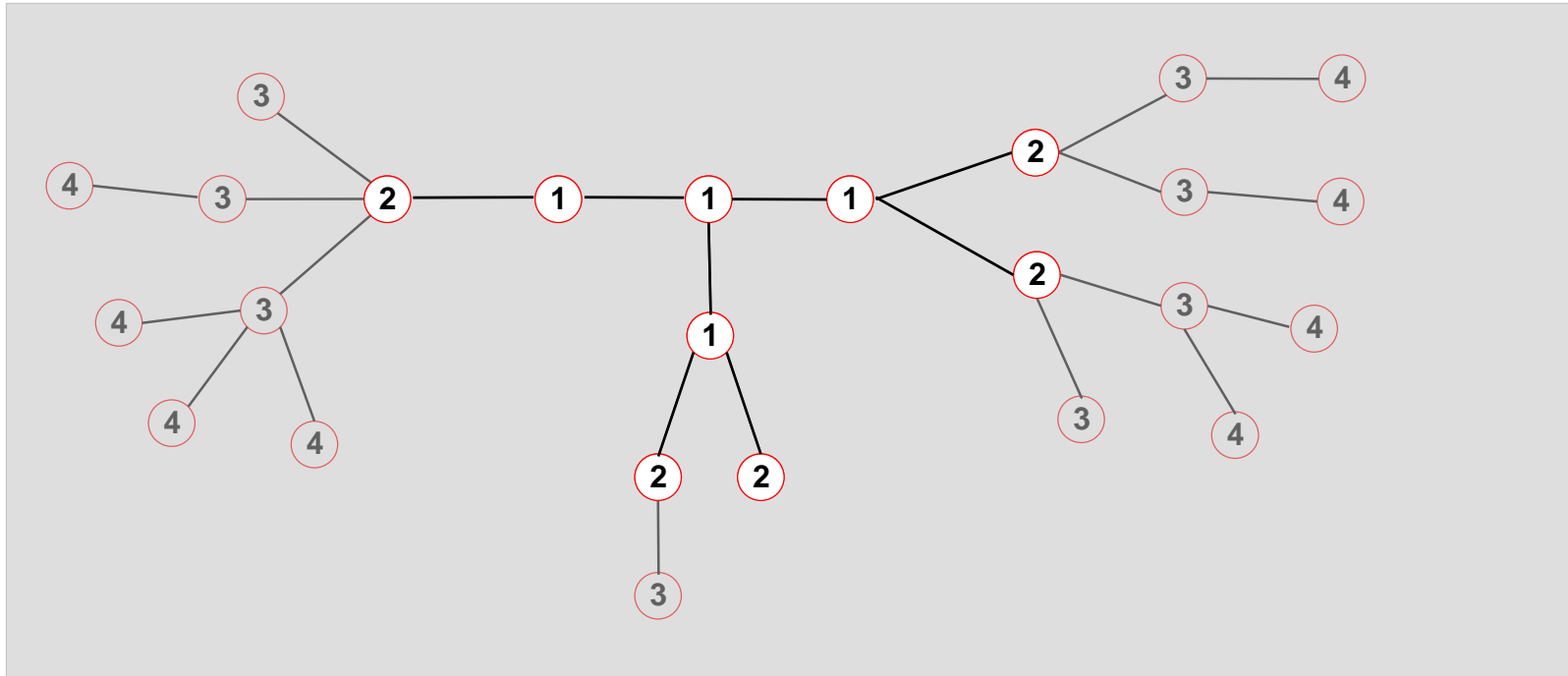
1. Start at 0.
2. Find the nodes adjacent to 1. Mark them as at distance 1. Put them in a queue.



