## ML Week

### 0x0A Recommendation

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### Definition

Given data about a user, his environment, and some items of interest (*training data*), determine items to recommend.

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Given data about a user, his environment, and some items of interest (*training data*), determine items to recommend.

We don't have to find the  $\max k$ .

It's enough to find k within some max n.

## Examples

- Amazon
- Google News (or Le Monde)
- Facebook
- Medical testing
- App Store / Google Play
- Youtube
- Advertising
- Netflix, last.fm, Spotify, Pandora, ...
- Browser (URL recommendations)
- Search

## Client Value Proposition

- Find opportunities
- Reduce choice
- Explore options
- Discover long tails
- Recreation

# **Provider Value Proposition**

- Offer a unique or additional service (beyond competitors)
- Customer trust and loyalty
- Increase sales, CTR, conversions
- Better understand customers

## Recommendation

Content-based filtering (filtrage basée sur le continu)	More things similar to what I like
Collaborative filtering (filtrage collaboratif)	More of what other peo- ple who like what I like like
Knowledge-based filtering (filtrage basée sur connaissance)	More of what I need.

## Content-based filtering

### More things similar to what I like

Pro

```
yes! No need for community yes! Possible to compare items
```

#### Con

```
no Understand content
```

- yes Cold start problem
  - no Serendipity

## Collaborative filtering

### More of what other people who like what I like like

Pro

```
yes! No need to understand content
```

yes! Serendipity

yes! Learn market

#### Con

```
no User feedback
```

yes Cold start problem (users)

yes Cold start problem (items)

# Knowledge-based filtering

#### More of what I need

Pro

yes! Deterministic

yes! Certainty

no! Cold start problem

yes! Market knowledge

#### Con

yes Studies to bootstrap

yes Static model, doesn't learn from trends

- Users (utilisateurs)
- Items (objets)

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- Items (objets)

The goal is to fill in the blanks.

Example: books sales at Amazon.

But thousands or millions of columns and rows.

- Users (utilisateurs)
- Items (objets)

The goal is to fill in the blanks.

Example: film advice at Netflix.

But thousands or millions of columns and rows.

How do we make the matrix?

- Ask users
- Observe users

That's usually expensive...

### Examples:

- Films  $\Rightarrow$  ?
- Books  $\Rightarrow$  ?
- News  $\Rightarrow$  ?
- Images ⇒ ?

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- News  $\Rightarrow$  ?
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#### Films:

Content: acters, directors, year (decade, etc.), length

Collaborative: seen, opinion (1–5), when seen relative to release

### Examples:

- Films  $\Rightarrow$  ?
- Books  $\Rightarrow$  ?
- News  $\Rightarrow$  ?
- Images ⇒ ?

#### Books:

Content: authers, genre, year (decade, etc.), number of pages, content (very difficult)

Collaborative: read, opinion (1-5), how read

### Examples:

- Films  $\Rightarrow$  ?
- Books  $\Rightarrow$  ?
- News  $\Rightarrow$  ?
- Images ⇒ ?

#### News:

Content: source, section, TF-IDF word vectors

Collaborative:

### Examples:

- Films  $\Rightarrow$  ?
- Books  $\Rightarrow$  ?
- News  $\Rightarrow$  ?
- Images ⇒ ?

### Images:

Content:

Collaborative:

### Examples:

- Films  $\Rightarrow$  ?
- Books  $\Rightarrow$  ?
- News ⇒ ?
- Images ⇒ ?

Also: user profile, user behavior

## **Mathematics**

Vectors

Similarity

# Similarity: Jaccard Index

or: Indice de Jaccard, Jaccard similarity coefficient

Similarity:

$$J(A,B) = \frac{|A \cap B|}{|A \cup B|}$$

# Similarity: Jaccard Index

Similarity:

$$J(A,B) = \frac{|A \cap B|}{|A \cup B|}$$

Distance:

$$J_{\delta}(A,B)=1-J(A,B)$$

or: mesure cosinus, Similarité cosinus

Similarity:

$$\cos\theta = \frac{A \cdot B}{\parallel A \parallel \parallel B \parallel}$$

Similarity:

$$S_C(A, B) = \frac{A \cdot B}{\parallel A \parallel \parallel B \parallel}$$

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We only consider non-empty components.

