

30.

$$195^\circ = \tan\theta \text{ \& \; } \cot\theta$$

32.

$$125^\circ = \sin\theta \text{ \& \; } \csc\theta$$

34.

$$855^\circ = \sin\theta \text{ \& \; } \csc\theta$$

39.

$$\sin\theta > 0, \csc\theta > 0 = \text{Quadrants I \& II}$$

47.

$$\sec\theta < 0, \csc\theta < 0 = \text{Quadrant III}$$

65.

$$\sin\theta = 3/5$$

$$\cos = x/5 = 4/5$$

$$\begin{aligned}\sqrt{x^2+3^2} \\ \sqrt{x^2+9} \\ \sqrt{16+9} \\ \sqrt{25} = 5\end{aligned}$$

$$25-9 = 16 = x^2$$

$$\sqrt{16} = 4 = x$$

74.

$$\begin{aligned}\sin\theta &= y/r = -(4/5) \\ \cos\theta &= x/r = -(3/5) \\ \tan\theta &= y/x = 4/3 \\ \csc\theta &= r/y = -(5/4) \\ \sec\theta &= r/x = -(5/3) \\ \cot\theta &= x/y = 3/4\end{aligned}$$

$$\begin{aligned}\sqrt{-3^2+y^2} \\ \sqrt{9+y^2} \\ \sqrt{9+16} \\ \sqrt{25} = 5 \\ y = 4\end{aligned}$$

85.

$$\begin{aligned}1+\cot\theta^2 &= \csc\theta^2 \\ -\cot\theta^2 &-\cot\theta^2 \\ \csc\theta^2 - \cot\theta^2 &= 1 \\ 1 &= (r/y)^2 - (x/y)^2 \\ 1 &= \csc\theta^2 - \cot\theta^2\end{aligned}$$

$$\begin{aligned}r &= \sqrt{x^2+y^2} \\ r^2/r^2 &= (x^2+y^2)/r^2 \\ 1 &= ((x^2)/(r^2))+((y^2)/(r^2))\end{aligned}$$

77.

$$\begin{aligned}\sin\theta &= y/r = 8/\sqrt{67} \\ \cos\theta &= x/r = \sqrt{3}/\sqrt{67} \\ \tan\theta &= y/x = 8/\sqrt{3} \\ \csc\theta &= r/y = \sqrt{67}/8 \\ \sec\theta &= r/x = \sqrt{67}/\sqrt{3} \\ \cot\theta &= x/y = \sqrt{3}/8\end{aligned}$$

$$\begin{aligned}\sqrt{(\sqrt{3})^2+8^2} &= r \\ \sqrt{3+64} &= r \\ \sqrt{67} &= r\end{aligned}$$

89.

$$\sin 2\theta = \text{Negative}$$

100.

$$\cos(\theta+180) = \text{Negative}$$

79.

$$\begin{aligned}\sin\theta &= y/r = \sqrt{2}/6 \\ \cos\theta &= x/r = -(\sqrt{34})/6 \\ \tan\theta &= y/x = \sqrt{2}/\sqrt{34} \\ \csc\theta &= r/y = 6/\sqrt{2} \\ \sec\theta &= r/x = 6/\sqrt{34} \\ \cot\theta &= x/y = -(\sqrt{34})/\sqrt{2}\end{aligned}$$

$$\begin{aligned}\sqrt{x^2+\sqrt{2}^2} \\ \sqrt{x^2+2} \\ \sqrt{34+2} \\ \sqrt{36} = 6\end{aligned}$$