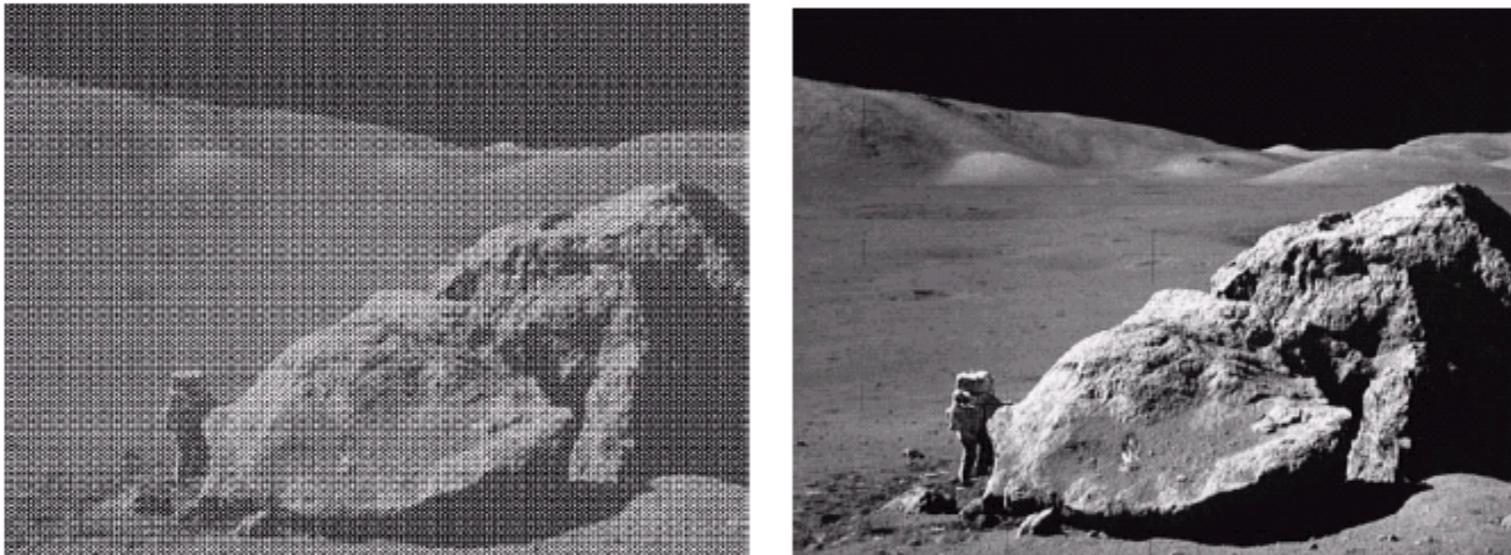


Image Processing and Pattern Recognition (IPPR)

Chapter 4:Image Restoration



Basanta Joshi, PhD

Asst. Prof., Depart of Electronics and Computer Engineering

Member, Laboratory for ICT Research and Development (LICT)

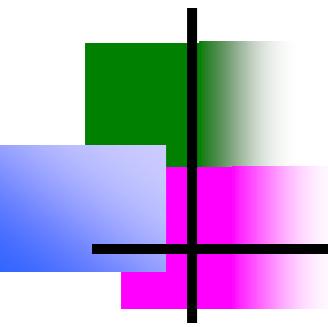
Institute of Engineering

basanta@ioe.edu.np

<http://www.basantajoshi.com.np>

<https://scholar.google.com/citations?user=iocLiGcAAAAJ>

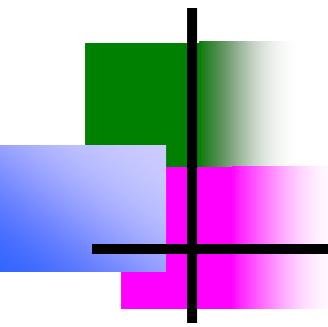
https://www.researchgate.net/profile/Basanta_Joshi2



Contents

In this lecture we will look at image restoration techniques used for noise removal

