# Function Words in Authorship Attribution Studies

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#### **Abstract**

The search for a reliable expression to measure an author's lexical richness has constituted many statisticians' holy grail over the last decades in their attempt to solve some controversial authorship attributions. The greatest effort has been devoted to find a formula grounded on the computation of tokens, word-types, most-frequent-word(s), hapax legomena, hapax dislegomena, etc., such that it would characterize a text successfully, independent of its length. In this line, Yule's K and Zipf's Z seem to be generally accepted by scholars as reliable measures of lexical repetition and lexical richness by computing content and function words altogether. Given the latter's higher frequency, they prove to be more reliable identifiers when isolatedly computed in p.c.a. and Delta-based attribution studies, and their rate to the former also measures the functional density of a text. In this paper, we aim to show that each constant serves to measure a specific feature and, as such, they are thought to complement one another since a supposedly rich text (in terms of its lemmas) does necessarily have to characterize by its low functional density, and vice versa. For this purpose, an annotated corpus of the West Saxon Gospels (WSG) and Apollonius of Tyre (AoT) has been used along with a huge raw corpus.

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#### 1 Introduction

The task of attributing the plausible authorship of a literary work resembles that of an art historian anxious to find even the least salient traces in the works of a plastic artist (either an architect, a sculptor, a painter, or a designer), insofar as the more the former knows about the latter, the more connections will undoubtedly lead him/her to relate work and author. The traditional methodology in authorship attribution employs differences and likenesses to ascertain the linguistic profile of the author behind the curtain. However, the issue is not

that straightforward in non-traditional approaches either, as these connections are often hard to validate.

Lexical richness may be accepted as a point of departure for identifying the stylistic idiosyncrasy of an author and, hence, for authorship attribution 'as they both (stylometrics and authorship attribution studies) share an interest in the size, coherence, and distribution of the vocabularies of texts and authors' (Hoover, 2003). Most stylometric studies are lexically based, especially because it is the level of language where repetitions may be reliably used as a basis for measurement (Holmes, 1994). In fact,

the language items of a work are assumed to entrap both conscious and unconscious aspects of the author's style; it would then be an asset to find the features of the unconscious aspect, since they cannot be consciously manipulated by the author (Laan, 1995).

The relevant literature reveals that divergent opinions can be attested as regards the numerous authorship attribution studies that, over the last years, have tried to obtain the most faithful statistical procedure, be the items morphological, syntactic, or lexical. In particular, the validity of some techniques employed in authorship attribution has been, to some extent, questioned with the argument that there is 'no consensus on results, nor there is consensus as to the accepted or correct methodology or technique', notwithstanding the persistent 'wish for a single method of analysis and a verifiable unique style' (Rudman, 1998). For the state of the art, we briefly review the contributions by Tweedy and Baayen, Somers and Tweedy, Burrows, and Hoover.

From a positive standpoint, Tweedie and Baayen (1998) consider that textual similarities between and within authors may become valid for authorship attribution, as they seem to validate the empirical trajectories of texts in the plane spanned by the dimensions of lexical richness and lexical repetition, providing thus a statistical technique for constructing confidence intervals around them. In relation to their experiment, Hoover (2003) points out that the success greatly depends on the variety of texts used (thematic and chronological), because the results would have been radically different, had the selection been also different. Actually, he is rather sceptical about the possibility of relying on a one-toone connectedness between lexical richness and authorship attribution and/or style description, on account of the following words: 'even though the measures of vocabulary richness may be effective in clustering texts by a same author, they cannot provide a consistent, reliable, or satisfactory means of identifying an author or describing a style' (Hoover, 2003), to conclude that 'the long-cherished goal of the measure of vocabulary richness that characterizes authors and their styles appears to be unattainable. The basic assumption that underlies it

is false'. Somers and Tweedie (2003) also distinguish a pastiche from the original by means of a discriminating study based on word usage and *lexical richness*. Lastly, Burrows's Delta (2002; 2003) performs rather successfully as the rate of unlikeness is reliable for relating English Restoration poems, both of known and unknown authors. The reliability and effectiveness of Burrows's *Delta* has been assessed by Hoover (2004a) who, in turn, tests successful modifications and alternatives to upgrade the model.

For opportunity, we refer to Miranda and Calle's multivariate word and lemma-based study (2005a) of the *West Saxon Gospels* (*WSG*), which was accomplished to rank them in terms of *lexical richness* measured by lemma-counting. The technique has proven reliable in Old English texts (a highly inflected language), as the same ordering of works by lemma-counting in the main study, namely Mt > Lk > Mk > Jn, is replicated in the partitioning and the contrastive studies carried out, and similar results are obtained by evaluating Zipf's Z or the expression  $HL^3/V(N)^2$ .

The present research aims to replicate the abovementioned ranking of the WSG by using function words (FW) in view of the consensus around their greater reliability in stylometric studies (Burrows, 2003) and their subsequent success for authorship attribution. Therefore, our hypothesis is grounded on the assumption that the particular distribution of FW may constitute the salient features which can identify an author's style and differentiate it from others. Three techniques are experimented to check this hypothesis, and each of them gives rise to each part of this article, besides the Introduction and the methodological procedure themselves. The first part deals with the computation of functional density, the second with the scoring of the most common function lemmas (FL), and the third with the Delta-scoring of the most common FW. To finish, some conclusions are drawn, especially to indicate whether each model (functional density, scoring of FL, and Delta-scoring of FW) yields the same ranking, or whether the types/tokens approach can be complemented or optimized with studies based on FL and/or FW.

# 2 Methodology

The field study comprises two different corpora as well as two handling techniques. The computation of functional density and the scoring of FL were done with the annotated corpus containing the WSG and the Old English Apollonius of Tyre (AoT) used in Miranda and Calle (2005a). The benefits derived from the annotation compensate for such a timeconsuming task, though it supposes 'the regrettable intrusion upon the data and avoids the interchange of information with colleagues' (Burrows, 2003), or even 'experimental corruption' (Rudman, 1998).<sup>2</sup> In the case of OE, unless you handle an annotated text, you cannot distinguish between (1) vowellength minimal pairs when no length marker is allocated, as ge versus ge, for versus for, etc; (2) homographs as ba which may be nominative/ accusative plural of all genders of {se, seo, bæt}, accusative singular feminine of {se, seo, bæt}, adverb of time, and/or conjunction of time.

The annotated corpus was then processed with the *Old English Concordancer* (henceforth *OEC*) (Miranda *et al.*, 2006), which retrieves morphosyntactic, lexical, and statistical information, both word- and lemma-based. Using this tool, all the sorting and counting operations were performed automatically, and the data were then downloaded onto Excel spread-sheets to accomplish the statistical study, and eventually plot the corresponding figures.

The study of FW, however, required a huger corpus for the sake of standardization, so a set of archives from the Toronto Complete Corpus of Old English Dictionary (Healey, 2000) was accordingly processed by means of WordSmith Tools 3.0 (Scott, 1996). Leaving aside the matter of size, which constitutes its main advantage, to cope with an untagged corpus of Old English (henceforth OE) is not free of intrusion either, in view of the fact that you cannot automatically compute the occurrences of allomorphs which are likely to be taken as different words owing to (1) the alternative employment of \(\dagger)\rangle, \(\delta\rangle\rangle, \delta\rangle, \delta\rangle, \delta\rangle, \delta\rangle, (bā), (Pā), (ðā), (obbe), (oPðe), (oðbe), (oðde), etc; (2) the existence of inter- and/or intradialectal variants, such as (angēan), (ongēan), (agēan), (hī), (hīe), (hig), (hỹ); and (3) the equivalence of (and), (ond), and the Tyronian nota, or of the forms (betweonan), (betweonon), (betweox), (betwix), (betwux), (betwyx).

To overcome these inconveniences, the results generated by *WordSmith Tools* required further replacement and grouping of the corresponding allomorphs. As in the annotated corpus, the data were also downloaded onto Excel spread-sheets for their statistical analysis.

