

# Deep Learning

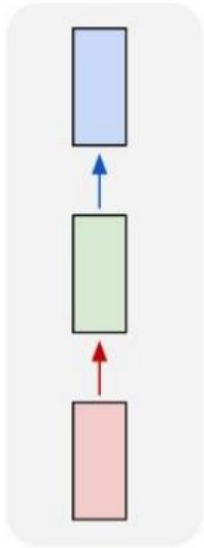
5주차

12기 이두형  
12기 임효진

# Feed Forward Neural Network (Vanilla Neural Network)

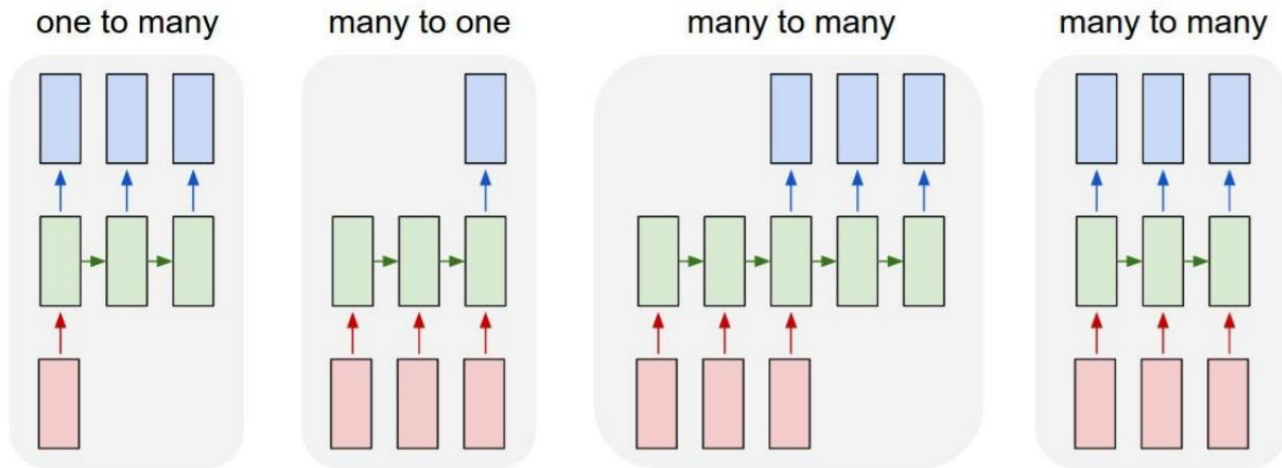
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one to one

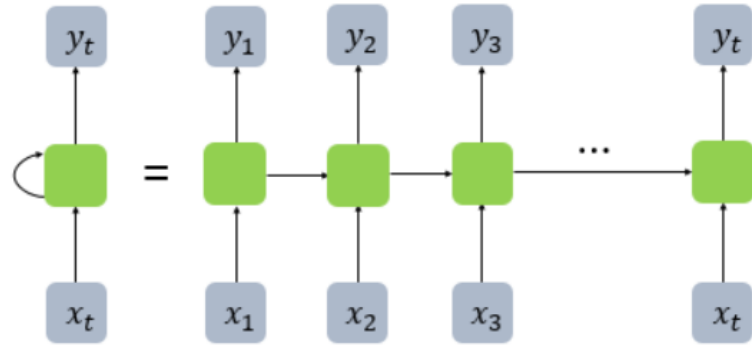


# Recurrent Neural Network (RNN)

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# Recurrent Neural Network (RNN)

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$$\boxed{h_t} = \boxed{f_W}(\boxed{h_{t-1}}, \boxed{x_t})$$

new state

some function  
with parameters  $W$

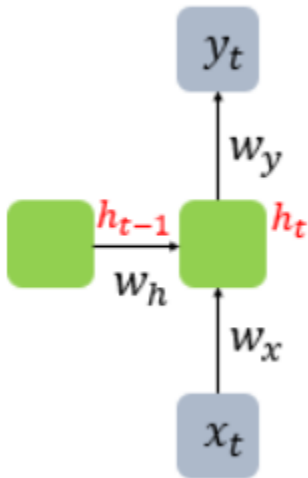
old state

input vector at  
some time step

Notice: the same function and the same set of parameters are used at every time step.

