# ODE-constrained mixture modeling

1.0

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# 1 ODEMM Documentation

# 1.1 Introduction

Cellular heterogeneity occurs at multiple levels. To cover these levels, ODEMM combines mixuture modeling with mechanistic models for the individual subpopulations.

#### **ODEMM offers**

- models that are able to include mechanistic descriptions of the **means** of individual subpopulations, e.g., by reaction rate equations (RRE) (Hasenauer et al., PloS CB (2014), Loos et al., CMSB (2016)). For more details see below.
- Hierarchical population models that incorporate means and covariances of the individual subpopulations, e.g., provided by the sigma-point approximation or the moment-closure approximation. For more details see below.

# 1.2 Availability

ODEMM is a freely available MATLAB (MathWorks) toolbox available at https://github.com/ICB-DCM/\leftarrow ODEMM/. It can be retrieved by downloading the zip archive at https://github.com/ICB-DCM/ODEM\leftarrow M/archive/master.zip or cloning the git repository.

# 1.3 Installation

If the repository was cloned, install\_ODEMM.m needs to be run to add the folders to the MATLAB search path. If the zip archive was downloaded the archive needs to be unzipped before executing install\_ODEMM.m.

Toolboxes required for the examples

In principle, every simulation that provides means (and covariances) can be incorporated into ODEMM. For our examples, we used the simulations obtained by AMICI and calibrated the models using the parameter estimation toolbox PESTO.

- AMICI (simulation): https://github.com/ICB-DCM/AMICI
- PESTO (parameter estimation): https://github.com/ICB-DCM/PESTO
- SPToolbox (sigma-point approximation): https://github.com/ICB-DCM/SPToolbox (required for the examples incorporating means and covariances)
- CERENA (moment approximation): https://cerenadevelopers.github.io/CERENA/ (required for the example two\_stage\_exandintrinsic)

# 1.4 Licensing

See LICENSE file in the ODEMM source directory.

1.5 Models 3

#### 1.5 Models

ODEMM implements different kinds of ODE constrained mixture models.

# 1.5.1 Incorporation of mechanistic description of the mean

If the mean of a subpopulation is described by, e.g., RRE, the variances of the measurements are treated as additional parameters. An example for setting up RRE constrained mixture models is given in models\_RRE() which can be found in examples/conversion\_reaction/.

### 1.5.2 Incorporation of mechanistic description of the mean and covariance

When not only a mechanistic description of the mean, but also of the covariance is provided by the simulation function for the individual subpopulations, a hierarchical population model can be created. In our examples, we assessed two approximations for obtaining the statistical moments of the subpopulations:

- Sigma-point approximation (/examples/conversion\_reaction/models\_SP)
- Moment-closure approximation (/examples/two\_stage\_exandintrinsic)

### 1.6 Distributions

For the mixture distribution, ODEMM implements

- · multivariate normal distributions and
- · multivariate log-normal distributions.

The density functions and corresponding functions required for the models can be found in /distributions.

# 2 Conversion Reaction

This example reproduces the results of the analysis of "Unraveling sources of heterogeneity" of Loos et al., Cell Systems (2018). In this example, models incorporating only the **mean** ( $model_RRE.m$ ), and models incorporating **mean and variance** (e.g.,  $model_SP_k3.m$ ) are implemented. The latter allow for cell-to-cell variability of certain parameters of the model and incorporate the sigma-point approximation to obtain the statistical properties of the individual subpopulations.

First, the simulation file needs to be compiled using the MATLAB Toolbox AMICI. This can be done by running ./simulation/generate\_simFiles\_cr.m.

All models for this example are optimized within the function main\_optimization\_cr.m.

The Bayesian model selection is performed in main\_sampling\_cr.m.

The prediction of single-cell trajectories is performed in main\_singlecell\_prediction.m.

To reproduce the figures of the paper, run\_plot\_cr.m.

# 3 Differential protein expression (one stage)

This example reproduces the results of the analysis of "Identification of differential protein expression using multivariate data" of Loos et al., Cell Systems (2018).

First, the simulation file needs to be compiled using the MATLAB Toolbox AMICI. This can be done by running ./simulation/generate\_simFile\_oneStage.m.

The script  $main\_oneStage\_SP\_1D.m$  reproduces the results for model calibration bsaed on the marginal distributions. The script  $main\_oneStage\_SP\_2D.m$  reproduces the results for model calibration bsaed on the marginal distributions.

The figures of the paper can be reproduced with the scripts  $plot_fit_oneStage.m$  and  $plot_fit_outline$  uncertainty.m.

# 4 Influence of extracellular scaffolds on pain signaling

This example reproduces the results of the analysis of the "influence of extracellular scaffolds on sensitization signaling" of Loos et al., Cell Systems (2018).

First the simulation file needs to be compiled using the MATLAB Toolbox AMICI. This can be done by running ../subpopulation\_differences/simulation/generate\_simFile\_ErkSignaling.m.

The main file for the analysis is main\_ECM\_differences.m.

# 5 Subpopulation differences of sensory neurons

This example reproduces the results of the analysis of "causal differences between subpopulations of cultured sensory neurons" of Loos et al., Cell Systems (2018).

First the simulation file needs to be compiled using the MATLAB Toolbox AMICI. This can be done by running ./simulation/generate\_simFile\_ErkSignaling.m.

The main file for the analysis is main\_subpopulation\_analysis.m.

# 6 File Index

### 6.1 File List

Here is a list of all documented files with brief descriptions:

# collectConditions.m

This function collects all different conditions regarding input/differences between subpopulations/experiments and timepoints

# computeMixtureProbability.m

Robust calculation of a mixture distribution likelihood

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generateODEMM.m  This function generates a file that defines the ODE-constrained mixture model	50
<code>getLognMeanVar.m</code> This function calculations the mean and variances, and the corresponding derivatives of a multivariate log-normal distribution given the parameters $\mu$ and $\Sigma$	52
getRREsigmas.m  This function defines the parameters needed for the parametrization of the variances in case Reaction Rate Equations are used for the mechanistic description of the means	53
getScalingFactors.m  Calculates scaling factors for replicates such that the distance between the means in log-space are minimal	55
getSigmaPointApp_status_mod.m  Modified version of the getSigmaPointApp.m function of the SPToolbox	56
install_ODEMM.m  Script that adds the required paths to the MATLAB search path	57
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logLikelihood.m  This function evaluates the likelihood function for a given model, data and parameter vector	57
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distributions/logn/func_dmudxi_logn_median.m This function calculates the derivative of $\mu$ of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the median of the (multivariate) log-normal distribution. This should only be used for the case of using only a mechanistic description of the means of the observables	14
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examples/conversion_reaction/main_sampling_cr.m  This is the main script for the Bayesian model selection for the conversion reaction	23
examples/conversion_reaction/main_singlecell_prediction.m  This script shows the analysis of the single-cell trajectory prediction. First the single-cell parameter based on one single-cell trajectory are sampled and the predicted results are visualized. Then the parameters are optimized for 100 single-cell trajectories. This analysis corresponds to Loos et al., Cell Systems (2018), Figure 3E-G	23
examples/conversion_reaction/model_SP_all.m  This function generates model and estimates parameters for the model accounting for means and variances (using Sigma Points (SP).  All kinetic parameters are assumed to vary between individual cells: k1: inter- and intra-subpopulation variable k2: cell-to-cell variable k3: cell-to-cell variable	
examples/conversion_reaction/model_SP_k1.m  This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be: k1: inter- and intra-subpopulation variable k2: homogeneous k3: homogeneous	
examples/conversion_reaction/model_SP_k1k2.m  This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be: k1: inter- and intra-subpopulation variable k2: cell-to-cell variable	

k3: homogeneous

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examples/conversion_reaction/model_SP_k1k3.m  This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be: k1: inter- and intra-subpopulation variable k2: homogeneous k3: cell-to-cell variable	
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examples/conversion_reaction/model_SP_k3.m  This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be: k1: subpopulation variable k2: homogenous k3: cell-to-cell variable	
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examples/differential_protein_expression/main_oneStage_SP_1D.m  This script generates the model for the 1-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO	34
examples/differential_protein_expression/main_oneStage_SP_2D.m  This script generates the model for the 2-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO	35
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# 7 File Documentation

# 7.1 collectConditions.m File Reference

This function collects all different conditions regarding input/differences between subpopulations/experiments and timepoints.

### **Functions**

mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, conditions >,mlhsInnerSubst< matlabtypesubstitute, D</li>
 > collectConditions (matlabtypesubstitute D, matlabtypesubstitute M)

This function collects all different conditions regarding input/differences between subpopulations/experiments and timepoints.

# 7.1.1 Detailed Description

This function collects all different conditions regarding input/differences between subpopulations/experiments and timepoints.

### 7.1.2 Function Documentation

7.1.2.1 mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, conditions >,mlhsInnerSubst< matlabtypesubstitute, D > collectConditions ( matlabtypesubstitute D, matlabtypesubstitute M )

This function collects all different conditions regarding input/differences between subpopulations/experiments and timepoints.

### **USAGE**

[conditions,D] = collectConditions(D,M)

# **Parameters**

D	data struct
М	model struct

# **Return values**

conditions	conditions struct
D	updated data struct

# Required fields of D:

- t -- time vector
- u -- vector of stimulations

# Required fields of M:

- n\_subpop -- number of subpopulations
- $u\left\{ s\text{,e}\right\} -\text{input vector capturing differences between subpopulations and experiments}$

# Generated fields of D:

• c -- n\_subpop x (n\_u + n\_differences) matrix linking condition to data

# Generated fields of conditions:

• input -- (n\_u + n\_differences) x 1 input vector

```
• time -- 1 x n_t time vector
```

• sigma -- 1 x n\_t vector of sigmas for condition c

Definition at line 17 of file collectConditions.m.

Referenced by generate\_ECM\_models(), generate\_nosubpop\_file(), generate\_subpop\_files(), generate\_subpop\_ $\_$ TrkA(), logLikelihood(), main\_MA(), main\_MA\_1subpop(), main\_MA\_1subpop\_extrinsic(), main\_oneStage\_S  $\hookrightarrow$  P\_1D(), main\_oneStage\_SP\_2D(), main\_RRE(), main\_subpopulation\_analysis(), model\_SP\_all(), model\_SP\_ $\leftrightarrow$  k1(), model\_SP\_k1k2(), model\_SP\_k1k3(), model\_SP\_k2(), model\_SP\_k2k3(), model\_SP\_k3(), model\_SRE(), plot\_ECM\_fit(), plot\_subpop\_fit(), plotODEMM(), run\_fitting\_subpop(), run\_fittings\_ECM(), run\_logmarg\_subpop(), run\_lppd\_subpop(), and run\_profile\_ECM().

# 7.2 computeMixtureProbability.m File Reference

Robust calculation of a mixture distribution likelihood.