# 3 Functional Density: the Ratio of Function Words to Content Words

The objective of this first study is to rank the WSG by the ratio FW to content words (CW), which requires to state what we understand by FW and CW in the context of OE: the set of the latter is assumed to comprise nouns, adjectives, verbs, and adverbs of manner (mostly derived with the suffix  $-(l\bar{\iota}c)e$ , such as  $s\bar{o}bl\bar{\iota}ce$ , witodl $\bar{\iota}ce$ , etc.), whereas the set of the former is assumed to comprise the rest (pronouns, prepositions, conjunctions, interjections, and other-than-manner adverbs). Although the line distributing adverbs into one set or another looks blurred, our proposal seems the most plausible insofar as only adverbs of manner ending in  $-(l\bar{\iota}c)e$  share their stems with CW and as such they must be considered to belong to the same open set.3 To help understand the scope of the ratio FW/CW, let us compare it with other common related expressions, namely: (word-based) richness = V/N, (lemma-based) richness = L/N, inflectional diversity (V/L), etc., in the following examples. Examples (1) and (2) illustrate two purposely created eight-word sentences, examples (3)-(7) contain each of the sentences of a real abstract, and (8) the whole abstract (see Note 4 for the text and reference).

That that that that student used was wrong. (1) False friends lead foreign students to make mistakes. (2)

First, the occurrences are counted and the results tabulated as in Table 1.

Next, the expressions are computed and their results illustrated in Table 2.

Table 1 Counting of words and lemmas in the examples

	Tokens (N)	Word-types (V)	Lemmas (L)	Most frequent words (MFW)	Hapax Legomena (HL)	Hapax Dislegomena (HD)	Content Words (CW)	Function Words (FW)
1	8	5	5	4	4	0	4	5
2	8	8	8	1	8	0	7	1
3	44	39	39	3	35	3	26	18
4	15	14	14	2	13	1	8	7
5	32	27	27	3	23	3	16	16
6	32	27	27	3	23	2	15	17
7	18	17	17	2	16	1	10	8
8	141	92	89	7	67	14	75	66

Table 2 Evaluation of the expressions

	Word-based lexical richness V/N	Lemma-based lexical richness $L/N$		Functional density FW/CW
1	0.625	0.625	1	1
2	1	0.625	1.6	0.142857143
3	0.909090909	0.909090909	1	0.517241379
4	1	1	1	0.875
5	0.875	0.875	1	0.882352941
6	0.875	0.875	1	1.133333333
7	0.94444444	0.94444444	1	0.384615385
8	0.680851064	0.638297872	1.066666667	0.698795181

In view of the results, it seems obvious that (2) is lexically richer than (1), whilst the latter happens to be denser than the former in functional terms. It goes without saying that V/N (Mendenhall's formula) and L/N (the corresponding expression in terms of lemmas) are not reliable for comparison unless the same N is involved, since they are textlength dependent as the relevant literature shows (Tweedy and Baayen, 1998).<sup>5</sup>

The maximum value for V/N and for L/N (2, 4) is the unity, although the average is less than one, L/N being always equal or less than V/N. In contrast, when V and L are rated to calculate the inflectional diversity (i.e. the average of word-forms per lemma), its minimum value is the unity, which is bound to increase in highly inflected languages such as Latin, OE, or Modern German. In an intermediate position, the ratio FW/CW ranges from below the unity to over one, likely to provide a greater

**Table 3** Counting of N in terms of class

Class	Jn	Lk	Mk	Mt	AoT
Noun	2,960	3,844	2,172	3,943	1,282
Adje(ctive)	353	713	418	685	348
Verb	3,938	4,833	2,817	4,477	1,330
Adve(rb)	1,353	1,584	1,114	1,664	610
Pron(oun)	5,367	5,972	3,459	5,646	1,766
Prep(osition)	1,295	1,638	896	1,513	533
CONJ(UNCTION)	1,805	2,369	1,456	2,262	656
Excl(amation)	5	36	18	40	0
N	17,076	20,989	12,350	20,230	6,525

discriminating power, which the other expressions cannot confer: when N is the same in some texts (1, 2) and (5, 6) and, therefore, no text-length dependency can be invoked, functional density can distinguish between them whereas the other ratios cannot. This observation made us consider the convenience of testing its reliability. In analogy to lexical density, which is undoubtedly bound to imply either lexical richness (V/N) or the ratio CW/N, we will henceforth adopt the term functional density to refer to the ratio FW/CW, avoiding thus any kind of likely terminological misunderstanding.

Once the discriminating power of functional density has been introduced, we need to determine the values of FW and CW in the works of the corpus to evaluate the functional density. For this purpose, N is first counted in terms of class (Table 3); then adverbs are sorted into manner and other-than-manner adverbs by means of the OEC (Table 4); and lastly the ratio is obtained (Table 5).

Table 4 Counting of adverbs

Adverbs	Jn	Lk	Mk	Mt	AoT
Manner	109	138	99	371	175
<>Manner	1,244	1,446	1,015	1,293	435
Total	1,353	1,584	1,114	1,664	610

Table 5 Functional density

Words	Jn	Lk	Mk	Mt	AoT
CW	7,360	9,528	5,506	9,476	3,135
FW	9,716	11,461	6,844	10,754	3,390
Functional density	1.320	1.202	1.243	1.134	1.081

With the values for *functional density*, the WSG are ranked in decreasing order as follows:

where *Jn* (*Mk* preceding) is ranked as having the greatest *functional density* and, conversely, *AoT* (*Mt* preceding) is ranked as having the lowest *functional density*, which proves our hypothesis of relating the ranking of the *WSG* by *functional density* as the inverse of the one by *lexical richness* (Miranda and Calle, 2005a), as follows:

This proof confirms the reliability of FW as salient features in authorship attribution tasks as we have been successful in opposing Jn against Mt, as having the highest inflectional density and the highest lexical richness, respectively; and conversely, Mt and Jn as having the lowest inflectional density and the highest lexical richness. In other words, we could somewhat oppose inflectional density against lexical richness without considering the latter as being actually the inverse of the former due to the different scope of the parameters applied: whereas all members of V and L are included in N (inclusion), all members of CW are excluded from FW (exclusion).

#### **4 Score of Function Lemmas**

Unlike *functional density*, whose computation requires to tabulate the whole set of *CW* and *FW*,

the scoring of FL only takes into account the occurrences of the most common ones. This study is based on lemmas for the convenience of having homographs regularized, allomorphs grouped together, verb forms, and pronominal forms linked under the corresponding lemma, be they personal, demonstrative, or possessive. For this reason, the same annotated corpus is used and the seventy-eight topmost common FL are chosen from the union set  $\{Jn, Lk, Mk, Mt, AoT\}$ , as listed in Table 6.

As expected, the ordering of FL by absolute or relative frequency does differ slightly from one work to another, the differences becoming greater between In, on the one hand, and Lk, Mk, Mt, on the other, even in the three topmost FL (see and,  $h\bar{e}$ , se, etc.). Therefore, to count on another reliable technique of ranking by means of FL, we resort to find out the difference between the relative frequency of each FL in each text and its frequency in the union set, which is taken as an ideal corpus on the assumption that their distribution and repetition rate is the standard. In other words, the greater the deviation found in a given text to the standard (which implies more occurrences of FL than in the ideal corpus), the less rich it will be in lexical terms and, conversely, the smaller the deviation found in a literary work, the richer it will be from a lexical point of view.

