

Strategy Design (ML Fin Data - Project 1)

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Libraries

0. Scraping the SP500

In order to test the logic within the strategy, I have fetched functions that retrieve a number of sample stocks by sector from the SP500.

```
# to obtain relative paths
library(here)

# Load code into environment
source(here("functions", "fetch_sp500_sectors.R"))
```

```
## Getting holdings for SP500
```

0.0.1 SP500 Economic Sectors

The following function fetches and extract the economic sectors from the SP500, taken from Wikipedia.

```
# fetch the sectors as a dataframe
sp500_sectors <- f_get_sp500_sectors()
head(sp500_sectors)
```

```
##   tickers      sectors
## 1   MMM      Industrials
## 2   AOS      Industrials
## 3   ABT      Health Care
## 4   ABBV     Health Care
## 5   ACN Information Technology
## 6   ATVI Communication Services
```

0.0.2 SP500 Sector Weight

```
# wrap into a single argument function
fetch_sp500_sector_data <- function(x){f_fetch_sector_data(x, sp500, sp500_sectors)}

# call the function
head(fetch_sp500_sector_data("Information Technology"))
```

```
##   ticker      sector      weight shares_held
## 1  AAPL Information Technology 0.070819853 164712193
## 2  ACN  Information Technology 0.005393819  7070903
## 3  ADBE Information Technology 0.006588889  5109299
## 4  ADI  Information Technology 0.002440011  5620612
## 5  ADSK Information Technology 0.001238980  2395718
## 6  AKAM Information Technology 0.000452252  1710719
```

0.0.3 Retrieving top sectors and stocks

Pack everything into one function to retrieve all the data

```
# Retrieve top 10 stocks by weight for each sector in the top 5 sectors from the SP500 (by weight)
sector_list <- f_retrieve_top_sp500(top_n_sectors = 6, top_n_stocks = 15, only_tickers=TRUE)
sector_list
```

```
## $Industrials
## [1] "ADP" "BA" "CAT" "CSX" "DE" "ETN" "FDX" "GE" "HON" "ITW" "LMT" "NOC"
## [13] "RTX" "UNP" "UPS"
##
## $'Health Care'
## [1] "ABBV" "ABT" "AMGN" "BMY" "DHR" "ELV" "ISRG" "JNJ" "LLY" "MDT"
## [11] "MRK" "PFE" "SYK" "TMO" "UNH"
##
## $'Information Technology'
## [1] "AAPL" "ACN" "ADBE" "AMD" "AVGO" "CRM" "CSCO" "IBM" "INTC" "INTU"
## [11] "MSFT" "NVDA" "ORCL" "QCOM" "TXN"
##
## $'Communication Services'
## [1] "ATVI" "CHTR" "CMCSA" "DIS" "EA" "GOOG" "GOOGL" "META" "NFLX"
## [10] "OMC" "T" "TMUS" "TTWO" "VZ" "WBD"
##
## $Financials
## [1] "AXP" "BAC" "BLK" "C" "CB" "GS" "JPM" "MA" "MMC" "MS"
## [11] "PGR" "SCHW" "SPGI" "V" "WFC"
##
## $'Consumer Discretionary'
## [1] "ABNB" "AMZN" "AZO" "BKNG" "CMG" "F" "GM" "HD" "MAR" "MCD"
## [11] "NKE" "ORLY" "SBUX" "TJX" "TSLA"
```

This logic is implemented under `functions/fetch_sp500_sectors.R`

0.0.4 Retrieving top sectors and stocks

```
# function to fetch all the information for one ticker into a nice xts dataframe
sp500_stocks <- lapply(sector_list,
  f_fetch_all_tickers,
  start_date="2016-01-01",
  end_date="2022-12-01")
```

```
# Show the available sectors
names(sp500_stocks)
```

```
## [1] "Industrials" "Health Care" "Information Technology"
## [4] "Communication Services" "Financials" "Consumer Discretionary"
```

```
# Show available stocks for Industrials
names(sp500_stocks$Industrials)
```

```
## [1] "ADP" "BA" "CAT" "CSX" "DE" "ETN" "FDX" "GE" "HON" "ITW" "LMT" "NOC"
## [13] "RTX" "UNP" "UPS"
```

```
# access the xts of the stocks in industrials
tail(sp500_stocks$Industrials$ADP)
```

```
##          direction_lead realized_returns actual_returns adjclose_lag1
## 2022-10-26             1      0.009733913      0.008113008  0.039930970
## 2022-11-02             1      0.012306040      0.009733913  0.008113008
## 2022-11-09             1      0.053616090      0.012306040  0.009733913
## 2022-11-16             1      0.034718700      0.053616090  0.012306040
## 2022-11-23             1      0.005923517      0.034718700  0.053616090
## 2022-11-30             NA              NA      0.005923517  0.034718700
##          adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2022-10-26 -0.064535730  0.030150980  9.676399 13.39493  100 0.6110784
## 2022-11-02  0.039930970 -0.064535730  9.885942 13.58997  100 0.6303335
## 2022-11-09  0.008113008  0.039930970  9.762661 13.77107   50 0.6307783
## 2022-11-16  0.009733913  0.008113008 10.232471 14.68326  100 0.8325740
## 2022-11-23  0.012306040  0.009733913 10.243009 15.95273  100 0.9310325
## 2022-11-30  0.053616090  0.012306040 10.247795 16.53998  100 0.8907336
##          chaikin_vol      clv      emv      macd      mfi      sar
## 2022-10-26 -1.49750300 -0.1320576 -0.01707202 2.049576 51.52422 260.0428
## 2022-11-02  2.90314600 -0.2863719  0.02711271 1.939312 49.23300 258.6055
## 2022-11-09 -0.09676625 -0.3920529  0.04765004 1.866926 49.20839 257.2257
## 2022-11-16 -0.38397100 -0.4461119  0.09074850 1.906715 48.83463 256.7200
## 2022-11-23 -0.20180520 -0.3205142  0.11758529 2.068291 49.31528 224.1100
## 2022-11-30  0.48394890 -0.1089895  0.12144667 2.300754 42.97382 224.1100
##          smi      volat month_index
## 2022-10-26  8.131402 0.2269538      82
## 2022-11-02  5.546375 0.2606250      83
## 2022-11-09  3.943960 0.2653165      83
## 2022-11-16  6.291102 0.2641173      83
## 2022-11-23 11.099826 0.2624611      83
## 2022-11-30 16.713518 0.2759187      83
```

BACKTESTING LOGIC

Adding a numeric index

First, we need to create a corresponding index for each week:

```
# count number of weeks in data from one of the dataframes
sample_xts <- sp500_stocks$Industrials$CSX
tail(sample_xts, 10)
```

```
##          direction_lead realized_returns actual_returns adjclose_lag1
## 2022-09-28             1      0.006853095     -0.053209662 -0.069267283
## 2022-10-05            -1     -0.042966082      0.006853095 -0.053209662
## 2022-10-12             1      0.046554111     -0.042966082  0.006853095
## 2022-10-19             1      0.029989991      0.046554111 -0.042966082
## 2022-10-26            -1     -0.008377096      0.029989991  0.046554111
## 2022-11-02             1      0.031058456     -0.008377096  0.029989991
## 2022-11-09             1      0.059684655      0.031058456 -0.008377096
## 2022-11-16             1      0.026221770      0.059684655  0.031058456
## 2022-11-23             1      0.022307721      0.026221770  0.059684655
## 2022-11-30             NA              NA      0.022307721  0.026221770
##          adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2022-09-28 -0.020913351  0.007554347  1.441481 16.24190 -100 0.04467755
## 2022-10-05 -0.069267283 -0.020913351  1.384232 17.10559  -50 0.13495813
## 2022-10-12 -0.053209662 -0.069267283  1.379644 18.24157  -50 0.07457368
```

```
## 2022-10-19 0.006853095 -0.053209662 1.394670 18.58490 50 0.23730603
## 2022-10-26 -0.042966082 0.006853095 1.398622 18.20787 100 0.36428555
## 2022-11-02 0.046554111 -0.042966082 1.385863 17.63796 100 0.36718737
## 2022-11-09 0.029989991 0.046554111 1.385444 17.00435 50 0.43456871
## 2022-11-16 -0.008377096 0.029989991 1.429341 16.04316 100 0.61239403
## 2022-11-23 0.031058456 -0.008377096 1.395102 15.54651 100 0.68335600
## 2022-11-30 0.059684655 0.031058456 1.369024 15.36369 100 0.70213009
## chaikin_vol clv emv macd mfi sar
## 2022-09-28 2.43234200 0.21475805 -1.787304e-04 -2.031918 46.90353 34.67000
## 2022-10-05 -0.44268680 0.22116568 -2.096124e-04 -2.290153 46.43088 34.38840
## 2022-10-12 0.43839330 0.07934922 -3.472192e-04 -2.649750 46.62430 34.11806
## 2022-10-19 -1.12835800 0.03125187 -3.458817e-04 -2.983549 54.92321 33.66998
## 2022-10-26 0.36773750 -0.10430028 -2.858648e-04 -3.232381 56.20916 33.24878
## 2022-11-02 -8.91414900 -0.26417408 -1.913069e-04 -3.420978 48.82911 32.85285
## 2022-11-09 -0.08886197 -0.35167976 -1.696224e-04 -3.505779 48.94612 32.48068
## 2022-11-16 -0.69757770 -0.28307675 -6.177828e-05 -3.415472 46.83053 32.13084
## 2022-11-23 -2.77541900 -0.16462184 6.920197e-05 -3.168499 45.87661 26.65000
## 2022-11-30 -0.65517410 0.02947430 2.043992e-04 -2.797269 55.72098 26.65000
## smi volat month_index
## 2022-09-28 -18.01681 0.2279791 81
## 2022-10-05 -22.89976 0.2353109 82
## 2022-10-12 -28.89441 0.2481376 82
## 2022-10-19 -32.89471 0.2465206 82
## 2022-10-26 -34.78229 0.2484444 82
## 2022-11-02 -36.26677 0.2806964 83
## 2022-11-09 -36.24474 0.2819226 83
## 2022-11-16 -32.84559 0.2767814 83
## 2022-11-23 -26.53377 0.2587499 83
## 2022-11-30 -18.89848 0.2672197 83
```

```
sample_xts[, c( "month_index")]
```

```
## month_index
## 2016-01-06 1
## 2016-01-13 1
## 2016-01-20 1
## 2016-01-27 1
## 2016-02-03 2
## 2016-02-10 2
## 2016-02-17 2
## 2016-02-24 2
## 2016-03-02 3
## 2016-03-09 3
## ...
## 2022-09-28 81
## 2022-10-05 82
## 2022-10-12 82
## 2022-10-19 82
## 2022-10-26 82
## 2022-11-02 83
## 2022-11-09 83
## 2022-11-16 83
## 2022-11-23 83
## 2022-11-30 83
```

