

[course_content](#)



Data Structures and Algorithms



Sorting Review & Intro Trees

Week 8

top

W8: Trees

W9: Heaps

W10: Graphs

W11: Greedy Algorithms

Quiz Time

Time:
5 min

bit.ly/DSA1920Quiz7

Sorting Review - Stability

- Stable Sorts - two identical elements maintain their existing order
- We want stable sorts when there are multiple properties to sort on
- Any algorithm that **swaps elements that are not near each other** can **break stability** e.g. Selection Sort, Shell Sort, Heap Sort, Quick Sort
- Any sorting algorithm can be made to be stable with $O(n)$ space by including the current position in the comparison (when comparing two equal elements)

Time:
5 min

Sorting Review

Algorithm	Time-Best	Time-Avg	Time-Worst	Aux Space	In-place	Stable
Bubble	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$	Yes	Yes
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$	$O(1)$	Yes	No
Insertion	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$	Yes	Yes
Shell	$O(n \log n)$	$O(n \log n)$	$O(n^2)$	$O(1)$	Yes	No
Merge	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n)$	No	Yes
Quick	$O(n)$	$O(n \log n)$	$O(n^2)$	$O(\log n)$	Yes/No	No
Heap	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(1)$	Yes	No

MidTerm Review

- What is the worst-case runtime for searching a sorted array?
- What is the worst-case runtime for deleting a node from a doubly-linked list?
- What is the worst-case runtime for accessing a hash table? (no collisions)
- Definition of 'x and y' and 'x or y' in Python.
- Mutable types in Python
- Number of Operations → Time Complexity

Trees

- A tree is a **non-linear** data structure
- It has a **root**, **branches** and **leaves**
- The **root** (only one) is at the **top**, branches come down with leaves at the bottom
- Each item in a tree is called a **node**
- Examples: Animal Kingdom Hierarchy, Family Tree, File System, XML/HTML data, Heaps, compilers (for managing syntax),

Trees

- What do the following mean in the context of trees?
 - Node, Edge, Root, Path, Children, Parent
 - Sibling, Subtree, Leaf Node, Level, Height
- You can think of a tree in 2 ways:
 - A root + one-way edges coming out of each node to new nodes such that there are no 'cycles' ---- the intuitive understanding
 - A tree is either empty or a root connecting to zero or more subtrees (which are also trees) ----- the recursive definition

Trees

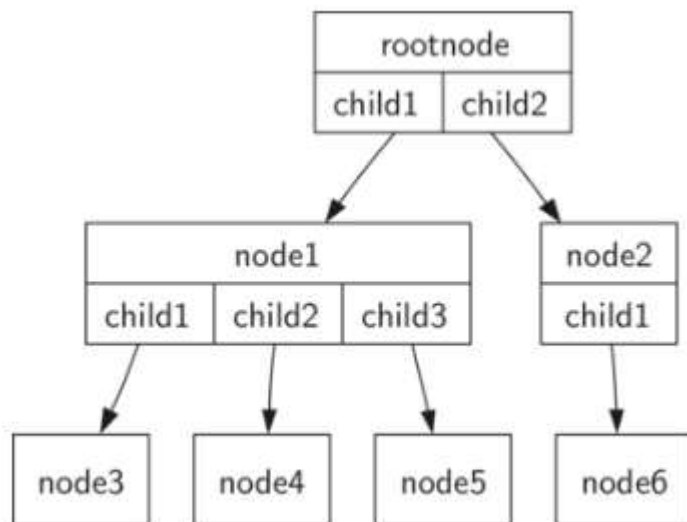


Figure 3: A Tree Consisting of a Set of Nodes and Edges

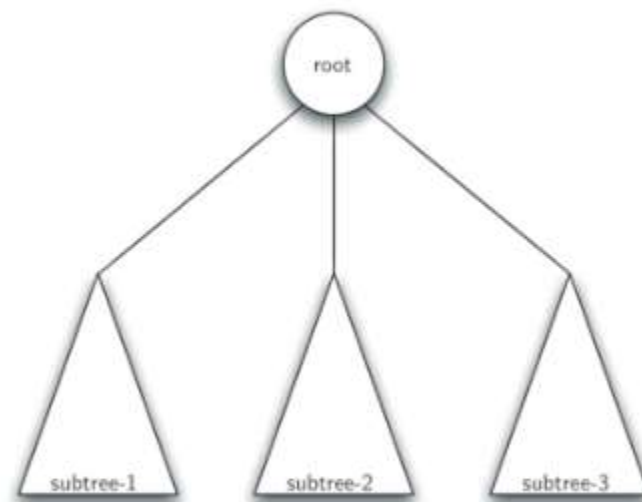


Figure 4: A recursive Definition of a tree

Trees - Implementation

- 2 main ways of implementing Trees
 - List of Lists
 - E.g. [3,[1],[2,[1],[3]]]
 - Node and list of children
 - Think of Linked Lists but instead of just one next node, you have a list of children nodes
- Binary Trees have at most 2 children - left Node and right Node (can be Empty)

Trees - Traversals

- There are many different traversal methods:
 - Depth-First Search (method)
 - Pre-order traversal
 - In-order traversal
 - Post-order traversal
 - Breadth-First Search (method)
- What do they mean? How do they work?

Time:
1 min

Questions?