The calculation procedure is explained stepwise, as follows. First, we score each FL in each of the WSG and in AoT (i.e. as the percentage resulting from *frequencies/N*). Second, we score each *FL* in the ideal corpus, constituted by the union set {In, Lk, Mk, Mt, AoT (i.e. also as the percentage of the total of lemma frequencies/N total, rather than as the mean of the individual percentages). Next, we subtract the score of each FL in each work to the score of each item in the ideal corpus. Fourth, we add up the absolute values of the differences in each text and divide the result by the number of function lemmas employed (78), as shown in Table 7 and fifth, we rank the texts in decreasing order, either by the sum or by the quotient, as follows:

Table 6 Frequencies of 78 topmost common FL in the corpus

	FL	Jn	Lk	Mk	Mt	AoT		FL	Jn	Lk	Mk	Mt	AoT
1	and	957	1,502	1,002	1,414	364	40	ofer	20	59	27	59	1
2	hē	1,030	1,401	912	1,081	334	41	nū	49	38	12	33	26
3	se	1,102	1,152	695	1,317	481	42	bus	18	25	24	54	23
4	bēon	723	907	415	793	155	43	hū	23	37	24	36	1
5	hīe	410	619	497	547	38	44	forþām	46	40	22	30	14
6	þā	308	667	370	530	192	45	hwilc	16	41	24	34	16
7	on	359	583	320	507	111	46	būtan	28	23	24	35	7
8	ic	695	386	146	350	163	47	twēgen	16	29	21	42	6
9	gē	415	365	160	497	22	48	foran	13	47	17	30	10
10	tō	389	314	150	314	150	49	manig	21	26	30	30	1
11	þe	340	342	152	297	99	50	eft	49	6	33	23	7
12	ne	338	312	172	304	55	51	ēower	27	31	4	36	6
13	þū	267	305	119	306	103	52	oþþe	6	24	12	48	4
14	þæt	329	277	155	121	121	53	ælc	20	31	3	35	1
15	þes	172	187	83	169	52	54	ūt	32	13	11	33	9
16	eall	55	157	89	122	43	55	hwā	32	19	15	22	10
17	of	131	146	28	115	15	56	æfter	24	32	12	20	26
18	sõþlīce	29	111	83	191	121	57	ær	25	21	13	23	16
19	hit	103	92	82	126	21	58	nāht	26	17	19	20	16
20	hēo	74	117	76	71	111	59	οþ	6	24	11	36	5
21	mid	78	141	98	115	110	60	þurh	13	18	11	30	10
22	ān	56	92	63	109	23	61	ongēan	8	20	20	23	12
23	wē	92	79	49	91	17	62	æt	27	14	7	14	11
24	swā	69	112	97	128	62	63	wiþ	15	24	4	15	5
25	þonne	50	86	38	101	20	64	gyt	14	16	10	10	3
26	mīn	148	65	39	54	54	65	hēr	14	20	15	18	4
27	hwæt	53	85	52	57	26	66	hwī	14		16	15	2
28	gif	80	56	30	77	21	67	betwux	4	18	14	13	5
29	þīn	43	76	44	69	33	68	sōna	4	14	35	7	10
30	ac	102	41	41	46	37	69	git	9	9	16	12	
31	witodlīce	77	27	16	103		70	hwær	24	7		7	4
32	fram	36	66	28	72	20	71	ūre	18	23	5	3	7
33	sum	26	93	42	41	11	72	þanon		4	22	2	2
34	nān	82	49	28	38	9	73	twelf	6	12	15	12	
35	be	69	51	24	32	14	74	ēac	15	7	3	5	9
36	þær	65	41	36	62	31	75	swīþe	5	5		16	10
37	forþāmþe	58	69		36		76	intō	6	11	3	11	9
38	ōþer	33	48	24	50	6	77	swilce	6	13	3	7	8
39	for	48	26	28	42	22	78	ge	3	6	1		7

Table 7 Sum and quotients of the differences of 78 topmost FL

	Jn	Lk	Mk	Mt	AoT
Sum	13.79447508	7.213282449	12.89773301	6.495542931	22.72113168
Quotient	0.174613609	0.091307373	0.163262443	0.082222062	0.287609262

In view of the ranking, we can state that Mt is the least unlike the ideal corpus, which is also applicable to Lk (second after Mt), and so on till AoT, which ranks as the most unlike. Recalling that the WSG are ranked as Mt > Lk > Mk > In in terms of lexical richness, we must admit that our hypothesis holds for the ranking of the WSG, whose order is as expected, and the discriminating value of the scoring of FL might be accepted in a near future if other authorship attribution studies validate its general reliability. In this particular case, some arguments may question its validity. One has to do with the limited size of the ideal corpus, which might be criticized as not being wholly representative, and the other can be established in the sense that the level of (dis)similitude with respect to the ideal corpus derives from the nature of its origin: the union of the constituent subsets. Therefore, to rule out any randomness, the technique must be experimented with larger corpora in English (Middle, Modern, or Contemporary) with the inherent inconvenience of their annotation.

#### 5 Delta-score of Function Words

In this third study, we attempt to check the hypothesis again by testing the Delta model, and, to gain accuracy, the annotated corpus (77,170 tokens) used in Sections 3 and 4 is replaced with a raw corpus (934,719 tokens, approximately one-fourth of the whole *OE* extant production) where lemmas are replaced by word-types, arresting thus the comparison and exchange of frequencies. This corpus (henceforth *entire corpus*) is formed by representative prose works (838,795 tokens) and a selection of poetry (95,924 tokens). The latter is included to compensate for any likely overweighting influence of the prose works selected, which are either authored or anonymous, some of which are translations from Latin. 7

First, a frequency hierarchy for *FW* is established (Table 8) to contain the 108 topmost common *FW*, ending with those words that occur 3 times in every 2,000. Their frequencies, which result as the sum of susceptible individual function words, that is, <and>, <pa>, <

amount to 440,112 tokens (47.084%) of the *entire* corpus, after having skipped over 57,107 tokens, which are related to CW.<sup>8</sup> The homographs are not tagged.<sup>9</sup>

Out of the works of the entire corpus, we select some for the main and others for the test corpus, taking into account that the main objective is to find out the level of (un)likeness between pairs of related works from each corpus. Thus, In and Mt, being the most unlike, are included in the main corpus, whereas Lk and Mk will be used in the test corpus. Also with a similar criterion, works by the same author (Ælfric) or similar versions of the same work (the Benedictine Rule for monks and for nuns) are assigned to each corpus to check their level of (un)likeness, thus following Hoover's suggestion of using works of known authorship to test the efficiency of Delta (Hoover, 2004b). The other works are included to serve as dummies. Accordingly, the distribution of works in each corpus is shown in Table 9, and the occurrences of each FW in the hierarchy are counted and added up  $(\Sigma)$ . For space, only the total values are provided along with the ratio FW/N, the mean  $(\mu)$ , and the standard deviation  $(\sigma)$ .

The procedure for calculation of Burrows's Delta (2003) is described stepwise, as follows. First, we score each FW in each work, as well as in the main corpus, where the scores are given as percentages of the frequencies of each FW to the total word-count (N), so that the larger do not exert an undue influence. In addition, we calculate  $\mu$  and  $\sigma$  in the *main corpus*, as indicated in Table 10, which contains, in descending order, the values for the thirty-six top FW in Jn, Mt, VRS, BenR, Æhom1, Whom, and ÆCHom2, though the list expands downwards for 108 FW. Thus, for and,  $\mu$  is 5.016501463, and  $\sigma$  is 1.602026783, respectively, and the score for In is 5.573751316, for Mt is 6.963542941, and so on. The scores result from rating the occurrences of such FW to N: in the case of Jn, and = 953 and N = 17.098. For space, the scores of only six works are included in the table.

Second, we calculate the *z-score* of each FW by subtracting its score in each work from  $\mu$  in the

