

## ELA DA 1 – DOS: 21.08.2022

### Task - 1: GENERATION OF ELEMENTARY SIGNALS AND SYSTEM ANALYSIS

**Q1) Generate the elementary signals that are employed for characterization of random signals. Also, generate a sinusoidal signal and subject the same to the following basic signal processing operations. a. Time Shifting / Delaying (TD) b. Folding / Reflection (FD) c. Verify, whether  $TD[FD]=FD[TD]$  d. Convolution e. Correlation Illustrate the above operations with relevant waveforms.**

#### CODE:

```
%Task - 1: GENERATION OF ELEMENTARY SIGNALS AND SYSTEM ANALYSIS
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%Course: ECE3051 - ELA

%SubTask 1 - Generate the elementary signals that are employed for
characterization of random
%signals. Also, generate a sinusoidal signal and subject the same to the following
basic
%signal processing operations
%a. Time Shifting / Delaying (TD)
%b. Folding / Reflection (FD)
%c. Verify, whether  $TD[FD]=FD[TD]$ 
%d. Convolution
%e. Correlation
%Illustrate the above operations with relevant waveforms.

%Elementary Functions:
%Zero Function
a = zeros(1,5);
b = a;
subplot(331),stem(b);
title('Zeros Function');
xlabel('Time');
ylabel('Magnitude');
grid;

%Ones Function
a = ones(1,5);
b = a;
subplot(332),stem(b);
title('Ones Function');
xlabel('Time');
```

```

ylabel('Magnitude');
grid;

%Impulse Function
a = zeros(1,4);
b = [a,1,a];
subplot(333),stem(b);
title('Impulse Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Unit Step Function
a = zeros(1, 4);
b = ones(1, 4);
c = [a,1,b];

t = (-1:0.01:5)';
% Start with all zeros:
unitstep = zeros(size(t));
% But make everything corresponding to t>=1 one:
unitstep(t>=0) = 1;
plot(t,unitstep,'b','linewidth',3)
% Repeat, with everything shifted to the right by 1 unit:
unitstep2 = zeros(size(t));
unitstep2(t>=2) = 1;
hold on
plot(t,unitstep2,'r:','linewidth',2)

subplot(334),stem(c);
title('Unit Step Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Sine Function
a = 0:15:360;
b = sind(a);
subplot(335),stem(b);
title('Sine Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Cosine Function
a = 0:15:360;
b = cosd(a);
subplot(336),stem(b);
title('Cosine Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Exponential Signal
a = 1:20;
b = exp(a);
subplot(337),stem(b); %plot(b)
title('Exponential Function');
xlabel('time');

```

```

ylabel('Magnitude');
grid;

%Ramp Function
a = 1:10;
b = a;
subplot(338),stem(b);
title('Ramp Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Parabolic Signal
a = linspace(-5,5,10);
b = 0.5*a.^2;
subplot(339),stem(a,b);
title('Parabolic Function');
xlabel('time');
ylabel('Magnitude');
grid;

%Generate a sinusoidal signal and subject the same to the following basic
a = 0:15:360;
b = sind(a);
subplot(331),stem(b);
title('Base Sinusoidal Function');
xlabel('time');
ylabel('Magnitude');
grid;

%signal processing operations:
%a. Time Shifting / Delaying (TD)
a = 0:15:360;
b = sind(a+30);
subplot(332),stem(b);
title('Time Delayed Sinusoidal Function');
xlabel('time');
ylabel('Magnitude');
grid;

%b. Folding / Reflection (FD)
a = 0:15:360;
b = sind(-a);
subplot(333),stem(b);
title('Folded Sinusoidal Function');
xlabel('time');
ylabel('Magnitude');
grid;

%c. Verify, whether TD[FD]=FD[TD]
a = 0:15:360;
x1 = sind(-sind(a+30));
y1 = sind(sind(-a-30));
subplot(211),stem(x1);
title('FD[TD] Function');
xlabel('time');
ylabel('Magnitude');
grid;

```

```

subplot(212),stem(y1);
title('TD[FD] Function');
xlabel('time');
ylabel('Magnitude');
grid;

%d. Convolution
Fs = 10000;
Ts = 1/Fs;
fc = 1000;
Tc = 1/fc;
t = 0:Ts:Tc;
% LTI impulse response h(t) = exp(-1000*t)
h = exp(-1000*t);
% angular frequency w = 2*pi*fc
w = 2*pi*fc;
% the signal x(t) = sin(wc*t)
x = sin(w*t);
% convolution of x(t) and h(t)
y = conv(x,h,'same');
subplot(3, 1, 1);
plot(t, h, 'LineWidth', 2);
grid on;
xlabel('t');
ylabel('h');
subplot(3, 1, 2);
plot(t, x, 'LineWidth', 2)
grid on;
xlabel('t');
ylabel('x');
subplot(3, 1, 3);
plot(t, y, 'LineWidth', 2)
grid on;
hold on
stem(t,y)
xlabel('t');
ylabel('y = x**h');

%e. Correlation
a = 0:15:360;
x = sind(a+30);
y = sind(-a);
R = corrcoef(x,y);
disp("The Result is: ");
disp(R);

```

### OUTPUT:

```
>> %Elementary Functions:
```

```
%Zero Function
```

```
a = zeros(1,5);
```

```
b = a;
```

```
subplot(331),stem(b);
```

```
title('Zeros Function');
```

```
xlabel('Time');  
ylabel('Magnitude');  
grid;
```

```
%Ones Function  
a = ones(1,5);  
b = a;  
subplot(332),stem(b);  
title('Ones Function');  
xlabel('Time');  
ylabel('Magnitude');  
grid;
```

```
%Impulse Function  
a = zeros(1,4);  
b = [a,1,a];  
subplot(333),stem(b);  
title('Impulse Function');  
xlabel('time');  
ylabel('Magnitude');  
grid;
```

```
%Unit Step Function  
a = zeros(1,4);  
b = ones(1,4);  
c = [a,1,b];
```

```
t = (-1:0.01:5)';  
% Start with all zeros:  
unitstep = zeros(size(t));  
% But make everything corresponding to  $t \geq 1$  one:
```

```

unitstep(t>=0) = 1;
plot(t,unitstep,'b','linewidth',3)
% Repeat, with everything shifted to the right by 1 unit:
unitstep2 = zeros(size(t));
unitstep2(t>=2) = 1;
hold on
plot(t,unitstep2,'r','linewidth',2)

```

```

subplot(334),stem(c);
title('Unit Step Function');
xlabel('time');
ylabel('Magnitude');
grid;

```

```

%Sine Function
a = 0:15:360;
b = sind(a);
subplot(335),stem(b);
title('Sine Function');
xlabel('time');
ylabel('Magnitude');
grid;

```

```

%Cosine Function
a = 0:15:360;
b = cosd(a);
subplot(336),stem(b);
title('Cosine Function');
xlabel('time');
ylabel('Magnitude');
grid;

```

```
%Exponential Signal
```

```
a = 1:20;
```

```
b = exp(a);
```

```
subplot(337),stem(b); %plot(b)
```

```
title('Exponential Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
%Ramp Function
```

```
a = 1:10;
```

```
b = a;
```

```
subplot(338),stem(b);
```

```
title('Ramp Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
%Parabolic Signal
```

```
a = linspace(-5,5,10);
```

```
b = 0.5*a.^2;
```

```
subplot(339),stem(a,b);
```

```
title('Parabolic Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
>> %Generate a sinusoidal signal and subject the same to the following basic
```

```
a = 0:15:360;
```

```
b = sind(a);
```

```
subplot(331),stem(b);
```

```
title('Base Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
%signal processing operations:
```

```
%a. Time Shifting / Delaying (TD)
```

```
a = 0:15:360;
```

```
b = sind(a+30);
```

```
subplot(332),stem(b);
```

```
title('Time Delayed Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
%b. Folding / Reflection (FD)
```

```
a = 0:15:360;
```

```
b = sind(-a);
```

```
subplot(333),stem(b);
```

```
title('Folded Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
>> %Generate a sinusoidal signal and subject the same to the following basic
```

```
a = 0:15:360;
```

```
b = sind(a);
```

```
subplot(311),stem(b);
```

```
title('Base Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```



%signal processing operations:

%a. Time Shifting / Delaying (TD)

