

ICDSS Lecture 4: Neural Networks

Instructor:

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DataCamp Donates





We have free licenses for our members through our partnership! Requires filling in a form to assess financial need (5-10 minutes) Form will be available on Wednesday.

"Pre-requisites" of L4



Not a mathematically rigorous lecture. We assume you know:

- Matrix Multiplication
- Chain Rule
- Linear and Logistic Regression

$$\begin{bmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & a_9 \end{bmatrix} \begin{bmatrix} b_1 & b_2 & b_3 \\ b_4 & b_5 & b_6 \\ b_7 & b_8 & b_9 \end{bmatrix} = \begin{bmatrix} c_1 & c_2 & c_3 \\ c_4 & c_5 & c_6 \\ c_7 & c_8 & c_9 \end{bmatrix}$$

$$\frac{dL}{dW_1} = \frac{dL}{da_2} \frac{da_2}{dz_2} \frac{dz_2}{da_1} \frac{da_1}{dz_1} \frac{dz_1}{dW_1}$$

Overview of L4



1

Linear Regression as a NN

2

Logistic Regression as a NN

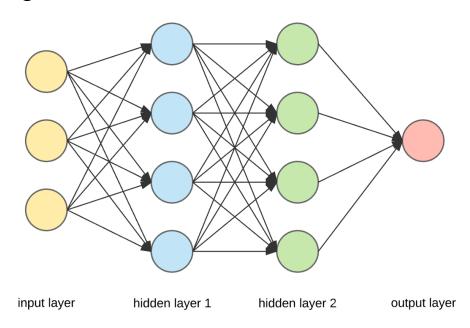
3

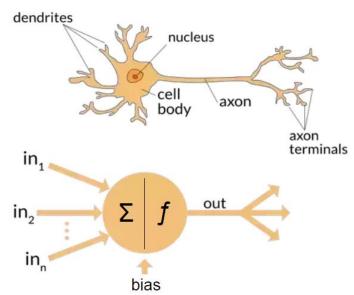
General NNs

Why are they called Neural Networks?



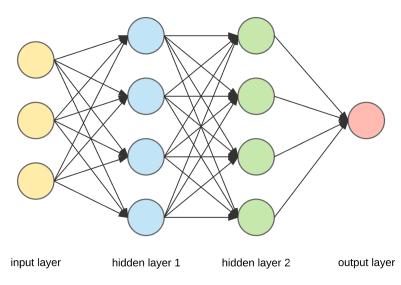
- Mimics the human brain (not exactly!)
- Output signals from other neurons as the input
- Each signal has a different "weighting"
- If signal is above some threshold value, it is "activated."

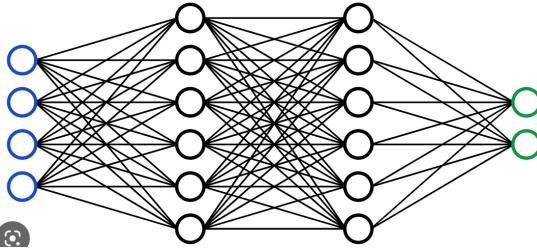




Some Notation



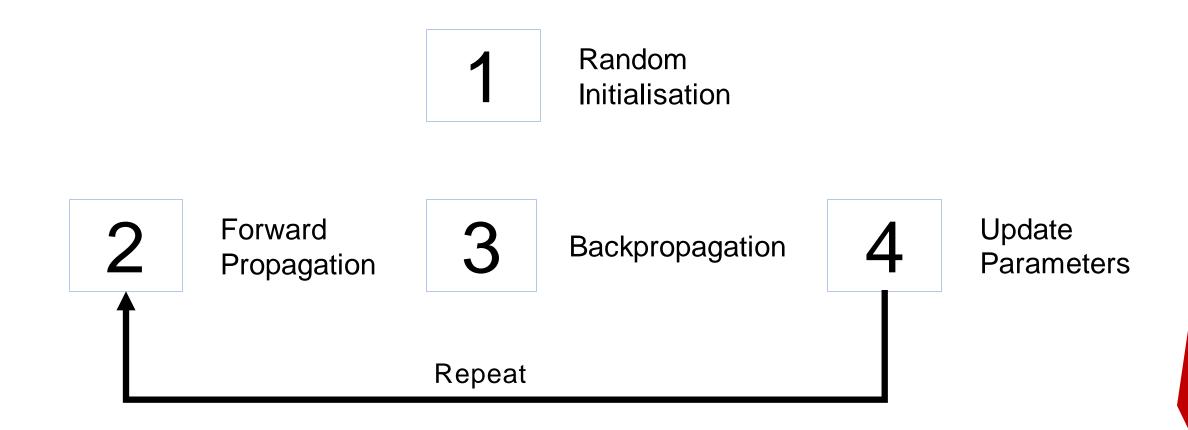




- Input, Label Matrix: X, Y
- Prediction Matrix: \hat{y}
- Number Of Layers: All layers excluding input
- Input Layer: Layer 0
- Number of examples: m
- Input, Label Size: n_x , n_y