Table 8 Frequencies of 108 topmost FW in the entire corpus

	FW	Tokens		FW	Tokens		FW	Tokens
1	and/ond <sup>10</sup>	44,571	37	heo/hio	2,837	73	na	1,100
2	þa	24,879	38	me/mec	2,832	74	þas	1,097
3	þæt/þat	23,451	39	ealle	2,716	75	soblice	1,086
4	on	21,128	40	gif/gyf	2,648	76	oþre	1,070
5	he	19,986	41	eac	2,598	77	þis	1,038
6	þe/þec	19,371	42	þær/þar	2,574	78	þy/þi	1,026
7	to	15,980	43	ær	2,465	79	þus	1,020
8	se	12,542	44	us/usic	2,455	80	hire/hyre/hiere	983
9	his/hys	11,938	45	seo/sio	2,320	81	þæra/þara	978
10	ne	11,191	46	æfter	2,277	82	οþ	972
11	mid	11,033	47	eft	2,230	83	mihte/meahte	961
12	swa/sua	10,928	48	wæron	2,023	84	sona	943
13	þam/þæm	9,870	49	man/mon	1,995	85	sume	873
14	him/hym	9,149	50	þeah/þeh	1,895	86	sum	857
15	hi/hy/hie	8,001	51	hwæt	1,880	87	siþþan/syþþan	854
16	is/ys	7,009	52	fram/from	1,806	88	þætte	845
17	wæs	6,979	53	eow	1,804	89	min/myn	842
18	ic	5,983	54	hu	1,790	90	æfre	820
19	þonne/þænne	5,677	55	oþþe/odþe	1,593	91	oþer	781
20	for	5,217	56	þan	1,578	92	þissum/þisum/þysum	766
21	þæs/þes	5,136	57	æt	1,550	93	oþrum	724
22	þære/þare	4,879	58	wære	1,497	94	oft	685
23	ac	4,765	59	wiþ	1,432	95	sind/synd/syndon/sint	670
24	þu	4,634	60	nan	1,376	96	beo/bio	647
25	we	4,509	61	an	1,376	97	magon	642
26	of	4,035	62	beob/biob	1,353	98	fela	642
27	bone/bæne	4,022	63	ofer	1,332	99	her	622
28	hine/hyne/hiene	3,817	64	swibe/swybe/suibe	1,319	100	anum	616
29	ge	3,786	65	buton/butan	1,256	101	forbæm/forbam	608
30	þurh	3,732	66	wolde	1,240	102	nis/nys	607
31	hit/hyt	3,578	67	beon/bion	1,223	103	ælc	606
32	be/bi/by/bie	3,169	68	sy/si/sie	1,205	104	witodlice	570
33	heora/hiora	3,090	69	ure	1,184	105	þon	549
34	biþ/byþ	3,018	70	eallum	1,136	106	ongean/angean	504
35	nu	2,862	71	sceal/sceall	1,125	107	hira/hyra	374
36	in	2,840	72	mæg	1,111	108	ymb/ymbe/embe	348
		346,755		U	65,031		, , , , , , , , , , , , , , , , , , , ,	28,326
		•			•			440,112

*main corpus*, and dividing the result by  $\sigma$ , as shown in Table 11. Thus, the *z-score* for *and* in *Jn* is 0.347840533, which derives from the referred expression. For space, the *z-scores* of only six works are included in the table.

Third, we calculate the difference between the *z-score* of each *FW* in the *main corpus* and that of each work in the *test corpus*. Then, we obtain the *Delta-score* by adding the absolute values of the differences obtained, and dividing the result by the number of *FW*.

Fourth, we rank each work in the *test corpus* according to Delta values, in such a way that the smaller the value, the least unlike it will become to the work of the *main corpus* under scrutiny. For the sake of clarity, we summarize all the values of Delta, along with those of  $\mu$  and  $\sigma$  in Table 12. To the right of the values for Delta-*score*, the ones for Delta-*z-score* are also included.

From the analysis of the values for Delta in the table, two main facts must be highlighted inasmuch as they seem to validate both points of our

	Main	corpus		Test corpus					
Works	FW	N	FW/N%	Works	FW	N	FW/N%		
Jn	9,736	17,098	56.94233244	Ad	3,095	6,345	48.7785658		
Æhom1	47,573	89,676	53.04986842	Alc	624	1,092	57.14285714		
ÆCHom2	49,986	100,954	49.51363988	Alex	3,443	6,690	51.46487294		
Mt	10,746	20,435	52.58624908	AoT	3,446	6,546	52.64283532		
CP	38,687	69,922	55.32879494	$\cancel{E}CHom1$	54,330	107,220	50.67151651		
BenR	11,270	22,763	49.51017001	Lk	11,295	21,126	53.46492474		
VRS	32,473	95,924	33.85284183	Ælet	14,678	30,299	48.44384303		
Whom	14,026	28,799	48.70307997	Mk	6,762	12,423	54.43129679		
				Or	25,771	51,097	50.43544631		
				BenRW	9,505	20,500	46.36585366		
$\sum$	214,497	445,571	48.13980264	$\sum$	132,949	263,338	0.504860673		
$\frac{-}{\mu}$			49.9358625	$\overline{\mu}$			51.38420122		
σ			7.125803781	σ			3.169190176		

Table 9 Frequency weight of the 108 FW in each work

hypothesis: (1) to confirm the level of (un)likeness among the WSG, as conjectured; (2) to relate works by the same author, as expected. With respect to (1), Luke's study evinces that Mt is the least unlike to Lk, whereas Jn is the second. Analogously, Mark's study shows that Mt is also the most like to Mk, whereas Jn is also the second. In addition, Mt and Lk look like each other the most. From these results the WSG can be ranked in terms of Delta the same way as by  $lexical\ richness$ , that is, Mt > Lk > Mk > Jn.

With respect to (2), our analysis is restricted to ÆCHom1, Ælet, and BenR, whose association with works in the main corpus was evident, and the results confirm the proof clearly: ÆCHom2 and Æhom1 are the least unlike to ÆCHom1; Æhom1 and ÆCHom2 are the least unlike to ÆLet: and BenRW is the least unlike to BenR. However, it is worth pointing the likeness observed by Whom with respect to Ælfric's works as well as by Or with respect to the latter and BenR. Following the scholarly suggestion of an anonymous reviewer, the Delta study was repeated by replacing Mt in the main corpus alternatively by Lk and Mk, and In by Lk and Mk, and Lk and Mk by Mt and In in the test corpus to gain reliability with the results of the six possible combinations of In, Lk, Mk, and Mt. For clarity, only the results of the Gospels, Ælfric's works, and BenR are included in Table 13, and for space some decimals have been suppressed.

As the results do not require a further interpretation, their values haven been plotted to ease their comparison and to help draw some conclusions (Fig. 1).

It is true that we have used the Delta technique for our purposes, though with scientific rigour and, in light of this, we must join Hoover in recognizing the excellence of the methodology proposed by Burrows, as it proves to operate efficiently and reliably. In this line, Hoover's detailed and (prospective) publications on Delta have encouraged us to check one of his proposals, in particular, the modification of the range of MCW to be considered and/or the possibility of eliminating pronouns from the counting, etc. Thus, when the values for Delta proved their efficiency for our study, we repeated the experiment in four ways, that is, leaving out (1) the topmost common FW (in number of 10, 20, 30, 40, 50, 60, 70, 80); (2) the bottommost common FW (in number of 10, 20, 30, 40, 50, 60, 70, 80); (3) the top and bottommost common FW (in number of 10, 20); and (4) all personal pronouns and possessives (hē, his, hī, him, ic, wē, bū, hine, hit, heora, hēo, ūs, mē, ēow, ūre, hire, mīn, hira). Although no homogeneous result can be expected, there is one constant common to all of them: the replication of the firstly ranked like work. In addition to this, more likenesses are observed in some of the variants experimented on test works, as shown in Table 14.