# Recurrent Neural Network (RNN)

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$$h_t = f_W(h_{t-1}, x_t)$$

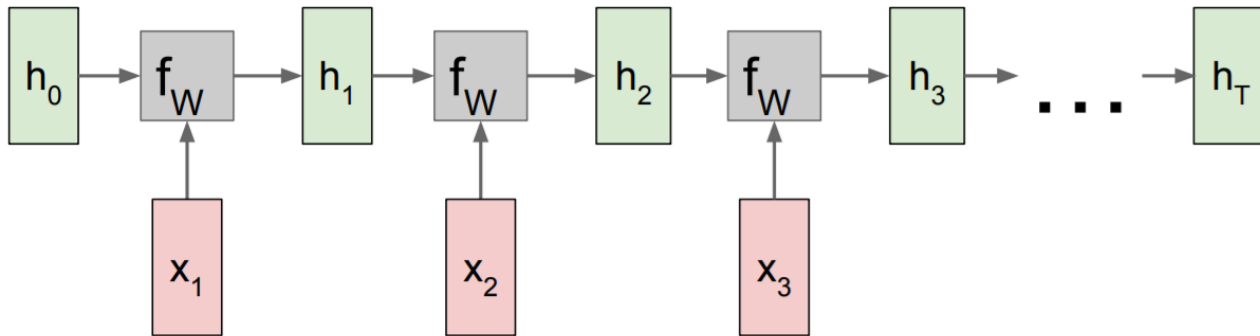


$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

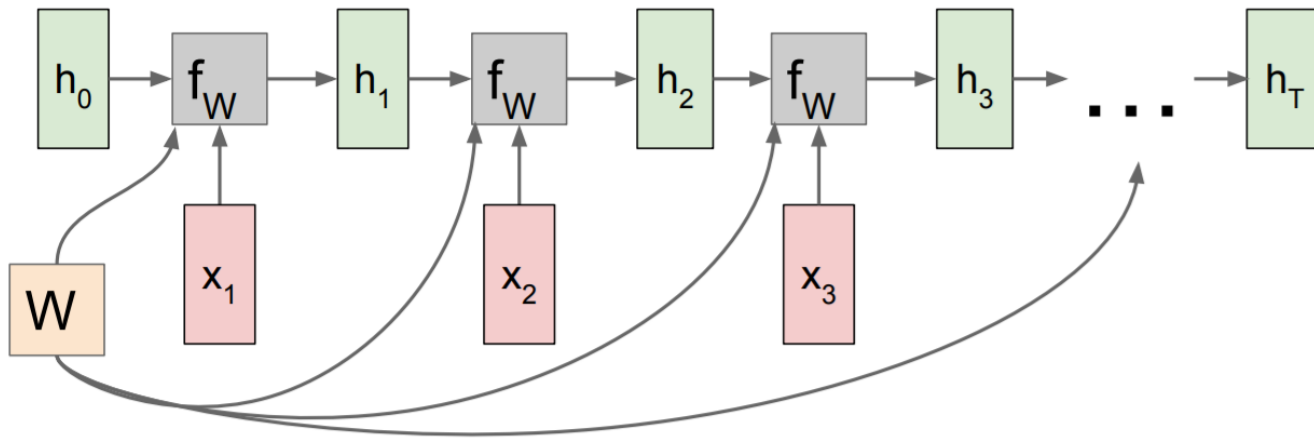
$$y_t = W_{hy}h_t$$

# Recurrent Neural Network (RNN)

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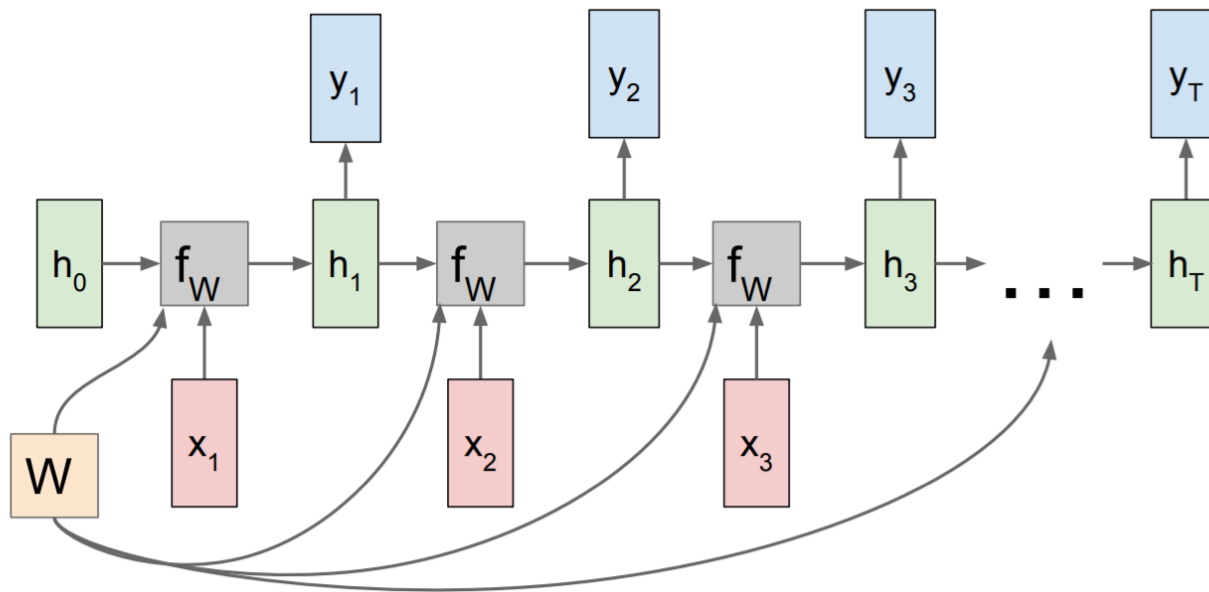


# Recurrent Neural Network (RNN)

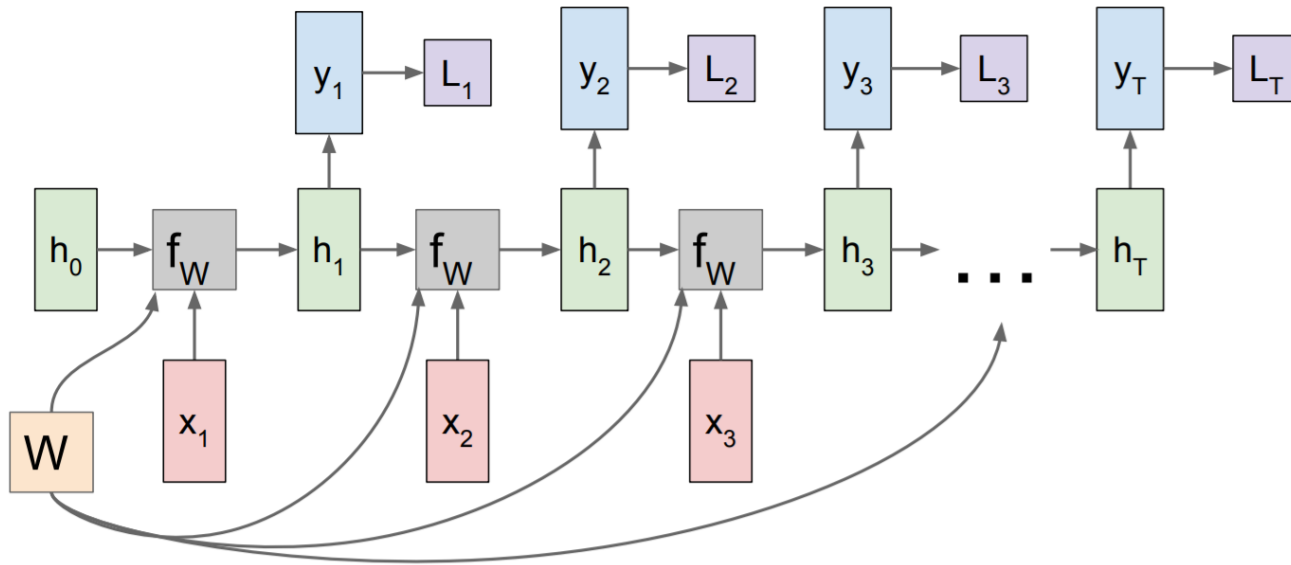




# Recurrent Neural Network (RNN)



# Recurrent Neural Network (RNN)



# Traditional Language Model – Statistical Language Model

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$$P(x_1, x_2, x_3 \dots x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1, x_2) \dots P(x_n|x_1 \dots x_{n-1})$$

$$P(\text{An adorable little boy is spreading smiles}) =$$

$$P(\text{An}) \times P(\text{adorable}|\text{An}) \times P(\text{little}|\text{An adorable}) \times P(\text{boy}|\text{An adorable little}) \times P(\text{is}|\text{An adorable little boy}) \\ \times P(\text{spreading}|\text{An adorable little boy is}) \times P(\text{smiles}|\text{An adorable little boy is spreading})$$

$$P(\text{is}|\text{An adorable little boy}) = \frac{\text{count}(\text{An adorable little boy is})}{\text{count}(\text{An adorable little boy})}$$

# Traditional Language Model - N-gram Language Model

---

$$P(\text{is}|\text{An adorable little boy}) \approx P(\text{is}|\text{boy})$$

$$P(\text{is}|\text{An adorable little boy}) \approx P(\text{is}|\text{little boy})$$

~~An adorable little~~ boy is spreading ?  
무시됨!  
n-1개의 단어

$$P(w|\text{boy is spreading}) = \frac{\text{count}(\text{boy is spreading } w)}{\text{count}(\text{boy is spreading})}$$

There are A LOT of n-grams!  
→ Gigantic RAM requirements!

