## GBS Generating $|011\rangle + |100\rangle$

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The input is given by

$$|r_i, \alpha_i\rangle = D(\alpha_i)S(r_i)|0\rangle,$$

where we set  $r_i, \alpha_i, \theta_i, \phi_i \in \mathbb{R}$ ,  $\forall i$ . In fact, my search parameter space was more strict

$$r_i \in [-1.73, 1.73]$$
 (note this is  $[-15 \text{ dB}, 15 \text{ dB}]$ )

$$\alpha_i \in [-1, 1]$$

$$\theta_i, \phi_i \in [-\pi, \pi]$$

using just global optimisation (basin hopping).

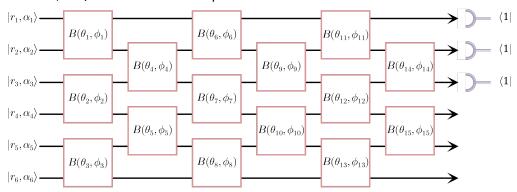
The gates are defined as

$$S(r) = \exp\left[\frac{1}{2}(r^*a^2 - ra^{\dagger^2})\right]$$
  
$$D(\alpha) = \exp\left[\alpha a^{\dagger} - \alpha^* a\right]$$

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$$B(\theta_i, \phi_i) = \exp[\theta(e^{i\phi}a_1a_2^{\dagger} - e^{-i\phi}a_1^{\dagger}a_2)]$$

and we detect  $\langle 111 |$  in the first three output modes as follows



An m=6 interferometer needs  $\frac{m(m-1)}{2}=15$  beam-splitters to make any unitary transformation.

See para\_x.csv files for ordered list of variables. This leads to a three mode output state  $|\psi\rangle$  with fidelity and probability

$$F = |\langle 011|\psi\rangle + \langle 100|\psi\rangle|^2 = 0.9998$$

$$P = 2.1065 \times 10^{-6}$$

Note that the output state has a global phase shift  $|\psi\rangle \approx e^{-0.4i}(|011\rangle + |001\rangle)$ .