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# CSC343 Notes

Introduction to Databases

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# 1 What is Data?

- Bits that represent values, such as:
  - Numbers
  - Strings
  - Images
- What do we want to do with it?
  - Manage it!!!
- We can manage a large collection of data with files
  - We used flat files, K/V pairs
  - If you combine K/V pairs with your favorite programming language, you get a database.
  - Of course, you'll have to implement all its methods yourself.
- The first commercial databased evolved using plain text. Now, how do we deal with:
  - Duplication
  - Organization (it is incredibly hard, especially when you have more than one person)
  - You'll have to reinvent various wheels:
    - \* Search
    - \* Sort
    - \* Modify, and so on
  - None of these would be optimized

What do we do instead

- We want an efficient, optimized system that specializes in handling **inconvincibly large amounts of data**.

In fact, some of the largest databases would already cram your hard drive in a second/

## 1.1 Databases and DBMS (Database Management System)

A **DBMS** is a powerful tool that can:

- Manage large amounts of data
- Allow it to persist for long amounts of time (protect it over time from being overwritten)

Every DBMS has a data model. It describes

- Structure (lowest level: rows and columns)
- Constraints (range, types)
- Operations (find all students with grades  $\geq 85$ )

We'll be looking with the **relational data model**. This has been very widespread since it has been invented. It has been proposed as an efficient model.

## 1.2 The Relational Data Model

CSVs. Spreadsheets. They look a lot like them. The main concept is a relation. The concept of relation is borrowed from math.

A relation is a **SET** of **TUPLES**. Here's an example:

$$\{(x,y) \in \mathbb{R}^2 : x < y\}$$

That defines a relation. Every pair of values that obeys  $x < y$  will be in it.

- A **column** (attribute, field) goes vertically.

- A **row** (tuple) goes horizontally).
- A table is a set of tuples (rows) (what about the header?)

A **schema** is a namespace where we collect some relations. When we do a lot of work with databases, we are likely to have some completely different areas of interest, and this helps us organize them at the top level.

### 1.3 What does a DBMS provide

- Can **explicitly** specify the logical structure of the data
  - And **enforce** it
- Can query (ask questions and it will respond) or modify data
  - Best to keep query and modify separate
- Good performance under heavy loads
  - We're talking about billions of data. We're getting into the range of  $10^{15}$  but we're starting to push way more
- Durability of the data
  - Keep it safe and intact (data integrity)
- Concurrent access by multiple users
  - MERGE CONFLICTS!!! Us or us and our partners? We need to have ways of having concurrent access without causing a mess.
  - Suppose tables A and B are bank accounts. We have a couple of queries that remove \$100 from A and deposit that amount in B. What happens if another user checks A before the \$100 is removed and B after \$100 is deposited?
  - If you're developing databases for multiple concurrent users, you'll have to worry about this exact issue, and it's important to pay attention to it.

The architecture of a DBMS relies **heavily** on the underlying operating system. You need access to direct pieces of the operating system. The DBMS sits between users and the data itself. Sometimes, it sits between an app you write and the database.

Rather than allowing someone who is pointing and clicking on the webpage, we have a DBMS that ensures that the queries sent by the person are well-formed and efficient.

Or maybe a Python program is forming proper DBMS queries first. We rarely have an end user directly interacting with the database.

## 1.4 Relations

The cartesian product is every possible ordered tuple.

- A domain is a set of values
- Suppose  $D_1, D_2, \dots, D_n$  are domains
- $D_1 \times D_2 \times \dots$ 
  - Is the set of all tuples  $(d_1, d_2, \dots, d_n)$
  - Every combination of a value from  $D_1, D_2$ , and so on

### 1.4.1 Example of a Mathematical Relation

Let  $A = \{p, q, r, s\}, B = \{1, 2, 3\}, C = \{100, 200\}$

Anything that is a subset of  $A \times B \times C$  is a **relation** on  $A, B, C$ .

For example,  $R = \{(q, 2, 100), (s, 3, 200), (p, 1, 200)\}$  is a relation on  $A, B, C$ .

Database tables are relations. The order of rows does not matter. We can represent a table as:

$\{\text{row 1 info, row 2 info, ...}\}$

## 1.5 Relation Schemas vs. Instances

- Schema is the **definition of the structure** (constraints, restrictions)
  - A database schema is a set of relation schemas
- We have notations for expressing a relation's schema:  
`Teams(Name, Homefield, Coach)`
- An instance is a particular data in a relation. It is a snapshot of a database at a point of time.
  - Instances change **constantly**, schemas change **rarely** and are inconvenient to change.
  - A database instance is a set of relation instances
  - As soon as we put in any data into a database schema, we get an instance.
- Conventional databases store the **current version** of the data. Databases that record history are temporal databases (diff files).

## 1.6 Terminology

- Relation (table)
- Attribute (columns) or fields
- Tuple (row)
- Arity (no. of attributes / column count)
- Cardinality (no. of tuples, or rows; size of  $R$ . Usually finite)

Relations are sets; no duplicates allowed, and we don't care about the order of the tuples.

There is another model called a **bag** – sets that allow duplicates / multisets. Commercial DBMSs use this model, but for now we'll stick with relations as sets.

- PostgreSQL uses bags
- Apparently they are more efficient

## 1.7 Making Constraints

TL: DR use IDs to prevent duplicates. Until we want to do some domain or range restrictions, but that's something else.

- We have `Teams(name, homefield, coach)` and `Games(hometeam, awayteam, homegoals, awaygoals)`.
- Do we allow duplicates? Not up to us. The responsibility for that decision is not you, the domain expert (a.k.a. you'll be asking them. Don't make the decisions, do what you're ordered to).
- Suppose we want to allow duplicate names and multiple teams with the same home field.
  - The schema allows it
- The only thing that would distinguish the two teams apart is another attribute where duplicates are not allowed.
- **What if we don't want that?** We can **constrain the data**.

A constraint that forbids duplicates:

$$\nexists \text{ tuples } t_1, t_2 \text{ such that } (t_1.name = t_2.name) \\ \wedge (t_1.homefield = t_2.homefield)$$

THEN, if we know the values for  $(name, homefield)$  then we can look up any team we want.

**SUPERKEY** – a set of 1 or more attributes whose combined values are unique. No two tuples can have the same values on all these attributes.

### 1.7.1 With Courses

For example: `Course(dept, number, name, breadth)`

- If `<"csc", "343", "Intro Databases", True>` were an instance

- `<"csc", "343", "AAAAAAAA", True>` violates `{dept, number}` being a superkey.

If `{dept, number}` is a super key, then so is `{dept, number, name}`.

