

\* بسم الله الرحمن الرحيم \*

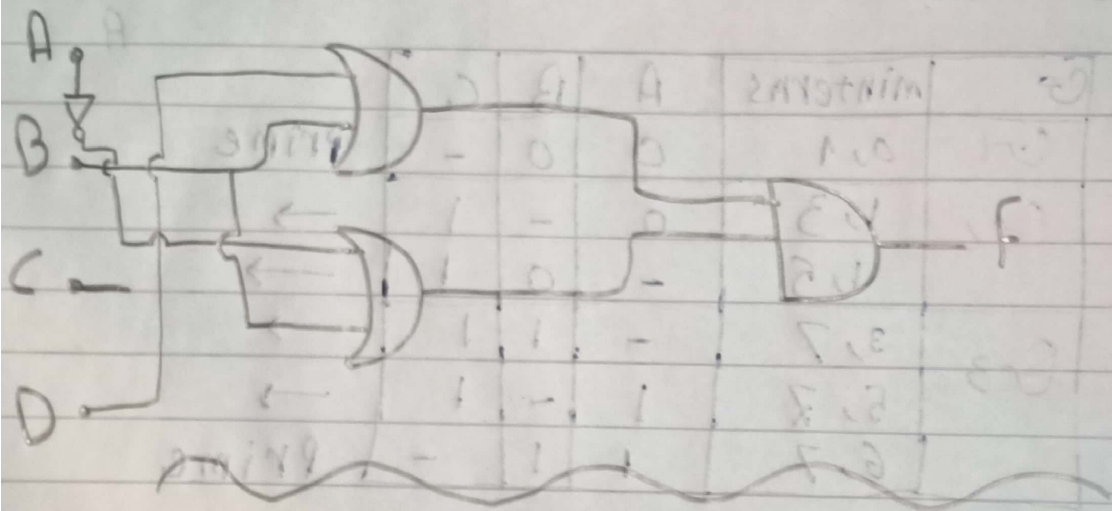
$$\textcircled{2} \textcircled{a} F(A, B, C, D) = B\bar{C} + \bar{A}B + B\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} + \bar{A}BCD$$

Pos

فمثلاً كأنها SOP:  $(+ \dots +)$  في F

AB \ CD	00	01	11	10
00	0	1	1	0
01	1	1	1	1
11	1	1	1	1
10	0	0	0	0

$$\text{Pos} = (B + D)(\bar{A} + B)$$



	D	B	A	المخرج
0000	1	-	-	1
0001	1	-	-	1
0010	-	1	0	1
0011	-	1	1	1
0100	-	-	1	1
0101	-	-	1	1
0110	-	-	1	1
0111	-	-	1	1
1000	-	-	-	0
1001	-	-	-	0
1010	-	-	-	0
1011	-	-	-	0
1100	-	-	-	0
1101	-	-	-	0
1110	-	-	-	0
1111	-	-	-	0

$$AB + C$$

②⑥  $F(A, B, C) = \sum_m (1, 3, 5, 6) + d(0, 7)$

$\begin{matrix} & 001 & 011 & 101 & 110 & 000 & 111 \\ & \swarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \end{matrix}$

Group	min terms	A	B	C	
G1	0	0	0	0	→
G2	1	0	0	1	→
G3	3	0	1	1	→
	5	1	0	1	→
	6	1	1	0	→
G4	7	1	1	1	→

G	min terms	A	B	C	
G1	0, 1	0	0	-	Prime
G2	1, 3	0	-	1	→
	1, 5	-	0	1	→
G3	3, 7	-	1	1	→
	5, 7	1	-	1	→
	6, 7	1	1	-	Prime

G	min terms	A	B	C	
	1, 3, 5, 7	-	-	1	Prime
	<del>1, 3, 5, 7</del>	<del>-</del>	<del>-</del>	<del>1</del>	
	<del>1, 5, 7</del>	<del>.</del>	<del>.</del>	<del>.</del>	

