Operations in the Field \mathbb{R}^n

As in any field, we can define the mathematical operations of the field \mathbb{R}^n

These **operations** are:

- Addition
- Multiplication

We also need to define the zero and one element in the field.

Zero element :
$$\vec{x} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

One element:
$$\vec{x} = \begin{bmatrix} 1 \\ 1 \\ 1 \\ \vdots \\ 1 \end{bmatrix}$$

The above operations satisfy the **field axioms**:

- Associativity
- Commutativity
- Distributivity
- Identity (defining zero addition and multiplication by one)
- Inverse (defining Subtraction-Additive Inverse and Division-Multiplicative Inverse)

In this lesson we will focus on **vector addition** and **scalar by vector multiplication**.