```
a = 0:15:360;
```

```
b = sind(a+30);
```

```
subplot(312),stem(b);
```

```
title('Time Delayed Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

%b. Folding / Reflection (FD)

```
a = 0:15:360;
```

```
b = sind(-a);
```

```
subplot(313),stem(b);
```

```
title('Folded Sinusoidal Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

>> %c. Verify, whether  $TD[FD]=FD[TD]$

```
a = 0:15:360;
```

```
x1 = sind(-sind(a+30));
```

```
y1 = sind(sind(-a-30));
```

```
subplot(211),stem(x1);
```

```
title('FD[TD] Function');
```

```
xlabel('time');
```

```
ylabel('Magnitude');
```

```
grid;
```

```
subplot(212),stem(y1);
```

```
title('TD[FD] Function');
```

```
xlabel('time');
```

```

ylabel('Magnitude');

grid;

>> %d. Convolution

Fs = 10000;

Ts = 1/Fs;

fc = 1000;

Tc = 1/fc;

t = 0:Ts:Tc;

% LTI impulse response  $h(t) = \exp(-1000*t)$ 

h = exp(-1000*t);

% angular frequency  $w = 2*\pi*fc$ 

w = 2*pi*fc;

% the signal  $x(t) = \sin(wc*t)$ 

x = sin(w*t);

% convolution of  $x(t)$  and  $h(t)$ 

y = conv(x,h,'same');

subplot(3, 1, 1);

plot(t, h, 'LineWidth', 2);

grid on;

xlabel('t');

ylabel('h');

subplot(3, 1, 2);

plot(t, x, 'LineWidth', 2)

grid on;

xlabel('t');

ylabel('x');

subplot(3, 1, 3);

plot(t, y, 'LineWidth', 2)

grid on;

