

# RNNs and LSTMs

*Time will explain.*  
Jane Austen, *Persuasion*

Language is an inherently temporal phenomenon. Spoken language is a sequence of acoustic events over time, and we comprehend and produce both spoken and written language as a continuous input stream. The temporal nature of language is reflected in the metaphors we use; we talk of the *flow of conversations*, *news feeds*, and *twitter streams*, all of which emphasize that language is a sequence that unfolds in time.

This temporal nature is reflected in some language processing algorithms. For example, the Viterbi algorithm we introduced for HMM part-of-speech tagging proceeds through the input a word at a time, carrying forward information gleaned along the way. Yet other machine learning approaches, like those we've studied for sentiment analysis or other text classification tasks don't have this temporal nature – they assume simultaneous access to all aspects of their input.

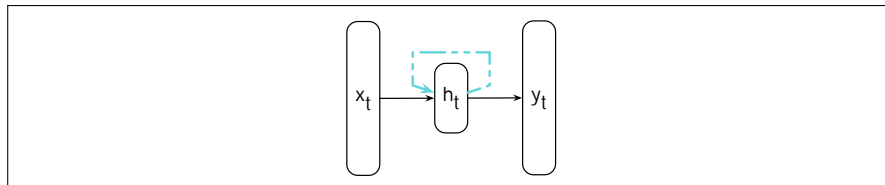
The feedforward networks of Chapter 7 also assumed simultaneous access, although they also had a simple model for time. Recall that we applied feedforward networks to language modeling by having them look only at a fixed-size window of words, and then sliding this window over the input, making independent predictions along the way. This sliding-window approach is also used in the transformer architecture we will introduce in Chapter 10.

This chapter introduces a deep learning architecture that offers an alternative way of representing time: recurrent neural networks (RNNs), and their variants like LSTMs. RNNs have a mechanism that deals directly with the sequential nature of language, allowing them to handle the temporal nature of language without the use of arbitrary fixed-sized windows. The recurrent network offers a new way to represent the prior context, in its **recurrent connections**, allowing the model's decision to depend on information from hundreds of words in the past. We'll see how to apply the model to the task of language modeling, to sequence modeling tasks like part-of-speech tagging, and to text classification tasks like sentiment analysis.

## 9.1 Recurrent Neural Networks

A recurrent neural network (RNN) is any network that contains a cycle within its network connections, meaning that the value of some unit is directly, or indirectly, dependent on its own earlier outputs as an input. While powerful, such networks are difficult to reason about and to train. However, within the general class of recurrent networks there are constrained architectures that have proven to be extremely effective when applied to language. In this section, we consider a class of recurrent networks referred to as **Elman Networks** (Elman, 1990) or **simple recurrent net-**

**works.** These networks are useful in their own right and serve as the basis for more complex approaches like the Long Short-Term Memory (LSTM) networks discussed later in this chapter. In this chapter when we use the term RNN we'll be referring to these simpler more constrained networks (although you will often see the term RNN to mean any net with recurrent properties including LSTMs).



**Figure 9.1** Simple recurrent neural network after [Elman \(1990\)](#). The hidden layer includes a recurrent connection as part of its input. That is, the activation value of the hidden layer depends on the current input as well as the activation value of the hidden layer from the previous time step.

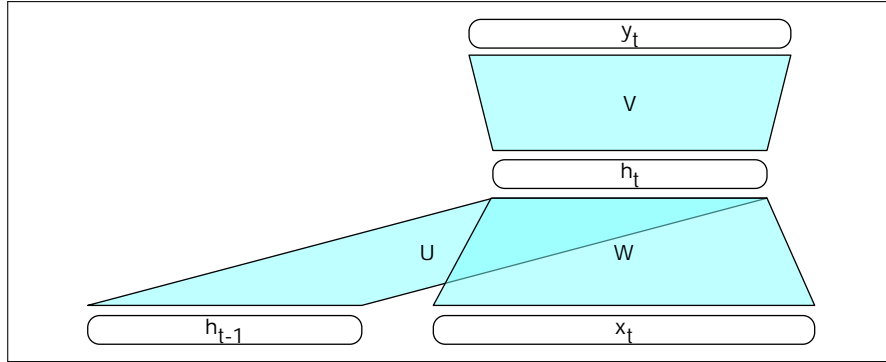
Fig. 9.1 illustrates the structure of an RNN. As with ordinary feedforward networks, an input vector representing the current input,  $\mathbf{x}_t$ , is multiplied by a weight matrix and then passed through a non-linear activation function to compute the values for a layer of hidden units. This hidden layer is then used to calculate a corresponding output,  $\mathbf{y}_t$ . In a departure from our earlier window-based approach, sequences are processed by presenting one item at a time to the network. We'll use subscripts to represent time, thus  $\mathbf{x}_t$  will mean the input vector  $\mathbf{x}$  at time  $t$ . The key difference from a feedforward network lies in the recurrent link shown in the figure with the dashed line. This link augments the input to the computation at the hidden layer with the value of the hidden layer *from the preceding point in time*.

The hidden layer from the previous time step provides a form of memory, or context, that encodes earlier processing and informs the decisions to be made at later points in time. Critically, this approach does not impose a fixed-length limit on this prior context; the context embodied in the previous hidden layer can include information extending back to the beginning of the sequence.

Adding this temporal dimension makes RNNs appear to be more complex than non-recurrent architectures. But in reality, they're not all that different. Given an input vector and the values for the hidden layer from the previous time step, we're still performing the standard feedforward calculation introduced in Chapter 7. To see this, consider Fig. 9.2 which clarifies the nature of the recurrence and how it factors into the computation at the hidden layer. The most significant change lies in the new set of weights,  $\mathbf{U}$ , that connect the hidden layer from the previous time step to the current hidden layer. These weights determine how the network makes use of past context in calculating the output for the current input. As with the other weights in the network, these connections are trained via backpropagation.

### 9.1.1 Inference in RNNs

Forward inference (mapping a sequence of inputs to a sequence of outputs) in an RNN is nearly identical to what we've already seen with feedforward networks. To compute an output  $\mathbf{y}_t$  for an input  $\mathbf{x}_t$ , we need the activation value for the hidden layer  $\mathbf{h}_t$ . To calculate this, we multiply the input  $\mathbf{x}_t$  with the weight matrix  $\mathbf{W}$ , and the hidden layer from the previous time step  $\mathbf{h}_{t-1}$  with the weight matrix  $\mathbf{U}$ . We add these values together and pass them through a suitable activation function,  $g$ , to arrive at the activation value for the current hidden layer,  $\mathbf{h}_t$ . Once we have the



**Figure 9.2** Simple recurrent neural network illustrated as a feedforward network.

values for the hidden layer, we proceed with the usual computation to generate the output vector.

$$\mathbf{h}_t = g(\mathbf{U}\mathbf{h}_{t-1} + \mathbf{W}\mathbf{x}_t) \quad (9.1)$$

$$\mathbf{y}_t = f(\mathbf{V}\mathbf{h}_t) \quad (9.2)$$

It's worthwhile here to be careful about specifying the dimensions of the input, hidden and output layers, as well as the weight matrices to make sure these calculations are correct. Let's refer to the input, hidden and output layer dimensions as  $d_{in}$ ,  $d_h$ , and  $d_{out}$  respectively. Given this, our three parameter matrices are:  $\mathbf{W} \in \mathbb{R}^{d_h \times d_{in}}$ ,  $\mathbf{U} \in \mathbb{R}^{d_h \times d_h}$ , and  $\mathbf{V} \in \mathbb{R}^{d_{out} \times d_h}$ .

In the commonly encountered case of soft classification, computing  $\mathbf{y}_t$  consists of a softmax computation that provides a probability distribution over the possible output classes.

$$\mathbf{y}_t = \text{softmax}(\mathbf{V}\mathbf{h}_t) \quad (9.3)$$

The fact that the computation at time  $t$  requires the value of the hidden layer from time  $t - 1$  mandates an incremental inference algorithm that proceeds from the start of the sequence to the end as illustrated in Fig. 9.3. The sequential nature of simple recurrent networks can also be seen by *unrolling* the network in time as is shown in Fig. 9.4. In this figure, the various layers of units are copied for each time step to illustrate that they will have differing values over time. However, the various weight matrices are shared across time.

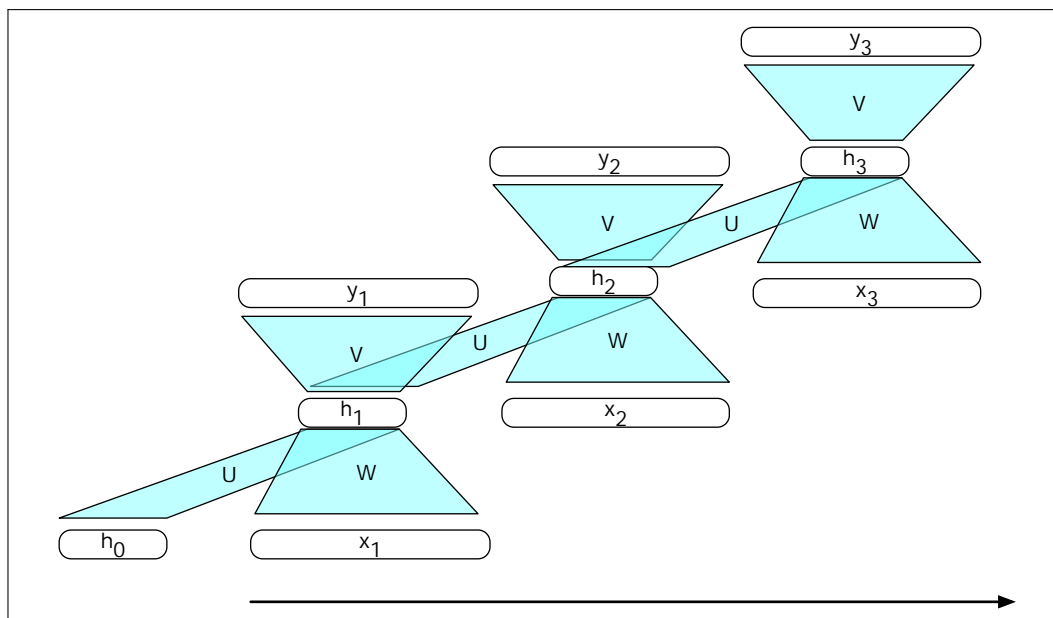
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function FORWARDRNN( $\mathbf{x}$ ,  $network$ ) returns output sequence  $\mathbf{y}$ 