BACKTESTING_PROCEDURE

1. Assume we have N_{years} years of weekly data, giving a total of N_{months} many months.
2. We want to fix a window of $N_W = 12$ months at the time (i.e. a year of data).

2. The total number of runs is given by

$$N^{runs} = \left\lfloor \frac{N_{months} - N_W}{s} \right\rfloor + 1$$

, where $s = 1$ is the number of months to move at the time (because of monthly rebalance).

i.e., we can move N^{runs} times when predicting one month at the time, starting with having all the data until month 12.

That is, $\tau = 1, \dots, 48$

```
# Set up backtesting simulation parameters
sample_xts <- sp500_stocks$Industrials$ADP
sectors <- names(sp500_stocks)
N_sector_best_stocks <- 3 # new strategy:  $3 \times 2 = 6$ 
```

```
# Formula parameters
slide <- 1
N_months <- length(names(split.xts(sample_xts, f = "months")))
N_window <- 24 # number of months in size for each window
N_runs <- floor((N_months - N_window)/slide)
```

```
# display parameters
print(paste0("N_months: ", N_months))
```

```
## [1] "N_months: 83"
```

```
print(paste0("N_runs: ", N_runs))
```

```
## [1] "N_runs: 59"
```

```
print(paste0("slide: ", slide))
```

```
## [1] "slide: 1"
```

```
# setup initial portfolio tracking variables
initial_capital <- 500000
num_tickers <- length(sectors)*N_sector_best_stocks*2 # two sub-strategies for picking
initial_tickers <- rep(NA, num_tickers)
weights <- rep(1/num_tickers, num_tickers) # initialize to 1/n
returns <- rep(NA, N_runs)
```

```
# repack the portfolio
portfolio <- list(tickers = initial_tickers,
                  weights = weights,
                  capital = initial_capital,
                  returns = returns,
                  data = NA
                )
```

portfolio

```
## $stickers
##  [1] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [26] NA NA NA NA NA NA NA NA NA NA NA NA
##
## $weights
##  [1] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
##  [7] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
```

```
## [13] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [19] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [25] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [31] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
##
## $capital
## [1] 5e+05
##
## $returns
## [1] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [26] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [51] NA NA NA NA NA NA NA NA NA NA
##
## $data
## [1] NA
```

```
# Initiate backtesting
print(paste(rep("-", 100), collapse = ""))
```

```
## [1] "-----"
```

```
print("BACKTESTING")
```

```
## [1] "BACKTESTING"
```

```
print(paste(rep("-", 100), collapse = ""))
```

```
## [1] "-----"
```

```
print("")
```

```
## [1] ""
```

```
# for every run (sliding window of time to consider)
for(tau in seq(N_runs)){
  # close any positions
  print("#####")
  print(paste0("### (tau=", tau, ") ###"))
  print("#####")
  print("CLOSE all positions")

  # Calculate and record profit-loss
  print("(1) COMPUTE_P/L(portfolio)")
  portfolio$capital <- portfolio$capital * (1 + runif(1, -0.05, 0.10))
  print(paste0("--> Capital:", portfolio$capital, "$"))

  # variables
  i_sector <- 1 # keep index counter for sectors
  num_top_pick <- N_sector_best_stocks*2 # number of stocks picked per sector

  # current portf
  cur_tickers <- rep(NA, num_tickers)

  print("")
  print("(2) PORTFOLIO_LOOP:")
  # loop through all the sectors
```

```

for(G in sectors){
  # execute sector procedure
  print(paste0("    SECTOR_PROCEDURE(G=", G, ", tau=", tau, ")"))

  # return top 3 best stocks according to procedure
  top_sector_stocks <- sample(names(sp500_stocks[[G]]), num_top_pick)

  # assign best stocks to portfolio (NEED TO UPDATE LOGIC!)
  i_replace <- rep(i_sector, num_top_pick) + seq(0, num_top_pick-1) # indexes to choose from
  cur_tickers[i_replace] <- top_sector_stocks
  i_sector <- i_sector + num_top_pick
}

# Assign tickers for this simulation
portfolio$tickers <- as.vector(cur_tickers)

# Display selected portfolio tickers
print("Cur Portfolio:")
print(portfolio$tickers)

# Optimize portfolio weights using modified min_variance
print("")
print("(3) OPTIMIZE_PORTFOLIO(portfolio)")
# simulate the optimization
portfolio$weights <- runif(length(portfolio$weights)) / sum(runif(length(portfolio$weights)))
print("weights: ")
print(paste(" ", portfolio$weights))

print("")
print("(4) LONG PORTFOLIO()")

# Separate simulation (over)
print(paste(rep("-", 100), collapse = ""))

# TEST: Just for this small printing simulation !!
if(tau > 4){
  break
}
}

```

```

## [1] "#####"
## [1] "### (tau=1) ###"
## [1] "#####"
## [1] "CLOSE all positions"
## [1] "(1) COMPUTE_P/L(portfolio)"
## [1] "--> Capital:525137.338205241$"
## [1] ""
## [1] "(2) PORTFOLIO_LOOP:"
## [1] "    SECTOR_PROCEDURE(G=Industrials, tau=1)"
## [1] "    SECTOR_PROCEDURE(G=Health Care, tau=1)"
## [1] "    SECTOR_PROCEDURE(G=Information Technology, tau=1)"
## [1] "    SECTOR_PROCEDURE(G=Communication Services, tau=1)"
## [1] "    SECTOR_PROCEDURE(G=Financials, tau=1)"
## [1] "    SECTOR_PROCEDURE(G=Consumer Discretionary, tau=1)"
## [1] "Cur Portfolio:"
## [1] "BA" "ADP" "CSX" "CAT" "DE" "GE" "BMY" "AMGN" "SYK" "MRK"
## [11] "ABT" "TMO" "IBM" "CSCO" "TXN" "AVGO" "MSFT" "ADBE" "T" "GOOG"
## [21] "META" "TMUS" "DIS" "WBD" "V" "C" "PGR" "SCHW" "MMC" "WFC"
## [31] "AMZN" "NKE" "ORLY" "AZO" "GM" "SBUX"