	1	3	5	6	
Prime					
$\overline{A}B$	1				
$A\overline{B}$					1
$C$	1	1	1		

$AB + C$



③ a

3 → input

$\begin{matrix} x \\ y \\ z \end{matrix}$

2 → output

$\begin{matrix} A \\ B \end{matrix}$

(2) 04 = 1010101010101010

x	y	z	A	B
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

تعداد الواجب

of (A)

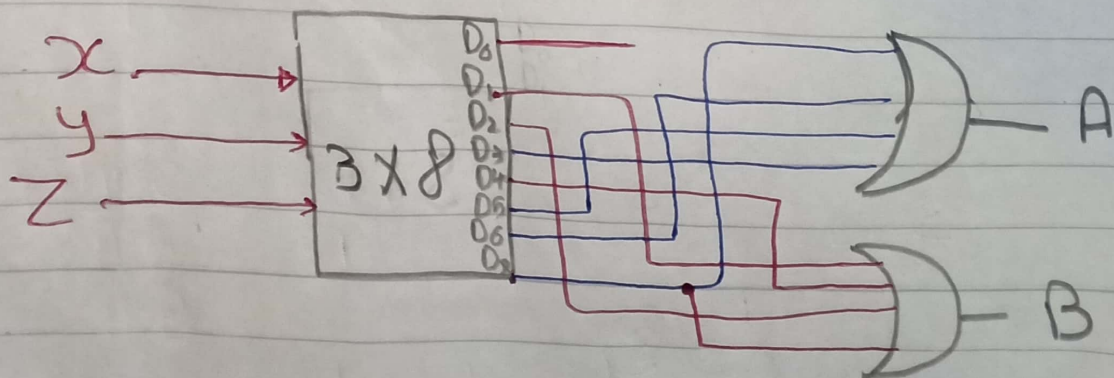
$$A(x, y, z) = \sum_m (3, 5, 6, 7) \quad D_3 \text{ OR } D_5 \text{ OR } D_6 \text{ OR } D_7$$

of (B)

$$B(x, y, z) = \sum_m (1, 2, 4, 7) \quad D_1 \text{ OR } D_2 \text{ OR } D_4 \text{ OR } D_7$$

Decoder  $N \rightarrow 2^N$

3 → 8



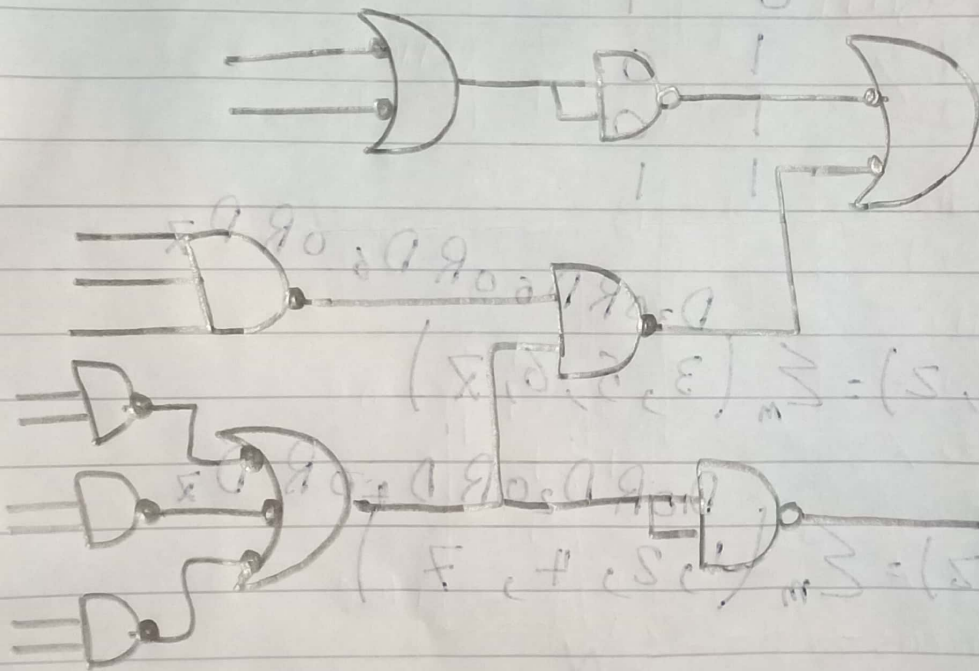
③

③⑥

3 10 10  
Not/or/and

Propagation Delay = 40 (s)