### **Functions**

mlhsInnerSubst< matlabtypesubstitute, varargout > computeMixtureProbability (matlabtypesubstitute varargin)

Robust calculation of a mixture distribution likelihood.

# 7.2.1 Detailed Description

Robust calculation of a mixture distribution likelihood.

### 7.2.2 Function Documentation

7.2.2.1 mlhslnnerSubst < matlabtypesubstitute, varargout > computeMixtureProbability ( matlabtypesubstitute varargin )

Robust calculation of a mixture distribution likelihood.

# USAGE

```
[logp,dlogpdxi] = computeMixtureProbability(w,q_i,H_i)
[logp] = computeMixtureProbability(w,q_i)
```

# **Parameters**

```
varargin

1 computeMixtureProbability ( w, q_i, H_i )

Required Parameters for varargin:

• w (1 x n_s) vector with weights w<sub>s</sub>

• q_i (n x n_s) matrix with log(p_i) for every column

• H_i (n x n_xi x n_s) s.th. d(w_i*p_i)/dxi = p_i*H_i
```

### Return values

logp	n x 1 scalar of loglikelihood
dlogpdxi	n x n_xi vector of gradient

Definition at line 17 of file computeMixtureProbability.m.

Referenced by logLikelihood(), run\_lppd\_cr(), and run\_lppd\_subpop().

# 7.3 distributions/logn/func\_dmudxi\_logn\_mean.m File Reference

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the mean of the (multivariate) log-normal distribution.

# Functions

• mlhsInnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_logn\_mean (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute Sigma, matlabtypesubstitute dSigmadxi, matlabtypesubstitute xi, matlabtypesubstitute u, matlabtypesubstitute dim)

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the mean of the (multivariate) log-normal distribution.

# 7.3.1 Detailed Description

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the mean of the (multivariate) log-normal distribution.

# 7.3.2 Function Documentation

7.3.2.1 mlhslnnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_logn\_mean ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute Sigma, matlabtypesubstitute dSigmadxi, matlabtypesubstitute xi, matlabtypesubstitute u, matlabtypesubstitute dim )

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the mean of the (multivariate) log-normal distribution.

#### **Parameters**

t	time vector (not used, included for consistency and possible extensions)
Х	vector of the means and covariances (not used, included for consistency and possible extensions)
dxdxi	derivatives of the means and covariances
Sigma	(not used, included for consistency and possible extensions)
dSigmadxi	(not used, included for consistency and possible extensions)
хi	parameter vector (not used, included for consistency and possible extensions)
и	input/stimulus (not used, included for consistency and possible extensions)
n_dim	dimension of measurements

#### Return values

	dmudxi	derivative of $\mu$ of the (multivariate) log-normal distribution	
--	--------	---	--

Definition at line 17 of file func dmudxi logn mean.m.

# 7.4 distributions/logn/func\_dmudxi\_logn\_median.m File Reference

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the median of the (multivariate) log-normal distribution. This should only be used for the case of using only a mechanistic description of the means of the observables.

### **Functions**

 mlhsInnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_logn\_median (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute Sigma, matlabtypesubstitute d
 Sigmadxi, matlabtypesubstitute xi, matlabtypesubstitute u, matlabtypesubstitute dim)

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the median of the (multivariate) log-normal distribution. This should only be used for the case of using only a mechanistic description of the means of the observables.

### 7.4.1 Detailed Description

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the median of the (multivariate) log-normal distribution. This should only be used for the case of using only a mechanistic description of the means of the observables.

### 7.4.2 Function Documentation

7.4.2.1 mlhslnnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_logn\_median ( matlabtypesubstitute *t*, matlabtypesubstitute *x*, matlabtypesubstitute *dxdxi*, matlabtypesubstitute *Sigma*, matlabtypesubstitute *dsigmadxi*, matlabtypesubstit

This function calculates the derivative of  $\mu$  of the (multivariate) log-normal distribution for the case of linking the mean of the observables to the median of the (multivariate) log-normal distribution. This should only be used for the case of using only a mechanistic description of the means of the observables.

#### **Parameters**

t	time vector (not used, included for consistency and possible extensions)
Х	vector of the means and covariances (not used, included for consistency and possible extensions)
dxdxi	derivatives of the means and covariances
Sigma	(not used, included for consistency and possible extensions)
dSigmadxi	(not used, included for consistency and possible extensions)
xi	parameter vector (not used, included for consistency and possible extensions)
и	input (not used, included for consistency and possible extensions)
n_dim	dimension of measurement

### Return values

dmudxi	derivative of $\mu$ of the (multivariate) log-normal distribution
--------	---

Definition at line 17 of file func dmudxi logn median.m.

# 7.5 distributions/logn/func\_dsigma2dxi\_logn.m File Reference

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a log-normal distribution assumption.

### **Functions**

• mlhsInnerSubst< matlabtypesubstitute, dsigma2dxi > func\_dsigma2dxi\_logn (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute varargin)

This function calcuatates the derivative of  $\sigma^2$  in case of univariate measurements and a log-normal distribution assumption.

# 7.5.1 Detailed Description

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a log-normal distribution assumption.

### 7.5.2 Function Documentation

7.5.2.1 mlhslnnerSubst< matlabtypesubstitute, dsigma2dxi> func\_dsigma2dxi\_logn ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtype

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a log-normal distribution assumption.

```
USAGE: dsigma2dxi = func_dsigma2dxi_logn(t,x,dxdxi,xi) dsigma2dxi = func_dsigma2dxi_logn(t,x,dxdxi,xi,noise,dnoisedxi,'additive') dsigma2dxi = func_dsigma2dxi_logn(t,x,dxdxi,xi,noise,dnoisedxi,'multiplicative')
```

### **Parameters**

time vector (not used, included for consistency and possible extensions)
vector of the means and variances (not used, included for consistency and possible extensions)
derivatives of the means and variances
parameter vector(not used, included for consistency and possible extensions)
noise: parameters for measurement noise
dnoisedxi: derivative of measurement noise
noisemodel: 'multiplicative' or 'additive'

### Return values

	dsigma2dxi	derivative of $\sigma^2$ of a log-normal distribution	
--	------------	---	--

Definition at line 17 of file func\_dsigma2dxi\_logn.m.

# 7.6 distributions/logn/func\_dSigmadxi\_logn.m File Reference

This function maps the means and covariances of the observables for a subpopulation to  $\Sigma$  of the multivariate log-normal distribution.

# **Functions**

• mlhsInnerSubst< matlabtypesubstitute, dSigmadxi > func\_dSigmadxi\_logn (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin)

This function maps the means and covariances of the observables for a subpopulation to  $\Sigma$  of the multivariate lognormal distribution.

# 7.6.1 Detailed Description

This function maps the means and covariances of the observables for a subpopulation to  $\Sigma$  of the multivariate log-normal distribution.

# 7.6.2 Function Documentation

7.6.2.1 mlhslnnerSubst< matlabtypesubstitute, dSigmadxi > func\_dSigmadxi\_logn ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute axdxi, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin )

This function maps the means and covariances of the observables for a subpopulation to  $\Sigma$  of the multivariate log-normal distribution.

### **USAGE**

```
dSigmadxi = func_dSigmadxi_logn(t,x,dxdxi,xi,n_n_dim)
dSigmadxi = func_dSigmadxi_logn(t,x,dxdxi,xi,n_n_dim,noise,dnoisedxi,'multiplicative')
dSigmadxi = func_dSigmadxi_logn(t,x,dxdxi,xi,n_n_dim,noise,dnoisedxi,'additive')
```

Definition at line 17 of file func\_dSigmadxi\_logn.m.

# 7.7 distributions/logn/func\_Sigma\_logn.m File Reference

This function maps the means and covariances to  $\Sigma$  of a (multivariate) log-normal distribution.

#### **Functions**

• mlhsInnerSubst< matlabtypesubstitute, Sigma > func\_Sigma\_logn (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin)

This function maps the means and covariances to  $\Sigma$  of a (multivariate) log-normal distribution.

### 7.7.1 Detailed Description

This function maps the means and covariances to  $\Sigma$  of a (multivariate) log-normal distribution.

#### 7.7.2 Function Documentation

7.7.2.1 mlhsInnerSubst< matlabtypesubstitute, Sigma > func\_Sigma\_logn ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin )

This function maps the means and covariances to  $\Sigma$  of a (multivariate) log-normal distribution.

### **USAGE**

```
Sigma = func_Sigma_logn(t,x,xi,n_dim)
Sigma = func_Sigma_logn(t,x,xi,n_dim,noise,'additive')
Sigma = func_Sigma_logn(t,x,xi,n_dim,noise,'multiplicative')
```

Definition at line 17 of file func\_Sigma\_logn.m.

# 7.8 distributions/logn/logoflognpdf.m File Reference

Modified version of MATLAB function LOGNPDF such that the log-density is returned.

# Functions

mlhsInnerSubst< matlabtypesubstitute, logy > logoflognpdf (matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute sigma)

Modified version of MATLAB function LOGNPDF such that the log-density is returned.

### 7.8.1 Detailed Description

Modified version of MATLAB function LOGNPDF such that the log-density is returned.

### 7.8.2 Function Documentation

7.8.2.1 mlhsInnerSubst < matlabtypesubstitute, logy > logoflognpdf ( matlabtypesubstitute *x*, matlabtypesubstitute *mu*, matlabtypesubstitute *sigma* )

Modified version of MATLAB function LOGNPDF such that the log-density is returned.

LOGNPDF Lognormal probability density function (pdf). Y = LOGNPDF(X,MU,SIGMA) returns values at X of the lognormal pdf with distribution parameters MU and SIGMA. MU and SIGMA are the mean and standard deviation, respectively, of the associated normal distribution. The size of Y is the common size of the input arguments. A scalar input functions as a constant matrix of the same size as the other inputs.

Default values for MU and SIGMA are 0 and 1 respectively.

#### See also

LOGNCDF, LOGNFIT, LOGNINV, LOGNLIKE, LOGNRND, LOGNSTAT.

Definition at line 17 of file logoflognpdf.m.

Referenced by logLikelihood().

# 7.9 distributions/logn/logofmvnpdf.m File Reference

Modified version of MATLAB function MVNPDF such that the log-density is returned.

#### **Functions**

• mlhsInnerSubst< matlabtypesubstitute, varargout > logofmvnpdf (matlabtypesubstitute varargin)

Modified version of MATLAB function MVNPDF such that the log-density is returned.

# 7.9.1 Detailed Description

Modified version of MATLAB function MVNPDF such that the log-density is returned.

# 7.10 distributions/norm/func dmudxi norm.m File Reference

This function calculates the derivative of  $\mu$  of the (multivariate) normal distribution.

### **Functions**

mlhsInnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_norm (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute Sigma, matlabtypesubstitute dSigmadxi, matlabtypesubstitute xi, matlabtypesubstitute u, matlabtypesubstitute n\_dim)

This function calculates the derivative of  $\mu$  of the (multivariate) normal distribution.