Neural Networks: General Steps









Consider a single feature linear regression problem:

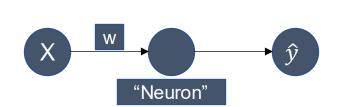
Predicting House Price based on Total Size

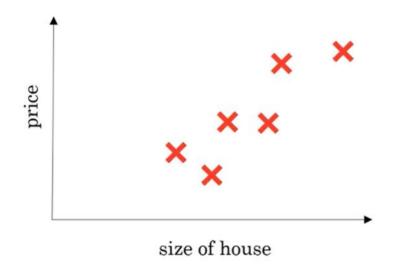
Linear Regression attempts to fit data into the form:

$$y = wx + b$$

w: Weighting, b: Bias

This can be visualised as a "Neural Network"







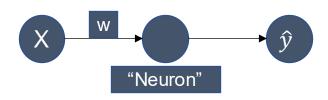
First, the "network" will randomly guess w and b.

Then, the model will calculate:

$$Z = wx + b$$

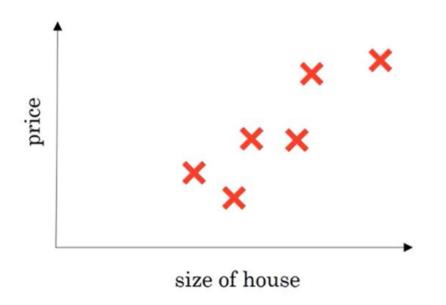
This value acts as the input of the Neuron

Forward Propagation!



In Linear Regression, there is no special "activation function:"

$$\hat{y} = Z = wx + b$$

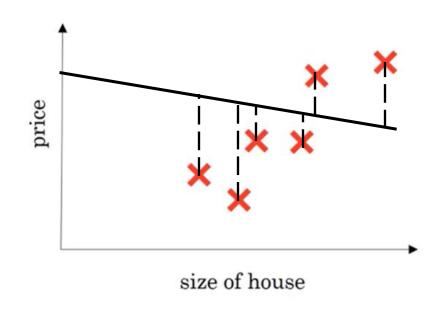




The "network" just guessed values, predictions can't be accurate

- A loss function (performance measure) needs to be defined and minimised
- Use Mean Squared Error (MSE)

$$MSE = \frac{1}{m} \sum_{i=1}^{m} (y_i - \hat{y}_i)^2$$



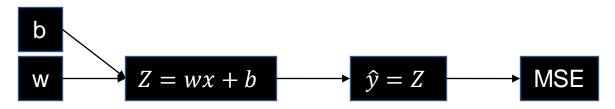
How do we change the parameters (such as w) so that we minimize the MSE?

Update the value of the parameter using its gradient (gradient descent)



How do we change the parameters (such as w) of the network to minimize the MSE?

Examine how MSE is calculated in terms of a computation diagram



Consider derivatives of MSE with respect to w and b

Use chain rule to get

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw} \qquad \qquad \frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$$

See that we are calculating derivatives from the output layer to the input layer (backwards)

Backpropagation!



Consider derivatives of MSE with respect to w and b

• Use chain rule to get:

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw}$$

$$\frac{d(MSE)}{d\hat{y}} = \frac{d}{d\hat{y}} \left(\frac{1}{m} \sum_{i=1}^{m} (y_i - \hat{y}_i)^2 \right) \qquad \longrightarrow \qquad \frac{d(MSE)}{d\hat{y}} = \frac{1}{m} \sum_{i=1}^{m} \left(\frac{d}{d\hat{y}} (y_i - \hat{y}_i)^2 \right)$$

 $\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$

$$\frac{d(MSE)}{d\hat{y}} = -\frac{2}{m} \sum_{i=1}^{m} (y_i - \hat{y}_i)$$



Consider derivatives of MSE with respect to w and b

$$Z = wx + b$$

$$\frac{d(MSE)}{d\hat{y}} = -\frac{2}{m} \sum_{i=1}^{m} (y_i - \hat{y}_i)$$

$$\frac{dZ}{d\hat{y}} = 1; \frac{d\hat{y}}{dw} = x; \frac{d\hat{y}}{db} = 1$$

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw} = -\frac{2}{m} x \sum_{i=1}^{m} (y_i - \hat{y}_i)$$

$$\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db} = -\frac{2}{m} \sum_{i=1}^{m} (y_i - \hat{y}_i)$$



The gradients can be used to **update parameters** (also known as "learning")

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw}$$

$$\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$$

Update as following:

$$w \to w - \alpha \frac{d(MSE)}{dw}$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$