   $\mathbf{h}_0 \leftarrow 0$ 
  for  $i \leftarrow 1$  to LENGTH( $\mathbf{x}$ ) do
     $\mathbf{h}_i \leftarrow g(\mathbf{U}\mathbf{h}_{i-1} + \mathbf{W}\mathbf{x}_i)$ 
     $\mathbf{y}_i \leftarrow f(\mathbf{V}\mathbf{h}_i)$ 
  return  $\mathbf{y}$ 

```

**Figure 9.3** Forward inference in a simple recurrent network. The matrices  $\mathbf{U}$ ,  $\mathbf{V}$  and  $\mathbf{W}$  are shared across time, while new values for  $\mathbf{h}$  and  $\mathbf{y}$  are calculated with each time step.



**Figure 9.4** A simple recurrent neural network shown unrolled in time. Network layers are recalculated for each time step, while the weights  $\mathbf{U}$ ,  $\mathbf{V}$  and  $\mathbf{W}$  are shared across all time steps.

### 9.1.2 Training

As with feedforward networks, we'll use a training set, a loss function, and backpropagation to obtain the gradients needed to adjust the weights in these recurrent networks. As shown in Fig. 9.2, we now have 3 sets of weights to update:  $\mathbf{W}$ , the weights from the input layer to the hidden layer,  $\mathbf{U}$ , the weights from the previous hidden layer to the current hidden layer, and finally  $\mathbf{V}$ , the weights from the hidden layer to the output layer.

Fig. 9.4 highlights two considerations that we didn't have to worry about with backpropagation in feedforward networks. First, to compute the loss function for the output at time  $t$  we need the hidden layer from time  $t - 1$ . Second, the hidden layer at time  $t$  influences both the output at time  $t$  and the hidden layer at time  $t + 1$  (and hence the output and loss at  $t + 1$ ). It follows from this that to assess the error accruing to  $\mathbf{h}_t$ , we'll need to know its influence on both the current output *as well as the ones that follow*.

Tailoring the backpropagation algorithm to this situation leads to a two-pass algorithm for training the weights in RNNs. In the first pass, we perform forward inference, computing  $\mathbf{h}_t$ ,  $\mathbf{y}_t$ , accumulating the loss at each step in time, saving the value of the hidden layer at each step for use at the next time step. In the second phase, we process the sequence in reverse, computing the required gradients as we go, computing and saving the error term for use in the hidden layer for each step backward in time. This general approach is commonly referred to as **backpropagation through time** (Werbos 1974, Rumelhart et al. 1986, Werbos 1990).

backpropagation  
through  
time

Fortunately, with modern computational frameworks and adequate computing resources, there is no need for a specialized approach to training RNNs. As illustrated in Fig. 9.4, explicitly unrolling a recurrent network into a feedforward computational graph eliminates any explicit recurrences, allowing the network weights to be trained directly. In such an approach, we provide a template that specifies the basic structure of the network, including all the necessary parameters for the input,

output, and hidden layers, the weight matrices, as well as the activation and output functions to be used. Then, when presented with a specific input sequence, we can generate an unrolled feedforward network specific to that input, and use that graph to perform forward inference or training via ordinary backpropagation.

For applications that involve much longer input sequences, such as speech recognition, character-level processing, or streaming continuous inputs, unrolling an entire input sequence may not be feasible. In these cases, we can unroll the input into manageable fixed-length segments and treat each segment as a distinct training item.

## 9.2 RNNs as Language Models

Let's see how to apply RNNs to the language modeling task. Recall from Chapter 3 that language models predict the next word in a sequence given some preceding context. For example, if the preceding context is “*Thanks for all the*” and we want to know how likely the next word is “*fish*” we would compute:

$$P(\textit{fish}|\textit{Thanks for all the})$$

Language models give us the ability to assign such a conditional probability to every possible next word, giving us a distribution over the entire vocabulary. We can also assign probabilities to entire sequences by combining these conditional probabilities with the chain rule:

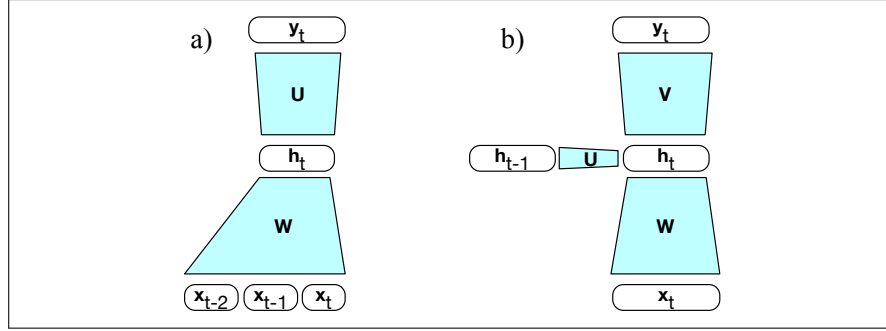
$$P(w_{1:n}) = \prod_{i=1}^n P(w_i|w_{<i})$$

The  $n$ -gram language models of Chapter 3 compute the probability of a word given counts of its occurrence with the  $n - 1$  prior words. The context is thus of size  $n - 1$ . For the feedforward language models of Chapter 7, the context is the window size.

RNN language models (Mikolov et al., 2010) process the input sequence one word at a time, attempting to predict the next word from the current word and the previous hidden state. RNNs thus don't have the limited context problem that  $n$ -gram models have, or the fixed context that feedforward language models have, since the hidden state can in principle represent information about all of the preceding words all the way back to the beginning of the sequence. Fig. 9.5 sketches this difference between a FFN language model and an RNN language model, showing that the RNN language model uses  $h_{t-1}$ , the hidden state from the previous time step, as a representation of the past context.

### 9.2.1 Forward Inference in an RNN language model

Forward inference in a recurrent language model proceeds exactly as described in Section 9.1.1. The input sequence  $\mathbf{X} = [\mathbf{x}_1; \dots; \mathbf{x}_t; \dots; \mathbf{x}_N]$  consists of a series of word embeddings each represented as a one-hot vector of size  $|V| \times 1$ , and the output prediction,  $\mathbf{y}$ , is a vector representing a probability distribution over the vocabulary. At each step, the model uses the word embedding matrix  $\mathbf{E}$  to retrieve the embedding for the current word, and then combines it with the hidden layer from the previous step to compute a new hidden layer. This hidden layer is then used to generate an output layer which is passed through a softmax layer to generate a probability



**Figure 9.5** Simplified sketch of (a) a feedforward neural language model versus (b) an RNN language model moving through a text.

distribution over the entire vocabulary. That is, at time  $t$ :

$$\mathbf{e}_t = \mathbf{E}\mathbf{x}_t \quad (9.4)$$

$$\mathbf{h}_t = g(\mathbf{U}\mathbf{h}_{t-1} + \mathbf{W}\mathbf{e}_t) \quad (9.5)$$

$$\mathbf{y}_t = \text{softmax}(\mathbf{V}\mathbf{h}_t) \quad (9.6)$$

The vector resulting from  $\mathbf{V}\mathbf{h}$  can be thought of as a set of scores over the vocabulary given the evidence provided in  $\mathbf{h}$ . Passing these scores through the softmax normalizes the scores into a probability distribution. The probability that a particular word  $i$  in the vocabulary is the next word is represented by  $\mathbf{y}_t[i]$ , the  $i$ th component of  $\mathbf{y}_t$ :

$$P(w_{t+1} = i | w_1, \dots, w_t) = \mathbf{y}_t[i] \quad (9.7)$$

The probability of an entire sequence is just the product of the probabilities of each item in the sequence, where we'll use  $\mathbf{y}_i[w_i]$  to mean the probability of the true word  $w_i$  at time step  $i$ .

$$P(w_{1:n}) = \prod_{i=1}^n P(w_i | w_{1:i-1}) \quad (9.8)$$

$$= \prod_{i=1}^n \mathbf{y}_i[w_i] \quad (9.9)$$

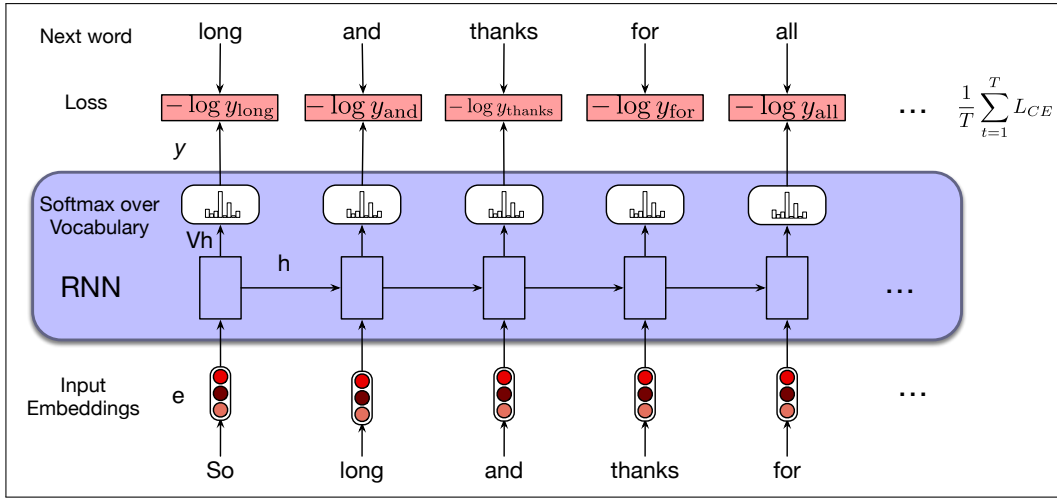
## 9.2.2 Training an RNN language model

### self-supervision

To train an RNN as a language model, we use the same **self-supervision** algorithm we saw earlier: we take a corpus of text as training material and at each time step  $t$  we have the model predict the next word. We call such a model self-supervised because we don't have to add any special gold labels to the data; the natural sequence of words is its own supervision! We simply train the model to minimize the error in predicting the true next word in the training sequence, using cross-entropy as the loss function. Recall that the cross-entropy loss measures the difference between a predicted probability distribution and the correct distribution.

$$L_{CE} = - \sum_{w \in V} \mathbf{y}_t[w] \log \hat{\mathbf{y}}_t[w] \quad (9.10)$$

