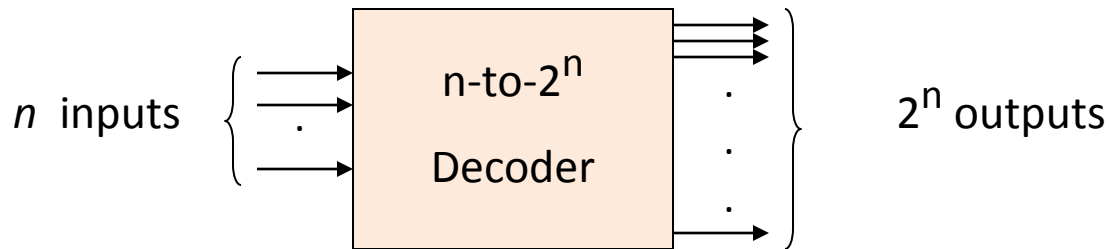


Sheet 5- Decoder and Multiplexer

Decoder



- A binary decoder is a combinational logic circuit that converts binary information from the n coded inputs to a maximum of 2^n unique outputs
- A decoder is a minterm generator
- Minterm of F = Maxterm of F'

Question 12(m)

- Design each of the following functions F using a decoder (*First decide the optimal size of the chip needed*)

$$m) F(W,X,Y,Z) = \sum_m (0,1,4,5,10,12,14)$$

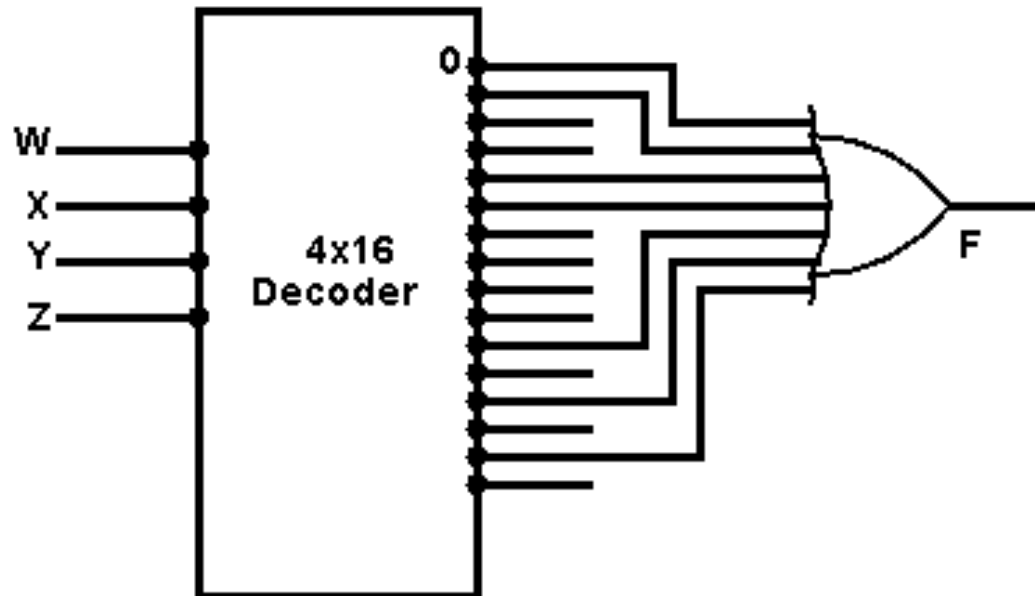
Using OR

Solution 12(m)

Number of inputs =4

So decoder size is $4 \times 2^4 = 4 \times 16$

$$F(W,X,Y,Z) = \sum_m (0,1,4,5,10,12,14)$$



Question 12(e)

- Design each of the following functions F using a decoder (*First decide the optimal size of the chip needed*)

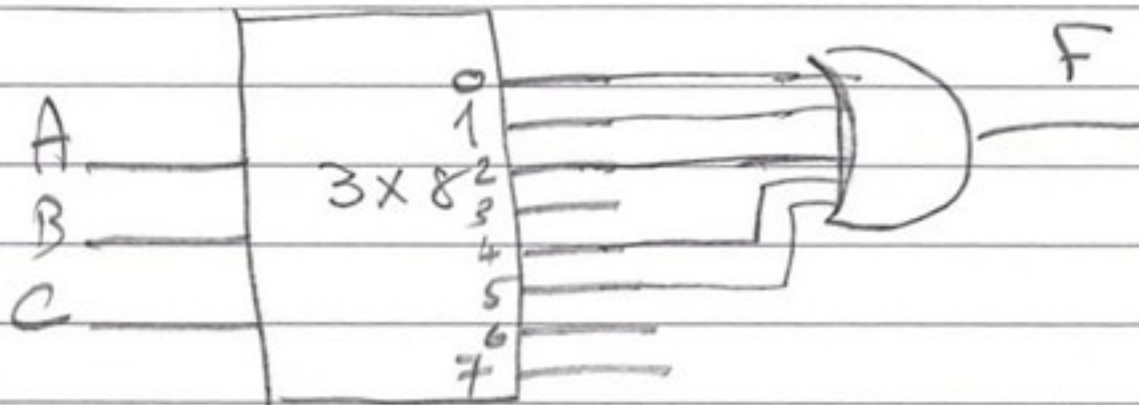
e) $F(A,B,C) = \prod_M (3,6,7)$

Question 12(e)

$$F(A, B, C) = \overline{\Pi M}(3, 6, 7) \\ = \Sigma m(0, 1, 2, 4, 5)$$

Using OR
OR \rightarrow min terms

OR \rightarrow min terms
3 inputs \rightarrow 3X8 decoder



Question 12(i)

- Design each of the following functions F using a decoder (*First decide the optimal size of the chip needed*)

i) $F(X, Y, Z) = X + Y(X + Z)(\bar{X} + \bar{Z})$

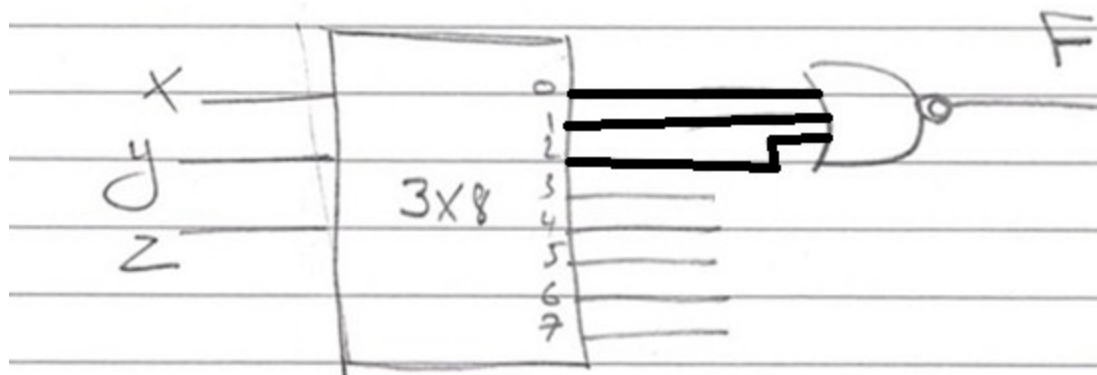
Question 12(i)

i) $F(x, y, z) = X + Y(X + Z)(\bar{X} + \bar{Z})$ → max terms (using NOR)
 $= X + Y(X\bar{X} + X\bar{Z} + \bar{X}Z + Z\bar{Z})$
 $= X + XY\bar{Z} + \bar{X}YZ$

$x \backslash yz$	00	01	11	10
0			1	
1	1	1	1	1

$F(x, y, z) = \Pi M(0, 1, 2)$

3 inputs → 3x8 decoder



Question 12(s)

- Design each of the following functions F using a decoder (*First decide the optimal size of the chip needed*)

s) $F(W, X, Y, Z) = (W + X + \bar{Y} + \bar{Z})(\bar{X} + \bar{Y} + Z)(\bar{W} + Y + \bar{Z})$

Question 12(s)

9) $F(w, x, y, z) = (\bar{w} + \bar{x} + \bar{y} + z)(\bar{x} + \bar{y} + z)(\bar{w} + y + \bar{z})$

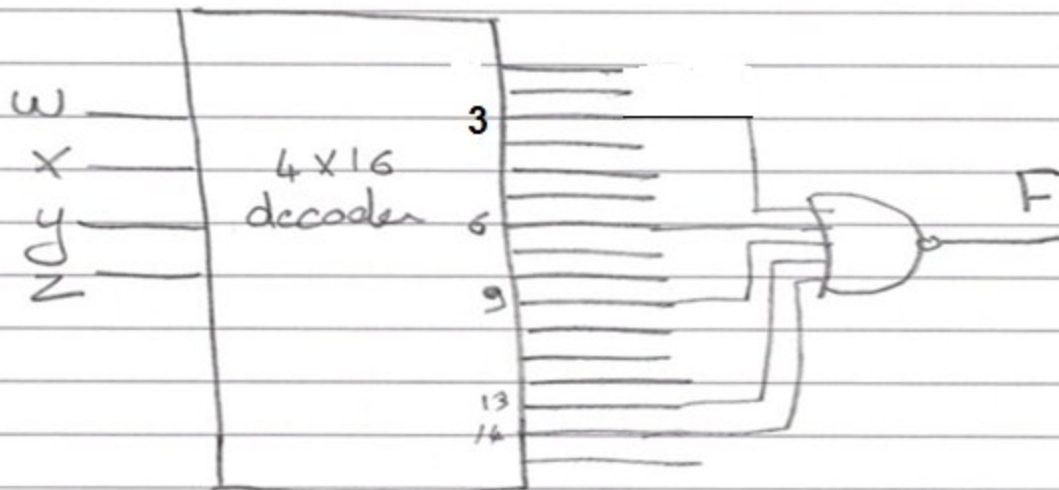
$w \backslash xz$	00	01	11	10
00	0	..
01	0
11	..	0	..	0
10	..	0