## FINDING DISTANCES: BREADTH FIRST SEARCH

### Distance between node 0 and node 4:

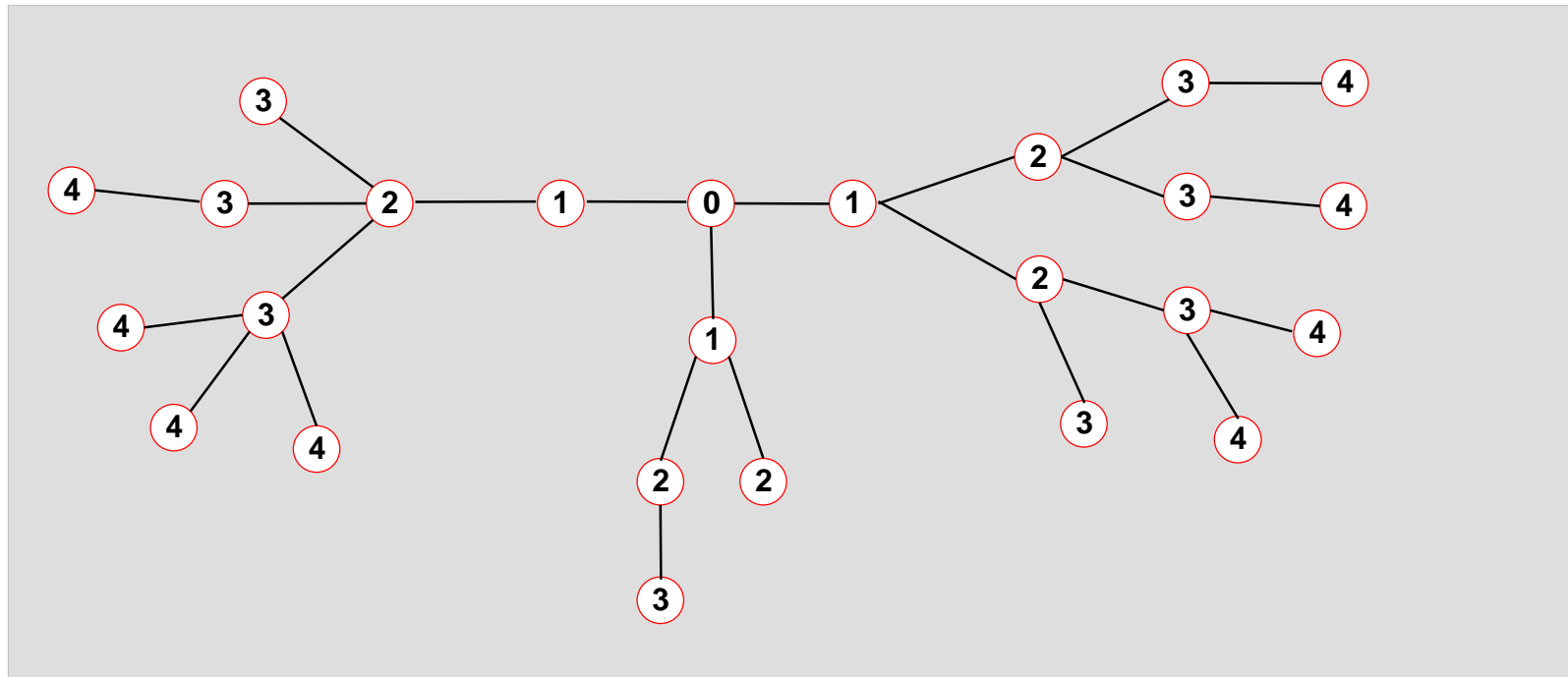
1. Start at 0.
2. Find the nodes adjacent to 0. Mark them as at distance 1. Put them in a queue.
3. Take the first node out of the queue. Find the unmarked nodes adjacent to it in the graph. Mark them with the label of 2. Put them in the queue.



## FINDING DISTANCES: BREADTH FIRST SEARCH

**Distance between node 0 and node 4:**

- 1.Repeat until you find node 4 or there are no more nodes in the queue.
- 2.The distance between 0 and 4 is the label of 4 or, if 4 does not have a label, infinity.



## NETWORK DIAMETER AND AVERAGE DISTANCE

*Diameter:*  $d_{\max}$  the maximum distance between any pair of nodes in the graph.

