## THE TEAM, AND HOW TO RUN THE CODE

The Team: The Walking Zed

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Partner: None

By turning in this assignment, I do affirm that we did not copy any code, text, or data except CS-171 course material provided by the textbook, class website, or Teaching Staff.

#### **Programming Languages and Versions used:**

• C++, c++11

#### **Environment Setup Required to Run:**

- Compiled via MinGW 4.7.2 32-bit and Qt 5.5
- Delivered executable compiled on openlab with gcc 5.2.0, using commands:
  - –static-libstdc++
  - –static-libgcc
  - o -std=c++11

#### Implementation:

- Variable & Domain Variable is a combination of an array position and a domain. The Domain is a vector of possible character values.
- Puzzle Holds the puzzle and its attributes as a 2-dimensional array of variables (array locations, combined with a character face value and a domain of character values)
- Generator Generates a puzzle based on the attributes of m (number of cells preassigned), n (size of the puzzle), p (row size of blocks), and q (column size of blocks).
- Reader Reads and writes puzzles from and to files.
- Solver Solves a puzzle based on a variety of heuristic methods, each of which can be toggled on and off. It generates a log file after solving the puzzle.
- Book Keeper Stores assignments, removals, and search depth after every assignment.
- Logger Writes to an output file with various attributes from the solver.

### WHAT MY TEAM DID

I coded it.			I tested it thoroughly.			It ran reliably and correctly.			What was it?
Yes	Yes Partly No		Yes Partly No		Yes	- i			
Required Coding Project				•					
Х			Х			Х			Backtracking Search (BT)
Х			Х				Х		Forward Checking (FC)
X			Х				Х		Minimum Remaining Values (MRV)
Х				Х				Х	Degree Heuristic (DH)
X				Х				Х	Least Constraining Value (LCV)
Extr	a Credit								
X			Х			Х			Writing My Own Shell
х			х			х			Writing My Own Random Problem Generator
Х				Х				Х	Arc Consistency AC-3/ACP/MAC
		Х			х			х	Local Search Using Min-Conflicts Heuristic
		х			х		х		Advanced Techniques, Extra Effort, or Creativity Not Reflected Above*

<sup>\*</sup>Advanced Techniques, Extra Effort, or Creativity Not Reflected Above:

None.

## ANALYSIS OF BEST METHODS

## **COMBINATION**

FC	MRV	DH	LCV	(ACP)	(MAC)	(OTHER)	Average # Nodes	Average Time	Std. Dev. Time		
1	The blank row below is for the case of no heuristics and no constraint propagation.										
							161576.7	1.1	2.385372		
Х							161576.7	2.6	5.986652		
	Х						161576.7	2.5	5.69649		
		Х					574099.6	Timeout	Timeout		
			Х				161576.7	9.8	20.89402		
				(X)			161576.7	1.1	2.385372		
					(X)		1276.1	3.0	4.898979		
						(X)	N/A	N/A	N/A		
Х	Х	Х	Х				927705.4	71.3	115.8594		
Х	Х	Х	Х	Х	Х		1105.7	2.6	7.144228		
F	Fill in the blank row above with the combination you found to be fastest on PH1-5.										

Note: These tests were run on 10 randomly generated 9x9 sudoku puzzles with M = 17, as stated in the professor's email., with timeout at 600 seconds.

#### Did you get the results you expected? Why or why not?

As a result of a less than stellar implementation of the heuristics and propagation, these operations end up taking more time to work than it reduces in the backtracking search. As you can see the fastest one is the one without any heuristics or propagation, or the one with only arc consistency preprocessor. While the degree heuristic and the least constraining value heuristic increases the average solution time by a large amount, combining them with the other heuristics and propagations causes the time to drop to around 2.6 seconds, with a drastically lower average node count, 1105.7 nodes. These were more or less the results I expected, although I expected the ACP + MAC to be much lower, and that all 6 combined would result in a much larger time.

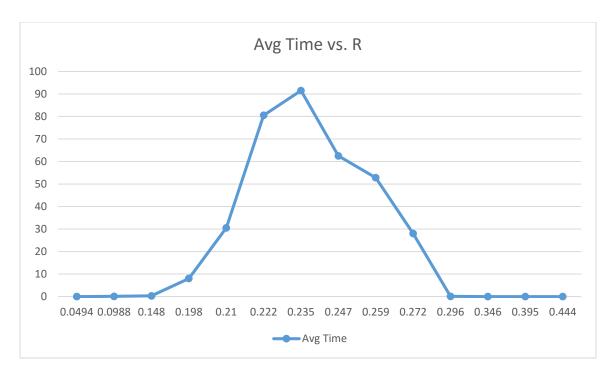
Did you implement any Advanced Techniques, Extra Effort, or Creativity not reflected above? If so, please tell us what you did.

No.

# ESTIMATION OF THE CRITICAL VALUE, HARDEST R

М	Ν	P	Q	$R = M/$ $N^2$	Average # Nodes	Average Time	Std. Dev. Time	# (%) Solvable
4	9	3	3	0.0494	329.8	0.0	0.0	100%
8	9	3	3	0.0988	4095.9	0.1	0.3	100%
12	9	3	3	0.148	45535.3	0.3	0.9	100%
16	9	3	3	0.198	1714470.0	8.0	18.60645	100%
17	9	3	3	0.210	6747953.0	30.5	90.17455	90%
18	9	3	3	0.222	13713488.0	80.5	124.9066	80%
19	9	3	3	0.235	16755347	91.5	137.1869	70%
20	9	3	3	0.247	9505533	62.5	103.7663	90%
21	9	3	3	0.259	8360421	52.8	92.8502	100%
22	9	3	3	0.272	4896441	28	57.89646	100%
24	9	3	3	0.296	4687.7	0.1	0.3	100%
28	9	3	3	0.346	10628.6	0	0	100%
32	9	3	3	0.395	611.8	0	0	100%
36	9	3	3	0.444	184.9	0	0	100%

Find the critical value of the "hardest R" for N=9 and your best combination above.