- Vectors of word frequencies
- Frequency ⇒ significance

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- Frequency ⇒ significance
- Term Frequency Inverse Document Frequency

$$TF_{ij} = \frac{f_{ij}}{\max_k f_{kj}}$$
  $IDF_l = \log_2\left(\frac{N}{n_i}\right)$   $TF\text{-}IDF_{ij} = TF_{ij} \cdot IDF_i$ 

#### with:

 $f_{ii}$  = frequency of word i in document j

*N* = number of documents

 $n_i$  = number of documents in which we find word i

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IDF is a mesure of how much information a word carries

TF-IDF tells us which words best characterise a document Variation: boolean, log, stop word filtering

## **Content-Based Filtering**

More things similar to what I like

# **Content-Based Filtering**

	<i>I</i> <sub>1</sub>	$I_2$	$I_3$	$I_4$	<i>I</i> <sub>5</sub>	
$U_1$	3					
$U_2$			5	1	4	
$U_3$		2		5	1	

More things similar to what I like

Then, we can cluster (regroupement, partitionnement de données), etc.

# Content-Based Filtering

### Based on item profiles

- More stable (in principle)
- O(n²) (but often less, items often aren't categorised together)
- Can reduce to threshold
- Can pre-calculate, queries become faster

# Collaborative Filtering

More of what other people who like what I like like

# Collaborative Filtering

User profile

# Collaborative Filtering

Item profile

#### **Utility Matrix Symmetry**

- Propose items based on users
- Proposer users based on items

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- Proposer users based on items

But remember: 2 items being similar  $\neq$  2 users similar.

# **Utility Matrix Symmetry**

- · Propose items based on users
- Proposer users based on items

To estimate  $m_{u,i}$ ,

- Find k users like U<sub>u</sub>
- Find k items like I<sub>i</sub>

- Find k users like  $U_u$ , take  $\frac{1}{k} \sum_{i=1}^k m_{u_i,i}$
- Find k items like  $I_i$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u,i_j}$

- Find k users like  $U_u$ , take  $\frac{1}{k} \sum_{i=1}^k m_{u_i,i}$
- Find k items like  $I_i$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u,i_j}$

We have to compute the entire line (or the part which is likely to be important)

- Find k users like  $U_u$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u_j,i}$
- Find k items like  $I_i$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u,i_j}$

Once we've computed  $U_u$ , the other k users lets us take a shortcut.

- Find k users like  $U_u$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u_j,i}$
- Find k items like  $I_i$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u,i_j}$

For  $I_i$ , we have to compute most of the  $I_j$  before we can fill in a single line. But item-item filters are often more reliable.

- Find k users like  $U_u$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u_j,i}$
- Find k items like  $I_i$ , take  $\frac{1}{k} \sum_{j=1}^k m_{u,i_j}$

In any case, we can mostly precompute in advance.

#### **Utility Matrix**

The matrix is sparse.

⇒ clustering ⇒ reduced matrix

# **Utility Matrix**

The matrix is sparse.

⇒ clustering ⇒ reduced matrix

Estimate on the reduced matrix, then take items and users as representative for the cluster.

Observations:

Clustering is expensive, reduces quality

Observations:

Dimension reduction reduces quality

Observations:

Users interact with very few items

Observations:

Rapid response desirable

#### Scales independent of the number of users or of items

- Online
- Offline

G. Linden, B. Smith, J. York, *Amazon.com Recommendations: Item-to-Item Collaborative Filtering*, Internet Computing (7, 1), 22 Jan 2003.

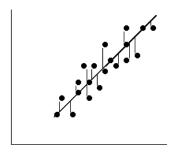
```
Offline (Precomputation)
for each item I<sub>1</sub> to sell do
    for each user C who has purchased I<sub>1</sub> do
        for each item I2 bought by C do
        (I_1, I_2)++
        end
    end
    for each item l<sub>2</sub> do
      S_{l_1,l_2} \leftarrow S(l_1,l_2)
    end
end
```

#### Slope One

Linear regression on user opinions

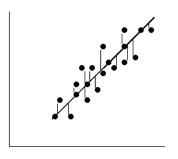
Daniel Lemire and Anna Maclachlan, *Slope One Predictors for Online Rating-Based Collaborative Filtering*, Proceedings of SIAM Data Mining (SDM) 2005.