hold on

stem(t,y)

```

```
xlabel('t');
ylabel('y = x**h');
```

```
%e. Correlation
```

```
a = 0:15:360;
```

```
x = sind(a+30);
```

```
y = sind(-a);
```

```
R = corrcoef(x,y);
```

```
disp("The Result is: ");
```

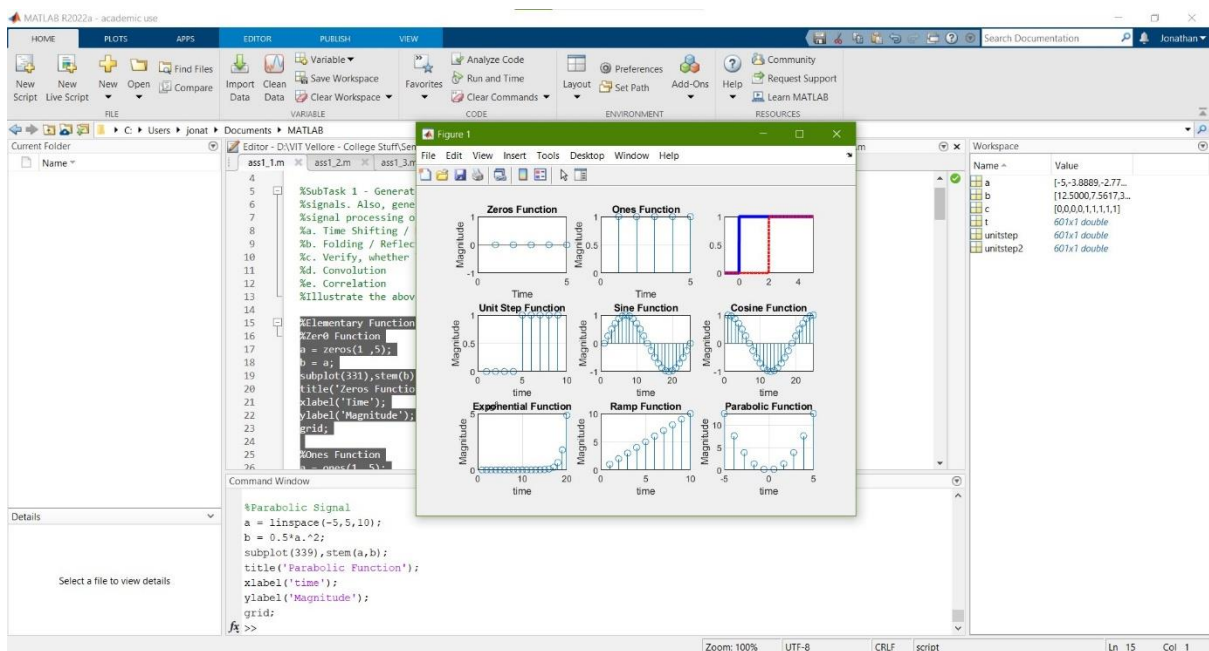
```
disp(R);
```

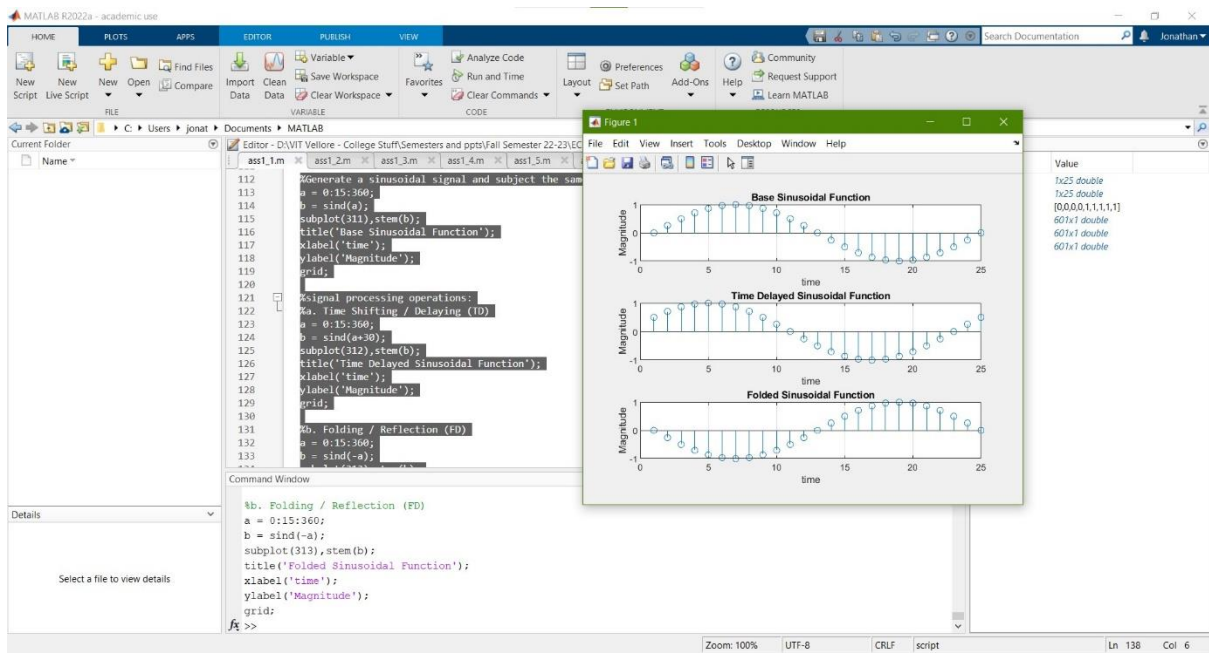
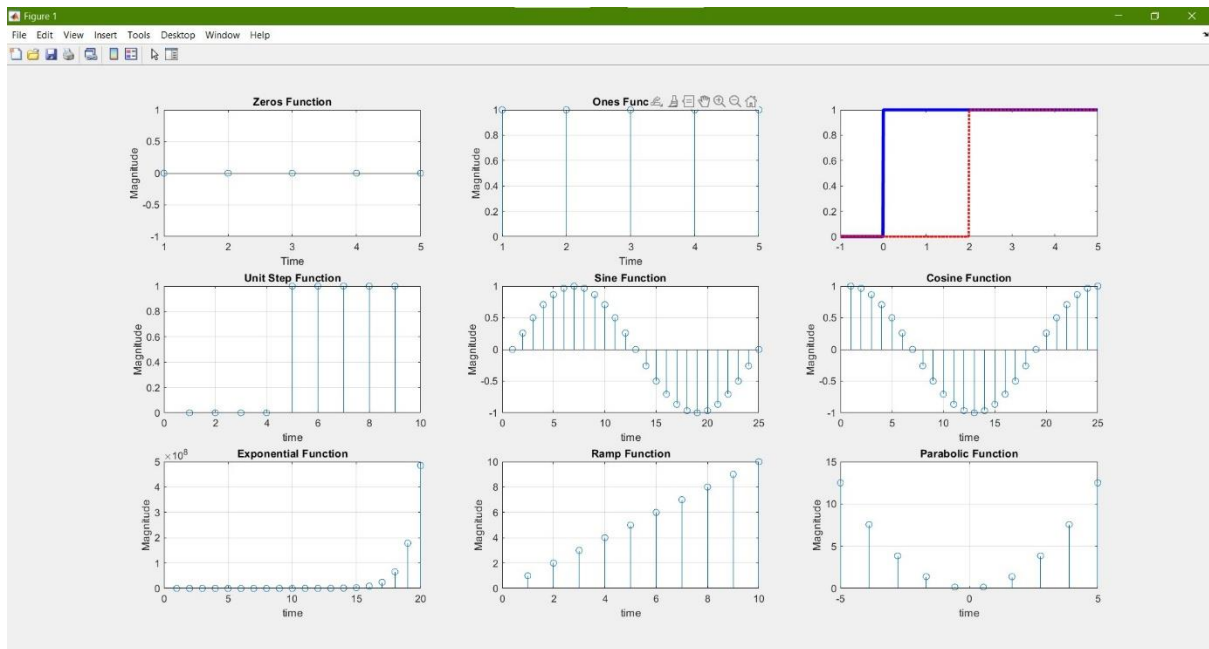
```
The Result is:
```

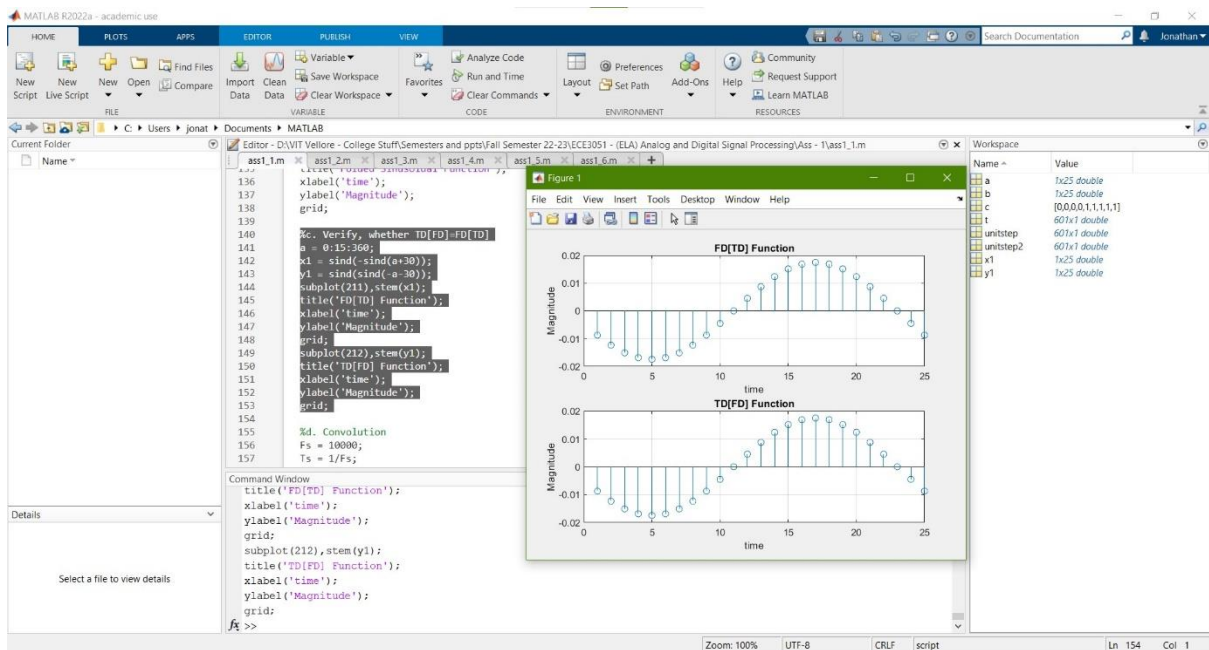
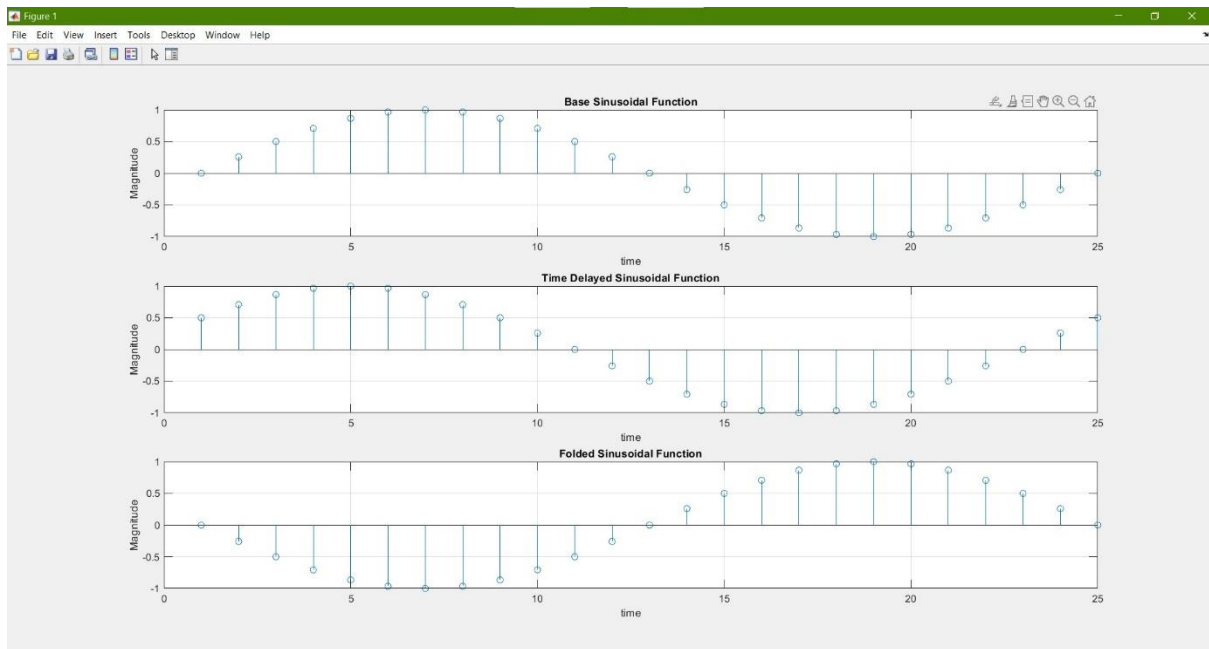
```
1.0000 -0.8575
```

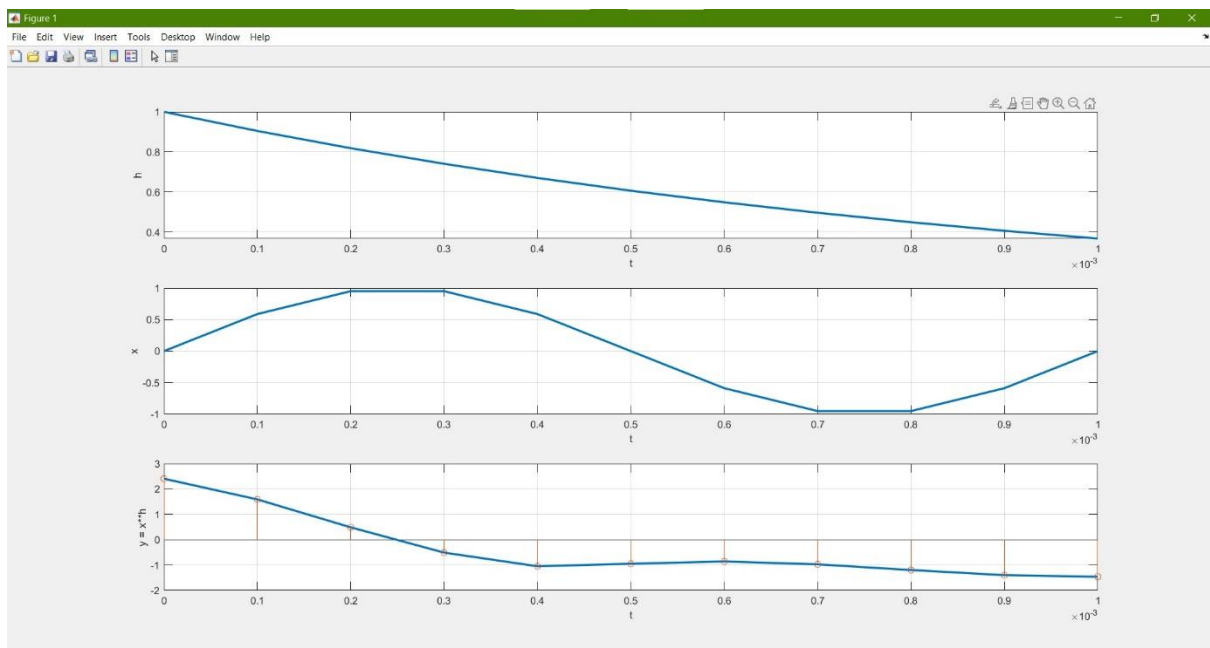
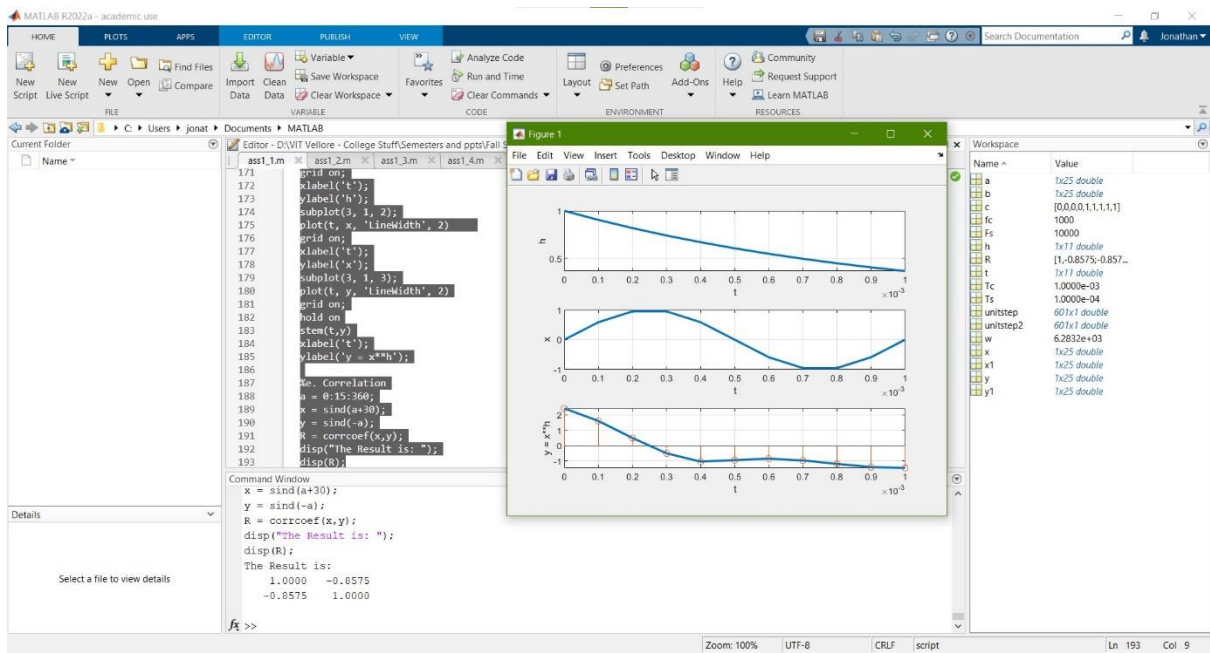
```
-0.8575 1.0000
```

