Cairo University
Faculty of Computers & Artificial Intelligence
Department of Computer Science
Genetic Algorithms Course - 2020

Lab 1 – Canonical Genetic Algorithm

What is the "Genetic Algorithm"?

The genetic algorithm (GA) is a **search heuristic** and a mathematical **simulation** of the process of **natural evolution**. It uses approximate calculations to solve both constrained and unconstrained **optimization** problems.

Genetic algorithms are commonly used to generate high-quality solutions (not necessarily optimal solutions) to optimization and search problems using biologically inspired **operators** such as mutation, crossover and selection.

The basic steps performed by the canonical GA are:

- Initialization (of the population)
- Looping over generations and performing:
 - > Fitness evaluation
 - Selection (of parents for reproduction)
 - Crossover
 - Mutation
 - > Replacement

Some terminologies used in GA:

Before you understand how to solve optimization or search problems using GA, there are a few terminologies that you need to know:

Chromosome	an individual in the population and consists of an array of genes. It
	models one particular solution to the problem we're trying to solve.
Gene	a particular bit in the chromosome. It models a particular trait in the
	solution.
Population	a constant number of chromosomes. It represents the pool of solutions .
Genotype	the genetic structure (how bits are organized) of a particular solution.
Phenotype	the actual solution itself. It can be encoded to or decoded from genotype.

How to solve problems using GA:

Firstly, you need to think how you can appropriately map solutions to chromosomes. Once you're done with that, you can easily apply the canonical GA. (We will explore each step in detail)

• Initialization:

The initial population is generated **randomly**, allowing the entire range of possible solutions (the search space). Occasionally, the solutions may be "**seeded**" in areas where optimal solutions are likely to be found. The population size depends on the nature of the problem, but typically contains several hundreds or thousands of possible solutions.

• Fitness Evaluation:

The fitness function can be the objective function you're trying to maximize (or its inverse if your objective is to minimize a function). The fitness function is evaluated for every chromosome and stored to be used in the selection process.

• Selection:

In this step, we are trying to select some fit parents to breed. A lot of different selection methods exist like "Roulette Wheel" which is one of the popular selection methods used in GA. In the roulette wheel selection, the probability of choosing an individual for breeding is proportional to its fitness; the better the fitness is, the higher chance for that individual to be chosen.

• Crossover:

Crossover is a process of **recombination**. This genetic operator is used to combine the genetic information of two parents to generate new offspring. Crossover is performed with a certain probability (**P**_c) and at a single random crossover point. (Note: We can also perform **k-point** crossover.)

• Mutation:

Mutation alters one or more gene values in a chromosome from its initial state to maintain diversity. It is also performed according to a certain probability (P_m).

• Replacement:

There are several different replacement schemes such as:

- Generational replacement: reproduce enough offspring to replace all population.
 Drawbacks: possibility of losing good genes.
- Steady-state replacement: a number of individuals are selected to reproduce, and the offspring replace their parents.
 - *Drawbacks:* possibility of losing of good chromosomes.
- **Elitist Strategy:** like steady-state replacement but allows keeping the best so far. *Drawbacks:* after some time, chromosomes will become a copy of each other.

Exercise:

How can we use the GA to solve the **"Knapsack Problem"**?

Given:

- A knapsack that can carry weights up to **W**
- N items; each item (x_i) has a weight (w_i) and a value (v_i)

Objective:

- Select the items to carry in the knapsack in order to maximize the total value.

(max.
$$\sum_{i=1}^{N} x_i$$
 . $v_i)$

Constraints:

- The selected items must fit inside the knapsack.
- The entire item is either selected or not.

$$(\sum_{i=1}^{N} x_i$$
 . $w_i \le W$ and $x_i = 0$ or 1)

Sol.:

We can represent a solution (the items selected) as a chromosome containing **N bits**; each bit (i) corresponds to item (i) where 1 means that the item is selected and 0 means that it is not selected.

Assume W = 10, N = 5 and we are given a list of pairs containing each items weight and value: [(5,4), (4,4), (2,1), (2,7), (4,6)]

Step 1: Let's say we started with following randomly initialized chromosomes:

0	1	0	1
1	1	1	0
1	0	0	0
0	0	0	0
1	0	0	0
<u>C1</u>	C2	C3	C4

Note: To make sure your mapping works, you can easily decode these genotypes into phenotypes. For example:

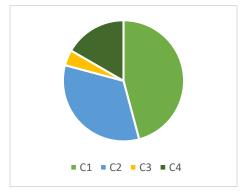
C1: C1[0]=0 -> item 1 is not selected, C1[1]=1 -> item 2 is selected, C1[3]=1 -> item 3 is selected, C1[4]=0 -> item 4 is not selected and C1[5]=1 -> item 5 is selected.

Step 2: Let's evaluate the fitness of each chromosome using the objective function:

Chromosome	Fitness
C1	11
C2	8
C3	1
C4	4

Step 3: Let's select the parents! First, we need to calculate the cumulative fitness function:

Chromosome	Fitness	Cumulative Fitness
C1	11	11
C2	8	19
C3	1	20
C4	4	24



Note: Another option is to **normalize** the fitness first by dividing it over the total fitness sum to make it range between 0 and 1 (representing the **probability** of selection) and then calculate the cumulative probabilities.

Second, generate a random number (r1) between 0 and 24:

If $0 \le r \le 11$, choose C1

If 11 <= r < 19, choose C2

If $19 \le r \le 20$, choose C3

If 20 <= r < 24, choose C4

Assume r1 = 2.32, therefore C1 is the first parent selected. Generate a random number (r2) between 0 and 24 and assume r2 = 16, so select C2 as the second parent.

Step 4: Let's perform crossover between C1 and C2:

First, generate a random integer (X_c) between 1 and len(C)-1 to be the crossover point. Second, generate a random number (r_c) between 0 and 1:

If $\mathbf{r}_c \ll \mathbf{P}_c$, perform crossover at \mathbf{X}_c .

If $\mathbf{r}_c > \mathbf{P}_{c}$, no crossover. (O1 = C1 and O2 = C2)

Assume $X_c = 2$, $r_c = 0.5$ and $P_c = 0.6$, so this means that we will perform crossover as follows:



Step 5: Let's perform mutation on the offspring:

Iterate over **each bit** in **each offspring** chromosome and:

- Generate a random number (r) between 0 and 1.
- If $r \leq P_m$, flip that bit.

Question: What will happen if we never performed mutation?

Step 6: Replace the current generation with the new offspring using any of the replacement strategies explained earlier, go to step 2 and repeat the process.