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		μ	$\sigma$	Jn	Mt	BenR	Æhom1	Whom	ÆCHom2
1	and	5.016501463	1.602026783	5.573751316	6.963542941	4.9158722	4.615504706	7.29886454	4.538700794
2	þa	2.324586792	0.950464853	2.88922681	3.944213359	1.1773492	2.446585486	1.16670718	2.645759455
3	þæt	2.568470047	0.641575273	2.63188677	2.069977979	2.8906559	2.274856149	2.91676794	2.164352081
4	on	2.352682728	0.294637863	2.111358054	2.485931001	2.6226772	2.873678576	2.15979722	2.400103017
5	he	2.151551934	0.606903717	2.433033103	2.123807194	2.2536573	2.286007404	1.84034168	1.925629495
6	þe	2.186766744	0.533904066	2.836589075	2.319549792	1.8275271	2.894865962	2.31952498	2.176238683
7	to	1.765414408	0.348423955	2.275119897	1.546366528	1.5551553	1.885677327	1.92715025	1.907799592
8	se	1.390915825	0.437815206	2.20493625	1.600195743	1.027984	1.528837147	1.06948158	1.660162054
9	his	1.263381163	0.403684728	1.07030062	1.389772449	1.1553837	1.768589143	1.11809438	1.754264318
10	ne	1.503849607	0.372830844	1.965142122	1.507218008	1.9900716	1.150809581	1.55908191	1.077718565
11	mid	0.96644616	0.416161666	0.438647795	0.567653536	1.6518034	1.215486864	0.82641758	1.234225489
12	swa	1.116984416	0.433495869	0.438647795	0.861267433	1.0455564	1.765243766	1.36115837	1.479881926
13	þam	1.260876655	0.452256644	0.918236051	1.086371422	1.5595484	1.866720193	0.88891975	1.488796878
14	him	1.110030325	0.509022863	2.152298514	1.463175924	0.7775776	1.126276819	0.48960033	0.812251124
15	hi	1.423475917	0.656160365	1.590829337	1.90359677	1.3838246	1.169766716	0.94794958	1.206490085
16	is	0.917744428	0.24718481	1.07030062	1.120626376	1.076308	0.855301307	1.15629015	0.84890148
17	wæs	0.532826556	0.279607944	0.924084688	0.557866406	0.0571102	0.578750167	0.37501302	0.52499158
18	bonne	0.798004037	0.785265169	0.298280501	0.494250061	0.7160743	0.453856104	0.86114101	0.318957149
19	ic	0.716369251	0.57077095	2.532459937	1.008074382	0.2416202	0.438244346	0.2187576	0.530934881
20	for	0.494658482	0.194475209	0.397707334	0.254465378	0.4832403	0.747134127	0.45834925	0.735978763
21	þæs	0.549270008	0.138116886	0.479588256	0.391485197	0.7556122	0.574289665	0.39584708	0.575509638
22	þære	0.426354986	0.235841897	0.350918236	0.259358943	0.562316	0.507382131	0.15278308	0.626027696
23	ac	0.480321444	0.171621544	0.579015089	0.200636163	0.4568818	0.604398055	0.49307268	0.541830933
24	þu	0.47318544	0.349262575	1.128786993	0.748715439	0.188903	0.394754449	0.07639154	0.465558571
25	we	0.518090319	0.256746131	0.380161422	0.239784683	0.3778061	0.735982872	0.97572832	0.65277255
26	of	0.454937293	0.17584225	0.772020119	0.567653536	0.3206959	0.585440921	0.36112365	0.437823167
27	bone	0.420296398	0.14268359	0.426950521	0.538292146	0.3294821	0.606628306	0.27431508	0.423955465
28	hine	0.534181818	0.262183061	1.029360159	0.6704184	0.4393094	0.579865293	0.34028959	0.494284526
29	ge	0.587500137	0.467765031	1.427067493	1.238071935	0.3953785	0.398099826	0.29862148	0.361550805
30	þurh	0.42952148	0.269801446	0.076032284	0.146806949	0.421737	0.449395602	0.9410049	0.593339541
31	hit	0.493619721	0.245520068	0.602409639	0.572547101	0.5008127	0.302199028	0.71183027	0.266457991
32	be	0.404669171	0.27614718	0.397707334	0.156594079	1.0104116	0.47504349	0.24653634	0.385324009
33	heora	0.251324046	0.228129489	0	0.078297039	0.562316	0.483964494	0.30903851	0.45664362
34	biþ	0.353603409	0.234686223	0.146215932	0	0.4964196	0.404790579	0.42709816	0.302117796
35	nu	0.264713049	0.132946214	0.32167505	0.166381209	0.0439309	0.428208216	0.36459599	0.267448541
36	in	0.159270848	0.314100872	0.023394549	0.02936139	0.0439309	0.063562157	0.11111497	0.055470808

Table 11 z-score of the 36 topmost FW

	FW	Jn	Mt	BenR	Æhom1	Whom	ÆCHom2
1	and	0.347840535	1.215361378	-0.06281369	-0.2503059	1.424672237	-0.29824762
2	þa	0.594067226	1.704036254	-1.20702789	0.12835687	-1.21822455	0.337911141
3	þæt	0.098845335	-0.77698142	0.502179331	-0.45764528	0.542879239	-0.62988395
4	on	-0.8190552	0.452244227	0.916360243	1.768258307	-0.65465284	0.160944315
5	he	0.463798723	-0.04571523	0.168239728	0.221543329	-0.51278357	-0.37225417
6	þe	1.217114405	0.248702072	-0.67285424	1.326266762	0.248655606	-0.01971901
7	to	1.462888764	-0.62868203	-0.60345768	0.345162602	0.464192653	0.408654978
8	se	1.859278557	0.478009706	-0.82896119	0.315021773	-0.73417789	0.614976879
9	his	-0.47829539	0.31309405	-0.26752913	1.251491436	-0.35990161	1.216006258
10	ne	1.237270259	0.009034663	1.304135665	-0.94691744	0.148143068	-1.14296081
11	mid	-1.2682532	-0.95826372	1.646853284	0.59842298	-0.33647639	0.643450254
12	swa	-1.56480527	-0.58989486	-0.16477211	1.495422211	0.563267092	0.837141797
13	þam	-0.75762426	-0.38585444	0.660403201	1.339601189	-0.82244652	0.503962133
14	him	2.047586198	0.693771584	-0.65311934	0.031917021	-1.21886469	-0.58500162
15	hi	0.255049571	0.731712671	-0.06042927	-0.38665731	-0.72471054	-0.33069025
16	is	0.617174624	0.820770291	0.641477994	-0.25261714	0.965050082	-0.278508
17	wæs	1.399309784	0.089553426	-1.70136916	0.164242869	-0.56441005	-0.02802129
18	þonne	2.208751858	0.267515171	-0.70852992	-0.45813784	-0.73764438	-0.3401006
19	ic	-0.7324983	-0.38915644	-0.00051671	-0.45992731	0.253642482	-0.69627248
20	for	-0.49852703	-1.23508341	-0.05871255	1.298240774	-0.18670366	1.240879402
21	þæs	-0.50451291	-1.14240059	1.493967721	0.181148427	-1.1108195	0.18998133
22	þære	-0.31986153	-0.70808472	0.576492367	0.343565526	-1.15998008	0.846637992
23	ac	0.575065596	-1.629663	-0.13657762	0.722966408	0.074298553	0.358401909
24	þu	1.877102211	0.788890704	-0.81395035	-0.22456168	-1.13609051	-0.02183706
25	we	-0.53721899	-1.08397208	-0.54639277	0.848669275	1.782453366	0.524573556
26	of	1.803223204	0.641007733	-0.76341964	0.742163087	-0.53351025	-0.09732659
27	þone	0.046635514	0.826974899	-0.63647364	1.305909865	-1.02311217	0.025644623
28	hine	1.88867404	0.519623889	-0.36185561	0.174242664	-0.73952994	-0.15217342
29	ge	1.794848486	1.390808967	-0.4107226	-0.40490481	-0.61757215	-0.48304024
30	þurh	-1.31018273	-1.04786144	-0.02885252	0.073662029	1.895777148	0.607180069
31	hit	0.443099901	0.321470177	0.029297	-0.77965396	0.888768698	-0.92522673
32	be	-0.0252106	-0.89834375	2.193549327	0.254843517	-0.57263968	-0.07005381
33	heora	-1.10167277	-0.75845962	1.363225751	1.019773682	0.252989926	0.900013301
34	biþ	-0.88367981	-1.50670714	0.608541131	0.218108971	0.313161776	-0.21938063
35	nu	0.428458993	-0.73963625	-1.66068744	1.229784304	0.751303411	0.020575933
36	in	-0.4325881	-0.41359152	-0.36720658	-0.30470686	-0.15331342	-0.33046721

These results serve to confirm the validity of Delta, independent of the range of frequency adopted without enlarging the initial scope of 108 function words, at least for the particular cases investigated.

### 6 Conclusions

We have proven, out of any reasonable doubt, both by lemma-counting and by Zipf's Z, that the *lexical* richness of the Gospel according to Saint Matthew is greater than that of the other three, which leads to the following ranking: Mt > Lk > Mk > Jn (Miranda and Calle, 2005a). The inverse ranking Jn > Lk > Mk > Mt (resembling a mirror image of the previous one) has been obtained by means of functional density. The same ranking has also been generated from the study of FL, and the values for Delta-score and Delta-z-score also point to this direction insofar as Mt and Lk are estimated as the least unlike whereas Mt and Jn were taken as the most unlike. From these results, it follows that the four works can be equally ranked in terms of functional density or by means of lemma-scoring and successfully clustered, thanks to Delta-score.