But we are more interested in a MINIMAL set of attributes with the superkey property.

- Minimal means it's no longer possible to remove attributes from the superkey without making it no longer a superkey

For example, if

- `{st. number, utorID}` is a superkey
- `{st. number, utorID, wordle average, fav color}` is a super key
  - I can remove `wordle average` and `fav color` from that key and it would remain a superkey.

## 1.8 Key

A **key** is a minimal superkey. By convention, we underline a key. Course (dept, number, name, breadth)

The word superkey comes from the word “superset”. This means that somewhere, a superkey must contain the **key** as a subset.

## 1.9 The Importance of IDs

Not everything can avoid duplicates, so sometimes we introduce attributes. This ensures that all tuples are unique. (Integrity constraint)

- USE IDs!!!
- Every site does this (unless there's something wrong with the person making the site)



## 1.10 References between Relations

Better to use separate tables for separate concepts. Rather than repeat information already stored elsewhere, we store the key instead of all the data associated with the thing.

- For example: for an artist, put their ID instead of literally everything else (if the ID is sufficient to identify the artist).

## 1.11 Foreign Keys and Constraints

If in one table we have an attribute that is the key to another table, that is called a foreign key. Firstly, notation:

**Notation:**  $R[A]$  is the set of all tuples from  $R$  only with the attributes in  $A$ .

We can declare foreign key constraints:

$$R_1[X] \subseteq R_2[Y]$$

If attribute  $X$  is a foreign key in relation 1, all values of  $X$  must occur in values of attribute  $Y$  in relation 2.

- $Y$  must be a key in  $R_2$ .

**To write that a bit more clearly:**

- For attribute  $X$ , if we observe in the relation  $R_1$
- If we perform `set(the column of attribute X)`
- That must be a subset of `set(the column of attribute Y)`
  - Most likely,  $X$  and  $Y$  share the same attribute name.

## 2 Relational Algebra

Source for many of these notes is from [HERE](#).

Queries operate on relations and provide relations as a result.

The simplest query is just the relation's name. If we run that query on the database: `student`, we just get `student`, the database, as the return value.

## 2.1 Select and Project (R was confusing)

Here are some operators:

- `select` ( $\sigma_{\text{condition}}$  Expr): filter the table by getting rid of the rows that don't meet the condition. Use the logical and operator  $\wedge$ , or the or  $\vee$  operator if you want some binary operators.
  - For example,  $\sigma_{\text{GPA} > 3.7 \wedge \text{HS} < 1000, \text{major} = \text{CS}}$
- `project` ( $\pi_{\text{attribute}_1, \text{attribute}_2, \dots}$  (Expr))
  - Project gets rid of all the attributes not subscripted. It also gets rid of duplicates afterwards, for the purposes of this course (MAYBE not for SQL).
- `Expr` is any expression that returns a relation, which can be passed in. They're like function arguments.

We can combine multiple operators by compositing them:

$$\pi_{\text{sID}, \text{sName}} (\sigma_{\text{GPA} > 3.7} \text{ Student})$$

## 2.2 The Cross Product

- The cross product: gluing two relations together, and attributes of each relation will be made unique (e.g. `student.ID`, `apply.ID`).
  - If I run `Student  $\times$  Apply`, if student has  $s$  tuple and apply has  $a$  tuples, the result of the Cartesian will have  $s \cdot a$  tuples.

- You're telling me, for each row in student, I'm making one row for each row in apply? Is there any use for this? Yes, if you combine it with multiple operators.

Given `Student` and `Apply` tuples, I want names and GPAs of students from high school student count over 1000 who applied to CS and were rejected. Here's what I do:

$$\pi_{\text{name, GPA}} \left( \sigma_{\text{student.sID=apply.sID} \wedge \text{HS} > 1000 \wedge \text{major=cs} \wedge \text{dec=R}} (\text{Student} \times \text{Apply}) \right)$$

The magic of this, is that `student.sID = apply.sID` removes all “garbage” rows created by the cartesian product. Instead of getting a square, we get its diagonal.

## 2.3 Natural Join $\bowtie$

Performs cross product but enforces equality on all attributes with the same name if the two tables joined have attribute names in common. This prevents the need for composition with  $\sigma_{\text{s.something=a.something}}$ .

The operator is  $\bowtie$ , called a bowtie. Now, we can make a more concise expression:

$$\pi_{\text{sName, GPA}} \left( \sigma_{\text{HS} > 1000 \wedge \text{major=cs} \wedge \text{dec=R}} (\text{Student} \bowtie \text{Apply}) \right)$$

I'm pretty sure the  $\bowtie$  operator is associative with the exception of the order of attributes, so get creative with joining more than two things at once. By the way:

$$E_1 \bowtie E_2 \equiv \pi_{\text{Schema}(E_1) \cup \text{Schema}(E_2)} \left( \sigma_{E_1A_1=E_2A_1 \wedge E_1A_2=E_2A_2 \wedge \dots} (E_1 \times E_2) \right)$$

## 2.4 Edge Cases For Natural Join

- No attribute names in common
  - Results in  $\text{auto} \times$  due to vacuous truth

- Has common attribute names but no matches
  - Results in no tuples

## 2.5 Renaming

Natural join can over-match: two objects may mean different things but its `str()` returns the same thing. What do we do?

What if they under-match ( `.equals(...)` is something we want to define by custom)? Use

⚡condition

## 2.6 Set Operations



ATTRIBUTES MUST MATCH EXACTLY FOR BOTH OPERANDS, OTHERWISE YOU'LL GET AN ERROR MESSAGE

Relations are sets, so we can use set operations. If you're doing this on a tuple of relations, they must have the same number of attributes with the same name, and in the same order.

- Union joins all the elements in one set and all elements in the other set, but no repeats.
- For intersections, we only keep the elements in common.
- For difference, it only has elements in the left operand but not the right operand.
  - Not commutative

If the names or order mismatch, we can:

- Rename attributes
- Use  $\pi$  to permute (re-order)

## 2.7 Renaming

Useful if you want to take a product of a table and itself.

$$\rho_{\text{new\_name}}$$

To prevent the issue of pairing  $(1, 2)$  and  $(2, 1)$ , you could use  $\sigma_{T1.i1 < T2.i1}$  to ensure that the pairs you get are sorted. This prevents pseudo-duplicates, and also prevents duplicates as well.

## 2.8 Renaming Attributes

You can't mutate an attribute to do this, but you can always create a new one:

$$\text{NewRelation}(a1, a2) = \pi_{x,y} \text{OldRelation}$$

This redefines its attribute names.