In the case of language modeling, the correct distribution  $\mathbf{y}_t$  comes from knowing the next word. This is represented as a one-hot vector corresponding to the vocabulary



**Figure 9.6** Training RNNs as language models.

where the entry for the actual next word is 1, and all the other entries are 0. Thus, the cross-entropy loss for language modeling is determined by the probability the model assigns to the correct next word. So at time  $t$  the CE loss is the negative log probability the model assigns to the next word in the training sequence.

$$L_{CE}(\hat{\mathbf{y}}_t, \mathbf{y}_t) = -\log \hat{\mathbf{y}}_t[w_{t+1}] \quad (9.11)$$

Thus at each word position  $t$  of the input, the model takes as input the correct sequence of tokens  $w_{1:t}$ , and uses them to compute a probability distribution over possible next words so as to compute the model's loss for the next token  $w_{t+1}$ . Then we move to the next word, we ignore what the model predicted for the next word and instead use the correct sequence of tokens  $w_{1:t+1}$  to estimate the probability of token  $w_{t+2}$ . This idea that we always give the model the correct history sequence to predict the next word (rather than feeding the model its best case from the previous time step) is called **teacher forcing**.

teacher forcing

The weights in the network are adjusted to minimize the average CE loss over the training sequence via gradient descent. Fig. 9.6 illustrates this training regimen.

### 9.2.3 Weight Tying

Careful readers may have noticed that the input embedding matrix  $\mathbf{E}$  and the final layer matrix  $\mathbf{V}$ , which feeds the output softmax, are quite similar. The columns of  $\mathbf{E}$  represent the word embeddings for each word in the vocabulary learned during the training process with the goal that words that have similar meaning and function will have similar embeddings. And, since the length of these embeddings corresponds to the size of the hidden layer  $d_h$ , the shape of the embedding matrix  $\mathbf{E}$  is  $d_h \times |V|$ .

The final layer matrix  $\mathbf{V}$  provides a way to score the likelihood of each word in the vocabulary given the evidence present in the final hidden layer of the network through the calculation of  $\mathbf{V}\mathbf{h}$ . This results in dimensionality  $|V| \times d_h$ . That is, the rows of  $\mathbf{V}$  provide a *second set* of learned word embeddings that capture relevant aspects of word meaning. This leads to an obvious question – is it even necessary to have both? **Weight tying** is a method that dispenses with this redundancy and simply uses a single set of embeddings at the input and softmax layers. That is, we

Weight tying

dispense with  $V$  and use  $E$  in both the start and end of the computation.

$$\mathbf{e}_t = \mathbf{E}\mathbf{x}_t \quad (9.12)$$

$$\mathbf{h}_t = g(\mathbf{U}\mathbf{h}_{t-1} + \mathbf{W}\mathbf{e}_t) \quad (9.13)$$

$$\mathbf{y}_t = \text{softmax}(\mathbf{E}^T \mathbf{h}_t) \quad (9.14)$$

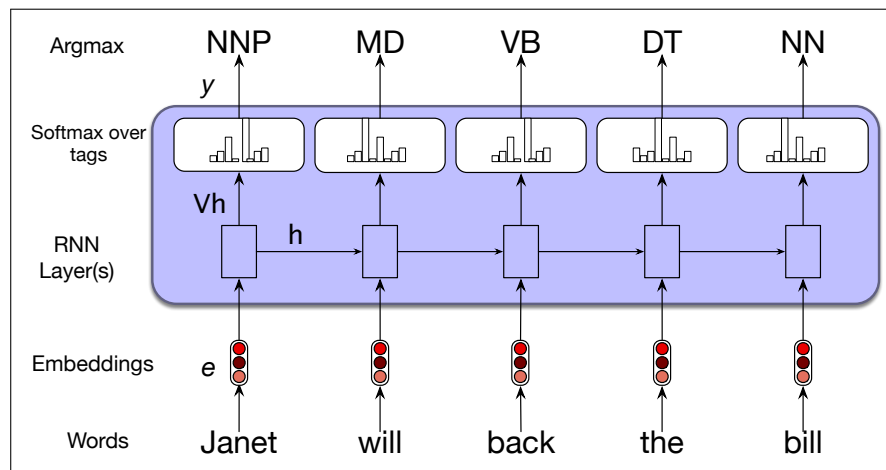
In addition to providing improved model perplexity, this approach significantly reduces the number of parameters required for the model.

## 9.3 RNNs for other NLP tasks

Now that we've seen the basic RNN architecture, let's consider how to apply it to three types of NLP tasks: *sequence classification* tasks like sentiment analysis and topic classification, *sequence labeling* tasks like part-of-speech tagging, and *text generation* tasks, including with a new architecture called the **encoder-decoder**.

### 9.3.1 Sequence Labeling

In sequence labeling, the network's task is to assign a label chosen from a small fixed set of labels to each element of a sequence, like the part-of-speech tagging and named entity recognition tasks from Chapter 8. In an RNN approach to sequence labeling, inputs are word embeddings and the outputs are tag probabilities generated by a softmax layer over the given tagset, as illustrated in Fig. 9.7.



**Figure 9.7** Part-of-speech tagging as sequence labeling with a simple RNN. Pre-trained word embeddings serve as inputs and a softmax layer provides a probability distribution over the part-of-speech tags as output at each time step.

In this figure, the inputs at each time step are pre-trained word embeddings corresponding to the input tokens. The RNN block is an abstraction that represents an unrolled simple recurrent network consisting of an input layer, hidden layer, and output layer at each time step, as well as the shared  $\mathbf{U}$ ,  $\mathbf{V}$  and  $\mathbf{W}$  weight matrices that comprise the network. The outputs of the network at each time step represent the distribution over the POS tagset generated by a softmax layer.

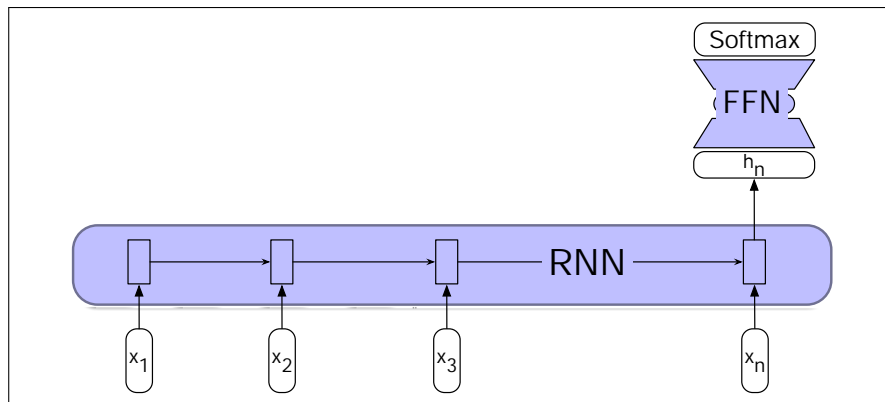


To generate a sequence of tags for a given input, we run forward inference over the input sequence and select the most likely tag from the softmax at each step. Since we're using a softmax layer to generate the probability distribution over the output tagset at each time step, we will again employ the cross-entropy loss during training.

### 9.3.2 RNNs for Sequence Classification

Another use of RNNs is to classify entire sequences rather than the tokens within them. This is the set of tasks commonly called **text classification**, like sentiment analysis or spam detection, in which we classify a text into two or three classes (like positive or negative), as well as classification tasks with a large number of categories, like document-level topic classification, or message routing for customer service applications.

To apply RNNs in this setting, we pass the text to be classified through the RNN a word at a time generating a new hidden layer at each time step. We can then take the hidden layer for the last token of the text,  $h_n$ , to constitute a compressed representation of the entire sequence. We can pass this representation  $h_n$  to a feedforward network that chooses a class via a softmax over the possible classes. Fig. 9.8 illustrates this approach.



**Figure 9.8** Sequence classification using a simple RNN combined with a feedforward network. The final hidden state from the RNN is used as the input to a feedforward network that performs the classification.

Note that in this approach we don't need intermediate outputs for the words in the sequence preceding the last element. Therefore, there are no loss terms associated with those elements. Instead, the loss function used to train the weights in the network is based entirely on the final text classification task. The output from the softmax output from the feedforward classifier together with a cross-entropy loss drives the training. The error signal from the classification is backpropagated all the way through the weights in the feedforward classifier through, to its input, and then through to the three sets of weights in the RNN as described earlier in Section 9.1.2. The training regimen that uses the loss from a downstream application to adjust the weights all the way through the network is referred to as **end-to-end training**.

end-to-end  
training

pooling

Another option, instead of using just the last token  $h_n$  to represent the whole sequence, is to use some sort of **pooling** function of all the hidden states  $h_i$  for each word  $i$  in the sequence. For example, we can create a representation that pools all

the  $n$  hidden states by taking their element-wise mean:

$$\mathbf{h}_{mean} = \frac{1}{n} \sum_{i=1}^n \mathbf{h}_i \quad (9.15)$$

Or we can take the element-wise max; the element-wise max of a set of  $n$  vectors is a new vector whose  $k$ th element is the max of the  $k$ th elements of all the  $n$  vectors.

### 9.3.3 Generation with RNN-Based Language Models

RNN-based language models can also be used to generate text. Text generation is of enormous practical importance, part of tasks like question answering, machine translation, text summarization, grammar correction, story generation, and conversational dialogue; any task where a system needs to produce text, conditioned on some other text. This use of a language model to generate text is one of the areas in which the impact of neural language models on NLP has been the largest. Text generation, along with image generation and code generation, constitute a new area of AI that is often called **generative AI**.