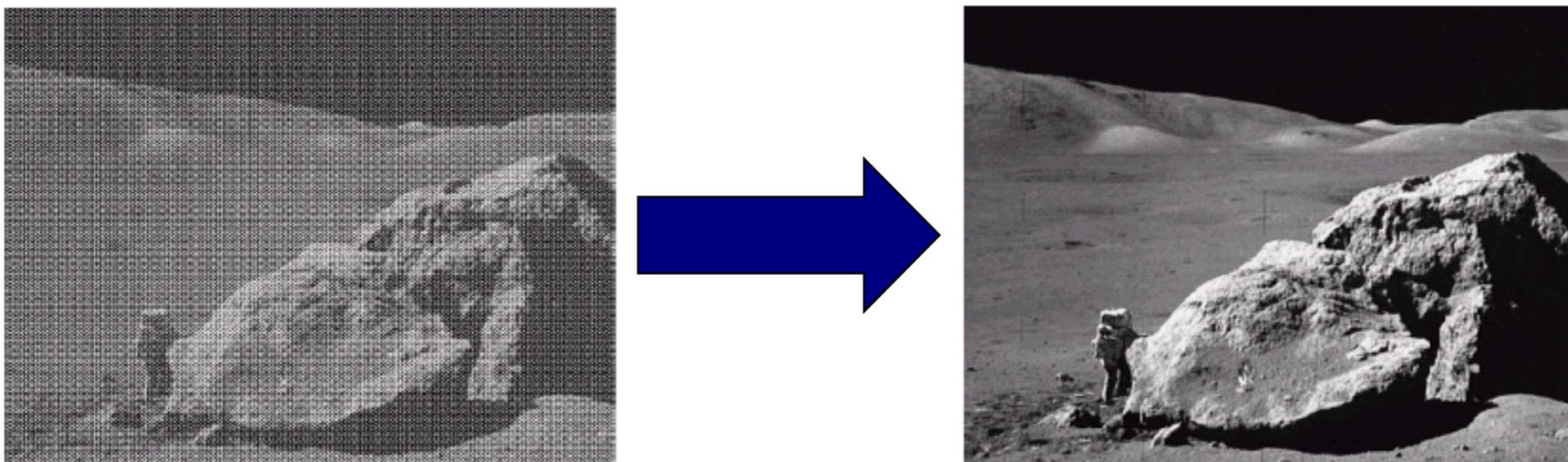
- What is image restoration?
- Noise and images
- Noise models
- Noise removal using spatial domain filtering
- Periodic noise
- Noise removal using frequency domain filtering

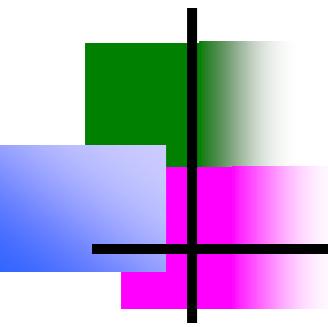


What is Image Restoration?

Image restoration attempts to restore images that have been degraded

- Identify the degradation process and attempt to reverse it
- Similar to image enhancement, but more objective



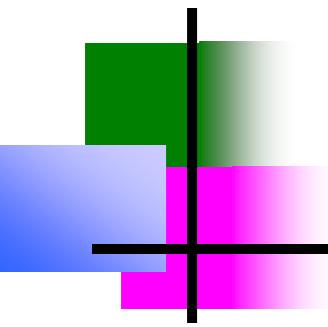


Noise and Images

The sources of noise in digital images arise during image acquisition (digitization) and transmission

- Imaging sensors can be affected by ambient conditions
- Interference can be added to an image during transmission

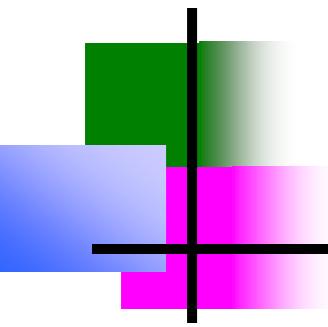




Noise and Images

Image restoration

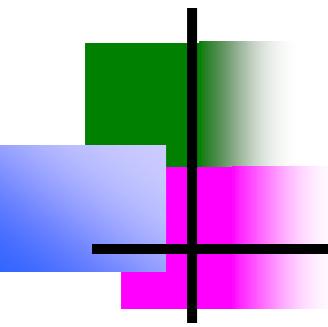
- Restoration is an objective process that attempts to recover an image that has been degraded
 - A priori knowledge of the degradation phenomenon
 - Restoration techniques generally oriented toward modeling the degradation
 - Application of the inverse process to “recover” the original image
 - Involves formulating some criterion (criteria) of “goodness” that is used to measure the desired result



