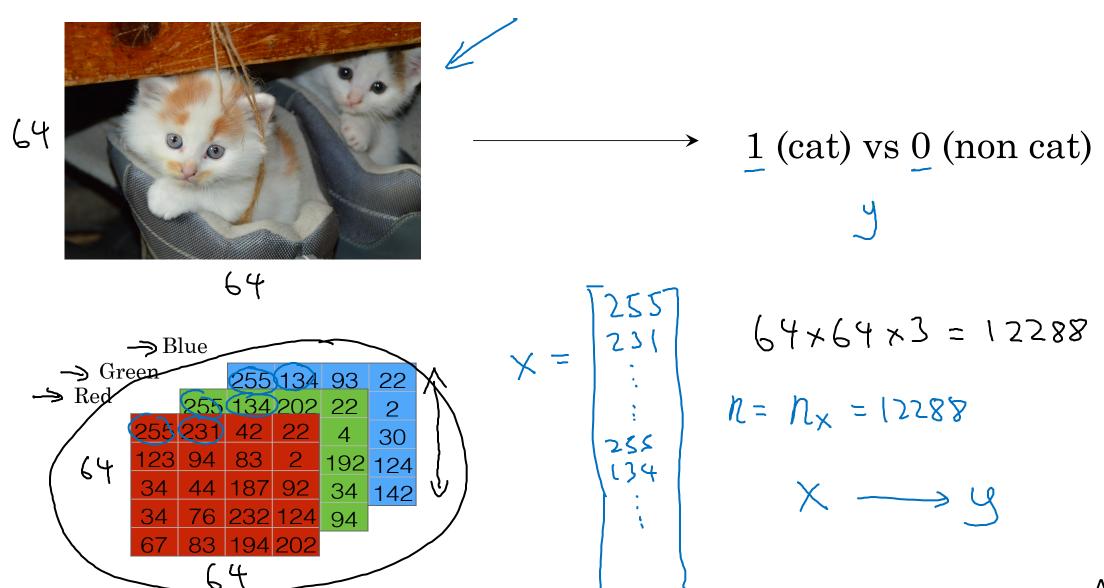


Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y) \times \in \mathbb{R}^{n_x}, y \in \{0,1\}$$

$$m + rainiy exceptes: \{(x^{(i)}, y^{(i)}), (x^{(i)}, y^{(ii)}), \dots, (x^{(m)}, y^{(m)})\}\}$$

$$M = M + rain$$

$$M + est = \# test exceptes.$$

$$Y = \begin{bmatrix} y^{(i)} & y^{(i)} & \dots & y^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(i)} & \dots & y^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(i)} & \dots & y^{(m)} \end{bmatrix}$$

$$Y \in \mathbb{R}^{n_x m}$$

$$X \in \mathbb{R}^{n_x m}$$

$$X \in \mathbb{R}^{n_x m}$$

$$X \in \mathbb{R}^{n_x m}$$



Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given
$$x$$
, want $\hat{y} = P(y=1|x)$
 $x \in \mathbb{R}^{n}x$
Pararters: $w \in \mathbb{R}^{n}x$, $b \in \mathbb{R}$.
Output $\hat{y} = \sigma(w^{T}x + b)$
Output $\hat{y} = \sigma(z)$

$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$\hat{Y} = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int_{\mathcal{A}} (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