Recall back in Chapter 3 we saw how to generate text from an  $n$ -gram language model by adapting a **sampling** technique suggested at about the same time by Claude Shannon (Shannon, 1951) and the psychologists George Miller and Jennifer Selfridge (Miller and Selfridge, 1950). We first randomly sample a word to begin a sequence based on its suitability as the start of a sequence. We then continue to sample words *conditioned on our previous choices* until we reach a pre-determined length, or an end of sequence token is generated.

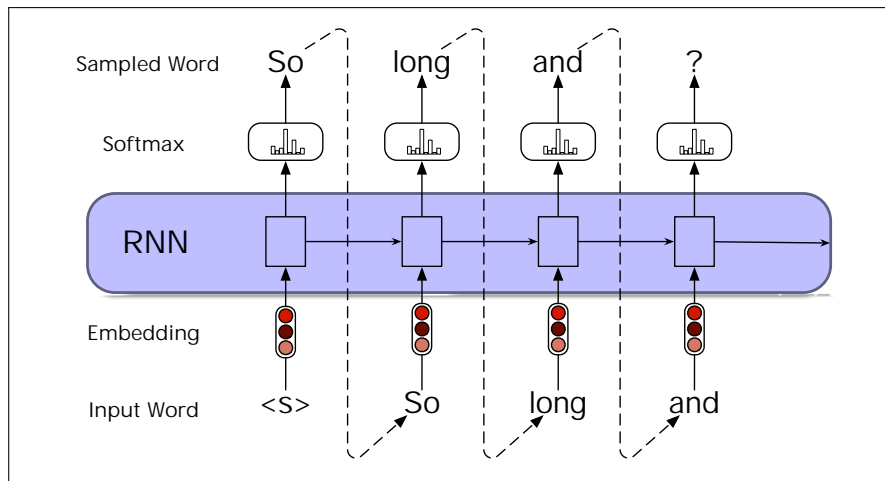
autoregressive  
generation

Today, this approach of using a language model to incrementally generate words by repeatedly sampling the next word conditioned on our previous choices is called **autoregressive generation** or **causal LM generation**. The procedure is basically the same as that described on page 40, but adapted to a neural context:

- Sample a word in the output from the softmax distribution that results from using the beginning of sentence marker,  $\langle s \rangle$ , as the first input.
- Use the word embedding for that first word as the input to the network at the next time step, and then sample the next word in the same fashion.
- Continue generating until the end of sentence marker,  $\langle /s \rangle$ , is sampled or a fixed length limit is reached.

Technically an **autoregressive** model is a model that predicts a value at time  $t$  based on a linear function of the previous values at times  $t - 1$ ,  $t - 2$ , and so on. Although language models are not linear (since they have many layers of non-linearities), we loosely refer to this generation technique as **autoregressive generation** since the word generated at each time step is conditioned on the word selected by the network from the previous step. Fig. 9.9 illustrates this approach. In this figure, the details of the RNN's hidden layers and recurrent connections are hidden within the blue block.

This simple architecture underlies state-of-the-art approaches to applications such as machine translation, summarization, and question answering. The key to these approaches is to prime the generation component with an appropriate context. That is, instead of simply using  $\langle s \rangle$  to get things started we can provide a richer task-appropriate context; for translation the context is the sentence in the source language; for summarization it's the long text we want to summarize.



**Figure 9.9** Autoregressive generation with an RNN-based neural language model.

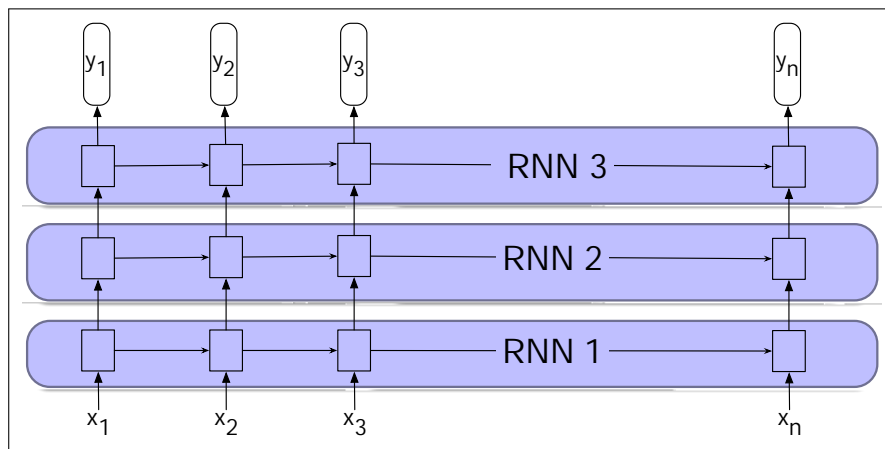
## 9.4 Stacked and Bidirectional RNN architectures

Recurrent networks are quite flexible. By combining the feedforward nature of unrolled computational graphs with vectors as common inputs and outputs, complex networks can be treated as modules that can be combined in creative ways. This section introduces two of the more common network architectures used in language processing with RNNs.

### 9.4.1 Stacked RNNs

In our examples thus far, the inputs to our RNNs have consisted of sequences of word or character embeddings (vectors) and the outputs have been vectors useful for predicting words, tags or sequence labels. However, nothing prevents us from using the entire sequence of outputs from one RNN as an input sequence to another one. **Stacked RNNs** consist of multiple networks where the output of one layer serves as the input to a subsequent layer, as shown in Fig. 9.10.

Stacked RNNs



**Figure 9.10** Stacked recurrent networks. The output of a lower level serves as the input to higher levels with the output of the last network serving as the final output.

Stacked RNNs generally outperform single-layer networks. One reason for this success seems to be that the network induces representations at differing levels of abstraction across layers. Just as the early stages of the human visual system detect edges that are then used for finding larger regions and shapes, the initial layers of stacked networks can induce representations that serve as useful abstractions for further layers—representations that might prove difficult to induce in a single RNN. The optimal number of stacked RNNs is specific to each application and to each training set. However, as the number of stacks is increased the training costs rise quickly.

### 9.4.2 Bidirectional RNNs

The RNN uses information from the left (prior) context to make its predictions at time  $t$ . But in many applications we have access to the entire input sequence; in those cases we would like to use words from the context to the right of  $t$ . One way to do this is to run two separate RNNs, one left-to-right, and one right-to-left, and concatenate their representations.

In the left-to-right RNNs we've discussed so far, the hidden state at a given time  $t$  represents everything the network knows about the sequence up to that point. The state is a function of the inputs  $x_1, \dots, x_t$  and represents the context of the network to the left of the current time.

$$\mathbf{h}_t^f = \text{RNN}_{\text{forward}}(\mathbf{x}_1, \dots, \mathbf{x}_t) \quad (9.16)$$

This new notation  $\mathbf{h}_t^f$  simply corresponds to the normal hidden state at time  $t$ , representing everything the network has gleaned from the sequence so far.

To take advantage of context to the right of the current input, we can train an RNN on a *reversed* input sequence. With this approach, the hidden state at time  $t$  represents information about the sequence to the *right* of the current input:

$$\mathbf{h}_t^b = \text{RNN}_{\text{backward}}(\mathbf{x}_t, \dots, \mathbf{x}_n) \quad (9.17)$$

Here, the hidden state  $\mathbf{h}_t^b$  represents all the information we have discerned about the sequence from  $t$  to the end of the sequence.

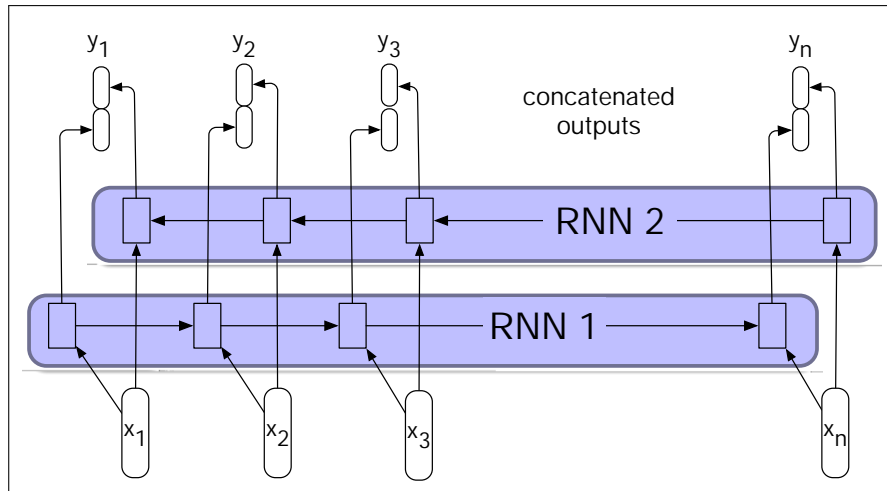
bidirectional  
RNN

A **bidirectional RNN** (Schuster and Paliwal, 1997) combines two independent RNNs, one where the input is processed from the start to the end, and the other from the end to the start. We then concatenate the two representations computed by the networks into a single vector that captures both the left and right contexts of an input at each point in time. Here we use either the semicolon ";" or the equivalent symbol  $\oplus$  to mean vector concatenation:

$$\begin{aligned} \mathbf{h}_t &= [\mathbf{h}_t^f ; \mathbf{h}_t^b] \\ &= \mathbf{h}_t^f \oplus \mathbf{h}_t^b \end{aligned} \quad (9.18)$$

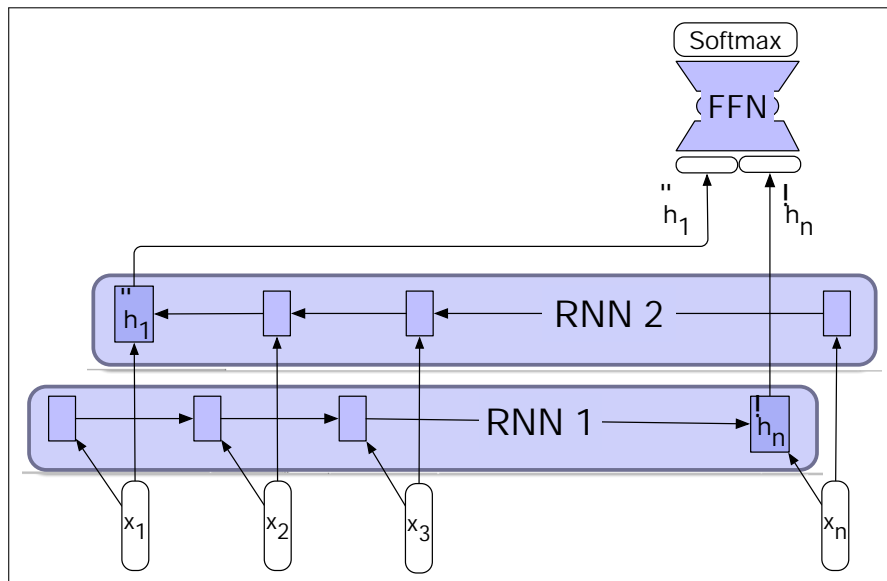
Fig. 9.11 illustrates such a bidirectional network that concatenates the outputs of the forward and backward pass. Other simple ways to combine the forward and backward contexts include element-wise addition or multiplication. The output at each step in time thus captures information to the left and to the right of the current input. In sequence labeling applications, these concatenated outputs can serve as the basis for a local labeling decision.

Bidirectional RNNs have also proven to be quite effective for sequence classification. Recall from Fig. 9.8 that for sequence classification we used the final hidden



**Figure 9.11** A bidirectional RNN. Separate models are trained in the forward and backward directions, with the output of each model at each time point concatenated to represent the bidirectional state at that time point.

state of the RNN as the input to a subsequent feedforward classifier. A difficulty with this approach is that the final state naturally reflects more information about the end of the sentence than its beginning. Bidirectional RNNs provide a simple solution to this problem; as shown in Fig. 9.12, we simply combine the final hidden states from the forward and backward passes (for example by concatenation) and use that as input for follow-on processing.



