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# Data Structures and Algorithms

## Arrays and Hash Tables

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# Week 3

# Class Quiz!

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Time:  
5 min

[bit.ly/DSA1920Quiz](https://bit.ly/DSA1920Quiz)  
3

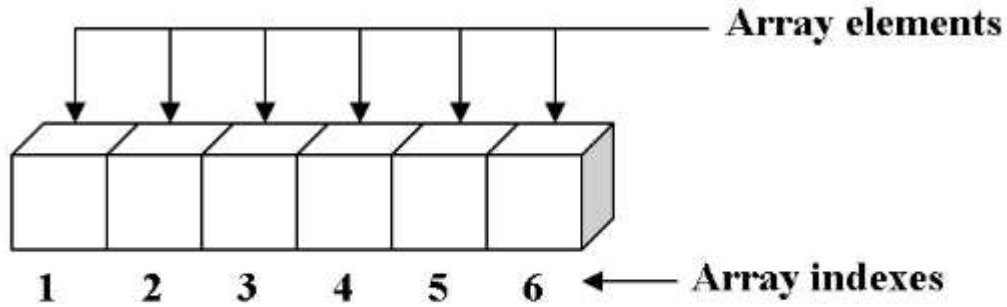
Bonus qn at the end to help you make  
up for other questions or missed  
quizzes..

# Arrays

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- Arrays are an **Abstract Data Type(ADT)**
- They hold a collection of data
- Each element can be accessed by its index
- The two primary operations in arrays are:
  - Store value in a specific index - *set(val,index)*
  - Retrieve value at a specific index - *get(index)*

# Arrays - Visualisation



**One-dimensional array with six elements**

Source: [Lucas Magnum Medium](#)

# Arrays - Exercise

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- Groups of 3 - discuss the following
- What are the more advanced operations we can do on arrays starting from just set and get?
- Write the pseudocode for those using the basic operations
- This should be independent of the programming language that you use
- You can use operations on atomic data types

# Arrays - Extra Operations

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- **Traversing** - as we can access each element, we can traverse the array
- **Searching** - as we can traverse the array, we can look for a specific element
- **Sorting** - if we have defined a definition of  $>$ , we can traverse through the elements and re-order our elements to produce a sorted array (assuming 1D)
- **Size** - we can know the number of elements in the array by checking each index until we can't access an element

# Arrays - Implementation Decisions

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- How many **dimensions**?
- Is it **fixed-size** or **dynamic-size**? (tuples vs lists)
- What **types** can we have within the array?
- Are the elements **mutable**?
- How much time does **set** and **get** take?
- Are operations between arrays **vectorized**? (not in Python, super fast if you can!)
- Find a comparison of [implementations](#) here

# Arrays - Implementation

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- In simple implementations, it is enough to simply store the memory address of the first index of the list.
- Some also store the size to prevent overflowing into another piece of allocated memory
- Accessing and setting the  $i$ 'th index is easy. You just take the first point in memory **M** and then multiply the number of bytes **B** per index by the index to get **M+iB** to get the location of the index you want to get/set. This causes the two basic operations to be  $O(1)$



# Arrays - Dynamic Arrays

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- Dynamic Arrays give you more operations
  - Adding - append to end or insert in the middle
  - Deleting - removing the last element or something in the middle
- Since only the memory address of the first item is stored, adding or deleting requires other elements to change memory location to continue to be able to set/get in  $O(1)$  time.
- Most dynamic arrays are implemented to have a fixed size (with some elements unused) and then doubling at a new memory space when necessary. This is because leaving room for infinite space is impossible.

# Associative Arrays

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- Associative Arrays are an **Abstract Data Type(ADT)**
- Often called **map**, **symbol table** or **dictionary**
- They store **key-value** pairs (with unique keys)
- The primary operations in associative arrays are:
  - Addition of a key-value pair - *add(key,value)*
  - Removal of a key-value pair - *remove(key)*
  - Modification of an existing key-value pair - *modify(key,newvalue)*
  - Lookup of a value - *lookup(key)*

# Associative Arrays - Exercise

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- Groups of 3 - discuss the following
- What are the more advanced operations we can do on associative arrays starting from just add, remove, modify and lookup?
- Write the pseudocode for those operations using the basic ones
- This should be independent of the programming language that you use
- You can use operations on atomic data types

# Associative Arrays - Extra Operations

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- **Searching** through keys is easy using lookup
- It is very difficult to do anything else without a **full set of keys!**
- Most implementations will allow you to find what available keys are!
- **Traverse, Searching** values, **Sizing** are now possible with the list of keys
- **Subsetting** or **duplicating** are also possible with the list of keys
- E.g. Finding all keys that have a certain value or counting the number of each value

# Associative Arrays - Implementation

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- 3 Primary ways to implement these
  - Association List (alist) - lists where each element contains a key-value pair
  - Binary Search Tree - a tree where the keys are sorted through the tree's relations
  - Hash Table - a hash function that computes an index for each key which looks up the desired value (**We will look at this on Thursday**)
- You should decide allowable **data types**

# Associative Arrays - Comparison

Underlying data structure	Lookup		Insertion		Deletion		Ordered
	average	worst case	average	worst case	average	worst case	
Hash table	$O(1)$	$O(n)$	$O(1)$	$O(n)$	$O(1)$	$O(n)$	No
Self-balancing binary search tree	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$	$O(\log n)$	Yes
unbalanced binary search tree	$O(\log n)$	$O(n)$	$O(\log n)$	$O(n)$	$O(\log n)$	$O(n)$	Yes
Sequential container of key-value pairs (e.g. association list)	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	No

Source: [Wikipedia - Associative Array](#)

# Ranges

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- Ways of specifying arithmetic sequences over integers
  - `range(n)` - (1,2,3,.....n-1)
  - `range(a,b)` - (a,a+1,a+2,.....b-1)
  - `range(a,b,k)` - (a,a+k, a+2k, a+3k, a+4k, .....b-1) (Note: k can be negative)
- Very useful for looping as it is **significantly faster** than for loops and while loops. Doesn't have to create, delete and iterate variables as often.
- There is just one range object and you iterate through it until you've reached the max level.
- You can concatenate ranges and access elements individual elements.

# Iterator

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- Lists, Sets, Tuples, Tuples, Dictionaries, Strings and Range Objects are all iterables - you can convert them to iterators.
- `Iter()` will convert an iterable to an iterator
- You loop through an iterator using the `next()` function
- For-loops do this implicitly. They convert an iterable into an iterator type and then loop through them using the `next()` function.
- While loops are different - there is no clearly defined start and end point.



# One-line Iteration

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- `[x+2 for x in [1,2,3]]` - create list using one line for loop
- `[x + 2 if x%2==1 else 0 for x in range(10)]` - if else statement within for loop
- `{x+3 for x in (1,2,3)}` - create set instead from tuple
- `tuple(x +3 for x in {1,2,3})` - create tuple from set
- `print(key,value) for key,value in myDict.items()` - using key,value in dictionary
- Module **itertools** is very good for more advanced iteration

Time:  
1 min

# Questions

# Next Steps

1. Week 3 Readings
2. Week 2 Implementations