### 7.10.1 Detailed Description

This function calculates the derivative of  $\mu$  of the (multivariate) normal distribution.

### 7.10.2 Function Documentation

7.10.2.1 mlhslnnerSubst< matlabtypesubstitute, dmudxi > func\_dmudxi\_norm ( matlabtypesubstitute *t*, matlabtypesubstitute *x*, matlabtypesubstitute *dxdxi*, matlabtypesubstitute *Sigma*, matlabtypesubstitute *dsigmadxi*, matlabtypesubstitute *xi*, matlabtypesubstitute *u*, matlabtypesubstitute *n\_dim* )

This function calculates the derivative of  $\mu$  of the (multivariate) normal distribution.

#### **Parameters**

t	time vector (not used, included for consistency and possible extensions)
X	vector of means and variances (not used, included for consistency and possible extensions)
dxdxi	derivatives of means and variances
Sigma	(not used, included for consistency and possible extensions)
dSigmadxi	(not used, included for consistency and possible extensions)
xi	parameter vector (not used, included for consistency and possible extensions)
и	input (not used, included for consistency and possible extensions)
n_dim	dimension of measurement

### Return values

C	lmudxi	derivative of $\mu$ of the (multivariate) normal distribution.
---	--------	--

Definition at line 17 of file func dmudxi norm.m.

# 7.11 distributions/norm/func\_dsigma2dxi\_norm.m File Reference

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a normal distribution assumption.

# **Functions**

• mlhsInnerSubst< matlabtypesubstitute, dsigma2dxi > func\_dsigma2dxi\_norm (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute xi, matlabtypesubstitute varargin)

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a normal distribution assumption.

# 7.11.1 Detailed Description

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a normal distribution assumption.

## 7.11.2 Function Documentation

7.11.2.1 mlhslnnerSubst< matlabtypesubstitute, dsigma2dxi > func\_dsigma2dxi\_norm ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute xi, matlabtypesubsti

This function calculates the derivative of  $\sigma^2$  in case of univariate measurements and a normal distribution assumption.

 $USAGE: dsigma2dxi = func\_dsigma2dxi\_norm(t,x,dxdxi,xi) \ dsigma2dxi = func\_dsigma2dxi\_norm(t,x,dxdxi,xi,noise,dnoisedxi, additive')$ 

# **Parameters**

e vector (not used, included for consistency and possible extensions)	t
---	---

### **Parameters**

X	vector of the means and variances of the observables (not used, included for consistency and possible extensions)
dxdxi	derivatives of the means and variances of the obsevables
xi	parameter vector(not used, included for consistency and possible extensions)
varargin	
	noise: parameter for measurement noise
	dnoisedxi: derivative of measurement noise
	noisemodel: (so far only 'additive' supported)

# Return values

$\sigma^2$ of the normal distribution.	dsigma2dxi
--	------------

Definition at line 17 of file func\_dsigma2dxi\_norm.m.

# 7.12 distributions/norm/func\_dSigmadxi\_norm.m File Reference

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# **Functions**

 mlhsInnerSubst< matlabtypesubstitute, dSigmadxi > func\_dSigmadxi\_norm (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin)

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# 7.12.1 Detailed Description

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# 7.12.2 Function Documentation

7.12.2.1 mlhslnnerSubst< matlabtypesubstitute, dSigmadxi > func\_dSigmadxi\_norm ( matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute varargin )

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# **USAGE**

Definition at line 17 of file func\_dSigmadxi\_norm.m.

# 7.13 distributions/norm/func\_Sigma\_norm.m File Reference

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# **Functions**

mlhsInnerSubst< matlabtypesubstitute, Sigma > func\_Sigma\_norm (matlabtypesubstitute t, matlabtypesubstitute x, matlabtypesubstitute xi, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin)

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# 7.13.1 Detailed Description

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

# 7.13.2 Function Documentation

7.13.2.1 mlhslnnerSubst< matlabtypesubstitute, Sigma > func\_Sigma\_norm ( matlabtypesubstitute *t*, matlabtypesubstitute *x*, matlabtypesubstitute *xi*, matlabtypesubstitute *n\_dim*, matlabtypesubstitute *varargin* )

This function maps the means and variances to  $\Sigma$  of the multivariate normal distribution.

### **USAGE**

Sigma = func\_Sigma\_norm(t,x,xi,n\_dim,noise,'additive')

# Parameters

t	time vector
X	vector including means and variances
xi	(not used, included for consistency and possible extensions)
n_dim	dimension of measurement
varargin	
	noise: parameter for measurement noise
	noisemodel: (so far only 'additive' supported)

# Return values

Sigma	(n_t x n_dim x n_dim) $\Sigma$ of the multivariate normal distribution.
-------	---

Definition at line 17 of file func\_Sigma\_norm.m.

# 7.14 distributions/norm/logofnormpdf.m File Reference

Modified version of MATLAB function NORMPDF such that the log-density is given back.

### **Functions**

mlhsInnerSubst< matlabtypesubstitute, logy > logofnormpdf (matlabtypesubstitute x, matlabtypesubstitute x, matlabtypesubstitute sigma)

Modified version of MATLAB function NORMPDF such that the log-density is given back.

# 7.14.1 Detailed Description

Modified version of MATLAB function NORMPDF such that the log-density is given back.

### 7.14.2 Function Documentation

7.14.2.1 mlhslnnerSubst< matlabtypesubstitute, logy > logofnormpdf ( matlabtypesubstitute *x,* matlabtypesubstitute *mu,* matlabtypesubstitute *sigma* )

Modified version of MATLAB function NORMPDF such that the log-density is given back.

NORMPDF Normal probability density function (pdf). Y = NORMPDF(X,MU,SIGMA) returns the pdf of the normal distribution with mean MU and standard deviation SIGMA, evaluated at the values in X. The size of Y is the common size of the input arguments. A scalar input functions as a constant matrix of the same size as the other inputs.

Default values for MU and SIGMA are 0 and 1 respectively.

See also

NORMCDF, NORMFIT, NORMINV, NORMLIKE, NORMRND, NORMSTAT.

Definition at line 17 of file logofnormpdf.m.

Referenced by logLikelihood().

7.15 examples/conversion\_reaction/data/generate\_data\_cr.m File Reference

This script generates the artificial data of a conversion process.

### **Functions**

• noret::substitute generate data cr ()

This script generates the artificial data of a conversion process.

# 7.15.1 Detailed Description

This script generates the artificial data of a conversion process.

# 7.16 examples/conversion\_reaction/main\_optimization\_cr.m File Reference

This is the main script for the first example, the conversion reaction. All Reaction Rate Equation (RRE) models are generated and their parameters are estimated by calling models\_RRE.m. All SP models are estimated, for which e.g. model\_SP\_k1.m indicates that k1 has an additional cell-to-cell variability modeled by the Sigma point approximation.

### **Functions**

• noret::substitute main optimization cr ()

This is the main script for the first example, the conversion reaction. All Reaction Rate Equation (RRE) models are generated and their parameters are estimated by calling models\_RRE.m. All SP models are estimated, for which e.g. model\_SP\_k1.m indicates that k1 has an additional cell-to-cell variability modeled by the Sigma point approximation.

# 7.16.1 Detailed Description

This is the main script for the first example, the conversion reaction. All Reaction Rate Equation (RRE) models are generated and their parameters are estimated by calling models\_RRE.m. All SP models are estimated, for which e.g. model\_SP\_k1.m indicates that k1 has an additional cell-to-cell variability modeled by the Sigma point approximation.

# 7.17 examples/conversion\_reaction/main\_sampling\_cr.m File Reference

This is the main script for the Bayesian model selection for the conversion reaction.

# **Functions**

• noret::substitute main\_sampling\_cr ()

This is the main script for the Bayesian model selection for the conversion reaction.

# 7.17.1 Detailed Description

This is the main script for the Bayesian model selection for the conversion reaction.

# 7.18 examples/conversion\_reaction/main\_singlecell\_prediction.m File Reference

This script shows the analysis of the single-cell trajectory prediction. First the single-cell parameter based on one single-cell trajectory are sampled and the predicted results are visualized. Then the parameters are optimized for 100 single-cell trajectories. This analysis corresponds to Loos et al., Cell Systems (2018), Figure 3E-G.

# **Functions**

• noret::substitute main singlecell prediction ()

This script shows the analysis of the single-cell trajectory prediction. First the single-cell parameter based on one single-cell trajectory are sampled and the predicted results are visualized. Then the parameters are optimized for 100 single-cell trajectories. This analysis corresponds to Loos et al., Cell Systems (2018), Figure 3E-G.

#### 7.18.1 Detailed Description

This script shows the analysis of the single-cell trajectory prediction. First the single-cell parameter based on one single-cell trajectory are sampled and the predicted results are visualized. Then the parameters are optimized for 100 single-cell trajectories. This analysis corresponds to Loos et al., Cell Systems (2018), Figure 3E-G.

### 7.18.2 Function Documentation

### 7.18.2.1 noret::substitute main\_singlecell\_prediction()

This script shows the analysis of the single-cell trajectory prediction. First the single-cell parameter based on one single-cell trajectory are sampled and the predicted results are visualized. Then the parameters are optimized for 100 single-cell trajectories. This analysis corresponds to Loos et al., Cell Systems (2018), Figure 3E-G.

Script for the single cell prediction for neurons cultured on poly-D-lysine.

Definition at line 17 of file main singlecell prediction.m.

References load\_plot\_settings(), and sclogLikelihood\_cr().

# 7.19 examples/subpopulation\_differences/main\_singlecell\_prediction.m File Reference

Script for the single cell prediction for neurons cultured on poly-D-lysine.

### **Functions**

• noret::substitute main\_singlecell\_prediction ()

# 7.19.1 Detailed Description

Script for the single cell prediction for neurons cultured on poly-D-lysine.

# 7.20 examples/conversion\_reaction/model\_SP\_all.m File Reference

This function generates model and estimates parameters for the model accounting for means and variances (using Sigma Points (SP).

All kinetic parameters are assumed to vary between individual cells:

k1: inter- and intra-subpopulation variable

k2: cell-to-cell variable k3: cell-to-cell variable

# **Functions**

• noret::substitute model SP all ()

This function generates model and estimates parameters for the model accounting for means and variances (using Sigma Points (SP).

All kinetic parameters are assumed to vary between individual cells:

k1: inter- and intra-subpopulation variable

k2: cell-to-cell variable

k3: cell-to-cell variable

.

# 7.20.1 Detailed Description

This function generates model and estimates parameters for the model accounting for means and variances (using Sigma Points (SP).