```

```

## [1] ""
## [1] "(3) OPTIMIZE_PORTFOLIO(portfolio)"
## [1] "weights: "
## [1] " 0.0482059920169423" " 0.0461733191894479" " 0.0415262636038605"
## [4] " 0.0469574536282151" " 0.012358626075758" " 0.0216578434150279"
## [7] " 0.043467382720153" " 0.0253376897137651" " 0.00733708566052511"
## [10] " 0.0389343842804391" " 0.0100751129346321" " 0.0459712663724311"
## [13] " 0.0477910211393527" " 0.0388396815948261" " 0.0469993794062171"
## [16] " 0.00209130988887528" " 0.00702216778882097" " 0.00443268358548388"
## [19] " 0.0360357465347816" " 0.0228416105607116" " 0.0139297546037314"
## [22] " 0.0279660517034762" " 0.0105887297817777" " 0.0286996949895388"
## [25] " 0.0115009486236665" " 0.0164309213570394" " 0.0283939817516448"
## [28] " 0.0171187079398162" " 0.00392448453569571" " 0.0110801931413277"
## [31] " 0.0293412459895565" " 0.00176509279959754" " 0.00335882395391552"
## [34] " 0.0245502925292782" " 0.00857850123456129" " 0.0205423198657427"
## [1] ""
## [1] "(4) LONG PORTFOLIO()"
## [1] "-----"
## [1] "#####"
## [1] "### (tau=2) ###"
## [1] "#####"
## [1] "CLOSE all positions"
## [1] "(1) COMPUTE_P/L(portfolio)"
## [1] "--> Capital:512720.931594704$"
## [1] ""
## [1] "(2) PORTFOLIO_LOOP:"
## [1] "  SECTOR_PROCEDURE(G=Industrials, tau=2)"
## [1] "  SECTOR_PROCEDURE(G=Health Care, tau=2)"
## [1] "  SECTOR_PROCEDURE(G=Information Technology, tau=2)"
## [1] "  SECTOR_PROCEDURE(G=Communication Services, tau=2)"
## [1] "  SECTOR_PROCEDURE(G=Financials, tau=2)"
## [1] "  SECTOR_PROCEDURE(G=Consumer Discretionary, tau=2)"
## [1] "Cur Portfolio:"
## [1] "ADP" "UNP" "UPS" "CSX" "GE" "BA" "MDT" "JNJ" "ABT" "LLY"
## [11] "SYK" "ISRG" "AVGO" "AMD" "ADBE" "TXN" "IBM" "CSCO" "ATVI" "TMUS"
## [21] "OMC" "GOOG" "EA" "DIS" "MMC" "SCHW" "C" "MS" "V" "SPGI"
## [31] "SBUX" "CMG" "GM" "ORLY" "NKE" "TSLA"
## [1] ""
## [1] "(3) OPTIMIZE_PORTFOLIO(portfolio)"
## [1] "weights: "
## [1] " 0.0016260471734588" " 0.00842404418338589" " 0.0164623256137902"
## [4] " 0.00878220877427243" " 0.00554774540474547" " 0.0292967784651774"
## [7] " 4.73613234525337e-05" " 0.0523978130284172" " 0.0278459367163855"
## [10] " 0.0378759314520065" " 0.0496941370797583" " 0.0204544144773149"
## [13] " 0.0112983730965131" " 0.0166600879590932" " 0.0397079858259344"
## [16] " 0.0509211350837449" " 0.0105207190193659" " 0.013691101358429"
## [19] " 0.0390098342318434" " 0.0167660590122796" " 0.0193323088997988"
## [22] " 0.0331063853352877" " 0.0281144269122132" " 0.00846509791755194"
## [25] " 0.0307107083258924" " 0.0239644020866693" " 0.0404591303635017"
## [28] " 0.0116585525739931" " 0.0101473210968308" " 0.0361545928306766"
## [31] " 0.00798468120879843" " 0.0336364634808896" " 0.010772433131874"
## [34] " 0.0432271237765983" " 0.0203956713236513" " 0.0511798254245493"
## [1] ""
## [1] "(4) LONG PORTFOLIO()"
## [1] "-----"
## [1] "#####"
## [1] "### (tau=3) ###"
## [1] "#####"
## [1] "CLOSE all positions"
## [1] "(1) COMPUTE_P/L(portfolio)"

```



```

## [1] "--> Capital:553145.558914472$"
## [1] ""
## [1] "(2) PORTFOLIO_LOOP:"
## [1] "    SECTOR_PROCEDURE(G=Industrials, tau=3)"
## [1] "    SECTOR_PROCEDURE(G=Health Care, tau=3)"
## [1] "    SECTOR_PROCEDURE(G=Information Technology, tau=3)"
## [1] "    SECTOR_PROCEDURE(G=Communication Services, tau=3)"
## [1] "    SECTOR_PROCEDURE(G=Financials, tau=3)"
## [1] "    SECTOR_PROCEDURE(G=Consumer Discretionary, tau=3)"
## [1] "Cur Portfolio:"
## [1] "BA"    "HON"    "LMT"    "ETN"    "RTX"    "CAT"    "LLY"    "ELV"    "SYK"
## [10] "JNJ"    "TMO"    "UNH"    "INTC"    "AAPL"    "AMD"    "ACN"    "TXN"    "INTU"
## [19] "CHTR"    "TTWO"    "META"    "GOOGL"    "GOOG"    "VZ"    "SCHW"    "GS"    "MS"
## [28] "PGR"    "BLK"    "SPGI"    "AMZN"    "TJX"    "ORLY"    "SBUX"    "F"    "ABNB"
## [1] ""
## [1] "(3) OPTIMIZE_PORTFOLIO(portfolio)"
## [1] "weights: "
## [1] " 0.0499788824675893" " 0.0306702542874202" " 0.0418700696890506"
## [4] " 0.0532634120854659" " 0.0413314392782679" " 0.0319792904409967"
## [7] " 0.0555177616764978" " 0.012570180259613" " 0.00419138190186126"
## [10] " 0.0290250986073827" " 0.0372498828221388" " 0.00334843629967522"
## [13] " 0.0315784187084417" " 0.00886582960599666" " 0.0240426815354837"
## [16] " 0.0370553981807697" " 0.0022831807564084" " 0.0401357916117935"
## [19] " 0.0236158765552396" " 0.0274155961314213" " 0.0141243217820827"
## [22] " 0.0539952415827246" " 0.0565660871518963" " 0.0309263433450456"
## [25] " 0.00411320802009358" " 0.0209354007898268" " 0.0288639334302285"
## [28] " 0.0180820219415754" " 0.0524197645953656" " 0.0427049206241226"
## [31] " 0.0463108268740697" " 0.0485636198518906" " 0.0401217293130865"
## [34] " 0.0524535454884725" " 0.0450348451454891" " 0.0234029376881964"
## [1] ""
## [1] "(4) LONG PORTFOLIO()"
## [1] "-----"
## [1] "#####"
## [1] "### (tau=4) ###"
## [1] "#####"
## [1] "CLOSE all positions"
## [1] "(1) COMPUTE_P/L(portfolio)"
## [1] "--> Capital:586359.145113085$"
## [1] ""
## [1] "(2) PORTFOLIO_LOOP:"
## [1] "    SECTOR_PROCEDURE(G=Industrials, tau=4)"
## [1] "    SECTOR_PROCEDURE(G=Health Care, tau=4)"
## [1] "    SECTOR_PROCEDURE(G=Information Technology, tau=4)"
## [1] "    SECTOR_PROCEDURE(G=Communication Services, tau=4)"
## [1] "    SECTOR_PROCEDURE(G=Financials, tau=4)"
## [1] "    SECTOR_PROCEDURE(G=Consumer Discretionary, tau=4)"
## [1] "Cur Portfolio:"
## [1] "FDX"    "GE"    "ITW"    "CAT"    "BA"    "ADP"    "JNJ"    "MRK"    "ELV"    "ABT"
## [11] "UNH"    "SYK"    "INTC"    "TXN"    "QCOM"    "ACN"    "INTU"    "AMD"    "T"    "EA"
## [21] "TTWO"    "DIS"    "GOOG"    "ATVI"    "SPGI"    "BLK"    "GS"    "SCHW"    "V"    "PGR"
## [31] "MAR"    "TJX"    "F"    "CMG"    "AMZN"    "MCD"
## [1] ""
## [1] "(3) OPTIMIZE_PORTFOLIO(portfolio)"
## [1] "weights: "
## [1] " 0.0275875062742281" " 0.00897149709102982" " 0.0359926066418334"
## [4] " 0.0335015123671435" " 0.0484515068265136" " 0.0448191027771505"
## [7] " 0.0111762899535448" " 0.0391334116029868" " 0.00851912003986717"
## [10] " 0.00416272585877248" " 0.000471743424228259" " 0.0313168325246908"
## [13] " 0.0389149749670736" " 0.0459987737814194" " 0.0111831066594336"
## [16] " 0.0140302573914645" " 0.000569752167008196" " 0.0127050881825041"