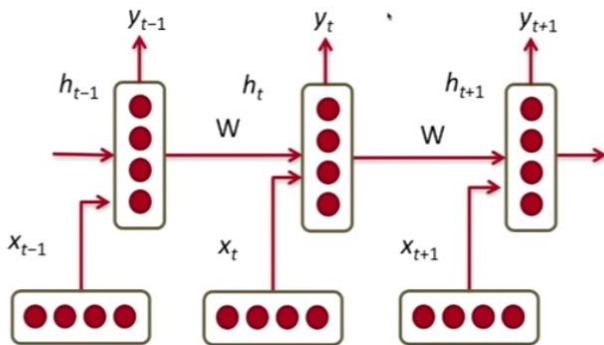
# RNN Language Model

Given list of word **vectors**:  $x_1, \dots, x_{t-1}, x_t, x_{t+1}, \dots, x_T$

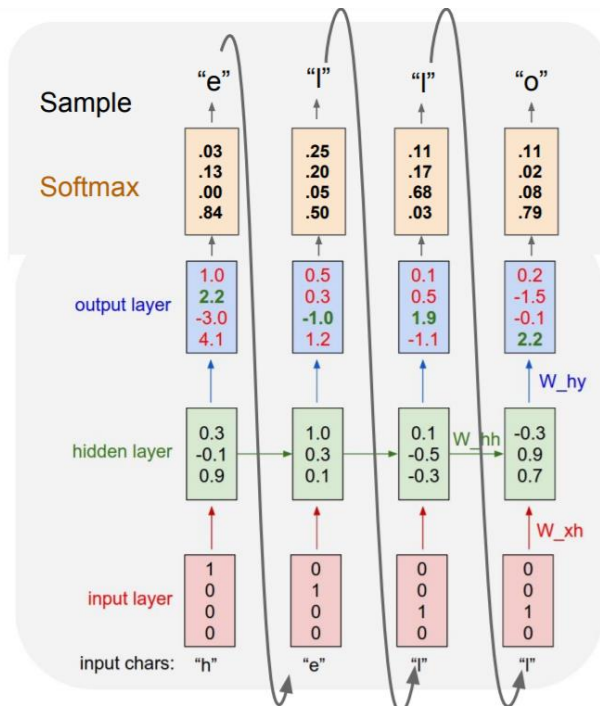
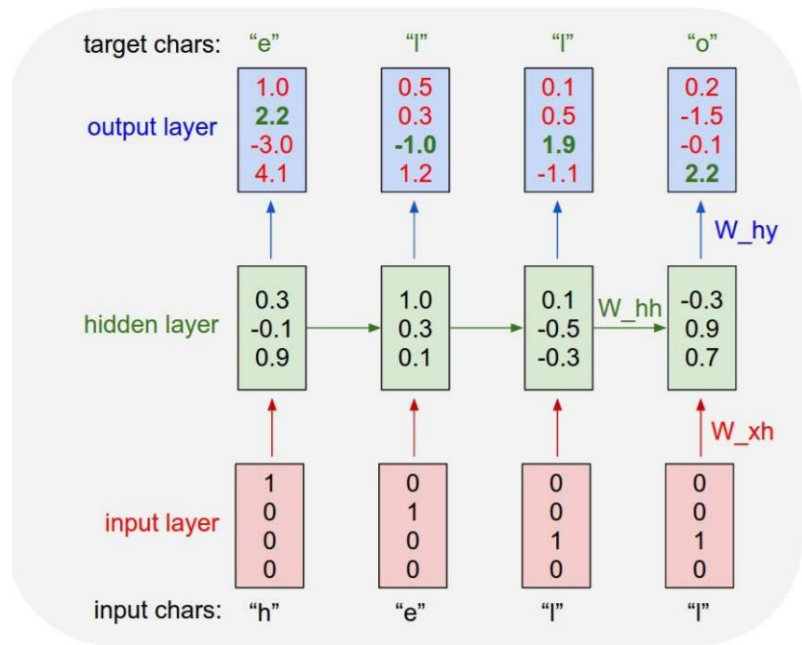
At a single time step:  $h_t = \sigma \left( W^{(hh)} h_{t-1} + W^{(hx)} x_{[t]} \right)$

$$\hat{y}_t = \text{softmax} \left( W^{(S)} h_t \right)$$

$$\hat{P}(x_{t+1} = v_j \mid x_t, \dots, x_1) = \hat{y}_{t,j}$$



# RNN Language Model



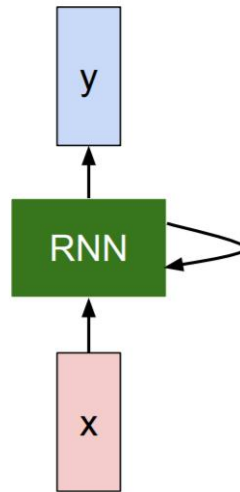
# Examples of RNN Language Models

## THE SONNETS

by William Shakespeare

From fairest creatures we desire increase,  
That thereby beauty's rose might never die,  
But as the ripper should by time decease,  
His tender heir might bear his memory:  
But thou, contracted to thine own bright eyes,  
Feed'st thy light's flame with self-substantial fuel,  
Making a famine where abundance lies,  
Thyself thy foe, to thy sweet self too cruel:  
Thou that art now the world's fresh ornament,  
And only herald to the gaudy spring,  
Within thine own buduriest thy content,  
And tender churl mak'st waste in niggarding:  
Pity the world, or else this glutton be,  
To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow,  
And dig deep trenches in thy beauty's field,  
Thy youth's proud livery so gazed on now,  
Will be a tatter'd weed of small worth held:  
Then being asked, where all thy beauty lies,  
Where all the treasure of thy lusty days;  
To say, within thine own deep sunken eyes,  
Were an all-eating shame, and thriftless praise.  
How much more praise deserv'd thy beauty's use,  
If thou couldst answer 'This fair child of mine  
Shall sum my count, and make my old excuse,'  
Proving his beauty by succession thine!  
This were to be new made when thou art old,  
And see thy blood warm when thou feel'st it cold.



at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e  
plia tklrge t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

↓  
train more

"Tmont thithey" fomesscerliund  
Keushey. Thom here  
sheulke, anmerenith ol sivh I lalterthend Bleipile shuw y fil on aseterlome  
coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

↓  
train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of  
her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort  
how, and Gogition is so overelical and ofter.

↓  
train more

"Why do what that day," replied Natasha, and wishing to himself the fact the  
princess, Princess Mary was easier, fed in had oftened him.  
Pierre aking his soul came to the packs and drove up his father-in-law women.



PANDARUS:

Alas, I think he shall be come approached and the day  
When little strain would be attain'd into being never fed,  
And who is but a chain and subjects of his death,  
I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul,  
Breaking and strongly should be buried, when I perish  
The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and  
my fair nudes begun out of the fact, to be conveyed,  
Whose noble souls I'll have the heart of the wars.

Clown:

Come, sir, I will make did behold your worship.

VIOLA:

I'll drink it.


VIOLA:

Why, Salisbury must find his flesh and thought  
That which I am not apt, not a man and in fire,  
To show the reining of the raven and the wars  
To grace my hand reproach within, and not a fair are hand,  
That Caesar and my goodly father's world;  
When I was heaven of presence and our fleets,  
We spare with hours, but cut thy council I am great,  
Murdered and by thy master's ready there  
My power to give thee but so much as hell:  
Some service in the noble bondman here,  
Would show him to her wine.

KING LEAR:







O, if you were a feeble sight, the courtesy of your law,  
Your sight and several breath, will wear the gods  
With his heads, and my hands are wonder'd at the deeds,  
So drop upon your lordship's head, and your opinion  
Shall be against your honour.

# The Stacks Project: open source algebraic geometry textbook

 **The Stacks Project**

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**Statistics**

The Stacks project now consists of

- 455910 lines of code
- 14221 tags (56 inactive tags)
- 2366 sections

Latex source

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For  $\bigoplus_{n=1, \dots, m}$  where  $\mathcal{L}_{m, \bullet} = 0$ , hence we can find a closed subset  $\mathcal{H}$  in  $\mathcal{H}$  and any sets  $\mathcal{F}$  on  $X$ ,  $U$  is a closed immersion of  $S$ , then  $U \rightarrow T$  is a separated algebraic space.