Based upon your results above, you estimate the "hardest  $R_9$ " = 0.235.

### How does puzzle solvability for your best combination vary with $R=M/N^2$ ?



Is the critical value for "hardest R" approximately the same as the value of R for which a random puzzle is solvable with probability 0.5?

From the sample population of the tests I have conducted, the "hardest R" value estimated from the first graph coincides with the critical point in this graph, 0.7. It is not the same value of R for a probability of 0.5 (as there is none from my sample), but it is as close as it can get to it.

# LARGEST N COMPLETABLE AT THE HARDEST R

"Hardest M" round ( $N^2  imes R_9$ )	N	Р	Q	# (%) Completed in 5 Minutes or Less	AVERAGE # NODES (Completed puzzles only)	AVERAGE TIME (Completed puzzles only)	STD.DEV. TIME (Completed puzzles only)
34	12	3	4	70%	318225.6	2.428571	4.494895
53	15	3	5	40%	10606751	112	115.0326
60	16	4	4	10%	703576	9	None
76	18	3	6	20%	2940854	40.5	39.5
94	20	4	5	0%	0	0	None
104	21	3	7	20%	18148210	51.5	0.5
135	24	4	6	0%	0	0	None
171	27	3	9	0%	0	0	None
184	28	4	7	0%	0	0	None
212	30	5	6	0%	0	0	None
241	32	4	8	0%	0	0	None
288	35	5	7	0%	0	0	None

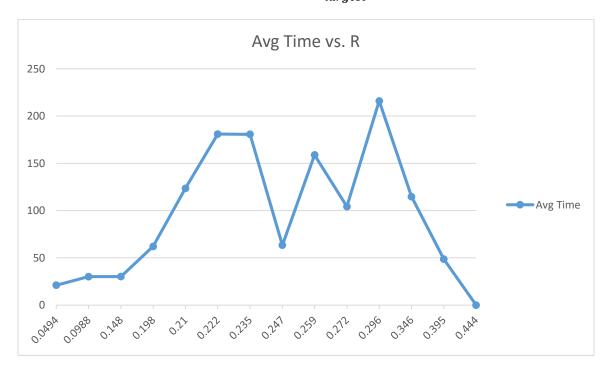
Based on the table above, the "Largest N" is 12, as it had the same probability of completion (70%) with the same R as 9.

# IS HARDEST R CONSTANT AS THE SUDOKU PUZZLES SCALE?

N.4	N	D		$R = M/N^2$	AVERAGE #	AVERAGE	STD.DEV.	# (%)
IVI	M N P	Q	$\mathbf{K} = \mathbf{M}/\mathbf{N}$	NODES	TIME	TIME	SOLVABLE	
7	12	3	4	0.0494	2357400	21.1	58.44493	100%
14	12	3	4	0.0988	3403260	30.1	124.1055	90%
21	12	3	4	0.148	6403874	30.2	90.23425	90%
29	12	3	4	0.198	6578884	62.1	150.0642	80%
30	12	3	4	0.210	12843255	123.6	144.9581	60%

32	12	3	4	0.222	19227834	181	146.9714	40%
34	12	3	4	0.235	19788930	180.7	141.1602	40%
36	12	3	4	0.247	5790776	63.4	93.81258	80%
37	12	3	4	0.259	16523606	158.9	138.9141	50%
39	12	3	4	0.272	12112925	104.3	139.2179	70%
43	12	3	4	0.296	28076684	216	117.978	40%
50	12	3	4	0.346	11959403	114.8	138.8156	80%
57	12	3	4	0.395	5670697	48.7	53.48878	90%
64	12	3	4	0.444	3314.8	0	0	100%

### Find the critical value of the "hardest R" for $N_{largest}$



Based upon your results above, you estimate the "hardest  $R_{N_{largest}}$ " = 0.296

How does puzzle solvability for your best combination vary with  $R=M/N^2$ ?



Is the critical value for "hardest R" approximately the same as the value of R for which a random puzzle is solvable with probability 0.5?

The hardest R has around solvability probability of 0.4. The R values for which the solvability probability is around 0.5 would be around 0.259.

Is hardest  $R_{N_{largest}} \approx$  "hardest  $R_9$ "? Why or why not? How is the hardest R related to the board parameter N? What is the shape of the function R(N), which gives you the hardest ratio for  $9, 12, 15, 16, 18, 20, \dots, 35$ ?

The hardest  $R_{Nlargest}=0.296$  is not approximately the hardest  $R_9=0.235$ . However, based on the tests, 0.296 and 0.235 had the same solvability probability at 0.4. 0.296 had a slightly higher average time, which is why this value is considered to be the hardest R for the largest N, N=12. As the puzzles scale, the number of cells, assignments, and backtracks increases. Thus, larger puzzles will take longer to complete, leading to higher average times and more chances of timeout. Based on these tests, the hardest R increases as R increases although more tests at different R and hardest R are required for a more accurate relationship.