Using NOR

→ max terms

$$F(w, x, y, z) = \prod M(3, 6, 9, 13, 14)$$

4 inputs → 4x16 decoder

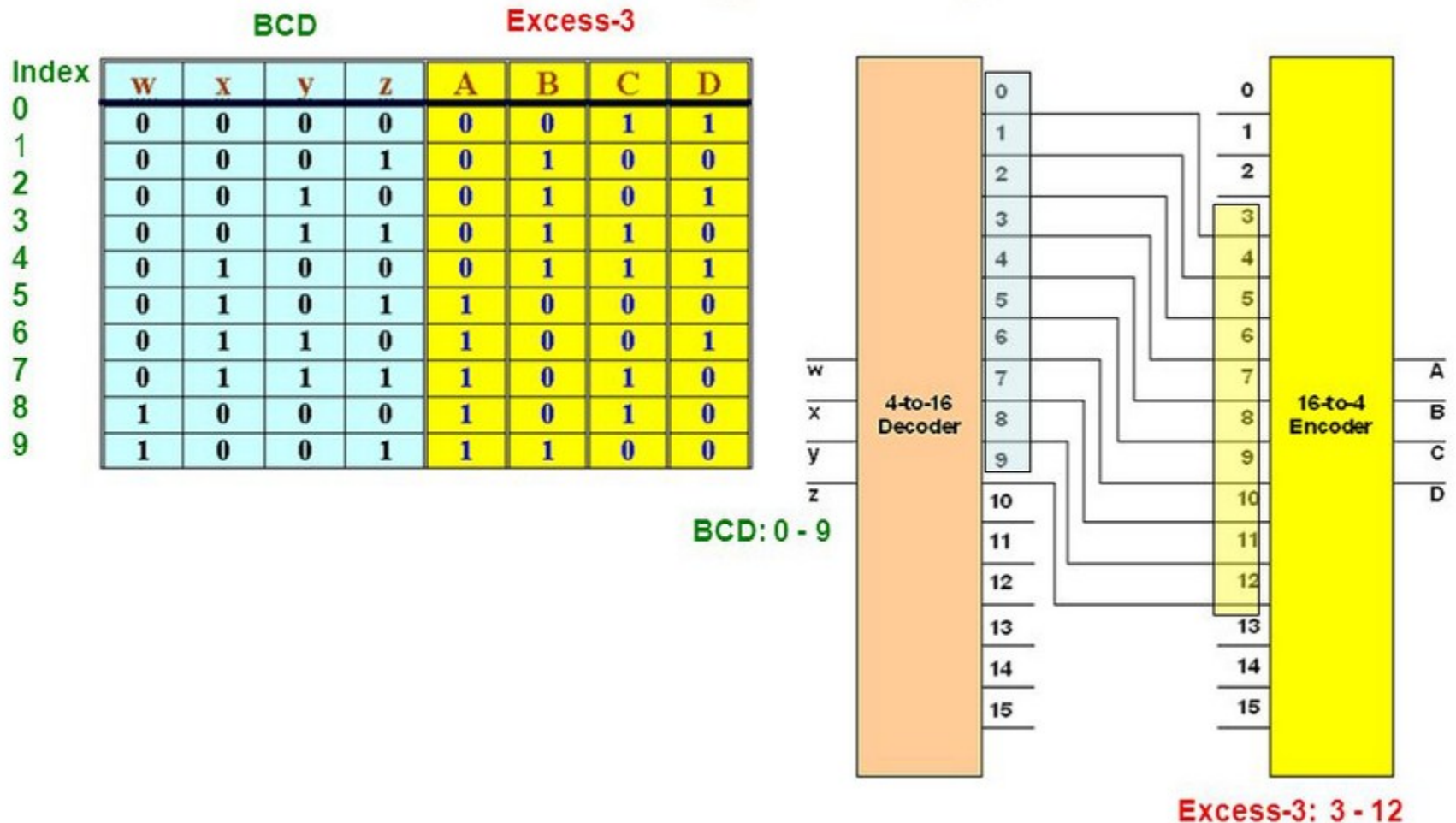


Question 14 covered in Lec.

14. Use a 4x16 decoder and a 16x4 encoder to convert a BCD number to excess-3.

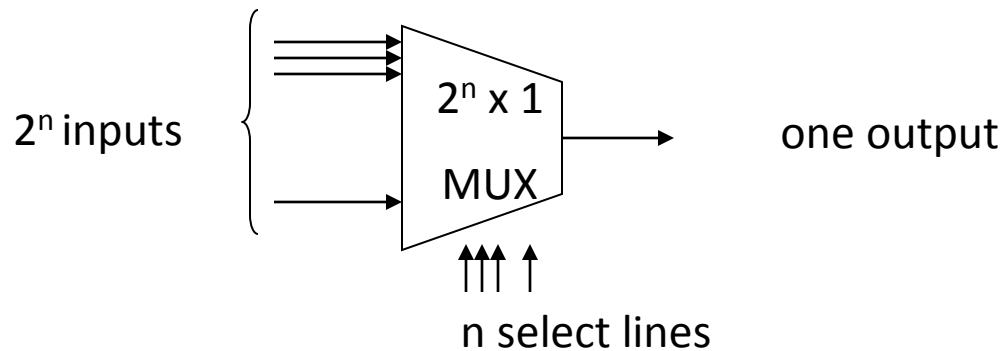
Question 14

14. Use a 4x16 decoder and a 16x4 encoder to convert a BCD number to excess-3.



Multiplexers

- Is a combinational circuit
- Has a single output
- Directs one of 2^n input to the output
- Input to output direction is done based on a set of n select bits



Question 17 (a)

17. Having two inputs A,B and a number of select lines and an output F. Design the following functions using a multiplexer (with the mentioned size) and any other gate you need:

a. If (S=0) then $F = \overline{A}$

If (S=1) then $F = A + B$

If (S=2) then $F = AB$

If (S=3) then $F = A \oplus B$

4x1 Multiplexer

Question 17 (a)

17. Having two inputs A,B and a number of select lines and an output F. Design the following functions using a multiplexer (with the mentioned size) and any other gate you need:

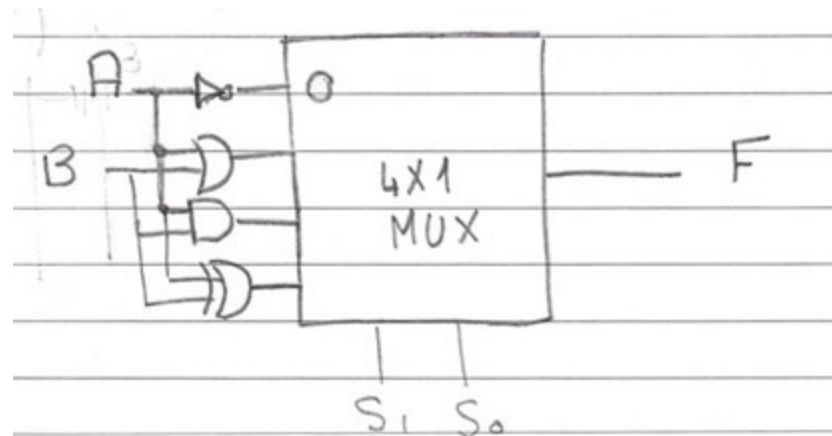
a. If (S=0) then $F = \bar{A}$

If (S=1) then $F = A+B$

If (S=2) then $F = AB$

If (S=3) then $F = A \oplus B$

4x1 Multiplexer



Question 15(q)

- Design each functions F in problem 12 using multiplexer (*First decide the optimal size of the chip needed*).

q) $F(A,B,C,D) = B\bar{C} + \bar{A}B + B\bar{C}\bar{D} + \bar{A}\bar{B}D + \bar{A}\bar{B}\bar{C}D$

Solution 15(q)

$$F(A,B,C,D) = B\bar{C} + \bar{A}B + B\bar{C}\bar{D} + \bar{A}B\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D}$$

Number of inputs =4

So Number of the multiplexer Selectors =

$$\text{Number of inputs} - 1 = 4 - 1 = 3$$

So Number of the Inputs' multiplexer is $2^3=8$

So Size of the multiplexer = 8x1

We need to get the truth table of the function.
The easiest way is to get the minterms using k-map.

Solution 15(q)

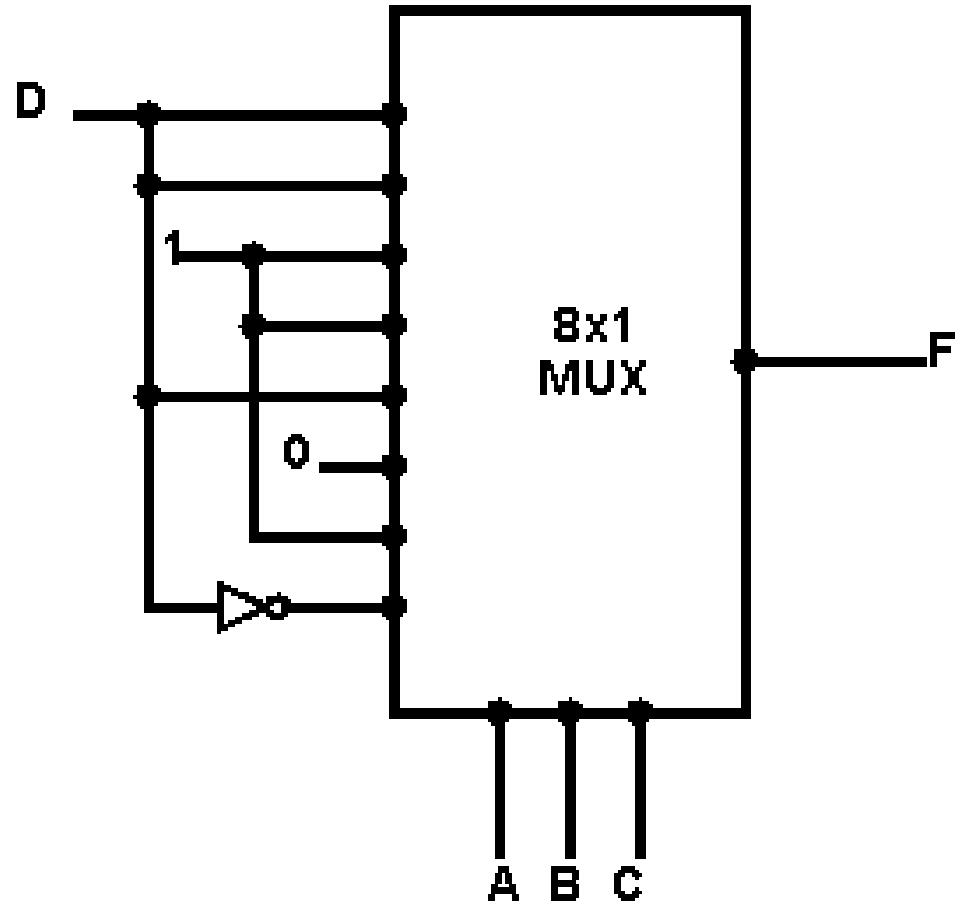
$$F(A,B,C,D) = B\bar{C} + \bar{A}B + B\bar{C}\bar{D} + \bar{A}B\bar{D} + \bar{A}\bar{B}\bar{C}D$$

		CD			
		00	01	11	10
AB	00		1	1	
	01	1	1	1	1
	11	1	1		1
	10		1		

$$F(A,B,C,D) = \sum_m (1,3,4,5,6,7,9,12,13,14)$$

Solution 15(q)

	A	B	C	D	F	
0	0	0	0	0	0	$F=D$
1	0	0	0	1	1	
2	0	0	1	0	0	$F=D$
3	0	0	1	1	1	
4	0	1	0	0	1	$F=1$
5	0	1	0	1	1	
6	0	1	1	0	1	$F=1$
7	0	1	1	1	1	
8	1	0	0	0	0	$F=D$
9	1	0	0	1	1	
10	1	0	1	0	0	$F=0$
11	1	0	1	1	0	
12	1	1	0	0	1	$F=1$
13	1	1	0	1	1	
14	1	1	1	0	1	$F=D'$
15	1	1	1	1	0	



Question 15(I)

- Design the below function F using 4*1 multiplexer
- I) $F(A,B,C,D) = \sum_m (0,5,8,9,11,12,13,14)$

Question 15(I)

Sometimes they ask for a specific size of MUX to be used e.g. for

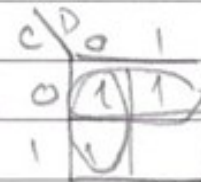
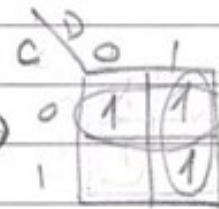
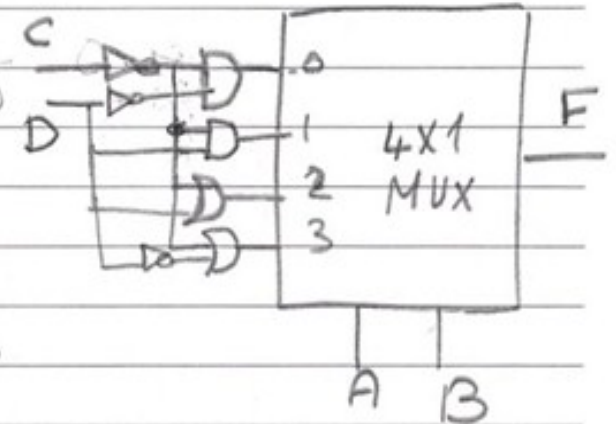
$$F(A, B, C, D) = \sum m(0, 5, 8, 9, 11, 12, 13, 14)$$