*Proof.* Proof of (1). It also start we get

$$S = \text{Spec}(R) = U \times_X U \times_X U$$

and the comparicoly in the fibre product covering we have to prove the lemma generated by  $\coprod Z \times_U U \rightarrow V$ . Consider the maps  $M$  along the set of points  $\text{Sch}_{fppf}$  and  $U \rightarrow U$  is the fibre category of  $S$  in  $U$  in Section, ?? and the fact that any  $U$  affine, see Morphisms, Lemma ???. Hence we obtain a scheme  $S$  and any open subset  $W \subset U$  in  $\text{Sh}(G)$  such that  $\text{Spec}(R') \rightarrow S$  is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that  $f_i$  is of finite presentation over  $S$ . We claim that  $\mathcal{O}_{X, x}$  is a scheme where  $x, x', s'' \in S'$  such that  $\mathcal{O}_{X, x'} \rightarrow \mathcal{O}_{X', x'}$  is separated. By Algebra, Lemma ?? we can define a map of complexes  $\text{GL}_{S'}(x'/S'')$  and we win.  $\square$

To prove study we see that  $\mathcal{F}|_U$  is a covering of  $\mathcal{X}'$ , and  $\mathcal{T}_i$  is an object of  $\mathcal{F}_{X/S}$  for  $i > 0$  and  $\mathcal{F}_p$  exists and let  $\mathcal{F}_i$  be a presheaf of  $\mathcal{O}_X$ -modules on  $\mathcal{C}$  as a  $\mathcal{F}$ -module. In particular  $\mathcal{F} = U/\mathcal{F}$  we have to show that

$$\widetilde{M}^\bullet = \mathcal{I}^\bullet \otimes_{\text{Spec}(k)} \mathcal{O}_{S, s} - i_X^{-1} \mathcal{F}$$

is a unique morphism of algebraic stacks. Note that

$$\text{Arrows} = (\text{Sch}/S)_{fppf}^{\text{opp}}, (\text{Sch}/S)_{fppf}$$

and

$$V = \Gamma(S, \mathcal{O}) \mapsto (U, \text{Spec}(A))$$

is an open subset of  $X$ . Thus  $U$  is affine. This is a continuous map of  $X$  is the inverse, the groupoid scheme  $S$ .

*Proof.* See discussion of sheaves of sets.  $\square$

The result for prove any open covering follows from the less of Example ??. It may replace  $S$  by  $X_{\text{spaces}, \text{étale}}$  which gives an open subspace of  $X$  and  $T$  equal to  $S_{Zar}$ , see Descent, Lemma ??. Namely, by Lemma ?? we see that  $R$  is geometrically regular over  $S$ .

**Lemma 0.1.** Assume (3) and (3) by the construction in the description.

Suppose  $X = \lim |X|$  (by the formal open covering  $X$  and a single map  $\text{Proj}_X(\mathcal{A}) = \text{Spec}(B)$  over  $U$  compatible with the complex

$$\text{Set}(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$$

When in this case of to show that  $\mathcal{Q} \rightarrow \mathcal{C}_{Z/X}$  is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If  $T$  is surjective we may assume that  $T$  is connected with residue fields of  $S$ . Moreover there exists a closed subspace  $Z \subset X$  of  $X$  where  $U$  in  $X'$  is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1)  $f$  is locally of finite type. Since  $S = \text{Spec}(R)$  and  $Y = \text{Spec}(R)$ .

*Proof.* This is form all sheaves of sheaves on  $X$ . But given a scheme  $U$  and a surjective étale morphism  $U \rightarrow X$ . Let  $U \cap U = \coprod_{i=1, \dots, n} U_i$  be the scheme  $X$  over  $S$  at the schemes  $X_i \rightarrow X$  and  $U = \lim_i X_i$ .  $\square$

The following lemma surjective restrocomposes of this implies that  $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{\mathcal{X}, \dots, 0}$ .

**Lemma 0.2.** Let  $X$  be a locally Noetherian scheme over  $S$ ,  $E = \mathcal{F}_{X/S}$ . Set  $\mathcal{I} = \mathcal{I}_1 \subset \mathcal{I}'_n$ . Since  $\mathcal{I}^n \subset \mathcal{I}^n$  are nonzero over  $i_0 \leq \mathfrak{p}$  is a subset of  $\mathcal{I}_{n,0} \circ \overline{A}_2$  works.

**Lemma 0.3.** In Situation ??. Hence we may assume  $\mathfrak{q}' = 0$ .

*Proof.* We will use the property we see that  $\mathfrak{p}$  is the next functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where  $K$  is an  $F$ -algebra where  $\delta_{n+1}$  is a scheme over  $S$ .  $\square$

*Proof.* Omitted. □

**Lemma 0.1.** *Let  $\mathcal{C}$  be a set of the construction.*

*Let  $\mathcal{C}$  be a gerber covering. Let  $\mathcal{F}$  be a quasi-coherent sheaves of  $\mathcal{O}$ -modules. We have to show that*

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

*Proof.* This is an algebraic space with the composition of sheaves  $\mathcal{F}$  on  $X_{\text{étale}}$  we have

$$\mathcal{O}_X(\mathcal{F}) = \{\text{morph}_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where  $\mathcal{G}$  defines an isomorphism  $\mathcal{F} \rightarrow \mathcal{F}$  of  $\mathcal{O}$ -modules. □

**Lemma 0.2.** *This is an integer  $Z$  is injective.*

*Proof.* See Spaces, Lemma ?? □

**Lemma 0.3.** *Let  $S$  be a scheme. Let  $X$  be a scheme and  $X$  is an affine open covering. Let  $\mathcal{U} \subset \mathcal{X}$  be a canonical and locally of finite type. Let  $X$  be a scheme. Let  $X$  be a scheme which is equal to the formal complex.*

*The following to the construction of the lemma follows.*

*Let  $X$  be a scheme. Let  $X$  be a scheme covering. Let*

$$b : X \rightarrow Y' \rightarrow Y \rightarrow Y \rightarrow Y' \times_X Y \rightarrow X.$$

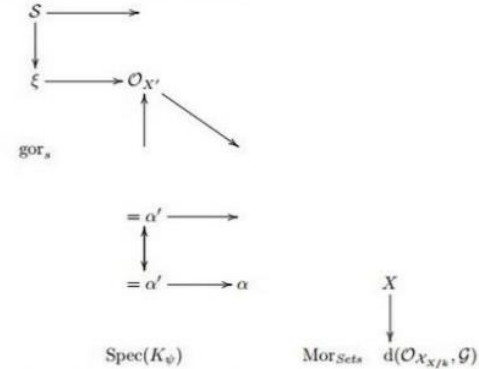
*be a morphism of algebraic spaces over  $S$  and  $Y$ .*

*Proof.* Let  $X$  be a nonzero scheme of  $X$ . Let  $X$  be an algebraic space. Let  $\mathcal{F}$  be a quasi-coherent sheaf of  $\mathcal{O}_X$ -modules. The following are equivalent

- (1)  $\mathcal{F}$  is an algebraic space over  $S$ .
- (2) If  $X$  is an affine open covering.

Consider a common structure on  $X$  and  $X$  the functor  $\mathcal{O}_X(U)$  which is locally of finite type. □

This since  $\mathcal{F} \in \mathcal{F}$  and  $x \in \mathcal{G}$  the diagram



is a limit. Then  $\mathcal{G}$  is a finite type and assume  $S$  is a flat and  $\mathcal{F}$  and  $\mathcal{G}$  is a finite type  $f_*$ . This is of finite type diagrams, and

- the composition of  $\mathcal{G}$  is a regular sequence,
- $\mathcal{O}_{X'}$  is a sheaf of rings.

□

*Proof.* We have see that  $X = \text{Spec}(R)$  and  $\mathcal{F}$  is a finite type representable by algebraic space. The property  $\mathcal{F}$  is a finite morphism of algebraic stacks. Then the cohomology of  $X$  is an open neighbourhood of  $U$ . □

*Proof.* This is clear that  $\mathcal{G}$  is a finite presentation, see Lemmas ??.