Noise and Images

Image restoration (continued)

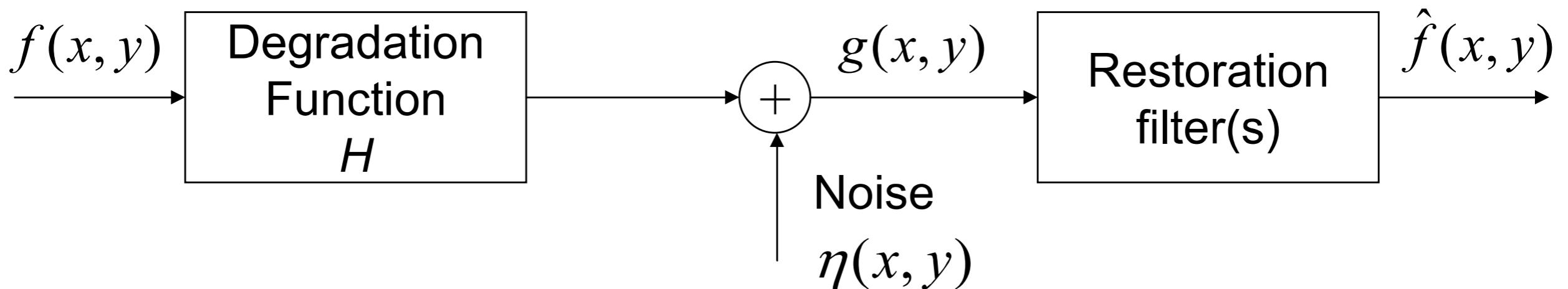
- Removal of blur by a deblurring function is an example restoration technique
- We will consider the problem only from where a degraded *digital* image is given
 - Degradation source will not be considered here
- Restoration techniques may be formulated in the
 - Frequency domain
 - Spatial domain

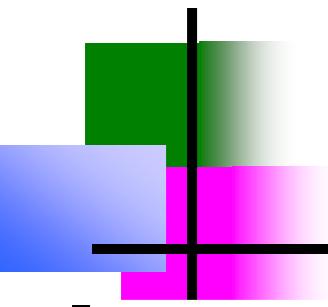


Noise and Images

Image degradation/restoration process

- Given $g(x,y)$, some knowledge about H , and some knowledge about the noise term, the objective is to produce an estimate of the original image.
 - The more that is known about H and the noise term the closer the estimate can be
- Various types of restoration filters are used to accomplish this.





Noise and Images

Image degradation/restoration process

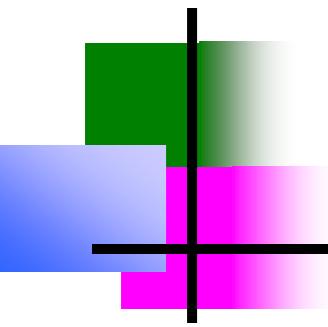
- If H is a linear, position invariant process, then the degraded image can be described as the convolution of h and f with an added noise term:

$$g(x, y) = h(x, y) * f(x, y) + \eta(x, y)$$

- $h(x, y)$ is the spatial domain representation of the degradation function.
- In the frequency domain, the representation is:

$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

- Each term in this expression is the Fourier transform of the corresponding terms in the equation above.



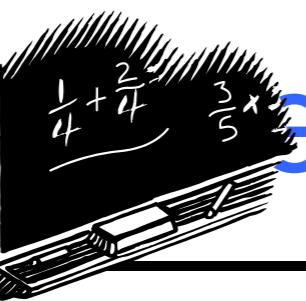
Noise Model

We can consider a noisy image to be modelled as follows:

$$g(x, y) = f(x, y) + \eta(x, y)$$

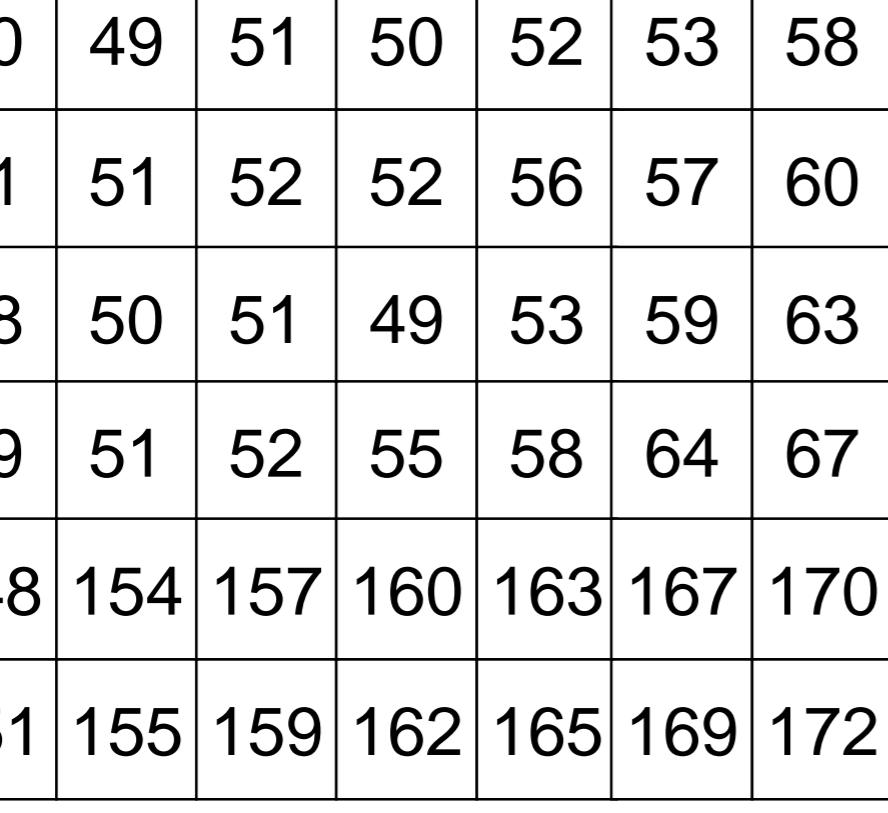
where $f(x, y)$ is the original image pixel, $\eta(x, y)$ is the noise term and $g(x, y)$ is the resulting noisy pixel

If we can estimate the model the noise in an image is based on this will help us to figure out how to restore the image



Corruption Example

Original Image

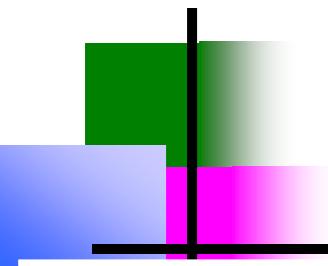


54	52	57	55	56	52	51
50	49	51	50	52	53	58
51	51	52	52	56	57	60
48	50	51	49	53	59	63
49	51	52	55	58	64	67
148	154	157	160	163	167	170
151	155	159	162	165	169	172

Image $f(x, y)$

Noisy Image

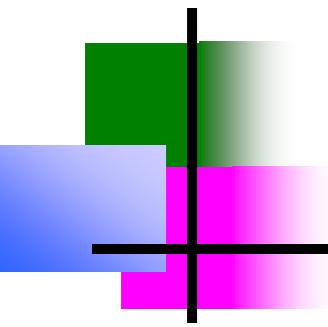
Image $f(x, y)$



Noise Models

Noise models

- Common sources of noise
 - Acquisition
 - Environmental conditions (heat, light), imaging sensor quality
 - Transmission
 - Noise in transmission channel
- Spatial and frequency properties of noise
 - Frequency properties of noise refer to the frequency content of noise in the Fourier sense
 - For example, if the Fourier spectrum of the noise is constant, the noise is usually called *white noise*
 - A carry over from the fact that white light contains nearly all frequencies in the visible spectrum in basically equal proportions
 - Excepting spatially periodic noise, we will assume that noise is independent of spatial coordinates and uncorrelated to the image



