Definition 1. The sample mean of database X of size n is

$$\bar{X} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

Theorem 1. Say database X has size n and is bounded above by M and bounded below by m. Then \bar{X} has sensitivity bounded above by

$$\frac{M-m}{n}$$
.

Proof. Say X and X' are neighboring databases which differ at data-point x_j . Then

$$\begin{split} \Delta \bar{X} &= \max_{X,X'} \left| \bar{X} - \bar{X}' \right| \\ &= \max_{X,X'} \frac{1}{n} \left| \left(\sum_{\{i \in [n] \mid i \neq j\}} x_i \right) + x_j - \left(\sum_{\{i \in [n] \mid i \neq j\}} x_i' \right) + x_j' \right| \\ &= \max_{X,X'} \frac{1}{n} \left| x_j - x_j' \right| \\ &\leq \frac{M-m}{n}. \end{split}$$