(NAND)



④ a

4 X 1 Multiplexer

$2^n \times 1$

4 input ( $I_3, I_2, I_1, I_0$ )

2 Selector ( $S_1, S_0$ )

1 output ( $Y$ )

$S_1$	$S_0$	$Y$
0	0	$I_0$
0	1	$I_1$
1	0	$I_2$
1	1	$I_3$

$$Y = I_0 \bar{S}_1 \bar{S}_0 + I_1 \bar{S}_1 S_0 + I_2 S_1 \bar{S}_0 + I_3 S_1 S_0$$

④ b

A	B
0	0
0	0
0	0
0	0

0	1
0	1
0	1
0	1

1	0
1	0
1	0
1	0

1	1
1	1
1	1
1	1

$S_1$	$S_0$	F
0	0	1
0	1	0
1	0	0
1	1	1
0	0	1
0	1	1
1	0	1
1	1	0
0	0	0
0	1	1
1	0	1
1	1	1
0	0	0
0	1	0
1	0	0
1	1	0

$S_1$	$S_0$	
0	0	$\bar{A}$
0	1	$A+B$
1	0	$A-B$
1	1	$\bar{B}$

$$F = A \oplus B$$

$$F = \bar{A} + \bar{B}$$

borrow

$$F = A + B$$

ignore carry

$$F = 0$$

⑤



\* عنوان این کار 15  
Full Adder

4X1 Multiplexer

B	0	1
A	0	1
	1	0

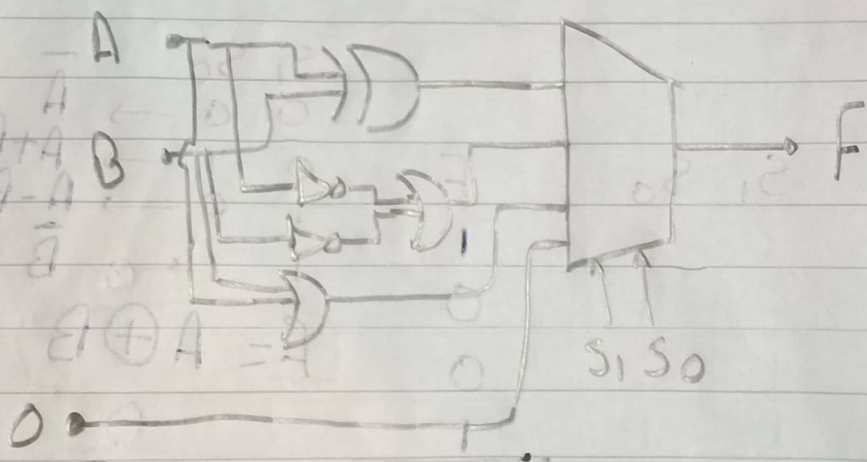
$$\bar{A}\bar{B} + AB = A \oplus B$$

B	0	1
A	0	1
	1	0

$$\bar{A} + \bar{B}$$

B	0	1
A	0	1
	1	1

$$A + B$$



$$B + \bar{A} = 2$$

Worrod

$$B + A = 2$$

(6)

④ ②

$$J_A = (A \oplus X)$$

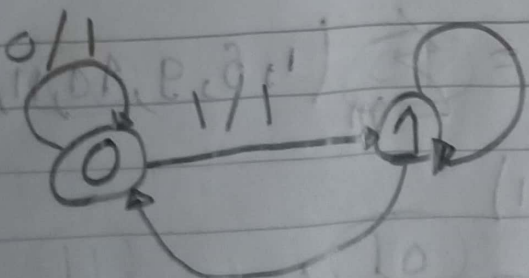
$$K_A = X \oplus \bar{B}$$

$$T_B = \bar{B} + A$$

④ ①

Present + Stat	input	$J_A$	$K_A$	Next + state $A(t+1)$	Y
0 0 A	0	0	1	0	1
0 0 0	0	0	1	1	1
0 0 1	0	1	1	0	0
0 1 0	1	1	1	1	0
0 1 1	1	0	0	1	0

