

Integration of ecological networks in a theoretical stochastic model of biogeography

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Biogeography

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- Grinnelian niche and Species Distribution Models (SDM)
- However in 1998, in Nature ...

Making mistakes when predicting shifts in species range in response to global warming

Andrew J. Davis⁺, Linda S. Jenkinson⁺, John H. Lawton[†],
Bryan Shorrocks⁺ & Simon Wood^{†‡}

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PNAS

Macroecological signals of species interactions in the Danish avifauna

Nicholas J. Gotelli^{a,1}, Gary R. Graves^b, and Carsten Rahbek^c

^aDepartment of Biology, University of Vermont, Burlington, VT 05405; ^bDepartment of Vertebrate Zoology, National Museum of Natural History, Smithsonian Institution, Washington, DC 20013; and ^cCenter for Macroecology, Evolution and Climate, Department of Biology, University of Copenhagen, DK-2100 Copenhagen Ø, Denmark

Communicated by Thomas W. Schoener, University of California, Davis, CA, December 21, 2009 (received for review August 6, 2009)

The role of intraspecific and interspecific interactions in structuring continental mainland regions (23). Inferences of community

Interactions, a matter a scale ?

■ Fundamental questions:

How interaction consequences propagate over spatial scales ?



Ecography 37: 001–010, 2014

doi: 10.1111/j.1600-0587.2013.00643.x

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Subject Editor: Carsten Rahbek. Accepted 21 October 2013

The geographic scaling of biotic interactions

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The geographic scaling of biotic interactions

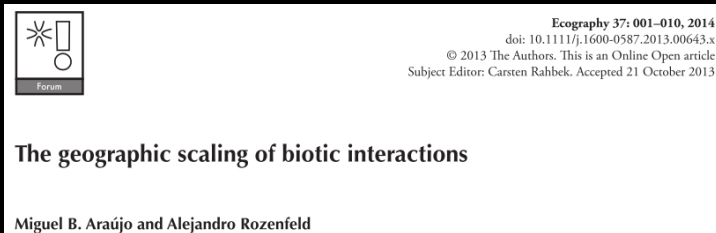
Miguel B. Araújo and Alejandro Rozenfeld

What does a co-occurrence mean ?

Interactions, a matter a scale ?

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What does a co-occurrence mean ?

- The Theory of Biogeography may require some changes !

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Theoretical development

- Recent attempt for integrating a subset of the above mentioned variables:

PNAS

Bitrophic interactions shape biodiversity in space

Franck Jabot^{a,b} and Jordi Bascompte^{b,1}

^aLaboratoire d'Ingénierie pour les Systèmes Complexes, Institut National de Recherche en Sciences et Technologies pour l'Environnement et l'Agriculture, 63172 Aubière, France; and ^bIntegrative Ecology Group, Estación Biológica de Doñana, Consejo Superior de Investigaciones Científicas, E-41092 Sevilla, Spain

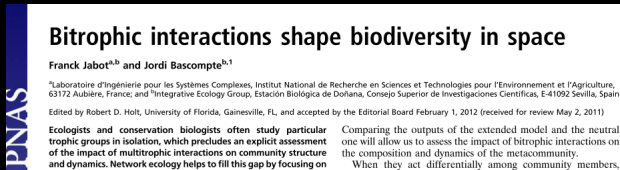
Edited by Robert D. Holt, University of Florida, Gainesville, FL, and accepted by the Editorial Board February 1, 2012 (received for review May 2, 2011)

Ecologists and conservation biologists often study particular trophic groups in isolation, which precludes an explicit assessment of the impact of multitrophic interactions on community structure and dynamics. Network ecology helps to fill this gap by focusing on

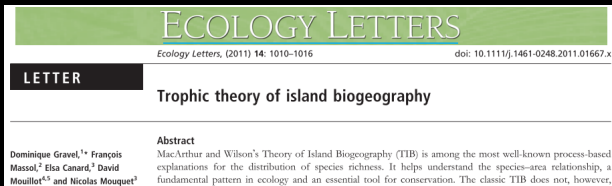
Comparing the outputs of the extended model and the neutral one will allow us to assess the impact of bitrophic interactions on the composition and dynamics of the metacommunity. When they act differentially among community members,