**Figure 9.12** A bidirectional RNN for sequence classification. The final hidden units from the forward and backward passes are combined to represent the entire sequence. This combined representation serves as input to the subsequent classifier.

## 9.5 The LSTM

In practice, it is quite difficult to train RNNs for tasks that require a network to make use of information distant from the current point of processing. Despite having access to the entire preceding sequence, the information encoded in hidden states tends to be fairly local, more relevant to the most recent parts of the input sequence and recent decisions. Yet distant information is critical to many language applications. Consider the following example in the context of language modeling.

(9.19) The flights the airline was cancelling were full.

Assigning a high probability to *was* following *airline* is straightforward since *airline* provides a strong local context for the singular agreement. However, assigning an appropriate probability to *were* is quite difficult, not only because the plural *flights* is quite distant, but also because the intervening context involves singular constituents. Ideally, a network should be able to retain the distant information about plural *flights* until it is needed, while still processing the intermediate parts of the sequence correctly.

One reason for the inability of RNNs to carry forward critical information is that the hidden layers, and, by extension, the weights that determine the values in the hidden layer, are being asked to perform two tasks simultaneously: provide information useful for the current decision, and updating and carrying forward information required for future decisions.

A second difficulty with training RNNs arises from the need to backpropagate the error signal back through time. Recall from Section 9.1.2 that the hidden layer at time  $t$  contributes to the loss at the next time step since it takes part in that calculation. As a result, during the backward pass of training, the hidden layers are subject to repeated multiplications, as determined by the length of the sequence. A frequent result of this process is that the gradients are eventually driven to zero, a situation called the **vanishing gradients** problem.

vanishing  
gradients

To address these issues, more complex network architectures have been designed to explicitly manage the task of maintaining relevant context over time, by enabling the network to learn to forget information that is no longer needed and to remember information required for decisions still to come.

The most commonly used such extension to RNNs is the **long short-term memory** (LSTM) network (Hochreiter and Schmidhuber, 1997). LSTMs divide the context management problem into two subproblems: removing information no longer needed from the context, and adding information likely to be needed for later decision making. The key to solving both problems is to learn how to manage this context rather than hard-coding a strategy into the architecture. LSTMs accomplish this by first adding an explicit context layer to the architecture (in addition to the usual recurrent hidden layer), and through the use of specialized neural units that make use of *gates* to control the flow of information into and out of the units that comprise the network layers. These gates are implemented through the use of additional weights that operate sequentially on the input, and previous hidden layer, and previous context layers.

long short-term  
memory

The gates in an LSTM share a common design pattern; each consists of a feed-forward layer, followed by a sigmoid activation function, followed by a pointwise multiplication with the layer being gated. The choice of the sigmoid as the activation function arises from its tendency to push its outputs to either 0 or 1. Combining this with a pointwise multiplication has an effect similar to that of a binary mask. Values

in the layer being gated that align with values near 1 in the mask are passed through nearly unchanged; values corresponding to lower values are essentially erased.

forget gate

The first gate we'll consider is the **forget gate**. The purpose of this gate is to delete information from the context that is no longer needed. The forget gate computes a weighted sum of the previous state's hidden layer and the current input and passes that through a sigmoid. This mask is then multiplied element-wise by the context vector to remove the information from context that is no longer required. Element-wise multiplication of two vectors (represented by the operator  $\odot$ , and sometimes called the **Hadamard product**) is the vector of the same dimension as the two input vectors, where each element  $i$  is the product of element  $i$  in the two input vectors:

$$\mathbf{f}_t = \sigma(\mathbf{U}_f \mathbf{h}_{t-1} + \mathbf{W}_f \mathbf{x}_t) \quad (9.20)$$

$$\mathbf{k}_t = \mathbf{c}_{t-1} \odot \mathbf{f}_t \quad (9.21)$$

The next task is to compute the actual information we need to extract from the previous hidden state and current inputs—the same basic computation we've been using for all our recurrent networks.

$$\mathbf{g}_t = \tanh(\mathbf{U}_g \mathbf{h}_{t-1} + \mathbf{W}_g \mathbf{x}_t) \quad (9.22)$$

add gate

Next, we generate the mask for the **add gate** to select the information to add to the current context.

$$\mathbf{i}_t = \sigma(\mathbf{U}_i \mathbf{h}_{t-1} + \mathbf{W}_i \mathbf{x}_t) \quad (9.23)$$

$$\mathbf{j}_t = \mathbf{g}_t \odot \mathbf{i}_t \quad (9.24)$$

Next, we add this to the modified context vector to get our new context vector.

$$\mathbf{c}_t = \mathbf{j}_t + \mathbf{k}_t \quad (9.25)$$

output gate

The final gate we'll use is the **output gate** which is used to decide what information is required for the current hidden state (as opposed to what information needs to be preserved for future decisions).

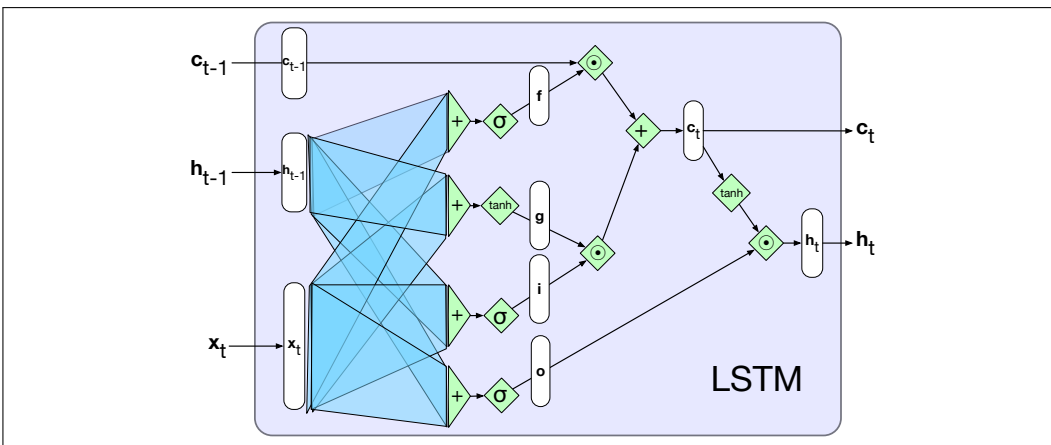
$$\mathbf{o}_t = \sigma(\mathbf{U}_o \mathbf{h}_{t-1} + \mathbf{W}_o \mathbf{x}_t) \quad (9.26)$$

$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{c}_t) \quad (9.27)$$

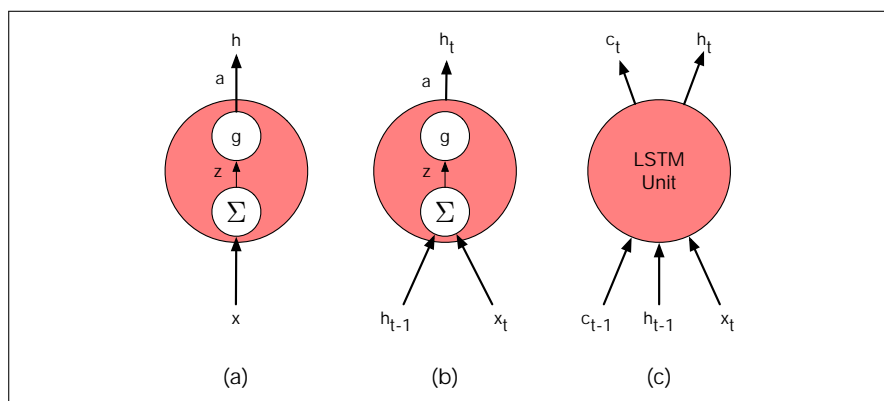
Fig. 9.13 illustrates the complete computation for a single LSTM unit. Given the appropriate weights for the various gates, an LSTM accepts as input the context layer, and hidden layer from the previous time step, along with the current input vector. It then generates updated context and hidden vectors as output. The hidden layer,  $\mathbf{h}_t$ , can be used as input to subsequent layers in a stacked RNN, or to generate an output for the final layer of a network.

### 9.5.1 Gated Units, Layers and Networks

The neural units used in LSTMs are obviously much more complex than those used in basic feedforward networks. Fortunately, this complexity is encapsulated within the basic processing units, allowing us to maintain modularity and to easily experiment with different architectures. To see this, consider Fig. 9.14 which illustrates the inputs and outputs associated with each kind of unit.



**Figure 9.13** A single LSTM unit displayed as a computation graph. The inputs to each unit consists of the current input,  $x$ , the previous hidden state,  $h_{t-1}$ , and the previous context,  $c_{t-1}$ . The outputs are a new hidden state,  $h_t$  and an updated context,  $c_t$ .



**Figure 9.14** Basic neural units used in feedforward, simple recurrent networks (SRN), and long short-term memory (LSTM).

At the far left, (a) is the basic feedforward unit where a single set of weights and a single activation function determine its output, and when arranged in a layer there are no connections among the units in the layer. Next, (b) represents the unit in a simple recurrent network. Now there are two inputs and an additional set of weights to go with it. However, there is still a single activation function and output.

The increased complexity of the LSTM units is encapsulated within the unit itself. The only additional external complexity for the LSTM over the basic recurrent unit (b) is the presence of the additional context vector as an input and output.

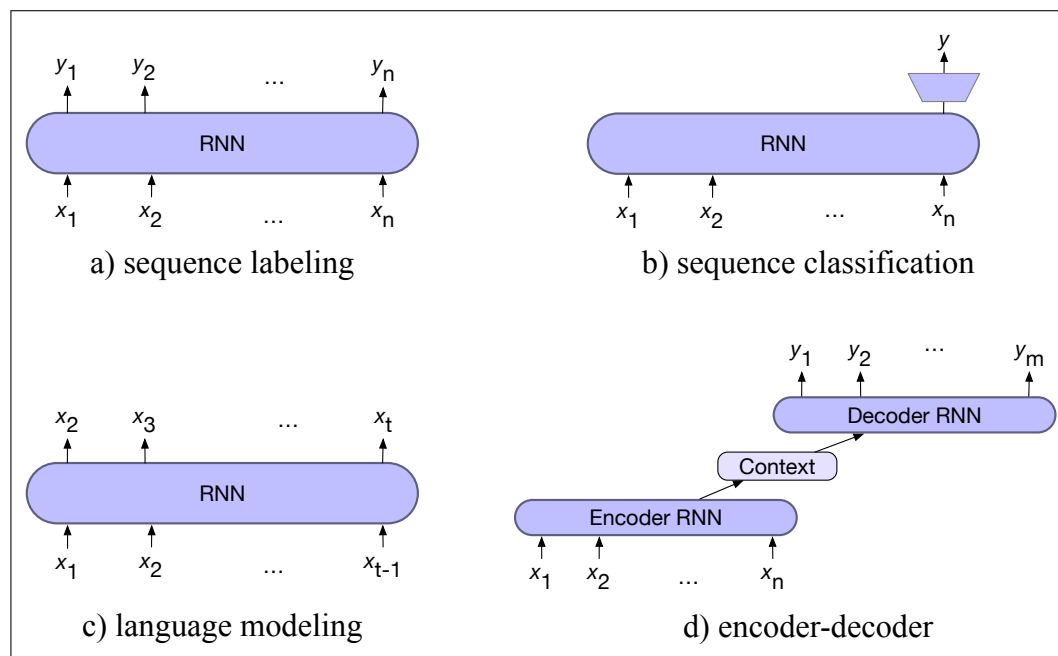
This modularity is key to the power and widespread applicability of LSTM units. LSTM units (or other varieties, like GRUs) can be substituted into any of the network architectures described in Section 9.4. And, as with simple RNNs, multi-layered networks making use of gated units can be unrolled into deep feedforward networks and trained in the usual fashion with backpropagation. In practice, therefore, LSTMs rather than RNNs have become the standard unit for any modern system that makes use of recurrent networks.