```
>>
```









**Q2)** Also, graphically verify whether the following system is linear / non-linear, Stable / unstable:  
 $y(n) = y^2(n-1) + x(n)$ , for the bounded input  $x(n) = u(n) + u(n-2)$

**CODE:**

```
%SubTask 2 - graphically verify whether the following system is linear / non-
linear,
% Stable /unstable:

%  $y(n) = y^2(n-1) + x(n)$ , for the bounded input  $x(n) = u(n) + u(n-2)$ 

n0 = -5:5; %range
syms x(n);
x(n) = heaviside(n)-heaviside(n-2);
syms y(n);
y(n) = ((n-1))^2 + x(n);
subplot(111),plot(y(n0),n0);
title('Sequence #1 - Stem');
xlabel('x(n)');
ylabel('n0');

%1) Condition for Linearity: Relationship between x & y is linear (straight
%line), and should cross the origin.
%Answer: NO, it is not Linear, as it does not pass through origin and does
%not satisfy superposition.

%2) Condition for Stability: Should Satisfy the BIBO stability condition.
B = isstable(y);
disp(B);
```

**OUTPUT:**

```
>> %SubTask 2 - graphically verify whether the following system is linear / non-linear,
% Stable /unstable:
```

```
%  $y(n) = y^2(n-1) + x(n)$ , for the bounded input  $x(n) = u(n) + u(n-2)$ 
```

```
n0 = -5:5; %range
syms x(n);
x(n) = heaviside(n)-heaviside(n-2);
syms y(n);
y(n) = ((n-1))^2 + x(n);
subplot(111),plot(y(n0),n0);
```

```
title('Sequence #1 - Stem');
```

```
xlabel('x(n)');
```

```
ylabel('n0');
```

%1) Condition for Linearity: Relationship between x & y is linear (straight %line), and should cross the origin.

%Answer: NO, it is not Linear, as it does not pass through origin and does

%not satisfy superposition.

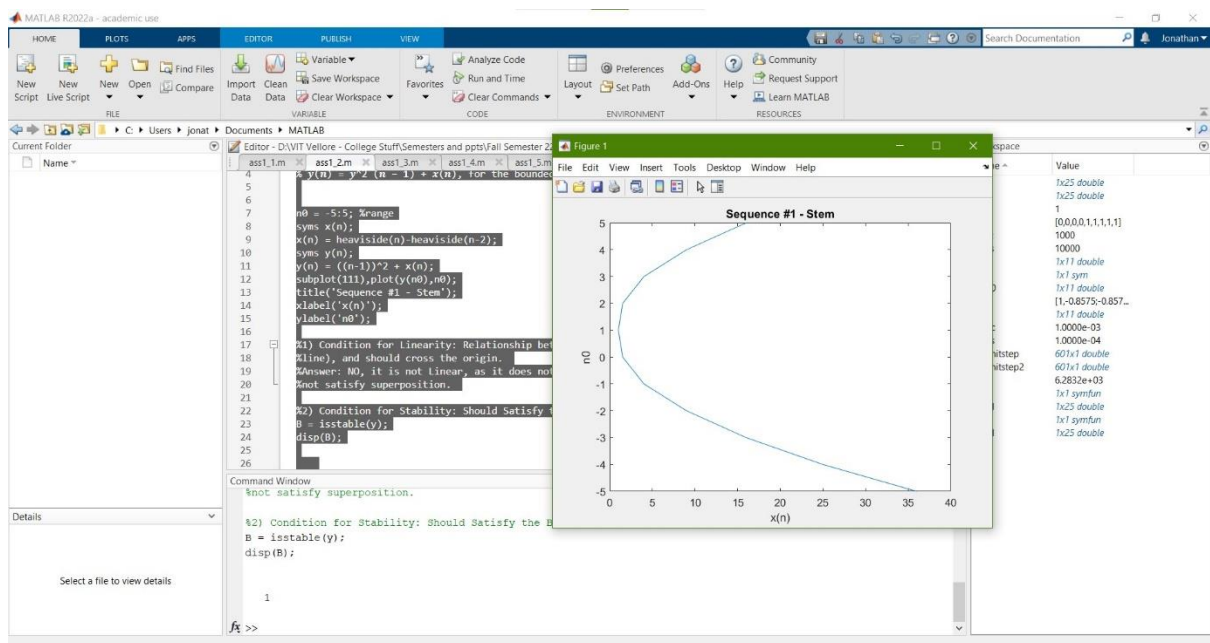
%2) Condition for Stability: Should Satisfy the BIBO stability condition.