*Average path length/distance,  $\langle d \rangle$ ,* for a **connected graph**:

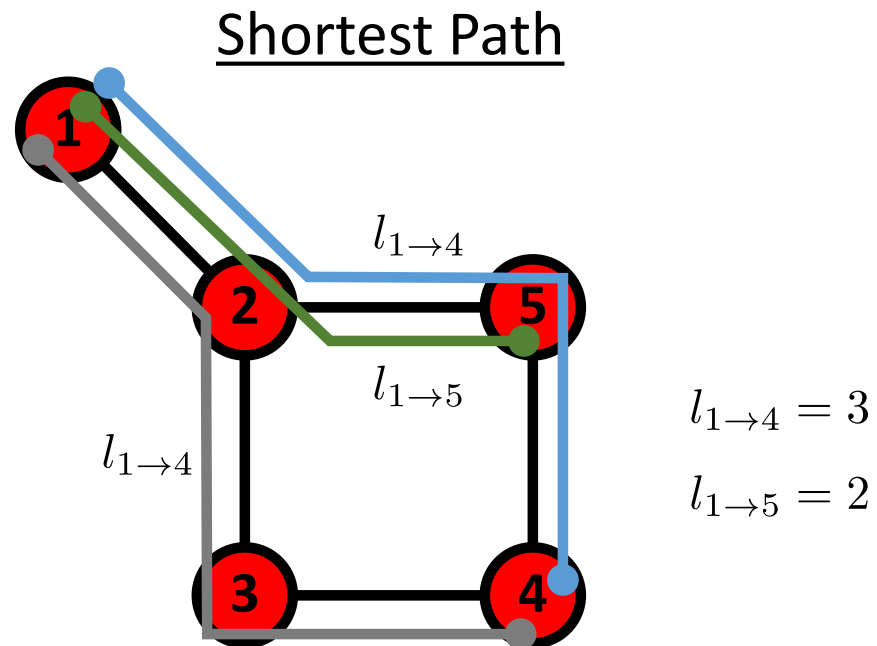
$$\langle d \rangle = \frac{1}{2L_{\max}} \sum_{i,j \neq i} d_{ij}$$

where  $d_{ij}$  is the distance from node  $i$  to node  $j$

In an *undirected graph*  $d_{ij} = d_{ji}$ , so we only need to count them once:

$$\langle d \rangle = \frac{1}{L_{\max}} \sum_{i,j > i} d_{ij}$$

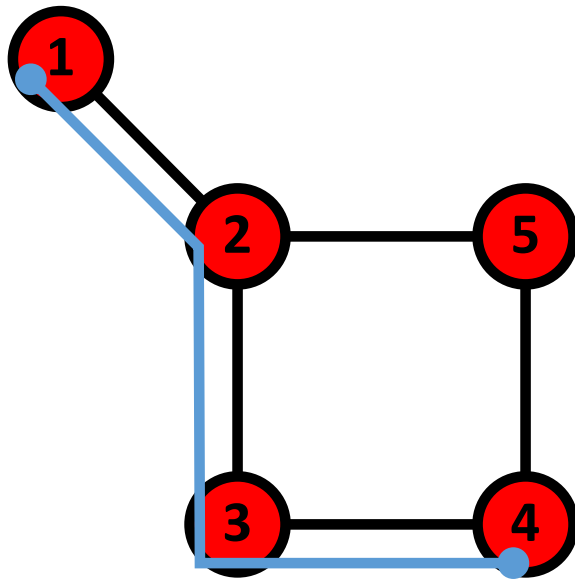
## PATHOLOGY: summary



The path with the shortest length between two nodes (distance).