 α Is the learning rate

• It is a hyperparameter: it needs to be specified when the network is created

Also, see that the negative value of the gradient is taken



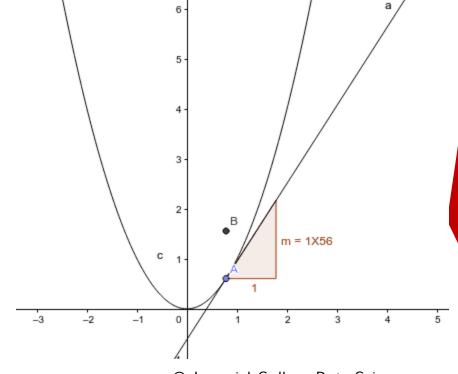
Why are the negative values of gradients used?

$$w \to w - \alpha \frac{d(MSE)}{dw}$$

- The gradient points towards the direction with the steepest increase
- To get direction of steepest decrease, the negative value should be taken

Forward, Backpropagation and Updating of parameters will repeat for a set number of "epochs"

$$b \to b - \alpha \frac{d(MSE)}{db}$$





Finding the right value for the learning rate can be an iterative process

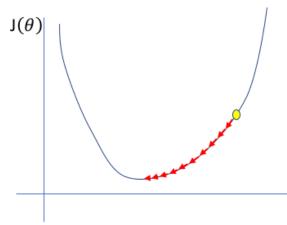
$$w \to w - \alpha \frac{d(MSE)}{dw}$$

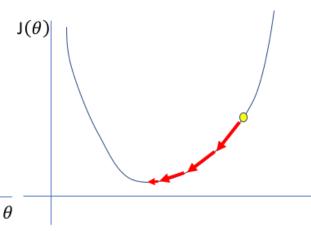
$$b \to b - \alpha \frac{d(MSE)}{db}$$

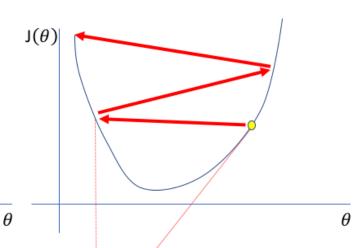
Too low











A small learning rate requires many updates before reaching the minimum point

The optimal learning rate swiftly reaches the minimum point

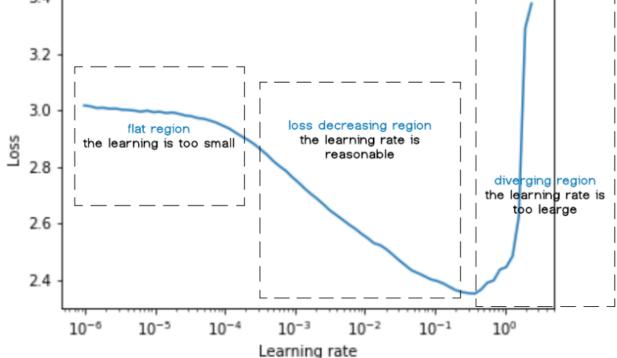
Too large of a learning rate causes drastic updates which lead to divergent behaviors



Starting from very small values, evaluate the loss of the model using a validation set

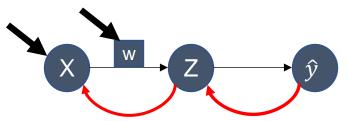
$$w \to w - \alpha \frac{d(MSE)}{dw}$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$
3.4





In Summary:



- 1. Random Initialisation: Neural Network assigns random values to W and b.
- 2. Forward Propagation: The Network Calculates:

$$Z = wx + b$$
; $\hat{y} = Z$

3. Backpropagation: The network calculates derivatives to minimise the loss function

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw}$$

$$\frac{d(MSE)}{dw} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw} \qquad \qquad \frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$$

4. Update Parameters: Using the gradients, parameters (w,b) are updated

$$w \to w - \alpha \frac{d(MSE)}{dw}$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$

5. Repeat 2-4 for a set number of "Epochs"



Linear Regression (Multiple Features)

Linear Regression:



What if there are multiple features?

• Predicting House Price based on House Size (x_1) , Number of Toilets $(x_2), \dots, (x_n)$

Linear Regression attempts to fit data into the form:

$$y = w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + \boldsymbol{b}$$

Let W be a vector containing all weightings and X be a vector containing all features:

$$W = \begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix}; X = \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{pmatrix}$$

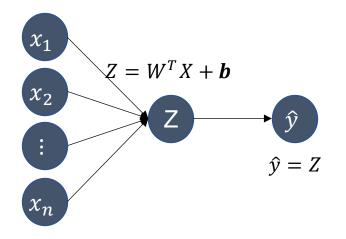
In terms of Matrix Multiplication:

$$Y = W^T X + \boldsymbol{b}$$

Linear Regression Example:



This can be illustrated as a neural network:



Forward Propagation:

$$w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + \boldsymbol{b}$$

Just like before, the network will first assign random values to w_1 , w_2 , ..., w_n , b