Noise Models

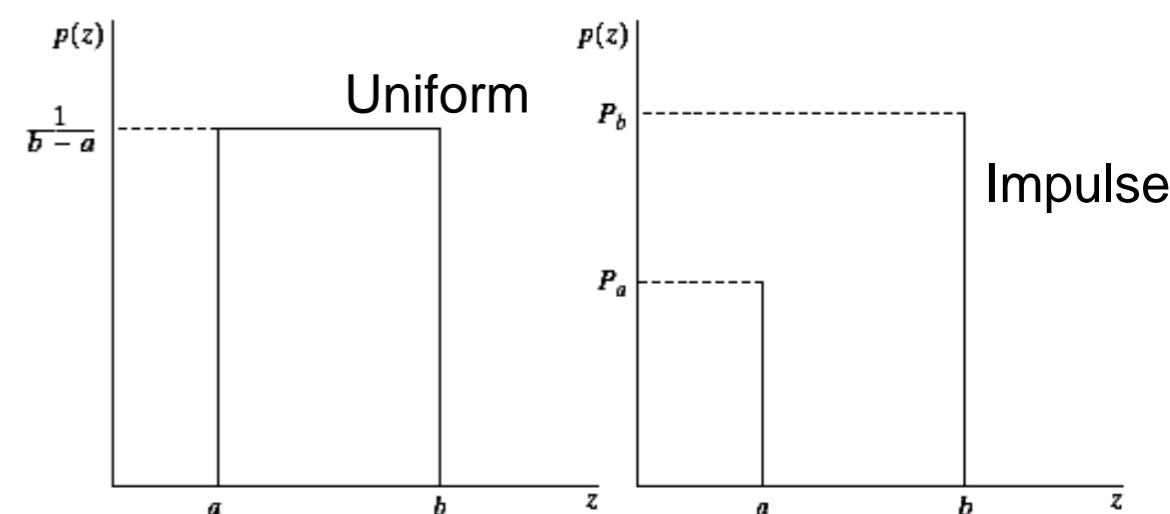
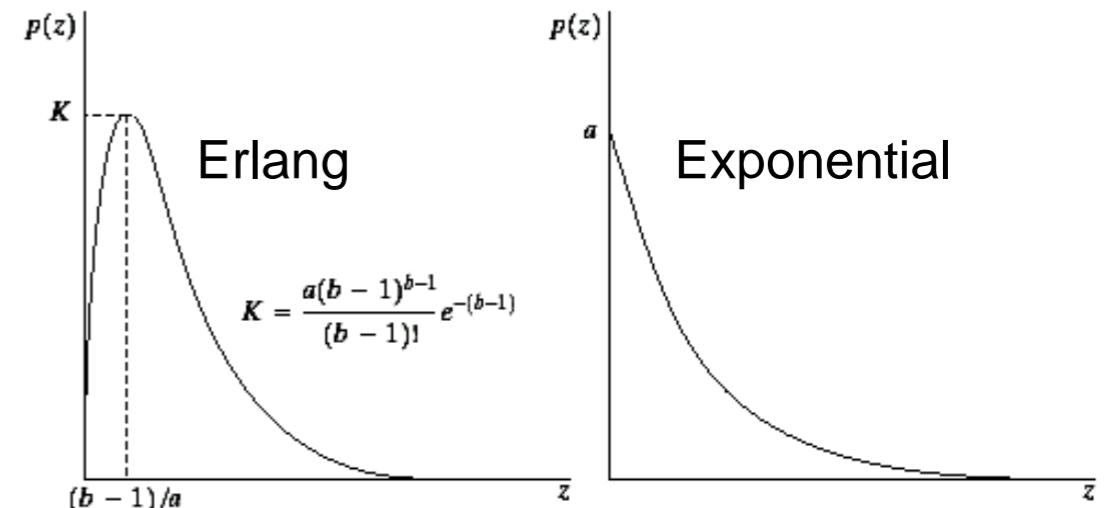
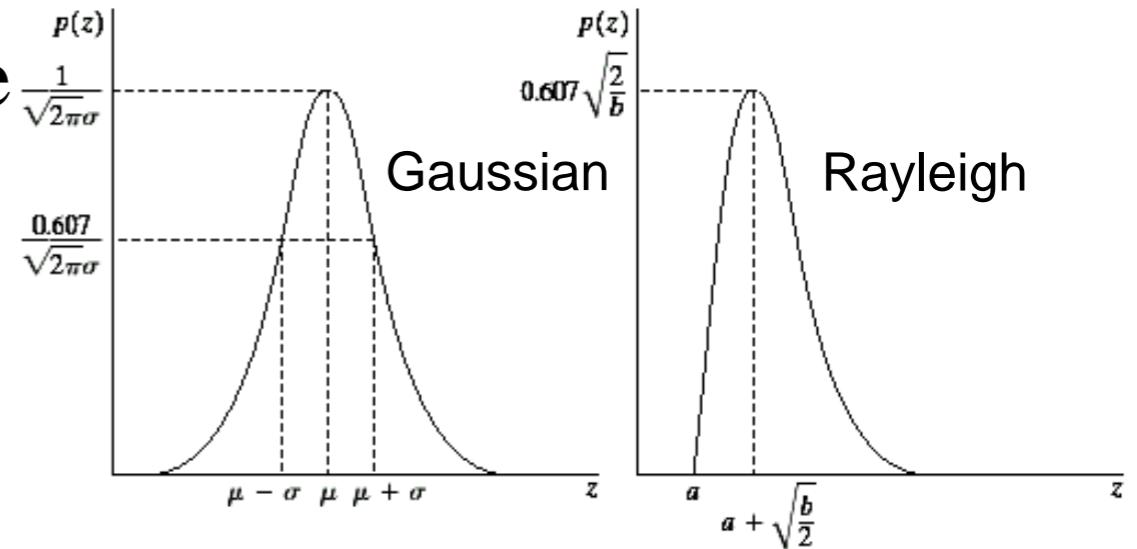
Noise probability density functions