## 2.9 Max and Min

Where  $i$  is the score:

$$S - \underbrace{(\pi_{\text{All of } T1} \sigma_{T1.i < T2.i} (\rho_{T1}(S) \times \rho_{T2}(S)))}_{\text{not max}}$$

Flip the direction of the inequality to get the `not min` set.

## 2.10 Occurred At Least Twice

Find all people who did this twice. Then  $oID$  is an instance of a person doing something, which is part of the distinguish step.

If you want to find the ID of an something that occurred at least twice, where  $oID$  is the disambiguator (key):

$$\pi_{T1.ID} \sigma_{\underbrace{T1.ID = T2.ID}_{\text{match}} \wedge \underbrace{T1.oID < T2.oID}_{\text{distinguish}} \wedge \underbrace{T1.A = N \wedge T2.A = N}_{\text{check}}} (\rho_{T1}(S) \times \rho_{T2}(S))$$

We use  $<$  to prevent any issues with doubling up, to only get a triangle instead of a rectangle.

You can omit the check component if everything is a pass.

## 2.11 Occurred Exactly Twice

Use set minus: Occurred at least twice minus Occurred at least three times

$$\sigma_{\underbrace{T1.ID = T2.ID = T3.ID}_{\text{match}} \wedge \underbrace{T1.oID < T2.oID < T3.oID}_{\text{distinguish}} \wedge \underbrace{T1.A = N \wedge T2.A = N \wedge T3.A = N}_{\text{check}}} \left( \begin{array}{c} \rho_{T1}(S) \times \\ \rho_{T2}(S) \times \rho_{T3}(S) \end{array} \right)$$

Twice minus three times:

At Least Twice – At Least Three Times

## 2.12 Occurred The Most Amount Of Times

This cannot be done in relational algebra.

## 2.13 Every

$AllOfThem(ID, Trait)$  is what happened;  $RequiredAll(Trait)$  contains attributes that all “people / unique identifiers” need to remain in the query. For example, if I want to query the following: the course codes of all courses offered in 20229 and 20231 (the trait would be the terms), `RequiredAll` would just contain the terms:

20229, 20231.

$$EveryPossible(ID, Trait) = (\pi_{ID} AllOfThem) \times \underset{\text{traits only}}{RequiredAll}$$

$$Missing(ID) = EveryPossible - AllOfThem$$

$$(\pi_{ID} AllOfThem - \pi_{ID} Missing)$$

In short:

- Make all combos that should've occurred.
- Subtract those that did occur to find those that didn't.
- Subtract what was missing from those that did occur after projecting each to persons only.

Here, *Missing* is a set of IDs that don't match the condition.

## 2.14 Set Difference Tips

Set difference takes away everything in the first set that is not in the second set. For example:

$$\{A, B, C, D\} - \{A, X, C, D, F\} = \{B\}$$

You might want to use this to find out the complement of things you would get in a natural join.

Items on the right set have no impact on the result.

## 2.15 Expressing Constraints

Query a violator and = it to  $\emptyset$  to say it can't occur.

Or if we want a query to capture everything, say that selecting and processing does nothing.

$$A \subseteq B \Leftrightarrow A - B = \emptyset$$

## 3 SQL

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RA	SQL
Pi	SELECT
Sigma	WHERE for rows, HAVING for aggregates after a group by
Renaming columns or relations	As
Cartesian product	Comma (,)

---

SQL is a declarative language. Take this with a grain of salt: say what you want but express it in a very specific form and order to get what you're asking for.

### 3.1 Aggregate Data and Group By

What does this query do?



```
1 SELECT oid, avg(grade)
2 FROM took
3 GROUP BY oid;
```

Gives me the course average for each offering.

We can obtain more idea and give more meaningful names:

```
1 SELECT oid as offering, avg(grade),
2 min(grade), max(grade)
3 FROM took
4 GROUP BY oid;
```

Newlines don't really matter but beware of commas. This also tells us about the order in which queries are made.

1. State your tables.
2. State how you're going to join them.
3. Which rows are you going to look at?
4. If you want to group portions (rows) of the table, you can use GROUP BY
5. Of those groups, which groups should we leave in or keep (HAVING)
  1. You must use HAVING right after GROUP BY
6. Order what you see (ORDER BY): the first argument takes the most priority
7. Tell us which columns we want to have in an output (SELECT).

Aggregate functions:

- min, max, avg, and all the tools you have in stats.
- count, which counts the number of rows in a group. If you want to count how many unique items are in a group, use `count(distinct columnName)`. Otherwise, just use `count(*)`
- REMEMBER THAT `distinct` has a low precedence, so `distinct dept, instructor` should be viewed as `distinct (dept, instructor)`.

## 3.2 Legal and Illegal Queries

Illegal queries will result in an error when sent. The list below may not list everything, so use your common sense.

### 3.2.1 Ambiguous with Group By

When you use GROUP BY, you may not select something that was not mentioned in `group by` without using `min`, `max`, `average`, or so on. Otherwise, you will get `ERROR: column reference "NAME" is ambiguous`

Be careful when using `*` in conjunction with `GROUP BY`, as due to how `*` evaluates, unless you are querying from a table with one column, you will get an ambiguous attribute error.

You cannot select anything that cannot be derived directly by other attributes. For example, you cannot give me the term based on the course code. That requires using natural joins.

## 3.3 Set operations (NO DUPLICATES)

These can be expressed as:

- `(subquery) UNION (subquery);`
- `(subquery) INTERSECT (subquery);`
- `(subquery) EXCEPT (subquery);`

If you are using queries in queries, you wrap them in parentheses and you don't put a semicolon at the end of a subquery. **The result from the three queries above will always be a set!! By default.**

But there are bag versions of union and intersection.

When writing views inside the parentheses, you MUST actually type

```
select * from <VIEW>
```

### 3.4 Bag operations (ALL, DUPLICATES)

Bag operations put the `all` keyword at the end. They are not on by default.

- `Union all` keeps all: if we treated bags like python lists, we get  
`bag1 + bag2`
  - add type operation
- `Intersect all`: keep the number of copies common to both. If set A has 4 instances of  $x$  and set B has 3 instances of  $x$ , the intersection will have 3 instances
  - `min()` type operation
- `Except all`: the elements on the right side are willing to explode and self-destruct if they see something equal to the one the left side, but one may only take one
  - max of subtract type operation, 0 type behavior.

### 3.5 Views

Names holding queries. Useful for compacting stuff.

`CREATE VIEW <view name> AS <query>`. Views persist until I drop them.