Table 12 Works ranked in descending order by Delta-score and Delta-z-score

Ad	$\Delta$ -score	$\Delta$ -z-score	Alc	$\Delta$ -score	$\Delta$ -z-score	Alex	$\Delta$ -score	$\Delta$ -z-score
Whom	1.607630889	1.459423071	Whom	1.607630889	1.459423071	VRS	1.941414074	1.621772993
Æhom1	1.643213468	0.946323726	$\cancel{E}hom1$	1.643213468	0.946323726	ÆCHom2	1.985796452	-17.039503
ÆCHom2	1.656853496	-23.89176	ÆCHom2	1.656853496	-23.89176	$\mathcal{E}hom1$	2.097954566	0.278547568
BenR	1.709373544	-0.00770188	BenR	1.709373544	-0.00770188	CP	2.137733003	-0.0627788
CP	1.714798392	-0.08592796	CP	1.714798392	-0.08592796	Whom	2.159908333	-0.2530585
VRS	1.755397694	-0.67136825	VRS	1.755397694	-0.67136825	Jn	2.225937655	-0.8196356
Mt	1.776415641	-0.97444619	Mt	1.776415641	-0.97444619	Mt	2.244754491	-0.9810970
Jn	1.807032331	-1.41593761	Jn	1.807032331	-1.41593761	BenR	2.249835081	-1.0246920
$\mu$	1.708839432		$\mu$	2.317452888		$\mu$	2.130416707	
σ	0.069348323		σ	0.090485188		σ	0.116540745	
AoT	$\Delta$ -score	$\Delta$ -z-score	ÆCHom1	$\Delta$ -score	$\Delta$ -z-score	Lk	$\Delta$ -score	$\Delta$ -z-score
ÆCHom2	1.145756764	-8.18061939	ÆCHom2	0.328103971	ÆCHom2	Mt	0.475261193	1.95323673
Æhom1	1.256157716	0.699006029	$\cancel{E}hom1$	0.519617857	Æ $hom1$	Jn	0.819544058	0.782988425
VRS	1.284450835	0.496995229	Whom	1.007994064	Whom	ÆCHom2	0.970644479	-3.2993075
Jn	1.30599764	0.343152618	Mt	1.008261252	Mt	Æ $hom1$	1.050966589	-0.00363749
Mt	1.335551102	0.132143062	BenR	1.013388759	BenR	VRS	1.17505739	-0.42543324
Whom	1.418122663	-0.45741183	CP	1.094359994	CP	Whom	1.228777702	-0.6080334
BenR	1.518976829	-1.1775032	In	1.094859707	In	BenR	1.317633024	-0.9100606
CP	1.567456242	-1.52364265	VRS	1.161962061	VRS	CP	1.361287179	-1.05844498
μ	1.354058724		$\mu$	0.903568458		$\mu$	1.049896452	
σ	0.140057459		σ	0.305254983		σ	0.294196423	
ÆLet	$\Delta$ -score	$\Delta$ -z-score	Mk	$\Delta$ -score	$\Delta$ -z-score	Or	$\Delta$ -score	$\Delta$ -z-score
Æhom1	0.5567814	1.516348812	Mt	0.670328977	1.74755156	BenR	0.517866923	2.373167693
ÆCHom2	0.567785101	-2.13759695	Jn	0.889686888	0.89372523	ÆCHom2	1.511840204	-3.40960444
Whom	0.929675474	0.112477466	ÆCHom2	1.038015514	-4.04036021	$\cancel{E}hom1$	1.625092551	-0.12392254
BenR	1.010329086	-0.1911672	$\mathcal{E}hom1$	1.039869082	0.309157704	VRS	1.652768592	-0.18633942
Mt	1.036780856	-0.2907528	VRS	1.245856592	-0.49262582	Whom	1.743589603	-0.39116512
VRS	1.135030297	-0.66064223	Whom	1.280458099	-0.62730835	CP	1.782758626	-0.47950176
CP	1.186425085	-0.85413329	BenR	1.37608883	-0.99954036	Mt	1.799638316	-0.51756998
Jn	1.253605177	-1.10705285	CP	1.414058345	-1.14733248	Jn	1.927601266	-0.80616069
$\mu$	0.95955156		$\mu$	1.119295291		$\mu$	1.57014451	
σ	0.265618409		σ	0.256911627		σ	0.443406334	
			BenRW	$\Delta$ -score	$\Delta$ -z-score			
			BenR	1.042748372	2.116493607			
			ÆCHom2	1.482854715	-5.53965446			
			$\mathcal{E}hom1$	1.558279397	0.190570783			
			Whom	1.609871292	-0.00216642			
			Mt	1.701461287	-0.34432869			
			VRS	1.767317142	-0.59035324			
			CP	1.797120968	-0.7016945			
			Jn	1.9146779	-1.14086414			
				1.9146779 1.609291384	-1.14086414			

Therefore, it is worth enhancing their complementary feature for tasks of ranking and clustering in authorship attribution studies.

The efficiency of *functional density* has been proven as an indirect measure to rank texts in terms of *lexical richness* from the least rich to the most, the ranking obtained being similar to the one resulting

by means of *Z*; in other words, *functional density* may be a helpful marker to relate works by the same author, once the technique has been refined and tested with larger corpora. An in-progress research based on an annotated corpus of the *Federalist Papers* seems to reveal traces confirming the validity of *functional density* in the attribution of authorship