All kinetic parameters are assumed to vary between individual cells:

k1: inter- and intra-subpopulation variable

k2: cell-to-cell variable k3: cell-to-cell variable

# 7.21 examples/conversion\_reaction/model\_SP\_k1.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneous k3: homogeneous

# Functions

• noret::substitute model SP k1 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneousk3: homogeneous

# 7.21.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneous k3: homogeneous

•

# 7.22 examples/conversion\_reaction/model\_SP\_k1k2.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: cell-to-cell variable

k3: homogeneous.

# **Functions**

noret::substitute model\_SP\_k1k2 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

*k2: cell-to-cell variable k3: homogeneous.* 

# 7.22.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: cell-to-cell variable

k3: homogeneous.

# 7.23 examples/conversion reaction/model SP k1k3.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneous

k3: cell-to-cell variable

.

### **Functions**

• noret::substitute model\_SP\_k1k3 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneous

k3: cell-to-cell variable

.

# 7.23.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)) The parameter are assumed to be:

k1: inter- and intra-subpopulation variable

k2: homogeneous

k3: cell-to-cell variable

.

# 7.24 examples/conversion\_reaction/model\_SP\_k2.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variable

k2: cell-to-cell variable

k3: homogeneous.

### **Functions**

noret::substitute model\_SP\_k2 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variable

k2: cell-to-cell variable

k3: homogeneous.

### 7.24.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variablek2: cell-to-cell variablek3: homogeneous.

# 7.25 examples/conversion\_reaction/model\_SP\_k2k3.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variablek2: cell-to-cell variablek3: cell-to-cell variable.

### **Functions**

• noret::substitute model SP k2k3 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variablek2: cell-to-cell variablek3: cell-to-cell variable.

# 7.25.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variablek2: cell-to-cell variablek3: cell-to-cell variable.

# 7.26 examples/conversion\_reaction/model\_SP\_k3.m File Reference

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variable

k2: homogenousk3: cell-to-cell variable

This model is the ground truth.

### **Functions**

• noret::substitute model SP k3 ()

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variable

k2: homogenous

k3: cell-to-cell variable

This model is the ground truth.

# 7.26.1 Detailed Description

This function generates the model and estimates the parameters in case of accounting for means and variances (using Sigma Points (SP)). The parameter are assumed to be:

k1: subpopulation variable

k2: homogenous

k3: cell-to-cell variable

This model is the ground truth.

# 7.27 examples/conversion reaction/models RRE.m File Reference

This function generates Reaction Rate Euqation model and estimates the parameters for the models with varying number of parameters for the variances.

#### **Functions**

• noret::substitute models\_RRE ()

This function generates Reaction Rate Euqation model and estimates the parameters for the models with varying number of parameters for the variances.

# 7.27.1 Detailed Description

This function generates Reaction Rate Euqation model and estimates the parameters for the models with varying number of parameters for the variances.

# 7.28 examples/conversion\_reaction/plot\_cr.m File Reference

This script visualizes the results for the conversion reaction.

### **Functions**

noret::substitute plot\_cr ()

This script visualizes the results for the conversion reaction.

# 7.28.1 Detailed Description

This script visualizes the results for the conversion reaction.

# 7.29 examples/conversion\_reaction/plot\_cr\_SIAppendix.m File Reference

This script generates the figures for the supplement for the conversion reaction example.

#### **Functions**

noret::substitute plot\_cr\_SIAppendix ()
 This script generates the figures for the supplement for the conversion reaction example.

## 7.29.1 Detailed Description

This script generates the figures for the supplement for the conversion reaction example.

7.30 examples/conversion\_reaction/plot\_cr\_variabilityReduction.m File Reference

clear all close all clc load\_plot\_settings

#### **Functions**

noret::substitute plot\_cr\_variabilityReduction ()
 clear all close all clc load\_plot\_settings

## 7.30.1 Detailed Description

clear all close all clc load\_plot\_settings

7.30.2 Function Documentation

7.30.2.1 noret::substitute plot\_cr\_variabilityReduction ( )

clear all close all clc load\_plot\_settings

% SP all

Definition at line 17 of file plot\_cr\_variabilityReduction.m.

Referenced by plot\_cr\_SIAppendix().

## 7.31 examples/conversion reaction/run lppd cr.m File Reference

This function runs the sampling for the log pointwise predictive density for the conversion reaction reaction example.

# **Functions**

mlhsInnerSubst< matlabtypesubstitute, lppd > run\_lppd\_cr (matlabtypesubstitute model\_name, matlabtypesubstitute burnin, matlabtypesubstitute nlter, matlabtypesubstitute saveFlag)

This function runs the sampling for the log pointwise predictive density for the conversion reaction reaction example.

## 7.31.1 Detailed Description

This function runs the sampling for the log pointwise predictive density for the conversion reaction reaction example.

#### 7.31.2 Function Documentation

7.31.2.1 mlhslnnerSubst< matlabtypesubstitute, lppd > run\_lppd\_cr ( matlabtypesubstitute model\_name, matlabtypesubstitute burnin, matlabtypesubstitute nlter, matlabtypesubstitute saveFlag )

This function runs the sampling for the log pointwise predictive density for the conversion reaction reaction example.

## **USAGE**

parameters\_lppd = run\_lppd\_cr(model\_name,burnin,nlter,saveFlag)

#### **Parameters**

model_name	string indicating model (RRE_timedep,RRE_subpop,	
	RRE_onlyone,SP_k1,SP_k2,SP_k3,SP_k1k2,SP_k1k3,SP_k2k3,orSP_all)	
burnin	number of burn-in steps for sampling	
nlter	number of total iterations for sampling	
saveFlag if results should be saved		

## Return values

lppd	log pointwise predictive density
------	----------------------------------

Definition at line 17 of file run\_lppd\_cr.m.

References computeMixtureProbability(), and logLikelihood().

Referenced by main\_sampling\_cr().

# 7.32 examples/conversion\_reaction/run\_thermIntegration\_cr.m File Reference

This function runs thermodynamic integration for the conversion reaction example.

## **Functions**

 mlhsInnerSubst< matlabtypesubstitute, Q > run\_thermIntegration\_cr (matlabtypesubstitute model\_name, matlabtypesubstitute burnin, matlabtypesubstitute nlter, matlabtypesubstitute saveFlag)

This function runs thermodynamic integration for the conversion reaction example.

## 7.32.1 Detailed Description

This function runs thermodynamic integration for the conversion reaction example.

#### 7.32.2 Function Documentation

7.32.2.1 mlhsInnerSubst< matlabtypesubstitute, Q > run\_thermIntegration\_cr ( matlabtypesubstitute model\_name, matlabtypesubstitute burnin, matlabtypesubstitute nlter, matlabtypesubstitute saveFlag )

This function runs thermodynamic integration for the conversion reaction example.

#### **USAGE**

Q = run\_thermIntegration\_cr(model\_name,burnin,nlter,saveFlag)

## **Parameters**

model_name	string indicating model (RRE_timedep,RRE_subpop,RRE_onlyone,SP_k1,SP_k2,	
	SP_k3,SP_k1k2,SP_k1k3,SP_k2k3, <b>or</b> SP_all)	
burnin	number of burn-in steps for sampling	
nlter	number of total iterations for sampling	
saveFlag	if results should be saved	

#### Return values

Q	log marginal likelihood
---	-------------------------

Definition at line 17 of file run\_thermIntegration\_cr.m.

References logLikelihood().

Referenced by main\_sampling\_cr().

# 7.33 examples/conversion\_reaction/sclogLikelihood\_cr.m File Reference

This function provides the likelihood for the optimization of the single cell trajectory in the conversion reaction example.

## **Functions**

mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, J >,mlhsInnerSubst< matlabtypesubstitute, dJ > sclogLikelihood\_cr (matlabtypesubstitute t, matlabtypesubstitute y, matlabtypesubstitute xi, matlabtypesubstitute k2, matlabtypesubstitute m\_k3, matlabtypesubstitute sigma\_k3, matlabtypesubstitute sigma\_noise, matlabtypesubstitute w, matlabtypesubstitute k1\_1, matlabtypesubstitute k1\_2, matlabtypesubstitute time-point)

This function provides the likelihood for the optimization of the single cell trajectory in the conversion reaction example.

#### 7.33.1 Detailed Description

This function provides the likelihood for the optimization of the single cell trajectory in the conversion reaction example.

#### 7.33.2 Function Documentation

7.33.2.1 mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, J>,mlhsInnerSubst< matlabtypesubstitute, dJ>> sclogLikelihood\_cr ( matlabtypesubstitute t, matlabtypesubstitute y, matlabtypesubstitute xi, matlabtypesubstitute k2, matlabtypesubstitute m\_k3, matlabtypesubstitute sigma\_k3, matlabtypesubstitute sigma\_noise, matlabtypesubstitute w, matlabtypesubstitute k1\_1, matlabtypesubstitute k1\_2, matlabtypesubstitute timepoint )

This function provides the likelihood for the optimization of the single cell trajectory in the conversion reaction example.

#### **USAGE**

[J,dJ] = sclogLikelihood\_cr(t,y,xi,k2,m\_k3,sigma\_k3,sigma\_noise,w,k1\_1,k1\_2,timepoint)

#### **Parameters**

t	time for simulation	
У	data	
xi	single-cell parameter vector which is optimized	
k2	pre-optimized parameter value for k2	
m_k3	pre-optimized parameter value for m_k3	
sigma_k3	pre-optimized parameter value for sigma_k3	
sigma_noise	pre-optimized parameter value for sigma_noise	
W	pre-optimized parameter value for 2	
k1_1	pre-optimized parameter value for k1_1	
k1_2	pre-optimized parameter value for k1_2	
timepoint	on which time point the function should be evaluated, last, or first	

# Return values

ſ	J	log-likelihood value
ſ	dJ	gradient of log-likelihood functoin

Definition at line 17 of file sclogLikelihood\_cr.m.

Referenced by main\_singlecell\_prediction().

# 7.34 examples/conversion\_reaction/simulation/CR\_log\_syms.m File Reference

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

# **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > CR\_log\_syms ()

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

## 7.34.1 Detailed Description

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

#### 7.34.2 Function Documentation

7.34.2.1 mlhslnnerSubst< matlabtypesubstitute, model > CR\_log\_syms ( )

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

## **Return values**

model model struct used with amiwrap	
--------------------------------------	--

#### Generated fields of model:

Definition at line 17 of file CR log syms.m.

# 7.35 examples/conversion reaction/simulation/CR syms.m File Reference

This function defines the model of the conversion process with the linear output, which is used for the Reaction Rate Equations.

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > CR\_syms ()
 This function defines the model of the conversion process with the linear output, which is used for the Reaction Rate Equations.

## 7.35.1 Detailed Description

This function defines the model of the conversion process with the linear output, which is used for the Reaction Rate Equations.

#### 7.35.2 Function Documentation

## 7.35.2.1 mlhsInnerSubst < matlabtypesubstitute, model > CR\_syms ( )

This function defines the model of the conversion process with the linear output, which is used for the Reaction Rate Equations.