The second second



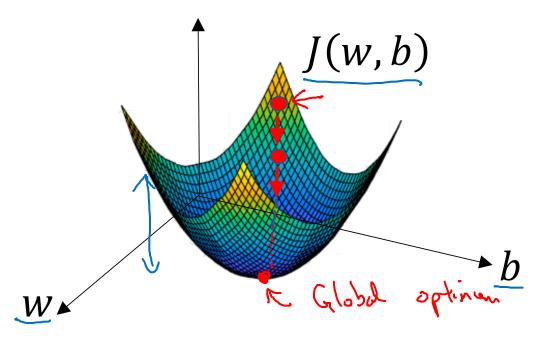
Basics of Neural Network Programming

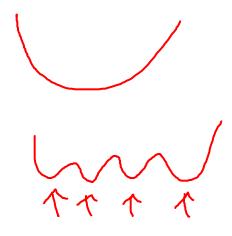
Gradient Descent

Gradient Descent

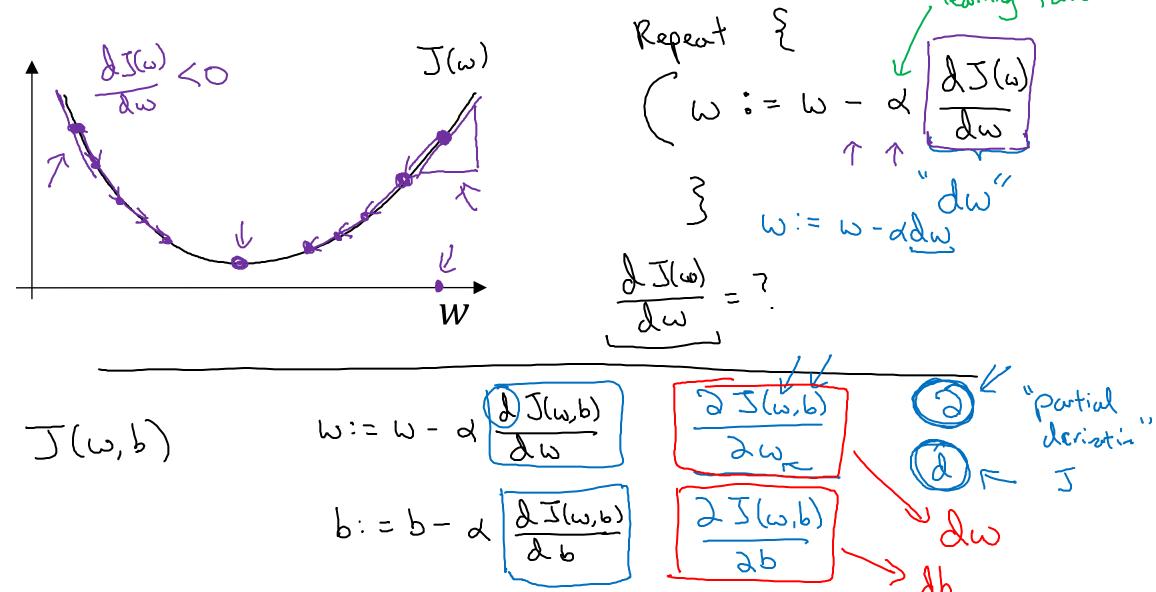
Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$ $\underbrace{J(w, b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$

Want to find w, b that minimize I(w, b)





Gradient Descent



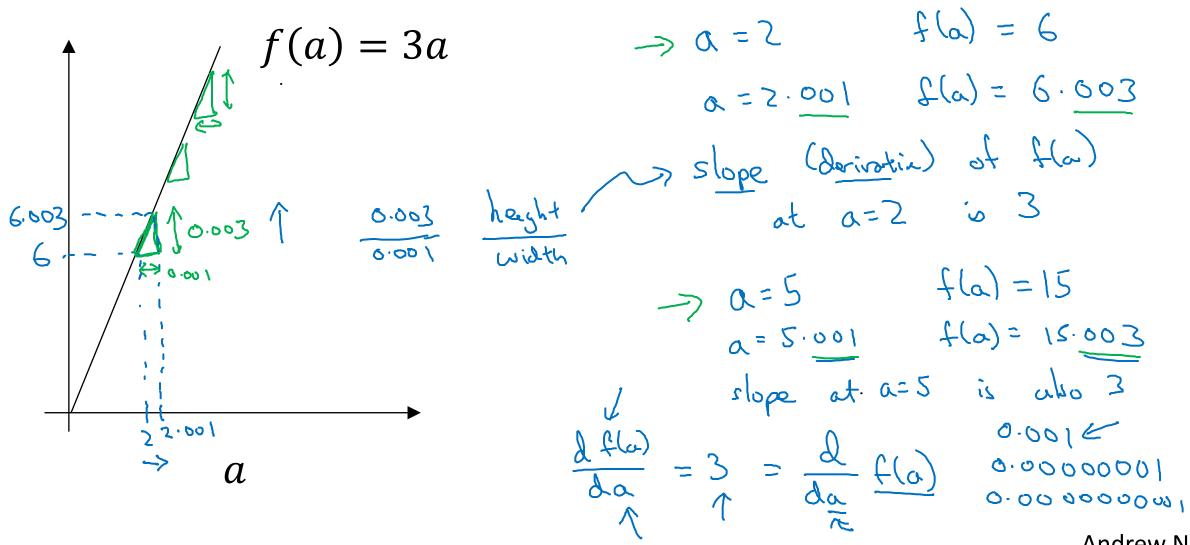
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Basics of Neural Network Programming

