

Sheet 2 – Logic gates

Question 1:

c)

A	B	C	F	\bar{F}
0	0	0	1	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	0	1

List of Minterms of F: (the decimal no corresponding to 1's)

$$F(A,B,C) = m_0, m_1, m_2, m_5, m_6.$$

List of Minterms of F' :

$$F'(A,B,C) = m_3, m_4, m_7.$$

List of Maxterms of F: (the decimal no corresponding to 0's)

$$F(A,B,C) = M_3, M_4, M_7.$$

List of Maxterms of F' :

$$F'(A,B,C) = M_0, M_1, M_2, M_5, M_6.$$

Sum of Product sop F (1's --.--+--.--+--.--, (0->x',1->x)):

$$F(A,B,C) = A'B'C' + A'B'C + A'BC' + AB'C + ABC'$$

Product of Sum pos F(0's (--+).(--+)).(1->x',0->x)):

$$F(A,B,C) = (A+B'+C').(A'+B+C).(A'+B'+C')$$

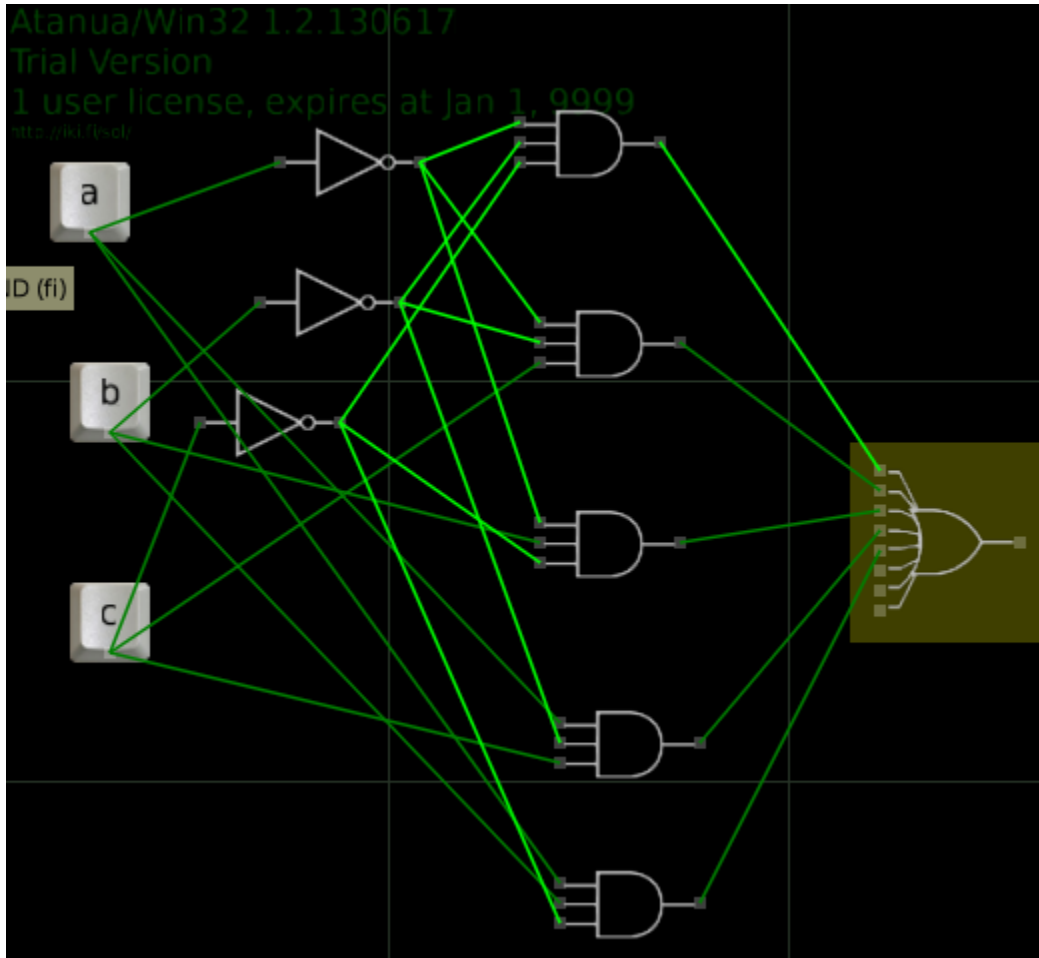
Sum of Product sop F' (1's --.--+--.--+--.--, (0->x',1->x)):

