Matrix Addition

To add one matrix to the other we need to:

- Verify that the matrices are of the same dimensions
- Make sure we add elements in the correct corresponding index.

To put this into context, let's look at an example:

We will focus on the random matrix we saw in equation 11:

$$A = egin{bmatrix} a_{11} & a_{12} & a_{13} & \dots & a_{1n} \\ a_{21} & a_{22} & a_{23} & \dots & a_{2n} \\ a_{31} & a_{32} & a_{33} & \dots & a_{3n} \\ \vdots & & & & & \\ a_{m1} & a_{m2} & a_{m3} & \dots & a_{mn} \end{bmatrix}$$

The dimensions of matrix A are $m \times n$. This means that the matrix has m rows and n columns.

Matrix A can only be added to another matrix with m rows and n columns. For example, matrix B.

$$B = \begin{bmatrix} b_{11} & b_{12} & b_{13} & \dots & b_{1n} \\ b_{21} & b_{22} & b_{23} & \dots & b_{2n} \\ b_{31} & b_{32} & b_{33} & \dots & b_{3n} \\ \vdots & & & & & \\ b_{m1} & b_{m2} & b_{m3} & \dots & b_{mn} \end{bmatrix}$$

Equation 12

As long as the dimensions match, the addition is very simple:

Simply add element a_{ij} in A to the corresponding element b_{ij} in B.

$$A+B=\begin{bmatrix} a_{11} & a_{12} & a_{13} & \dots & a_{1n}\\ a_{21} & a_{22} & a_{23} & \dots & a_{2n}\\ a_{31} & a_{32} & a_{33} & \dots & a_{3n}\\ \vdots & & & & & \\ a_{m1} & a_{m2} & a_{m3} & \dots & a_{mn} \end{bmatrix}+\begin{bmatrix} b_{11} & b_{12} & b_{13} & \dots & b_{1n}\\ b_{21} & b_{22} & b_{23} & \dots & b_{2n}\\ b_{31} & b_{32} & b_{33} & \dots & b_{3n}\\ \vdots & & & & & \\ b_{m1} & b_{m2} & b_{m3} & \dots & b_{mn} \end{bmatrix}$$

$$A+B=\begin{bmatrix} a_{11}+b_{11} & a_{12}+b_{12} & a_{13}+b_{13} & .. & a_{1n}+b_{1n}\\ a_{21}+b_{21} & a_{22}+b_{22} & a_{23}+b_{23} & .. & a_{2n}+b_{2n}\\ a_{31}+b_{31} & a_{32}+b_{32} & a_{33}+b_{33} & .. & a_{3n}+b_{3n}\\ \vdots & & & & & \\ a_{m1}+b_{m1} & a_{m2}+b_{m2} & a_{m3}+b_{m3} & & a_{mn}+b_{mn} \end{bmatrix}$$

Equation 12