## 9.6 Summary: Common RNN NLP Architectures

We've now introduced the RNN, seen advanced components like stacking multiple layers and using the LSTM version, and seen how the RNN can be applied to various tasks. Let's take a moment to summarize the architectures for these applications.

Fig. 9.15 shows the three architectures we've discussed so far: sequence labeling, sequence classification, and language modeling. In sequence labeling (for example for part of speech tagging), we train a model to produce a label for each input word or token. In sequence classification, for example for sentiment analysis, we ignore the output for each token, and only take the value from the end of the sequence (and similarly the model's training signal comes from backpropagation from that last token). In language modeling, we train the model to predict the next word at each token step. In the next section we'll introduce a fourth architecture, the **encoder-decoder**.



**Figure 9.15** Four architectures for NLP tasks. In sequence labeling (POS or named entity tagging) we map each input token  $x_i$  to an output token  $y_i$ . In sequence classification we map the entire input sequence to a single class. In language modeling we output the next token conditioned on previous tokens. In the encoder model we have two separate RNN models, one of which maps from an input sequence  $\mathbf{x}$  to an intermediate representation we call the **context**, and a second of which maps from the context to an output sequence  $\mathbf{y}$ .

## 9.7 The Encoder-Decoder Model with RNNs

In this section we introduce a new model, the encoder-decoder model, which is used when we are taking an input sequence and translating it to an output sequence that is of a different length than the input, and doesn't align with it in a word-to-word way. Recall that in the sequence labeling task, we have two sequences, but they are

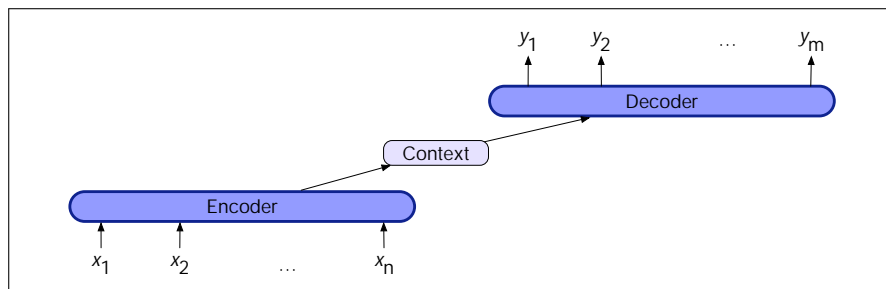
the same length (for example in part-of-speech tagging each token gets an associated tag), each input is associated with a specific output, and the labeling for that output takes mostly local information. Thus deciding whether a word is a verb or a noun, we look mostly at the word and the neighboring words.

By contrast, encoder-decoder models are used especially for tasks like machine translation, where the input sequence and output sequence can have different lengths and the mapping between a token in the input and a token in the output can be very indirect (in some languages the verb appears at the beginning of the sentence; in other languages at the end). We'll introduce machine translation in detail in Chapter 13, but for now we'll just point out that the mapping for a sentence in English to a sentence in Tagalog or Yoruba can have very different numbers of words, and the words can be in a very different order.

encoder-decoder

**Encoder-decoder** networks, sometimes called **sequence-to-sequence** networks, are models capable of generating contextually appropriate, arbitrary length, output sequences given an input sequence. Encoder-decoder networks have been applied to a very wide range of applications including summarization, question answering, and dialogue, but they are particularly popular for machine translation.

The key idea underlying these networks is the use of an **encoder** network that takes an input sequence and creates a contextualized representation of it, often called the **context**. This representation is then passed to a **decoder** which generates a task-specific output sequence. Fig. 9.16 illustrates the architecture



**Figure 9.16** The encoder-decoder architecture. The context is a function of the hidden representations of the input, and may be used by the decoder in a variety of ways.

Encoder-decoder networks consist of three components:

1. An **encoder** that accepts an input sequence,  $x_1^n$ , and generates a corresponding sequence of contextualized representations,  $h_1^n$ . LSTMs, convolutional networks, and Transformers can all be employed as encoders.
2. A **context vector**,  $c$ , which is a function of  $h_1^n$ , and conveys the essence of the input to the decoder.
3. A **decoder**, which accepts  $c$  as input and generates an arbitrary length sequence of hidden states  $h_1^m$ , from which a corresponding sequence of output states  $y_1^m$ , can be obtained. Just as with encoders, decoders can be realized by any kind of sequence architecture.

In this section we'll describe an encoder-decoder network based on a pair of RNNs, but we'll see in Chapter 13 how to apply them to transformers as well. We'll build up the equations for encoder-decode models by starting with the conditional RNN language model  $p(y)$ , the probability of a sequence  $y$ .

Recall that in any language model, we can break down the probability as follows:

$$p(y) = p(y_1)p(y_2|y_1)p(y_3|y_1, y_2) \dots P(y_m|y_1, \dots, y_{m-1}) \quad (9.28)$$

In RNN language modeling, at a particular time  $t$ , we pass the prefix of  $t - 1$  tokens through the language model, using forward inference to produce a sequence of hidden states, ending with the hidden state corresponding to the last word of the prefix. We then use the final hidden state of the prefix as our starting point to generate the next token.

More formally, if  $g$  is an activation function like  $\tanh$  or ReLU, a function of the input at time  $t$  and the hidden state at time  $t - 1$ , and  $f$  is a softmax over the set of possible vocabulary items, then at time  $t$  the output  $\mathbf{y}_t$  and hidden state  $\mathbf{h}_t$  are computed as:

$$\mathbf{h}_t = g(\mathbf{h}_{t-1}, \mathbf{x}_t) \quad (9.29)$$

$$\mathbf{y}_t = f(\mathbf{h}_t) \quad (9.30)$$

sentence  
separation

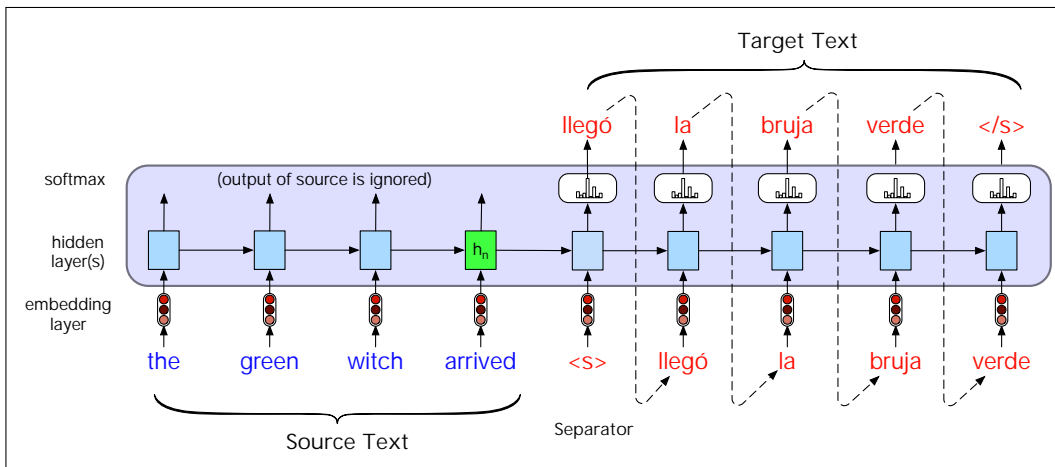
We only have to make one slight change to turn this language model with autoregressive generation into an encoder-decoder model that is a translation model that can translate from a **source text** in one language to a **target text** in a second: add a **sentence separation** marker at the end of the source text, and then simply concatenate the target text.

Let's use  $\langle s \rangle$  for our sentence separate token, and let's think about translating an English source text ("the green witch arrived"), to a Spanish sentence ("*llegó la bruja verde*") (which can be glossed word-by-word as 'arrived the witch green'). We could also illustrate encoder-decoder models with a question-answer pair, or a text-summarization pair, but m

Let's use  $x$  to refer to the source text (in this case in English) plus the separator token  $\langle s \rangle$ , and  $y$  to refer to the target text  $y$  (in this case in Spanish). Then an encoder-decoder model computes the probability  $p(y|x)$  as follows:

$$p(y|x) = p(y_1|x)p(y_2|y_1,x)p(y_3|y_1,y_2,x)\dots P(y_m|y_1,\dots,y_{m-1},x) \quad (9.31)$$

Fig. 9.17 shows the setup for a simplified version of the encoder-decoder model (we'll see the full model, which requires the new concept of **attention**, in the next section).

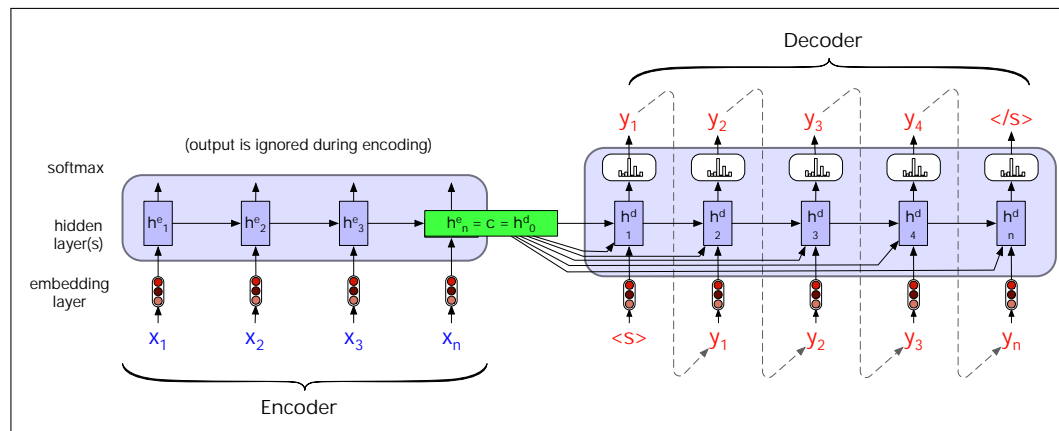


**Figure 9.17** Translating a single sentence (inference time) in the basic RNN version of encoder-decoder approach to machine translation. Source and target sentences are concatenated with a separator token in between, and the decoder uses context information from the encoder's last hidden state.

Fig. 9.17 shows an English source text ("the green witch arrived"), a sentence separator token  $\langle s \rangle$ , and a Spanish target text ("*llegó la bruja verde*"). To trans-

late a source text, we run it through the network performing forward inference to generate hidden states until we get to the end of the source. Then we begin autoregressive generation, asking for a word in the context of the hidden layer from the end of the source input as well as the end-of-sentence marker. Subsequent words are conditioned on the previous hidden state and the embedding for the last word generated.