A reduced above we conclude that  $U$  is an open covering of  $\mathcal{C}$ . The functor  $\mathcal{F}$  is a "field

$$\mathcal{O}_{X,x} \rightarrow \mathcal{F}_x \rightarrow \mathcal{O}_{X_{\text{étale}}} \rightarrow \mathcal{O}_{X_{\text{étale}}}^{-1} \mathcal{O}_{X_{\text{étale}}}(\mathcal{O}_{X_{\text{étale}}})$$

is an isomorphism of covering of  $\mathcal{O}_{X_1}$ . If  $\mathcal{F}$  is the unique element of  $\mathcal{F}$  such that  $X$  is an isomorphism.

The property  $\mathcal{F}$  is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme  $\mathcal{O}_X$ -algebra with  $\mathcal{F}$  are opens of finite type over  $S$ .

If  $\mathcal{F}$  is a scheme theoretic image points. □

If  $\mathcal{F}$  is a finite direct sum  $\mathcal{O}_{X_{\lambda}}$  is a closed immersion, see Lemma ??.





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branch: master

linux / +



Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux



torvalds authored 9 hours ago

latest commit 4b1706927d

Documentation	Merge git://git.kernel.org/pub/scm/linux/kernel/git/nab/target-pending	6 days ago
arch	Merge branch 'x86-urgent-for-linus' of git://git.kernel.org/pub/scm/...	a day ago
block	block: discard bdi_unregister() in favour of bdi_destroy()	9 days ago
crypto	Merge git://git.kernel.org/pub/scm/linux/kernel/git/herbert/crypto-2.6	10 days ago
drivers	Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux	9 hours ago
firmware	firmware/ihex2fw.c: restore missing default in switch statement	2 months ago
fs	vfs: read file_handle only once in handle_to_path	4 days ago
include	Merge branch 'perf-urgent-for-linus' of git://git.kernel.org/pub/scm/...	a day ago
init	init: fix regression by supporting devices with major:minor:offset fo...	a month ago
io	Merge branch 'for-linus' of git://git.kernel.org/pub/scm/linux/kernel...	a month ago



Code



Pull requests

74



Pulse



Graphs

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```

static void do_command(struct seq_file *m, void *v)
{
    int column = 32 << (cmd[2] & 0x80);
    if (state)
        cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
    else
        seq = 1;
    for (i = 0; i < 16; i++) {
        if (k & (1 << 1))
            pipe = (in_use & UMTHREAD_UNCCA) +
                ((count & 0x00000000ffffffff8) & 0x000000f) << 8;
        if (count == 0)
            sub(pid, ppc_md.kexec_handle, 0x20000000);
        pipe_set_bytes(i, 0);
    }
    /* Free our user pages pointer to place camera if all dash */
    subsystem_info = &of_changes[PAGE_SIZE];
    rek_controls(offset, idx, &soffset);
    /* Now we want to deliberately put it to device */
    control_check_polarity(&context, val, 0);
    for (i = 0; i < COUNTER; i++)
        seq_puts(s, "policy ");
}

```

```

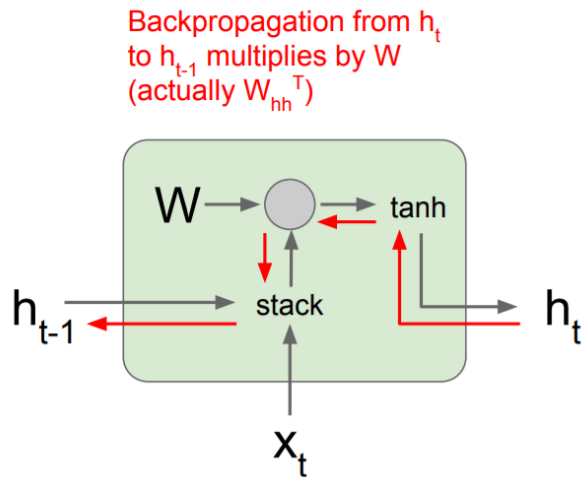
/*
 * Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
 *
 * This program is free software; you can redistribute it and/or modify it
 * under the terms of the GNU General Public License version 2 as published by
 * the Free Software Foundation.
 *
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 * but WITHOUT ANY WARRANTY; without even the implied warranty of
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 * along with this program; if not, write to the Free Software Foundation,
 * Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
 */

#include <linux/kexec.h>
#include <linux/errno.h>
#include <linux/io.h>
#include <linux/platform_device.h>
#include <linux/multi.h>
#include <linux/ckevent.h>

#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system_info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>

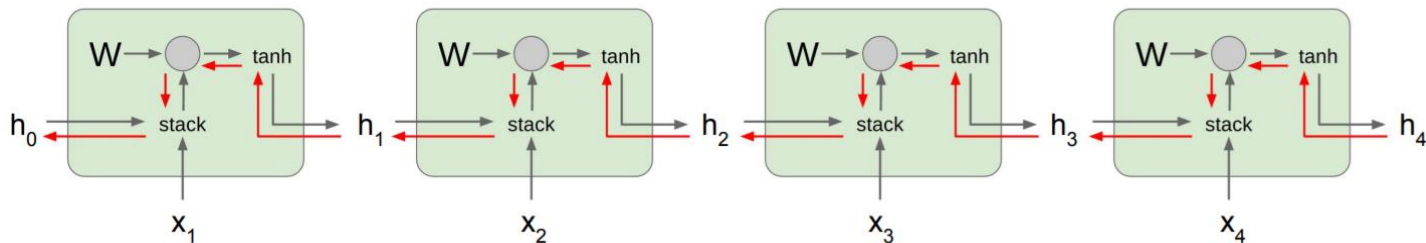
```

# Vanishing / Exploding Gradient Problem



$$\begin{aligned} h_t &= \tanh(W_{hh}h_{t-1} + W_{hx}x_t) \\ &= \tanh\left((W_{hh} \quad W_{hx}) \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \end{aligned}$$

# Vanishing / Exploding Gradient Problem



Computing gradient  
of  $h_0$  involves many  
factors of  $W$   
(and repeated tanh)

Largest singular value  $> 1$ :

**Exploding gradients**

Largest singular value  $< 1$ :

**Vanishing gradients**



# Vanishing / Exploding Gradient Problem

- The solution first introduced by Mikolov is to clip gradients to a maximum value.

**Algorithm 1** Pseudo-code for norm clipping the gradients whenever they explode