The optimal size to be used is 8×1

It is needed to build it using 4×1 MUX

Question 15(I)

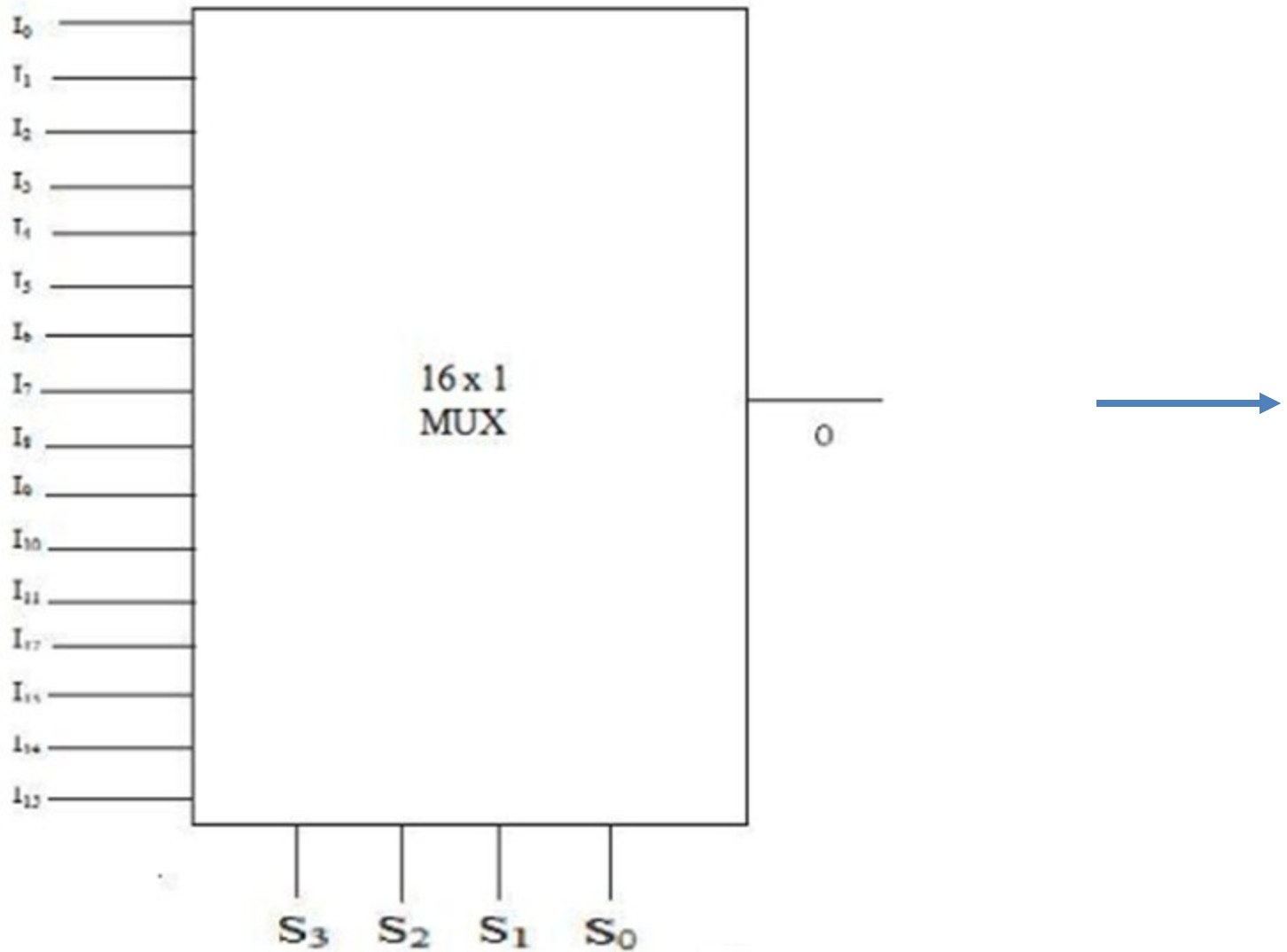
Used as Selectors	A	B	C	D	F	
0	0	0	0	0	1	
1	0	0	0	1	0	$F = \bar{C}\bar{D}CD$
2	0	0	1	0	0	
3	0	0	1	1	0	
4	0	1	0	0	0	
5	0	1	0	1	1	$F = E\bar{C}D$
6	0	1	1	0	0	
7	0	1	1	1	0	
8	1	0	0	0	1	
9	1	0	0	1	1	$F = \bar{E} + D$
10	1	0	1	0	0	
11	1	0	1	1	1	
12	1	1	0	0	1	
13	1	1	0	1	1	$F = \bar{E} + \bar{D}$
14	1	1	1	0	1	
15	1	1	1	1	0	



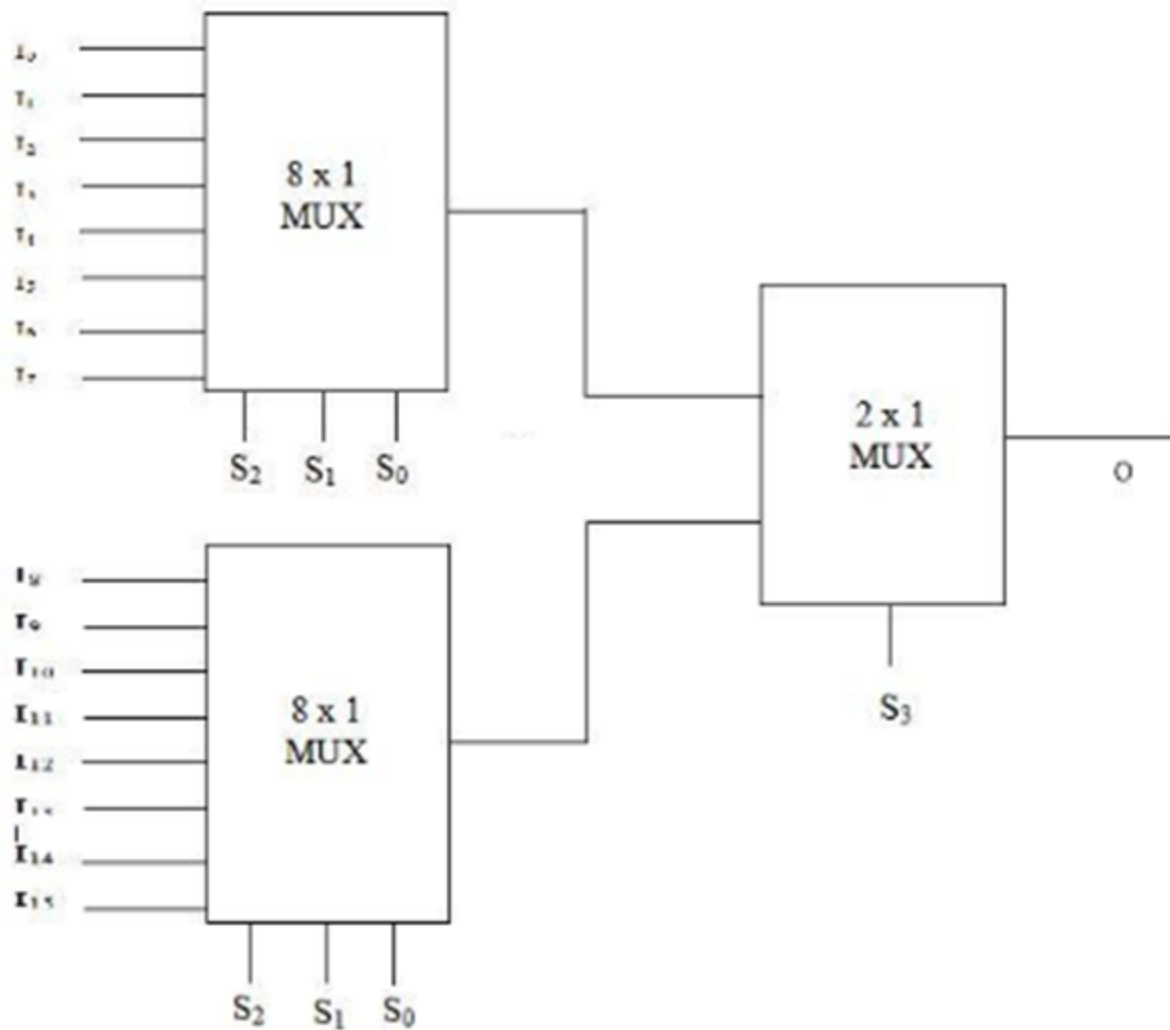
Question 16

- Construct a 16x1 multiplexer using two 8x1 and one 2x1 multiplexers

Solution 16



Solution 16



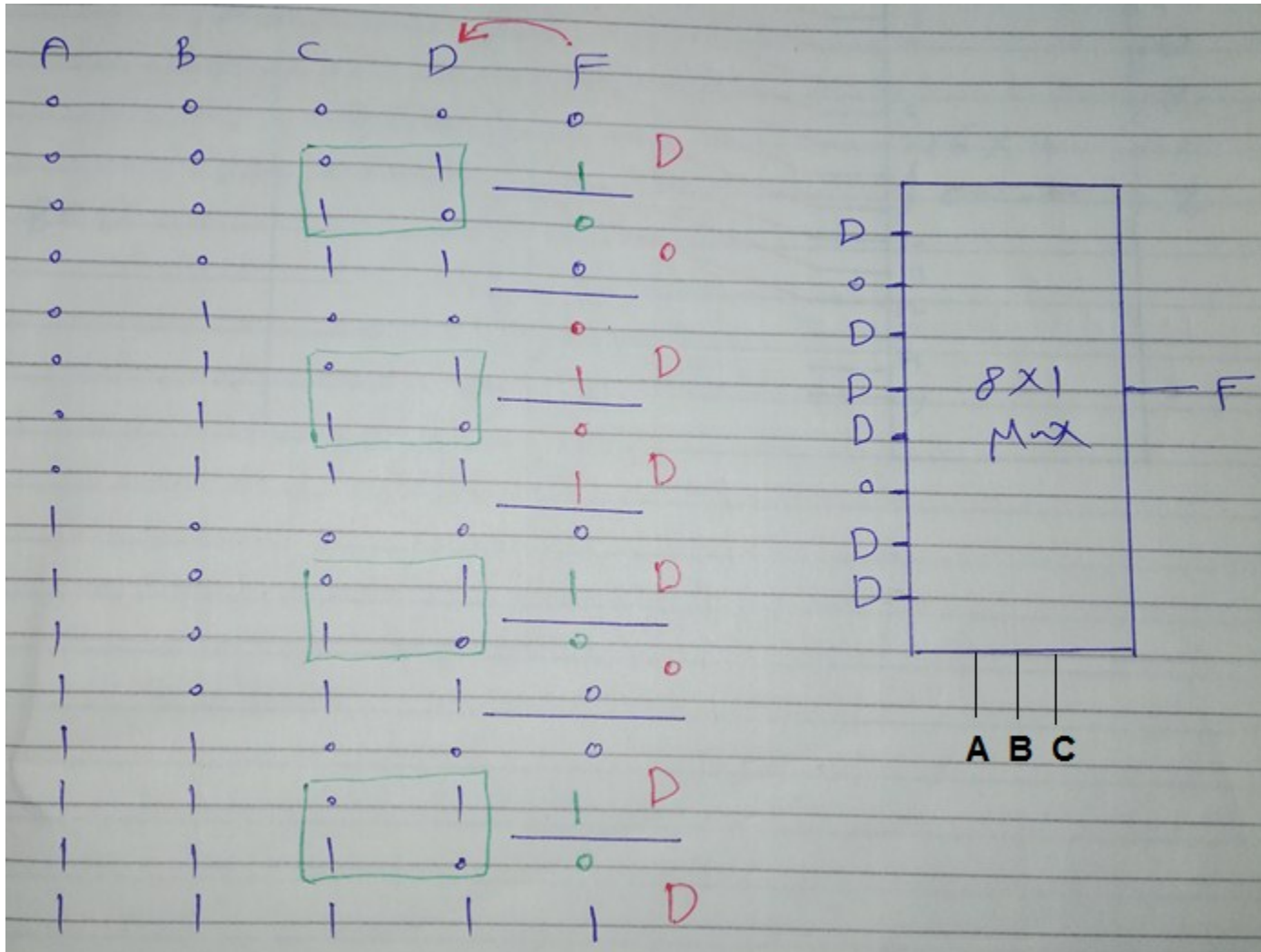
Question 18(k)

18. Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (*First determine its optimal size*):

k. If $(A=0 \text{ and } B=1 \text{ or } C \neq D)$ then $F=D$ else $F=ABC$

Question 18(k)

k. If $(A=0 \text{ and } B=1 \text{ or } C \neq D)$ then $F=D$ else $F=ABC$



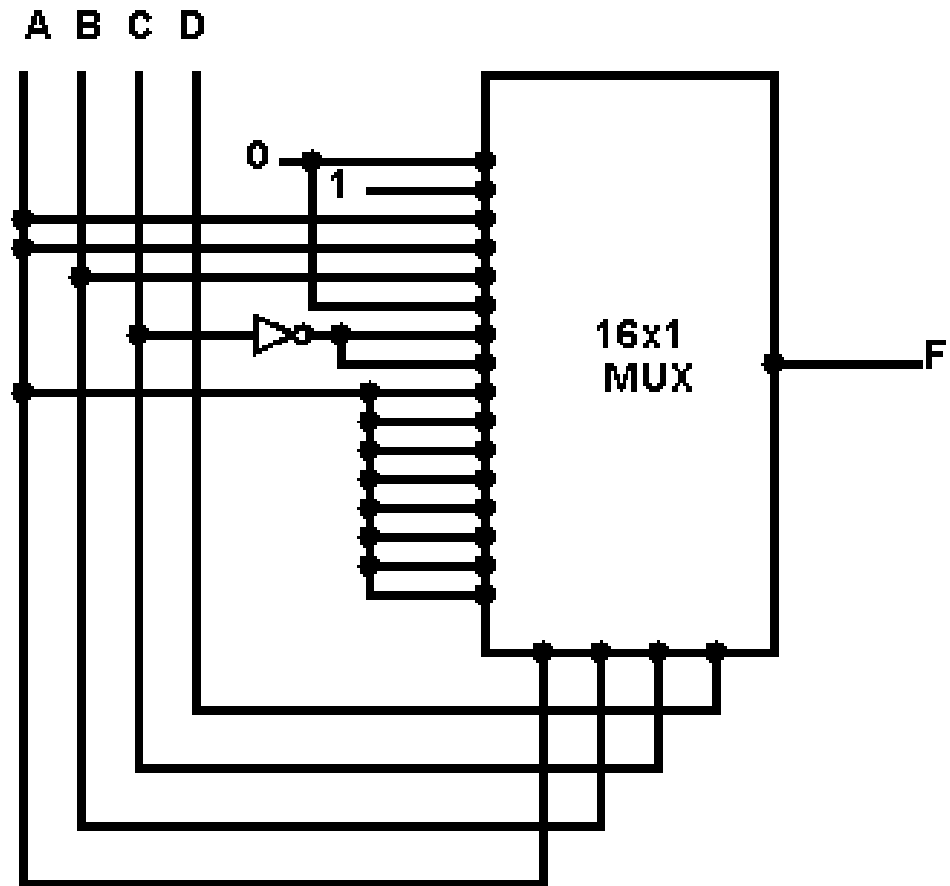
Question 18 (c)

Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (First determine its optimal size)

A	B	C	D	F
0	0	0	0	0
0	0	0	1	1
0	0	1	X	A
0	1	0	0	B
0	1	0	1	0
0	1	1	X	C'
1	X	X	X	A

Solution 18(c)

	A	B	C	D	F
0	0	0	0	0	0
1	0	0	0	1	1
2	0	0	1	0	A
3	0	0	1	1	A
4	0	1	0	0	B
5	0	1	0	1	0
6	0	1	1	0	C'
7	0	1	1	1	C'
8	1	0	0	0	A
9	1	0	0	1	A
10	1	0	1	0	A
11	1	0	1	1	A
12	1	1	0	0	A
13	1	1	0	1	A
14	1	1	1	0	A
15	1	1	1	1	A

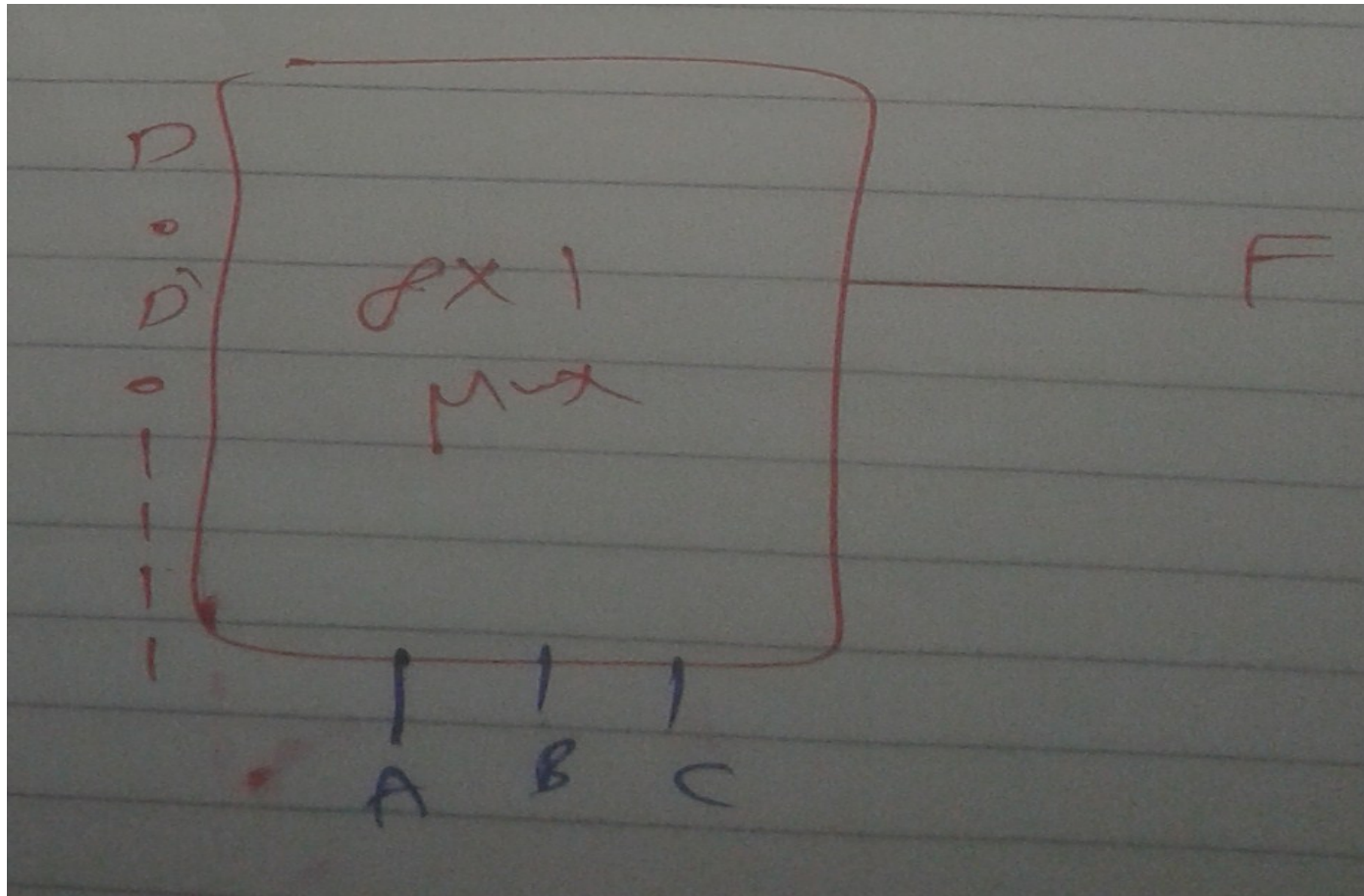


as F column includes variables not only ones and zeros so in this case Dr. allow you to consider No. of selectors = No. of inputs.

Solution 18(c)

	A	B	C	D	F	
0	0	0	0	0	0	
1	0	0	0	1	1	D
<hr/>						
A	0	0	1	0	0	0
	0	0	1	1	0	
<hr/>						
B	0	1	0	0	1	
0	0	1	0	1	0	D'
<hr/>						
C'	0	1	1	0	0	0
	0	1	1	1	0	
<hr/>						
A	1	0	0	0	1	1
	1	0	0	1	1	
	1	0	1	0	1	1
	1	0	1	1	1	
	1	1	0	0	1	1
	1	1	0	1	1	
	1	1	1	1	1	1
	1	1	1	0	1	

Solution 18(c)



Question 18(g)