Let's formalize and generalize this model a bit in Fig. 9.18. (To help keep things straight, we'll use the superscripts  $e$  and  $d$  where needed to distinguish the hidden states of the encoder and the decoder.) The elements of the network on the left process the input sequence  $x$  and comprise the **encoder**. While our simplified figure shows only a single network layer for the encoder, stacked architectures are the norm, where the output states from the top layer of the stack are taken as the final representation. A widely used encoder design makes use of stacked biLSTMs where the hidden states from top layers from the forward and backward passes are concatenated as described in Chapter 9 to provide the contextualized representations for each time step.



**Figure 9.18** A more formal version of translating a sentence at inference time in the basic RNN-based encoder-decoder architecture. The final hidden state of the encoder RNN,  $h_n^e$ , serves as the context for the decoder in its role as  $h_0^d$  in the decoder RNN.

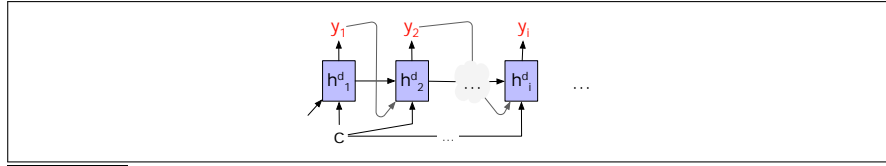
The entire purpose of the encoder is to generate a contextualized representation of the input. This representation is embodied in the final hidden state of the encoder,  $h_n^e$ . This representation, also called **c** for **context**, is then passed to the decoder.

The **decoder** network on the right takes this state and uses it to initialize the first hidden state of the decoder. That is, the first decoder RNN cell uses  $c$  as its prior hidden state  $h_0^d$ . The decoder autoregressively generates a sequence of outputs, an element at a time, until an end-of-sequence marker is generated. Each hidden state is conditioned on the previous hidden state and the output generated in the previous state.

One weakness of this approach as described so far is that the influence of the context vector,  $c$ , will wane as the output sequence is generated. A solution is to make the context vector  $c$  available at each step in the decoding process by adding it as a parameter to the computation of the current hidden state, using the following equation (illustrated in Fig. 9.19):

$$\mathbf{h}_t^d = g(\hat{y}_{t-1}, \mathbf{h}_{t-1}^d, \mathbf{c}) \quad (9.32)$$

Now we're ready to see the full equations for this version of the decoder in the basic



**Figure 9.19** Allowing every hidden state of the decoder (not just the first decoder state) to be influenced by the context  $c$  produced by the encoder.

encoder-decoder model, with context available at each decoding timestep. Recall that  $g$  is a stand-in for some flavor of RNN and  $\hat{y}_{t-1}$  is the embedding for the output sampled from the softmax at the previous step:

$$\begin{aligned}
 \mathbf{c} &= \mathbf{h}_n^e \\
 \mathbf{h}_0^d &= \mathbf{c} \\
 \mathbf{h}_t^d &= g(\hat{y}_{t-1}, \mathbf{h}_{t-1}^d, \mathbf{c}) \\
 \mathbf{z}_t &= f(\mathbf{h}_t^d) \\
 y_t &= \text{softmax}(\mathbf{z}_t)
 \end{aligned} \tag{9.33}$$

Finally, as shown earlier, the output  $y$  at each time step consists of a softmax computation over the set of possible outputs (the vocabulary, in the case of language modeling or MT). We compute the most likely output at each time step by taking the argmax over the softmax output:

$$\hat{y}_t = \operatorname{argmax}_{w \in V} P(w | x, y_1 \dots y_{t-1}) \tag{9.34}$$

### 9.7.1 Training the Encoder-Decoder Model

Encoder-decoder architectures are trained end-to-end, just as with the RNN language models of Chapter 9. Each training example is a tuple of paired strings, a source and a target. Concatenated with a separator token, these source-target pairs can now serve as training data.

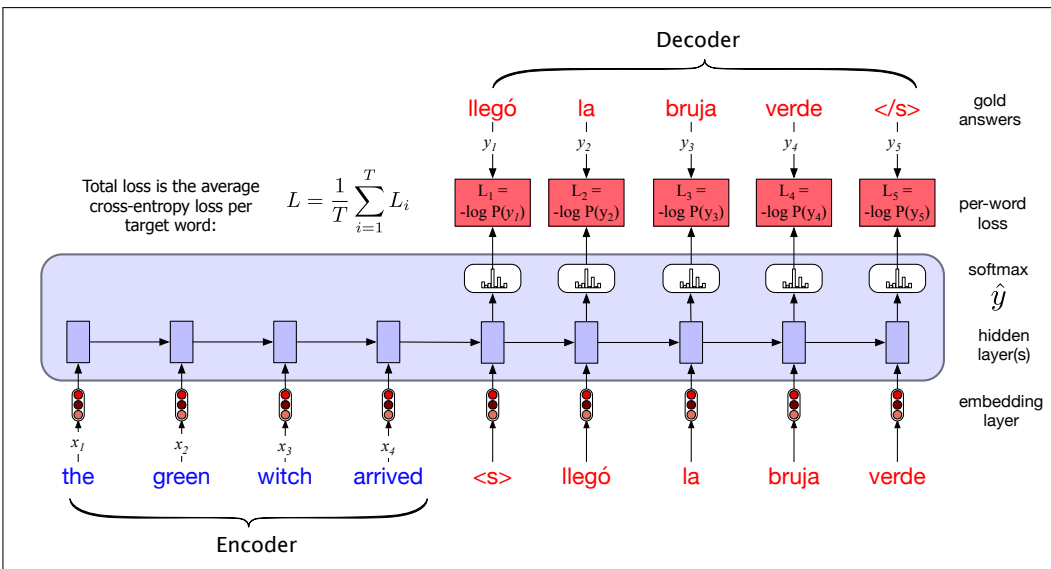
For MT, the training data typically consists of sets of sentences and their translations. These can be drawn from standard datasets of aligned sentence pairs, as we'll discuss in Section 13.2.2. Once we have a training set, the training itself proceeds as with any RNN-based language model. The network is given the source text and then starting with the separator token is trained autoregressively to predict the next word, as shown in Fig. 9.20.

Note the differences between training (Fig. 9.20) and inference (Fig. 9.17) with respect to the outputs at each time step. The decoder during inference uses its own estimated output  $\hat{y}_t$  as the input for the next time step  $x_{t+1}$ . Thus the decoder will tend to deviate more and more from the gold target sentence as it keeps generating more tokens. In training, therefore, it is more common to use **teacher forcing** in the decoder. Teacher forcing means that we force the system to use the gold target token from training as the next input  $x_{t+1}$ , rather than allowing it to rely on the (possibly erroneous) decoder output  $\hat{y}_t$ . This speeds up training.

teacher forcing

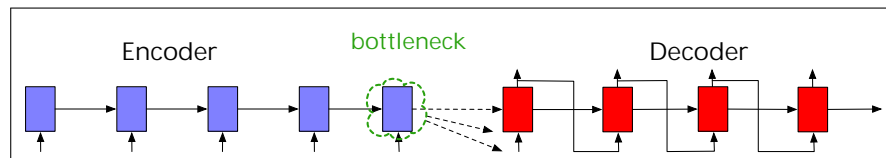
## 9.8 Attention

The simplicity of the encoder-decoder model is its clean separation of the encoder—which builds a representation of the source text—from the decoder, which uses this



**Figure 9.20** Training the basic RNN encoder-decoder approach to machine translation. Note that in the decoder we usually don't propagate the model's softmax outputs  $\hat{y}_t$ , but use **teacher forcing** to force each input to the correct gold value for training. We compute the softmax output distribution over  $\hat{y}$  in the decoder in order to compute the loss at each token, which can then be averaged to compute a loss for the sentence.

context to generate a target text. In the model as we've described it so far, this context vector is  $h_n$ , the hidden state of the last (nth) time step of the source text. This final hidden state is thus acting as a **bottleneck**: it must represent absolutely everything about the meaning of the source text, since the only thing the decoder knows about the source text is what's in this context vector (Fig. 9.21). Information at the beginning of the sentence, especially for long sentences, may not be equally well represented in the context vector.



**Figure 9.21** Requiring the context  $c$  to be only the encoder's final hidden state forces all the information from the entire source sentence to pass through this representational bottleneck.

#### attention mechanism

The **attention mechanism** is a solution to the bottleneck problem, a way of allowing the decoder to get information from *all* the hidden states of the encoder, not just the last hidden state.

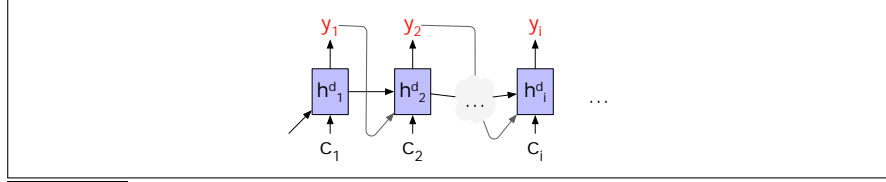
In the attention mechanism, as in the vanilla encoder-decoder model, the context vector  $\mathbf{c}$  is a single vector that is a function of the hidden states of the encoder, that is,  $\mathbf{c} = f(\mathbf{h}_1^e \dots \mathbf{h}_n^e)$ . Because the number of hidden states varies with the size of the input, we can't use the entire tensor of encoder hidden state vectors directly as the context for the decoder.

The idea of attention is instead to create the single fixed-length vector  $c$  by taking a weighted sum of all the encoder hidden states. The weights focus on ('attend to') a particular part of the source text that is relevant for the token the decoder is currently producing. Attention thus replaces the static context vector with one that is dynamically derived from the encoder hidden states, different for each token in

decoding.

This context vector,  $\mathbf{c}_i$ , is generated anew with each decoding step  $i$  and takes all of the encoder hidden states into account in its derivation. We then make this context available during decoding by conditioning the computation of the current decoder hidden state on it (along with the prior hidden state and the previous output generated by the decoder), as we see in this equation (and Fig. 9.22):

$$\mathbf{h}_i^d = g(\hat{y}_{i-1}, \mathbf{h}_{i-1}^d, \mathbf{c}_i) \quad (9.35)$$



**Figure 9.22** The attention mechanism allows each hidden state of the decoder to see a different, dynamic, context, which is a function of all the encoder hidden states.

The first step in computing  $\mathbf{c}_i$  is to compute how much to focus on each encoder state, how *relevant* each encoder state is to the decoder state captured in  $\mathbf{h}_{i-1}^d$ . We capture relevance by computing—at each state  $i$  during decoding—a *score*( $\mathbf{h}_{i-1}^d, \mathbf{h}_j^e$ ) for each encoder state  $j$ .