Derivatives

Intuition about derivatives



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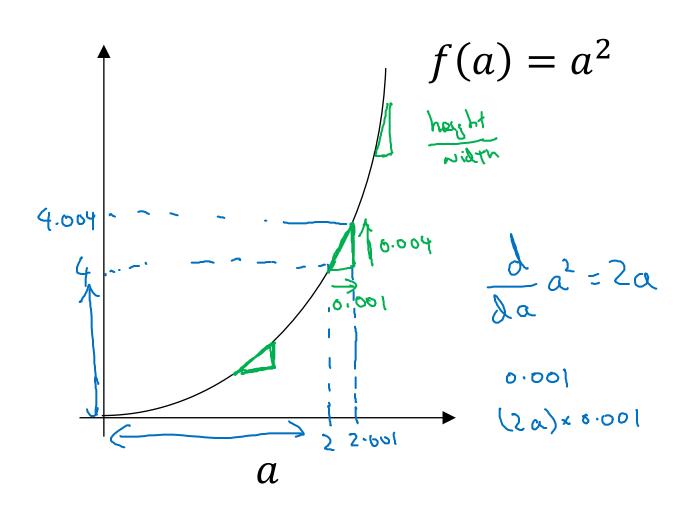


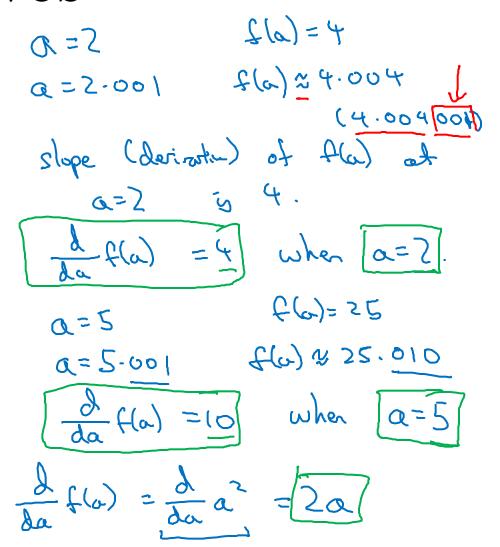
Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives







More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{d}{da}(a) = 3a^{2}$$
 $3x2^{3} = 12$

$$a = 2$$
 $f(a) = 4$
 $a = 2-001$ $f(a) = 4-004$

$$a = 5.001$$
 $f(a) = 8$
 $a = 5.001$ $f(a) = 8$

$$0.0002 < 0.0002$$

$$0.0002 < 0.0002$$

$$0.0002 < 0.0002$$



Basics of Neural Network Programming

Computation Graph

Computation Graph

$$J(a,b,c) = 3(a+bc) = 3(5+3x^2) = 33$$
 $U = bc$
 $V = atu$
 $J = 3v$
 $V = a+u$
 $J = 3v$
 $V = a+u$
 $J = 3v$