## PATHOLOGY: summary

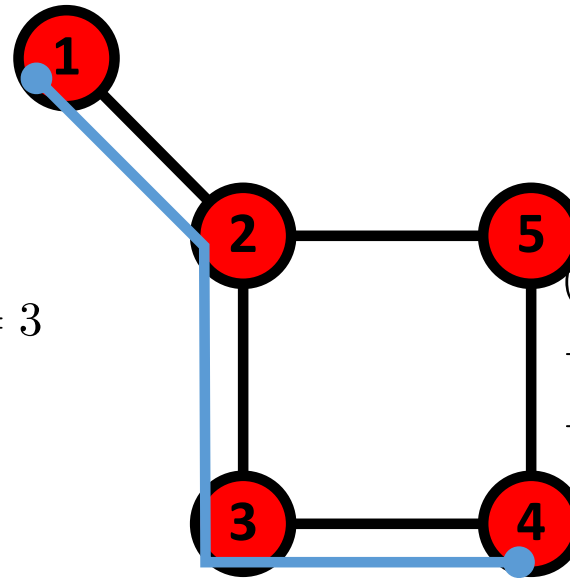
### Diameter



The longest shortest path in  
a graph

### Average Path Length

$$l_{1 \rightarrow 4} = 3$$



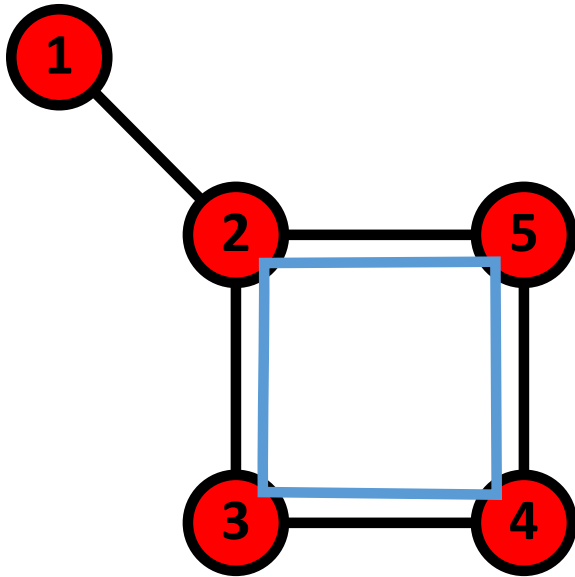
The average of the shortest paths for  
all pairs of nodes.

$$\begin{aligned} & (l_{1 \rightarrow 2} + l_{1 \rightarrow 3} + l_{1 \rightarrow 4} + \\ & + l_{1 \rightarrow 5} + l_{2 \rightarrow 3} + l_{2 \rightarrow 4} + \\ & + l_{2 \rightarrow 5} + l_{3 \rightarrow 4} + l_{3 \rightarrow 5} + \\ & + l_{4 \rightarrow 5}) / 10 = 1.6 \end{aligned}$$



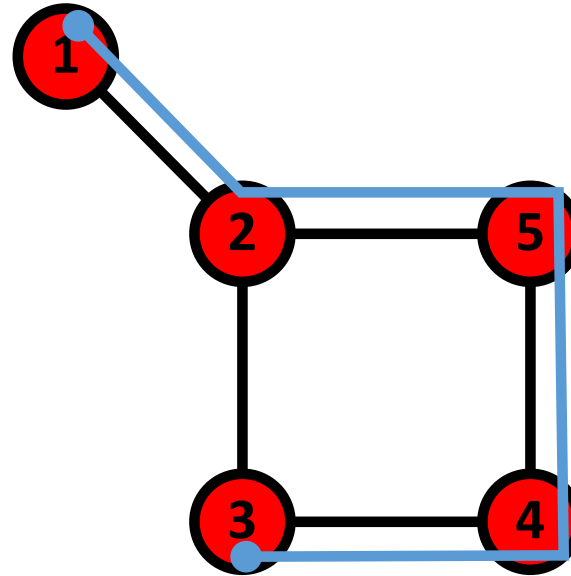
## PATHOLOGY: summary

Cycle



A path with the same start and end node.

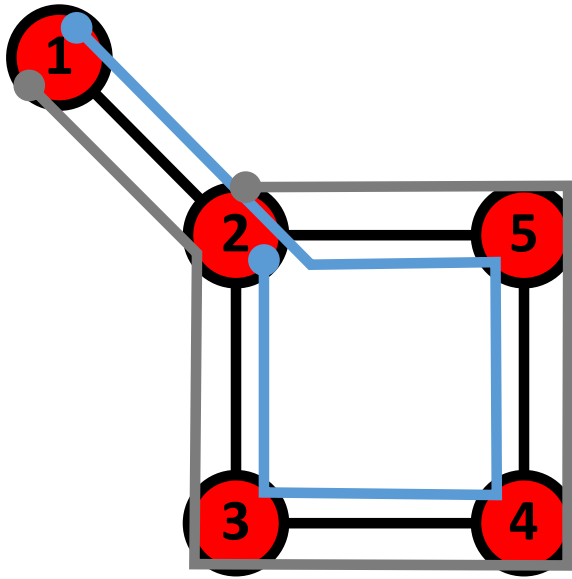
Self-avoiding Path



A path that does not intersect itself.

