

course\_content



# Data Structures and Algorithms



## Traversals & Binary Search Trees

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# Week 9

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W9: BSTs and Heaps

W10: Graphs

W11: Greedy Algorithms

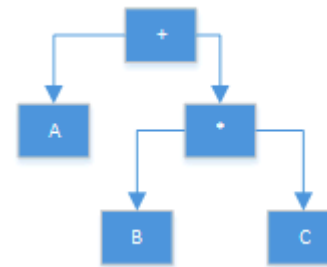
# Trees - Traversals (Self-learning)

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- There are many different traversal methods:
  - Depth-First Search (Mostly Binary Trees)
    - Pre-order traversal
    - In-order traversal
    - Post-order traversal
  - Breadth-First Search (All Graphs)
- What do they mean? How do they work?
- Can you write the method recursively?
- Can you write the method iteratively?

# Traversal Applications

- In-order Traversals: Binary Search Trees (see next slides)
- Pre-order Traversal: duplicating a tree (have to do parents first)
- Post-order Traversal: deleting trees, expression trees (compiling calculations)
- E.g. In the expression tree, you calculate children first
- Same if you have tasks dependent on other tasks
- Breadth-first: Shortest Path Algorithms! Facebook Friend!



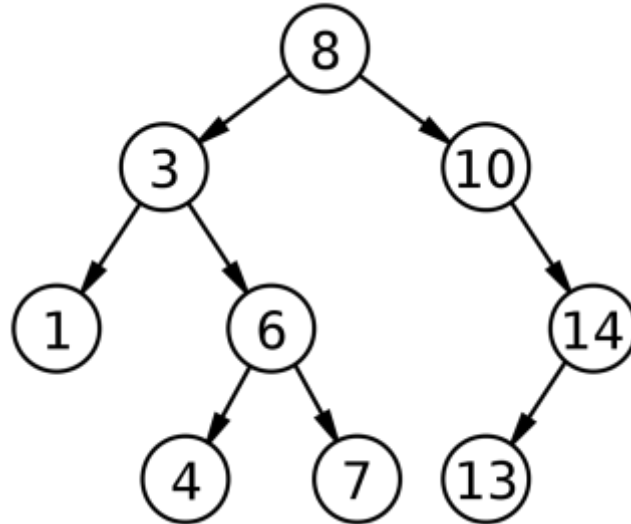
# Trees - Binary Search Tree

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- We previously looked at sorted arrays and found that maintaining them was hard
- A binary search tree can be a better way of doing this
- Values are inserted into their correct position. Smaller than root means left sub-tree, larger than root means right sub-tree.
- Construct a BST (binary search tree) with the following 5,10,7,8,1,3,6.
- What are the runtimes of the following in a BST? (self-learning)
  - Insert, Search, Delete, Create (with a list of given values)
- An in-order traversal of a BST produces a sorted list.

# Trees - Binary Search Tree

Binary search tree conducted from list: 8,3,6,10,1,14,7,4,13



Try with the order 1,14,13,3,4,10,8,6,7. How many levels does this have? Too many!

# Trees - AVL Tree

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- To minimise the height of a BST, we use an 'AVL Tree'

$$\text{balanceFactor} = \text{height}(\text{leftSubTree}) - \text{height}(\text{rightSubTree})$$

- An AVL Tree has balanceFactor 1, 0 or -1 (for all roots)
- This forces it to be *balanced*
- Once the balance factor leaves this range, it has a procedure to fix it.
- This is a fairly involved procedure that you can read about but it involves a 'rotation' of your tree by changing the root and one of the branches. (optional self-learning)

# Using BST/AVL trees as ordered maps

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- Back in Week 3, we discussed maps and how they can be implemented as associative lists or hash tables. We can also implement them as BSTs (or AVLs)
- How does it work?
  - Decide on an ordering of your keys. (small to large, alphabetical etc)
  - Store as a BST(AVL) based on the order of the keys.
  - At each node, store an extra parameter which is the value.
- Searching, Accessing, Inserting and Deleting are all  $O(\log n)$  time now.
- Not as good as hash tables but no need to worry about collisions.
- Easier to extract all keys here.

# Videos

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- [Breadth-First vs Depth-First Search](#) using Queues & Stacks
- [Pre-order, In-order, Post-order traversals](#) (Binary Trees)
- [Binary Search Tree & AVL Tree](#) (Also great for how to represent binary tree as array and how to rotate AVL trees to make them balanced)



Time:  
10 min

# Quiz Time

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[bit.ly/DSA1920Quiz8](https://bit.ly/DSA1920Quiz8)

Deadline: Monday 30th March (midnight)

Time:  
1 min

**Questions?....Office Hours!**