We can rename columns:

`CREATE VIEW <view name> (col1name, col2name, ...) as ...`

Use `drop view <view name>` to get rid of it. There are two types of views:

- **Virtual**
  - Attaches a name to the query (we'll only use this)
  - Every time you reuse this value, you will have to query again
  - This means that if the table updates, you always get an up-to-date table
- **Materialized**

- Constructs and stores the results of the query. Expensive to maintain! (PostgreSQL didn't support this for a long time)
- We won't use this
- It's great if the underlying tables don't change very much

To use a view as a query, you must wrap it around with `(select * from <view>)` otherwise it will not work.

### 3.5.1 View use cases

- Break down a large query
- Provided another way of looking at the same data for one category of user

## 3.6 Joining in SQL

The result of a join could make keys no longer keys, because your result is a different table, which should mean something different in context.

We have these types of joins:

- `CROSS JOIN` (same as the comma in SQL)
- `NATURAL JOIN`
- `JOIN ON`
  - Theta join (join with given condition)
- `LEFT JOIN (ON CONDITION)`
- `RIGHT JOIN (ON CONDITION)`
- `FULL JOIN (ON CONDITION)`

Left join ensures that we keep all the rows on the left and fill the missing correspondences on the right with NULL. If we see all the rows on our resulting table from the left tuple, then we know that we have performed a `LEFT JOIN`.

We use theta joins ( `JOIN ON` ) instead of `NATURAL JOIN` as schemas tend to change **to help us catch errors when making queries when schemas do change.**

`NATURAL LEFT JOIN` is valid syntax.

### 3.7 Subquery as a value in Where

$$\sigma_{\text{value}} \langle \text{a query} \rangle$$

You cannot put a subquery in a condition in relational algebra, but you can in sub-queries like normal in SQL, which only works fine if your sub-query returns a  $1 \times 1$  table. You will get an error otherwise if your subquery is larger than that (no results count as `NULL` ), as you cannot run comparisons with multiple results.

But if you want to do a comparison with **multiple** values, we can require that:

- Value we are comparing is greater than every value, or
- Greater than at least one value (ANY/SOME)

**THESE COMPARISONS ARE ROW-WISE. WE ARE COMPARING ONE ROW TO MANY OTHERS.** This means a 2-column operation would feel like

`(2, 3) in [(2, 3), (4, 5), (6, 7)]`.

#### 3.7.1 Any/Some $\exists$

The syntax for ANY/SOME (these two words are interchangeable) is:

- `X <comparison> ANY (<subquery>)`

This evaluates to true if and only if the comparison holds for at least one tuple in the subquery result:

$$\exists y \in \langle \text{subquery results} \rangle \text{ such that } x \langle \text{comparison} \rangle y$$

### 3.7.2 All $\forall$

- `X <comparison> ALL (<subquery>)`

This evaluates to true iff the comparison holds for every tuple in the subquery result.

We could rewrite this query using `max` instead.

### 3.7.3 In $\in$

Syntax:

- `x in (<subquery>)`

True if  $x$  is in the set of rows given by the subquery

### 3.7.4 Exists

Syntax:

- `Exists (<subquery>)`

True if and only if the subquery has at least one tuple (is not empty).

Even if the tuple is null.

## 3.8 Making your own tables

Want to create something like

Level	Average
Easy	69
Hard	32

Use union and selecting a name:

```
1 (SELECT "Easy" as level, avg(...) from [...])
2 UNION
3 (SELECT "Hard" as level, avg(...) from [...])
```

Remember that `SELECT` happens last. `SELECT "Easy" as level` creates a column named `level` and just populates all the rows as `"Easy"`.

### 3.9 Search Paths

The top level is called `public`. `SET search_path to <SCHEMA>` is like changing the directory. Otherwise, use dots ( `.` ) to delimit directories and tables. The default schema is `public`, and you cannot nest schemas inside schemas. It is a flat structure.

```
1 table university.student
```

I can show search paths by using `show search_path`

If I want to remove schemas:

```
Drop schema <SCHEMA> cascade;
```

(Use `cascade` to make sure everything inside of it is dropped so no errors occur. To prevent error messages, you must make sure it exists so use `if exists`). That's why on the top of a lot of files, you would see:

- Drop the schema if it exists, and cascade down
- Re-create it
- Set the search path to the schema

### 3.10 Workflow

- Create a DDL file with the schema

- Create a file with inserts to put content in the database (duplicate keys are NOT allowed! Under any circumstances, even in the bag concept.)
  - Tuples do not need keys, but if they do then you outright cannot have duplicates.
- Import these in PostgreSQL
- Run queries directly in the shell or by importing queries written in files

### 3.11 Defining Types in Table Attributes

When creating a table in SQL, you **must** define the type of that variable. Here are some types:

- `CHAR(n)`
  - Fixed length string of *n* characters, padded with blanks
- `VARCHAR(n)`
  - Variable length string up to *n* characters.
- `TEXT`
  - Free-for-all string
- `INT` or `INTEGER`
- `FLOAT` or `REAL`
- `BOOLEAN`
- `DATE`
- `TIME`
- `TIMESTAMP`

SQL defines a string enclosed in ‘single quotes’, and NOT smart quotes.



## 3.12 Defining our own type (Constrained Types)

Defined in terms of a built-in type. You can constrain them or give them a default value. For example:

```
1 CREATE DOMAIN Grade as int
2 Default null
3 Check (value >=0 and value <= 100)
4 CREATE DOMAIN State as varchar(4)
5 Default 'ohio'
6 Check (value in ('ohio', 'oklahoma', 'wyoming'))
```

### 3.12.1 Default Values

When no value has been specified.

## 3.13 Primary Keys

Every table can either have 0 or 1 primary keys (but all tables should have one). It is the key to the table. You can never have more than one value of it (it is unique), and it **cannot** be null. If you declare something to be a primary key, its value can't be null.

That is, the **PRIMARY KEY** – a set of one or more attributes for a relation. You can declare primary keys:

```
1 Create table TBL
2 ID integer primary key,
3 ...;
```

Or

```
1 Create tabke TBL (
2 ...,
3 primary key(this, that)); -- means (this, that), a pair,
    is a key, like dept, cNum
```

**A TABLE CANNOT HAVE TWO PRIMARY KEYS.** Do not use the primary key keyword twice. If you want a key that is made of two parts, then you do have to declare it in the last line. `Primary key(dept, cNum)` (same syntax for `unique` as well).