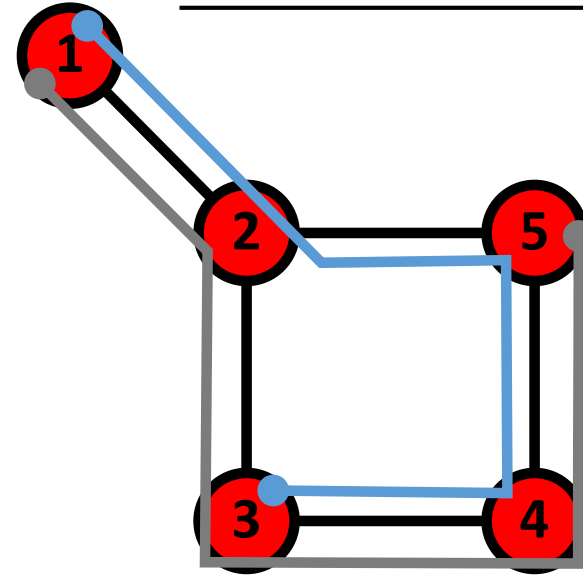
## PATHOLOGY: summary

Eulerian Path



A path that traverses each link exactly once.

Hamiltonian Path

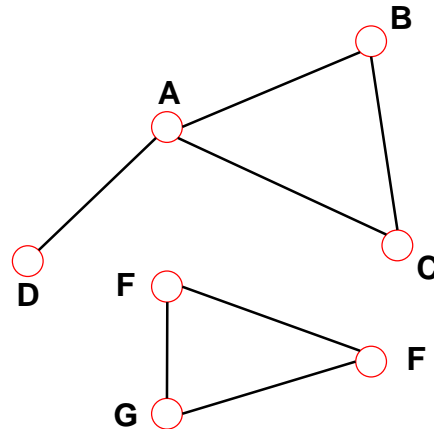
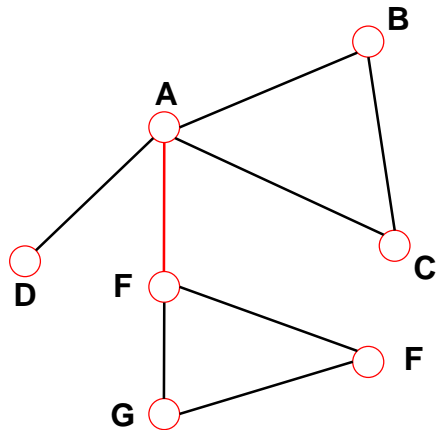


A path that visits each node exactly once.

# CONNECTEDNESS

## CONNECTIVITY OF UNDIRECTED GRAPHS

Connected (undirected) graph: any two vertices can be joined by a path.  
A disconnected graph is made up by two or more connected components.