#### Return values

model model struct used with amiwra	ap
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Generated fields of model:

Definition at line 17 of file CR\_syms.m.

7.36 examples/conversion\_reaction/simulation/generate\_simFiles\_cr.m File Reference

This script generates the functions for the conversion reaction using the toolbox AMICI.

#### **Functions**

noret::substitute generate\_simFiles\_cr ()

This script generates the functions for the conversion reaction using the toolbox AMICI.

## 7.36.1 Detailed Description

This script generates the functions for the conversion reaction using the toolbox AMICI.

7.37 examples/differential\_protein\_expression/data/generate\_data\_oneStage.m File Reference

This script generates the artificial data of the differential gene protein expression.

## **Functions**

noret::substitute generate\_data\_oneStage ()

This script generates the artificial data of the differential gene protein expression.

## 7.37.1 Detailed Description

This script generates the artificial data of the differential gene protein expression.

7.38 examples/differential\_protein\_expression/main\_oneStage\_SP\_1D.m File Reference

This script generates the model for the 1-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

#### **Functions**

• noret::substitute main\_oneStage\_SP\_1D ()

This script generates the model for the 1-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

## 7.38.1 Detailed Description

This script generates the model for the 1-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

## 7.39 examples/differential protein expression/main oneStage SP 2D.m File Reference

This script generates the model for the 2-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

#### **Functions**

noret::substitute main\_oneStage\_SP\_2D ()

This script generates the model for the 2-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

## 7.39.1 Detailed Description

This script generates the model for the 2-dimensional measurements of the differential gene expression example using the sigma point approximation. The parameters are estimated and also the profile likelihoods are calculated using the toolbox PESTO.

## 7.40 examples/differential\_protein\_expression/plot\_fit\_oneStage.m File Reference

This script visualizes the model fit for the two-dimensional data.

## **Functions**

noret::substitute plot\_fit\_oneStage ()

This script visualizes the model fit for the two-dimensional data.

# 7.40.1 Detailed Description

This script visualizes the model fit for the two-dimensional data.

# 7.41 examples/differential\_protein\_expression/plot\_uncertainty\_oneStage.m File Reference

This script visualizes the confidence intervals for the one- and the two-dimensional models.

#### **Functions**

noret::substitute plot\_uncertainty\_oneStage ()
 This script visualizes the confidence intervals for the one- and the two-dimensional models.

#### 7.41.1 Detailed Description

This script visualizes the confidence intervals for the one- and the two-dimensional models.

7.42 examples/differential\_protein\_expression/simulation/generate\_simFile\_oneStage.m File Reference

Compilation of one stage simulation file.

## **Functions**

noret::substitute generate\_simFile\_oneStage ()
 Compilation of one stage simulation file.

## 7.42.1 Detailed Description

Compilation of one stage simulation file.

# 7.43 examples/differential\_protein\_expression/simulation/oneStage\_syms.m File Reference

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > oneStage\_syms ()
 This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

#### 7.43.1 Detailed Description

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

## 7.43.2 Function Documentation

# 7.43.2.1 mlhsInnerSubst< matlabtypesubstitute, model > oneStage\_syms ( )

This function defines the model of the conversion process with the logarithm of the output, which are used for the sigma point approximation.

#### Return values

model model struct used with amiwra	ap
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#### Generated fields of model:

Definition at line 17 of file oneStage\_syms.m.

## 7.44 examples/ECM differences/data/load datasets PDL Coll.m File Reference

Script for loading the datasets of extracellular scaffolds poly-D-lysin (PDL) and Collagen I (Coll).

#### **Functions**

noret::substitute load\_datasets\_PDL\_Coll ()
 Script for loading the datasets of extracellular scaffolds poly-D-lysin (PDL) and Collagen I (Coll).

## 7.44.1 Detailed Description

Script for loading the datasets of extracellular scaffolds poly-D-lysin (PDL) and Collagen I (Coll).

## 7.45 examples/ECM\_differences/generate\_ECM\_models.m File Reference

This function generates the 128 hierarchical models accounting for all possible differences between the extracellular scaffolds. The underlying model for each scaffolds assumes inter- and intra-subpopulation variability of TrkA activity and cell-to-cell variability of relative Erk1/2 levels.

## **Functions**

noret::substitute generate\_ECM\_models ()

This function generates the 128 hierarchical models accounting for all possible differences between the extracellular scaffolds. The underlying model for each scaffolds assumes inter- and intra-subpopulation variability of TrkA activity and cell-to-cell variability of relative Erk1/2 levels.

# 7.45.1 Detailed Description

This function generates the 128 hierarchical models accounting for all possible differences between the extracellular scaffolds. The underlying model for each scaffolds assumes inter- and intra-subpopulation variability of TrkA activity and cell-to-cell variability of relative Erk1/2 levels.

## 7.46 examples/ECM\_differences/main\_ECM\_differences.m File Reference

Main script for the analysis of the influence of extracellular scaffolds on pain signaling in sensory neurons.

#### **Functions**

noret::substitute main\_ECM\_differences ()
 Main script for the analysis of the influence of extracellular scaffolds on pain signaling in sensory neurons.

## 7.46.1 Detailed Description

Main script for the analysis of the influence of extracellular scaffolds on pain signaling in sensory neurons.

# 7.47 examples/ECM\_differences/plot\_ECM\_fit.m File Reference

Visualization script for the results of the influence of extracellular scaffolds on pain signaling in sensory neurons.

#### **Functions**

noret::substitute plot\_ECM\_fit ()
 Visualization script for the results of the influence of extracellular scaffolds on pain signaling in sensory neurons.

#### 7.47.1 Detailed Description

Visualization script for the results of the influence of extracellular scaffolds on pain signaling in sensory neurons.

# 7.48 examples/ECM\_differences/plot\_ECM\_ranks.m File Reference

Visualization script for ranking of the models and differences.

# **Functions**

noret::substitute plot\_ECM\_ranks ()
 Visualization script for ranking of the models and differences.

#### 7.48.1 Detailed Description

Visualization script for ranking of the models and differences.

# 7.49 examples/ECM\_differences/plot\_ECM\_valid.m File Reference

Visualization script for the validation of the TrkA and Erk differences.

## **Functions**

noret::substitute plot\_ECM\_valid ()
 Visualization script for the validation of the TrkA and Erk differences.

## 7.49.1 Detailed Description

Visualization script for the validation of the TrkA and Erk differences.

## 7.50 examples/ECM\_differences/run\_fittings\_ECM.m File Reference

This function performs optimization for the all model accounting for differences between PDL and Coll.

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, parameters > run\_fittings\_ECM ()
 This function performs optimization for the all model accounting for differences between PDL and Coll.

## 7.50.1 Detailed Description

This function performs optimization for the all model accounting for differences between PDL and Coll.

## 7.50.2 Function Documentation

## 7.50.2.1 mlhslnnerSubst< matlabtypesubstitute, parameters > run\_fittings\_ECM ( )

This function performs optimization for the all model accounting for differences between PDL and Coll.

## Return values

parameters	struct of parameters for each of the 128 models obtained by getMultiStarts.m

# Generated fields of parameters:

Definition at line 17 of file run\_fittings\_ECM.m.

References collectConditions(), and logLikelihood().

Referenced by main\_ECM\_differences().

# 7.51 examples/ECM\_differences/run\_profile\_ECM.m File Reference

This function calculates the profile likelihoods for the final model accounting for differences in TrkA activity, Erk levels and Erk inactivation.

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, parameters > run\_profile\_ECM ()
 This function calculates the profile likelihoods for the final model accounting for differences in TrkA activity, Erk levels and Erk inactivation.

## 7.51.1 Detailed Description

This function calculates the profile likelihoods for the final model accounting for differences in TrkA activity, Erk levels and Erk inactivation.

7.52 examples/subpopulation\_differences/dephosphorylation/exp\_decay.m File Reference

Likelihood function for the fit of the dephosphorylation rate.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, J > exp\_decay (matlabtypesubstitute k5, matlabtypesubstitute t, matlabtypesubstitute pErk)

Likelihood function for the fit of the dephosphorylation rate.

## 7.52.1 Detailed Description

Likelihood function for the fit of the dephosphorylation rate.

7.53 examples/subpopulation differences/dephosphorylation/import dephospho data.m File Reference

Script for the import of the dephosphorylation data.

#### **Functions**

noret::substitute import\_dephospho\_data ()
 Script for the import of the dephosphorylation data.

# 7.53.1 Detailed Description

Script for the import of the dephosphorylation data.

7.54 examples/subpopulation\_differences/dephosphorylation/main\_analysis\_dephospho.m File Reference

Main script for the analysis of the dephosphorylation data.

## **Functions**

noret::substitute main\_analysis\_dephospho ()
 Main script for the analysis of the dephosphorylation data.

## 7.54.1 Detailed Description

Main script for the analysis of the dephosphorylation data.

7.55 examples/subpopulation\_differences/dephosphorylation/plot\_subpop\_dephoshp\_supplement.m File Reference

Visualization script for the dephosphorylation analysis.

#### **Functions**

noret::substitute plot\_subpop\_dephoshp\_supplement ()
 Visualization script for the dephosphorylation analysis.

## 7.55.1 Detailed Description

Visualization script for the dephosphorylation analysis.

7.56 examples/subpopulation\_differences/generate\_nosubpop\_file.m File Reference

Generate file for model without any subpopulations.

#### **Functions**

noret::substitute generate\_nosubpop\_file ()
 Generate file for model without any subpopulations.

# 7.56.1 Detailed Description

Generate file for model without any subpopulations.

7.57 examples/subpopulation\_differences/generate\_subpop\_files.m File Reference

Generation of all models accounting for subpopulation differences.

## **Functions**

noret::substitute generate\_subpop\_files ()
 Generation of all models accounting for subpopulation differences.

## 7.57.1 Detailed Description

Generation of all models accounting for subpopulation differences.

# 7.58 examples/subpopulation\_differences/generate\_subpop\_TrkA.m File Reference

Generation of final model including differences in TrkA levels.

## **Functions**

noret::substitute generate\_subpop\_TrkA ()
 Generation of final model including differences in TrkA levels.

## 7.58.1 Detailed Description

Generation of final model including differences in TrkA levels.

# 7.59 examples/subpopulation\_differences/main\_subpopulation\_analysis.m File Reference

Script for the analysis of subpopulation differences in sensory neurons cultured on poly-D-lysine.

#### **Functions**

noret::substitute main\_subpopulation\_analysis ()
 Script for the analysis of subpopulation differences in sensory neurons cultured on poly-D-lysine.

## 7.59.1 Detailed Description

Script for the analysis of subpopulation differences in sensory neurons cultured on poly-D-lysine.

## 7.60 examples/subpopulation\_differences/plot\_subpop\_fit.m File Reference

Visualization script for the fits of cells on poly-D-lysine.