- With respect to the *spatial* noise term, we will be concerned with the statistical behavior of the intensity values.
- May be treated as random variables characterized by a probability density function (PDF)
- Common PDFs used will describe:
 - Gaussian noise
 - Rayleigh noise
 - Erlang (Gamma) noise
 - Exponential noise
 - Uniform noise
 - Impulse (salt-and-pepper) noise

Noise Models

There are many different models for the image noise term $\eta(x, y)$:

- Gaussian
 - Most common model
- Rayleigh
- Erlang
- Exponential
- Uniform
- Impulse
 - *Salt and pepper* noise



Noise Models

Gaussian noise

- Gaussian (normal) noise models are simple to consider
- The PDF of a Gaussian random variable, z , is given to the right as:
- In this case, approximately 70% of the values of z will be within within one standard deviation
- Approximately 95% of the values of z will be within within two standard deviations

$$p(z) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(z-\bar{z})^2/2\sigma^2}$$

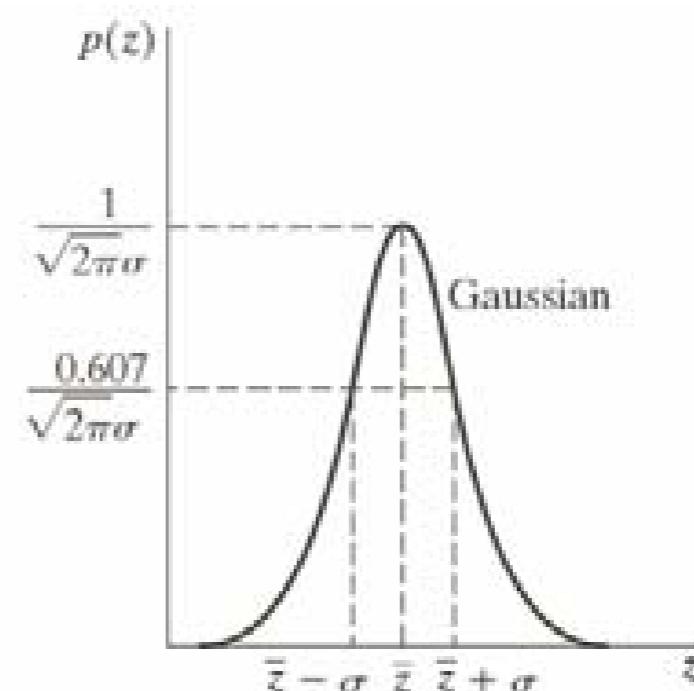
where

z represents intensity

\bar{z} represents the mean (average) value of z

σ is the standard deviation

σ^2 is the variance of z



Noise Models

Rayleigh noise

- The PDF of Rayleigh noise is given as:

$$p(z) = \begin{cases} \frac{2}{b}(z-a)e^{-(z-a)^2/b} & \text{for } z \geq a \\ 0 & \text{for } z < a \end{cases}$$