Table 13 Works ranked in descending order by Delta-score

2nd study )	2nd study Jn and Lk		3rd study Jn and Mk		4th study Lk and Mt		5th study Mk and Mt		6th study $Lk$ and $Mk$	
ÆCHom1	$\Delta$ -score	ÆCHom1	$\Delta$ -score	ÆCHom1	$\Delta$ -score	ÆCHom1	$\Delta$ -score	ÆCHom1	$\Delta$ -score	
ÆCHom2	0.325776	ÆCHom2	0.320598	ÆCHom2	0.341022	ÆCHom2	0.335463	ÆCHom2	0.332518	
Æhom $1$	0.517612	$\cancel{E}hom1$	0.496124	Æ $hom1$	0.544182	$\cancel{E}hom1$	0.517041	Æ $hom1$	0.516929	
Lk	0.991538	Whom	0.987619	Whom	1.036373	Whom	1.027869	BenR	1.047549	
Whom	0.994752	BenR	1.008894	Lk	1.041115	Mt	1.040511	CP	1.120692	
BenR	1.002550	Mk	1.054923	Mt	1.045140	BenR	1.053916	Lk	1.037608	
CP	1.079067	CP	1.079768	BenR	1.047844	Mk	1.083725	Mk	1.090885	
Jn	1.093989	Jn	1.089985	CP	1.128949	CP	1.127017	VRS	1.199552	
VRS	1.149178	VRS	1.152916	VRS	1.202198	VRS	1.198391	Whom	1.017836	
$\mu$	0.894308	$\mu$	0.898853	$\mu$	0.923353	$\mu$	0.922992	$\mu$	0.920446	
ÆLet	$\Delta$ -score	ÆLet	$\Delta$ -score	ÆLet	$\Delta$ -score	ÆLet	$\Delta$ -score	ÆLet	$\Delta$ -score	
Æhom1	0.556263	$\cancel{E}hom1$	0.539412	Æ $hom1$	0.575250	$\mathcal{A}hom1$	0.554755	Æ $hom1$	0.557326	
ÆCHom2	0.562786	ÆCHom2	0.556398	ÆCHom2	0.594242	ÆCHom2	0.587587	ÆCHom2	0.585490	
Whom	0.924538	Whom	0.925670	Whom	0.949785	Whom	0.947763	Whom	0.946296	
BenR	1.009186	BenR	1.009798	BenR	1.036715	BenR	1.039371	BenR	1.048854	
Lk	1.060437	Mk	1.103473	Mt	1.082660	Mt	1.083937	Lk	1.116699	
VRS	1.126672	VRS	1.141735	Lk	1.117185	Mk	1.135830	Mk	1.144354	
CP	1.178421	CP	1.176385	VRS	1.179883	VRS	1.192051	VRS	1.194545	
In	1.254020	Jn	1.242305	CP	1.208654	CP	1.203810	CP	1.210030	
$\mu$	0.959040	$\mu$	0.961897	$\mu$	0.968047	$\mu$	0.968138	$\mu$	0.975449	
Mt	$\Delta$ -score	Mt	$\Delta$ -score	Jn	$\Delta$ -score	Jn	$\Delta$ -score	Jn	$\Delta$ -score	
Lk	0.605078	Mk	0.624428	Mt	1.365191	Mt	1.686223	Lk	1.446777	
In	0.906291	In	0.761435	Lk	1.405802	Mk	1.799534	Mk	1.524938	
Æhom1	1.042117	ÆCHom2	0.982350	ÆCHom2	1.718466	ÆCHom2	2.032705	ÆCHom2	1.754757	
ÆCHom2	1.045090	Æhom1	1.084829	Æhom1	1.849307	Æ $hom1$	2.160880	Æhom1	1.879825	
VRS	1.249480	Whom	1.194722	Whom	1.972625	VRS	2.275701	Whom	1.999863	
Whom	1.276425	VRS	1.200277	VRS	1.976360	Whom	2.286760	VRS	2.012682	
BenR	1.378135	BenR	1.234368	CP	2.071564	CP	2.402522	CP	2.123087	
CP	1.412151	CP	1.358265	BenR	2.120602	BenR	2.450025	BenR	2.170008	
$\mu$	1.114346	$\mu$	1.055084	$\mu$	1.809990	$\mu$	2.136793	$\mu$	1.863992	
Mk	$\Delta$ -score	Lk	$\Delta$ -score	Mk	$\Delta$ -score	Lk	$\Delta$ -score	Mt	$\Delta$ -score	
Lk	0.477990	Mk	0.575626	Lk	0.658944	Mt	0.515407	Lk	0.551254	
Jn	0.773175	Jn	0.822087	Mt	0.727092	Mk	0.621508	Mk	0.710431	
ÆCHom2	0.994175	ÆCHom2	0.968821	ÆCHom2	1.079849	ÆCHom2	1.015977	VRS	1.301363	
Æhom1	1.097400	Æ $hom1$	1.044130	Æ $hom1$	1.084331	Æ $hom 1$	1.102217	BenR	1.364239	
Whom	1.204772	VRS	1.160328	VRS	1.294856	VRS	1.204210	Æ $hom1$	1.170908	
VRS	1.218111	Whom	1.216995	Whom	1.345670	Whom	1.302810	Whom	1.309478	
BenR	1.235341	BenR	1.316051	BenR	1.452950	BenR	1.414650	ÆCHom2	1.066385	
CP	1.344573	CP	1.346741	CP	1.478661	CP	1.442436	CP	1.462047	
$\mu$	1.043192	$\mu$	1.056347	$\mu$	1.140294	$\mu$	1.077402	$\mu$	1.117013	
BenRW	$\Delta$ -score	BenRW	$\Delta$ -score	BenRW	$\Delta$ -score	BenRW	$\Delta$ -score	BenRW	$\Delta$ -score	
BenR	0.975306	BenR	1.005156	BenR	1.003975	BenR	1.025948	BenR	0.970164	
ÆCHom2	1.414815	ÆCHom2	1.447568	ÆCHom2	1.477369	ÆCHom2	1.508901	ÆCHom2	1.454624	
Æhom1	1.495624	$\cancel{E}hom1$	1.513084	Æhom1	1.548551	Æhom1	1.558427	$\cancel{E}hom1$	1.508144	
Whom	1.538838	Whom	1.571288	Whom	1.576304	Whom	1.602620	Whom	1.544700	
Lk	1.655793	Mk	1.694348	Mt	1.711224	Mt	1.742054	Mk	1.706974	
VRS	1.696357	VRS	1.742286	Lk	1.741837	Mk	1.756083	Lk	1.717326	
CP	1.724854	CP	1.75592	CP	1.760902	CP	1.776575	CP	1.717903	
Jn	1.849024	Jn	1.871348	VRS	1.761349	VRS	1.811641	VRS	1.744048	
$\mu$	1.543826	$\mu$	1.575129	$\mu$	1.572689	$\mu$	1.597781	$\mu$	1.545485	

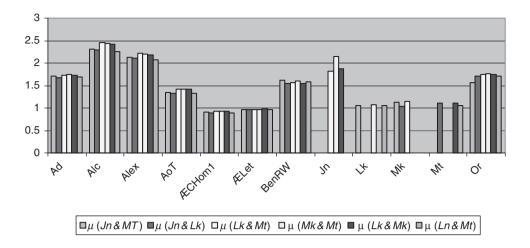


Fig. 1 Plotting of works in terms of their Delta-score mean

Table 14 Ranking by Delta-score after hierarchy truncation or reduction 11

Tops off								
	10	20	30	40	50	60	70	80
Lk	D	D	AG	В	В	В	В	В
$\cancel{E}$ Let	AI	AG	AG	AG	AG	E	A	E
Mk	AI	AI	AI	AI	AI	A	A	
BenRW	A	D	D	D	D	D	D	D
Bottoms	off							
	10	20	30	40	50	60	70	80
Lk	D	D	D	D	D	D	D	D
ÆLet	F	С	С	F	С	C	С	С
Mk	E	E	D	D	A	A	В	A
BenRW	EI	E	E	В				A
Tops and	bottoms	off or prono	uns off					
	10 tops and 10 bottoms off			20 tops an	20 tops and 20 bottoms off			
Lk	C				EI	EI		
Ælet	1st and 2nd, and 7th and 8th alternate				1st and 2r	1st and 2nd, and 7th and 8th alternate		
Mk	AI				A	A		
BenRW	D				D	D		

of these 18th-century American English texts. After having handled the *Disputed Papers* and a significant part of the undisputed contributions (all by Jay, and by Madison, and some by Hamilton), the computation of *functional density* points to the fact that Madison's and the *Disputed Papers* are the least unlike, as is generally acknowledged (Mosteller and

Wallace, 1984). However, the application of *functional density* has to overcome the difficulties deriving from the requirement of an annotated corpus and an appropriate concordancer.

Likewise, the use of the top FL has proven to measure the divergence from an ideal corpus as an indirect technique to ascertain *lexical richness*. The technique may be helpful at least to signal the main tendency, but its accuracy depends on the availability of a large annotated corpus to avert the problems of text-length dependency.

Lastly, Burrows's methodology has been successfully tested as Delta was able to cluster the pairs of gospels under experiment as the most (un)like as well as to associate works by the same author. Considering that our aim was to corroborate what we already knew: (1) the ranking of the WSG by lexical richness (by lemma-counting and by Z) and (2) the leading candidates in the case of Aelfric's works (Homilies and Letters) and of the Benedict Rule, the hypothesis also holds true in both cases. Besides, Hoover's proposal for top and/or bottom truncation, and/or for neglecting pronominals has been successfully From experience, we must highlight the simplicity of the procedure of accounting only FW, although it would be useful to check whether similar results can be obtained by applying Delta methodology to the hierarchies of the whole works or to their corresponding partitions (for example, of 3,000 words). In this line, we cannot help insisting on the suitability of FW in quantitative studies (Craig, 1999), irrespective of the aims pursued. Several facts will be argued to support our statement. One is quantitatively featured as their suitability is given by the weight within the text: only the frequencies of the top 108 most common FW range from 48.1398% in the main corpus to 50.4861% of the test corpus (i), the ratio FW to CW (functional density) ranges from 1.134867033 in AoT to 1.320108696 in In (ii). The other is qualitatively featured as the distribution of their use can certainly describe the style of an author.

Before closing this section, some lines are to be devoted to the nature of the works which bear this study: the translation of the *Holy Gospels* into West Saxon (henceforth WS), the most prestigious dialect of OE. It is necessary to insist on the word *translation* because it is an actual rendering from a Latin source rather than a gloss (unlike the cases of the *Lindisfarne* Gospels, written in the Northumbrian dialect, or of the Mercian *Rushworth*). Without assessing the quality of the

version (not free of mistakes!), we must admit that all the evidences found in our study signal the common lexical similarities of the so-called Synoptic Gospels since Mt and Lk are supposed to have their common textual source in Mk, but these likenesses are not so markedly significant and regularly distributed as to counterbalance the differences that can serve to put them apart. Previous to this research, we accomplished a comparative lexical study between the Latin source and the WS renderings of the Gospels, by computing N, V, MFW, HL, HD, K and Z to conclude that, in general terms, the data concerning each WS gospel resembled its Latin counterpart: both are ranked as Mk > Lk > Mt > In, if Yule's K is applied, and as Mt > Lk > Mk > Jn, if Zipf's Z is applied. Obviously, the WS texts are numerically greater than the Latin ones, as the latter relies on a more synthetic system than OE. In fact, the ratio N(WS) to N(L) ranges from 10.63 in Lkto 11.16 in Mt. The reason for this numerical difference in N must be associated with the unbalanced use of certain FW in each language: demonstratives (acting as determiners) are more common in OE, personal pronouns acting as subjects are usually omitted in Latin, and prepositions are more than once unnecessary in Latin due to its stronger casual system. Therefore, the weight of FW within N differs from one language to another, which makes them reliable enough for authorship difference. Despite the low value of N, the widely known The Lord's Prayer can illustrate our argument better, as shown in Table 15 (de la Cruz et al., 2003).