```
B = isstable(y);
```

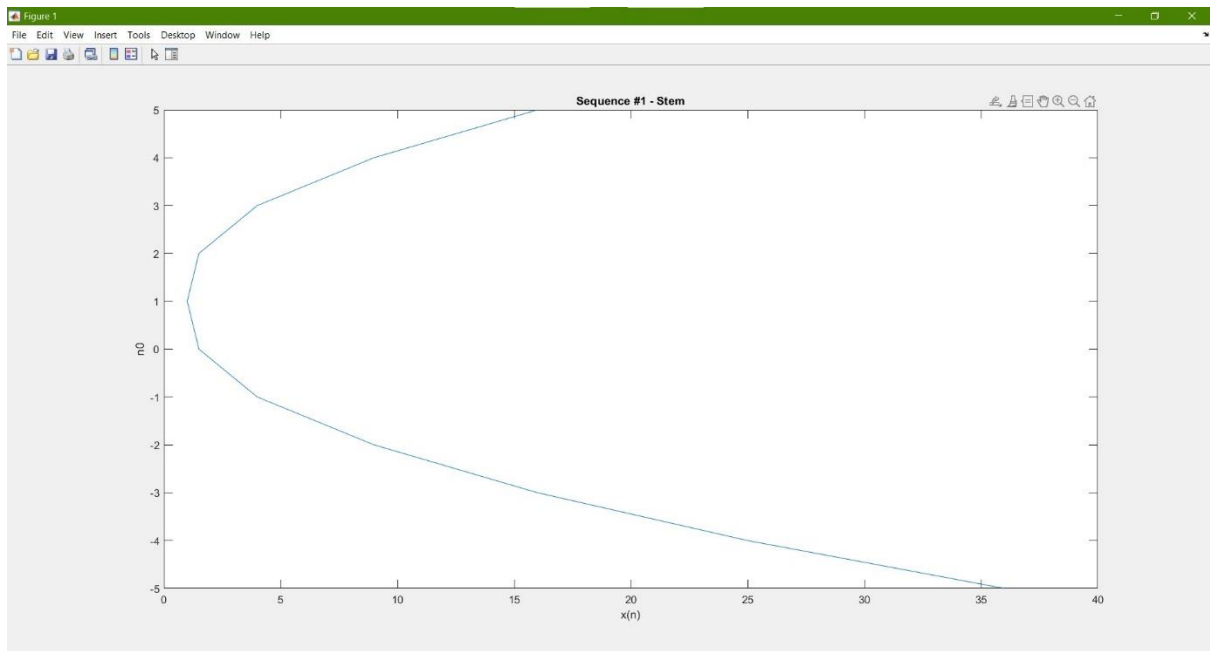
```
disp(B);
```

1

>>







**Q3) Generate and plot each of the following sequences over the indicated interval.**

**a)  $x(n) = 2\delta(n+2) - \delta(n-4)$ ,  $-5 \leq n \leq 5$**

**b)  $x(n) = n[u(n)-u(n-10)] + 10e^{-0.3(n-10)} [u(n-10) - u(n-20)]$**

**c)  $x(n) = \cos(0.04\pi n) + 0.2 * w(n)$ ,  $0 \leq n \leq 50$ , where  $w(n)$  is a Gaussian Random Sequence with zero limit and unit variance.**

**CODE:**

%SubTask 3 - Generate and plot each of the following sequences over the indicated interval.

%a)  $x(n) = 2\delta(n+2) - \delta(n-4)$ ,  $-5 \leq n \leq 5$

$n_0 = -5:5$ ; %range

syms  $x(n)$ ;

$x(n) = 2*\text{dirac}(n+2) - \text{dirac}(n-4)$ ;

subplot(321),stem( $x(n_0)$ , $n_0$ );

title('Sequence #1 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(322),plot( $x(n_0)$ , $n_0$ );

title('Sequence #1');

xlabel('x(n)');

ylabel('n0');

grid;

%b)  $x(n) = n[u(n)-u(n-10)] + 10e^{-0.3(n-10)} [u(n-10) - u(n-20)]$

$n_0 = -20:20$ ; %range

syms  $x(n)$ ;

$x(n) = n*(\text{heaviside}(n)-\text{heaviside}(n-10)) + (10*\exp(-0.3*(n-10))) * (\text{heaviside}(n-10) - \text{heaviside}(n-20))$ ;

subplot(323),stem( $x(n_0)$ , $n_0$ );

title('Sequence #2 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(324),plot( $x(n_0)$ , $n_0$ );

title('Sequence #2');

xlabel('x(n)');

ylabel('n0');

grid;

%c)  $x(n) = \cos(0.04\pi n) + 0.2 * w(n)$ ,  $0 \leq n \leq 50$ , where  $w(n)$  is a Gaussian

%Random Sequence with zero limit and unit variance.

$n_0 = 0:50$ ; %range

syms  $x(n)$ ;

$x(n) = \cos(0.04*\pi*n) + 0.2*\text{normrnd}(0,50);\text{normrnd}(n)$ ;

subplot(325),stem( $x(n_0)$ , $n_0$ );

title('Sequence #3 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(326),plot( $x(n_0)$ , $n_0$ );

title('Sequence #3');

xlabel('x(n)');

ylabel('n0');

grid;

### OUTPUT:

>> %SubTask 3 - Generate and plot each of the following sequences over the indicated interval.

%a)  $x(n) = 2\delta(n+2) - \delta(n-4)$ ,  $-5 \leq n \leq 5$

$n_0 = -5:5$ ; %range

syms  $x(n)$ ;

$x(n) = 2*\text{dirac}(n+2) - \text{dirac}(n-4)$ ;

subplot(321),stem( $x(n_0)$ , $n_0$ );

title('Sequence #1 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(322),plot( $x(n_0)$ , $n_0$ );

title('Sequence #1');

xlabel('x(n)');

ylabel('n0');

grid;

%b)  $x(n) = n[u(n)-u(n-10)] + 10e^{-0.3(n-10)} [u(n-10) - u(n-20)]$

$n_0 = -20:20$ ; %range

syms  $x(n)$ ;

$x(n) = n*(\text{heaviside}(n)-\text{heaviside}(n-10)) + (10*\exp(-0.3*(n-10)) * (\text{heaviside}(n-10) - \text{heaviside}(n-20)))$ ;

subplot(323),stem( $x(n_0)$ , $n_0$ );

title('Sequence #2 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(324),plot( $x(n_0)$ , $n_0$ );

title('Sequence #2');

xlabel('x(n)');

ylabel('n0');

grid;

%c)  $x(n) = \cos(0.04\pi*n) + 0.2 * w(n)$ ,  $0 \leq n \leq 50$ , where  $w(n)$  is a Gaussian

%Random Sequence with zero limit and unit variance.

n0 = 0:50; %range

syms x(n);

x(n) = cos(0.04\*pi\*n) + 0.2\*normrnd(0,50);%normrnd(n);

subplot(325),stem(x(n0),n0);

title('Sequence #3 - Stem');

xlabel('x(n)');

ylabel('n0');

subplot(326),plot(x(n0),n0);

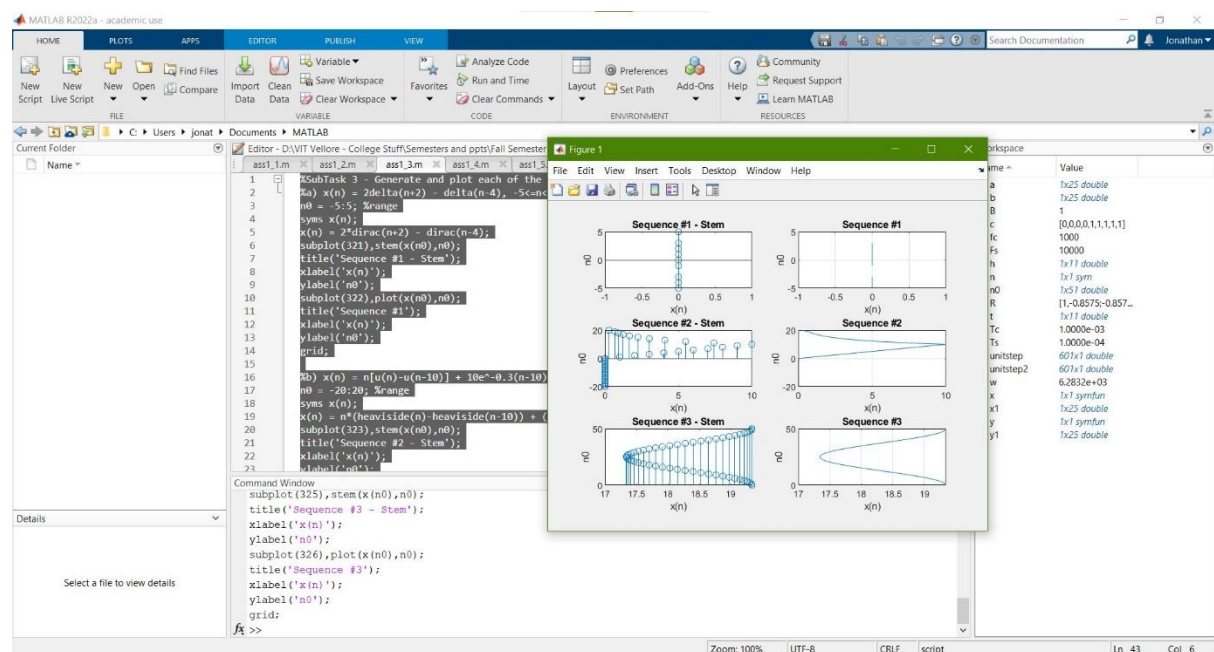
title('Sequence #3');

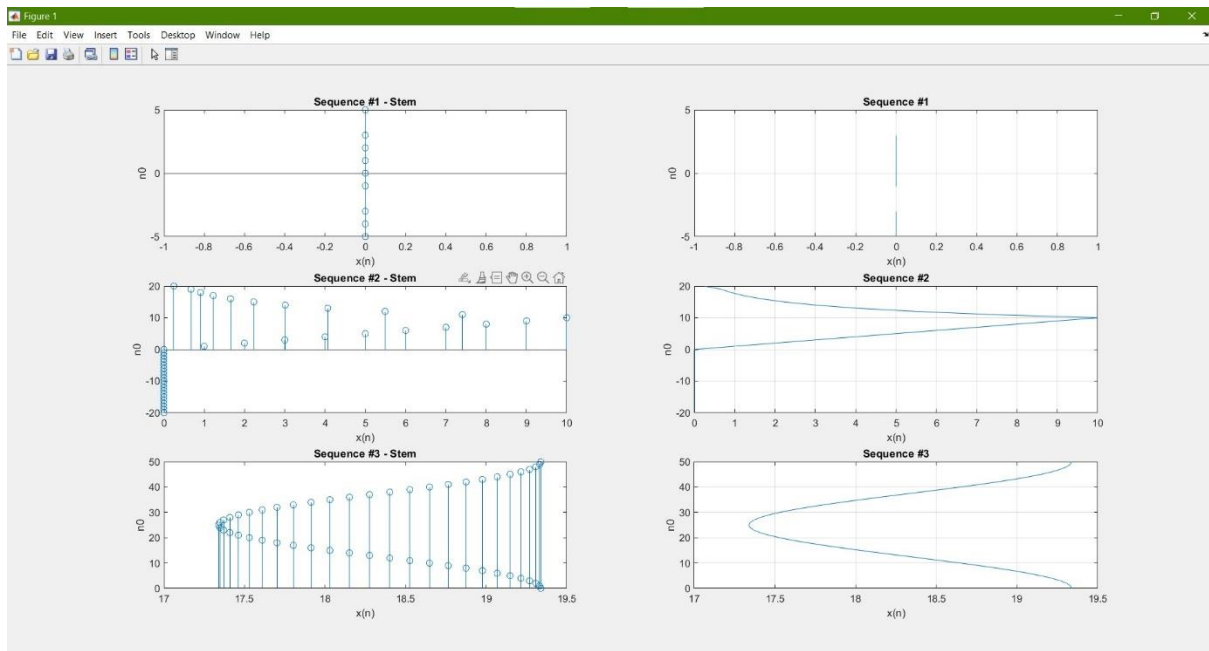
xlabel('x(n)');

ylabel('n0');

grid;

>>





**Q4) Given the following difference equation:**

$$y(n) - y(n-1) + 0.9y(n-2) = x(n); \text{ for all } n$$

**a) Calculate and plot the impulse response  $h(n)$  at  $n = -20, \dots, 100$ .**

**b) Calculate and plot the unit step response  $s(n)$  at  $n = -20, \dots, 100$ .**

**c) Is the system specified by  $h(n)$  stable?**

**CODE:**