### 3.14 Uniqueness Constraints

When an attribute is `UNIQUE` for a relation, it means:

- They can form a key (unique and no subset is)
- Multiple attributes can be declared unique
- Nulls are never equal to each other (primary keys don't allow null values anyway)

```
1 CREATE table tbl(...,  
2 Unique(ID, ID2)); -- for multiple attributes in a key
```

For example, you can use `Unique(firstname, lastname)`. This will prevent two insertions of the same `firstname - lastname` pair.

In the same table, an attribute can be labelled as a primary key, and another attribute can be labelled as unique. If I have a default value for a unique, if I do two blank insertions, the program generates an error.

Note that `unique` per attribute is DIFFERENT than `unique(a1, a2)`. The second one `unique(a1, a2)` restricts pairs. The first one just restricts duplicates if I project only that property.

### 3.15 Foreign Key Constraints

```
1 Foreign key (sID) references Student
```

Means that `sID` in this table is a foreign key that references the primary key of the table Student.

- Every value for `sID` in this table must actually occur in the `Student` table (keys in this table  $\subseteq$  those in the student table).

- `sID` must be a primary or unique key there

### 3.15.1 The References Keyword

```
1 Create table people (  
2   SIN integer primary key,  
3   Name text,  
4   OHIP text unique);  
5 Create table Volunteers (  
6   Email text primary key,  
7   OHIP text references People(OHIP));
```

Here, for each row in Volunteers, `Volunteers[text] ⊆ people[text]`

### 3.15.2 Referring table example

Took refers to both offering and student. It has `sID`s and `oID`s. If I remove a student from the student table, then the references within the took table about that student no longer makes sense. So we should remove them or do something.

I either put in a table that doesn't refer to anything in the home table, or a deletion in the home table that makes something in the referring table make no sense.

### 3.15.3 Safe and Risky Operations Regarding Foreign Key Constraints

So what can I do, and what can I not do?

- Safe to delete from `Took`
- Risky to insert and update anything in/to `Took` (what if the `sID` is not in `Student`?)
- Safe to insert into `Student`
- Risky to delete or update anything inside in/to `Student`

### 3.16 Reaction Policies - Enforcing Foreign Key Constraints

#### How could a database react to a risky operation?

1. Prevent it from happening
2. Allow the operation if it doesn't break constraint rules
3. Propagate the change to the affected tables such that no constraint rules are broken
  4. Deleting or updating from `Student` will also delete/update all matching `sID`s from `Took`.
4. Propagate the change, but instead of deleting, set any instance of the deleted key to `NULL`
5. If affected columns aren't primary keys, then we can set to `NULL`

Because of asymmetry, any affected table decides what would happen (the owner/designer of the table).

When does the DBMS bring the rules here? When we try to insert a tuple. If we try to insert a tuple that violates the foreign key constraint, then there is a violation. We respond it by specifying a reaction policy. These help us deal with insertions in the referring table that violate key constraint or changes in the home table.

If you don't say anything in the reaction policy, then the program gives you an error when you try to violate a key constraint.

If you say something, then something should be done in the referring table to get rid of the violation.

---

Primary	Unique
One of a kind	One of a kind
No nulls allowed	Can have nulls; nulls are never equal to each other

---

### 3.17 Types of Reaction Policies

A reaction policy can be set up on a table to either block unsafe queries or update/change at most **itself**. It keeps its hands off all other tables.

- `cascade`: propagate the change to the referring table
- `set null`: set the referring attributes to null
- default: forbid the change

Suppose `R` refers to `S`.

- Doing anything unsafe to `R` (insert) cannot modify `S`, so it will prevent the query from being made
- Doing anything unsafe in `S` (delete or update) **can** modify `R`.

This means if anything is referred to, change it can change the things that refer to it.

#### 3.17.1 What I can react to

All scenarios in **the table that is looking at another table**:

```
1 on delete -- each row: if the table I'm looking at deletes
   this, I will
2 on update -- each row: if the table I'm looking at updates,
   I will
3 on delete restrict on update cascade
```

Why no insert? Because inserting to a table that is referred to has no effect on foreign relationship. And regardless, I am not allowed to modify the table I'm looking at, so violating a constraint by inserting into the table that refers to another is not allowed.

Changing constraints:

```
1 ALTER TABLE took
2 DROP CONSTRAINT took_sid_fkey;
3 ADD CONSTRAINT took_sid_fkey
4   FOREIGN KEY (sid)
5   REFERENCES student(sid)
6   ON DELETE CASCADE ON UPDATE CASCADE;
```

Setting a value to null counts as an update.

### 3.17.2 An instance of trying to update

```
1 update student set sid = 111 where sid = 11111;  
2 ERROR: update or delete on table "student" violates the  
   foreign key constraint...
```

## 3.18 Save points and Rolling Back

When I write `begin;`, I create a transaction. If I make a mistake, I have to roll back to the safe point. I can also roll back if I do something I didn't mean to.

I type `ROLLBACK;` to undo my changes.

- `begin;` to start a transaction or a safe point
- `rollback;` if an error occurs or if you want to undo and exit the transaction
- `commit;` once you're done and want to save and exit the transaction

If I'm NOT in a transaction, every query (after a `;`) commits.

## 4 Pyscopg

SQL is not Turing complete. There's a trade-off:

- It's optimized for certain things
- But it can't do everything

You cannot control the format. End users (not necessarily with programming knowledge) should not be writing queries.

If we combine SQL with a language like Python, we can solve these problems, but SQL is based on relations and conventional relations don't have that. We'll use `pyscopg2`.

This allows us to connect from inside the Python program out to databases (like PostgreSQL).

When using `pyscopg2.connect`:

- Your database name is `csc343h-UTORID`
- Your user is your `UTORID`
- Don't put anything into the password field

## 4.1 Creating Queries

First, open a cursor. It allows the Python program to pass information back and forth to the SQL database. Then, you can pass in SQL queries directly from Python strings. We **do NOT recommend this**.

```
1 import pyscopg2
2 conn = pyscopg2.connect("dbname=csc343h-UTORID user=UTORID
    password=") # could also use py kwargs
3 cur = conn.cursor()
4 cur.execute("SELECT name, netWorth FROM MovieExec;")
5 for row in cur:
6     name = row[0]
7     worth = row[1]
8     # do something interesting with name and worth on the
        python side
9 conn.close()
```

If this code changes anything, it won't be reflected after close as nothing is committed. You will have to `conn.commit()`

A cursor can hold the results of a query and allow us to iterate over them.

Sometimes, you may not know the queries ahead of time. Then:

- Hard code the parts of the queries you know
- Use string substitution

The `cur.execute` has a second argument, like format strings in C. This method sanitizes the strings to prevent mischief.