Theoretical development

- Recent attempt for integrating a subset of the above mentioned variables:



- Trophic extension of the Theory of Island Biogeography (TTIB):



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- Supporting the development of the theory of Biogeography
- Generalizing the TTIB model to any kind of networks
- Adding environmental gradients

Theory of Island Biogeography (1967)

- 1 The theory of MacArthur and Wilson is often summarized as follows:

$$\frac{dS}{dt} = c(P - S) - eS$$

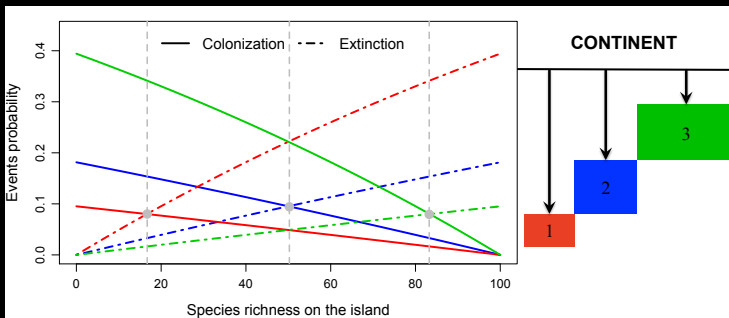
Theory of Island Biogeography (1967)

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- 2 Equilibrium reached for:

$$S_{eq} = P \frac{c}{c + e}$$



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- Let us consider 2 species 1 and 2
- Presence on the island: $X_t = (X_{1,t}, X_{2,t})$
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- How to switch from X_t to X_{t+dt} ?
- Markov chain !

Transition Matrix of the Markov Chains

For independent species:

$(X_{1,t}, X_{2,t})$	$(X_{1,t+dt}, X_{2,t+dt})$			
	$(1,1)$	$(1,0)$	$(0,1)$	$(0,0)$
$(1,1)$	$(1 - e_1 dt)(1 - e_2 dt)$	$(1 - e_1 dt)e_2 dt$	$e_1 dt(1 - e_2 dt)$	$e_1 dt e_2 dt$
$(1,0)$	$(1 - e_1 dt)c_2 dt$	$(1 - e_1 dt)(1 - c_2 dt)$	$e_1 dt c_2 dt$	$e_1 dt(1 - c_2 dt)$
$(0,1)$	$c_1 dt(1 - e_2 dt)$	$c_1 dt e_2 dt$	$(1 - c_1 dt)(1 - e_2 dt)$	$(1 - c_1 dt)e_2 dt$
$(0,0)$	$c_1 dt c_2 dt$	$c_1 dt(1 - c_2 dt)$	$(1 - c_1 dt)c_2 dt$	$(1 - c_1 dt)(1 - c_2 dt)$

Transition Matrix of the Markov Chains

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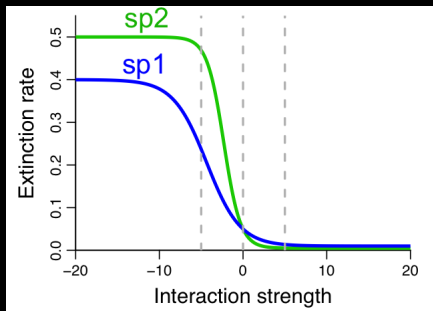
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- Generally applicable to n species.
- Probabilities of all communities at the equilibrium.

Transition Matrix of the Markov Chains

- How interactions impact presence probabilities ?

$$(\text{Interaction Strength})_t = BX_t$$



- Without interaction, we get the classical model.