#### **Functions**

noret::substitute plot\_subpop\_fit ()
 Visualization script for the fits of cells on poly-D-lysine.

#### 7.60.1 Detailed Description

Visualization script for the fits of cells on poly-D-lysine.

# 7.61 examples/subpopulation\_differences/plot\_subpop\_profiles.m File Reference

Visualization script for the profile likelihoods.

#### **Functions**

noret::substitute plot\_subpop\_profiles ()
 Visualization script for the profile likelihoods.

# 7.61.1 Detailed Description

Visualization script for the profile likelihoods.

# 7.62 examples/subpopulation\_differences/plot\_subpop\_valid.m File Reference

Visualization script for the validation Figure 5D-F of Loos et al., Cell Systems (2018).

#### **Functions**

noret::substitute plot\_subpop\_valid ()
 Visualization script for the validation Figure 5D-F of Loos et al., Cell Systems (2018).

# 7.62.1 Detailed Description

Visualization script for the validation Figure 5D-F of Loos et al., Cell Systems (2018).

# 7.63 examples/subpopulation\_differences/run\_fitting\_subpop.m File Reference

This function optimizes the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, parameters > run\_fitting\_subpop (matlabtypesubstitute icomb)
 This function optimizes the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

## 7.63.1 Detailed Description

This function optimizes the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

#### 7.63.2 Function Documentation

7.63.2.1 mlhslnnerSubst < matlabtypesubstitute, parameters > run\_fitting\_subpop ( matlabtypesubstitute icomb )

This function optimizes the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

Generated fields of parameters:

Definition at line 17 of file run\_fitting\_subpop.m.

References collectConditions(), and logLikelihood().

# 7.64 examples/subpopulation\_differences/run\_logmarg\_subpop.m File Reference

This function calculates the log marginals for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, logmarg > run\_logmarg\_subpop (matlabtypesubstitute icomb)
 This function calculates the log marginals for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

## 7.64.1 Detailed Description

This function calculates the log marginals for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

## 7.65 examples/subpopulation differences/run lppd subpop.m File Reference

This function calculates the log pointwise predictive density for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, lppd > run\_lppd\_subpop (matlabtypesubstitute icomb)
 This function calculates the log pointwise predictive density for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

## 7.65.1 Detailed Description

This function calculates the log pointwise predictive density for the model of NGF-induced Erk1/2 signaling accounting for the differences in subpopulations denoted by icomb.

7.66 exa	amples/subpopulation	differences/simulation/generate	simFile	ErkSignaling.m	File Refere	ence
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This script generates the functions for the NGF-induced Erk1/2 signaling using the toolbox AMICI.

#### **Functions**

noret::substitute generate\_simFile\_ErkSignaling ()
 This script generates the functions for the NGF-induced Erk1/2 signaling using the toolbox AMICI.

## 7.66.1 Detailed Description

This script generates the functions for the NGF-induced Erk1/2 signaling using the toolbox AMICI.

7.67 examples/subpopulation\_differences/simulation/ODEmodel\_syms\_sPsET\_loglog.m File Reference

This function provides the model of NGF-induced Erk1/2 signaling. It is compiled using AMICI.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > ODEmodel\_syms\_sPsET\_loglog ()
 This function provides the model of NGF-induced Erk1/2 signaling. It is compiled using AMICI.

## 7.67.1 Detailed Description

This function provides the model of NGF-induced Erk1/2 signaling. It is compiled using AMICI.

7.67.2 Function Documentation

7.67.2.1 mlhsInnerSubst< matlabtypesubstitute, model > ODEmodel\_syms\_sPsET\_loglog ( )

This function provides the model of NGF-induced Erk1/2 signaling. It is compiled using AMICI.

Generated fields of model:

Definition at line 17 of file ODEmodel\_syms\_sPsET\_loglog.m.

7.68 examples/two\_stage\_exandintrinsic/data/generate\_data\_twostage.m File Reference

This script generates the data for the two stage gene expression example using the Stochastic Simulation Algorithm (SSA) implemented in the toolbox CERENA.

#### **Functions**

• noret::substitute generate\_data\_twostage ()

This script generates the data for the two stage gene expression example using the Stochastic Simulation Algorithm (SSA) implemented in the toolbox CERENA.

#### 7.68.1 Detailed Description

This script generates the data for the two stage gene expression example using the Stochastic Simulation Algorithm (SSA) implemented in the toolbox CERENA.

## 7.69 examples/two\_stage\_exandintrinsic/main\_MA.m File Reference

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

#### **Functions**

• noret::substitute main MA()

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

#### 7.69.1 Detailed Description

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

# 7.70 examples/two\_stage\_exandintrinsic/main\_MA\_1subpop.m File Reference

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

#### **Functions**

noret::substitute main\_MA\_1subpop ()

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

# 7.70.1 Detailed Description

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

# 7.71 examples/two\_stage\_exandintrinsic/main\_MA\_1subpop\_extrinsic.m File Reference

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

#### **Functions**

• noret::substitute main\_MA\_1subpop\_extrinsic ()

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

#### 7.71.1 Detailed Description

This script generates the model incorporating the moment approximation, estimates the parameters and calculates the profile likelihoods.

# 7.72 examples/two\_stage\_exandintrinsic/main\_RRE.m File Reference

This script generates the model incorporating only the means by reaction rate equations, estimates the parameters and calculates the profile likelihoods.

#### **Functions**

noret::substitute main\_RRE ()

This script generates the model incorporating only the means by reaction rate equations, estimates the parameters and calculates the profile likelihoods.

# 7.72.1 Detailed Description

This script generates the model incorporating only the means by reaction rate equations, estimates the parameters and calculates the profile likelihoods.

## 7.73 examples/two stage exandintrinsic/simulation/compile simFiles geneExp.m File Reference

This script generate the simulation files for the example of two stage gene expression including intrinsic and extrinsic noise. This requires the MATLAB Toolbox CERENA. The \_syms.m files are generate using CERENA and the model definition files modelDef\_geneExp.m for the reaction rate equations and the moment approximation, and model Def\_geneExp\_extrinsic.m for the moment approximation with additional extrinsic noise.

## **Functions**

noret::substitute compile\_simFiles\_geneExp ()

This script generate the simulation files for the example of two stage gene expression including intrinsic and extrinsic noise. This requires the MATLAB Toolbox CERENA. The \_syms.m files are generate using CERENA and the model definition files modelDef\_geneExp.m for the reaction rate equations and the moment approximation, and modelDef← \_geneExp\_extrinsic.m for the moment approximation with additional extrinsic noise.

#### 7.73.1 Detailed Description

This script generate the simulation files for the example of two stage gene expression including intrinsic and extrinsic noise. This requires the MATLAB Toolbox CERENA. The \_syms.m files are generate using CERENA and the model definition files modelDef\_geneExp.m for the reaction rate equations and the moment approximation, and model Def\_geneExp\_extrinsic.m for the moment approximation with additional extrinsic noise.

7.74 examples/two\_stage\_exandintrinsic/simulation/MEC\_2\_LD\_2\_c\_geneExp\_extrinsic\_syms.m File Reference

This function provides the model definition for the moment approximation with additional extrinsic noise of the two stage gene expression. It is generated by the toolbox CERENA.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > MEC\_2\_LD\_2\_c\_geneExp\_extrinsic\_syms (matlabtype-substitute varargin)

This function provides the model definition for the moment approximation with additional extrinsic noise of the two stage gene expression. It is generated by the toolbox CERENA.

#### 7.74.1 Detailed Description

This function provides the model definition for the moment approximation with additional extrinsic noise of the two stage gene expression. It is generated by the toolbox CERENA.

## 7.74.2 Function Documentation

7.74.2.1 mlhslnnerSubst< matlabtypesubstitute, model > MEC\_2\_LD\_2\_c\_geneExp\_extrinsic\_syms ( matlabtypesubstitute varargin )

This function provides the model definition for the moment approximation with additional extrinsic noise of the two stage gene expression. It is generated by the toolbox CERENA.

Generated fields of model:

Definition at line 17 of file MEC\_2\_LD\_2\_c\_geneExp\_extrinsic\_syms.m.

7.75 examples/two\_stage\_exandintrinsic/simulation/MEC\_2\_LD\_2\_c\_geneExp\_MA\_syms.m File Reference

This function provides the model definition for the moment approximation of the two stage gene expression. It is generated by the toolbox CERENA.

**Functions** 

mlhsInnerSubst< matlabtypesubstitute, model > MEC\_2\_LD\_2\_c\_geneExp\_MA\_syms (matlabtypesubstitute varargin)

This function provides the model definition for the moment approximation of the two stage gene expression. It is generated by the toolbox CERENA.

#### 7.75.1 Detailed Description

This function provides the model definition for the moment approximation of the two stage gene expression. It is generated by the toolbox CERENA.

#### 7.75.2 Function Documentation

7.75.2.1 mlhsInnerSubst < matlabtypesubstitute, model > MEC\_2\_LD\_2\_c\_geneExp\_MA\_syms ( matlabtypesubstitute *varargin* )

This function provides the model definition for the moment approximation of the two stage gene expression. It is generated by the toolbox CERENA.

Generated fields of model:

Definition at line 17 of file MEC\_2\_LD\_2\_c\_geneExp\_MA\_syms.m.

7.76 examples/two\_stage\_exandintrinsic/simulation/modelDef\_geneExp.m File Reference

Model definition of the reaction network for the two stage gene expression.

#### **Functions**

noret::substitute modelDef\_geneExp ()

Model definition of the reaction network for the two stage gene expression.

# 7.76.1 Detailed Description

Model definition of the reaction network for the two stage gene expression.

7.77 examples/two\_stage\_exandintrinsic/simulation/modelDef\_geneExp\_extrinsic.m File Reference

Model definition of the reaction network for the two stage gene expression with additional extrinsic noise.

#### **Functions**

noret::substitute modelDef\_geneExp\_extrinsic ()
 Model definition of the reaction network for the two stage gene expression with additional extrinsic noise.

## 7.77.1 Detailed Description

Model definition of the reaction network for the two stage gene expression with additional extrinsic noise.

7.78 examples/two\_stage\_exandintrinsic/simulation/RRE\_geneExp\_RRE\_syms.m File Reference

This function provides the model definition for the reaction rate equations of the two stage gene expression. It is generated by the toolbox CERENA.

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, model > RRE\_geneExp\_RRE\_syms (matlabtypesubstitute varargin)
 This function provides the model definition for the reaction rate equations of the two stage gene expression. It is generated by the toolbox CERENA.

## 7.78.1 Detailed Description

This function provides the model definition for the reaction rate equations of the two stage gene expression. It is generated by the toolbox CERENA.

7.78.2 Function Documentation

7.78.2.1 mlhsInnerSubst< matlabtypesubstitute, model > RRE\_geneExp\_RRE\_syms ( matlabtypesubstitute varargin )

This function provides the model definition for the reaction rate equations of the two stage gene expression. It is generated by the toolbox CERENA.