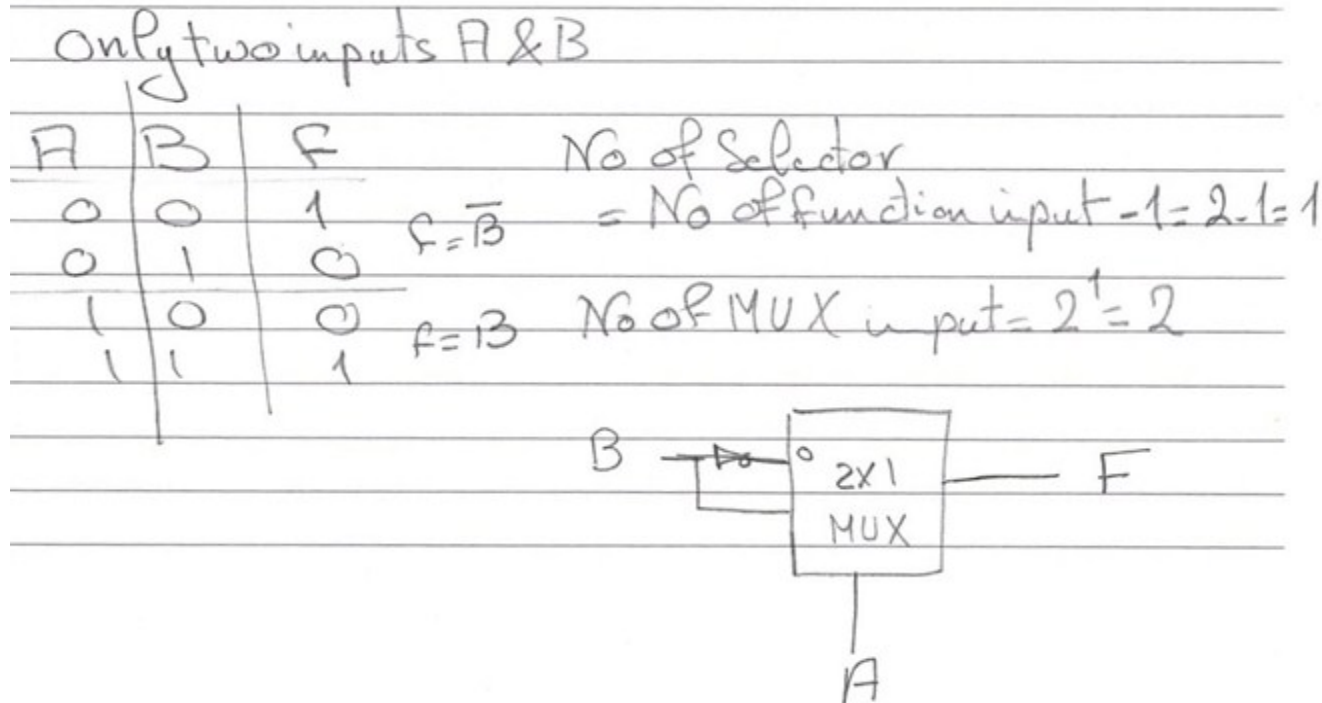
18. Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (*First determine its optimal size*):

g. If $(A \diamond B)$ then $F=0$ else $F=1$

Question 18(g)

18. Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (*First determine its optimal size*):

g. If $(A \diamond B)$ then $F=0$ else $F=1$



Question 18(I)

18. Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (*First determine its optimal size*):

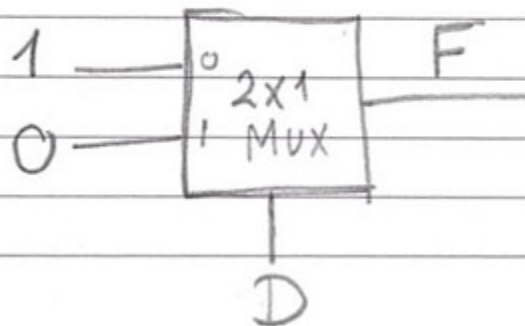
I. If (ABCD is an odd number) $F=0$ else $F=1$

Question 18(I)

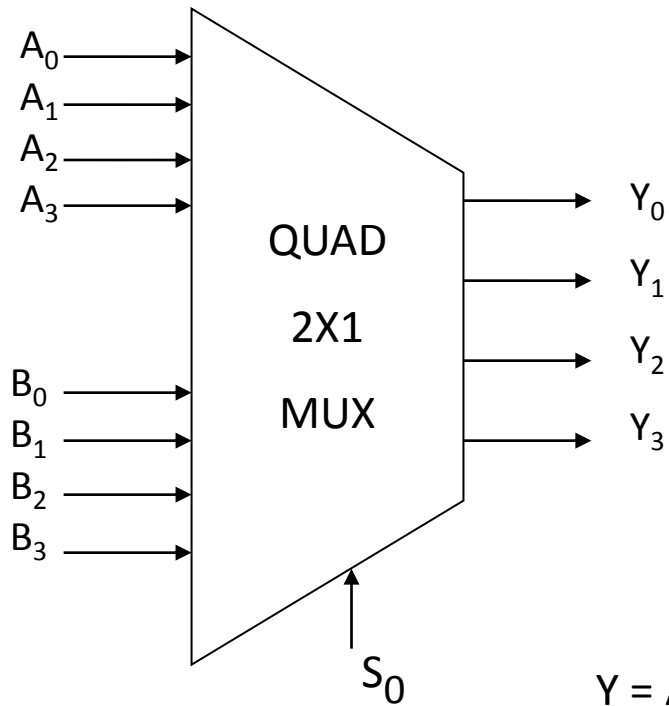
18. Having a number of four digits A,B,C,D and an output F, use a multiplexer to design the following functions (*First determine its optimal size*):