Simulations

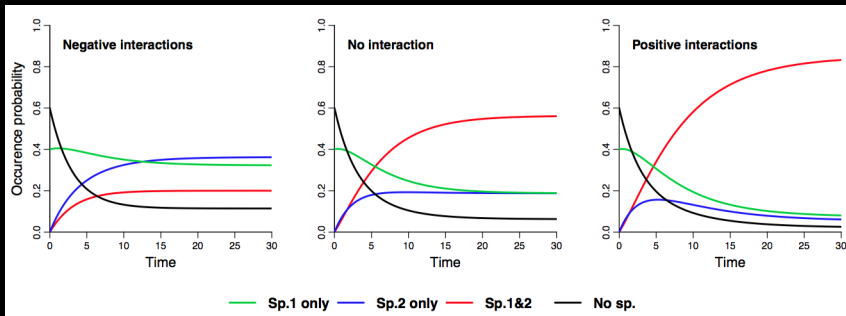
Given:

- ecological network

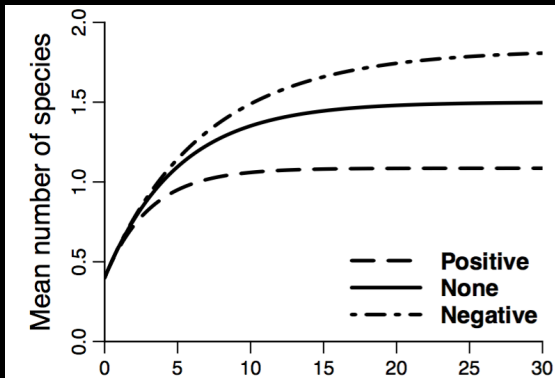
We get:

- Presence probabilities of all communities at equilibrium
- Any probability defined as a sum of the latter, *e.g.* the presence probability of any species

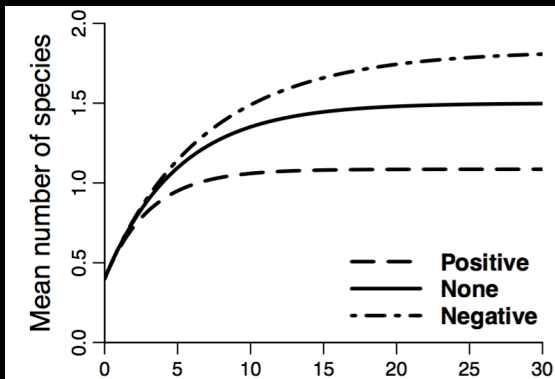
Example with two species



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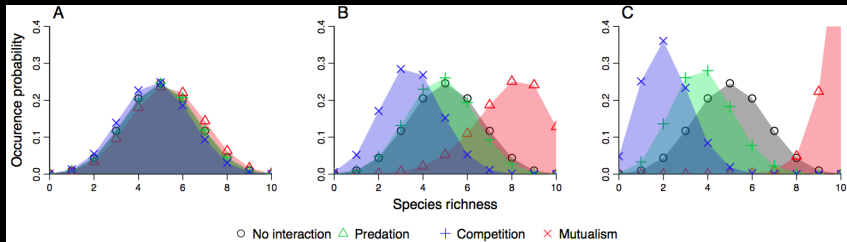
Example with two species



Exploration for networks of 10 species (niche model).

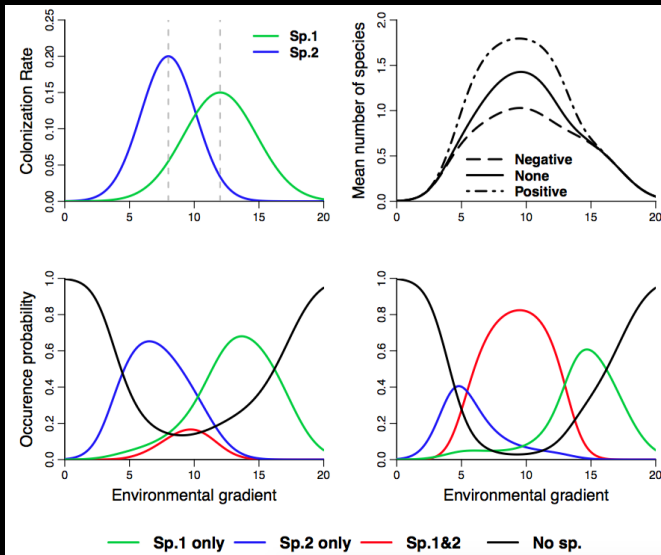
Presence probability of communities of a given diversity