Linear Regression Example:



 w_1, w_2, \dots, w_n, b need to be modified

$$\frac{d(MSE)}{dw_1}$$
; $\frac{d(MSE)}{dw_2}$; ...; $\frac{d(MSE)}{dw_n}$; $\frac{d(MSE)}{db}$

Follow similar workings to single variable linear regression:

$$\frac{d(MSE)}{dw_i} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw_i}$$

$$\frac{d(MSE)}{dw_i} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw_i} = -\frac{2}{m} x_i \sum_{k=1}^{m} (y_k - \hat{y}_k)$$

$$\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db} = -\frac{2}{m} \sum_{k=1}^{m} (y_k - \hat{y}_k)$$

Linear Regression Example:



With the gradients and the learning rate, update the parameters

$$w_1 \rightarrow w_1 - \alpha \frac{d(MSE)}{dw_1}$$
 $w_2 \rightarrow w_2 - \alpha \frac{d(MSE)}{dw_2}$ $w_n \rightarrow w_n - \alpha \frac{d(MSE)}{dw_n}$ $b \rightarrow b - \alpha \frac{d(MSE)}{db}$

$$w_2 \rightarrow w_2 - \alpha \frac{d(MSE)}{dw_2}$$

$$w_n \to w_n - \alpha \frac{d(MSE)}{dw_n}$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$

In terms of vectors:

$$\begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix} \rightarrow \begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix} - \alpha \begin{pmatrix} \frac{d(MSE)}{dw_1} \\ \frac{d(MSE)}{dw_2} \\ \vdots \\ \frac{d(MSE)}{dw_n} \end{pmatrix} \qquad if \ dW = \begin{pmatrix} \frac{d(MSE)}{dw_1} \\ \frac{d(MSE)}{dw_2} \\ \vdots \\ \frac{d(MSE)}{dw_n} \end{pmatrix} \equiv \nabla MSE$$

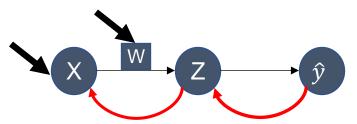
$$if \ dW = \begin{pmatrix} \frac{d(MSE)}{dw_1} \\ \frac{d(MSE)}{dw_2} \\ \vdots \\ \frac{d(MSE)}{dw_n} \end{pmatrix} \equiv \nabla MSE$$

$$W \rightarrow W - \alpha dW$$

Linear Regression



In Summary:



- 1. Random Initialisation: Neural Network assigns random values to W and b.
- 2. Foreward Propagation: The Network Calculates:

$$Z = W^T X + b$$
; $\hat{y} = Z$

3. Backpropagation: The network calculates derivatives to minimise the loss function

$$\frac{d(MSE)}{dw_i} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{dw_i} \qquad \qquad \frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$$

$$\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dZ} \frac{dZ}{db}$$

4. **Update Parameters**: Using the gradients, parameters (w,b) are updated

$$W \rightarrow W - \alpha dW$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$

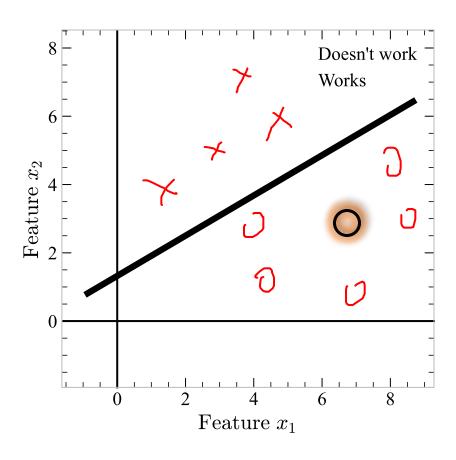
5. Repeat 2-4 for a set number of "Epochs"



Logistic Regression

Logistic Regression: Recap





We want to predict the probability that the engine will work.

Will this engine work?

Do this using **Logistic Regression**

Linear regression or Logistic Regression?



We want to predict a probability that is either 0 = 0% or 1 = 100%.

Linear regression gave us a value that is not between 0 and 1

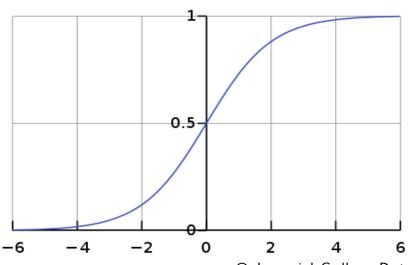
$$\hat{y} = w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_n x_n + \mathbf{b} = W^T X + \mathbf{b}$$

Wrap the result of the linear regression with another function.