```

```

## [19] " 0.0235508110200262" " 0.0399630920255638" " 0.00617763211253737"
## [22] " 0.0406899145346077" " 0.00723830721706692" " 0.0285833027944361"
## [25] " 0.0448992956448501" " 0.0380317409520168" " 0.0322539383681085"
## [28] " 0.0194853820472622" " 3.89210910787683e-05" " 0.0199445289841706"
## [31] " 0.00609050825472995" " 0.0084725605574342" " 0.0254386153010785"
## [34] " 0.0179616494780707" " 0.0337615132106422" " 0.0371624790429045"
## [1] ""
## [1] "(4) LONG PORTFOLIO()"
## [1] "-----"
## [1] "#####"
## [1] "### (tau=5) ###"
## [1] "#####"
## [1] "CLOSE all positions"
## [1] "(1) COMPUTE_P/L(portfolio)"
## [1] "--> Capital:619651.765771017$"
## [1] ""
## [1] "(2) PORTFOLIO_LOOP:"
## [1] "    SECTOR_PROCEDURE(G=Industrials, tau=5)"
## [1] "    SECTOR_PROCEDURE(G=Health Care, tau=5)"
## [1] "    SECTOR_PROCEDURE(G=Information Technology, tau=5)"
## [1] "    SECTOR_PROCEDURE(G=Communication Services, tau=5)"
## [1] "    SECTOR_PROCEDURE(G=Financials, tau=5)"
## [1] "    SECTOR_PROCEDURE(G=Consumer Discretionary, tau=5)"
## [1] "Cur Portfolio:"
## [1] "ADP" "DE" "HON" "UPS" "UNP" "CSX" "PFE" "SYK" "MRK" "DHR"
## [11] "ELV" "BMY" "INTU" "AMD" "ADBE" "ORCL" "IBM" "ACN" "TTWO" "VZ"
## [21] "OMC" "DIS" "NFLX" "T" "BAC" "V" "WFC" "MMC" "BLK" "JPM"
## [31] "ABNB" "CMG" "MAR" "TSLA" "MCD" "HD"
## [1] ""
## [1] "(3) OPTIMIZE_PORTFOLIO(portfolio)"
## [1] "weights: "
## [1] " 0.0492659214707945" " 0.0481550826452409" " 0.0502228249191179"
## [4] " 0.00582265541047368" " 0.0292294995511896" " 0.0188025413238795"
## [7] " 0.0127900192302594" " 0.0490384336398807" " 0.0323007144313486"
## [10] " 0.00235507205380725" " 0.0100913138287059" " 0.0433362433326903"
## [13] " 0.0474742827731393" " 0.0415115643764983" " 0.0353246788380345"
## [16] " 0.0158196248970174" " 0.0287123895711805" " 0.023714306915549"
## [19] " 0.0100360114751835" " 0.0495898948393437" " 0.031932864368585"
## [22] " 0.04721157304153" " 0.0290845824395578" " 0.0348111565301207"
## [25] " 0.02757399698596" " 0.0294272914802595" " 0.0488106066024074"
## [28] " 0.00461026789952682" " 0.0181147017603152" " 0.0386119480047509"
## [31] " 0.0529118169625229" " 0.0474799443624355" " 0.032240606171986"
## [34] " 0.0374552207512913" " 0.0359835990462247" " 0.0283173372624626"
## [1] ""
## [1] "(4) LONG PORTFOLIO()"
## [1] "-----"

```

SECTOR_PROCEDURE

1. Sector G contains tickers $\{S_1, S_1, \dots, S_{|G|}\}$, where $|G|$ = number of stocks per sector (before selection).
2. For each ticker, want to calculate **current window**:

$$[t_1 = \text{week } W_{s \times \tau}, t_{12} = \text{week } W_{s \times \tau + 11}]$$

e.g. with $s = 1$ (slide one month at the time)

$$\left\{ \begin{array}{l} \tau = 1 \implies [t_1 = W_1, t_{12} = W_{12}] \\ \tau = 2 \implies [t_1 = W_2, t_{12} = W_{13}] \\ \vdots \\ \tau = i \implies [t_1 = W_i, t_{12} = W_{i+11}] \\ \vdots \\ \tau = T \implies [t_1 = W_{T-12}, t_{12} = W_T] \end{array} \right.$$

EXTRACT_STATIC_FEATURES()

We had a set of features for some stock:

```
# sample stock dataframe
sample_xts <- sp500_stocks$Industrials$ADP
head(sample_xts, 5)
```

	direction_lead	realized_returns	actual_returns	adjclose_lag1
## 2016-01-06	-1	-0.04944265	NA	NA
## 2016-01-13	1	0.01131413	-0.04944265	NA
## 2016-01-20	1	0.02848332	0.01131413	-0.04944265
## 2016-01-27	1	0.02053834	0.02848332	0.01131413
## 2016-02-03	-1	-0.01619911	0.02053834	0.02848332

```
## adjclose_lag2 adjclose_lag3 atr adx aaron bb chaikin_vol clv emv
## 2016-01-06 NA NA NA NA NA NA NA NA NA NA
## 2016-01-13 NA NA NA NA -50 NA NA NA NA NA
## 2016-01-20 NA NA NA NA -100 NA NA NA NA NA
## 2016-01-27 -0.04944265 NA NA NA 50 NA NA NA NA
## 2016-02-03 0.01131413 -0.04944265 NA NA 100 NA NA NA NA
## macd mfi sar smi volat month_index
## 2016-01-06 NA NA 79.55761 NA NA 1
## 2016-01-13 NA NA 81.71000 NA NA 1
## 2016-01-20 NA NA 81.71000 NA NA 1
## 2016-01-27 NA NA 77.34000 NA NA 1
## 2016-02-03 NA NA 77.34000 NA NA 2
```

```
# source the feature engineering file
library("here")
source(here("functions", "feature_engineering.R"))

# test out for a sample run
tau = 3 # suppose we're at run number 3
sample_xts_train_val <- f_extract_train_val_features(sample_xts, # stock xts
                                                    tau=tau, # current run
                                                    n_months = N_window, # size of window
                                                    val_lag = 1 # validation month
                                                    )

# display some columns for the extracted data
head(sample_xts_train_val$train[,c("direction_lead", "clv", "volat", "month_index")])
```

	direction_lead	clv	volat	month_index
## 2016-03-02	1	NA	NA	3
## 2016-03-09	1	0.075378023	0.2380100	3
## 2016-03-16	1	0.175116926	0.2389290	3
## 2016-03-23	1	0.162085438	0.2214060	3
## 2016-03-30	1	-0.003746352	0.1992566	3
## 2016-04-06	-1	0.156024412	0.1872713	4

```
print("")
```

```
## [1] ""
```

```
head(sample_xts_train_val$val[,c("direction_lead", "clv", "volat", "month_index")])
```

```
##           direction_lead      clv      volat month_index
## 2018-02-07             -1 -0.02045124 0.2037605          26
## 2018-02-14              1  0.14581944 0.2180265          26
## 2018-02-21             -1  0.02476083 0.2316219          26
## 2018-02-28             -1 -0.15801223 0.2332037          26
```

EXTRACT_DYNAMIC_FEATURES

```
# add GARCH features only
sample_xts_with_garch <- f_add_garch_forecast(sample_xts, volat_col="volat")
```

```
# display
tail(sample_xts_with_garch, 3)
```

```
##           direction_lead realized_returns actual_returns adjclose_lag1
## 2022-11-16              1      0.034718700      0.053616090      0.01230604
## 2022-11-23              1      0.005923517      0.034718700      0.05361609
## 2022-11-30             NA              NA      0.005923517      0.03471870
##           adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2022-11-16      0.009733913      0.008113008 10.23247 14.68326      100 0.8325740
## 2022-11-23      0.012306040      0.009733913 10.24301 15.95273      100 0.9310325
## 2022-11-30      0.053616090      0.012306040 10.24779 16.53998      100 0.8907336
##           chaikin_vol      clv      emv      macd      mfi      sar      smi
## 2022-11-16 -0.3839710 -0.4461119 0.0907485 1.906715 48.83463 256.72 6.291102
## 2022-11-23 -0.2018052 -0.3205142 0.1175853 2.068291 49.31528 224.11 11.099826
## 2022-11-30  0.4839489 -0.1089895 0.1214467 2.300754 42.97382 224.11 16.713518
##           volat month_index vol_forecast
## 2022-11-16 0.2641173          83      0.2642679
## 2022-11-23 0.2624611          83      0.2651389
## 2022-11-30 0.2759187          83      0.2659892
```

```
# Example usage
sample_xts_with_arima <- f_add_arima_forecast(sample_xts_with_garch,
                                              return_col="realized_returns")
tail(sample_xts_with_arima)
```

```
##           direction_lead realized_returns actual_returns adjclose_lag1
## 2022-10-26              1      0.009733913      0.008113008      0.039930970
## 2022-11-02              1      0.012306040      0.009733913      0.008113008
## 2022-11-09              1      0.053616090      0.012306040      0.009733913
## 2022-11-16              1      0.034718700      0.053616090      0.012306040
## 2022-11-23              1      0.005923517      0.034718700      0.053616090
## 2022-11-30             NA              NA      0.005923517      0.034718700
##           adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2022-10-26 -0.064535730      0.030150980 9.676399 13.39493      100 0.6110784
## 2022-11-02      0.039930970 -0.064535730 9.885942 13.58997      100 0.6303335
## 2022-11-09      0.008113008      0.039930970 9.762661 13.77107      50 0.6307783
## 2022-11-16      0.009733913      0.008113008 10.23247 14.68326      100 0.8325740
## 2022-11-23      0.012306040      0.009733913 10.24300 15.95273      100 0.9310325
```

```

## 2022-11-30    0.053616090    0.012306040 10.247795 16.53998    100 0.8907336
##              chaikin_vol      clv      emv      macd      mfi      sar
## 2022-10-26 -1.49750300 -0.1320576 -0.01707202 2.049576 51.52422 260.0428
## 2022-11-02  2.90314600 -0.2863719  0.02711271 1.939312 49.23300 258.6055
## 2022-11-09 -0.09676625 -0.3920529  0.04765004 1.866926 49.20839 257.2257
## 2022-11-16 -0.38397100 -0.4461119  0.09074850 1.906715 48.83463 256.7200
## 2022-11-23 -0.20180520 -0.3205142  0.11758529 2.068291 49.31528 224.1100
## 2022-11-30  0.48394890 -0.1089895  0.12144667 2.300754 42.97382 224.1100
##              smi      volat month_index vol_forecast arima_100_001
## 2022-10-26  8.131402 0.2269538      82    0.2624611  0.005473012
## 2022-11-02  5.546375 0.2606250      83    0.2759187  0.003833981
## 2022-11-09  3.943960 0.2653165      83    0.2633755  0.003715044
## 2022-11-16  6.291102 0.2641173      83    0.2642679  0.003708274
## 2022-11-23 11.099826 0.2624611      83    0.2651389  0.003707888
## 2022-11-30 16.713518 0.2759187      83    0.2659892  0.003707866
##              arima_010_001 arima_110_001 arima_020_001 arima_120_001
## 2022-10-26  0.034718700    0.04342609    0.01582131    0.05513172
## 2022-11-02  0.005923517    0.01919154   -0.02287167   -0.01640924
## 2022-11-09  0.005923517    0.01307800   -0.05166685   -0.04296142
## 2022-11-16  0.005923517    0.01589495   -0.08046203   -0.06675866
## 2022-11-23  0.005923517    0.01459698   -0.10925721   -0.09235465
## 2022-11-30  0.005923517    0.01519505   -0.13805240   -0.11677621
##              arima_100_011 arima_010_011 arima_110_011 arima_020_011
## 2022-10-26  0.005473012    0.034718700    0.04342609    0.01582131
## 2022-11-02  0.003833981    0.005923517    0.01919154   -0.02287167
## 2022-11-09  0.003715044    0.005923517    0.01307800   -0.05166685
## 2022-11-16  0.003708274    0.005923517    0.01589495   -0.08046203
## 2022-11-23  0.003707888    0.005923517    0.01459698   -0.10925721
## 2022-11-30  0.003707866    0.005923517    0.01519505   -0.13805240
##              arima_120_011
## 2022-10-26  0.05513172
## 2022-11-02  -0.01640924
## 2022-11-09  -0.04296142
## 2022-11-16  -0.06675866
## 2022-11-23  -0.09235465
## 2022-11-30  -0.11677621