**DO NOT USE F-STRINGS OR ANY BUILT-IN STRING OPERATIONS (+) WITH USER-INPUTTED STRINGS INSIDE ARGUMENTS FOR `cur.execute`, AS THIS COULD CAUSE SECURITY PROBLEMS**

For example, a malicious user could input

`John'; delete from please_do_not_delete; --` and the `'` is something you do NOT want. `Pyscopg` automatically sanitizes these types of mischief.

```
1 cur.execute("%s", (to_place_here,))
```

## 4.2 Merge Conflicts

In Pyscopg, nothing persists until you commit. This is different than the SQL shell, who commits right after a semicolon (by the way, your session is preserved when you quit PSQL unless you reload your database).

## 5 Privileges and Transactions

- Roles can be assigned to one or more users to determine what permissions they have.
- The user that initiates a session owns it. Whether they initiate it through sql or by running a python script.
- Schemas and their contents are owned by the suer who creates them.
- SQL checks whether the session owner has sufficient privileges to carry out a task.

Owners can create roles and assign (groups of) users to them. Superusers (Postgres) and owners can grant privileges to roles, and revoke them.



For each query or role, you want to grant the minimal privilege necessary for a role to do its job. You don't want to show someone everyone's home addresses, right?

## 5.1 Adjusting Privileges

Owners will always be able to `DROP`, `GRANT` `REVOKE`, and so on. These are special privileges.

To grant a privilege **TO**, use:

```
1 GRANT <OPERATION> ON <some_object> TO <user>;
2 GRANT <OPERATION> (specific_column) ON <some_object> TO <
  user>;
```

To revoke a privilege **FROM**:

```
1 REVOKE <OPERATION> ON <some_object> FROM <user>;
2 REVOKE <OPERATION> (specific_column) ON <some_object> FROM
  <user>;
```

Do not mix up to and from.

Objects can be schemas and tables.

Ordinary privileges are as follows:

- `SELECT` (r “read”)
  - Allows `COPY` to
- `INSERT` (a “append”)
  - Allows `INSERT` and `COPY FROM`
- `UPDATE` (w “write”)
  - Allows `UPDATE`
- `DELETE` (d)
  - Allows a row to be deleted. Oftentimes requires `SELECT` as well.

- **TRUNCATE**
  - Allows this operator
- **REFERENCES**
  - Allows foreign key constraints to be created on this table
- **TRIGGER**
  - Allows creation of this on a table
- **CREATE**
  - For databases, allow new schemas and publications to be created.
  - For schemas, allow new objects to be created within. To rename an object, you must own it and have this privilege for the schema.
- **CONNECT**
  - Allows connection
- **TEMPORARY**
  - Allows creation of temporary tables in this database
- **EXECUTE**
  - TBA
- **USAGE**
  - TBA
- **ALL**
  - All of them

Most privileges require the **SELECT** privilege to work completely as intended. Creating a view does not run the query, so SQL will not stop me from creating a view. You can revoke privileges on views.

If you don't have any privileges, if you try to look for a schema, you wouldn't be able to see it.

## 5.2 Accessing Privileges

`\dp` (display privilege) displays privileges. Access privileges display:

```
1 name=vector of access control characters/who gave those permissions`
```

Ex: `user=arwdDxt/givenby`

## 5.3 Granting Some Privileges

```
1 grant select(dept, cnum) on course to name;
```

Gives me select permissions for just `dept` and `cnum`. If I try to select anything else, or my queries involve attributes that I don't have the permissions for, I wouldn't have permission for it. And I certainly can't look at `*`. Rule of thumb: if you can CTRL+F the words, then you should probably have been given permissions for them.

```
grant select(dept, cnum, instructor)on offering to name;  
grant select(dept, cnum, breadth)on course to name
```

## 5.4 Constraints and Foreign keys

`update` maintains constraints, and `select` can help verify constraints.

### 5.4.1 Inserting or updating a table that references another table

When inserting, we need to be able to verify if the foreign key constraint is met, so we must be able to see specific attributes in the tables that the table we're inserting to is referencing.

There are no issues when deleting.

### 5.4.2 Deleting or updating a referenced key

I must be able to perform all reaction policies, and I must be able to know that there's a reaction policy in the first place. Databases have NO loopholes.

Note that I do not need permission to know that I don't have permission to do something.

### 5.4.3 Deleting in general

#### REQUIRED AT ALL TIMES

When deleting, you need to grant `DELETE` on the entire table, because you are really deleting by rows. This means that when you delete a row from a table that other tables are referencing, you need to have deleted or update perms on all the tables that reference the table I'm deleting from.

## 6 Transactions

### 6.1 Concurrent users

Single statements in a PSQL shell begins with a snapshot of the DB the MOMENT we hit ENTER and either succeeds or fails (and rollbacks) after the statement finishes executing.

However, we want transactions (groups of statement) to either all succeed or all fail, for correct behavior (in other words, atomicity).

### 6.2 Problems with Transactions

#### 6.2.1 Dirty read

Using uncommitted changes from other sessions; not allowed in PSQL

### 6.2.2 Non-repeatable reads

View of DB items can change between the start and end of transaction due to other transactions **committing** (I get balance, someone else changes balance, then I subtract from the balance)

### 6.2.3 Serialization anomaly

Occurs when the result of executing transactions  $T_1$  and  $T_2$  concurrently is **not** ( $T_1$  then  $T_2$ ) or ( $T_2$  then  $T_1$ )

## 6.3 Levels of Isolation

The SQL standard has 4 levels of isolation. Postgres only has the strictest three, so this avoids reading uncommitted.

```
1 SET TRANSACTION ISOLATION LEVEL serializable
```

### 6.3.1 Read committed (default)

- Only committed results from other transactions are seen in the transactions
- When a row is being modified by a transaction  $T_1$ , it locks those rows the moment I submit a query that modifies those rows. Other transactions  $T_2$  that try to UPDATE (not read) an uncommitted, but modified row by  $T_1$  will lock (wait) until it gets committed by transaction  $T_1$ .
- When you try to delete a row, and a block occurs, the rows that are deleted are rows who meet the delete condition before and after I run the delete command  
### Repeatable read

During a transaction, we don't see anything that was committed from start to end except for the transaction itself

### 6.3.2 Serializable (strictest)

If your results are different than your transactions happening in either order (permutations of transactions running in order), then committing will fail

The other one risks dirty reads

## 6.4 Costs vs. Certainty

Isolation levels come at a cost. The `serializable` level has substantial overhead, and it is very costly for the DBMS. Mostly, use the default.