```
 $\hat{\mathbf{g}} \leftarrow \frac{\partial \mathcal{E}}{\partial \theta}$   
if  $\|\hat{\mathbf{g}}\| \geq \text{threshold}$  then  
   $\hat{\mathbf{g}} \leftarrow \frac{\text{threshold}}{\|\hat{\mathbf{g}}\|} \hat{\mathbf{g}}$   
end if
```

- Makes a big difference in RNNs.

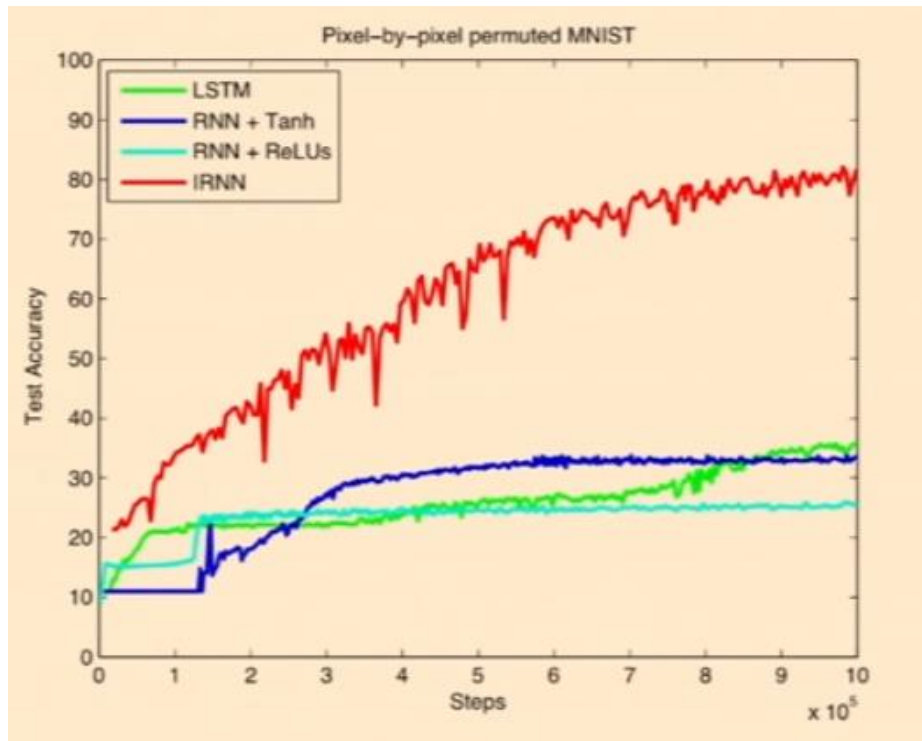
**Gradient clipping:** Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)  
if grad_norm > threshold:  
    grad *= (threshold / grad_norm)
```

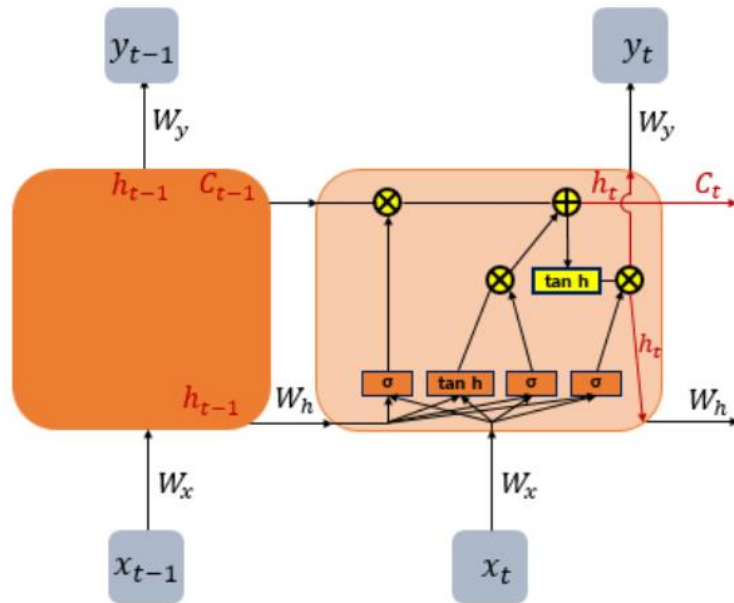
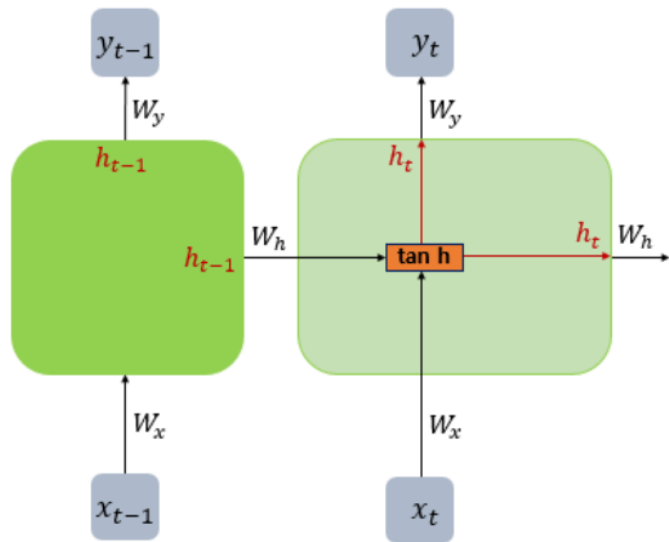
# Vanishing / Exploding Gradient Problem

Jane walked into the room. John walked in too. It was late in the day. Jane said hi to \_\_\_\_

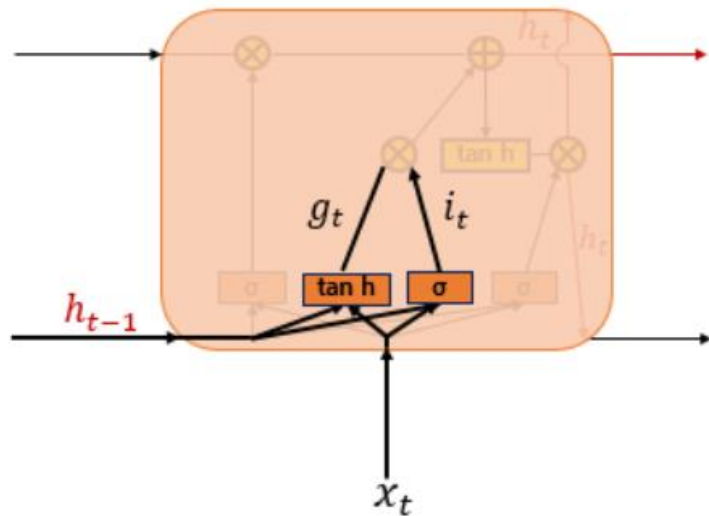
- Initialize  $W^{(*)}$ 's to identity matrix  $I$  and  $f(z) = \text{rect}(z) = \max(z, 0)$
- → Huge difference!



# Long Short Term Memory (LSTM)

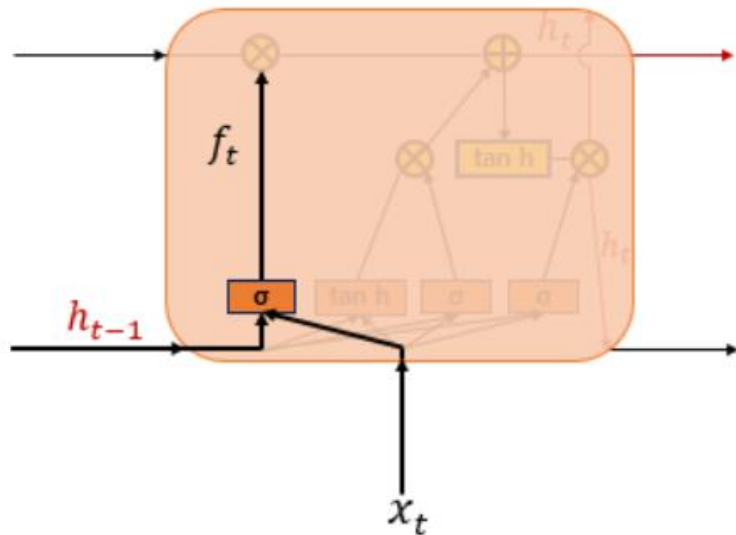


# Input Gate



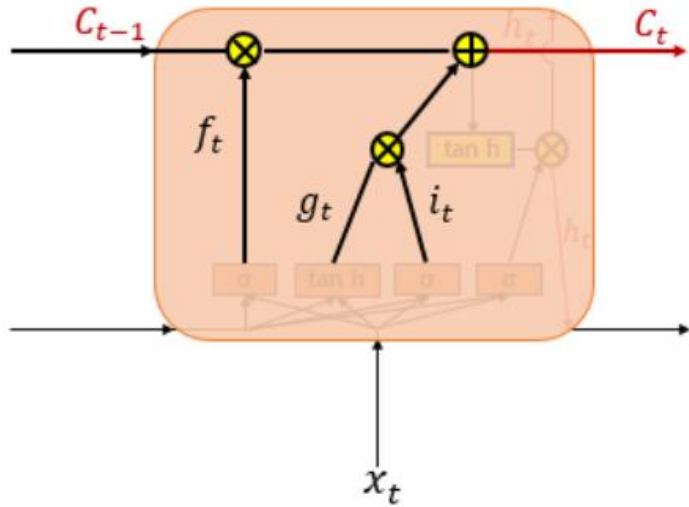
$$i_t = \sigma(W_{xi}x_t + W_{hi}h_{t-1} + b_i)$$
$$g_t = \tanh(W_{xg}x_t + W_{hg}h_{t-1} + b_g)$$