$J_A$	$K_A$	$Q_{next}$
0	0	Q
0	1	0
1	0	1
1	1	$\bar{Q}$



Mealy	Moore
depend Current State and input	depend Current State only

~~Moore~~ Moore

⑦



5

Q	Q <sub>next</sub>	D	Q	Q <sub>next</sub>	T
0	0	0	0	0	0
0	1	1	0	1	1
1	0	0	1	0	1
1	1	1	1	1	0

Present State      Input      From excitation table

A → D flip flop      B → T flip flop

Present State		Input		Next State			
A	B	X	Y	D <sub>A</sub>	T <sub>B</sub>	A(t+1)	B(t+1)
0	0	0	0	0	0	0	0
0	0	0	1	1	0	1	0
0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	0	0	0	0	0
0	1	0	1	1	0	1	1
0	1	1	0	0	1	0	1
0	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1
1	0	0	1	1	0	1	0
1	0	1	0	1	0	1	0
1	0	1	1	1	1	1	1
1	1	0	0	0	0	0	0
1	1	0	1	1	0	1	1
1	1	1	0	1	0	1	1
1	1	1	1	0	1	0	1

min terms of A(t+1)

$$A(t+1)[A, B] = \sum_m (1, 5, 9, 10, 11, 13, 14, 15)$$

min terms of B(t+1)