$$F'(A,B,C) = A'BC + AB'C' + ABC$$

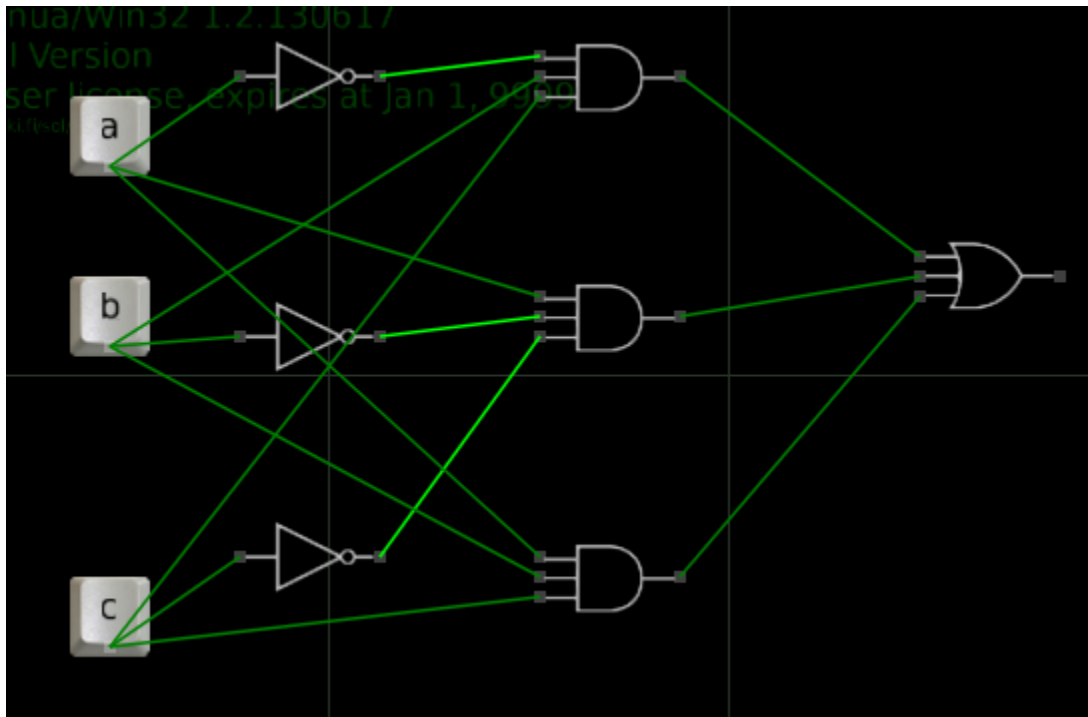
Product of Sum pos $F'(0's ((-+-).(-+-)), (1 \rightarrow x', 0 \rightarrow x))$:

$$F'(A,B,C) = (A+B+C).(A+B+C').(A+B'+C)+(A'+B+C').(A'+B'+C)$$

Logic Diagram of $F(sop)$:



Logic Diagram of $F'(sop)$:



Question 2:

$$B:F(X,Y,Z)=XY+YZ+XY'Z$$

X	Y	Z	XY	YZ	Y'	XY'Z	F
0	0	0	0	0	1	0	0
0	0	1	0	0	1	0	0
0	1	0	0	0	0	0	0
0	1	1	0	1	0	0	1
1	0	0	0	0	1	0	0
1	0	1	0	0	1	1	1
1	1	0	1	0	0	0	1
1	1	1	1	1	0	0	1