```
%Given the following difference equation:
% y(n) - y(n-1) + 0.9y(n-2) = x(n); for all n

%Therefore: We need to use the filter function
%Let us take coefficients of both y (here a) and x (here b)

a = [1 -1 9/10];
b = 1;
y = -20:100;
x = filter(a,b,y);
subplot(321),plot(x,y);
title('Difference Equation of following equation');
xlabel('x');
ylabel('y');
subplot(322),stem(x,y);
title('Difference Equation of following equation');
xlabel('x');
ylabel('y');

% a) Calculate and plot the impulse response h(n) at n = -20, . . . ,100.
subplot(323),plot(dirac(x));
title('impulse response h(n) at n = -20, . . . ,100. ');
xlabel('x');
ylabel('y');
subplot(324),stem(dirac(x));
title('impulse response h(n) at n = -20, . . . ,100. ');
xlabel('x');
ylabel('y');

% b) Calculate and plot the unit step response s(n) at n = -20, . . . , 100.
subplot(325),plot(heaviside(x));
title('unit step response s(n) at n = -20, . . . ,100. ');
xlabel('x');
ylabel('y');
subplot(326),stem(heaviside(x));
title('unit step response s(n) at n = -20, . . . ,100. ');
xlabel('x');
ylabel('y');
% c) Is the system specified by h(n) stable?
B = isstable(dirac(x));
disp(B);
```

### OUTPUT:

>> %Given the following difference equation:

%  $y(n) - y(n-1) + 0.9y(n-2) = x(n)$ ; for all  $n$

%Therefore: We need to use the filter function

%Let us take coefficients of both  $y$  (here  $a$ ) and  $x$  (here  $b$ )

$a = [1 \ -1 \ 9/10];$

$b = 1;$

$y = -20:100;$

$x = \text{filter}(a,b,y);$

$\text{subplot}(321), \text{plot}(x,y);$

$\text{title}('Difference \text{ Equation of following equation}');$

$\text{xlabel}('x');$

$\text{ylabel}('y');$

$\text{subplot}(322), \text{stem}(x,y);$

$\text{title}('Difference \text{ Equation of following equation}');$

$\text{xlabel}('x');$

$\text{ylabel}('y');$

% a) Calculate and plot the impulse response  $h(n)$  at  $n = -20, \dots, 100$ .

$\text{subplot}(323), \text{plot}(\text{dirac}(x));$

$\text{title}('impulse \text{ response } h(n) \text{ at } n = -20, \dots, 100.');$

$\text{xlabel}('x');$

$\text{ylabel}('y');$

$\text{subplot}(324), \text{stem}(\text{dirac}(x));$

$\text{title}('impulse \text{ response } h(n) \text{ at } n = -20, \dots, 100.');$

$\text{xlabel}('x');$

$\text{ylabel}('y');$

% b) Calculate and plot the unit step response  $s(n)$  at  $n = -20, \dots, 100$ .

