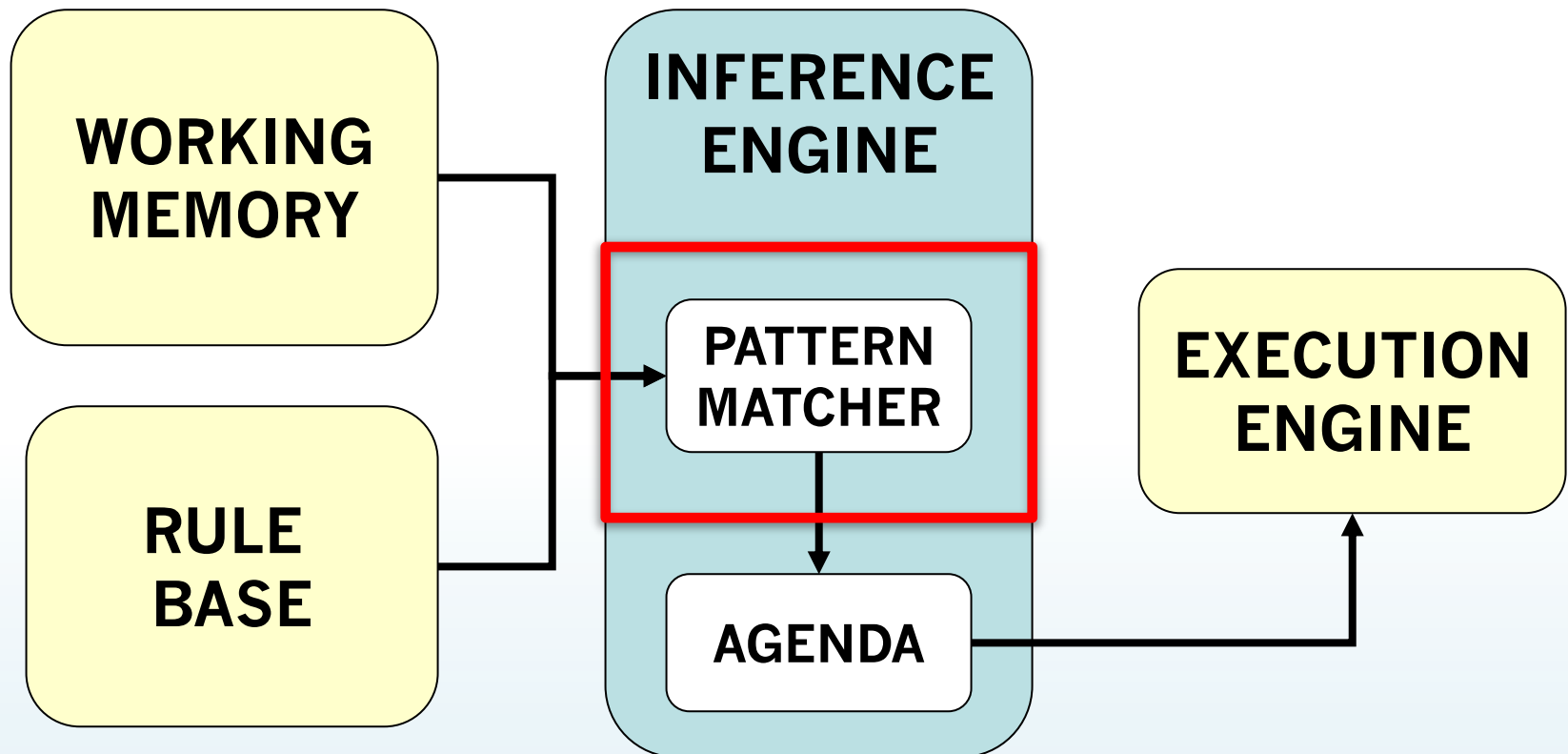


# RBS



# Inference with Production Rules

- ❖ There are two main issues involved in the implementation of a rule-based system
  - ❖ How is conflict resolution implemented?
    - ❖ Various strategies
  - ❖ How are facts matched to rules?
    - ❖ Pattern matching required
    - ❖ And many more issues need to be resolved

# Inference Mechanisms

- ❖ Pattern matching and unification are powerful operations to determine the similarity and consistency of complex structures
- ❖ They are at the core of many rule-based and predicate logic mechanisms
- ❖ Their application goes beyond rule-based systems

# Variables and bindings

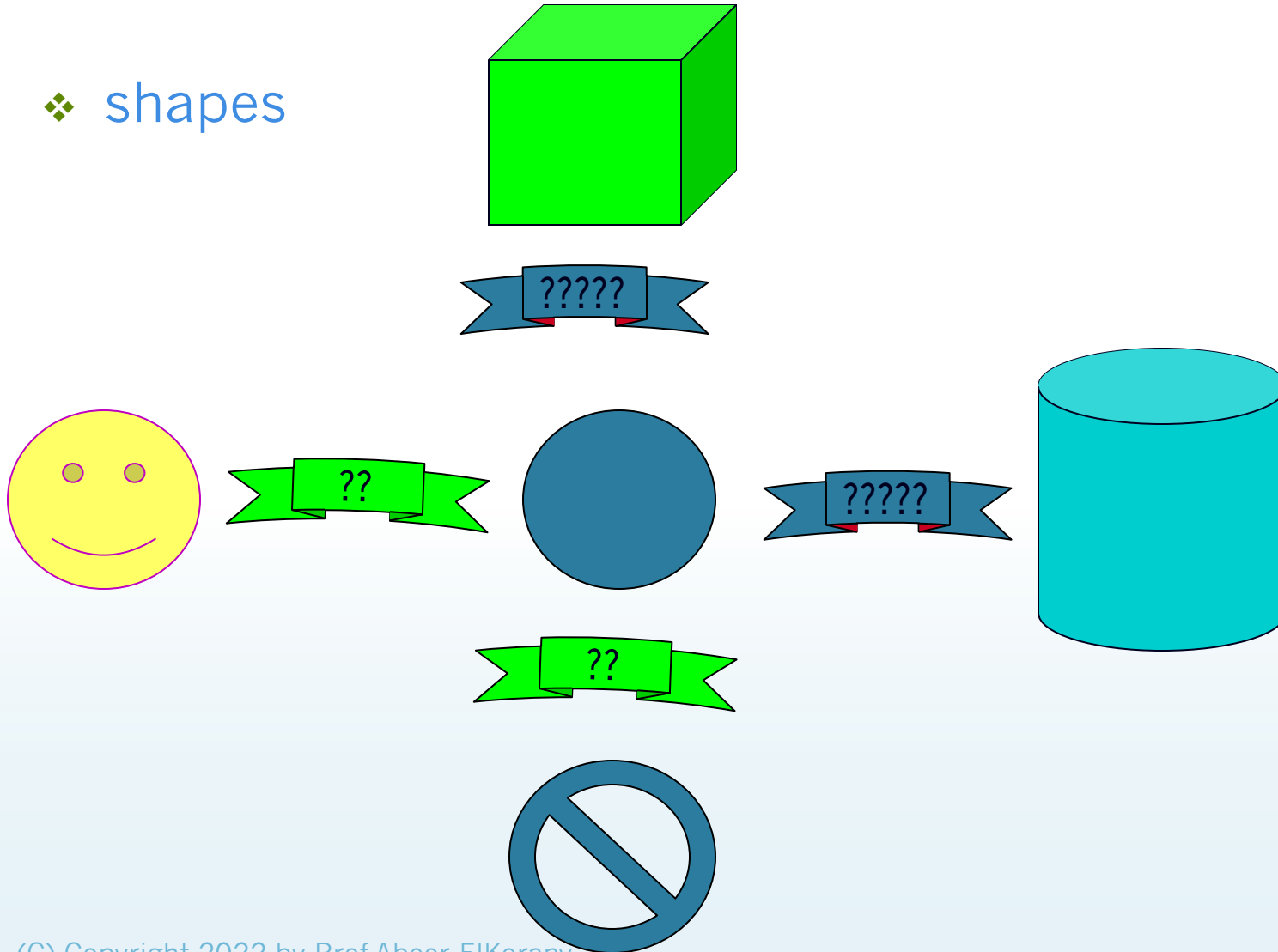
- ❖ Antecedents and consequents contain variables (?x)
- ❖ Variables acquire values during the matching process

# Bindings

- ❖ Once a variable is bound, that variable is replaced by its binding wherever it appears in the same or subsequently processed patterns
- ❖ Whenever the variables in a pattern are replaced by their bindings, the pattern is said to be instantiated

# Pattern Matching Example

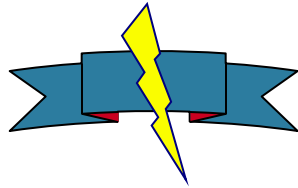
❖ shapes



# Pattern Matching Examples

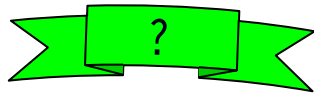
## ❖ constants and variables

“Hans”



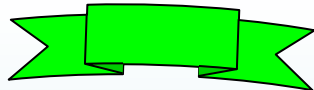
“Franz”

“Josef”



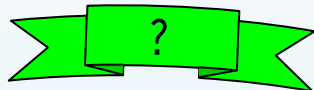
“Joseph”

?first\_name



“Joseph”

?last\_name



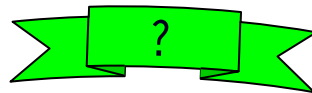
“Joseph”

# Pattern Matching Examples

## ❖ terms

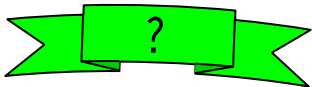
- ❖ composed of constants, variables, functions

father (X)



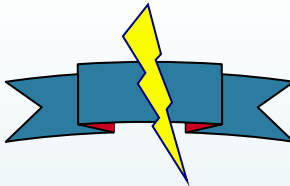
“Joseph”

father (X)



father (Y)

father (X)



mother (X)

father (father (X) )



grandfather (X)



# Applications of Pattern Matching

## search and retrieval

- ❖ Precise matching

- ❖ strings, images, documents, objects
- ❖ the query and the result have to match perfectly
- ❖ the two should be identical
- ❖ all requirements specified in the query have to be met by the result

- ❖ Similarity-based matching

- ❖ imprecise

# Pattern Matching in Rule-Based Systems

- ❖ Matching is the process of identifying which combinations of facts in the WM satisfy which rules
- ❖ Used to match rules with appropriate facts in working memory
  - ❖ rules for which facts can be found are *satisfied*
  - ❖ the combination of a rule with the facts that satisfy it is used to form *activation records*
    - ❖ one of the activation records is selected for execution
      - ❖ the respective rule “fires”

# Search and Retrieval(cont.)

- ❖ similarity-based matching
  - ❖ requires specification of a similarity measure
  - ❖ often domain/application/task-specific
    - ❖ some aspects of the result are different from the query specification
      - ❖ but not too different
- ❖ partial match
  - ❖ not all requirements specified in the query are met

# Pattern Matching

?