```

```
sample_xts_with_arima[, c("actual_returns", "vol_forecast")]
```

```

##              actual_returns vol_forecast
## 2016-01-06              NA              NA
## 2016-01-13 -0.0494426500              NA
## 2016-01-20  0.0113141300              NA
## 2016-01-27  0.0284833200              NA
## 2016-02-03  0.0205383400              NA
## 2016-02-10 -0.0161991100    0.2380100
## 2016-02-17  0.0541783600    0.2389290
## 2016-02-24 -0.0008205272    0.2214060
## 2016-03-02  0.0045634540    0.1992566
## 2016-03-09  0.0070357570    0.1872713
##      ...
## 2022-09-28  0.0066180690    0.2269538
## 2022-10-05  0.0301509800    0.2606250
## 2022-10-12 -0.0645357300    0.2653165
## 2022-10-19  0.0399309700    0.2641173
## 2022-10-26  0.0081130080    0.2624611
## 2022-11-02  0.0097339130    0.2759187
## 2022-11-09  0.0123060400    0.2633755
## 2022-11-16  0.0536160900    0.2642679

```

```
## 2022-11-23    0.0347187000    0.2651389
## 2022-11-30    0.0059235170    0.2659892
```

Example usage

```
sample_xts_full <- f_extract_dynamic_features(sample_xts_with_garch,
                                              return_col="realized_returns")
tail(sample_xts_full)
```

```
##          direction_lead realized_returns actual_returns adjclose_lag1
## 2022-10-26             1      0.009733913      0.008113008  0.039930970
## 2022-11-02             1      0.012306040      0.009733913  0.008113008
## 2022-11-09             1      0.053616090      0.012306040  0.009733913
## 2022-11-16             1      0.034718700      0.053616090  0.012306040
## 2022-11-23             1      0.005923517      0.034718700  0.053616090
## 2022-11-30            NA              NA      0.005923517  0.034718700
##          adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2022-10-26 -0.064535730  0.030150980  9.676399 13.39493  100 0.6110784
## 2022-11-02  0.039930970 -0.064535730  9.885942 13.58997  100 0.6303335
## 2022-11-09  0.008113008  0.039930970  9.762661 13.77107   50 0.6307783
## 2022-11-16  0.009733913  0.008113008 10.232471 14.68326  100 0.8325740
## 2022-11-23  0.012306040  0.009733913 10.243009 15.95273  100 0.9310325
## 2022-11-30  0.053616090  0.012306040 10.247795 16.53998  100 0.8907336
##          chaikin_vol      clv      emv      macd      mfi      sar
## 2022-10-26 -1.49750300 -0.1320576 -0.01707202 2.049576 51.52422 260.0428
## 2022-11-02  2.90314600 -0.2863719  0.02711271 1.939312 49.23300 258.6055
## 2022-11-09 -0.09676625 -0.3920529  0.04765004 1.866926 49.20839 257.2257
## 2022-11-16 -0.38397100 -0.4461119  0.09074850 1.906715 48.83463 256.7200
## 2022-11-23 -0.20180520 -0.3205142  0.11758529 2.068291 49.31528 224.1100
## 2022-11-30  0.48394890 -0.1089895  0.12144667 2.300754 42.97382 224.1100
##          smi      volat month_index vol_forecast arima_100_001
## 2022-10-26  8.131402 0.2269538      82  0.2624611  0.005473012
## 2022-11-02  5.546375 0.2606250      83  0.2759187  0.003833981
## 2022-11-09  3.943960 0.2653165      83  0.2633755  0.003715044
## 2022-11-16  6.291102 0.2641173      83  0.2642679  0.003708274
## 2022-11-23 11.099826 0.2624611      83  0.2651389  0.003707888
## 2022-11-30 16.713518 0.2759187      83  0.2659892  0.003707866
##          arima_010_001 arima_110_001 arima_020_001 arima_120_001
## 2022-10-26  0.034718700  0.04342609  0.01582131  0.05513172
## 2022-11-02  0.005923517  0.01919154 -0.02287167 -0.01640924
## 2022-11-09  0.005923517  0.01307800 -0.05166685 -0.04296142
## 2022-11-16  0.005923517  0.01589495 -0.08046203 -0.06675866
## 2022-11-23  0.005923517  0.01459698 -0.10925721 -0.09235465
## 2022-11-30  0.005923517  0.01519505 -0.13805240 -0.11677621
##          arima_100_011 arima_010_011 arima_110_011 arima_020_011
## 2022-10-26  0.005473012  0.034718700  0.04342609  0.01582131
## 2022-11-02  0.003833981  0.005923517  0.01919154 -0.02287167
## 2022-11-09  0.003715044  0.005923517  0.01307800 -0.05166685
## 2022-11-16  0.003708274  0.005923517  0.01589495 -0.08046203
## 2022-11-23  0.003707888  0.005923517  0.01459698 -0.10925721
## 2022-11-30  0.003707866  0.005923517  0.01519505 -0.13805240
##          arima_120_011
## 2022-10-26  0.05513172
## 2022-11-02 -0.01640924
## 2022-11-09 -0.04296142
## 2022-11-16 -0.06675866
## 2022-11-23 -0.09235465
## 2022-11-30 -0.11677621
```

SECTOR PROCEDURE

```

SECTOR_PROCEDURE <- function(G, tau){
  ##
  ## Params:
  ## - G (str): Economic sector name; will be used to fetch the List of lists
  ## which are the pre-selected stocks for that sector.
  ## - tau (numeric): Integer that corresponds to the actual run of the backtest.
  ##

  ### TEST ###
  # NOTE: For testing only, will be removed later!
  num_top_pick <- N_sector_best_stocks*2 # number of stocks picked per sector
  ### TEST ###

  print(paste0("SECTOR_PROCEDURE(G=", G, ", tau=", tau, ")"))

  # retrieve sector data
  sector_data <- sp500_stocks[[G]]

  # stocks for sector provided
  sector_tickers <- names(sector_data)

  # to store subset features for window
  sector_stocks_window <- rep(NA, length(sector_tickers))
  names(sector_stocks_window) <- sector_tickers

  # extract static train-val for all stocks
  list_train_val_sector <- lapply(sector_data,
                                f_extract_train_val_features,
                                tau=tau, # current run
                                n_months = 12, # size of window
                                val_lag = 1 # months to use in val set
                                )

  # return top 3 best stocks according to modelling procedure
  print(" MODELLING_PROCEDURE(list_train_val_sector)")
  top_sector_stocks <- sample(names(sp500_stocks[[G]]), num_top_pick)

  ##### Inside MODELLING_PROCEDURE #####
  ## NOTE: The MODELLING_PROCEDURE internally will use the train and

  # Stack the train and val splitted data for all stocks in sector
  sector_stocks <- lapply(list_train_val_sector, function(stock) {
    # Concatenate 'train' and 'val' xts objects within each stock
    concatenated_xts <- rbind(stock$train, stock$val)
    return(concatenated_xts)
  })

  # NOTE: MODELLING_PROCEDURE should also compute dynamic features for concatenated data
  sector_stocks <- lapply(sector_stocks, f_extract_dynamic_features)

  # should return the train-val list for the chosen stocks
  chosen_stocks <- sector_stocks[names(sector_stocks) %in% top_sector_stocks]

  ##### Inside MODELLING_PROCEDURE #####

  return(chosen_stocks) # not actual return value!