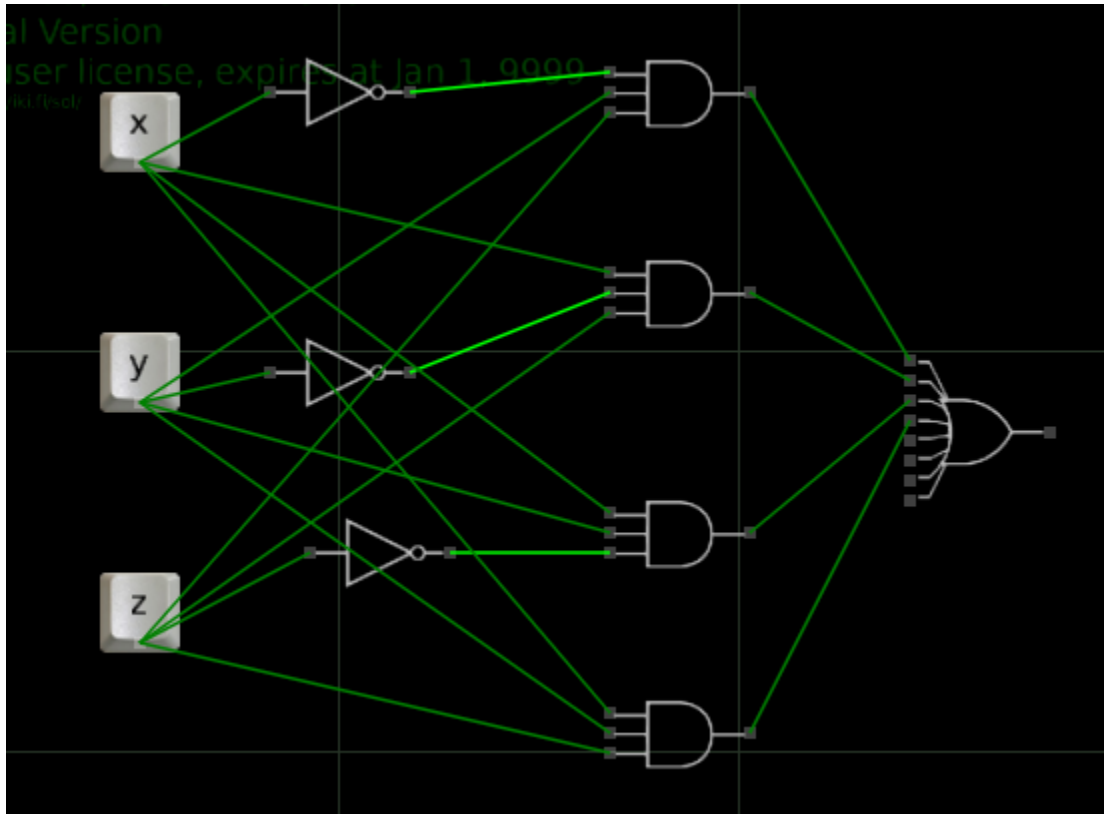
Minterms :m3,m5,m6,m7

$$SOP : X'.Y.Z+X.Y'.Z+X.Y.Z'+X.Y.Z$$

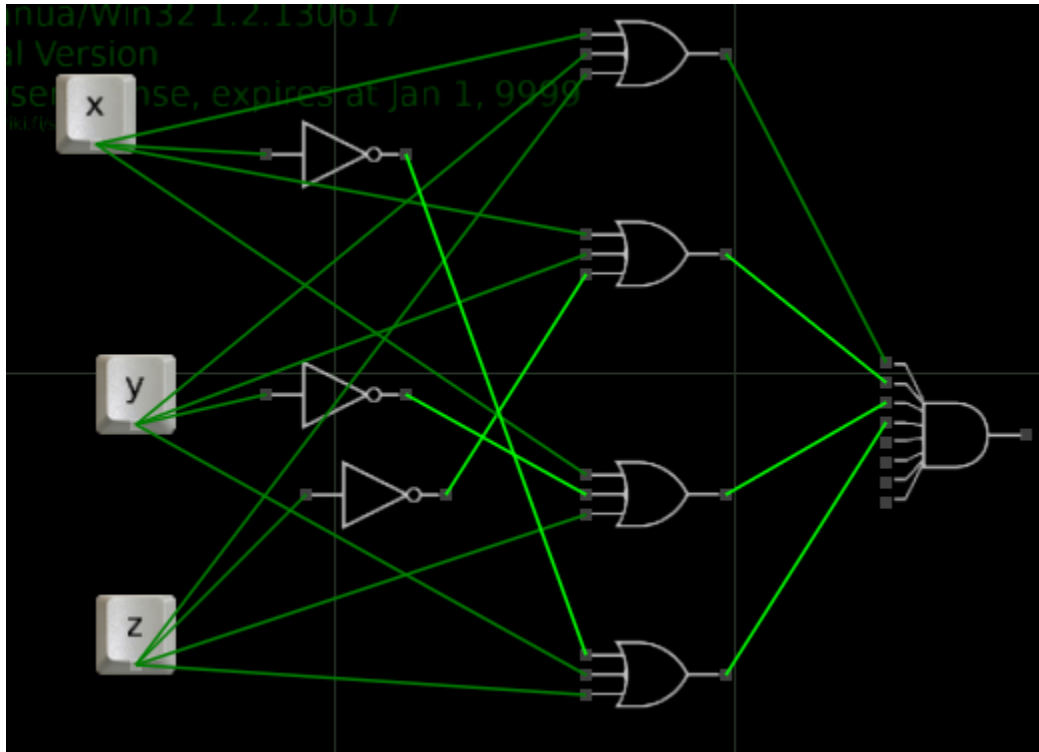
Maxterms : M0,M1,M2,M4