```

subplot(325),plot(heaviside(x));

title('unit step response s(n) at n = -20,...,100.');
```

xlabel('x');

ylabel('y');

```

subplot(326),stem(heaviside(x));

title('unit step response s(n) at n = -20,...,100.');
```

xlabel('x');

ylabel('y');

% c) Is the system specified by h(n) stable?

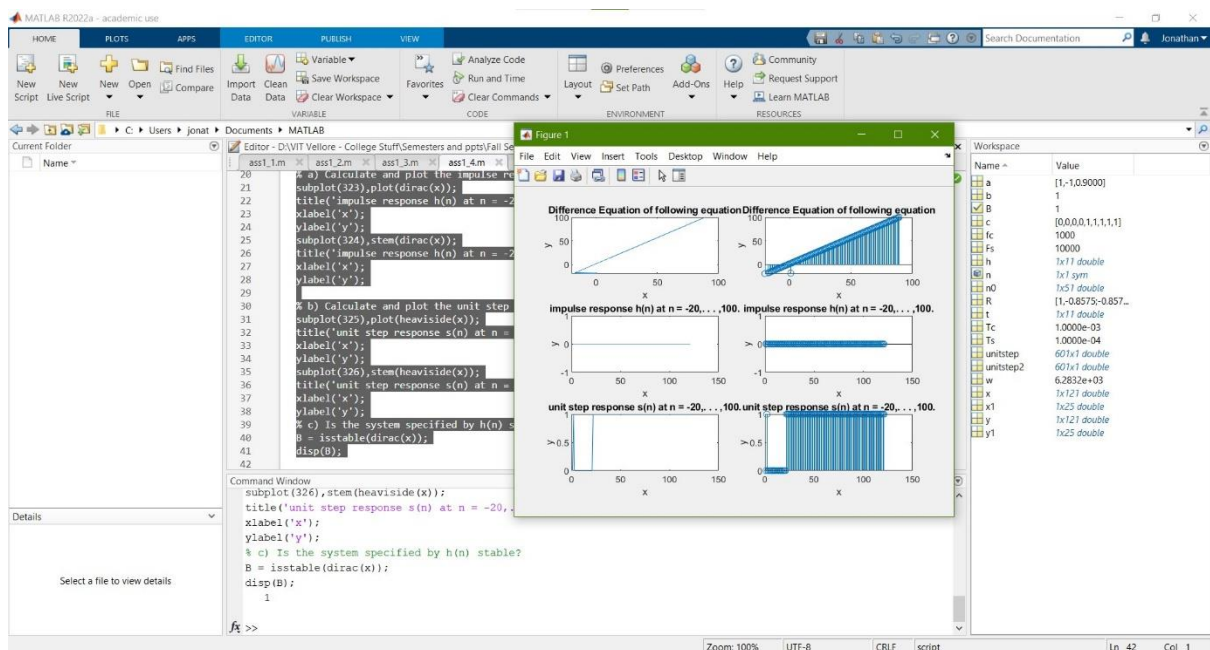
```

B = isstable(dirac(x));

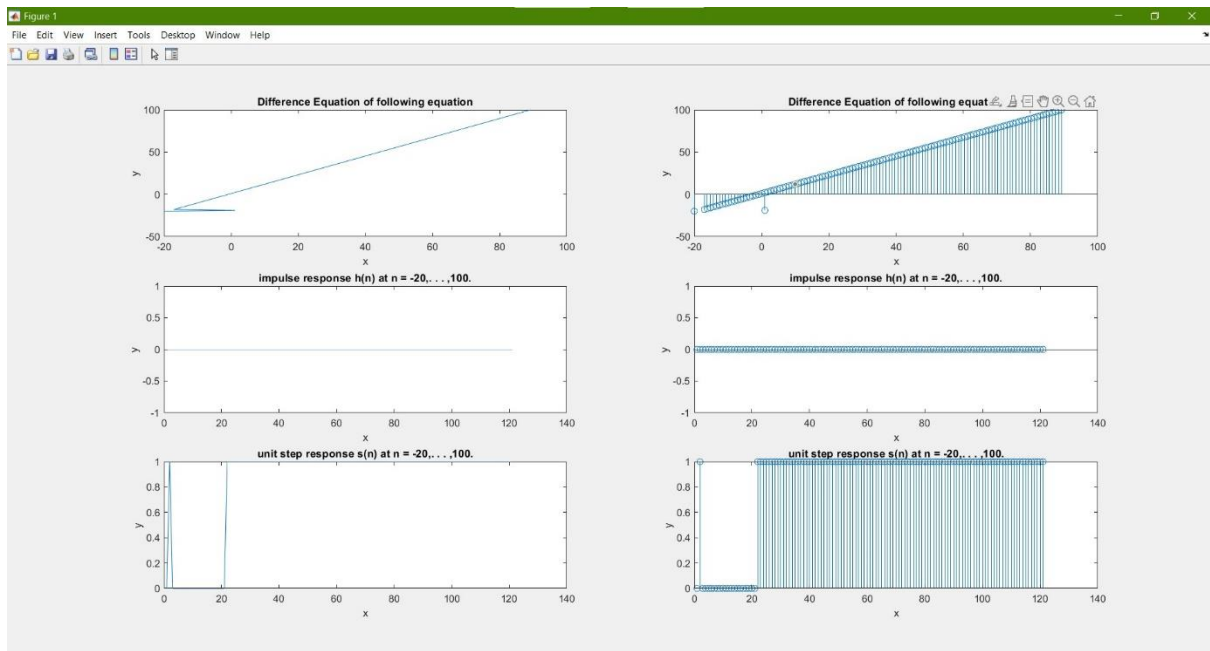
disp(B);
```

1

>>







**Q5) A particular linear and time-invariant system is described by the difference equation:**

$$y(n) - 0.5y(n-1) + 0.25y(n-2) = x(n) + 2x(n-1) + x(n-3)$$

- a) Determine the stability of the system.
- b) Determine and plot the impulse response of the system over  $0 \leq n \leq 100$ .
- c) Determine the stability from this impulse response

**CODE:**

```
%A particular linear and time-invariant system is described by the
%difference equation:

% y(n) - 0.5y(n-1) + 0.25y(n-2) = x(n) + 2x(n-1) + x(n-3)

% a) Determine the stability of the system.
%Therefore: We need to use the filter function
%Let us take coefficients of both y (here a) and x (here b)

a = [1 -5/10 25/100];
b = [1 2 1];
y = 0:100;
x = filter(a,b,y);
subplot(211),plot(x,y);
title('Difference Equation of following equation');
xlabel('x');
ylabel('y');
B = isstable(x);
disp(B);
% b) Determine and plot the impulse response of the system over 0<=n<=100.
z = dirac(x);
subplot(212),stem(z,y);
title('Impulse Response of Difference Equation of following equation');
xlabel('z');
ylabel('y');
% c) Determine the stability from this impulse response
B2 = isstable(z);
disp(B2);
```

**OUTPUT:**

```
>> %A particular linear and time-invariant system is described by the
%difference equation:
```

$$y(n) - 0.5y(n-1) + 0.25y(n-2) = x(n) + 2x(n-1) + x(n-3)$$

```
% a) Determine the stability of the system.
%Therefore: We need to use the filter function
```

%Let us take coefficients of both y (here a) and x (here b)

```
a = [1 -5/10 25/100];
```

```
b = [1 2 1];
```

```
y = 0:100;
```

```
x = filter(a,b,y);
```

```
subplot(211),plot(x,y);
```

```
title('Difference Equation of following equation');
```

```
xlabel('x');
```

```
ylabel('y');
```

```
B = isstable(x);
```

```
disp(B);
```

% b) Determine and plot the impulse response of the system over  $0 \leq n \leq 100$ .