- ❖ single field wildcard
- ❖ matches anything in corresponding field of fact

\$?

- ❖ multi-field wildcard
- ❖ matches zero or more fields of a fact

# Pattern Matching (cont.)

?<var>

- ❖ single field variable
- ❖ <var> is some word
- ❖ this symbol matches anything in the corresponding field of a fact
- ❖ value matched is bound to ?<var> for scope of rule
- ❖ examples: ?cat ?color ?machine

\$?<var>

- ❖ multi-field variable
- ❖ matches zero or more fields of a fact
- ❖ the value(s) of the matched fields is bound to \$?<var> for the scope of the rule

# Examples

Single field wild cards

LHS Condition	Fact in Fact Base	Match?
(? ?)	(data red)	Yes
(data ?)	(data red)	Yes
(data ?)	(data red green)	NO!
(data ? ?)	(data red green)	Yes
(data red ?)	(data red green)	Yes
(data ? green)	(data green)	NO!

# Examples

## Single Field Variables

LHS Condition	Fact in Fact Base	Match?
(data red ?x)	(data red green)	?x=green
(data red ?x)	(data red "green")	?x="green"
(data red ?x)	(data red 17.4)	?x=17.4
(data ?x ?x)	(data red red)	?x=red
(data ?x ?x)	(data red green)	NO!
(data ?x ?y)	(data red green)	?x=red ?y=green
(data ?x ?y)	(data red red)	?x=red ?y=red

# Examples

## Multi-field wild cards

LHS Condition	Fact in Fact Base	Match?
(\$?)	(data red)	Yes
(data \$?)	(data red)	Yes
(data red \$?)	(data red)	Yes
(data \$?)	(data red green)	Yes
(data red green \$?)	(data red green)	Yes
(\$? green)	(data red green)	Yes
(\$? red \$?)	(data red green)	Yes
(data red \$?)	(data green red)	NO!
(data \$? red \$?)	(data green red)	Yes
(\$? \$?)	(data red)	Yes



# Examples

## Multi-Field Variables

LHS Condition	Fact in Fact Base	Match?
(data red \$?x)	(data red)	\$?x=()
(data red \$?x)	(data red green)	\$?x=(green)
(data red \$?x)	(data red one two)	\$?x=(one two)
(data \$?x \$?x)	(data red red)	\$?x=(red)
(data \$?x \$?y)	(data red green)	Multiple matches:
	\$?x=()	\$?y=(red green)
	\$?x=(red)	\$?y=(green)
	\$?x=(red green)	\$?y=()

# Rule-Based Pattern Matching

- ❖ Go through the list of rules, and check the antecedent (LHS) of each rule against the facts in working memory
  - ❖ create an activation record for each rule with a matching set of facts
  - ❖ repeat after each rule firing
- ❖ Very inefficient
  - ❖ roughly (number of rules) \* (number of facts)
  - ❖ the actual performance depends on the formulation of the rules and the contents of the working memory

# Disadvantages of Rule Systems

- ❖ Require exact matching

IF        The motor is hot  
THEN    Shut the motor down

What about

- ❖ The motor is running hot.
- ❖ The motor's temperature is hot.

- ❖ Have opaque rule relationship(difficult to debug for a large rule base)

- ❖ IF C THEN D
- ❖ IF B THEN C
- ❖ IF A THEN B

- ❖ Can be slow (May need to scan the whole rule set several times)

# Problems with Inference cycle

1. Complete scan of the working memory (facts list) during each cycle of execution
  2. More rules will result in more rules that apply and more facts being derived that both apply and do not apply
- ❖ Suppose you have the following situation:
    - ❖ –  $r$  rules in KB with average of  $p$  conditions
    - ❖ –  $f$  facts in the fact base
  - ❖ – Then our inference engine will have to perform roughly  $r * f * p$  comparisons each cycle

# Match step

- ❖ Disadvantage of RBS – large computational requirement to perform match of LHS – determine if all instantiations of rules are satisfied by the content of the WM (Working Memory)
- ❖  $O(\text{comparison to check the satisfaction of a rule}) = |WM| |CE|$

$|WM|$  - no of WMEs (Working Memory Elements)

$|CE|$  - number of condition elements in a rule

# Rule example

(deftemplate student

(slot name)  
(slot gender)  
(slot placed\_in (default nil))  
(slot special\_considerations  
 (default no))

(deffacts start

(student (name Mary) (gender F))  
(student (name Peter) (gender M))  
 (special\_consideration yes))  
(room (number 221) (capacity 1) (vacancies 1))  
(room (number 346) (capacity 2) (vacancies 1)))

(deftemplate room

(slot number)  
(slot capacity (type INTEGER)(default 4))  
(slot genders\_are)  
(slot vacancies (type INTEGER))  
(multislot occupants))

WMEs

41 (student name Mary gender F placed\_in nil  
 special\_consideration no)  
52 (student name Peter gender M placed\_in nil  
 special\_consideration yes)  
9 (room number 221 capacity 1 vacancies 1)  
12 (room number 346 capacity 2 vacancies 1)

# Rule example

```
(defrule assign-student-empty-room
  ?unplaced_student ← (student (name ?stud_name)
                               (placed_in nil)
                               (gender ?gen))
  ?empty_room ← (room (number ?room_no)
                   (capacity ?room_cap)
                   (vacancies ?free_places))
  (test (= ?room_cap ?free_places))
=>
  (modify ?unplaced_student (placed_in ?room_no))
  (modify ?empty_room (occupants ?stud_name) (gender_are ?gen)
            (vacancies (-- ?free_places))))
```

$$\forall s \forall r \forall x \forall y \forall z \forall t \text{ name}(s,x) \wedge \text{placed\_in}(s,\text{nil}) \wedge \text{gender}(s,y) \wedge$$
$$\text{number}(r,z) \wedge \text{capacity}(r,t) \wedge \text{vacancies}(r,t) \rightarrow$$
$$\text{placed\_in}(s,z) \wedge \dots$$

# Making it more efficient

- ❖ The **Rete algorithm** is an efficient pattern matching algorithm for implementing rule-based expert systems.
- ❖ The Rete algorithm was designed by Dr. Charles L. Forgy of Carnegie Mellon University in 1979.
- ❖ the name comes from the latin word *rete*
  - ❖ stands for net
- ❖ Rete has become the basis for many popular expert systems, including OPS5, CLIPS, and JESS.
- ❖ The Rete algorithm was the first efficient solution to the facts-rules pattern matching problem
  - ❖ It stores information about matches in a network structure



# Rete Algorithm

- ❖ Rete looks for changes to match in each cycle
- ❖ Focus on few facts that are added, changed or removed at every step in the process of inference. Instead of doing all these comparisons every time only new facts added can be taken into consideration.
- ❖ Unnecessary Computations Facts Change (Keep track of changes) Rules remain unchanged
- ❖ the Rete algorithm performs an improved matching of rules and facts
  - ❖ basis for many rule-based expert system shells

# The Rete Matching Algorithm

- ❖ Nodes of the network correspond to individual condition elements
  - ❖ Conditions and conjunctions of conditions
- ❖ Each node has two sets associated with it
  - ❖ The first set contains all the working memory elements that the condition node matches
  - ❖ The second set contains combinations of working memory elements and the bindings which produce a consistent match of the conditions that chain up to the node condition

# RETE algorithm

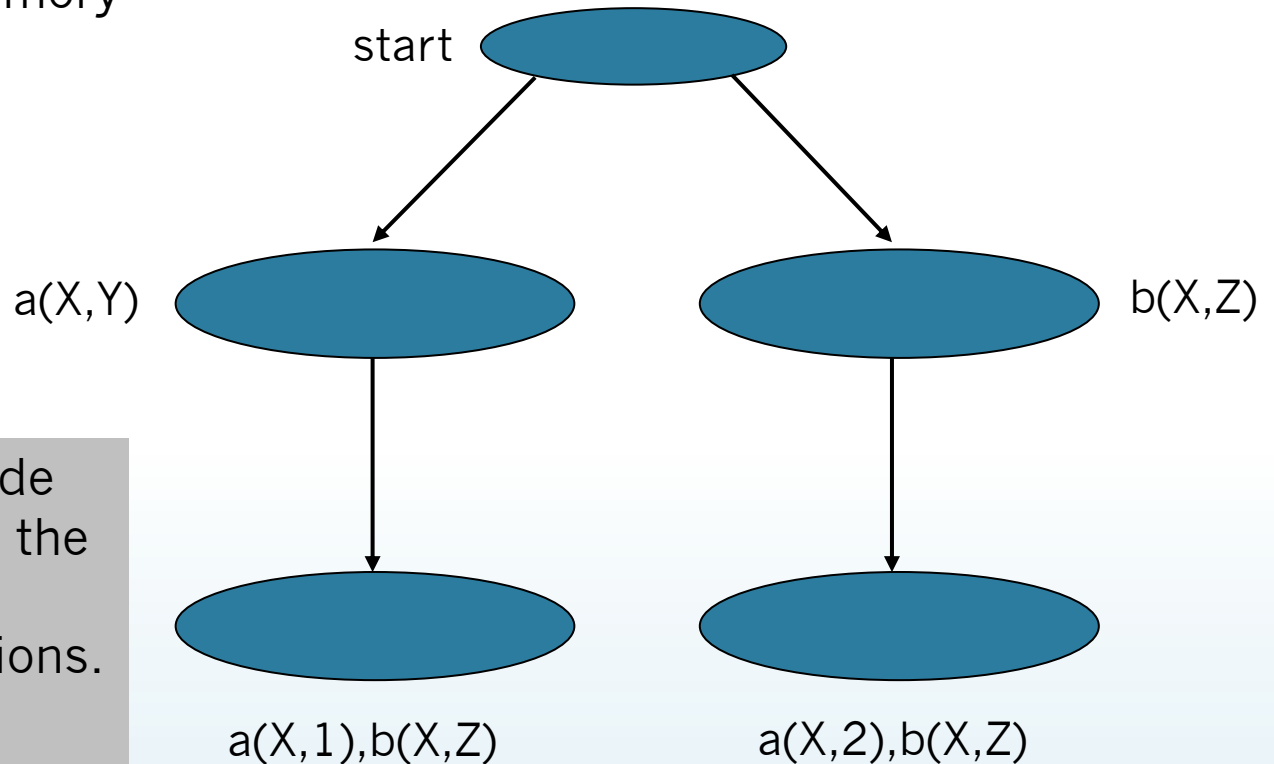
- ❖ Consists of a network of interconnected nodes
- ❖ Creates a decision tree where each node corresponds to a pattern occurring at the left-hand side of a rule
- ❖ Each node has a memory of facts that satisfy the pattern
  - input nodes are at the top, output nodes at the bottom
  - *join nodes* have two inputs, and combine facts
  - *terminal node* at the bottom of the network represent individual rules
- ❖ a rule is satisfied if there is a combination of facts that passes all the test nodes from root to a leaf.