# Forget Gate



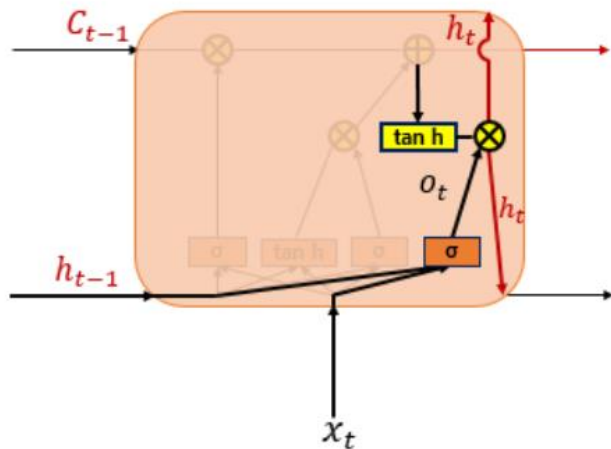
$$f_t = \sigma(W_{xf}x_t + W_{hf}h_{t-1} + b_f)$$

# Cell State



$$C_t = f_t \circ C_{t-1} + i_t \circ g_t$$

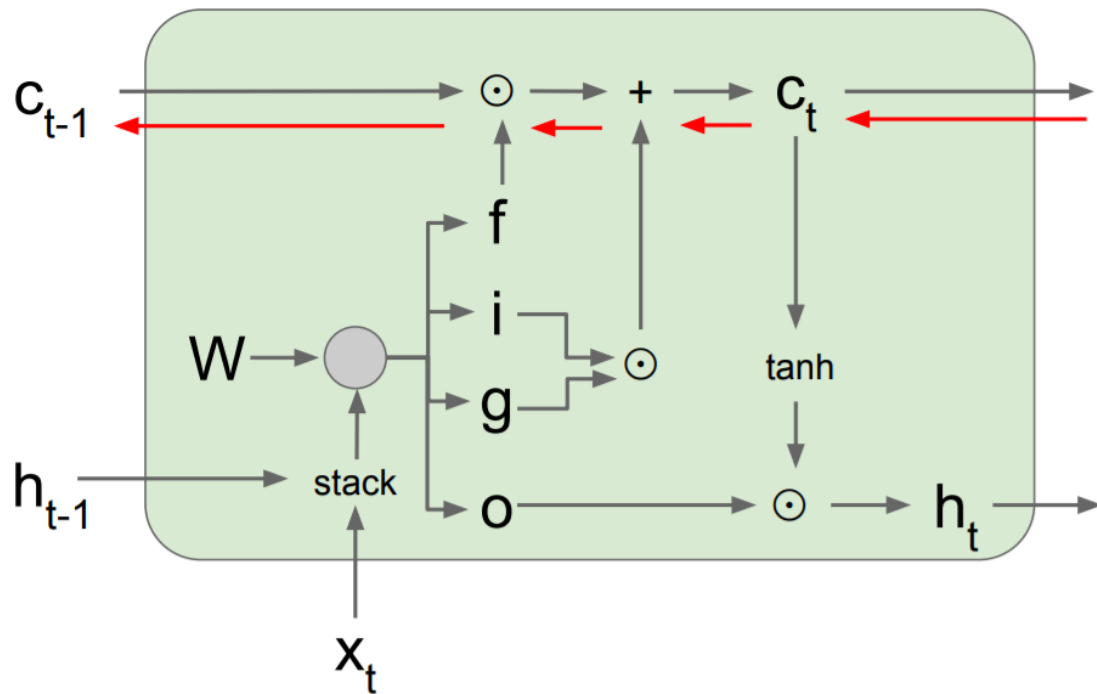
# Output Gate



$$o_t = \sigma(W_{xo}x_t + W_{ho}h_{t-1} + b_o)$$

$$h_t = o_t \circ \tanh(c_t)$$

[Hochreiter et al., 1997]



Backpropagation from  $c_t$  to  $c_{t-1}$  only elementwise multiplication by  $f$ , no matrix multiply by  $W$

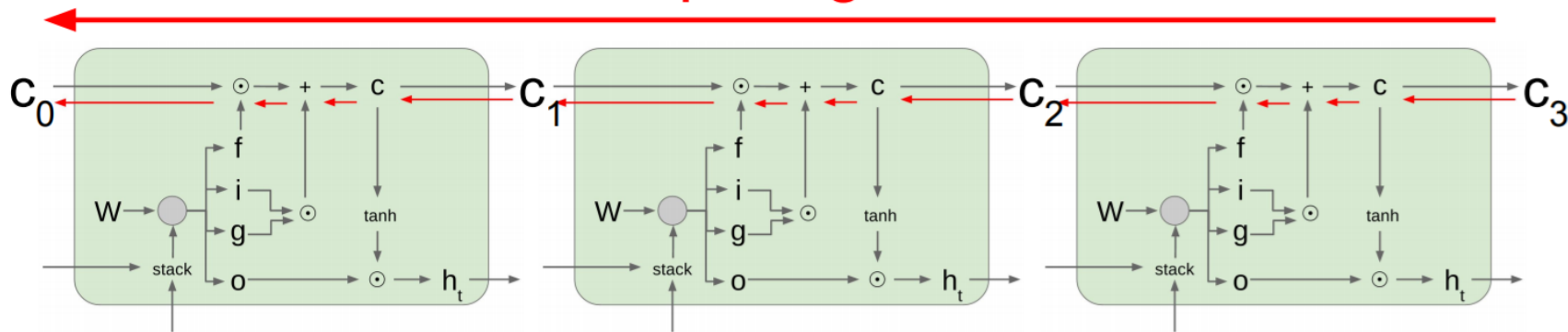
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