I. If (ABCD is an odd number) $F=0$ else $F=1$

(e) $ABCD$ is odd if $D=1$ } so only one var controls
is even if $D=0$ } the O/P

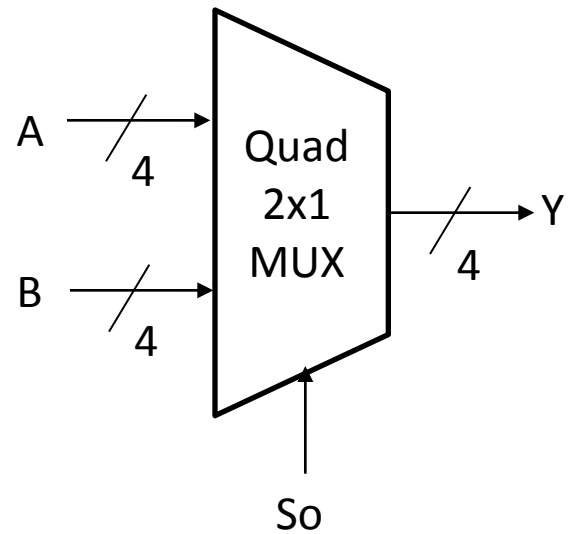


Quad 2x1 MUX



$Y = A$ if $S_0 = 0$

$Y = B$ if $S_0 = 1$

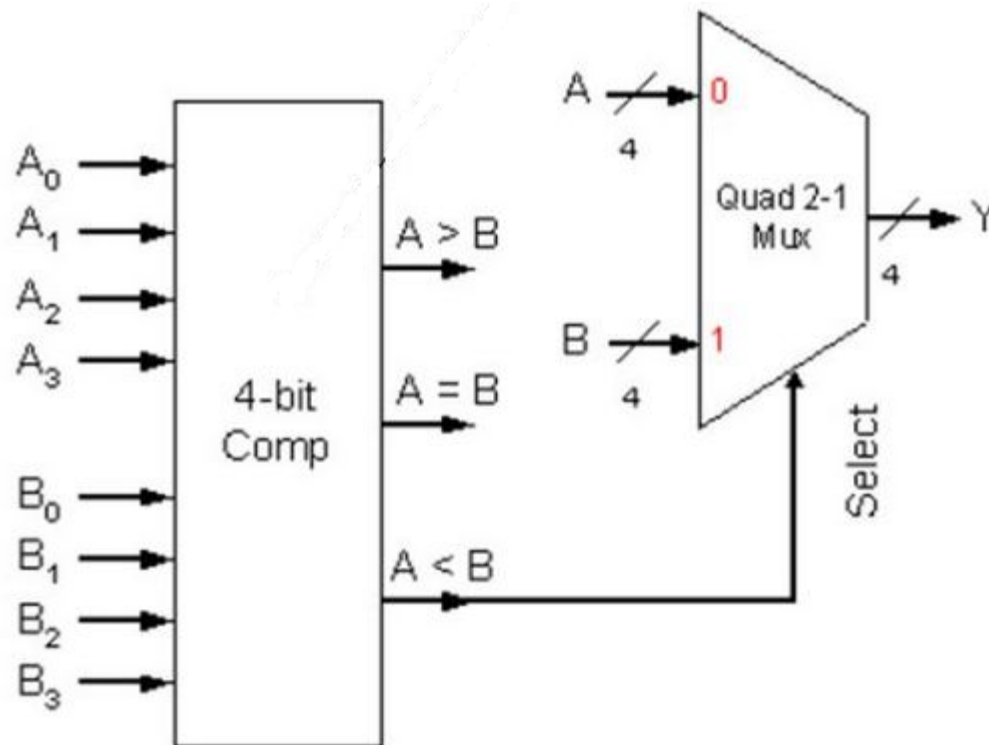


Question 19

19. Using a 4-bit comparator and a Quad 2-1 multiplexer, design a circuit that outputs the larger of two numbers.

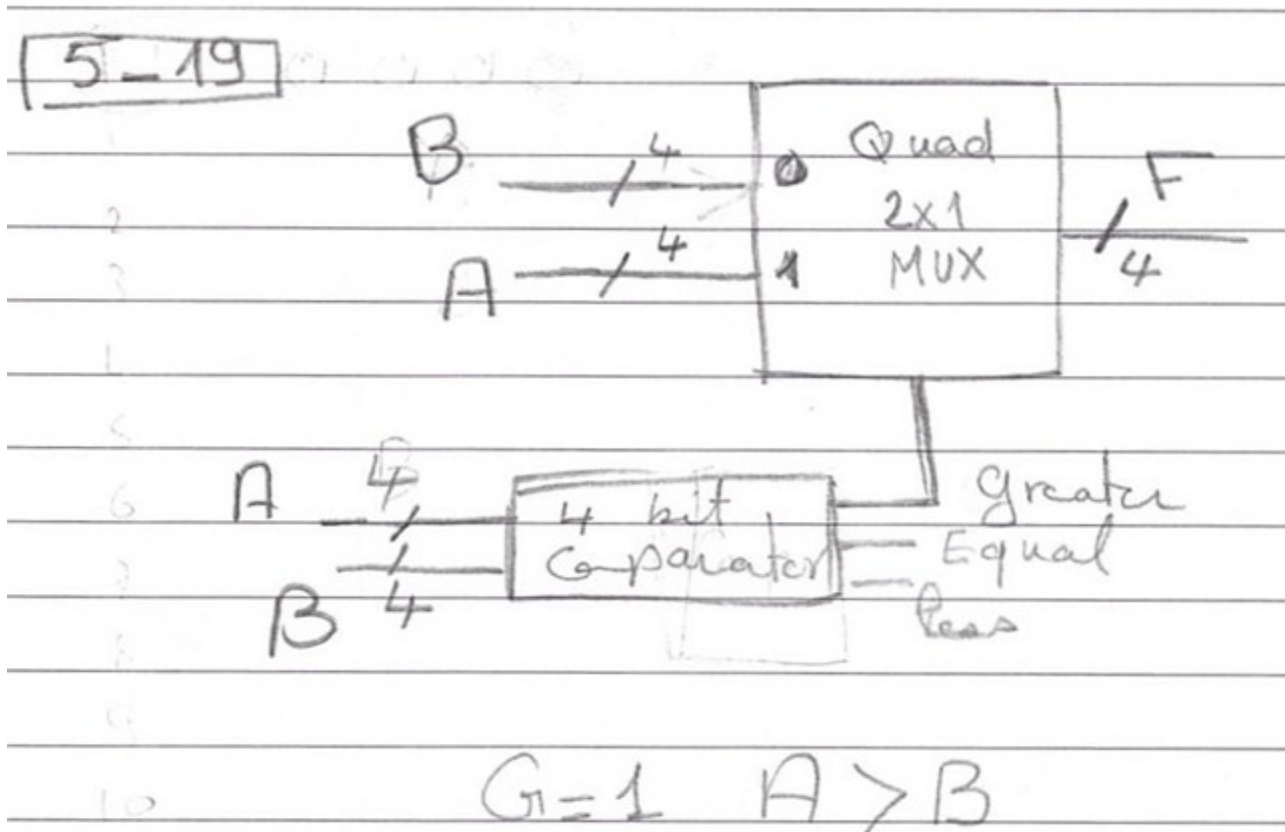
Question 19

19. Using a 4-bit comparator and a Quad 2-1 multiplexer, design a circuit that outputs the larger of two numbers.



Question 19

19. Using a 4-bit comparator and a Quad 2-1 multiplexer, design a circuit that outputs the larger of two numbers.



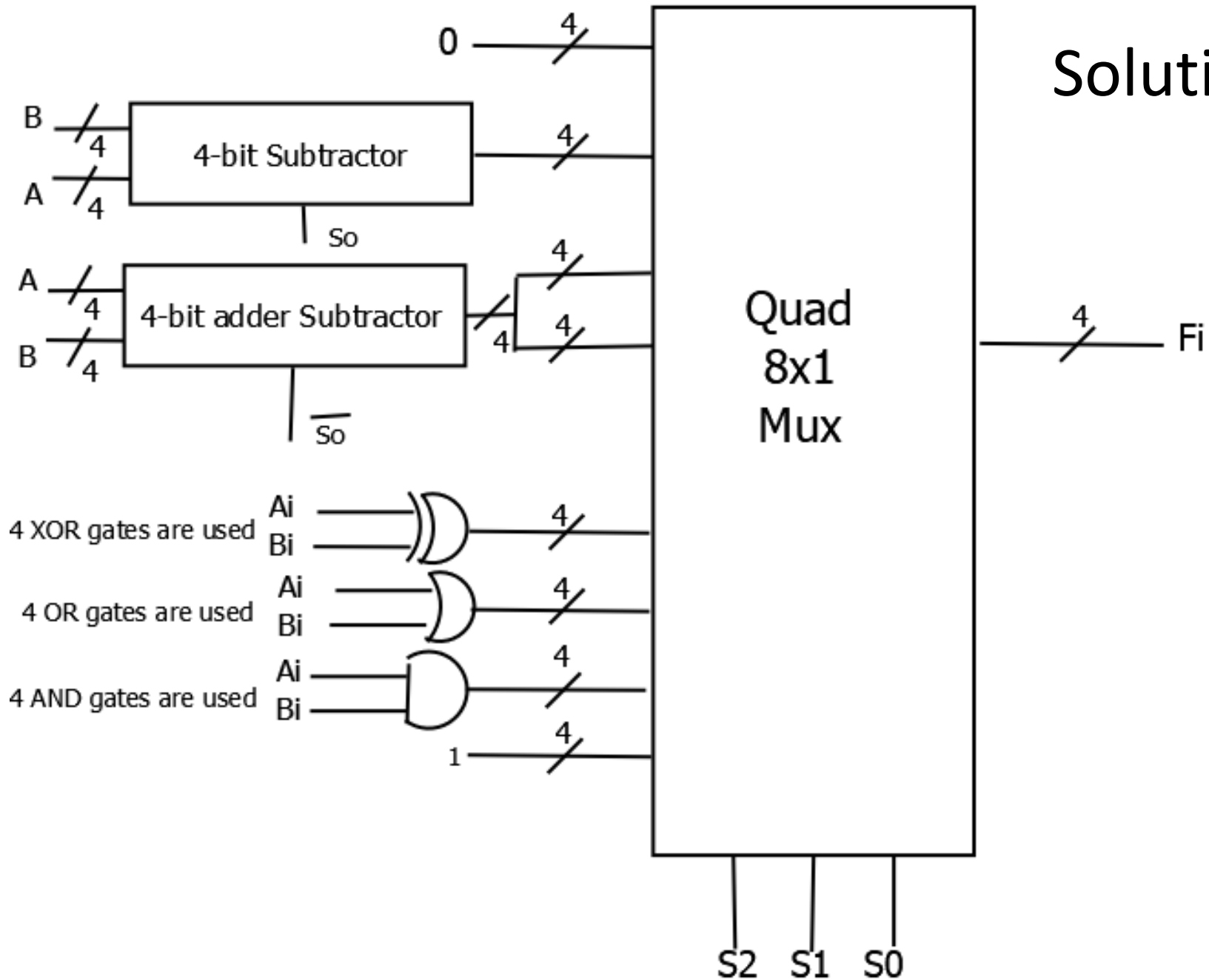
Question 21

Using Quad 8x1 multiplexer to build the functions in this table, where A, B and F are 4-bit I/O.

Inputs			Functions
S ₂	S ₁	S ₀	
0	0	0	F=0000
0	0	1	F=B minus A (B-A)
0	1	0	F=A minus B (A-B)
0	1	1	F=A plus B (A+B)
1	0	0	F=A XOR B
1	0	1	F=A OR B
1	1	0	F=A AND B
1	1	1	F=1111

8 inputs means 3 Selectors
Quad means each input is 4 bits, also the output is 4 bits

Solution 21



Revision

Having a Boolean function $F(A, B, C) = \bar{A}C + B\bar{C}$, without simplification, do the following:

- Construct the full truth table, then list the minterms, maxterms
- Draw the logic diagram of F.

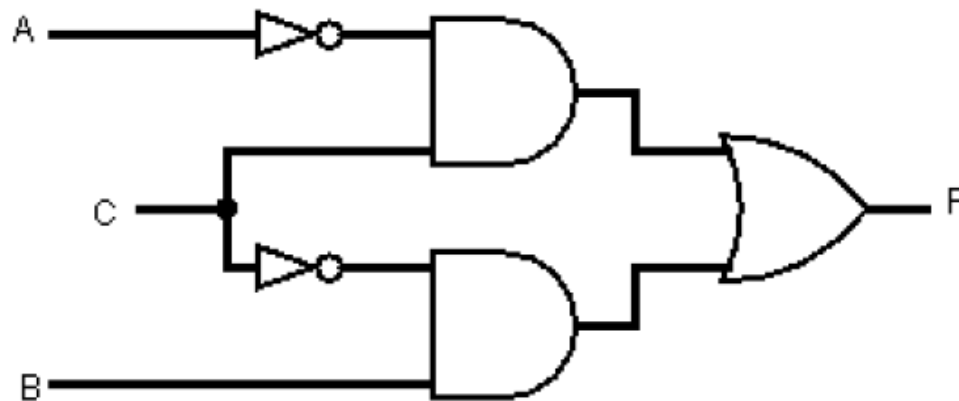
Having a Boolean function $F(A, B, C) = \bar{A}C + B\bar{C}$, without simplification, do the following:

- Construct the full truth table, then list the minterms, maxterms
- Draw the logic diagram of F.

	A	B	C	\bar{A}	$\bar{A}C$	\bar{C}	$B\bar{C}$	F
0	0	0	0	1	0	1	0	0
1	0	0	1	1	1	0	0	1
2	0	1	0	1	0	1	1	1
3	0	1	1	1	1	0	0	1
4	1	0	0	0	0	1	0	0
5	1	0	1	0	0	0	0	0
6	1	1	0	0	0	1	1	1
7	1	1	1	0	0	0	0	0

$$F(A, B, C) = \sum m(1, 2, 3, 6)$$

$$F(A, B, C) = \prod M(0, 4, 5, 7)$$



Having a Boolean function $F(A, B, C) = (\bar{A} + C)(B + \bar{C})$, without simplification, do the following:

- Construct the full truth table, then list the minterms, maxterms
- Draw the logic diagram of F.

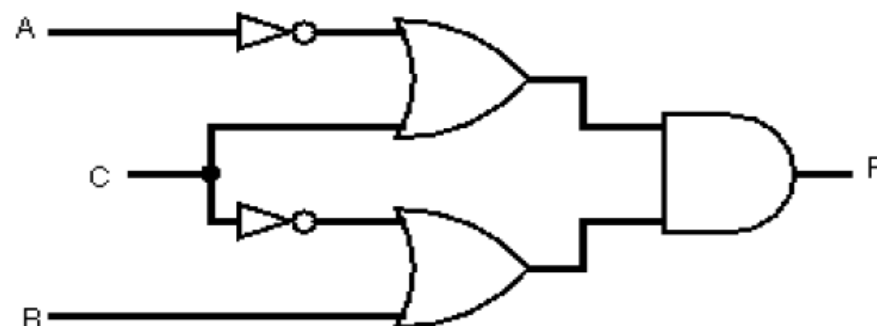
Having a Boolean function $F(A, B, C) = (\bar{A} + C)(B + \bar{C})$, without simplification, do the following:

- Construct the full truth table, then list the minterms, maxterms
- Draw the logic diagram of F.

	A	B	C	\bar{A}	$\bar{A} + C$	\bar{C}	$B + \bar{C}$	F
0	0	0	0	1	1	1	1	1
1	0	0	1	1	1	0	0	0
2	0	1	0	1	1	1	1	1
3	0	1	1	1	1	0	1	1
4	1	0	0	0	0	1	1	0
5	1	0	1	0	1	0	0	0
6	1	1	0	0	0	1	1	0
7	1	1	1	0	1	0	1	1

$$F(A, B, C) = \sum m(0, 2, 3, 7)$$

$$F(A, B, C) = \prod M(1, 4, 5, 6)$$



Use a K-map to simplify the following Boolean function as a Sum of Product:

$$F(A, B, C, D) = \pi_M(1, 3, 6, 9, 11, 12, 14)$$

Use a K-map to simplify the following Boolean function as a Sum of Product:

$$F(A, B, C, D) = \pi_M(1, 3, 6, 9, 11, 12, 14)$$

CD	00	01	11	10
AB				
00	1			1
01	1	1	1	
11		1	1	
10	1			1

$$F = A'BC' + BD + B'D'$$

OR $F = A'C'D' + BD + B'D'$

Simplify function in Product-of-Sum form using k-maps:

$$F(A,B,C) = A'B'C + AB'C' + BC$$

Simplify function in Product-of-Sum form using k-maps:

$$F(A,B,C) = A'B'C + AB'C' + BC$$

A/BC	00	01	11	10
0	0	1	1	0
1	1	0	1	0

$$F = (A+C)(B'+C)(A'+B+C')$$

Using tabular method, simply $F(A, B, C) = AB + BC' + C + A'$

Using tabular method, simply $F(A, B, C) = AB + BC' + C + A'$

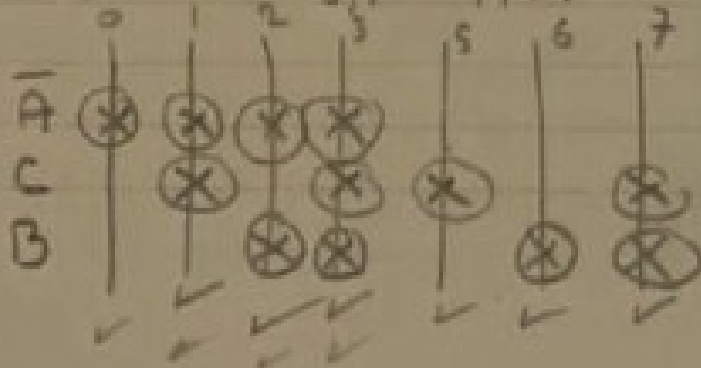
4. Using tabular method, simply $F(A, B, C) = AB + BC' + C + A'$ (5 marks)