In a neural network, this is called the **Activation Function**

$$g(x) = \frac{1}{1+e^{-x}}$$

Logistic Function

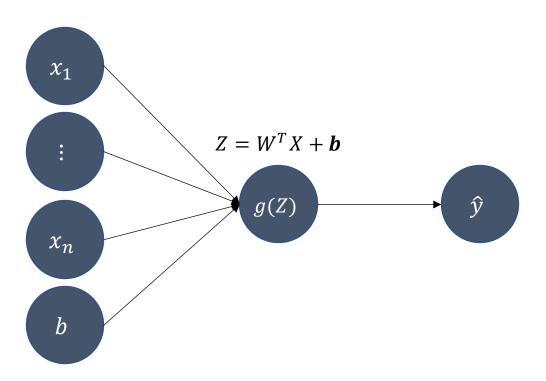


Logistic Regression as a NN



We can represent Logisitic Regression as a Simple Neural Network

$$g(x)=rac{1}{1+e^{-x}}$$

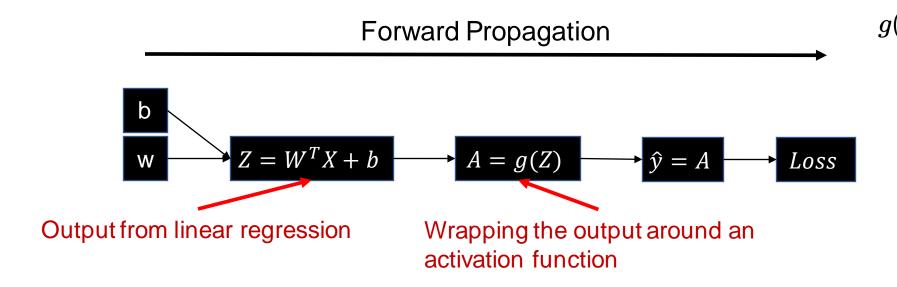


Logistic regression: the model



Logistic regression model:

Sigmoid function:



The probability that the engine works is represented by g(Z)

We still need to define a Loss function

Logistic Regression Loss Function



A measure of how "badly" the model performed.

Logistic Regression uses a "Cross Entropy" Loss Function

$$J = -\frac{1}{m} \sum_{i=1}^{m} y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$

y_i Label for the i-th example

 \hat{y}_i Prediction for the i-th example

Loss Function



$$J = -\frac{1}{m} \sum_{i=1}^{m} y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$
Average over all m examples
Loss for one example

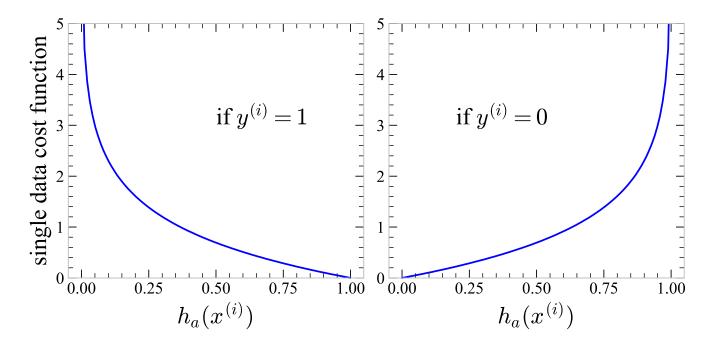
Note that: $0 \le \hat{y}_i \le 1$

- Meaning both $\log \hat{y}_i$ and $\log (1 \hat{y}_i)$ are negative
- A larger value of J should mean worse performance: minus sign added

Loss Function

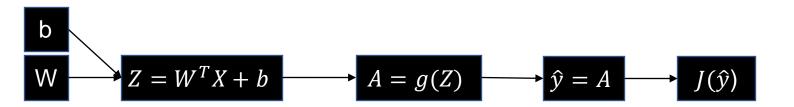


$$J = -\frac{1}{m} \sum_{i=1}^{m} y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$



Backpropagation in Logistic Regression





We need to compute:

$$\frac{d(J)}{dw_1}$$
; $\frac{d(J)}{dw_2}$; ...; $\frac{d(J)}{dw_n}$; $\frac{d(J)}{db}$

$$\frac{d(J)}{dw_i} = \frac{d(J)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{dw_i}$$

$$\frac{d(J)}{db} = \frac{d(J)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{db}$$

$$\begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix} \rightarrow \begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix} - \alpha \begin{pmatrix} \frac{d(J)}{dw_1} \\ \frac{d(J)}{dw_2} \\ \vdots \\ \frac{d(J)}{dw_n} \end{pmatrix}$$

$$W \to W - \alpha dW$$

$$b \to b - \alpha \frac{d(MSE)}{db}$$

Loss Function Derivative



$$J = -\frac{1}{m} \sum_{i=1}^{m} y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$

Determine
$$\frac{dJ}{d\hat{y}}$$
: Let $L(y_i, \hat{y}_i) = y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$