$$POS : (X+Y+Z).(X+Y+Z').(X+Y'+Z).(X'+Y+Z)$$

SOP



POS



Question 3:

g. $F(X,Y,Z)=M(1,3,4,7)$

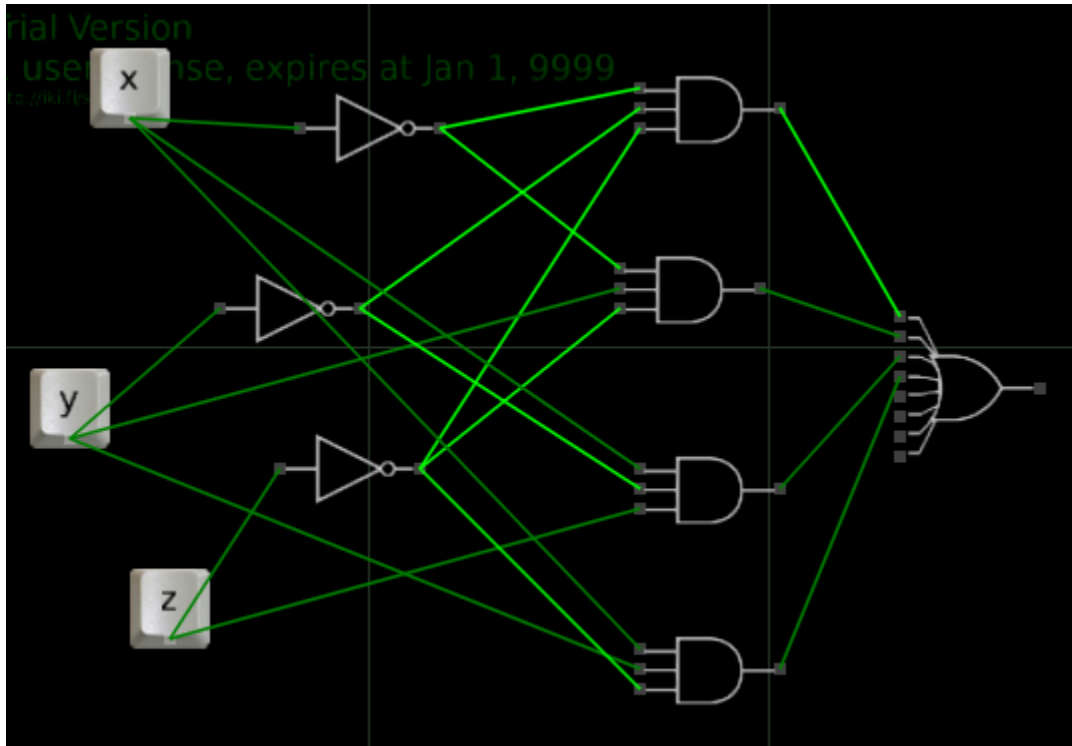
other form= $m(0,2,5,6)$.