$$\mathbb{P}(S_{eq} = n) = \sum_{i \mid |S_i|^2 = n} \mathbb{P}(X_{eq} = S_i)$$

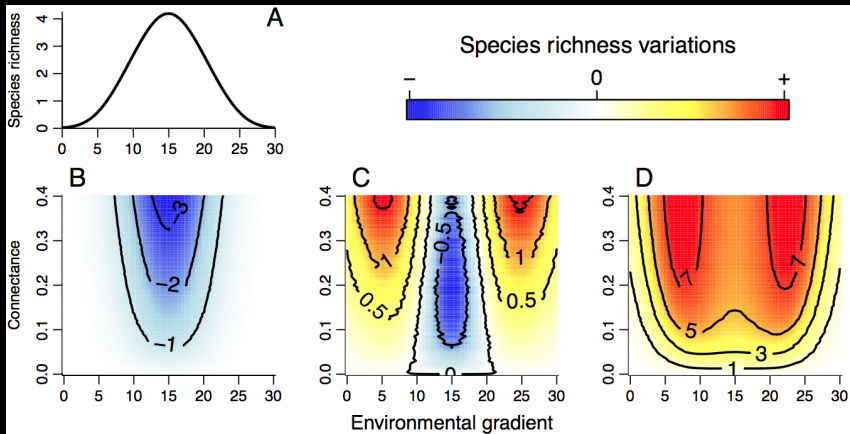


From A to C we increase the interaction strengths.

Environmental gradient + interaction



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Towards applications ?

- Large transition matrix: $2^n \times 2^n$

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- How to fit data ? Using set of species ? Species correlation ?
- Theoretical foundations for emerging approaches:

Methods in Ecology and Evolution



Methods in Ecology and Evolution 2014, **5**, 397–406

doi: 10.1111/2041-210X.12180

Understanding co-occurrence by modelling species simultaneously with a Joint Species Distribution Model (JSDM)

Laura J. Pollock^{1†}, Reid Tingley^{1†}, William K. Morris¹, Nick Golding², Robert B. O'Hara³, Kirsten M. Parris¹, Peter A. Vesk¹ and Michael A. McCarthy^{1*}

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Many questions remain unanswered:

- How the interaction propagate over spatial scales ?

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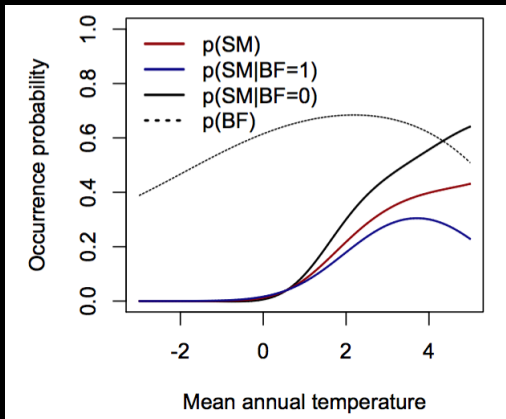
Towards applications ?

Many questions remain unanswered:

- How the interaction propagate over spatial scales ?
- What the meaning of matrix B at large scale ?
- Is there a way to scale $B(\sigma)$?
- Are correlations sufficient to capture “signals” and conclude ?

Work in progress

- Conditional probabilities of occurrence along environmental gradients



BF = Balsam Fir, SM = Sugar Maple

Are ecosystems concerned?

- The challenge is obviously to go further than two species, but...

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