Largest Component:  
**Giant Component**

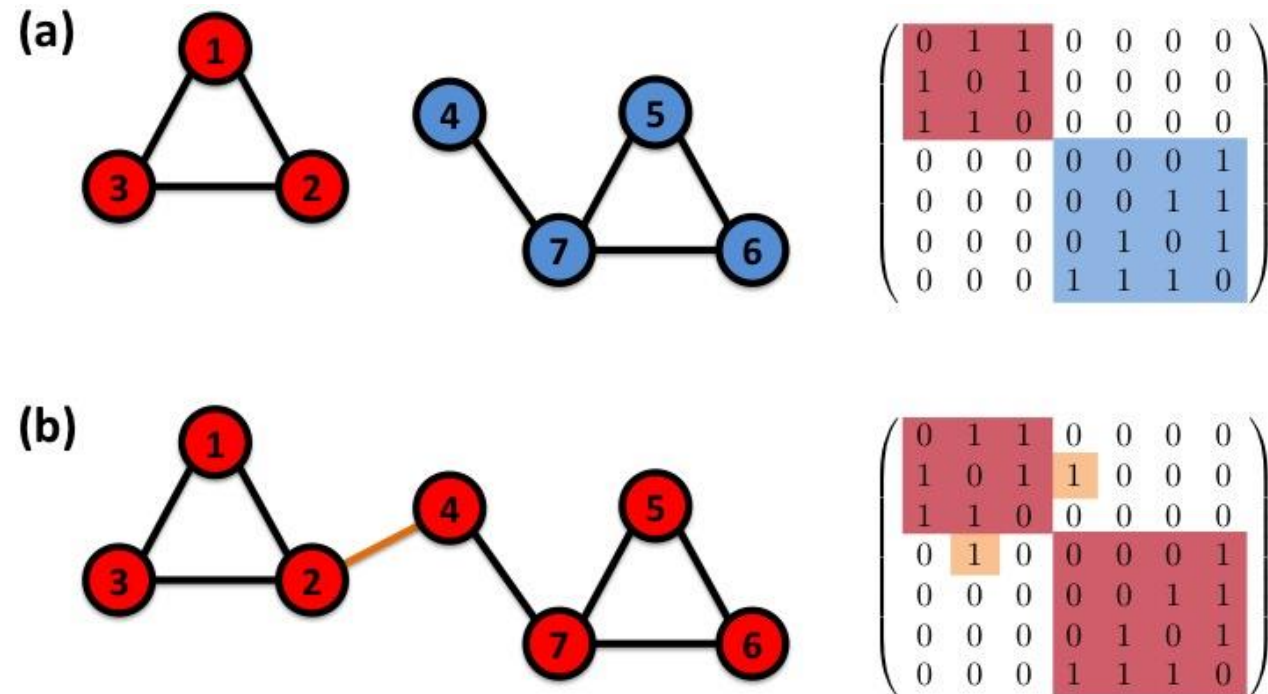
The rest: **Isolates**

Bridge: if we erase it, the graph becomes disconnected.

# CONNECTIVITY OF UNDIRECTED GRAPHS

## Adjacency Matrix

The adjacency matrix of a network with several components can be written in a block-diagonal form, so that nonzero elements are confined to squares, with all other elements being zero:

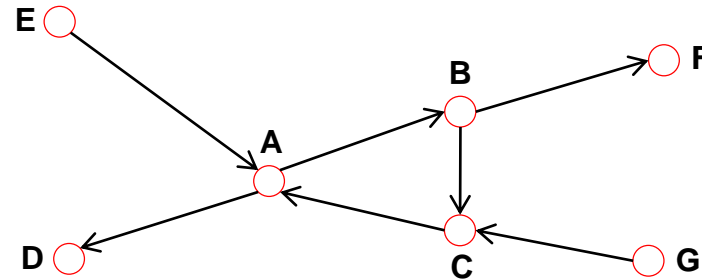
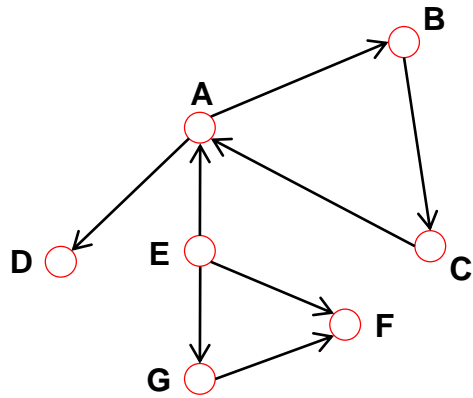


## CONNECTIVITY OF DIRECTED GRAPHS

**Strongly connected directed** graph: has a path from each node to every other node **and vice versa** (e.g. AB path and BA path).

**Weakly connected** directed graph: it is connected if we disregard the edge directions.

Strongly connected components can be identified, but not every node is part of a nontrivial strongly connected component.