$$B(t+1)[A, B] = \sum_m (4, 5, 10, 11, 12, 13, 14, 15)$$

min terms of Y

$$Y(A, B) = \sum_m (4, 5, 6, 7, 12, 13, 14, 15)$$

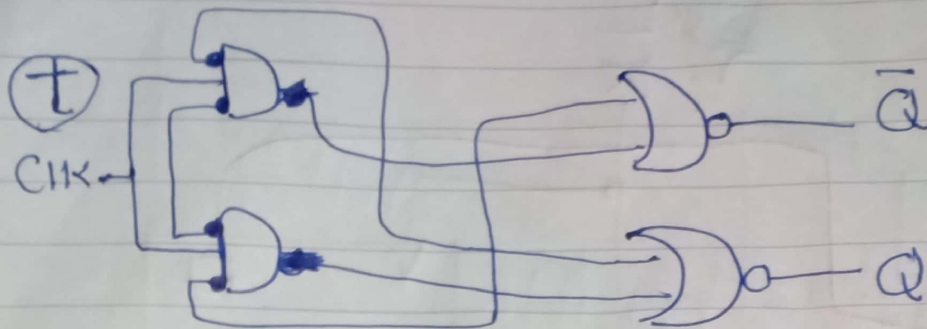
SOP  $\sum$   $\sum$   $\sum$

8



T	En	x	y
	0	x	Q
	1	0	Q
	1	1	$\overline{Q}$

6

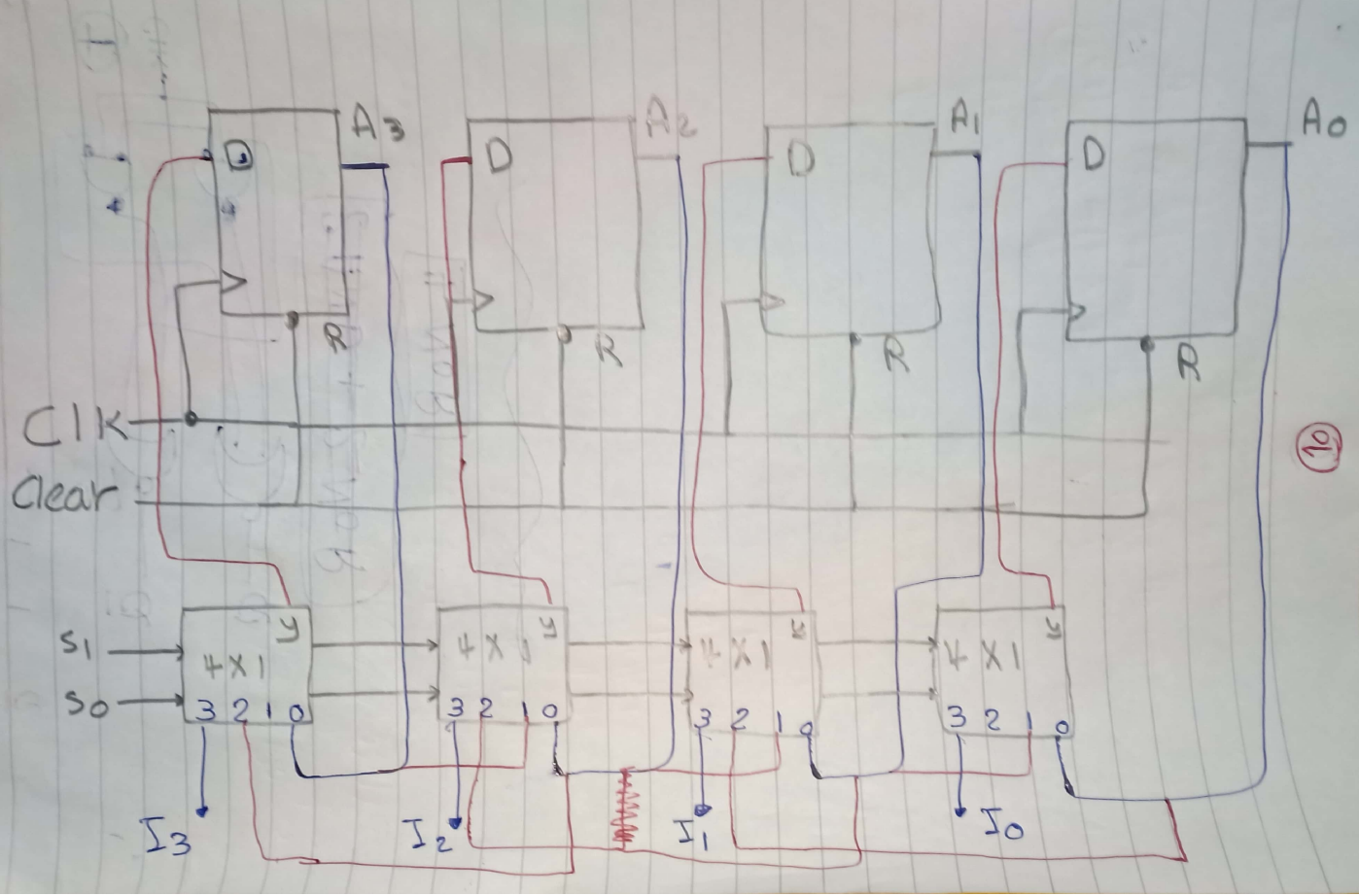


~~2 AND + 2 NOR~~

4 NOR

9

6.0



10



7.a X

7.b

Present State		Next State		F	
		X=0	X=1	X=0	X=1
A	A	A	E	0	0
B	B	B	A	1	0
C	C	A	G	0	0
D	D	F	C	1	1
E	E	G	<del>X</del> H	1	1
F	F	E	<del>X</del> H	1	1
G	G	G	H	1	1
H	H	B	C	1	0
<del>I</del>	<del>I</del>	<del>B</del>	<del>C</del>	<del>1</del>	<del>0</del>
<del>J</del>	<del>J</del>	<del>B</del>	<del>A</del>	<del>1</del>	<del>0</del>

A	A	E	0	0
B	B	A	1	0
<del>C</del>	<del>A</del>	<del>G</del> E	<del>0</del>	<del>0</del>
D	<del>E</del> F	<del>C</del> A	1	1
E	<del>E</del> G	<del>H</del> B	1	1
F	<del>E</del>	<del>H</del> B	1	1
<del>G</del>	<del>G</del>	<del>H</del>	1	1
H	B	<del>C</del> A	1	0

A	A	E	0	0
B	B	A	1	0
D	E	A	1	1
E	E	B	1	1