X	Y	Z	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

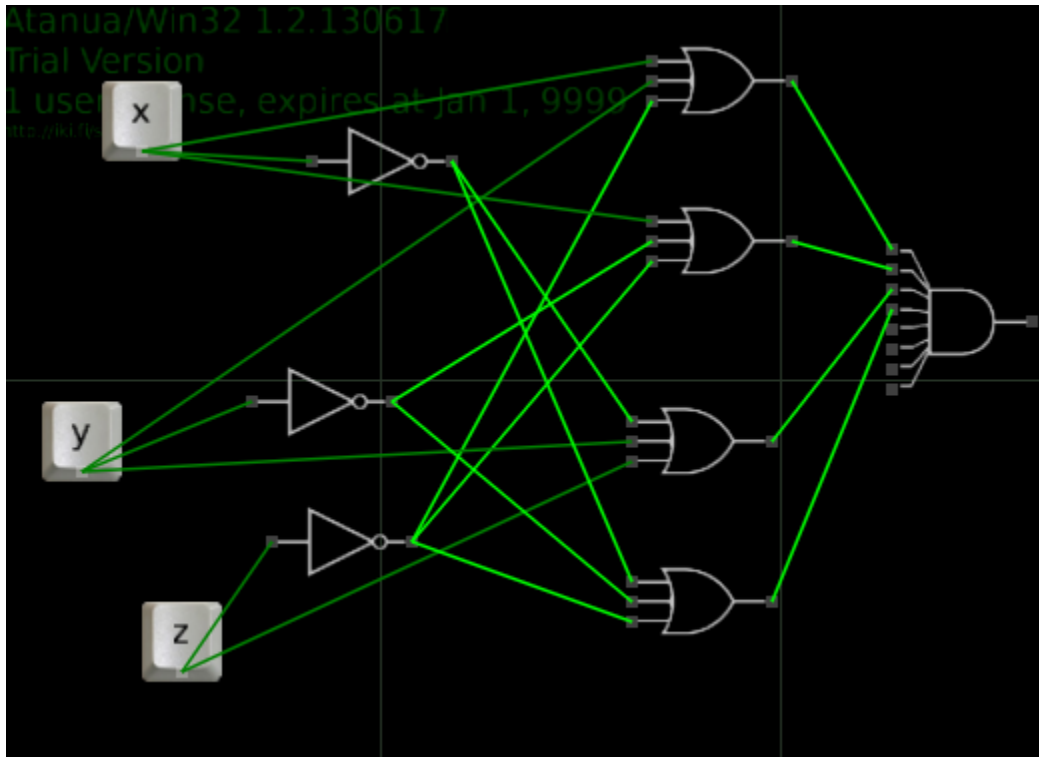
$$\text{SOP} = X'.Y'.Z' + X'.Y.Z' + X.Y'.Z + X.Y.Z'$$