# The Rete Matching Algorithm

- ❖ With this configuration repetitive testing of all rule conditions in each cycle is avoided
- ❖ Only the nodes affected by a newly inserted or modified fact are checked
- ❖ For example, consider the rules
  - ❖ IF  $a(X,1)$  and  $b(X,Z)$  THEN  $g1(X,Z)$
  - IF  $a(X,2)$  and  $b(X,Z)$  THEN  $g2(X,Z)$

# The Rete Matching Algorithm

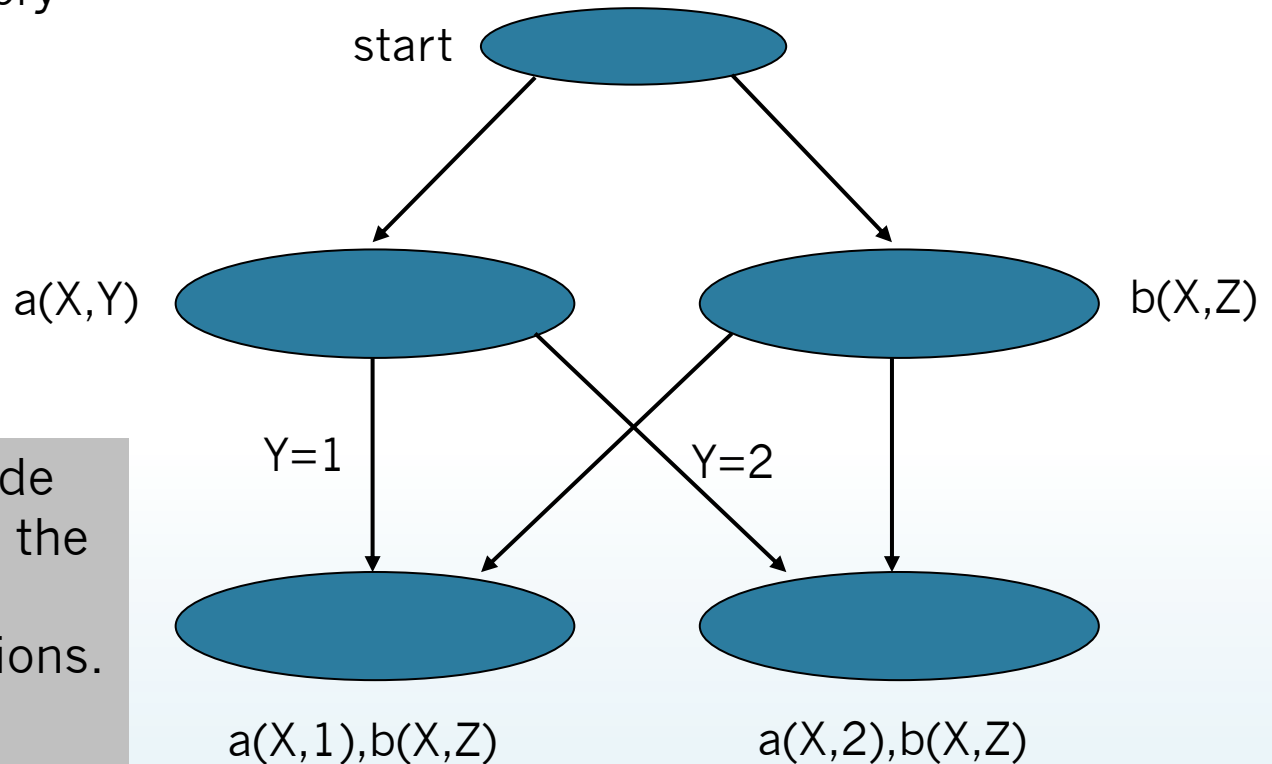
Initially the working memory is empty



- There is a starting node and a node for each of the rule conditions and conjunctions of conditions.
- Arcs are labeled with variable bindings

# The Rete Matching Algorithm

Initially the working memory is empty

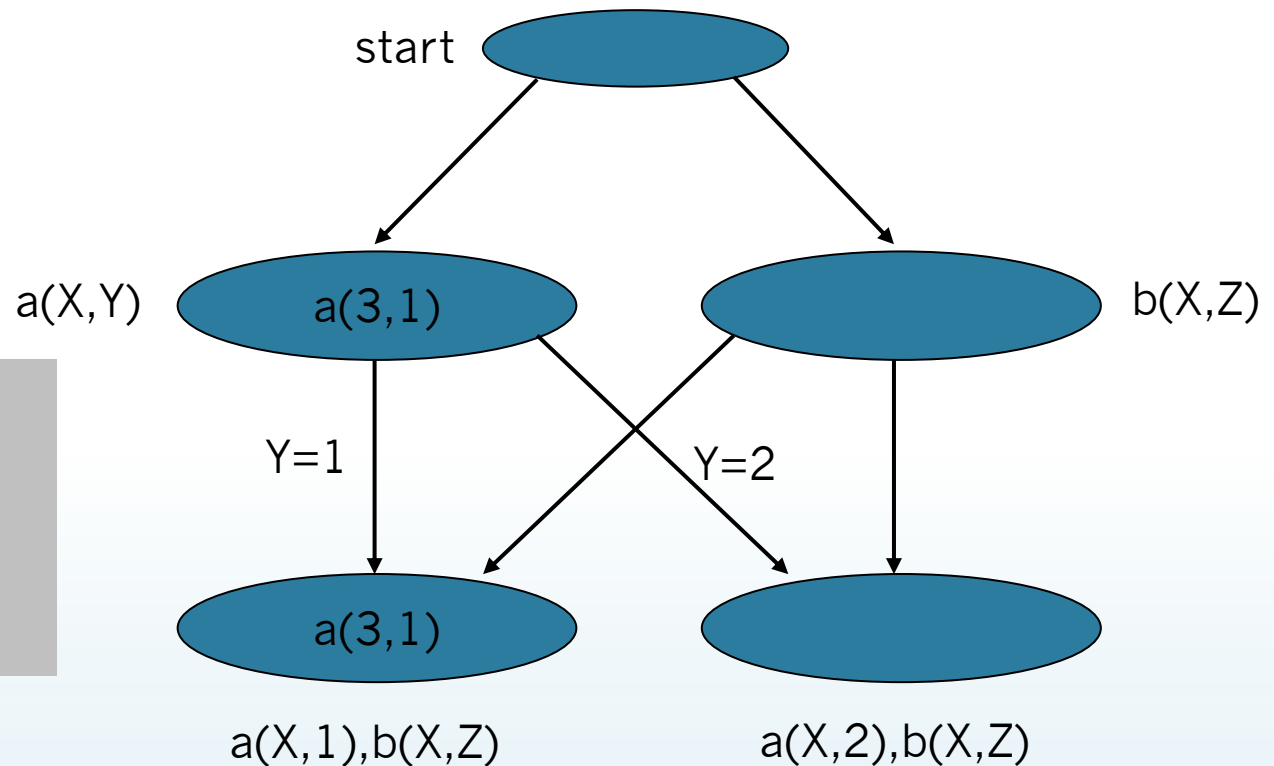


- There is a starting node and a node for each of the rule conditions and conjunctions of conditions.
- Arcs are labeled with variable bindings

# The Rete Matching Algorithm

Fact  $a(3,1)$  is added to the working memory

$a(3,1)$  is deposited in the node labeled  $a(X,Y)$  and will propagate through the arc labeled  $Y=1$