A	BC			
	00	01	11	10
0	1	1	1	1
1		1	1	1

$$F(A, B, C) = \sum_m (0, 1, 2, 3, 5, 6, 7)$$

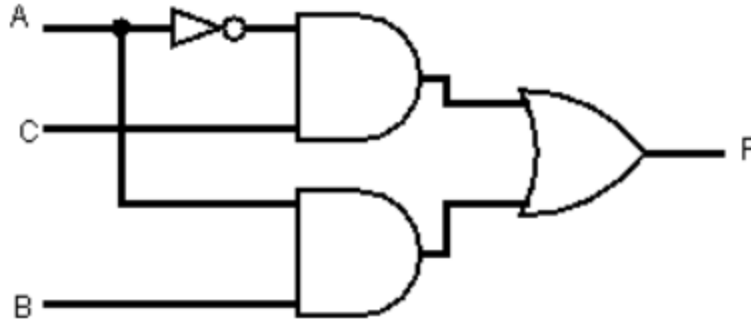
000, 001, 010, 011, 101, 110, 111

0	000✓	0,1	00-✓	0,1,2,3	0-- \bar{A}
1	001✓	0,2	0-0✓	0,2,1,3	0--
2	010✓	1,3	0-1✓	1,3,5,7	--1 C
3	011✓	1,5	-01✓	1,3,3,7	--1
5	101✓	2,3	01-✓	2,3,6,7	-1- B
6	110✓	2,6	-10✓	2,6,3,7	-1-
7	111✓	3,7	-11✓		
		5,7	1-1✓		
		6,7	11-✓		

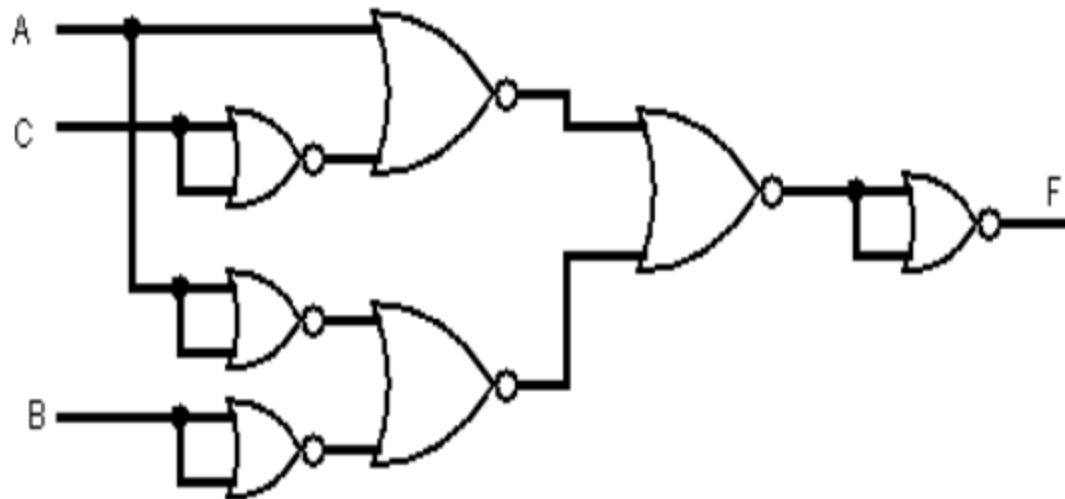
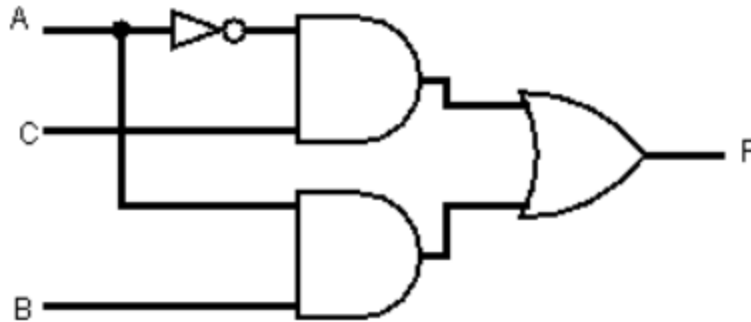


$$F(A, B, C) = C + B + \bar{A}$$

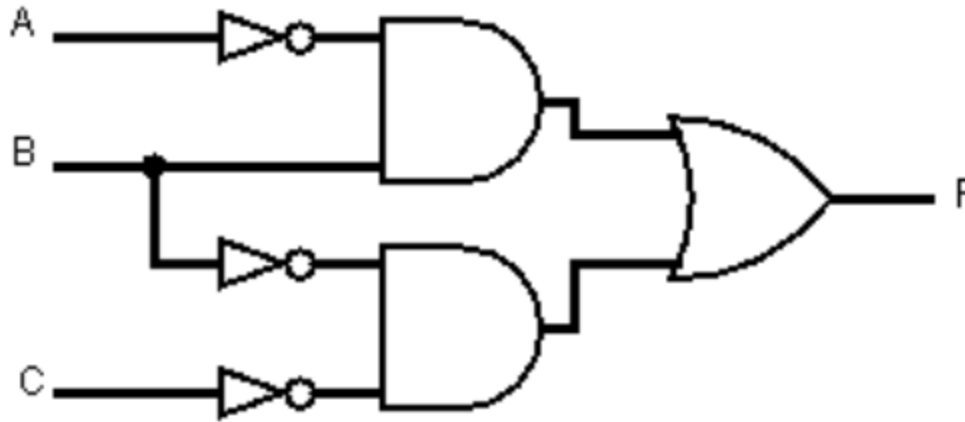
Build the following function using only NORs



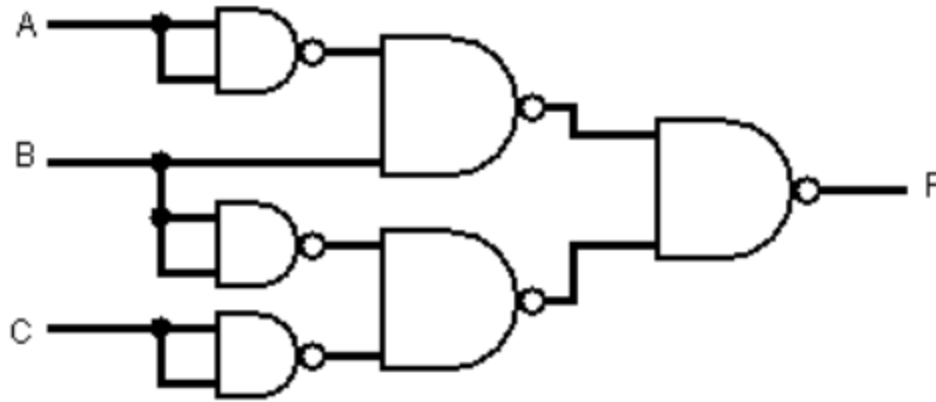
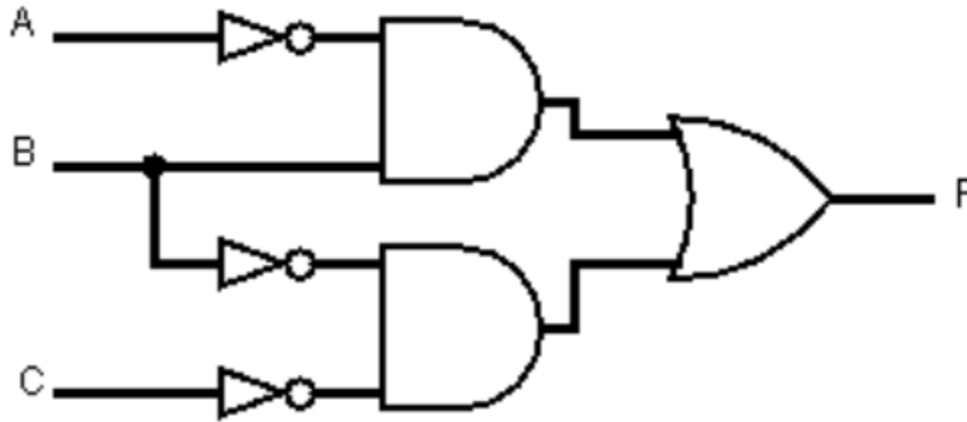
Build the following function using only NORs



Build the following function using only NANDs



Build the following function using only NANDs



**Design a logic circuit
to translate a BCD code to
a 2421 code.**

Design a logic circuit to translate a **BCD** code to a **2421** code.

- Step 1: how many inputs and how many outputs?
 - four inputs and four outputs
- Step 2: – Obtain the truth table
- Step 3: Obtain simplified Boolean expression for each output
- Step 4: Draw the logic diagram

Inputs					Outputs			
BCD					2421			
	A	B	C	D	x	y	z	t
0	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	1
2	0	0	1	0	0	0	1	0
3	0	0	1	1	0	0	1	1
4	0	1	0	0	0	1	0	0
5	0	1	0	1	1	0	1	1
6	0	1	1	0	1	1	0	0
7	0	1	1	1	1	1	0	1
8	1	0	0	0	1	1	1	0
9	1	0	0	1	1	1	1	1

- Step 3: Obtain simplified Boolean expression for each output
- Output x:

A	B	C	D	x
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
The rest				x

AB \ CD	CD			
	00	01	11	10
00	0	0	0	0
01	0	1	1	1
11	X	X	X	X
10	1	1	X	X

$$x = BD + BC + A$$

• Output y:

CD \ AB	00	01	11	10
00	0	0	0	0
01	1	0	1	1
11	X	X	X	X
10	1	1	X	X

$$y = A + BD' + BC$$

A	B	C	D	y
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
The rest				X

• Output z:

CD \ AB	00	01	11	10
00	0	0	1	1
01	0	1	0	0
11	X	X	X	X
10	1	1	X	X

$$z = A + B'C + BC'D$$

A	B	C	D	z
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
The rest				X

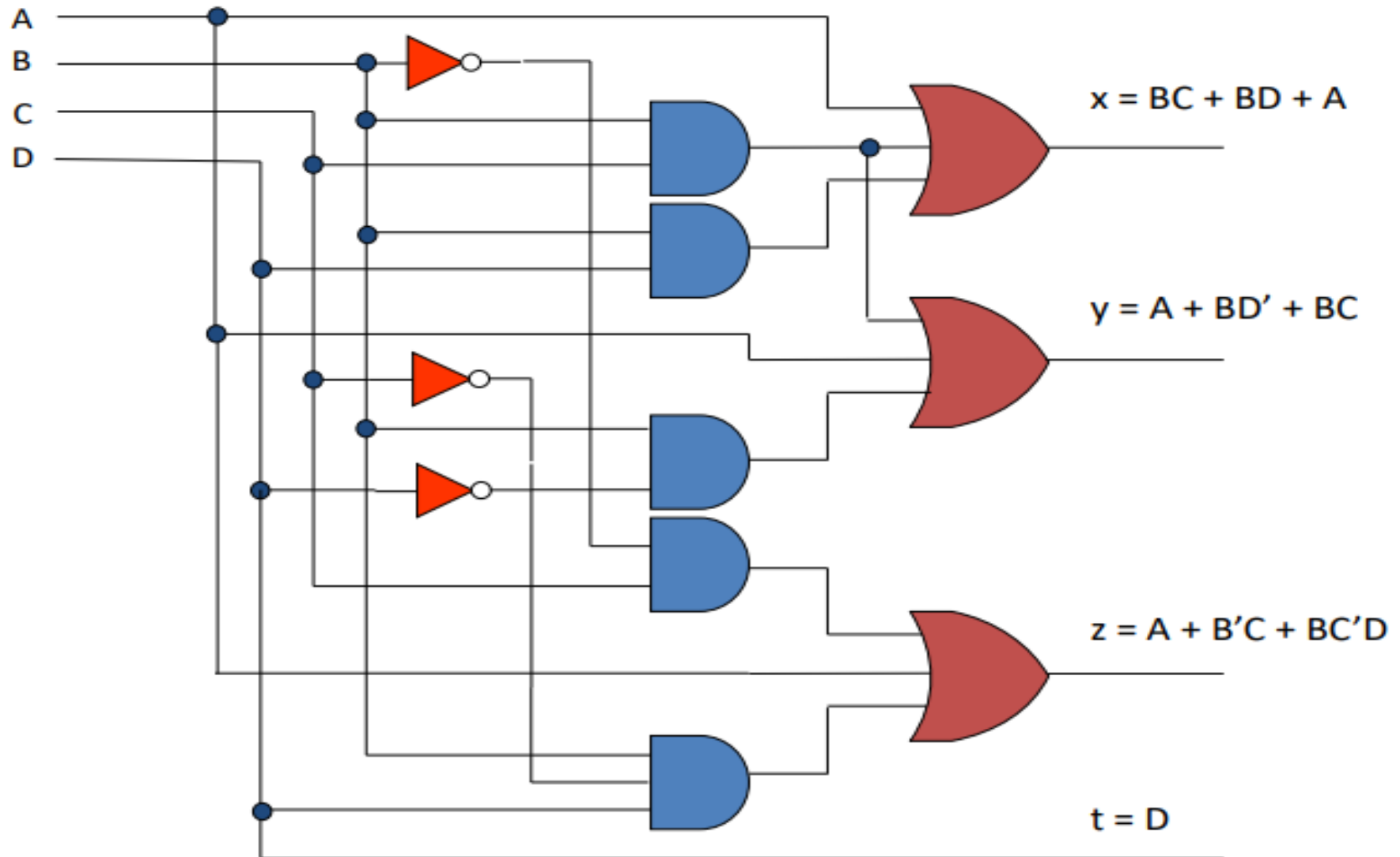
- Output t:

CD \ AB	00	01	11	10
00	0	1	1	0
01	0	1	1	0
11	X	X	X	X
10	0	1	X	X

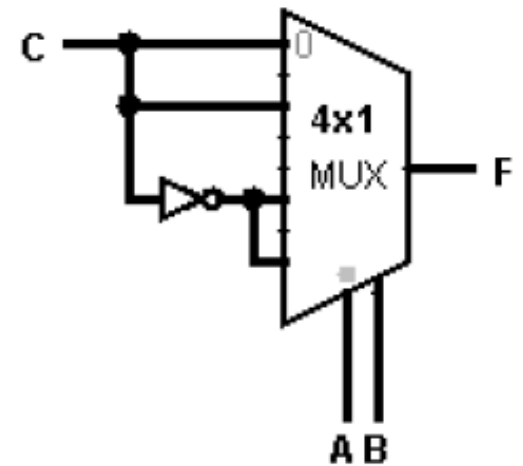
$$t = D$$

A	B	C	D	T
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
The rest				X

Logic Diagram

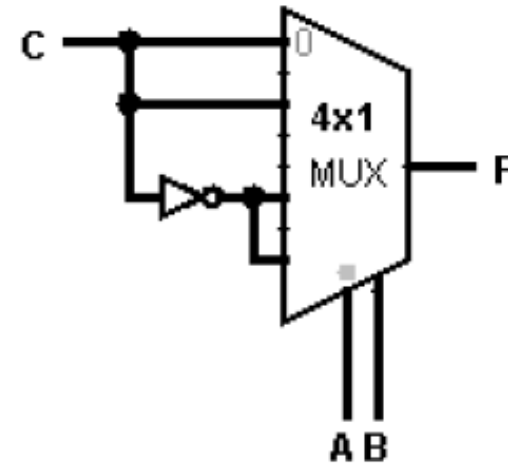
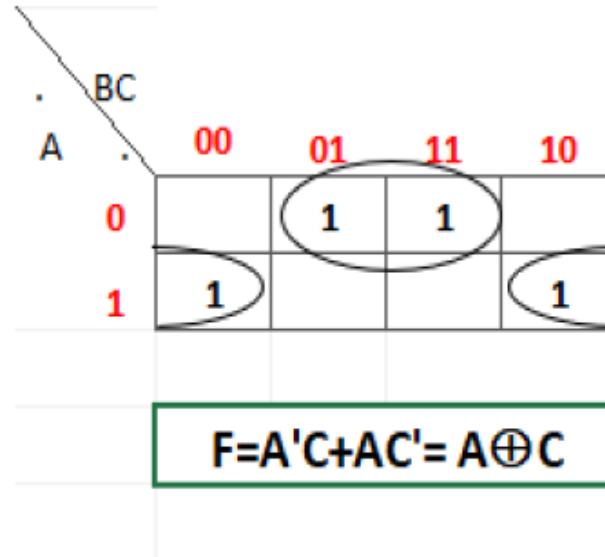


Derive a function $F(A,B,C)$ using a single gate.



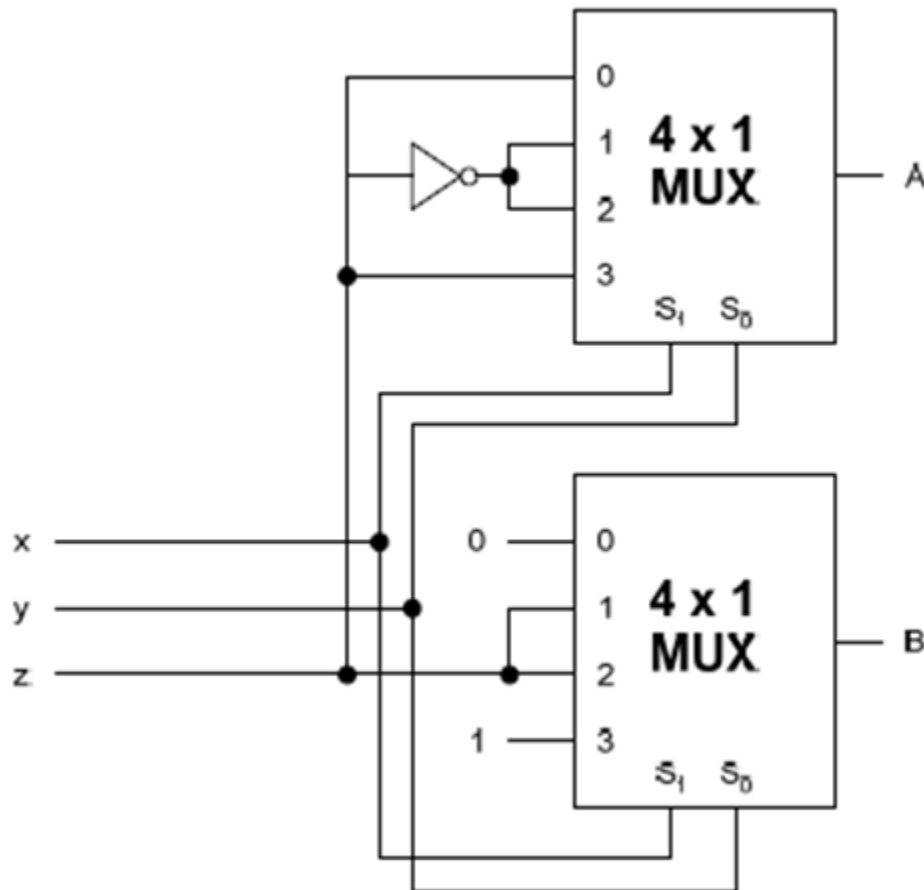
Derive a function $F(A,B,C)$ using a single gate.

	A	B	C	F	
0	0	0	0	0	$F=C$
1	0	0	1	1	
2	0	1	0	0	$F=C$
3	0	1	1	1	
4	1	0	0	1	$F=C'$
5	1	0	1	0	
6	1	1	0	1	$F=C'$
7	1	1	1	0	



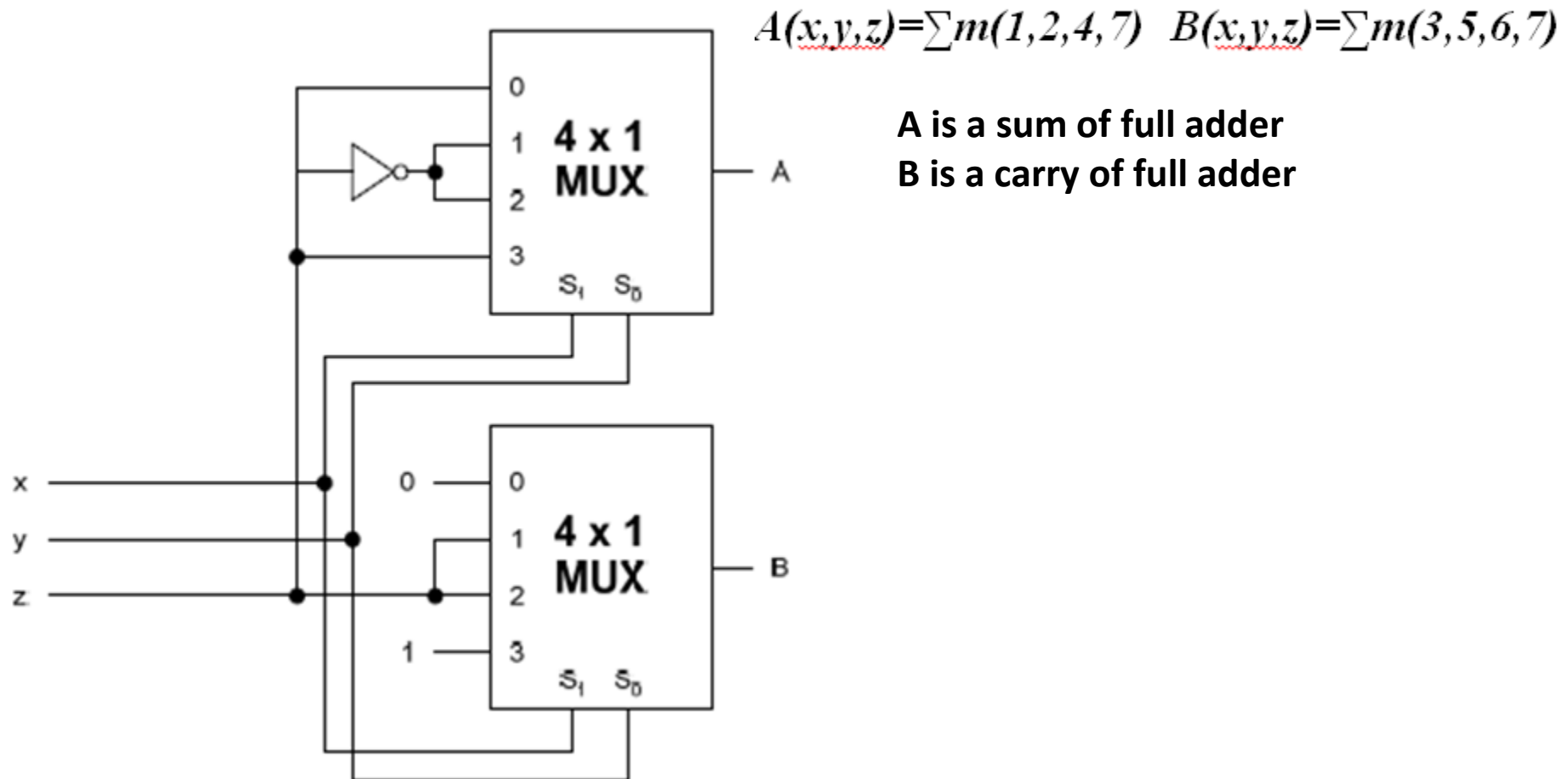
Determine the outputs of functions (two functions) A and B as sums of minterms for the following circuit.

The circuit shown in has a functionality of a commonly used arithmetic component. What does the circuit do and what are other names for A and B ?



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Thanks