# Slope One: Regression



http://www.upa.pdx.edu/IOA/newsom/pa551/Image255.gif

# Slope One: Regression



$$\min \sum (y_i - (ax_i + b))^2$$

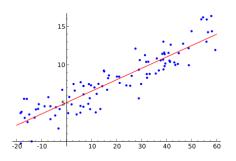
http://www.upa.pdx.edu/IOA/newsom/pa551/Image255.gif

#### Slope One: algorithm

```
Offline : for chaque I_i, I_j do  \mid \mathcal{U} \leftarrow \{ \text{users who have expressed an opinion on } I_i, I_j \}   | \text{dev}_{i,j} \leftarrow \frac{1}{\|\mathcal{U}\|} \sum_{u \in \mathcal{U}} (r_u(i) - r_u(j))  end
```

Online (for 
$$u$$
): 
$$\mathcal{V} \leftarrow \{j \mid u \text{ has expressed an opinion on } I_j\}$$
 
$$r_u(i) \leftarrow \frac{1}{\|\mathcal{V}\|} \sum_{u \in \mathcal{V}} (\text{dev}_{i,j} - r_u(j))$$

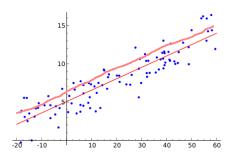
# Slope One: Regression



"Linear regression" by Sewaqu - Own work. Licensed under Public domain via Wikimedia Commons -

http://commons.wikimedia.org/wiki/File:Linear\_
regression.svg#mediaviewer/File:Linear\_regression.svg

## Slope One: Regression



SVD, typically 
$$k = 20 \dots 100$$

$$M = U\Sigma V^*$$

SVD, typically 
$$k = 20...100$$

$$(a_1 \quad \cdots \quad a_m) \begin{pmatrix} b_1 \\ \vdots \\ b_n \end{pmatrix} = \text{scalar}$$

SVD, typically k = 20...100

$$\begin{pmatrix} a_1 \\ \vdots \\ a_m \end{pmatrix} \begin{pmatrix} b_1 & \cdots & b_n \end{pmatrix} = \begin{pmatrix} c_{1,1} & \cdots & c_{1,n} \\ \vdots & & \vdots \\ c_{m,1} & \cdots & c_{m,n} \end{pmatrix}$$

SVD, typically k = 20...100

$$\begin{pmatrix} a_{1,1} & a_{1,2} & a_{1,3} \\ \vdots & \vdots & \vdots \\ a_{m,1} & a_{m,2} & a_{m,3} \end{pmatrix} \begin{pmatrix} b_{1,1} & \cdots & b_{1,n} \\ b_{2,1} & \cdots & b_{2,n} \\ b_{3,1} & \cdots & b_{3,n} \end{pmatrix} = \begin{pmatrix} c_{1,1} & \cdots & c_{1,n} \\ \vdots & & \vdots \\ c_{m,1} & \cdots & c_{m,n} \end{pmatrix}$$

SVD, typically  $k = 20 \dots 100$ 

$$\begin{pmatrix} a_{1,1} & \cdots & a_{1,k} \\ \vdots & & \vdots \\ a_{m,1} & \cdots & a_{m,k} \end{pmatrix} \begin{pmatrix} c_{1,1} & \cdots & c_{1,n} \\ \vdots & & \vdots \\ c_{k,1} & \cdots & c_{k,n} \end{pmatrix} = \begin{pmatrix} c_{1,1} & \cdots & c_{1,n} \\ \vdots & & \vdots \\ c_{m,1} & \cdots & c_{m,n} \end{pmatrix}$$

#### Challenges

- How do we measure success?
- What are our features?

# Clustering

- kNN
- · Curse of Dimensionality
- Scalability

# Clustering

- kNN k-Nearest Neighbor
- Curse of Dimensionality
- Scalability 10<sup>7</sup> clients, 10<sup>6</sup> objets

#### Questions?

purple.com/talk-feedback