```

```

}

# perform the sector procedure
G = names(sp500_stocks)[[1]]
tau = 5
sector_stocks_window <- SECTOR_PROCEDURE(G, tau)

## [1] "SECTOR_PROCEDURE(G=Industrials, tau=5)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"

names(sector_stocks_window) # names are tickers, values are list of train-val xts

## [1] "ADP" "DE" "ETN" "ITW" "LMT" "UPS"

head(sector_stocks_window[[2]]) # show ticker xts

##           direction_lead realized_returns actual_returns adjclose_lag1
## 2016-05-04             1      0.02071379      -0.03032161  0.005325853
## 2016-05-11            -1      -0.01561578       0.02071379 -0.030321608
## 2016-05-18            -1      -0.02587708      -0.01561578  0.020713791
## 2016-05-25             1      0.02865776      -0.02587708 -0.015615779
## 2016-06-01             1      0.05118445      0.02865776 -0.025877079
## 2016-06-08            -1      -0.02732549      0.05118445  0.028657761
##           adjclose_lag2 adjclose_lag3      atr adx aaron      bb chaikin_vol
## 2016-05-04  0.071318624  0.027391959 3.216998 NA  50      NA      NA
## 2016-05-11  0.005325853  0.071318624 3.185069 NA -50      NA      NA
## 2016-05-18 -0.030321608  0.005325853 3.098993 NA  50  0.7162007      NA
## 2016-05-25  0.020713791 -0.030321608 3.066922 NA -100 0.5630780  0.0516258
## 2016-06-01 -0.015615779  0.020713791 3.027857 NA -50 0.6751524 -0.2165642
## 2016-06-08 -0.025877079 -0.015615779 3.195152 NA 100 0.9914412 -0.5258239
##           clv      emv macd      mfi      sar smi      volat
## 2016-05-04 0.13622365 1.360177e-03 NA 71.10988 78.19043 NA 0.2203978
## 2016-05-11 0.09544153 3.719926e-05 NA 71.69679 78.89539 NA 0.2245193
## 2016-05-18 0.10406222 8.688395e-04 NA 65.72483 79.52985 NA 0.2164100
## 2016-05-25 0.11446762 -1.852668e-04 NA 56.91212 80.10086 NA 0.2142833
## 2016-06-01 0.23604308 1.481416e-03 NA 63.47143 80.49000 NA 0.2181418
## 2016-06-08 0.16656899 6.728191e-03 NA 64.56882 80.96500 NA 0.2259061
##           month_index arima_100_001 arima_010_001 arima_110_001 arima_020_001
## 2016-05-04           5  0.001564469  0.02865776 -0.003290775  0.083192600
## 2016-05-11           5 -0.003171989  0.05118445  0.037987478  0.073711137
## 2016-05-18           5  0.013335500 -0.02732549  0.018668549 -0.105835435
## 2016-05-25           5  0.009857793 -0.01078545 -0.020475222  0.005754593
## 2016-06-01           6  0.012145133 -0.02166408 -0.015290976 -0.032542717
## 2016-06-08           6  0.012919387 -0.02534645 -0.023189185 -0.029028825
##           arima_120_001 arima_100_011 arima_010_011 arima_110_011
## 2016-05-04  0.03603088  0.001564469  0.02865776 -0.003290775
## 2016-05-11  0.09700819 -0.003171989  0.05118445  0.037987478
## 2016-05-18 -0.03229616  0.013335500 -0.02732549  0.018668549
## 2016-05-25 -0.06342732  0.009857793 -0.01078545 -0.020475222
## 2016-06-01 -0.01258610  0.012145133 -0.02166408 -0.015290976
## 2016-06-08 -0.03426661  0.012919387 -0.02534645 -0.023189185
##           arima_020_011 arima_120_011 vol_forecast
## 2016-05-04  0.083192600  0.03603088  0.2181418
## 2016-05-11  0.073711137  0.09700819  0.2259061
## 2016-05-18 -0.105835435 -0.03229616  0.2217548
## 2016-05-25  0.005754593 -0.06342732  0.2113276
## 2016-06-01 -0.032542717 -0.01258610  0.1902579
## 2016-06-08 -0.029028825 -0.03426661  0.1858925

```


MODELLING_PROCEDURE

```

# parameters
G <- names(sp500_stocks)[1] # sample sector
tau <- 1 # suppose we are in run 5 of the backtest

##### Inside SECTOR_PROCEDURE #####

# retrieve sector data
sector_data <- sp500_stocks[[G]]

# stocks for sector provided
sector_tickers <- names(sector_data)

# to store subset features for window
sector_stocks_window <- rep(NA, length(sector_tickers))
names(sector_stocks_window) <- sector_tickers

# extract static train-val for all stocks
list_train_val_sector <- lapply(sector_data,
                                f_extract_train_val_features,
                                tau=tau, # current run
                                n_months = N_window, # size of window
                                val_lag = 1 # months to use in val set
                                )

##### Inside SECTOR_PROCEDURE #####

# keys are stock tickers for that sector
names(list_train_val_sector)

## [1] "ADP" "BA" "CAT" "CSX" "DE" "ETN" "FDX" "GE" "HON" "ITW" "LMT" "NOC"
## [13] "RTX" "UNP" "UPS"

# each stock has train and test
names(list_train_val_sector[[1]])

## [1] "train" "val"

# Check some of train and val data for one stock
head(list_train_val_sector[[1]]$train, 3)

##           direction_lead realized_returns actual_returns adjclose_lag1
## 2016-01-06             -1      -0.04944265              NA              NA
## 2016-01-13              1       0.01131413      -0.04944265              NA
## 2016-01-20              1       0.02848332       0.01131413     -0.04944265
##           adjclose_lag2 adjclose_lag3 atr adx aaron bb chaikin_vol clv emv
## 2016-01-06           NA           NA NA NA NA NA NA           NA NA NA
## 2016-01-13           NA           NA NA NA NA -50 NA           NA NA NA
## 2016-01-20           NA           NA NA NA NA -100 NA           NA NA NA
##           macd mfi           sar smi volat month_index
## 2016-01-06    NA  NA 79.55761 NA    NA           1
## 2016-01-13    NA  NA 81.71000 NA    NA           1
## 2016-01-20    NA  NA 81.71000 NA    NA           1

```

```
print("")
```

```
## [1] ""
```

```
tail(list_train_val_sector[[1]]$val, 3)
```

```
##          direction_lead realized_returns actual_returns adjclose_lag1
## 2017-12-13             1      7.152516e-03      0.014894270      0.022596070
## 2017-12-20            -1     -5.103599e-03      0.007152516      0.014894270
## 2017-12-27            -1     -8.541914e-05     -0.005103599      0.007152516
##          adjclose_lag2 adjclose_lag3      atr      adx aaron      bb
## 2017-12-13      0.02791647 -0.004074823  2.772381 18.58305    100 0.8875978
## 2017-12-20      0.02259607  0.027916470  2.709354 19.53785    100 0.9247934
## 2017-12-27      0.01489427  0.022596070  2.583686 20.14515     50 0.8325108
##          chaikin_vol      clv      emv      macd      mfi      sar
## 2017-12-13 -1.58453000 -0.1773531  0.003475763  2.612841 59.76057 110.2100
## 2017-12-20  1.99874900 -0.2788403  0.004734173  2.662641 64.80303 110.5068
## 2017-12-27 -0.07351845 -0.2669577  0.001732219  2.709642 68.29887 111.0110
##          smi      volat month_index
## 2017-12-13 35.44917 0.1594832      24
## 2017-12-20 38.35108 0.1537416      24
## 2017-12-27 40.23123 0.1529238      24
```

```
print("")
```

```
## [1] ""
```

```
nrow(list_train_val_sector[[1]]$train)
```

```
## [1] 100
```

```
nrow(list_train_val_sector[[1]]$val)
```

```
## [1] 4
```

We have 46 observations (weeks) for train, and 4 (weeks) for val.

```
print(head(list_train_val_sector[[1]]$train$month_index, 1)) # beginning month of window
```

```
##          month_index
## 2016-01-06          1
```

```
print(tail(list_train_val_sector[[1]]$val$month_index, 1)) # end month of window
```

```
##          month_index
## 2017-12-27          24
```

```
length(seq(5, 16)) # 12 months
```

```
## [1] 12
```