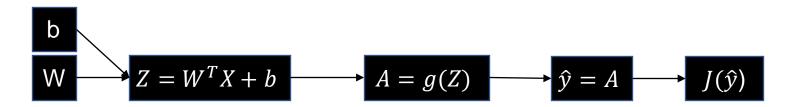
$$\frac{dJ}{d\hat{y}} = \frac{d}{d\hat{y}} \left(-\frac{1}{m} \sum_{i=1}^{m} L(y_i, \hat{y}_i) \right) \qquad \qquad \frac{dJ}{d\hat{y}} = -\frac{1}{m} \sum_{i=1}^{m} \frac{d}{d\hat{y}} (L(y_i, \hat{y}_i))$$

$$\frac{d}{d\hat{y}}\left(L(y_i, \hat{y}_i)\right) = \frac{y_i}{\hat{y}_i} - \frac{(1 - y_i)}{1 - \hat{y}_i}$$

$$\frac{dJ}{d\widehat{y}} = -\frac{1}{m} \sum_{i=1}^{m} \left\{ \frac{y_i}{\widehat{y}_i} - \frac{(1-y_i)}{1-\widehat{y}_i} \right\}$$

Backpropagation in Logistic Regression





Now compute the derivatives

$$\frac{d(J)}{dw_{i}} = \frac{d(J)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{dw_{i}} \qquad \qquad \frac{d(J)}{db} = \frac{d(J)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{db}$$

$$\frac{dJ}{d\hat{y}} = -\frac{1}{m} \sum_{i=1}^{m} \left\{ \frac{y_{i}}{\hat{y}_{i}} - \frac{(1 - y_{i})}{1 - \hat{y}_{i}} \right\} \qquad \qquad \frac{d\hat{y}}{dA} = 1; \frac{dA}{dZ} = A(1 - A); \frac{dZ}{dw_{i}} = x_{i}; \frac{dZ}{db} = 1$$

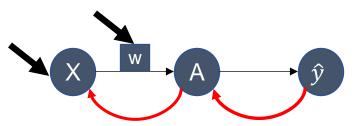
$$\frac{d(J)}{dw_{i}} = -\frac{1}{m} A(1 - A) x_{i} \sum_{k=1}^{m} \left\{ \frac{y_{k}}{\hat{y}_{k}} - \frac{(1 - y_{k})}{1 - \hat{y}_{k}} \right\}$$

$$\frac{d(J)}{db} = -\frac{1}{m} A(1 - A) \sum_{k=1}^{m} \left\{ \frac{y_{k}}{\hat{y}_{k}} - \frac{(1 - y_{k})}{1 - \hat{y}_{k}} \right\}$$

Logistic Regression



In Summary:



- 1. Random Initialisation: Neural Network assigns random values to W and b.
- 2. Forward Propagation: The Network Calculates:

$$Z = W^{T}X + b$$
; $A = g(Z)$; $\hat{y} = A$

3. Backpropagation: The network calculates derivatives to minimise the loss function

$$\frac{d(J)}{dw_i} = \frac{d(J)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{dw_i}$$

$$\frac{d(MSE)}{db} = \frac{d(MSE)}{d\hat{y}} \frac{d\hat{y}}{dA} \frac{dA}{dZ} \frac{dZ}{db}$$

4. Update Parameters: Using the gradients, parameters (w,b) are updated

$$w \rightarrow w - \alpha dW$$

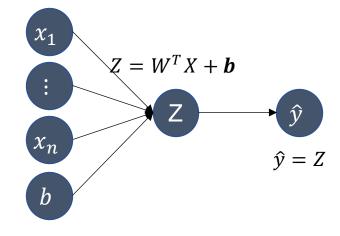
$$b \to b - \alpha \frac{d(MSE)}{db}$$

5. Repeat 2-4 for a set number of "Epochs"

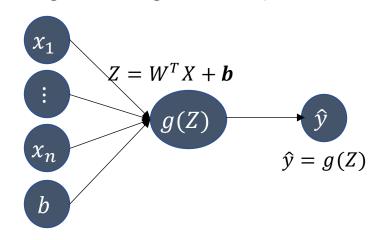
What about General NNs?



Linear Regression



Logistic Regression (Classification)



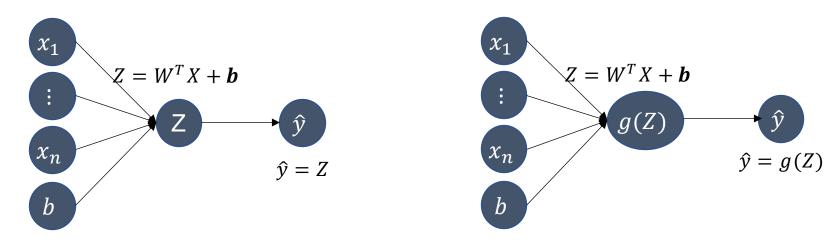
See that a neural network can function as a regressor or a classifier It only depends on which activation function we are using!