$$\text{POS} = (X+Y+Z').(X+Y'+Z).(X'+Y+Z).(X'+Y'+Z')$$

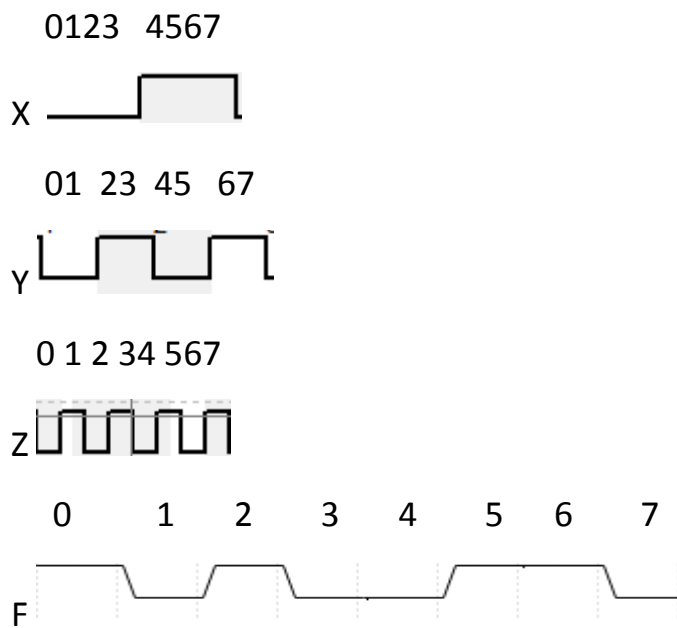
SOP



POS

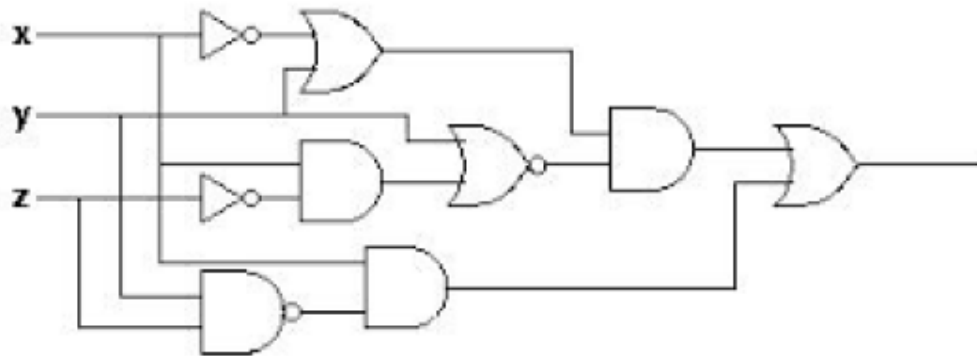


Input-output signal



Question 4

e.



$$F(X,Y,Z)=(X'+Y).((X.Z')+Y)+X.(Y.Z)'$$

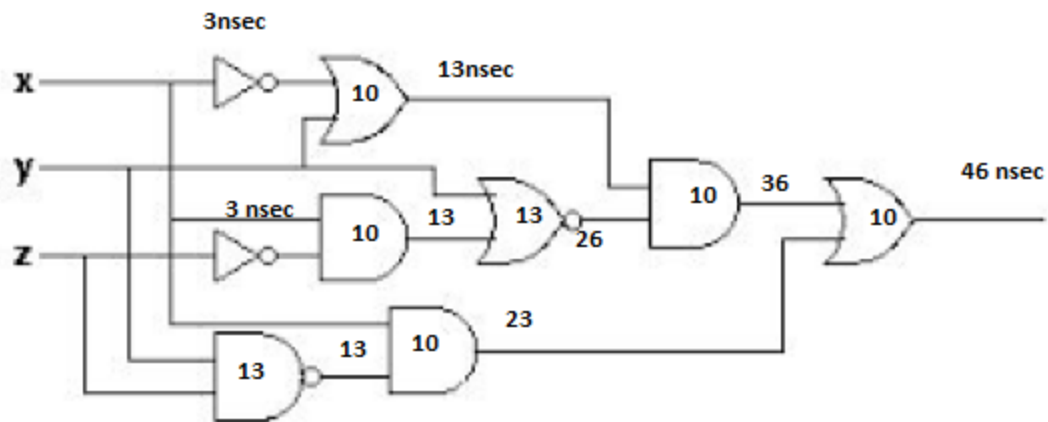
X	Y	Z	(X'+Y)	(X.Z')	(Y+(X.Z'))'	(X'+Y). (Y+(X.Z'))'	(Y.Z)'	(Y.Z)'.X	F
0	0	0	1	0	1	1	1	0	1
0	0	1	1	0	1	1	1	0	1
0	1	0	1	0	0	0	1	0	0
0	1	1	1	0	0	0	0	0	0
1	0	0	0	1	0	0	1	1	1
1	0	1	0	0	1	0	1	1	1
1	1	0	1	1	0	0	1	1	1
1	1	1	1	0	0	0	0	0	0

Minterms : m0,1,4,5,6

Maxterm: M2,3,7

$$\text{SOP: } (X'.Y'Z')+(X'.Y'.Z)+(X.Y'.Z')+(X.Y'.Z)+(X.Y.Z')$$

$$\text{POS: } (X+Y'+Z).(X+Y'+Z').(X'+Y'+Z')$$



Propagation delay = 46 nsec.

Question 5:

e. Four input NAND

TTL SSI 14 pin

2 pin for power

12 are remaining

Four input nand = 4 input and 1 output total=5 pin

$12/5=2.4$ take floor then 2.

Then we need 2 gates.