dot-product  
attention

The simplest such score, called **dot-product attention**, implements relevance as similarity: measuring how similar the decoder hidden state is to an encoder hidden state, by computing the dot product between them:

$$\text{score}(\mathbf{h}_{i-1}^d, \mathbf{h}_j^e) = \mathbf{h}_{i-1}^d \cdot \mathbf{h}_j^e \quad (9.36)$$

The score that results from this dot product is a scalar that reflects the degree of similarity between the two vectors. The vector of these scores across all the encoder hidden states gives us the relevance of each encoder state to the current step of the decoder.

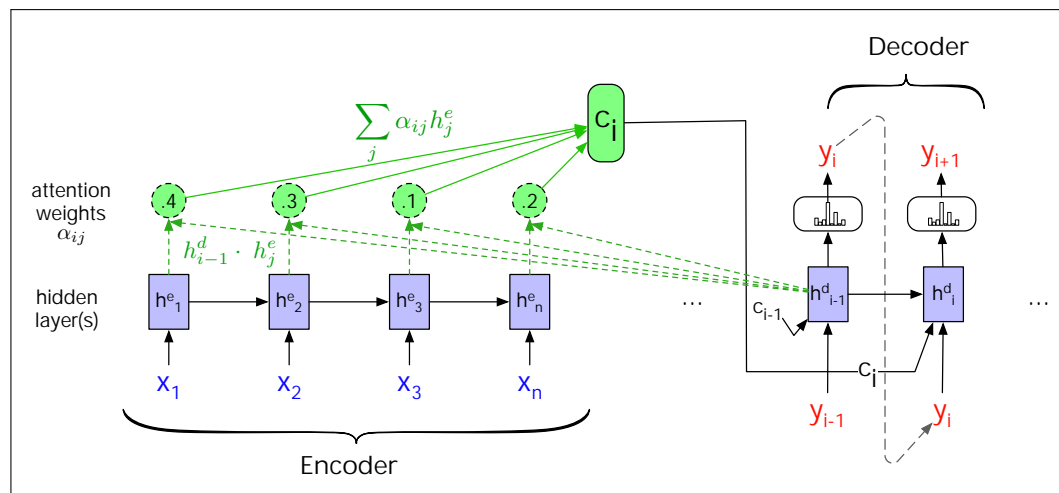
To make use of these scores, we'll normalize them with a softmax to create a vector of weights,  $\alpha_{ij}$ , that tells us the proportional relevance of each encoder hidden state  $j$  to the prior hidden decoder state,  $\mathbf{h}_{i-1}^d$ .

$$\begin{aligned} \alpha_{ij} &= \text{softmax}(\text{score}(\mathbf{h}_{i-1}^d, \mathbf{h}_j^e) \quad \forall j \in e) \\ &= \frac{\exp(\text{score}(\mathbf{h}_{i-1}^d, \mathbf{h}_j^e))}{\sum_k \exp(\text{score}(\mathbf{h}_{i-1}^d, \mathbf{h}_k^e))} \end{aligned} \quad (9.37)$$

Finally, given the distribution in  $\alpha$ , we can compute a fixed-length context vector for the current decoder state by taking a weighted average over all the encoder hidden states.

$$\mathbf{c}_i = \sum_j \alpha_{ij} \mathbf{h}_j^e \quad (9.38)$$

With this, we finally have a fixed-length context vector that takes into account information from the entire encoder state that is dynamically updated to reflect the needs of the decoder at each step of decoding. Fig. 9.23 illustrates an encoder-decoder network with attention, focusing on the computation of one context vector  $\mathbf{c}_i$ .



**Figure 9.23** A sketch of the encoder-decoder network with attention, focusing on the computation of  $c_i$ . The context value  $c_i$  is one of the inputs to the computation of  $h_i^d$ . It is computed by taking the weighted sum of all the encoder hidden states, each weighted by their dot product with the prior decoder hidden state  $h_{i-1}^d$ .

It's also possible to create more sophisticated scoring functions for attention models. Instead of simple dot product attention, we can get a more powerful function that computes the relevance of each encoder hidden state to the decoder hidden state by parameterizing the score with its own set of weights,  $\mathbf{W}_s$ .

$$\text{score}(\mathbf{h}_{i-1}^d, \mathbf{h}_j^e) = \mathbf{h}_{i-1}^d \mathbf{W}_s \mathbf{h}_j^e$$

The weights  $\mathbf{W}_s$ , which are then trained during normal end-to-end training, give the network the ability to learn which aspects of similarity between the decoder and encoder states are important to the current application. This bilinear model also allows the encoder and decoder to use different dimensional vectors, whereas the simple dot-product attention requires that the encoder and decoder hidden states have the same dimensionality.

We'll return to the concept of attention when we defined the transformer architecture in Chapter 10, which is based on a slight modification of attention called **self-attention**.

## 9.9 Summary

This chapter has introduced the concepts of recurrent neural networks and how they can be applied to language problems. Here's a summary of the main points that we covered:

- In simple Recurrent Neural Networks sequences are processed one element at a time, with the output of each neural unit at time  $t$  based both on the current input at  $t$  and the hidden layer from time  $t - 1$ .
- RNNs can be trained with a straightforward extension of the backpropagation algorithm, known as **backpropagation through time** (BPTT).
- Simple recurrent networks fail on long inputs because of problems like **vanishing gradients**; instead modern systems use more complex gated architec-



tures such as **LSTMs** that explicitly decide what to remember and forget in their hidden and context layers.

- Common language-based applications for RNNs include:
  - Probabilistic language modeling: assigning a probability to a sequence, or to the next element of a sequence given the preceding words.
  - Auto-regressive generation using a trained language model.
  - Sequence labeling like part-of-speech tagging, where each element of a sequence is assigned a label.
  - Sequence classification, where an entire text is assigned to a category, as in spam detection, sentiment analysis or topic classification.
  - Encoder-decoder architectures, where an input is mapped to an output of different length and alignment.

## Bibliographical and Historical Notes

Influential investigations of RNNs were conducted in the context of the Parallel Distributed Processing (PDP) group at UC San Diego in the 1980's. Much of this work was directed at human cognitive modeling rather than practical NLP applications (Rumelhart and McClelland 1986c, McClelland and Rumelhart 1986). Models using recurrence at the hidden layer in a feedforward network (Elman networks) were introduced by Elman (1990). Similar architectures were investigated by Jordan (1986) with a recurrence from the output layer, and Mathis and Mozer (1995) with the addition of a recurrent context layer prior to the hidden layer. The possibility of unrolling a recurrent network into an equivalent feedforward network is discussed in (Rumelhart and McClelland, 1986c).

In parallel with work in cognitive modeling, RNNs were investigated extensively in the continuous domain in the signal processing and speech communities (Giles et al. 1994, Robinson et al. 1996). Schuster and Paliwal (1997) introduced bidirectional RNNs and described results on the TIMIT phoneme transcription task.

While theoretically interesting, the difficulty with training RNNs and managing context over long sequences impeded progress on practical applications. This situation changed with the introduction of LSTMs in Hochreiter and Schmidhuber (1997) and Gers et al. (2000). Impressive performance gains were demonstrated on tasks at the boundary of signal processing and language processing including phoneme recognition (Graves and Schmidhuber, 2005), handwriting recognition (Graves et al., 2007) and most significantly speech recognition (Graves et al., 2013).

Interest in applying neural networks to practical NLP problems surged with the work of Collobert and Weston (2008) and Collobert et al. (2011). These efforts made use of learned word embeddings, convolutional networks, and end-to-end training. They demonstrated near state-of-the-art performance on a number of standard shared tasks including part-of-speech tagging, chunking, named entity recognition and semantic role labeling without the use of hand-engineered features.

Approaches that married LSTMs with pre-trained collections of word-embeddings based on word2vec (Mikolov et al., 2013a) and GloVe (Pennington et al., 2014) quickly came to dominate many common tasks: part-of-speech tagging (Ling et al., 2015), syntactic chunking (Søgaard and Goldberg, 2016), named entity recognition (Chiu and Nichols, 2016; Ma and Hovy, 2016), opinion mining (Irsoy and Cardie,

2014), semantic role labeling (Zhou and Xu, 2015a) and AMR parsing (Foland and Martin, 2016). As with the earlier surge of progress involving statistical machine learning, these advances were made possible by the availability of training data provided by CONLL, SemEval, and other shared tasks, as well as shared resources such as Ontonotes (Pradhan et al., 2007b), and PropBank (Palmer et al., 2005).

The modern neural encoder-decoder approach was pioneered by Kalchbrenner and Blunsom (2013), who used a CNN encoder and an RNN decoder. Cho et al. (2014) (who coined the name “encoder-decoder”) and Sutskever et al. (2014) then showed how to use extended RNNs for both encoder and decoder. The idea that a generative decoder should take as input a soft weighting of the inputs, the central idea of attention, was first developed by Graves (2013) in the context of handwriting recognition. Bahdanau et al. (2015) extended the idea, named it “attention” and applied it to MT.