Generated fields of model:

Definition at line 17 of file RRE\_geneExp\_RRE\_syms.m.

## 7.79 generateODEMM.m File Reference

This function generates a file that defines the ODE-constrained mixture model.

#### **Functions**

mlhsInnerSubst< matlabtypesubstitute, varargout > generateODEMM (matlabtypesubstitute D, matlabtypesubstitute D, matlabtypesubstitute M, matlabtypesubstitute parameters, matlabtypesubstitute conditions, matlabtypesubstitute varargin)

This function generates a file that defines the ODE-constrained mixture model.

- mlhsInnerSubst< matlabtypesubstitute, retstr > mtoc\_subst\_generateODEMM\_m\_tsbus\_cotm\_←
   replace\_xi\_x\_u (matlabtypesubstitute symexpr)
- mlhsInnerSubst< matlabtypesubstitute, str\_dzdxi > mtoc\_subst\_generateODEMM\_m\_tsbus\_cotm
   \_getStrDerivative2Terms (matlabtypesubstitute sym\_expr, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute xi)
- mlhsInnerSubst< matlabtypesubstitute, str\_dzdxi > mtoc\_subst\_generateODEMM\_m\_tsbus\_cotm\_

   getStrDerivative3Terms (matlabtypesubstitute deriv\_name, matlabtypesubstitute sym\_expr, matlabtypesubstitute s, matlabtypesubstitute e, matlabtypesubstitute x, matlabtypesubstitute dxdxi, matlabtypesubstitute sigma, matlabtypesubstitute dsigmadxi, matlabtypesubstitute xi)

#### 7.79.1 Detailed Description

This function generates a file that defines the ODE-constrained mixture model.

#### 7.79.2 Function Documentation

7.79.2.1 mlhslnnerSubst < matlabtypesubstitute, varargout > generateODEMM ( matlabtypesubstitute *D*, matlabtypesubstitute *M*, matlabtypesubstitute *parameters*, matlabtypesubstitute *conditions*, matlabtypesubstitute *varargin* )

This function generates a file that defines the ODE-constrained mixture model.

## USAGE

M = generateODEMM(D,M,parameters,conditions,options)

#### **Parameters**

D	data struct	
М	model struct	
parameters	parameters struct	
conditions	conditions struct obtained by collectConditions.m	
varargin		
	1 generateODEMM (, options )	
	Required Parameters for varargin:	
	options (options for the generation)	

## Required fields of M:

- name -- name of the model
- model -- simulation file with input (T,theta,u) (e.g., generated by amiwrap of the toolbox AMICI), the first output needs to be the status of thesimulation (whether it failed or not) the 4th the simulation output, and the 6th the sensitivities

• sim\_type -- simulation type ('RRE' for a mechanistic description of the mean, e.g., by reaction rate equations, 'HO' for a mechanistic description of the mean and covariance, e.g., by moment-closure approximation or sigma-point approximation)

- n\_subpop -- number of subpopulations
- distribution { s,e} distribution assumption
  - = 'norm' for normal distribution assumption
  - = 'logn\_median' for log-normal distribution assumption when mean of simulation linked to median of distribution
  - = 'logn\_mean' for log-normal distribution assumption when mean of simulation is % linked to mean of distribution
- mean\_ind{s,e} indices of simulation output describing the mean of the measurand(s) of experiment
- var\_ind{s,e} indices of simulation output describing the variance (empty if RREs used)
- u (s,e) input vector describing differences between subpopulations and experiments
- sym -- symbolic description of properties of the model with fields
  - w{s,e}: weights of subpopulation s in experiment e
  - theta: parameter needed for simulation of individual subpopulations
  - scaling{r,e}: scaling factor for replicate r in experiment e, if the replicates are not considered seperately, use r=1
  - offset{r,e}: offset parameter for replicate r in experiment e

#### Required fields of D:

• conditions -- obtained by collectConditions.m

#### Required fields of parameters:

## Optional fields of options:

- write\_parameter -- write parameter definition in file (true by default)
- measurement\_noise -- if measurement noise is included
  - = true
  - = false (default)
- replicates -- if individual replicates are modeled = true
  - = false (default)
- sigmas -- parametrization of the variance in case of using only a mechanistic description of the mean
  - = 'condition-dependent': (default) assign sigma for every time point
  - = 'time-independent': sigma stays the same for subpopulation and some dosage
  - = 'only-one': only one sigma for everything

## Definition at line 17 of file generateODEMM.m.

Referenced by generate\_ECM\_models(), generate\_nosubpop\_file(), generate\_subpop\_files(), generate\_subpop\_index(), generate\_subpop\_index(), generate\_subpop\_index(), generate\_subpop\_index(), generate\_subpop\_index(), generate\_subpop\_files(), generate\_subpop\_files(), generate\_subpop\_index(), generate\_subpop\_files(), generate

## 7.80 getLognMeanVar.m File Reference

This function calculations the mean and variances, and the corresponding derivatives of a multivariate log-normal distribution given the parameters  $\mu$  and  $\Sigma$ .

#### **Functions**

mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, Zout >,mlhsInnerSubst< matlabtypesubstitute, varargout >> getLognMeanVar (matlabtypesubstitute Z, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin)

This function calculations the mean and variances, and the corresponding derivatives of a multivariate log-normal distribution given the parameters  $\mu$  and  $\Sigma$ .

#### 7.80.1 Detailed Description

This function calculations the mean and variances, and the corresponding derivatives of a multivariate log-normal distribution given the parameters  $\mu$  and  $\Sigma$ .

#### 7.80.2 Function Documentation

7.80.2.1 mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, Zout >,mlhsInnerSubst< matlabtypesubstitute, varargout > > getLognMeanVar ( matlabtypesubstitute Z, matlabtypesubstitute n\_dim, matlabtypesubstitute varargin )

This function calculations the mean and variances, and the corresponding derivatives of a multivariate log-normal distribution given the parameters  $\mu$  and  $\Sigma$ .

#### **USAGE**

```
[Zout] = getLognMeanVar(Z,n_dim)
[Zout,dZdthetaout] = getLognMeanVar(Z,n_dim,dZdtheta)
```

#### **Parameters**

Z	(n_dim + n_dim(n_dim+1)/2) x n_t vector with $\mu$ and $\Sigma$
n_dim	dimension of the multivariate log-normal distribution
varargin	
	1 getLognMeanVar (, dZdtheta )
	Required Parameters for varargin:
	• dZdtheta ((n_dim + n_dim(n_dim+1)/2) x n_theta x n_t derivative)

## Return values

Zout	(n_dim + n_dim(n_dim+1)/2) x n_t vector with mean and coariance
dZdthetaout	derivative of Zout

Definition at line 17 of file getLognMeanVar.m.

Referenced by logLikelihood(), and plotODEMM().

# 7.81 getRREsigmas.m File Reference

This function defines the parameters needed for the parametrization of the variances in case Reaction Rate Equations are used for the mechanistic description of the means.

## **Functions**

• mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, parameters >,mlhsInnerSubst< matlabtypesubstitute, conditions >,mlhsInnerSubst< matlabtypesubstitute, varargout >> getRREsigmas (matlabtypesubstitute parameters, matlabtypesubstitute conditions, matlabtypesubstitute varargin)

This function defines the parameters needed for the parametrization of the variances in case Reaction Rate Equations are used for the mechanistic description of the means.

#### 7.81.1 Detailed Description

This function defines the parameters needed for the parametrization of the variances in case Reaction Rate Equations are used for the mechanistic description of the means.

#### 7.81.2 Function Documentation

7.81.2.1 mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, parameters >,mlhsInnerSubst< matlabtypesubstitute, conditions >,mlhsInnerSubst< matlabtypesubstitute, varargout >> getRREsigmas ( matlabtypesubstitute parameters, matlabtypesubstitute conditions, matlabtypesubstitute varargin )

This function defines the parameters needed for the parametrization of the variances in case Reaction Rate Equations are used for the mechanistic description of the means.

## **USAGE**

[parameters,conditions] = getRREsigmas(parameters,conditions)
[parameters,conditions,D] = getRREsigmas(parameters,conditions,options,D,M)

## **Parameters**

parameters	parameters struct
conditions	conditions struct (see collectConditions.m)
varargin	
	1 getRREsigmas (, options, D, M )
	Required Parameters for varargin:
	• options
	D data struct (see logLikelihood.m)
	M model struct (see generateODEMM.m)

## Return values

parameters	updated parameters struct
conditions	updated conditions struct
D	updated data struct

# Required fields of parameters:

## Optional fields of options:

- sigmas --
  - = 'condition-dependent': (default) assign sigma for every time point
  - = 'time-dependent': one sigma for every subpopulation and time point
  - = 'only-one': only one sigma for everything
  - = 'subpopulation-specific': for every subpopulation one sigma
- boundaries -- boundaries for optimization for the sigma parameters with fields
  - min
  - max

## Generated fields of parameters:

• names -- names for sigma parameters are added

## Generated fields of D:

```
    sigma -- (if n_dim = 1)
    Sigma -- (if n_dim = 2)
```

Definition at line 17 of file getRREsigmas.m.

Referenced by main\_RRE(), and models\_RRE().

# 7.82 getScalingFactors.m File Reference

Calculates scaling factors for replicates such that the distance between the means in log-space are minimal.

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, s > getScalingFactors (matlabtypesubstitute varargin)
 Calculates scaling factors for replicates such that the distance between the means in log-space are minimal.

#### 7.82.1 Detailed Description

Calculates scaling factors for replicates such that the distance between the means in log-space are minimal.

#### 7.82.2 Function Documentation

 $7.82.2.1 \quad \text{mlhsInnerSubst} < \text{matlabtypesubstitute}, \ \text{s} > \text{getScalingFactors} \ ( \ \text{matlabtypesubstitute} \ \textit{varargin} \ )$ 

Calculates scaling factors for replicates such that the distance between the means in log-space are minimal.

## **USAGE**

```
\begin{split} s &= getScalingFactors(\log, ExpC) \\ s &= getScalingFactors(\log, ExpC_1, ExpC_2) \end{split}
```

## **Parameters**

# varargin 1 getScalingFactors ( ExpC ) Required Parameters for varargin: • ExpC struct of experiments

## **Return values**

s (1 x n\_r) vector including scaling factor for every replicate

## Required fields of ExpC:

- name -- string specifying the conditions
- time -- time point of measurement
- stimulus -- stimulus for measurement
- replicate -- struct of replicates
  - name: string specifying the replicate
  - measurands: names of measurands
  - ndata: matrices under different conditions (one row represents one observed cell with the data in the order of the measurands. The different rows provide measurement data for different cells)

Definition at line 17 of file getScalingFactors.m.

Referenced by load datasets PDL Coll().