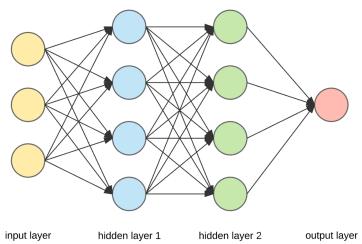
What about General NNs?



Until now, we only considered problems where there are only 1 neuron and 1 hidden layer.

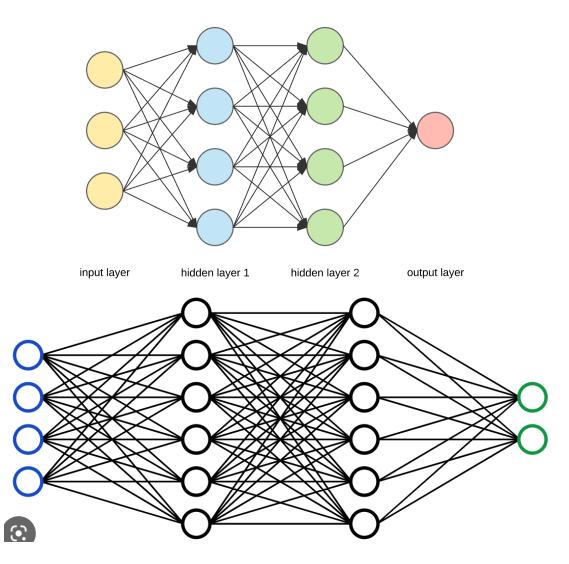


What about general neural networks?



Some (More) Notation



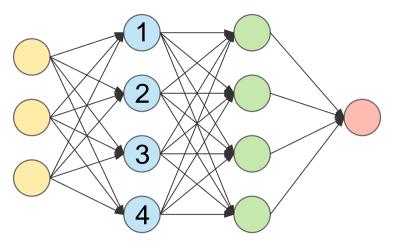


- Input, Label Matrix: X, Y
- Prediction Matrix: \hat{y}
- Number Of Layers: All layers excluding input
- Input Layer: Layer 0
- Number of examples: m
- Input, Label Size: n_x , n_y
- Values in layer L is denoted by: W^[L]
- Number of neurons in (hidden) layer L: $n_h^{[L]}$



Consider Input Layer to hidden layer 1 and number each hidden neuron 1 to 4 with some activation

function $g^{[1]}(x)$

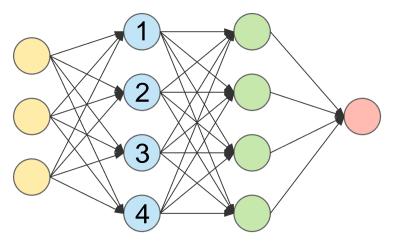


 $A_{1}^{[1]} = g^{[1]}\left(Z_{1}^{[1]}\right); where \ Z_{1}^{[1]} = w_{1,1}x_{1} + w_{2,1}x_{2} + w_{3,1}x_{3} + b_{1} = W_{1}^{[1]T}X + b_{1}$ $A_{2}^{[1]} = g^{[1]}\left(Z_{2}^{[1]}\right); where \ Z_{2}^{[1]} = w_{1,2}x_{1} + w_{2,2}x_{2} + w_{3,2}x_{3} + b_{2} = W_{2}^{[1]T}X + b_{2}$ $A_{3}^{[1]} = g^{[1]}\left(Z_{3}^{[1]}\right); where \ Z_{3}^{[1]} = w_{1,3}x_{1} + w_{2,3}x_{2} + w_{3,3}x_{3} + b_{3} = W_{3}^{[1]T}X + b_{3}$ $A_{4}^{[1]} = g^{[1]}\left(Z_{4}^{[1]}\right); where \ Z_{4}^{[1]} = w_{1,4}x_{1} + w_{2,4}x_{2} + w_{3,4}x_{3} + b_{4} = W_{4}^{[1]T}X + b_{4}$



Consider Input Layer to hidden layer 1 and number each hidden neuron 1 to 4 with some activation

function g(x)



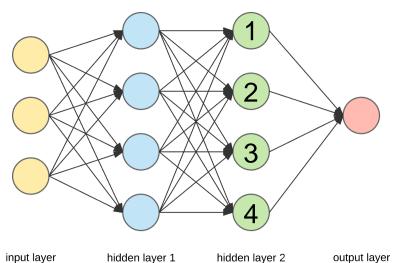
$$A^{[1]} = \begin{bmatrix} A_1^{[1]} \\ A_2^{[1]} \\ A_3^{[1]} \\ A_4^{[1]} \end{bmatrix} = \begin{bmatrix} g^{[1]}(W_1^{[1]T}X + b_1^{[1]}) \\ g^{[1]}(W_2^{[1]T}X + b_2^{[1]}) \\ g^{[1]}(W_3^{[1]T}X + b_3^{[1]}) \\ g^{[1]}(W_4^{[1]T}X + b_4^{[1]}) \end{bmatrix}$$