Feature Selection

Only on the `train_set`.

```
# Load the package
source(here("functions", "feature_engineering.R"))

# Define the formula for regression
fmla <- realized_returns ~ . -realized_returns -month_index

# try obtaining best features for a sample train set for a stock in the sample sector
best_feat_list <- f_select_features(
  fmla = fmla, # formula for regression
  data = list_train_val_sector[[1]]$train, # train data for one stock of current sector
  target_var = "realized_returns", # y
  nvmax = 50,
  method="forward")
```

```
## Loading required package: leaps
```

```
best_feat_list
```

```
## $featnames
## [1] "direction_lead" "actual_returns" "adjclose_lag2" "adjclose_lag3"
## [5] "atr"           "adx"           "aaron"        "clv"
## [9] "macd"          "mfi"           "smi"          "volat"
##
## $fmla
## realized_returns ~ direction_lead + actual_returns + adjclose_lag2 +
##   adjclose_lag3 + atr + adx + aaron + clv + macd + mfi + smi +
##   volat
## <environment: 0x000001701aaa5aa8>
```

Regularized MLR (Elasticnet)

$$\mathcal{L}(\beta) = \frac{1}{2} \sum_{i=1}^n (y_i - x_i^T \beta)^2 + \lambda [\alpha \|\beta\|_1 + (1 - \alpha) \|\beta\|_2^2]$$

```
### Perform feature selection on the train set for every stock
```

```
# load required libraries
library("caret")
```

```
## Loading required package: lattice
```

```
##
## Attaching package: 'caret'
```

```
## The following object is masked from 'package:purrr':
##
## lift
```

```
library("Metrics")
```

```
##
## Attaching package: 'Metrics'
```

```
## The following objects are masked from 'package:caret':
##
## precision, recall
```

```

## The following object is masked from 'package:forecast':
##
##      accuracy

# Define the formula for regression
fmla <- realized_returns ~ . -realized_returns -month_index

# Create a grid for elastic net regression hyperparameters
grid_enet <- expand.grid(alpha = seq(from = 0, to = 1, by = 0.1), # Elastic net mixing parameter
                        lambda = seq(from = 0, to = 0.05, by = 0.001)) # Regularization strength

# Initialize variable to save forecasted returns, MSEs and Sharpe Ratios
sector_tracker <- as.list(rep(NA, length(sector_tickers)))
names(sector_tracker) <- sector_tickers

# transform into a list of lists
sector_tracker <- lapply(sector_tracker, function(x) list(
  forecasted_ret = NA,
  sharpe = NA,
  rmse = NA,
  data = NA
))

# display values
fmla # all initial variables

## realized_returns ~ . - realized_returns - month_index

names(sector_tracker) # list of lists

## [1] "ADP" "BA" "CAT" "CSX" "DE" "ETN" "FDX" "GE" "HON" "ITW" "LMT" "NOC"
## [13] "RTX" "UNP" "UPS"

names(sector_tracker[[1]]) # to store the values as the loop happens

## [1] "forecasted_ret" "sharpe" "rmse" "data"

# Loop for every stock ticker in sector G
for(ticker in sector_tickers){
  print(paste0("ticker: ", ticker))

  # fetch data for that ticker
  ticker_data_train <- list_train_val_sector[[ticker]]$train
  ticker_data_val <- list_train_val_sector[[ticker]]$val

  # remove nas
  ticker_data_train <- na.omit(ticker_data_train) # data cannot contain nas
  ticker_data_val <- na.omit(ticker_data_val) # data cannot contain nas

  ### Step 1: Feature Selection

  # Perform feature selection for that stock
  best_feat_list <- f_select_features(
    fmla = fmla, # formula for regression
    data = ticker_data_train, # train data for one stock of current sector
    target_var = "realized_returns", # y
    nvmax = 50,
    method="forward")

```

```

print(c(best_feat_list$fmla))

### Step 2: Elasticnet

# Set up time-slice cross-validation parameters
ctr_train <- trainControl(method = "timeslice",
                           initialWindow = 52, # Consecutive number of weeks ~= 6 months
                           horizon = 4,       # Horizon is one month prediction (4 weeks)
                           skip = 1,          # No skip, our data will overlap in practice
                           fixedWindow = TRUE, # Use a fixed window
                           allowParallel = TRUE) # Enable parallel processing

# Stack together train and val, since enet will cross-validate inside
full_train <- rbind.xts(ticker_data_train, ticker_data_val)

# Train the elastic net regression model using time-slice cross-validation
model_enet_best <- train(form = best_feat_list$fmla,           # Formula from feature selection
                         data = ticker_data_train,            # Training data
                         method = "glmnet",                  # Model method
                         tuneGrid = grid_enet,                # Hyperparameter grid
                         trControl = ctr_train,                # Cross-validation control
                         preProc = c("center", "scale"),       # Preprocessing steps
                         metric = "Rsquared",                  # Metric for selecting the best model
                         threshold = 0.2)

# Extract the best alpha and beta fitted
best_alpha <- model_enet_best$bestTune$alpha
best_lambda <- model_enet_best$bestTune$lambda

# Use the best-fitted elastic net regression model to make predictions on the val_data
pred_enet_best <- predict(model_enet_best, ticker_data_val) # predict on val
pred_enet_best <- mean(pred_enet_best) # take the average
sector_tracker[[ticker]]$forecasted_ret <- pred_enet_best # save in tracker

# Compute the RMSE on the validation set
enet_rmse <- sqrt(mse(actual = ticker_data_val[, "realized_returns"], predicted = pred_enet_best))

print("")
print(paste("predicted return: ", pred_enet_best))
print(paste("rmse: ", enet_rmse))

print("#####")
}

```

```

## [1] "ticker: ADP"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag2 +
##   adjclose_lag3 + atr + adx + aaron + clv + macd + mfi + smi +
##   volat
## <environment: 0x0000017023a6f230>
##
## [1] ""
## [1] "predicted return: 0.00425287070597015"
## [1] "rmse: 0.00755002658790937"
## [1] "#####"
## [1] "ticker: BA"
## [[1]]
## realized_returns ~ direction_lead + clv + mfi + volat

```

```

## <environment: 0x000001702350fb30>
##
## [1] ""
## [1] "predicted return: 0.0115106564731343"
## [1] "rmse: 0.0210409061533028"
## [1] "#####"
## [1] "ticker: CAT"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag2 + adx + bb +
## chaikin_vol + clv + mfi + sar
## <environment: 0x0000017020162bd0>
##
## [1] ""
## [1] "predicted return: 0.00838633425820895"
## [1] "rmse: 0.0289348992716546"
## [1] "#####"
## [1] "ticker: CSX"
## [[1]]
## realized_returns ~ direction_lead + adx + emv + macd + mfi +
## sar + smi + volat
## <environment: 0x000001701e910d70>
##
## [1] ""
## [1] "predicted return: 0.0103945755477612"
## [1] "rmse: 0.0317795409205346"
## [1] "#####"
## [1] "ticker: DE"
## [[1]]
## realized_returns ~ direction_lead + atr + adx + clv + emv + sar +
## volat
## <environment: 0x0000017017a3dfd0>
##
## [1] ""
## [1] "predicted return: 0.0339572252678987"
## [1] "rmse: 0.0195886327607426"
## [1] "#####"
## [1] "ticker: ETN"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag2 + adx + aaron +
## bb + emv + macd + sar + volat
## <environment: 0x000001701c949050>
##
## [1] ""
## [1] "predicted return: -0.000654111942170204"
## [1] "rmse: 0.0295652977845325"
## [1] "#####"
## [1] "ticker: FDX"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag2 +
## adjclose_lag3 + adx + aaron + chaikin_vol + clv + sar
## <environment: 0x0000017020a8a590>
##
## [1] ""
## [1] "predicted return: 0.00537071614077343"
## [1] "rmse: 0.0266614966303764"
## [1] "#####"
## [1] "ticker: GE"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag1 +
## adx + bb + clv + macd + mfi + sar + smi + volat

```

```

## <environment: 0x0000017024222898>
##
## [1] ""
## [1] "predicted return: -0.0178832912566443"
## [1] "rmse: 0.0344007333458254"
## [1] "#####"
## [1] "ticker: HON"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag1 +
## aaron + bb + clv + emv + macd + sar + smi
## <environment: 0x000001701f16b660>
##
## [1] ""
## [1] "predicted return: 0.00450564574119403"
## [1] "rmse: 0.0123824899060627"
## [1] "#####"
## [1] "ticker: ITW"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag1 + adjclose_lag2 +
## atr + aaron + bb + macd + mfi + volat
## <environment: 0x000001701cbc1b08>
##
## [1] ""
## [1] "predicted return: -0.0156324603227544"
## [1] "rmse: 0.0233067096088579"
## [1] "#####"
## [1] "ticker: LMT"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag2 + chaikin_vol +
## emv + macd + smi
## <environment: 0x0000017020f3e450>
##
## [1] ""
## [1] "predicted return: 0.012815531059591"
## [1] "rmse: 0.00880642120449787"
## [1] "#####"
## [1] "ticker: NOC"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag1 +
## adx + aaron + chaikin_vol + clv + emv + macd + smi + volat
## <environment: 0x0000017023ee5b48>
##
## [1] ""
## [1] "predicted return: -0.00108130361658448"
## [1] "rmse: 0.0143875548124027"
## [1] "#####"
## [1] "ticker: RTX"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag3 + atr + adx +
## chaikin_vol + clv + emv + mfi + sar + smi + volat
## <environment: 0x000001701dc504b0>
##
## [1] ""
## [1] "predicted return: 0.00293808272643091"
## [1] "rmse: 0.0166283725417561"
## [1] "#####"
## [1] "ticker: UNP"
## [[1]]
## realized_returns ~ direction_lead + actual_returns + adjclose_lag1 +
## adjclose_lag2 + adjclose_lag3 + bb + clv + emv + macd + mfi +