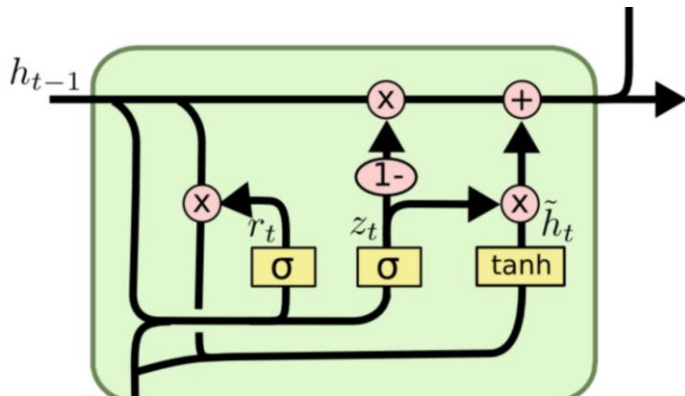
$$h_t = o \odot \tanh(c_t)$$



## Uninterrupted gradient flow!



# Gated Recurrent Unit (GRU)



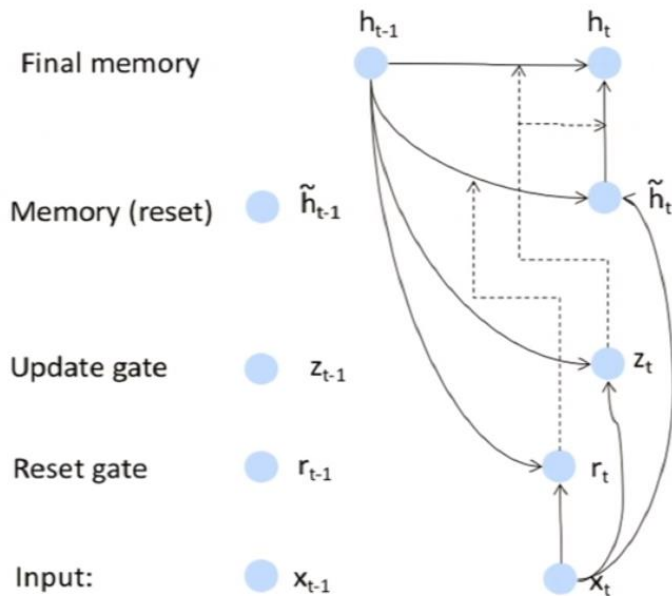
$$z_t = \sigma \left( W^{(z)} x_t + U^{(z)} h_{t-1} \right)$$

$$r_t = \sigma \left( W^{(r)} x_t + U^{(r)} h_{t-1} \right)$$

$$\tilde{h}_t = \tanh \left( W x_t + r_t \circ U h_{t-1} \right)$$

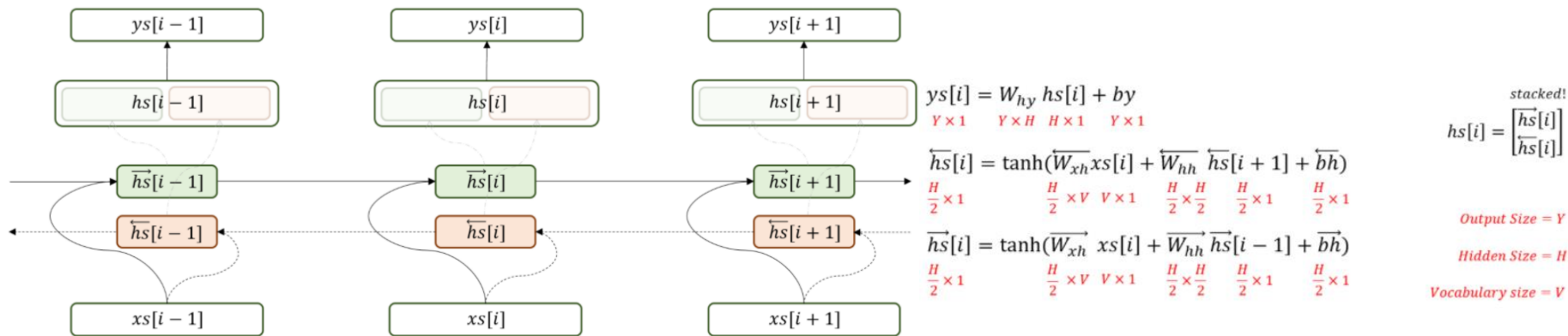
$$h_t = z_t \circ h_{t-1} + (1 - z_t) \circ \tilde{h}_t$$

# Gated Recurrent Unit (GRU)

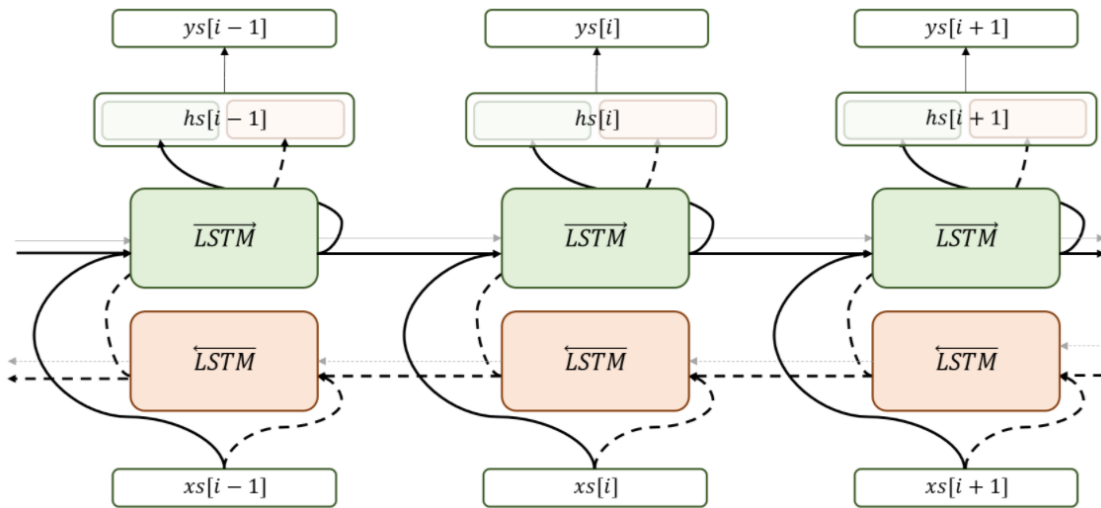
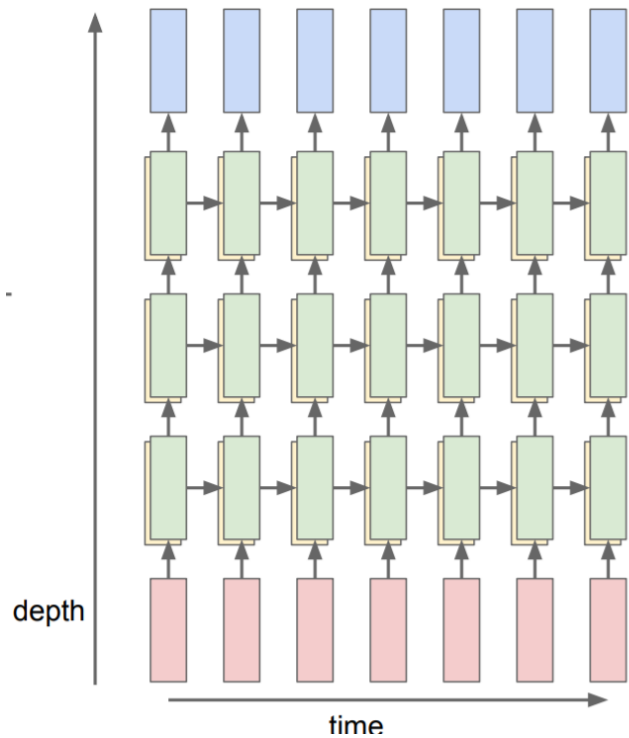


- If reset is close to 0, ignore previous hidden state  
→ Allows model to drop information that is irrelevant in the future
- Update gate  $z$  controls how much of past state should matter now.
  - If  $z$  close to 1, then we can copy information in that unit through many time steps! **Less vanishing gradient!**

# Bidirectional RNN



# Deep RNN



# reference

- Stanford CS231n
- Stanford Natural Language Processing with Deep Learning
- WikiDocs 딥 러닝을 이용한 자연어 처리 입문
- Deep Learning from Scratch 2