Now $A^{[1]}$ acts as the input for hidden layer 2



Now consider Hidden Layer 1 to Hidden Layer 2. Follow similar logic to previous slides, using

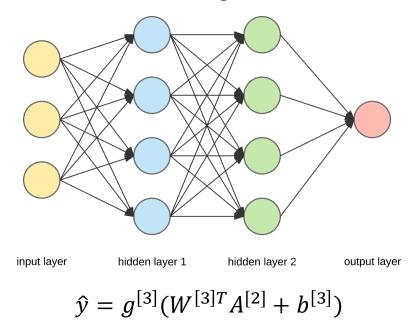
 $g^{[2]}(x)$ as the activation function



$$A^{[2]} = \begin{bmatrix} A_1^{[2]} \\ A_2^{[2]} \\ A_3^{[2]} \\ A_4^{[2]} \end{bmatrix} = \begin{bmatrix} g^{[2]}(W_1^{[2]T}A_1^{[1]} + b_1^{[2]}) \\ g^{[2]}(W_2^{[2]T}A_2^{[1]} + b_2^{[2]}) \\ g^{[2]}(W_3^{[2]T}A_3^{[1]} + b_3^{[2]}) \\ g^{[2]}(W_4^{[2]T}A_4^{[1]} + b_4^{[2]}) \end{bmatrix}$$



Finally for the output layer with activation function $g^{[3]}(x)$:



A general neural network will have to assign random values for: $W^{[1]}; W^{[2]}; W^{[3]}; b^{[1]}; b^{[2]}; b^{[3]}$

And then calculate derivatives for all parameters and then update using:

$$W \to W - \alpha dW \qquad \qquad b \to b - \alpha \frac{d(Loss)}{db}$$

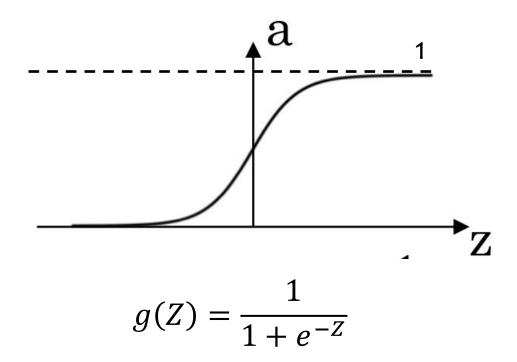


Activation Functions

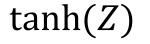
Activation Functions

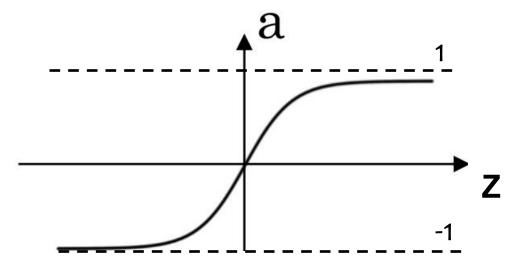


Sigmoid Function



Generally, **only** used for the output layer in a binary classification problem



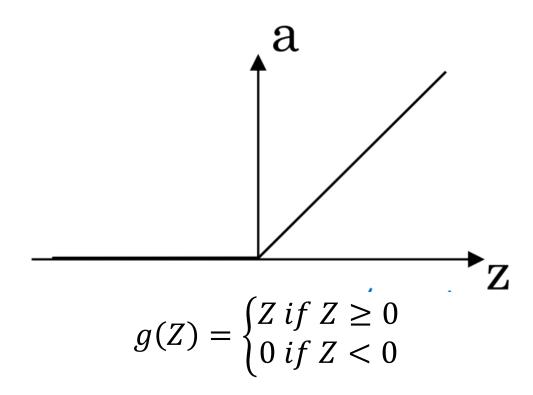


$$g(Z) = \tanh(Z) = \frac{e^{Z} - e^{-Z}}{e^{Z} + e^{-Z}}$$

Activation Functions



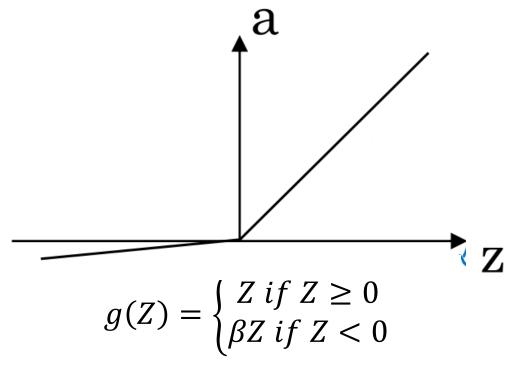




When in doubt, use ReLU

Easy to implement, closest to how a Neuron actually works

Leaky ReLU



Tends to perform better than just ReLU But 1 more hyperparameter to tune



Questions?