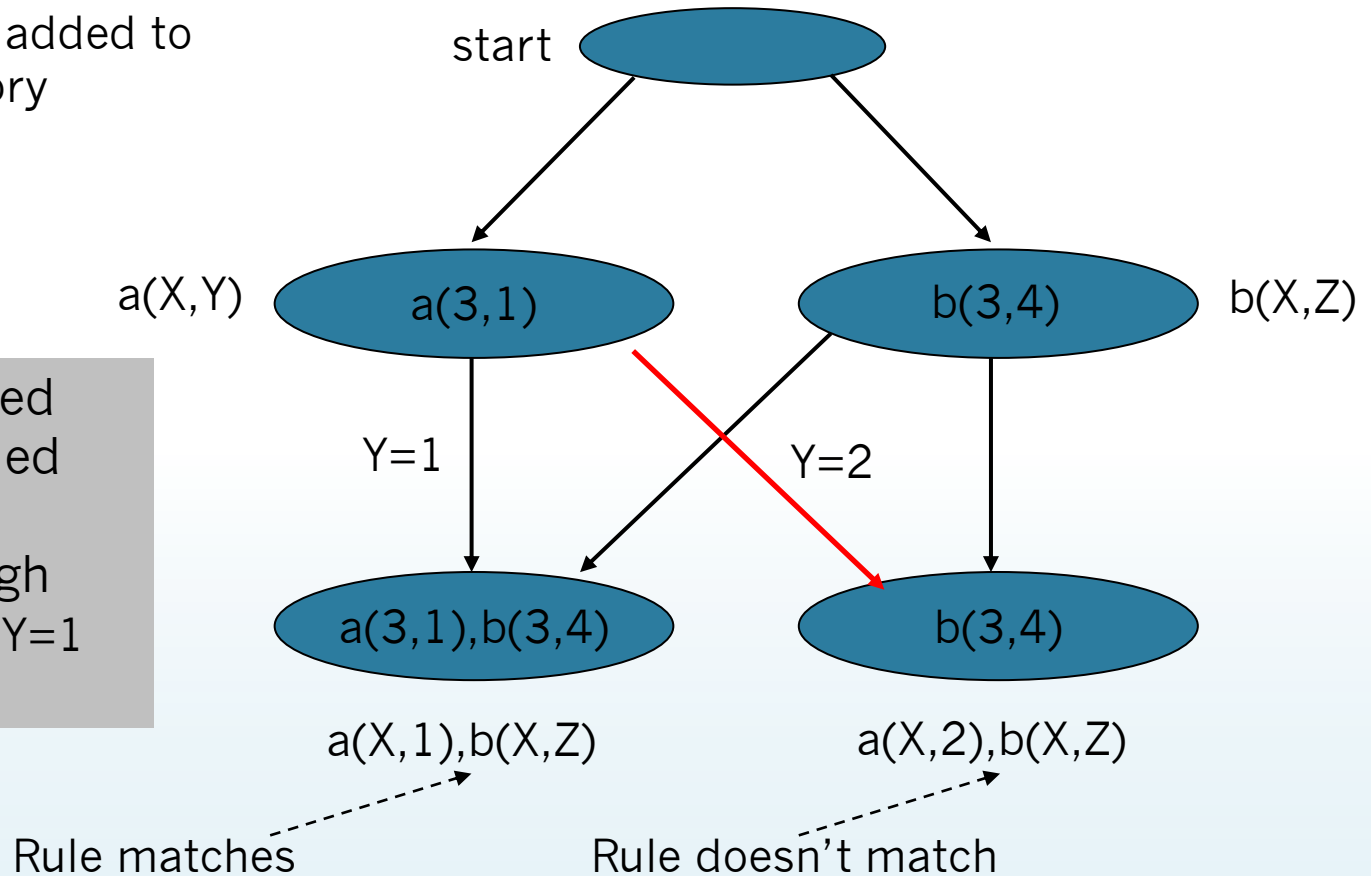
Rule doesn't match

# The Rete Matching Algorithm

Fact  $a(3,1)$

Fact  $b(3,4)$  is now added to the working memory

$b(3,4)$  is deposited in the node labeled  $b(Y,Z)$  and will propagate through the arcs labeled  $Y=1$  and  $Y=2$

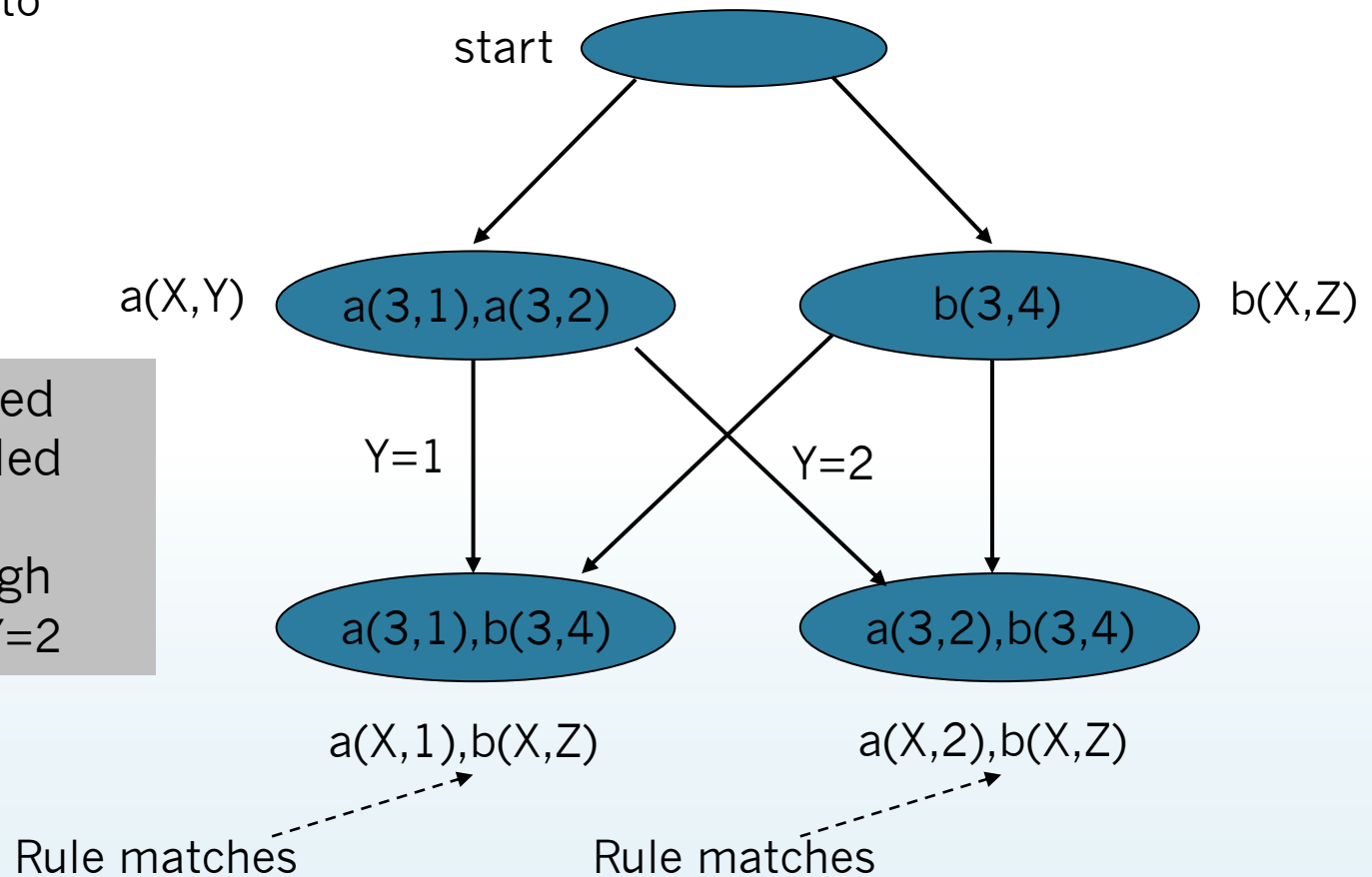




# The Rete Matching Algorithm

Fact  $a(3,1)$   
Fact  $b(3,4)$   
Fact  $a(3,2)$  is added to  
the working memory

$a(3,2)$  is deposited  
in the node labeled  
 $a(X,Y)$  and will  
propagate through  
the arc labeled  $Y=2$



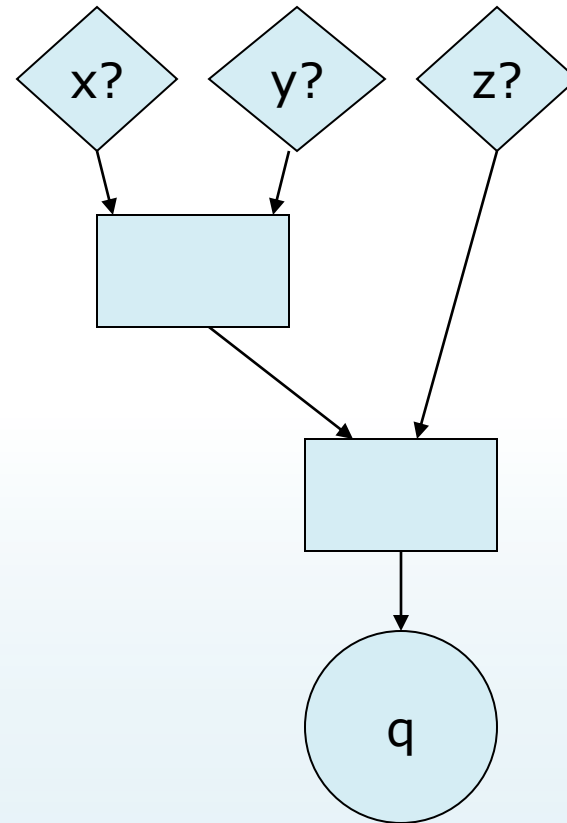
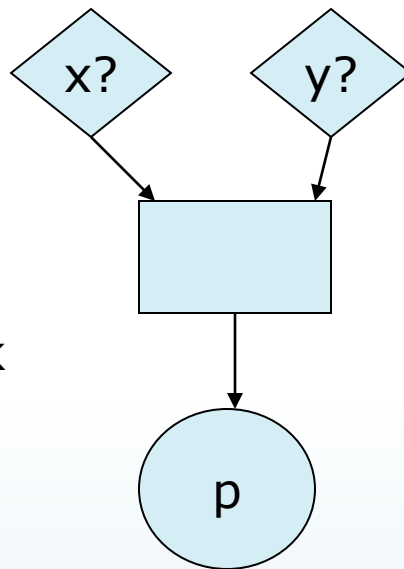
# Rete example