## 7 Functional Dependencies

### Source

Functional dependencies are a generalization of the notion of keys. They allow the system to store data more easily. They can be used to reason about query and do query optimization. This allows declarative queries to be executed efficiently.

Suppose we have two relations:

```
1 Student(SSN, sName, address, HScode,  
2         HSname, HScity, GPA, prio)  
3  
4 Apply(SSN, cName, state, date, major)
```

Suppose that `priority` is determined by GPA:

- $GPA > 3.8 \rightarrow \text{priority} = 1$
- $3.3 < GPA \leq \rightarrow \text{priority} = 2$
- $GPA \leq 3.3 \rightarrow \text{priority} = 3$

If this relationship is guaranteed, then any two tuples that have the same GPA has the same priority. Formalizing this:

$$\forall t_1, t_2 \in \text{student} : (t_1.\text{GPA} = t_2.\text{GPA}) \Rightarrow (t_1.\text{prio} = t_2.\text{prio})$$

This logical statement is the definition of a functional dependency and we would write this as

$$\text{GPA} \rightarrow \text{Priority}$$

## 7.1 Generalizing Functional Dependencies

$$\forall t_1, t_2 \in R : (t_1.A = t_2.A) \Rightarrow (t_1.B = t_2.B)$$

Means in  $R, A \rightarrow B$ .

Functional dependencies don't always need to have one attribute on each side. They can have to.

If  $A_1, A_2, \dots$  and  $B_1, B_2, \dots$  are attributes of relation  $R$ , we can instead use:

$$\forall t_1, t_2 \in R : (t_1[A_1, \dots, A_n] = t_2[A_1, \dots, A_n]) \Rightarrow (t_1[B_1, \dots, B_n] = t_2[B_1, \dots, B_n])$$

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_n$$

Means that if two tuples  $t_1$  and  $t_2$  has the same values for all of  $A_1, A_2, \dots, A_n$ , then they must also have the same values for all of  $B_1, B_2, \dots, B_n$ .

I may abbreviate  $\bar{A} = A_1, A_2, \dots$  and the same for  $\bar{B}$ .

## 7.2 Creating Functional Dependencies

They are based on knowledge of the real world. All instances of relation must adhere. Meaning if we have:

$$\bar{A} \rightarrow \bar{B} \quad R(\bar{A}, \bar{B}, \bar{C})$$

This means  $R$  would look like this:

$\bar{A}$	$\bar{B}$	$\bar{C}$
$\bar{a}$	$\bar{b}$	???
$\bar{a}$	$\bar{b}$	?!?

If the  $a$  values are the same then so does the  $b$  values.

For `student`:

$$\text{SSN} \rightarrow \text{sName}$$

This means we require the identifier to uniquely identify the student name. And also:

$$\text{SSN} \rightarrow \text{address}$$

This means that social security number can't link to more than two addresses.

$$\text{HSCode} \rightarrow \text{HSname}, \text{HScity}$$

The same high school code can't be associated with an ambiguous high school name or city.

Functional dependencies can be in the other direction:

$$\text{HSname}, \text{HScity} \rightarrow \text{HSCode}$$

And if we assume we have one GPA for each student, then we have



$$\text{SSN} \rightarrow \text{GPA}$$

$$\text{GPA} \rightarrow \text{Priority}$$

Functional dependencies are **transitive**, so this automatically implies

$$\text{SSN} \rightarrow \text{Priority}$$

Functional dependencies really depend on real-world data. For example, **if all college names are unique**, then we can state that every application to a college has a single date. If that were the case, then  $\text{cName} \rightarrow \text{date}$ .

If we want students to only apply to one major, then  $\text{SSN}, \text{cName} \rightarrow \text{major}$ .

## 7.3 Functional Dependencies and Keys

### 7.3.1 “Is a key” condition



If  $\bar{A} \rightarrow$  all other attributes, then  $\bar{A}$  is a **key**.

### 7.3.2 Trivial FDs

We have a trivial functional dependency if this statement holds:

$$\bar{A} \rightarrow \bar{B} \text{ AND } \bar{B} \subseteq \bar{A}$$

### 7.3.3 Nontrivial FDs

We have a nontrivial functional dependency if this statement holds:

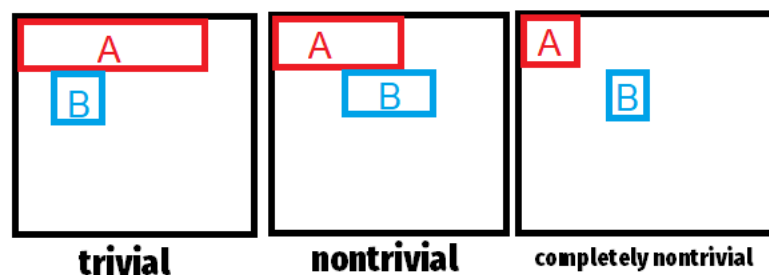
$$\bar{A} \rightarrow \bar{B} \text{ AND } \bar{B} \not\subseteq \bar{A}$$

### 7.3.4 Completely nontrivial FD

We have a completely nontrivial FD if this holds:

$$\bar{A} \rightarrow \bar{B} \text{ AND } \bar{A} \cap \bar{B}$$

### 7.3.5 In summary



**Figure 1:** Functional dependency diagram

## 7.4 Rules for FDs

### 7.4.1 Splitting/combining Rule

Feels like the distributive property (splitting is  $\Rightarrow$ , combining is  $\Leftarrow$ )

$$(\bar{A} \rightarrow B_1, B_2, \dots, B_m) \iff (\bar{A} \rightarrow B_1 \text{ AND } \bar{A} \rightarrow B_2 \text{ AND } \dots)$$

This does NOT work the other way around:

$$(A_1, A_2, \dots, A_n \rightarrow \bar{B}) \not\Leftarrow (A_1 \rightarrow \bar{B} \text{ AND } A_2 \rightarrow \bar{B} \text{ AND } \dots)$$

Why doesn't this work? Because if `HSname` and `HScity`  $\rightarrow$  `HScode`, then we don't want to have `HScity` standalone, as this removes a lot of information when it comes to choosing the HS.

### 7.4.2 Trivial Dependency Rules

If we have a trivial dependency (the following hold):

$$\bar{A} \rightarrow \bar{B} \text{ AND } \bar{B} \subseteq \bar{A}$$

THEN both the following hold:

$$(\bar{A} \rightarrow \bar{B}) \Rightarrow (\bar{A} \rightarrow \bar{A} \cup \bar{B})$$

$$(\bar{A} \rightarrow \bar{B}) \Rightarrow (\bar{A} \rightarrow \bar{A} \cap \bar{B})$$

### 7.4.3 Transitive rule

The  $\rightarrow$  operator is transitive.

$$(\bar{A} \rightarrow \bar{B} \text{ AND } \bar{B} \rightarrow \bar{C}) \Rightarrow (\bar{A} \rightarrow \bar{C})$$

This is really obvious if you try to look at it, or draw an example.