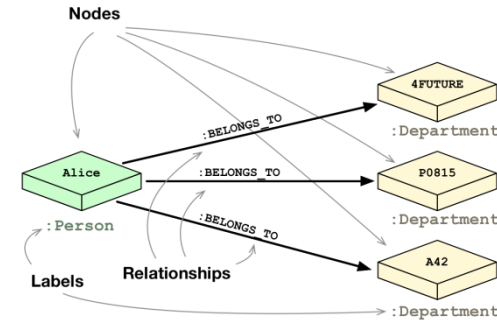


**In-component:** nodes that can reach the scc,

**Out-component:** nodes that can be reached from the scc.

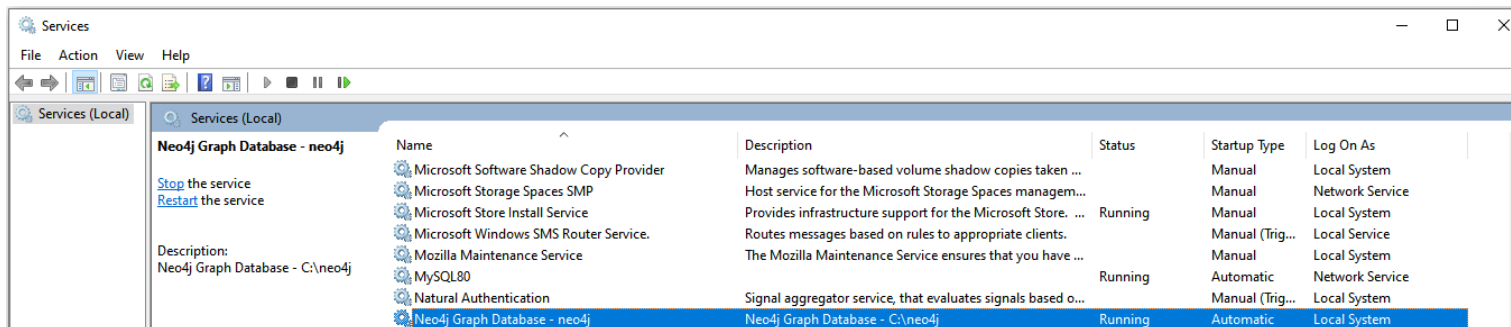
# Neo4j Graph Database

- First class support for nodes, relationships, and properties
- Efficient management of *semi-structured* and *network-oriented* data
- *Embedded* persistence engine – implemented as a small, light-weight, and non-intrusive Java library
- *Robust* – full support for distributed ACID transactions, configurable isolation levels, and transaction recovery
- *Highly scalable* – can handle large networks of data (no limits on the number of nodes, relationships, and properties that can be stored and indexed)
- *High-performance* – index-free adjacency, cost-based query optimizer, parallel indexes capability, binary protocol
- Open source, two editions – Community (GPL v3) and Enterprise (for commercial deployments with enterprise-grade availability, management, and scale-up and scale-out capabilities)



# Neo4j Installation

- Community Edition
- Server, not Desktop
- Start the Neo4j service
- Default login is username '**neo4j**' and password '**neo4j**'; must be changed on the first login



## Current Releases

Enterprise Server	Community Server	Neo4j Desktop
<h2>Neo4j Community Edition 4.1.1</h2> <p>14 July 2020 <a href="#">Release Notes</a>   <a href="#">Read More</a></p>		
OS	Download	
Linux/Mac	<a href="#">Neo4j 4.1.1 (tar)</a> SHA-256	
Windows	<a href="#">Neo4j 4.1.1 (zip)</a> SHA-256	
<h2>Neo4j Repositories</h2>		
Debian/Ubuntu	<a href="#">Neo4j on Debian and Ubuntu Cypher Shell</a>	
Linux Yum	<a href="#">Neo4j Stable Yum Repo</a>	
Docker	<a href="#">Neo4j Docker Image</a>	