R1: IF x & y THEN p  
R2: IF x & y & z THEN q

Pattern  
Network

Join Network

8 nodes



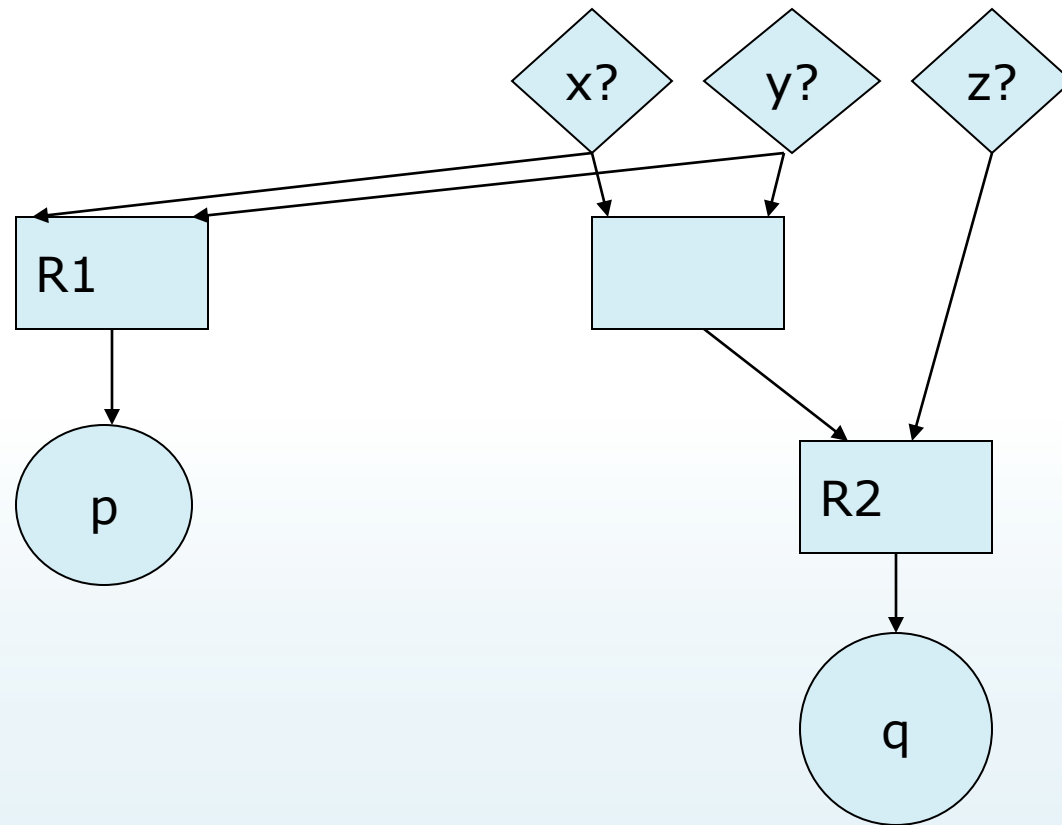
# Rete example

R1: IF x & y THEN p  
R2: IF x & y & z THEN q

Pattern  
Network

Join Network

6 nodes



# Rete example

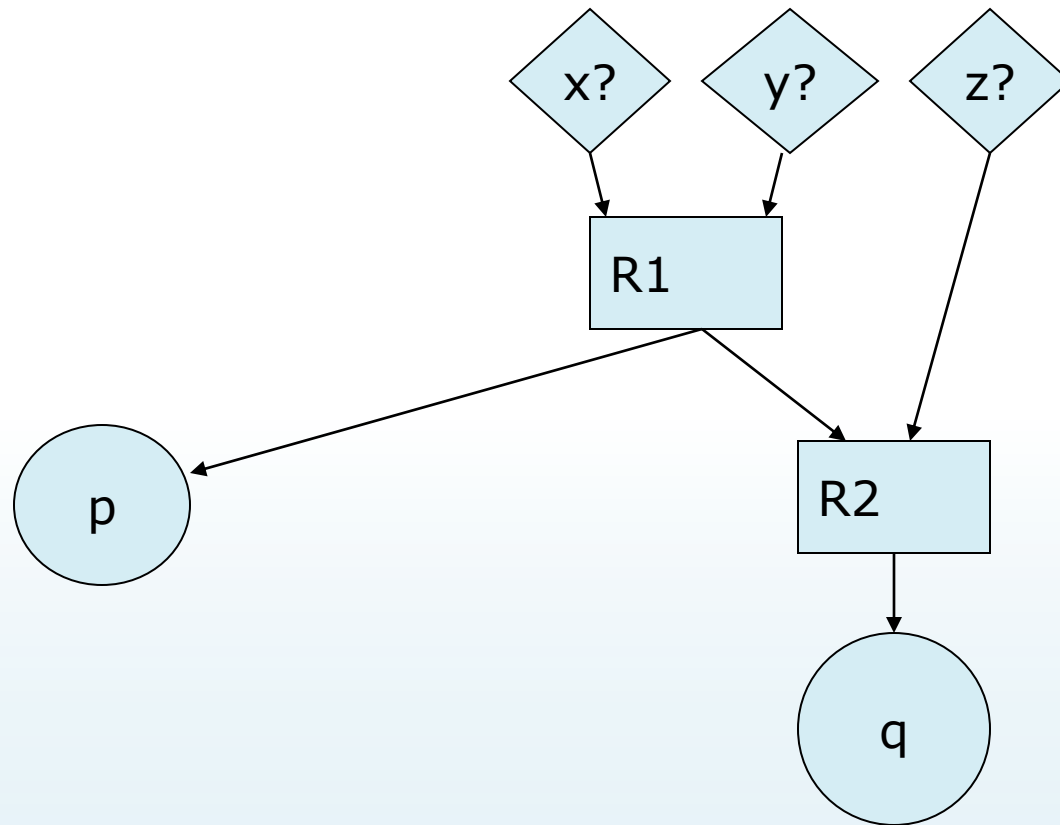
R1: IF x & y THEN p

R2: IF x & y & z THEN q

Pattern  
Network

Join Network

5 nodes



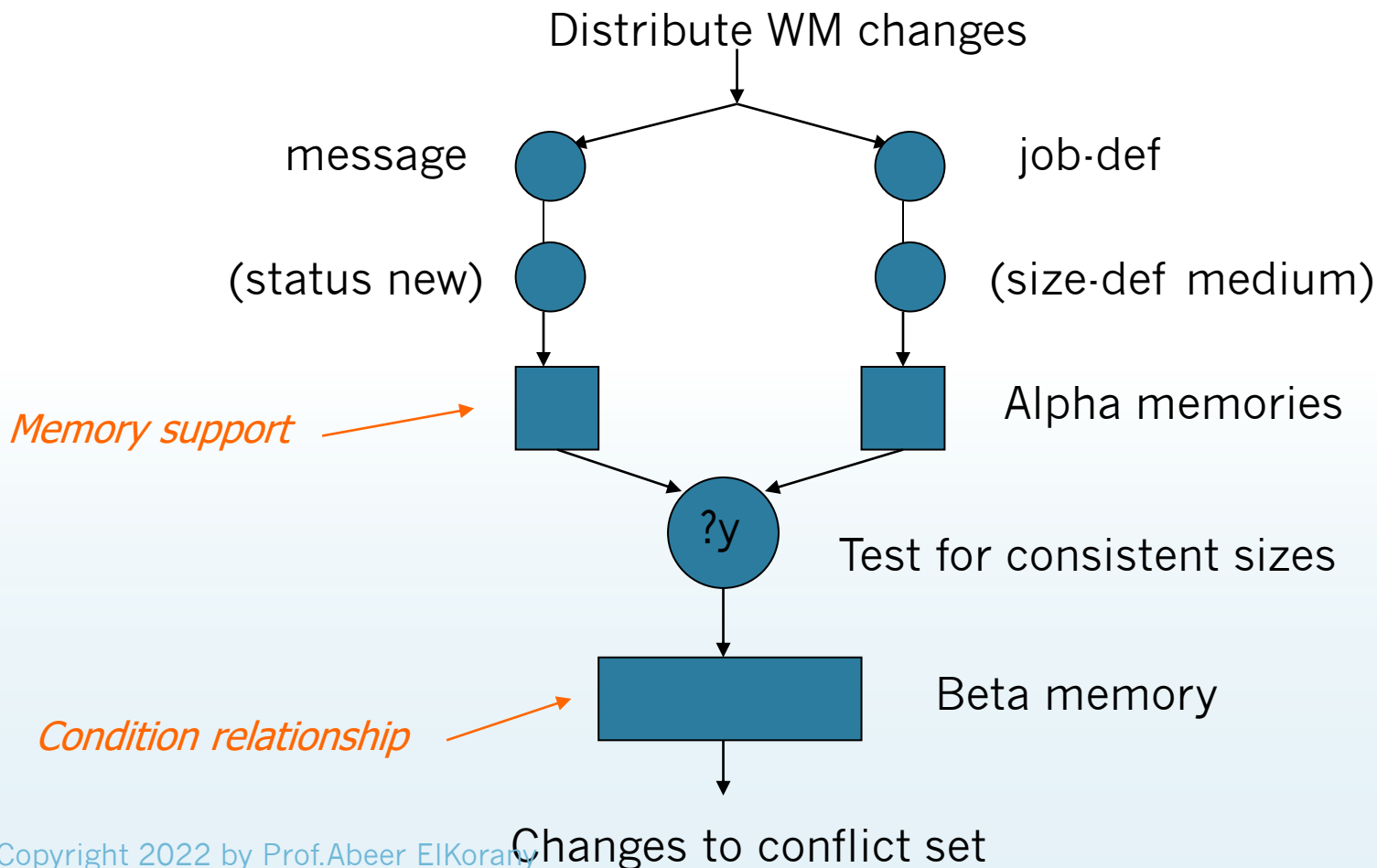
## (defrule job-size

(message (jobs ?x) (size ?y) (status new))

(job-def (size ?y) (size-def medium))

=>  
(assert (job (job-name ?x) (job-size ?y))))

## RETE match Network for the rule



(defrule show-act

(a ?x)

(b ?x ?y)

(c ?y )

=> ...