As can be observed, the difference is not too sharp due to the fact that the imperative is the most common tense used and, therefore, the pronominal subject can be omitted in both. Text-length N is expected to increase with decreasing level of synthesis, as happens when two other prayers in Latin are compared with their versions in Contemporary English (Table 16).

All in all, the data concerning the *FW* used in Latin are bound to offer such significant variations with respect to their WS counterparts that it would be daring to state that their distribution is alike in both versions. Add to this the differences observed

Table 15	Several	versions	of	The	Lord's	Prayer	in	numbers
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	Latin	Northumbrian	West Saxon	Middle English	King's James	Protestant	Catholic	μ	σ
FW	26	27	29	32	35	29	29	29.5714286	3.047247
CW	23	24	23	23	30	26	26	25	2.581988897
N	49	51	52	55	65	55	55	54.5714285	5.15936504

Table 16 Nicene Creed and the Glory in numbers

	Nice	ne Creed	Glory		
	Latin	Catholic	Latin	Catholic	
FW	61	117	33	58	
CW	102	115	50	71	
N	163	232	83	129	

in the translation of Latin absolute ablatives and/or the rendering of amen, autem, vero, etc. into OE. Therefore, we estimate that the WS Gospels, notwithstanding their condition of translated pieces, can be the object of an independent study of authorship, and in view of the evidences found in the use of FW we can even dare to affirm that the translatorship of The Gospel according to Saint Matthew and that of Saint John cannot be assigned to the same person, as Liuzza (2000) proposes. Furthermore, the features distinguishing between Mt and In cannot be necessarily attributed to their inclusion within or exclusion from the Synoptic Gospels, but rather to the different usage of FW, which amounts to 50% of N as an average.

# **Acknowledgements**

This research has been funded by the Spanish Ministry of Science and Technology (grant number HUM2004-01075/FILO). This grant is hereby gratefully acknowledged. We would also like to thank the Dictionary of Old English project at the University of Toronto for granting permission to use files of the *Toronto Complete Corpus of Old English Dictionary*. Our gratitude also to both anonymous reviewers for their suggestions as they have served to

improve the presentation and clarity of the argument as well as to offer much grounded results in Delta.

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#### Notes

- 1 See Tweedy and Baayen (1998) for a review of *K* and *Z*. See also Miranda and Calle (2005b: 287–94) for an updated interpretation.
- 2 The annotation was accomplished as follows. First, the corpus was typed using the TT font *Fonetik* for special characters and vowel length markers. Second, it was tagged by *MAOET* (standing for *Morphological Analyser of Old English Texts*; see Miranda, Triviño, and Calle 2000: 127–45), which provides all the possible tags for each word, regardless of context, including lemma, morphological analysis (class, type, case, gender, number, etc.), and meaning(s). Third, it was semi-automatically

- disambiguated according to context by means of an ad hoc tool.
- 3 Even with a clear-cut definition, the subjectivity of the disambiguator cannot be ruled out because some examples admit more than one plausible tagging.
- John F. Burrows has proposed Delta, a simple new measure of textual difference, as a tool for authorship attribution and has shown that it has great potential, especially in attribution problems, where the possible authors are numerous and difficult to limit by traditional methods (3). In tests on prose, Delta has performed nearly as well as for Burrows's verse texts (4). A series of further tests using automated methods, however, shows that two modified methods of calculating Delta and three alternatives to or transformations of Delta produce results that are even more accurate (5). Four of these five new measures produce much better results than Delta both on a very diverse group of 104 novels and on a group of forty-four smaller contemporary literary critical texts testing (6). Although further is needed. Delta and its modifications should prove valuable and effective tools for authorship attribution (7) (Hoover, 2004a).
- 5 Recall that V(N)/N is blamed for text-dependency. Confer, also, Guiraud's  $R=V(N)/\sqrt{N}$  was established to correct the text-dependency of the results (Tweedy and Baayen, 1998).
- 6 Just fifty-seven of the function lemmas listed in Table 6 comprise the function words in Table 8. The twenty-one extant function lemmas are: þīn, witodlīce, forþāmþe, hwilc, twēgen, foran, manig, ēower, ælc, ūt, hwā, ongēan, gyt, hwī, betwux, git, hwær, þanon, twelf, intō, swilce.
- 7 As mentioned in the methodological procedure, the *entire* corpus contains a set of files from the *Toronto Corpus of Old English Dictionary* (see Appendix).
- 8 cwæþ 4061; godes 3463; god 3208; gode 2092; men(n) 1648; fæder 1467; hælend 1437; wearþ 1345; halgan 1301; þing 1248; dryhten 1170; c(w)om 1097; soþlice 1069; hæfde 1040; crist 1032; rice 986; geleafan 966; sunu 959; sona 892; cristes 865; het 849; cyning 836; mannum 787; eorþan 775; life 761; manna 754; sæde 750; word 712; lare 691; folc 673; sylf 671; dæge 660; lif 652; worulde 591; cwædon 591; hæfþ 578; witodlice 570; gast 553; mode 543; mod 536; geseah 535; micel 527; deaþe 505; swylce 503; lifes 500; criste 499; naman 495; heortan 483; eode 480; habban 466; don 466; willan 463; secge 458; mann 453; wurdon 443; stowe 443; wif 441; halga 439; wel 428; yfel 423; folce 420; tide 413;

ferde 406; gehaten 405; synna 402; lichaman 401; mannes 395; wuldres 146; wordum 146; bearn 123; ece 109; engla 99; foldan 97; wide 94; weard 91; waldend 91; halig 84; dryhtnes 82; ham 81; siþ 73; middangeard 73; ende 73; soþ 71; tid 70; hafaþ 70; fæste 70; wiht 68; secgan 67; monna 67; heofonum 67; þeoden 63; leoht 61; ful 60; frean 60; wera 58; helle 58; hæleþ 58; gumena 58; helm 57; ælmihtig 56; wuldre 55; ongan 55; frofre 55; hyrde 54; hæfdon 53; gewat 53; georne 53; feorh 51; dom 51; blæd 51.

- 9 Burrows warns of the convenience of tagging homographs to generate more accurate results, although Hoover (2003) considers unnecessary to take this prevention.
- 10 Note that allomorphs are separated by slashes.
- 11 Capital letters denote a similar/different ranking for the works tested (represented by ordinal numbers) that is, A = 1st; B = 1st and 2nd; C = 1st, 2nd, and 3rd; D = 1st but 2nd and 3rd alternate; E = 1st, 2nd, 3rd, and 4th; F = 1st, 2nd, 3rd, 4th and 5th; G = 1st, 2nd, but 3rd and 4th alternate; H = 5th and 6th; I = 5th, 6th, 7th, and 8th.

# **Appendix**

**Appendix: list of abbreviations** (archives from the *Toronto Complete Corpus of Old English Dictionary*).

Adrian and Ritheus (Ad); Ælfric's Catholic Homilies I (ÆCHom1); Ælfric's Catholic Homilies II (ÆCHom2); Homilies of Ælfric (Æhom1); Ælfric's Letters (Ælet); Alcuin De virtutibus et vitiis (Alc), Alexander's Letter to Aristotle (Alex); The Old English Apollonius of Tyre (AoT); The Rule of St. Benedict (BenR); The Rule of St. Benedict — Winteney Version (BenRW); Pastoral Care (CP); The Old English Gospel according to Saint John (Jn); The Old English Gospel according to Saint Luke (Lk); The Old English Gospel according to Saint Mark (Mk); The Old English Gospel according to Saint Matthew (Mt); The Old English Orosius (Or); Beowulf and minor poems (VRS); The Homilies of Wulfstan (Whom).