## Windows (zip)

1. If it is not already installed, get [OpenJDK 8](#) or [Oracle Java 8](#), recommended for Neo4j 3.0.x Version 7 is recommended for releases prior to 2.3.0.
2. Find the zip file you just downloaded and right-click, extract all.
3. Place the extracted files in a permanent home on your server, for example `D:\neo4j\`. The top level directory is referred to as `NEO4J_HOME`.
  - To run Neo4j as a console application, use:  
`<NEO4J_HOME>\bin\neo4j console`
  - To install Neo4j as a service use:  
`<NEO4J_HOME>\bin\neo4j install-service`
  - For additional commands and to learn about the Windows PowerShell module included in the Zip file, see the [Windows installation documentation](#).
4. Visit <http://localhost:7474> in your web browser.
5. Connect using the username 'neo4j' with default password 'neo4j'. You'll then be prompted to change the password.



# Graph Databases

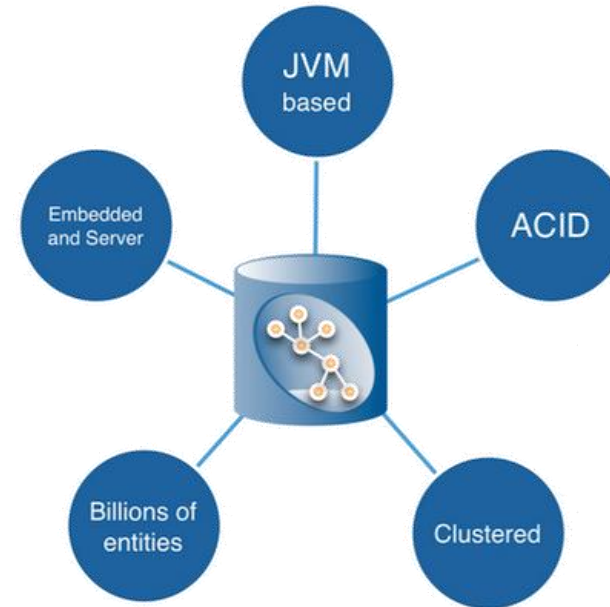
- Use graph structures for semantic queries with nodes, edges, and properties to represent and store data
- Use the Property Graph Model:
  - Connected entities (nodes) can hold any number of attributes (key-value-pairs) and can be tagged with labels representing their different roles in your domain
  - Relationships provide directed, named connections between two node-entities. A relationship always has a direction, a type, a start node, and an end node.
- Well suited for semi-structured and highly connected data
- Require a new query language

# Relational vs. Graph Databases

- Relational
  - Store highly structured data in tables with predetermined columns of certain types and many rows of the same type of information
  - Require developers and applications to strictly structure the data used in their applications
  - References to other rows and tables are indicated by referring to their (primary-)key attributes via foreign-key columns
  - In case of many-to-many relationships, you have to introduce a JOIN table (or junction table) that holds foreign keys of both participating tables which further increases join operation costs
- Graph
  - Relationships are first-class citizens of the graph data model
  - Each node (entity or attribute) directly and physically contains a list of relationship-records that represent its relationships to other nodes
  - The ability to pre-materialize relationships into database structures provides performances of several orders of magnitude advantage

# Neo4j Graph Database

- NoSQL Graph Database
- Implemented in Java and Scala
- Open source
- Free and open-source Community edition and Enterprise editions which provide all of the functionality of the Community edition in addition to scalable clustering, fail-over, high-availability, live backups, and comprehensive monitoring.
- Full database characteristics including ACID transaction compliance, cluster support, and runtime failover
- Constant time traversals for relationships in the graph both in depth and in breadth



# Cypher Query Language

- SQL-inspired language for describing patterns in graphs visually using an ASCII-art syntax
- Declarative – allows us to state **what** we want to select, insert, update or delete from our graph data without requiring us to describe exactly **how** to do it
- Contains clauses for searching for patterns, writing, updating, and deleting data
- Queries are built up using various clauses. Clauses are chained together, and they feed intermediate result sets between each other
- Cypher query gets compiled to an execution plan that can run and produce the desired result
- Statistical information about the database is kept up to date to optimize the execution plan
- Indexes on Node or Relationships properties are supported to improve the performance of the application

//TODO before next lecture:

- Homework 4 due on 4/20 at 11:59 pm EDT. Must be submitted on Submittity.