WM

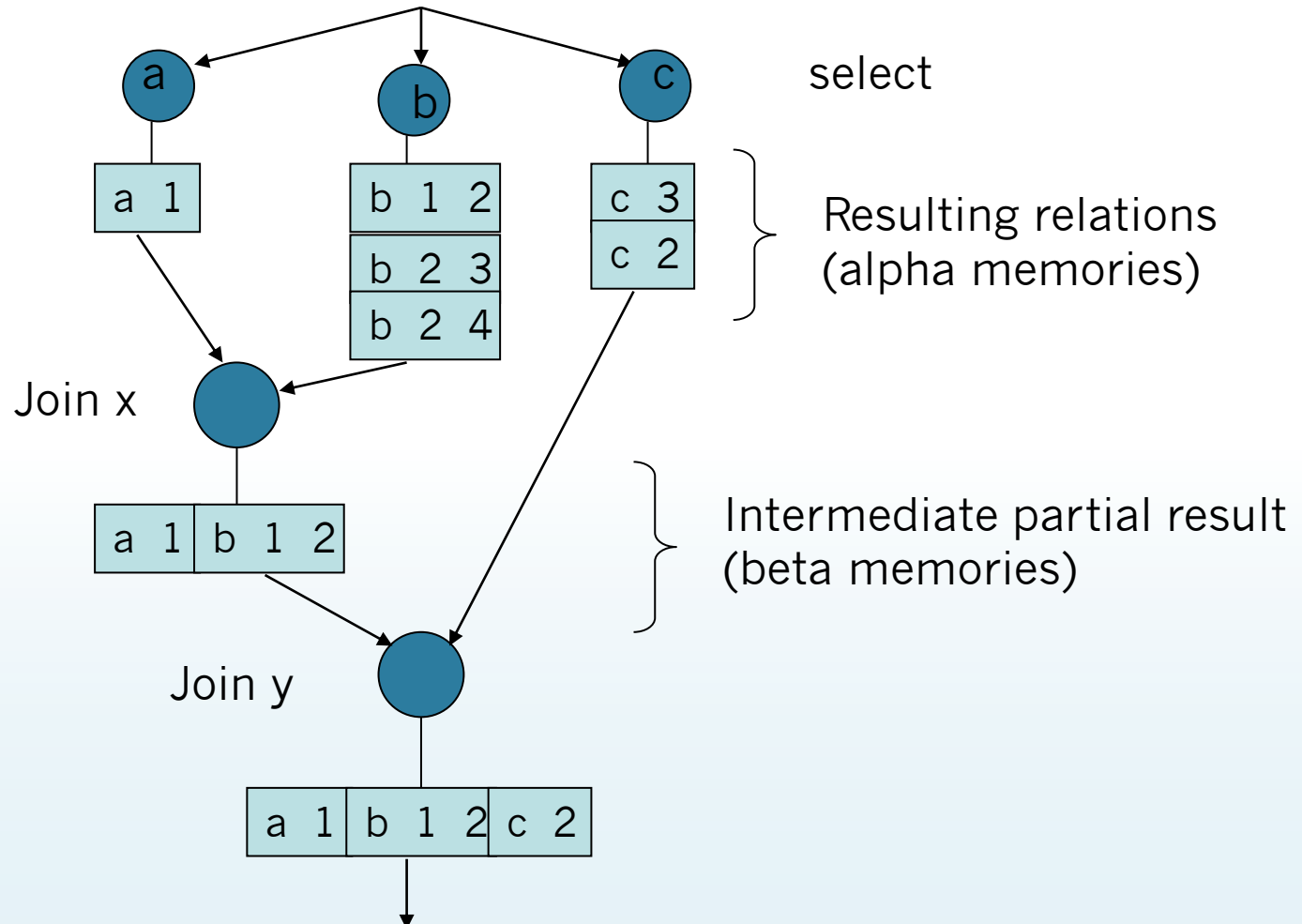
(a 1)

(b 1 2) (b 2 3) (b 2 4)

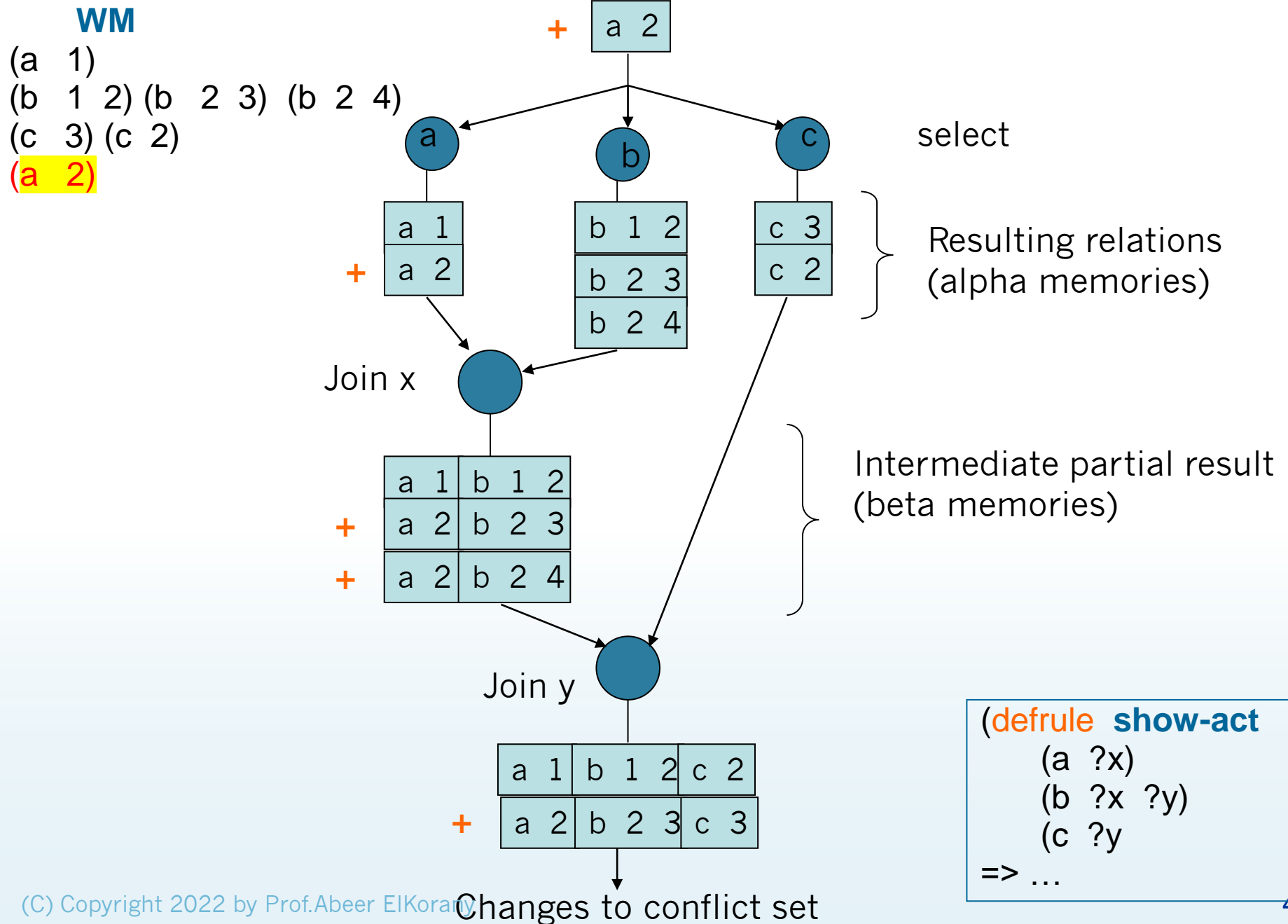
(c 3) (c 2)

## Initial state of RETE Network

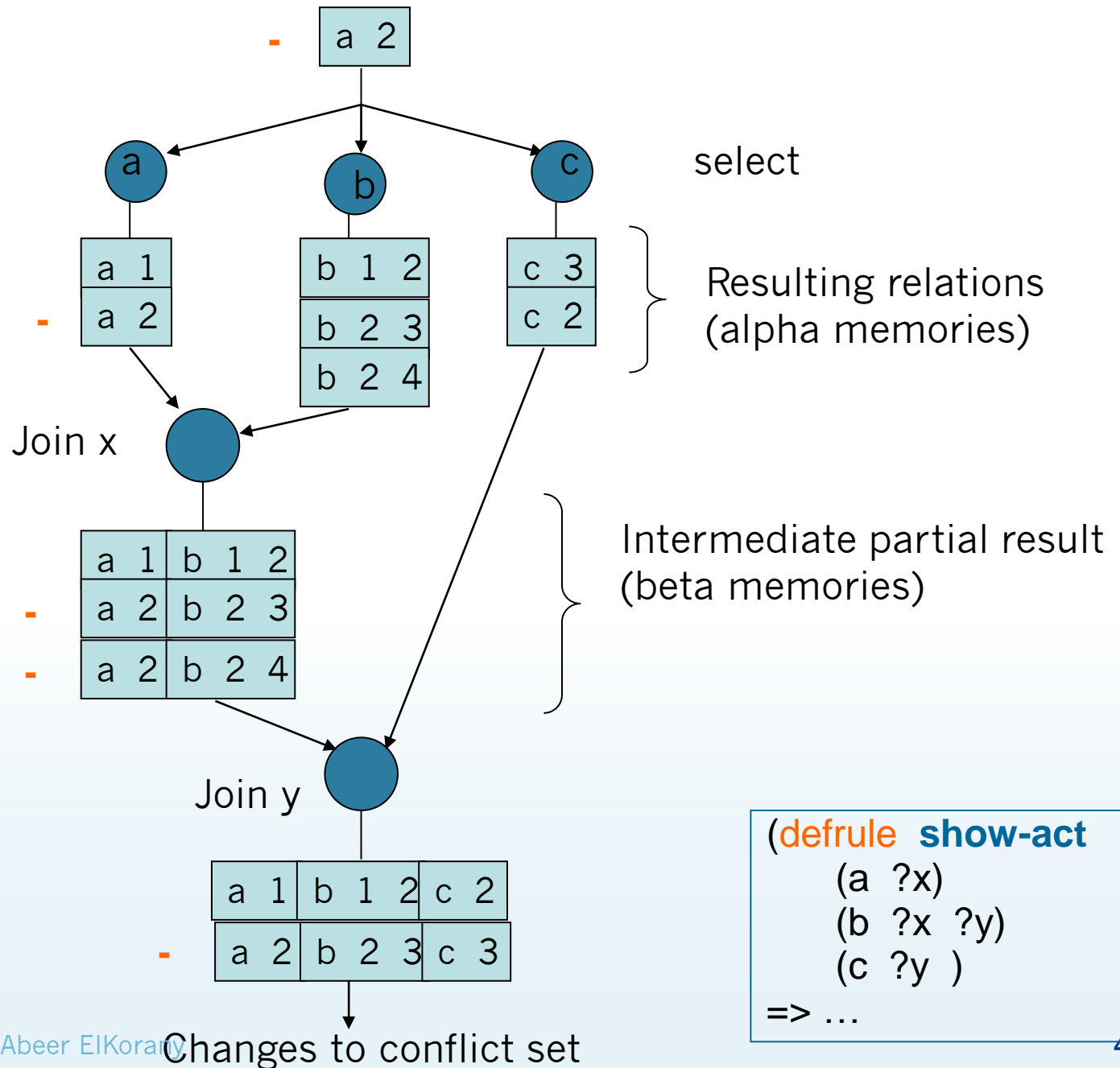
show-act



# Activity of the RETE Match during an Addition



# Activity of the RETE Match during a Deletion





# Assert and Retract with Rete

- ❖ asserting additional facts imposes some more constraints on the network
- ❖ retracting facts indicates that some previously computed activation records are not valid anymore, and should be discarded
- ❖ in addition to the actual facts, *tags* are sent through the networks
  - ❖ `ADD` to add facts (i.e. for `assert`)
  - ❖ `REMOVE` to remove facts (i.e. for `retract`)
  - ❖ `CLEAR` to flush the network memories (i.e. for `reset`)
  - ❖ `UPDATE` to populate the join nodes of newly added rules
    - ❖ already existing join nodes can neglect these tokens