## 7.5 Closure of Attributes

(Everyone follows itself)

Given relation, a set of FDs, and a set of attributes  $\bar{A}$ . I want to find all  $B$  such that  $\bar{A} \rightarrow B$ .

The “all  $B$ ” is known as the closure. Notationally, the closure of  $\bar{A}$  is  $\bar{A}^+$ , or  $\{A_1, A_2, \dots, A_n\}^+$

This means that  $\bar{A}^+$  is all attributes, from our functional dependencies, that can be unambiguously determined by  $\bar{A}$

How do I find that? Here’s the algorithm:

- Start with  $A_1, \dots, A_n$
- Add attributes to that set until I get to that closure. REPEAT UNTIL NO CHANGE:
  - If  $\bar{A} \rightarrow \bar{B}$  and  $\bar{A}$  in the set above, then add  $\bar{B}$  flattened to the set

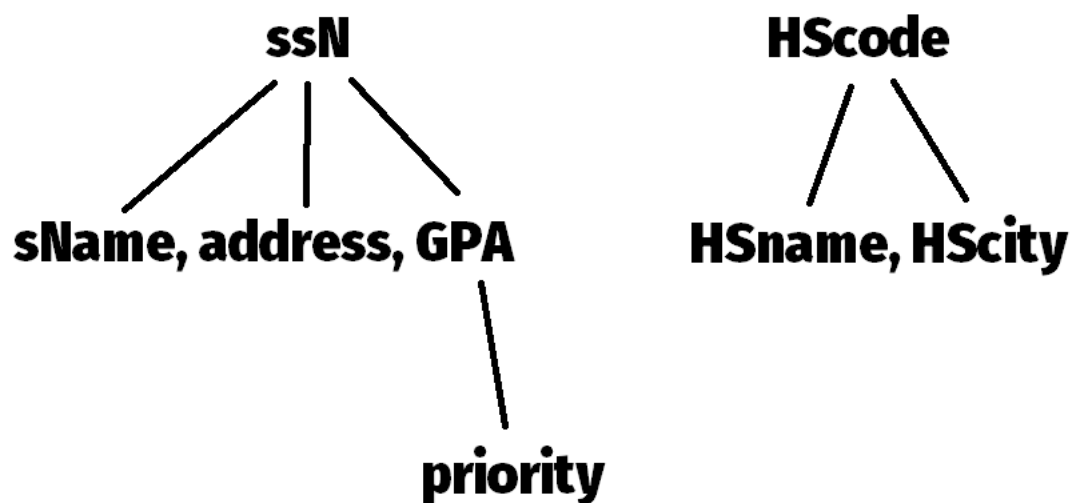
### 7.5.1 Running the closure algorithm

If we are given:

```
1 Student(SSN, sName, address,  
2         HScore, HSname, HScity,  
3         GPA, priority)  
4  
5 SSN -> sName, address, GPA  
6 GPA -> priority  
7 HScore -> HSname, HScity
```

And we want to find  $\{SSN, HScore\}^+$

Just add attributes that are functionally determined in this set. This algorithm feels like a graph search algorithm. This is how I would do it:



**Figure 2:** Flatten this tree and all words we see are elements in the closure

Apparently, from this, `SSN` and `sName` are able to unambiguously determine all other attributes of a student (if recorded). This means that `{SSN, sName}` form a **KEY**.

### 7.5.2 Closure to determine Keys: verification

Is  $\bar{A}$  a key for  $R$ ? We can use closure to do that.

1. Compute  $\bar{A}^+$
2. If  $\bar{A}^+ = \text{all attributes}$ , then  $\bar{A}$  is a key.

### 7.5.3 Closure to determine Keys: finding all keys

Brute force the algorithm above with every possible subset of attributes in our relation. Note that this doesn't give me the primary key alone; it gives me all superkeys as well.

To run this more efficiently, consider running this algorithm in increasing size of attribute subsets. This means the real algorithm would rather

- Test if each single attribute is a key, then
- Test if each pair of attributes are keys
- And so on

(Stop when we find one?)

## 7.6 Following from

- $S_1$  and  $S_2$  are sets of FDs.
- $S_2$  **follows from**  $S_1$  if every relation instance satisfying  $S_1$  also satisfies  $S_2$ .

For instance:

$$S_2 : \{SSN \rightarrow \text{priority}\}$$

$$S_1 : \{SSN \rightarrow GPA, GPA \rightarrow \text{priority}\}$$

How do we test this?

Does  $A \rightarrow B$  follow from  $S$ ? We can use closure:

1.  $\bar{A}^+$  based on  $S$ , check if  $\bar{B}$  is in the set.
2. Use Armstrong's Axioms.

## 7.7 Specifying FDs for a relation

We want: **minimal** set of **completely nontrivial FDs** such that all FDs that hold on the relation **follow from** the **dependencies in the set**.

Get this by actually making FDs. You'll need practice.

## 8 Database design

Try not to stuff all your information into one table. For example:

A table that stores:

- A part
- Manufacturer
- Manufacturer address
- Seller
- Seller Address
- Price

It is a waste of space (redundant) to store attributes you tend to see repeated many times in a table, in a table with a lot of columns.

Another thing is that manufacturer address will always be consistent with manufacturer address, making the fact that manufacturer address there be redundant.

Key lesson: **AVOID REDUNDANCY**. Redundant data can lead to anomalies.

- If a manufacturer moves and we only update one tuple, the data is inconsistent. So it's not just the space, it's the work we have to do and **the potential sources of error. That's why we have helper functions.**
- part  $\rightarrow$  manufacturer, so do we really need the manufacturer data anyway?
- Every seller has one address: seller  $\rightarrow$  seller address

That's why we use functional dependencies. We can only know what FDs apply through context of the domain.

We call FDs functional because there is a mathematical function that takes a value for  $X$  and gives a unique value for  $Y$ . It is just a lookup table – not a function.

The rule for the mathematical function is unknown, it comes from domain knowledge. Maybe we could call the function  $dk(LHS) \rightarrow RHS$ .

When we write a set of CDs, we mean that all of them hold. But we can write sets of CDs in equivalent ways. When we say that  $S_1$  is equivalent to  $S_2$ , we mean that  $S_1$  holds  $\Leftrightarrow S_2$  holds.