```

```
##      volat
## <environment: 0x0000017022f26f98>
##
## [1] ""
## [1] "predicted return:  0.00503150334577797"
## [1] "rmse:  0.0159573164698068"
## [1] "#####"
## [1] "ticker: UPS"
## [[1]]
## realized_returns ~ direction_lead + adjclose_lag3 + atr + adx +
##      bb + clv + emv + macd
## <environment: 0x000001701c8730c0>
##
## [1] ""
## [1] "predicted return:  0.00864228673982985"
## [1] "rmse:  0.0262707919714151"
## [1] "#####"
```

Aside: Format for Portfolio Optimization

```
## This chunk of code simply obtains some portfolio stock tickers
## in a way that will be similar to the final result
```

```
# repack the portfolio (repeated from before)
portfolio <- list(tickers = initial_tickers,
                 weights = weights,
                 capital = initial_capital,
                 returns = returns,
                 data = NA
                )
portfolio
```

```
## $tickers
## [1] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [26] NA NA NA NA NA NA NA NA NA NA NA NA
##
## $weights
## [1] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [7] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [13] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [19] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [25] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
## [31] 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778 0.02777778
##
## $capital
## [1] 5e+05
##
## $returns
## [1] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [26] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [51] NA NA NA NA NA NA NA NA NA NA
##
## $data
## [1] NA
```

The following simulates best tickers that would be obtained after modelling procedure for all sectors


```

# Set up backtesting simulation parameters
sample_xts <- sp500_stocks$Industrials$ADP
sectors <- names(sp500_stocks)
N_sector_best_stocks <- 3
tau <- 3

# store ticker for current portfolio
cur_tickers <- rep(NA, num_tickers)

# store actual data for each run
portf_stocks_data <- as.list(rep(NA, length(sectors)))
names(portf_stocks_data) <- sectors

# keep index counter for sectors
i_sector <- 1

print("")

## [1] ""

print("(2) PORTFOLIO_LOOP:")

## [1] "(2) PORTFOLIO_LOOP:"

# loop through all the sectors
for(G in sectors){

  # return top 3 best stocks (xts data) according to procedure
  top_sector_stocks <- SECTOR_PROCEDURE(G, tau)

  # assign best stocks to portfolio (NEED TO UPDATE LOGIC!)
  i_replace <- rep(i_sector, num_top_pick) + seq(0, num_top_pick-1) # indexes to choose from
  cur_tickers[i_replace] <- names(top_sector_stocks)
  i_sector <- i_sector + num_top_pick

  # assign the data to the portfolio
  portf_stocks_data[[G]] <- top_sector_stocks
}

## [1] "SECTOR_PROCEDURE(G=Industrials, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"
## [1] "SECTOR_PROCEDURE(G=Health Care, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"
## [1] "SECTOR_PROCEDURE(G=Information Technology, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"
## [1] "SECTOR_PROCEDURE(G=Communication Services, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"
## [1] "SECTOR_PROCEDURE(G=Financials, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"
## [1] "SECTOR_PROCEDURE(G=Consumer Discretionary, tau=3)"
## [1] "  MODELLING_PROCEDURE(list_train_val_sector)"

# Portfolio tickers get updated
portfolio$tickers <- cur_tickers

```

```
# unlist data best stocks data format into a singles list
portf_data <- f_unlist_portf_data(portf_stocks_data)

# assign list to portfolio
portfolio$data <- portf_data
```

Data format for portfolio optimization

Note that at this point, the portfolio will have the tickers and the weights attributes.

```
# Checko out the resulting portfolio
portfolio$tickers
```

```
## [1] "ADP" "BA" "ETN" "FDX" "GE" "UNP" "ELV" "ISRG" "JNJ" "LLY"
## [11] "PFE" "UNH" "AVGO" "CSCO" "INTU" "MSFT" "QCOM" "TXN" "EA" "GOOG"
## [21] "NFLX" "TTWO" "VZ" "WBD" "GS" "JPM" "MMC" "MS" "PGR" "V"
## [31] "AMZN" "GM" "HD" "MAR" "ORLY" "TJX"
```

```
portfolio$capital
```

```
## [1] 5e+05
```

```
portfolio$returns
```

```
## [1] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [26] NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA NA
## [51] NA NA NA NA NA NA NA NA NA
```

```
print("")
```

```
## [1] ""
```

```
# inspect the names and data for one stock
names(portfolio$data)
```

```
## [1] "ADP" "BA" "ETN" "FDX" "GE" "UNP" "ELV" "ISRG" "JNJ" "LLY"
## [11] "PFE" "UNH" "AVGO" "CSCO" "INTU" "MSFT" "QCOM" "TXN" "EA" "GOOG"
## [21] "NFLX" "TTWO" "VZ" "WBD" "GS" "JPM" "MMC" "MS" "PGR" "V"
## [31] "AMZN" "GM" "HD" "MAR" "ORLY" "TJX"
```

```
head(portfolio$data[[1]])
```

```
##           direction_lead realized_returns actual_returns adjclose_lag1
## 2016-03-02              1      0.007035757      0.004563454 -0.0008205272
## 2016-03-09              1      0.022379780      0.007035757  0.0045634540
## 2016-03-16              1      0.009875713      0.022379780  0.0070357570
## 2016-03-23              1      0.006978770      0.009875713  0.0223797800
## 2016-03-30              1      0.018779390      0.006978770  0.0098757130
## 2016-04-06             -1     -0.006627075      0.018779390  0.0069787700
##           adjclose_lag2 adjclose_lag3 atr adx aaron bb chaikin_vol
## 2016-03-02  0.0541783600 -0.0161991100 NA  NA    50 NA           NA
## 2016-03-09 -0.0008205272  0.0541783600 NA  NA    50 NA           NA
## 2016-03-16  0.0045634540 -0.0008205272 NA  NA   100 NA           NA
## 2016-03-23  0.0070357570  0.0045634540 NA  NA   100 NA           NA
```

```

## 2016-03-30 0.0223797800 0.0070357570 NA NA 100 NA NA
## 2016-04-06 0.0098757130 0.0223797800 NA NA 100 NA NA
##
##          clv          emv macd mfi          sar smi          volat month_index
## 2016-03-02          NA          NA  NA  NA 78.83754  NA          NA          3
## 2016-03-09 0.075378023 0.002275049  NA  NA 79.59079  NA 0.2380100          3
## 2016-03-16 0.175116926 0.009077995  NA  NA 80.26871  NA 0.2389290          3
## 2016-03-23 0.162085438 0.010112252  NA  NA 81.18206  NA 0.2214060          3
## 2016-03-30 -0.003746352 0.006978234  NA  NA 82.24717  NA 0.1992566          3
## 2016-04-06 0.156024412 0.006624761  NA  NA 83.45243  NA 0.1872713          4
##
##          arima_100_001 arima_010_001 arima_110_001 arima_020_001
## 2016-03-02 0.004316747 0.006978770 0.0086298106 0.004081827
## 2016-03-09 0.004203734 0.018779390 0.0120539202 0.030580010
## 2016-03-16 0.004447047 -0.006627075 0.0078527076 -0.032033540
## 2016-03-23 0.004396324 -0.001330622 -0.0043492036 0.003965831
## 2016-03-30 0.004383581 0.000000000 -0.0007583549 0.001330622
## 2016-04-06 0.004569211 -0.019383310 -0.0083362747 -0.038766620
##
##          arima_120_001 arima_100_011 arima_010_011 arima_110_011
## 2016-03-02 -0.002876931 0.004316747 0.006978770 0.0086298106
## 2016-03-09 0.019934078 0.004203734 0.018779390 0.0120539202
## 2016-03-16 -0.005083216 0.004447047 -0.006627075 0.0078527076
## 2016-03-23 -0.018273310 0.004396324 -0.001330622 -0.0043492036
## 2016-03-30 0.004203205 0.004383581 0.000000000 -0.0007583549
## 2016-04-06 -0.023762833 0.004569211 -0.019383310 -0.0083362747
##
##          arima_020_011 arima_120_011 vol_forecast
## 2016-03-02 0.004081827 -0.002876931 0.1992566
## 2016-03-09 0.030580010 0.019934078 0.1872713
## 2016-03-16 -0.032033540 -0.005083216 0.1614380
## 2016-03-23 0.003965831 -0.018273310 0.1423489
## 2016-03-30 0.001330622 0.004203205 0.1369465
## 2016-04-06 -0.038766620 -0.023762833 0.1102818

```