# Further Optimizations

- ❖ sophisticated data structures to optimize the network
  - ❖ hash table to presort the tokens before running the join node tests
- ❖ fine-tuning via parameters
  - ❖ frequently trade-off between memory usage and time

# Further Optimizations

## Example:

1 IF Shape=long  
& Color=(green or yellow)  
THEN Fruit=banana

2 IF Shape=(round or oblong)  
& Diam>4

THEN Fruitclass=vine

3 IF Shape=round & Diam<4  
THEN Fruitclass=tree

4 IF Seedcount=1

THEN Seedclass=stonefruit

5 IF Seedcount>1

THEN Seedclass=multiple

6 IF Fruitclass=vine & Color=green  
THEN Fruit=watermelon

7 IF Fruitclass=vine

& Surface=smooth & Color=yellow

THEN Fruit=honeydew

8 IF Fruitclass=vine &

Surface=rough

& Color=tan THEN Fruit=cantaloupe

9 IF Fruitclass=tree & Color=orange  
& Seedclass=stonefruit & Diam>3  
THEN Fruit=peach

10 IF Fruitclass=tree & Color=orange  
& Seedclass=multiple

THEN Fruit=orange

11 IF Fruitclass=tree & Color=red  
& Seedclass=stonefruit

THEN Fruit=cherry

12 IF Fruitclass=tree & Color=orange  
& Seedclass=stonefruit & Diam < 3

THEN Fruit=abricot

13 IF Fruitclass=tree

& Color=(red or yellow or green)

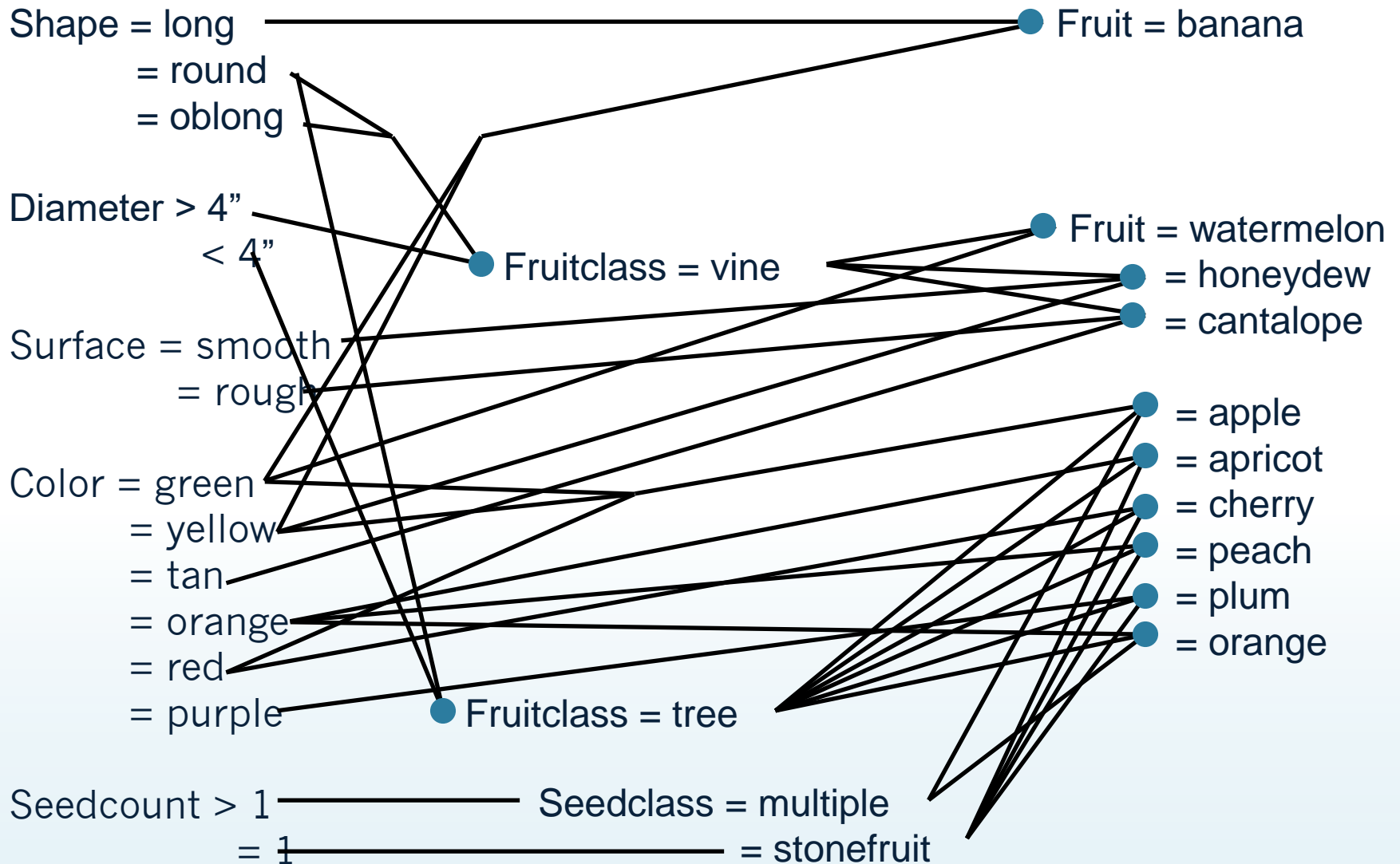
& Seedclass=multiple

THEN Fruit=apple

14 IF Fruitclass=tree & Color=purple  
& Seedclass=stonefruit

THEN Fruit=plum

# Fruit Knowledge Base Example



# Sample Facts

(deffact list

(color is red)

(shape is round)

(= seedcount 1)

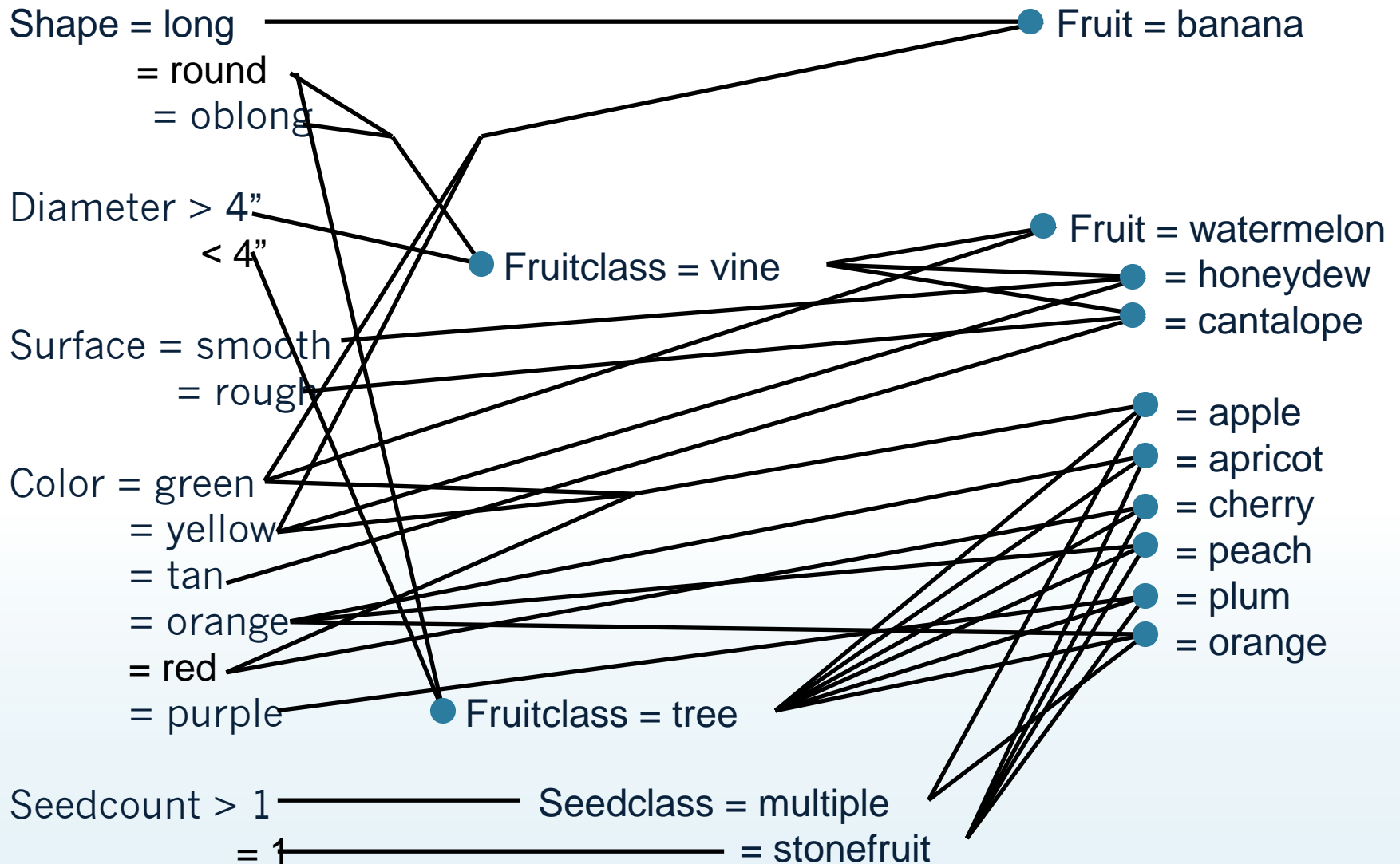
(< diameter 4)