# 7.83 getSigmaPointApp\_status\_mod.m File Reference

Modified version of the getSigmaPointApp.m function of the SPToolbox.

#### **Functions**

mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, status >,mlhsInnerSubst< matlabtypesubstitute, SP > getSigmaPointApp\_status\_mod (matlabtypesubstitute varargin)

Modified version of the getSigmaPointApp.m function of the SPToolbox.

## 7.83.1 Detailed Description

Modified version of the getSigmaPointApp.m function of the SPToolbox.

## 7.83.2 Function Documentation

7.83.2.1 mlhsSubst< mlhsInnerSubst< matlabtypesubstitute, status >,mlhsInnerSubst< matlabtypesubstitute, SP >> getSigmaPointApp\_status\_mod ( matlabtypesubstitute *varargin* )

Modified version of the getSigmaPointApp.m function of the SPToolbox.

Generated fields of SP:

Definition at line 17 of file getSigmaPointApp\_status\_mod.m.

Referenced by testSigmaPointApp\_mod().

## 7.84 install\_ODEMM.m File Reference

Script that adds the required paths to the MATLAB search path.

## **Functions**

noret::substitute install\_ODEMM ()
 Script that adds the required paths to the MATLAB search path.

## 7.84.1 Detailed Description

Script that adds the required paths to the MATLAB search path.

## 7.85 load\_plot\_settings.m File Reference

Functions to set font sizes and colors for the visualization.

#### **Functions**

noret::substitute load\_plot\_settings ()
 Functions to set font sizes and colors for the visualization.

#### 7.85.1 Detailed Description

Functions to set font sizes and colors for the visualization.

# 7.86 logLikelihood.m File Reference

This function evaluates the likelihood function for a given model, data and parameter vector.

## **Functions**

• mlhsInnerSubst< matlabtypesubstitute, varargout > logLikelihood (matlabtypesubstitute xi, matlabtypesubstitute Xi, matlabtypesubstitute Varargin)

This function evaluates the likelihood function for a given model, data and parameter vector.

## 7.86.1 Detailed Description

This function evaluates the likelihood function for a given model, data and parameter vector.

#### 7.86.2 Function Documentation

7.86.2.1 mlhsInnerSubst< matlabtypesubstitute, varargout > logLikelihood ( matlabtypesubstitute *xi*, matlabtypesubstitute *M*, matlabtypesubstitute *D*, matlabtypesubstitute *varargin* )

This function evaluates the likelihood function for a given model, data and parameter vector.

## **USAGE**

```
[...] = logLikelihood(xi,M,D,options,conditions,I)
[...] = logLikelihood(xi,M,D,options,conditions)
[...] = logLikelihood(xi,M,D,options)
[logL] = logLikelihood(...)
[logL, dlogL] = logLikelihood(...)
```

## **Parameters**

xi	parameter values
М	model struct
D	data struct
varargin	
	1 logLikelihood (, options, conditions, I )
	Required Parameters for varargin:
	options struct
	<ul> <li>conditions generated by function collectConditions.m</li> </ul>
	I indices for which of the data the likelihood function should be evaluated

## Return values

logL	log-likelihood value
dlogL	gradient of log-likelihood function

# Required fields of M:

• n\_subpop -- number of subpopulations

- model -- simulation file with input (T,theta,u) (e.g., generated by amiwrap), the first output needs to be the status of the simulation, the 4th the simulation output and the 6th the sensitivities (n\_t x n\_obs x n theta)
- mean\_ind -- indices of output for mean
- var\_ind -- indices of output for variances (empty if using RREs)
- theta -- parameters needed for simulation dependend on xi and u the following fields of M are generated by generate ODEMM
- distribution { s,e} distribution assumption
  - = 'norm': normal distribution assumption
  - = 'logn\_median': log-normal distribution assumption, mean of simulation linked to median of distribution
  - = 'logn mean': log-normal distribution assumption, mean of simulation linked to mean of distribution

The following fields are automatically added by generateODEMM.m

- dthetadxi -- gradient of theta
- mu { s,e} specification of mixture parameter mu for subpopulation s and experiment e
- dmudxi{s,e} gradient of mu
- sigma (s,e) specification of mixture parameter σ (M.Sigma in multivariate case (covariance matrix))
- dsigmadxi { s,e} gradient of sigma (M.dSigmadxi in multivariate case)
- w { s,e} specification of weights  $w_s$
- dwdxi { s,e} gradient of weights
- scaling { r,e} scaling parameter of replicate r in experiment e
- dscalingdxi{r,e} gradient of scaling
- offset { r,e} offset
- doffsetdxi{r,e} gradient of offset

# Required fields of D:

- n\_dim -- dimension of the measurements
- t -- 1 x n t vector of timepoints
- u -- n\_maxu x n\_u vector of inputs with n\_maxu: maximal number of inputs simulatenously used
- y -- n\_u x n\_t x n\_cells x n\_dim data matrix (only needed if replicates are merged and already scaled), dim is the dimension of the measurement
- c -- n\_subpop x (n\_u + n\_differences) corresponding condition (automatically added by calling collectCondition.m)
- replicate(r).y n\_u x n\_t x n\_cells x n\_dim data matrix of replicate r in experiment e (only needed if individual replicates should be fitted)

# Optional fields of options:

- use\_robust -- robust calculation of mixture probability
  - = true: uses reformulation (default)
  - = false: classical calculation (not recommended)
- simulate\_musigma -- true if simulation directly provides ...
- negLogLikelihood -- true if negativev log-likelihood required
- replicates -- true if replicates are fitted individually

## Definition at line 17 of file logLikelihood.m.

References collectConditions(), computeMixtureProbability(), getLognMeanVar(), logoflognpdf(), logofmvnpdf(), and logofnormpdf().

Referenced by main\_MA(), main\_MA\_1subpop(), main\_MA\_1subpop\_extrinsic(), main\_oneStage\_SP\_1  $\leftarrow$  D(), main\_oneStage\_SP\_2D(), main\_RRE(), main\_subpopulation\_analysis(), model\_SP\_all(), model\_SP\_k1(), model\_SP\_k1(), model\_SP\_k2(), model\_SP\_k2(), model\_SP\_k2k3(), model\_SP\_k3(), model\_SP\_k3(), model\_SP\_k3(), run\_ $\leftarrow$  fitting\_subpop(), run\_fittings\_ECM(), run\_logmarg\_subpop(), run\_lppd\_subpop(), run\_profile\_EC  $\leftarrow$  M(), and run\_thermIntegration\_cr().

## 7.87 plotODEMM.m File Reference

Routine to plot the ODE-constrained mixture model.

## **Functions**

• mlhsInnerSubst< matlabtypesubstitute, varargout > plotODEMM (matlabtypesubstitute varargin)

Routine to plot the ODE-constrained mixture model.

- mlhsInnerSubst< matlabtypesubstitute, str\_dose > mtoc\_subst\_plotODEMM\_m\_tsbus\_cotm\_getStr
   — Dose (matlabtypesubstitute D, matlabtypesubstitute e, matlabtypesubstitute d)
- noret::substitute mtoc\_subst\_plotODEMM\_m\_tsbus\_cotm\_evalModel (matlabtypesubstitute xi, matlabtypesubstitute M, matlabtypesubstitute D, matlabtypesubstitute e, matlabtypesubstitute r, matlabtypesubstitute d, matlabtypesubstitute X\_c, matlabtypesubstitute options, matlabtypesubstitute conditions)
- noret::substitute mtoc\_subst\_plotODEMM\_m\_tsbus\_cotm\_evalPdf (matlabtypesubstitute M, matlabtypesubstitute D, matlabtypesubstitute e, matlabtypesubstitute d, matlabtypesubstitute k, matlabtypesubstitute options, matlabtypesubstitute legendflag, matlabtypesubstitute ind, matlabtypesubstitute lim, matlabtypesubstitute plotData)

## 7.87.1 Detailed Description

Routine to plot the ODE-constrained mixture model.

#### 7.87.2 Function Documentation

7.87.2.1 mlhsInnerSubst < matlabtypesubstitute, varargout > plotODEMM ( matlabtypesubstitute varargin )

Routine to plot the ODE-constrained mixture model.

#### USAGE

```
[...] = plotODEMM(D,M,xi)
[...] = plotODEMM(D,M,xi,options)
[...] = plotODEMM(D,M,xi,options,fh)
[fh] = plotODEMM(...)
[fh,fhm] = plotODEMM(...)
```

#### **Parameters**

varargin	
	D: data struct
	M: model struct
	xi: parameter vector
	options: plotting options
	fh: figure handle where the plots are added

#### Return values

fh	struct of function handles for each data set
fhm	struct of function handles for the plots of the marginals

Definition at line 17 of file plotODEMM.m.

References collectConditions(), and getLognMeanVar().

Referenced by main\_MA(), main\_MA\_1subpop(), main\_MA\_1subpop\_extrinsic(), main\_RRE(), plot\_cr(), plot\_cr(\to SIAppendix(), plot\_ECM\_fit(), plot\_fit\_oneStage(), and plot\_subpop\_fit().

## 7.88 printParams.m File Reference

Help function to print parameters names and values.

## **Functions**

• noret::substitute printParams (matlabtypesubstitute parameters, matlabtypesubstitute varargin)

Help function to print parameters names and values.

# 7.88.1 Detailed Description

Help function to print parameters names and values.

# 7.88.2 Function Documentation

7.88.2.1 noret::substitute printParams ( matlabtypesubstitute parameters, matlabtypesubstitute varargin )

Help function to print parameters names and values.

## **USAGE**

[] = printParams(parameters,xi)

#### **Parameters**

parameters	parameters struct
varargin	
	1 printParams (, xi )
	Required Parameters for varargin:
	xi parameter values printed together with parameter names

# Required fields of parameters:

• name -- struct with names of parameters

Definition at line 17 of file printParams.m.

# 7.89 testSigmaPointApp\_mod.m File Reference

 $Modified\ version\ of\ the\ testSigmaPointApp\_status.m\ function\ of\ the\ SPToolbox.$ 

## **Functions**

mlhsInnerSubst< matlabtypesubstitute, SP > testSigmaPointApp\_mod (matlabtypesubstitute varargin)
 Modified version of the testSigmaPointApp\_status.m function of the SPToolbox.

## 7.89.1 Detailed Description

Modified version of the testSigmaPointApp\_status.m function of the SPToolbox.

## 7.89.2 Function Documentation

7.89.2.1 mlhsInnerSubst< matlabtypesubstitute, SP > testSigmaPointApp\_mod ( matlabtypesubstitute varargin )

 $Modified\ version\ of\ the\ testSigmaPointApp\_status.m\ function\ of\ the\ SPToolbox.$ 

Generated fields of SP:

Definition at line 17 of file testSigmaPointApp\_mod.m.

References getSigmaPointApp\_status\_mod().

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