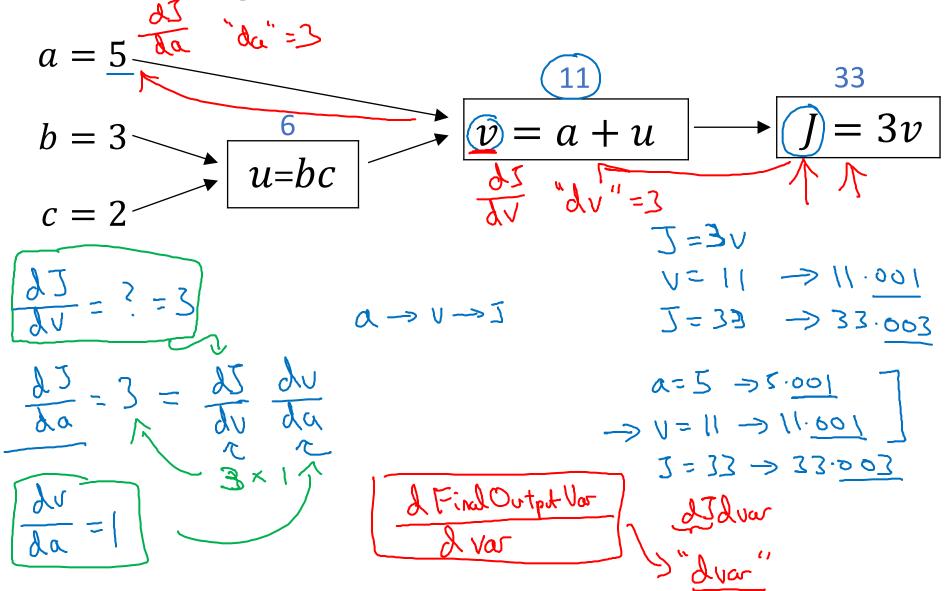


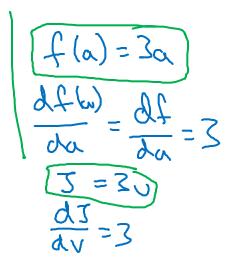
Basics of Neural Network Programming

Derivatives with a Computation Graph

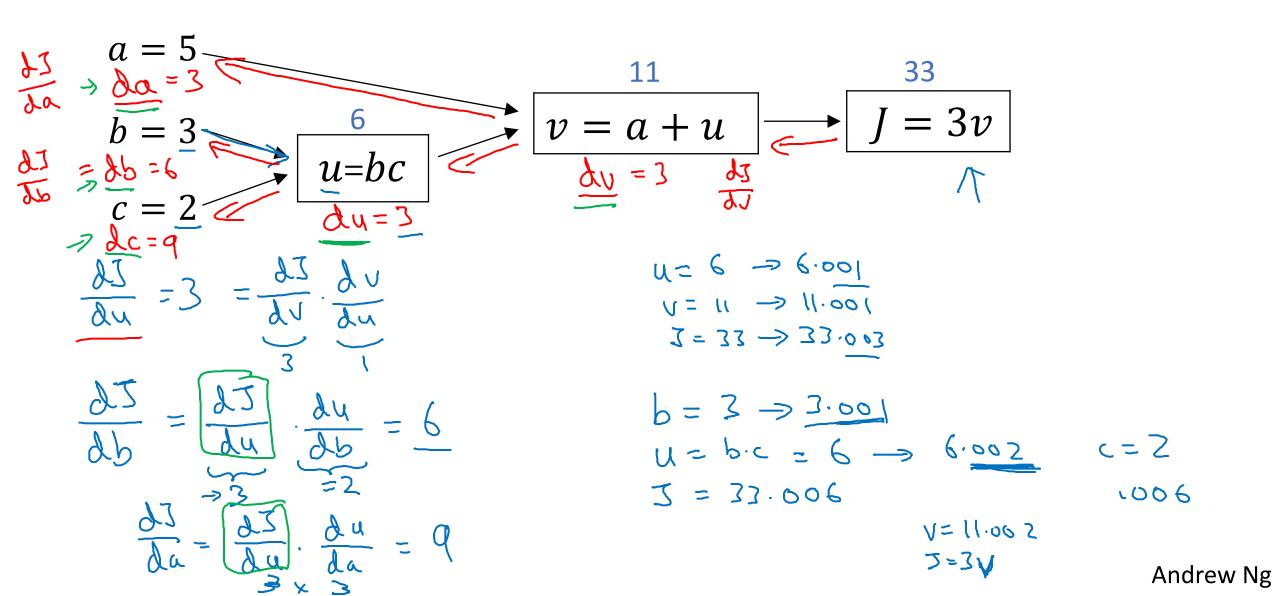
deeplearning.ai

Computing derivatives





Computing derivatives





Basics of Neural Network Programming

Logistic Regression Gradient descent

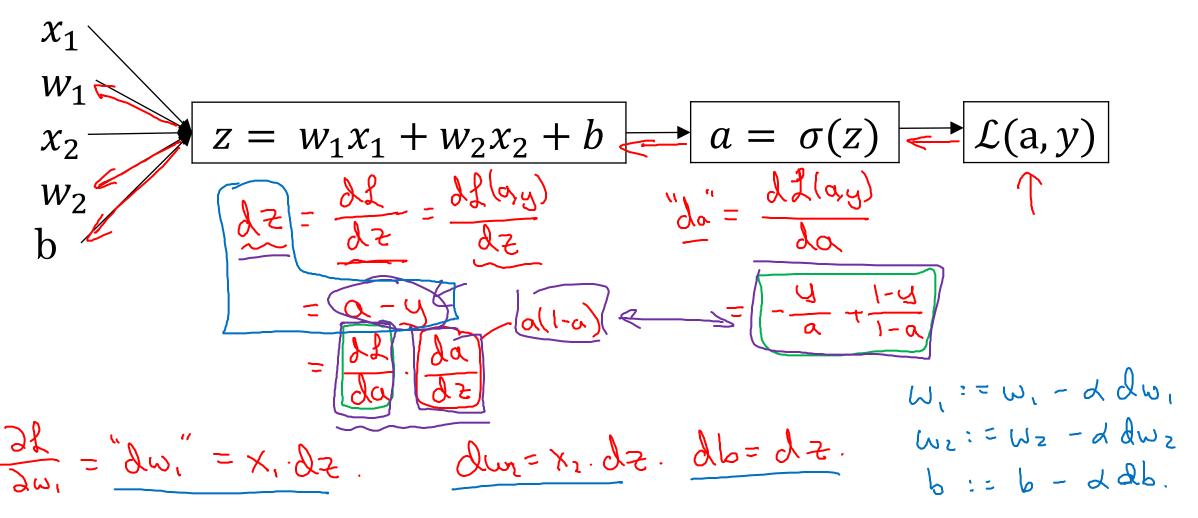
Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

Logistic regression derivatives





Basics of Neural Network Programming

Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0$$
; $d\omega_{1}=0$; $d\omega_{2}=0$; $db=0$
 $Z^{(i)}=\omega^{T}x^{(i)}+b$
 $Z^{$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - \alpha d\omega_2$
 $b := b - d db$

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