) )

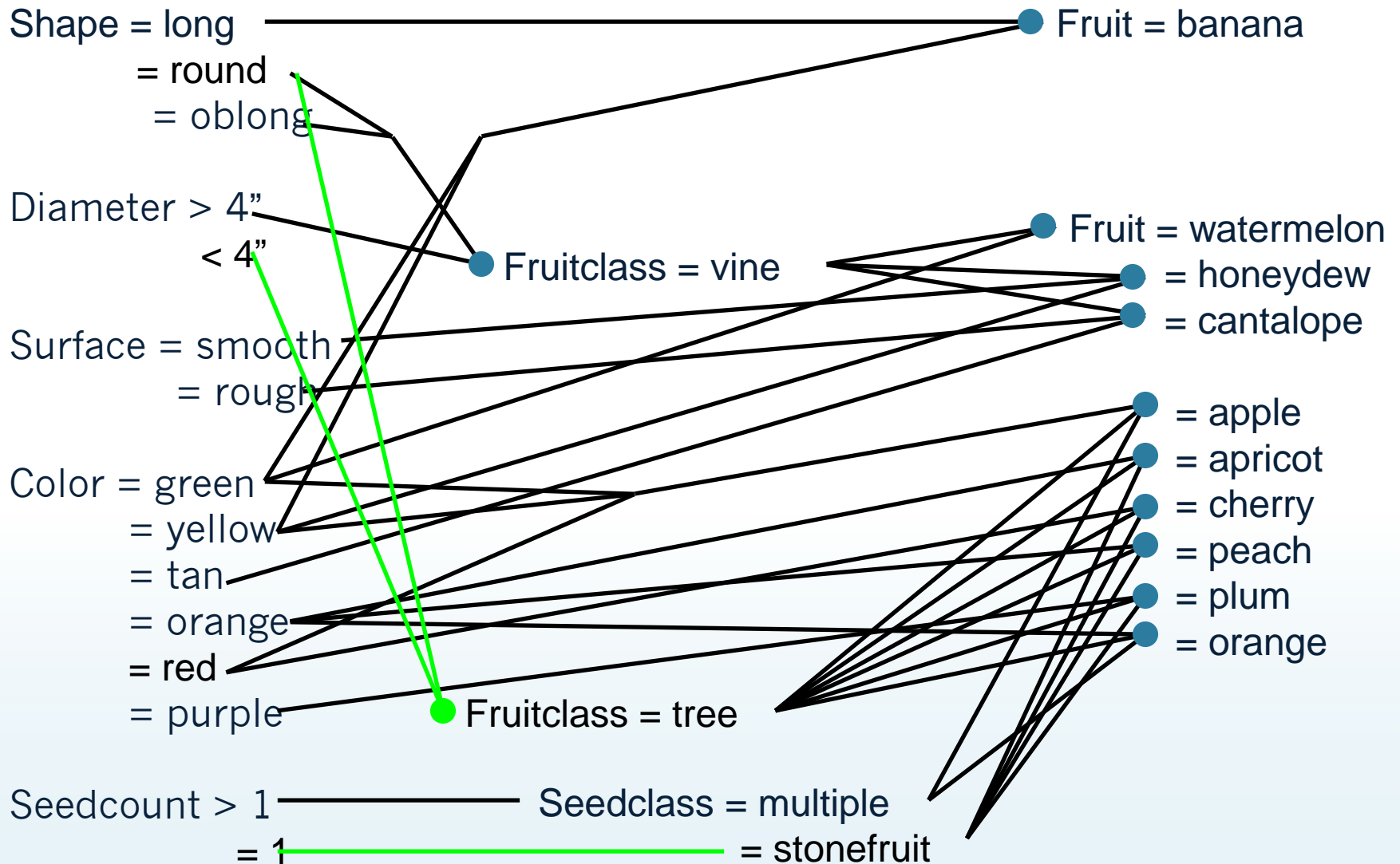
What is the result  
from execution?

The value of fruitclass is tree  
The value of seedclass is stonefruit  
The value of fruit is cherry

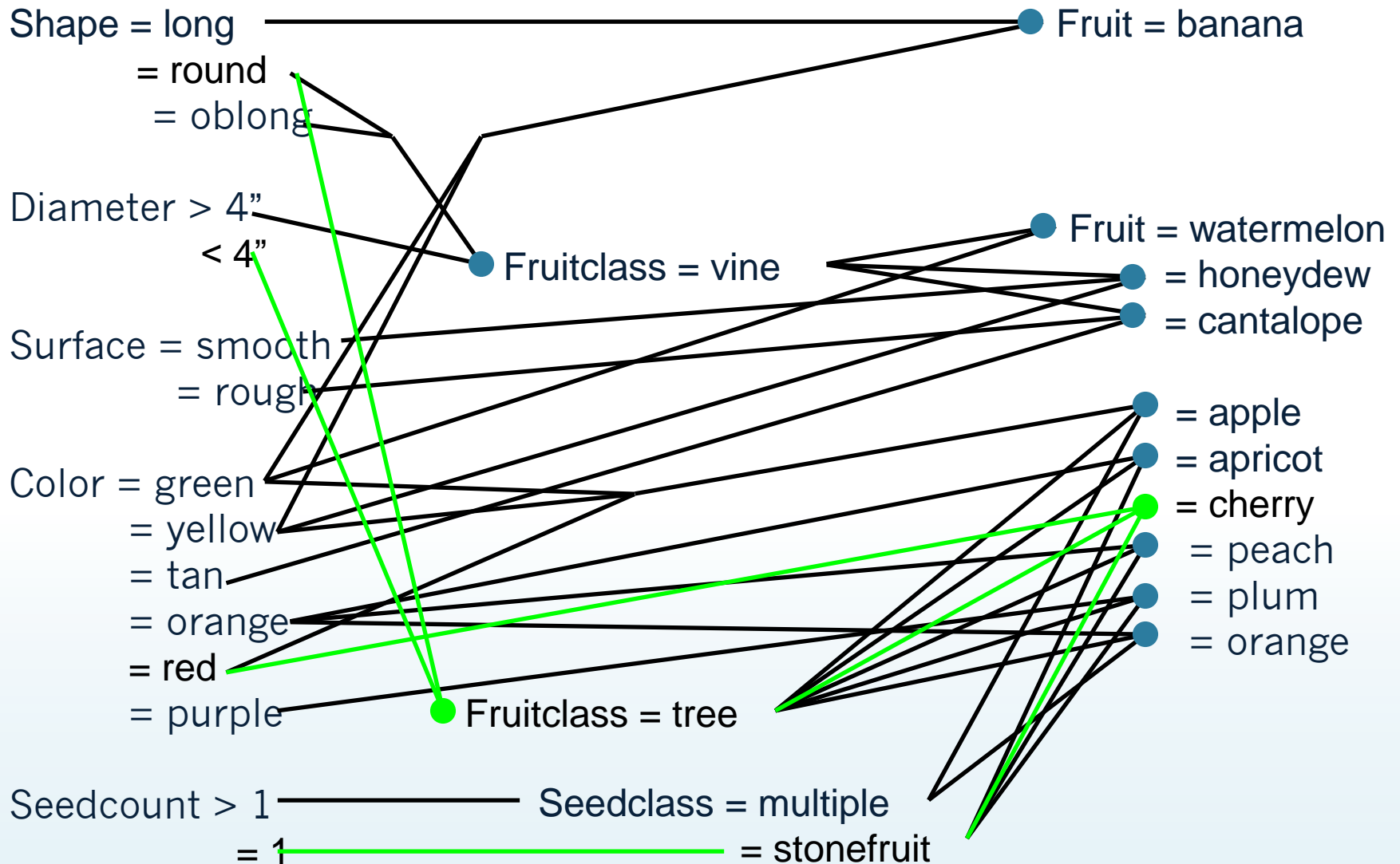
# Fruit Knowledge Base



# Fruit Knowledge Base



# Fruit Knowledge Base

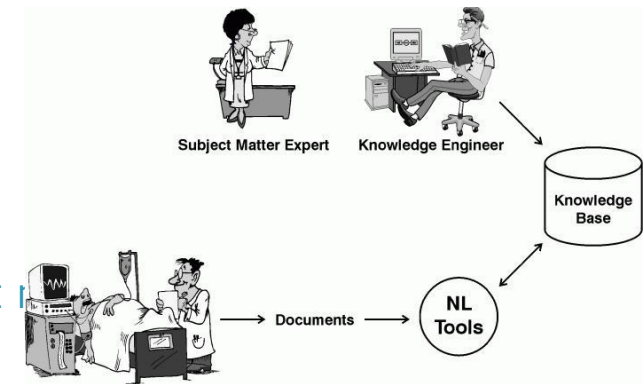




# Designing efficient rule-based systems

## ❖ Knowledge Engineer

- ❖ Tasked with working with the expert to extract expertise and codify in a set of rules
  - ❖ Has training in the development of expert systems, but is not necessarily in the application domain
  - ❖ Know the capabilities of technology and knows how to apply it
- 
- ❖ The most specific pattern should be placed toward the front of the left-hand side of the rule
  - ❖ A specific pattern will generally have the **smallest** number of matching facts in the facts list and will have the **largest** number of variable bindings which constrain other patterns.



# Most specific pattern goes first

- ❖ R1: (item ?x) (item ?y) (item ?z) (match ?x ?y ?z) -> (buy ?x)
- ❖ R2 : (match ?x ?y ?z) (item ?x) (item ?y) (item ?z) ) -> (buy ?x)

The most specific pattern should be placed toward the front of the left-hand side of the rule

A specific pattern will generally have the smallest number of matching facts in the facts list and will have **the largest number of variable bindings** which constrain other patterns.

# Control: Meta-Rules

## ❖ Meta-Rules

Use **Meta-Rules** to divide rules into classes. Choose one class over another at a given point.

This implements **domain-dependent knowledge** about which set of rules to use during reasoning.

CLIPS provides a **Module**-construct with similar effects.

# Categories of Rules

- ❖ Saliency values are arbitrary; often what we want is that a certain class of rules are considered before others.
- ❖ This can be built into the rules themselves using a kind of 'tag'
- ❖ Another rule can be implemented to change status to the next group of rules.