```
z = dirac(x);
```

```
subplot(212),stem(z,y);
```

```
title('Impulse Response of Difference Equation of following equation');
```

```
xlabel('z');
```

```
ylabel('y');
```

% c) Determine the stability from this impulse response

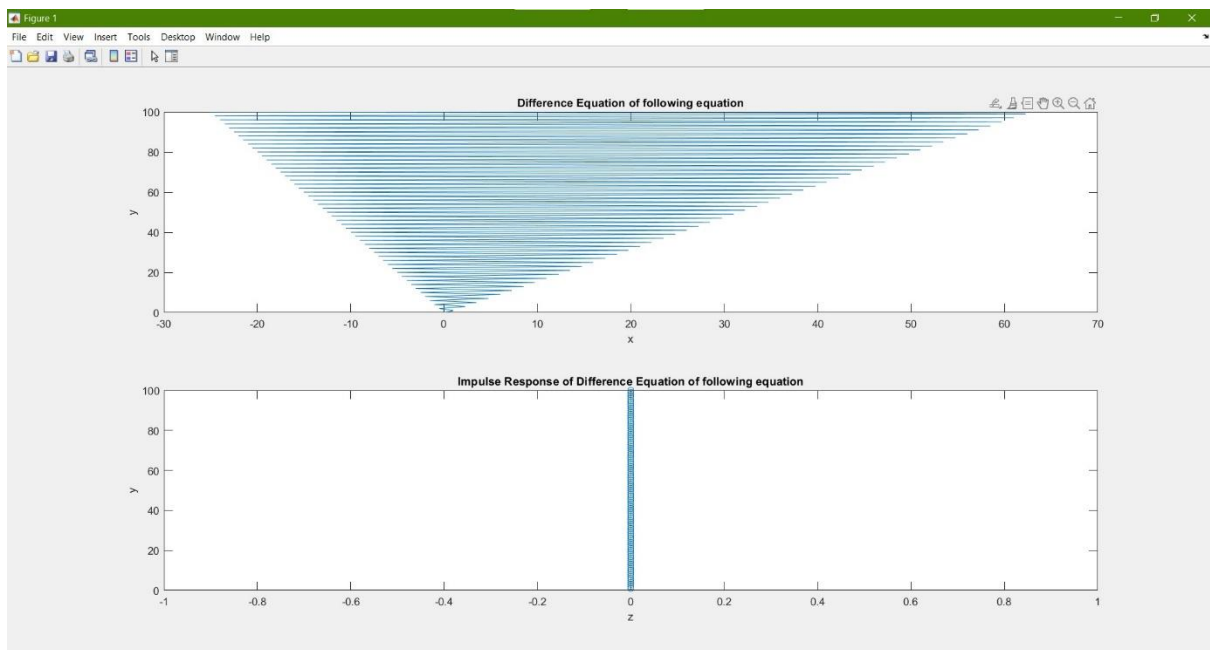
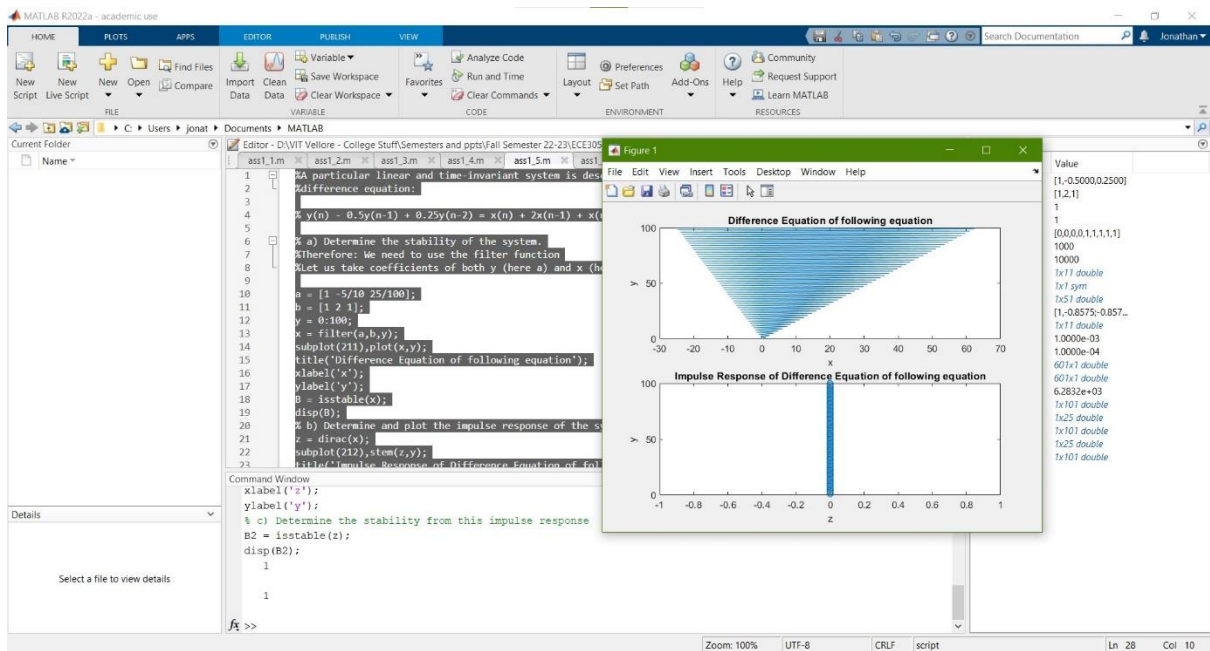
```
B2 = isstable(z);
```

```
disp(B2);
```

```
1
```

```
1
```

```
>>
```



**Q6) A simple digital differentiator is given by:**

$$y(n) = x(n) - x(n-1)$$

which computes a backward first-order difference in the input sequence. Implement this differentiator on the following sequences and plot the results. Comment on the appropriateness of this simple differentiator.

- a)  $x(n) = 5[u(n)-u(n-20)]$ : a rectangular pose
- b)  $x(n) = n[u(n) - u(n-10)] + (20-n)[u(n-10)-u(n-20)]$ : a triangular pose.
- c)  $x(n) = \sin(\pi n/25) * [u(n) - u(n-100)]$ : a sinusoidal pulse

**CODE:**

```
% A simple digital differentiator is given by:
% y(n) = x(n) - x(n-1)
% which computes a backward first-order difference in the input sequence.
% Implement this differentiator on the following sequences and plot the
% results. Comment on the appropriateness of this simple differentiator.
syms y(n);
n0 = 1:5;
% a) x(n) = 5[u(n)-u(n-20)]: a rectangular pose
syms x(n);
x(n) = 5*heaviside(n)-heaviside(n-20);
y(n) = x(n) - x(n-1);
subplot(321),stem(y(n0),n0);
title('Rectangular Pose - Stem');
xlabel('y(n)');
ylabel('n');
subplot(322),plot(y(n0),n0);
title('Rectangular Pose - Plot');
xlabel('y(n)');
ylabel('n');

% b) x(n) = n[u(n) - u(n-10)] + (20-n)[u(n-10)-u(n-20)]: a triangular pose.
x(n) = n*(heaviside(n)-heaviside(n-10)) + ((20-n)*(heaviside(n-10) - heaviside(n-20)));
y(n) = x(n) - x(n-1);
subplot(323),stem(y(n0),n0);
title('Triangular Pose - Stem');
xlabel('y(n)');
ylabel('n');
subplot(324),plot(y(n0),n0);
title('Triangular Pose - Plot');
xlabel('y(n)');
ylabel('n');

% c) x(n) = sin(pi*n/25) * [u(n) - u(n-100)]: a sinusoidal pulse
x(n) = sin((pi*n)/25) * (heaviside(n) - heaviside(n-100));
y(n) = x(n) - x(n-1);
subplot(325),stem(y(n0),n0);
title('Sinusoidal Pose - Stem');
xlabel('y(n)');
ylabel('n');
subplot(326),plot(y(n0),n0);
title('Sinusoidal Pose - Plot');
xlabel('y(n)');
```

```
ylabel('n');
```

### OUTPUT:

```
>> % A simple digital differentiator is given by:
```

```
%  $y(n) = x(n) - x(n-1)$ 
```

```
% which computes a backward first-order difference in the input sequence.
```

```
% Implement this differentiator on the following sequences and plot the
```

```
% results. Comment on the appropriateness of this simple differentiator.
```

```
syms y(n);
```

```
n0 = 1:5;
```

```
% a)  $x(n) = 5[u(n)-u(n-20)]$ : a rectangular pose
```

```
syms x(n);
```

```
 $x(n) = 5*\text{heaviside}(n)-\text{heaviside}(n-20);$ 
```

```
 $y(n) = x(n) - x(n-1);$ 
```

```
subplot(321),stem(y(n0),n0);
```

```
title('Rectangular Pose - Stem');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
subplot(322),plot(y(n0),n0);
```

```
title('Rectangular Pose - Plot');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
% b)  $x(n) = n[u(n) - u(n-10)] + (20-n)[u(n-10)-u(n-20)]$ : a triangular pose.
```

```
 $x(n) = n*(\text{heaviside}(n)-\text{heaviside}(n-10)) + ((20-n)*(\text{heaviside}(n-10) - \text{heaviside}(n-20)));$ 
```

```
 $y(n) = x(n) - x(n-1);$ 
```

```
subplot(323),stem(y(n0),n0);
```

```
title('Triangular Pose - Stem');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
subplot(324),plot(y(n0),n0);
```

```
title('Triangular Pose - Plot');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
% c)  $x(n) = \sin(\pi n/25) * [u(n) - u(n-100)]$ : a sinusoidal pulse
```

```
x(n) = sin((pi*n)/25) * (heaviside(n) - heaviside(n-100));
```

```
y(n) = x(n) - x(n-1);
```

```
subplot(325),stem(y(n0),n0);
```

```
title('Sinusoidal Pose - Stem');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
subplot(326),plot(y(n0),n0);
```

```
title('Sinusoidal Pose - Plot');
```

```
xlabel('y(n)');
```

```
ylabel('n');
```

```
>>
```