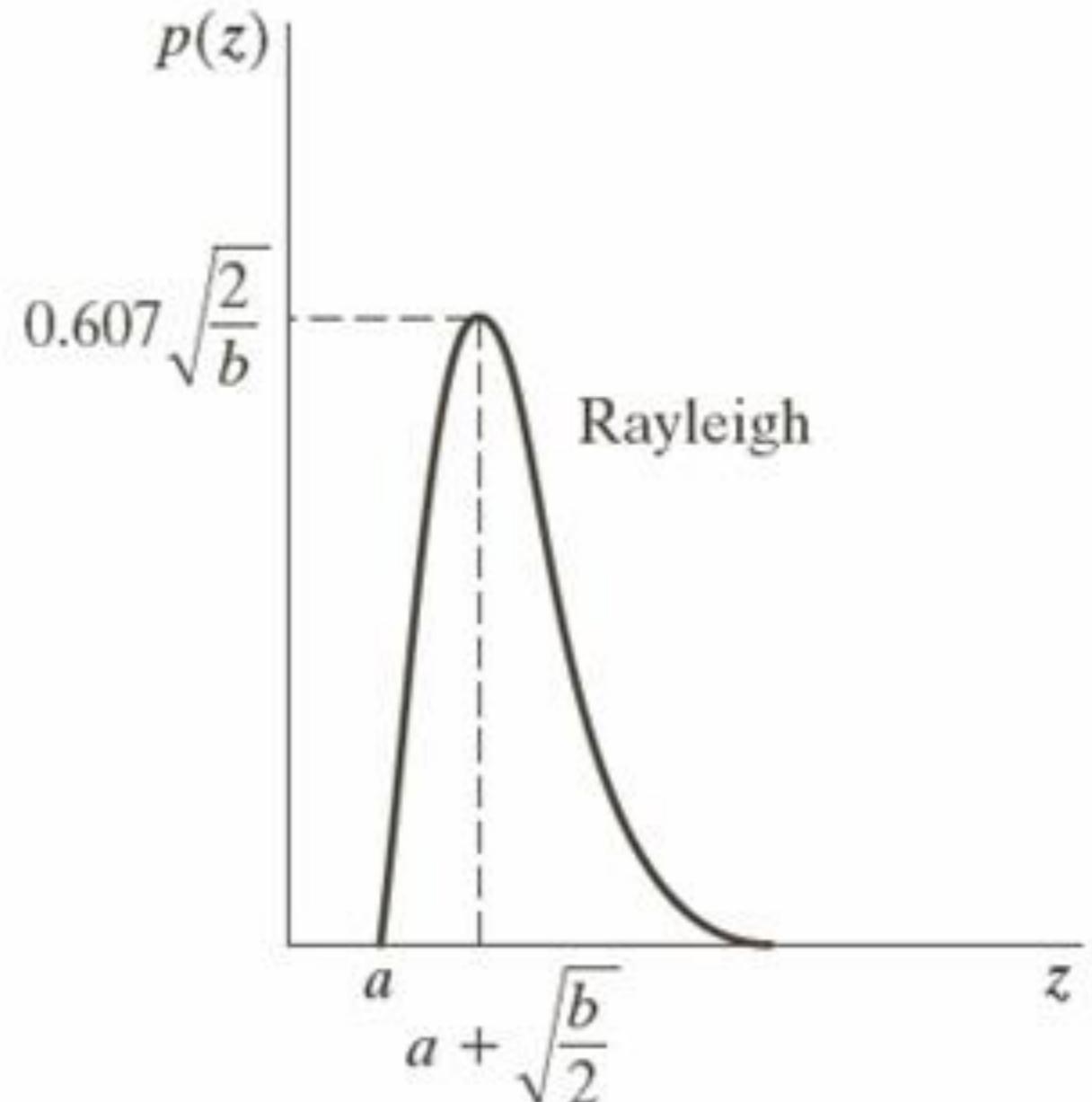
where

z represents intensity

$$\bar{z} = a + \sqrt{\pi b / 4}$$

$$\sigma^2 = \frac{b(4-\pi)}{4}$$

- Note the displacement, by a , from the origin
- The basic shape of this PDF is skewed to the right
 - Can be useful in approximating skewed histograms



Noise Models

Erlang (Gamma) noise

- The PDF of Erlang noise is given as:

$$p(z) = \begin{cases} \frac{a^b z^{b-1}}{(b-1)!} e^{-az} & \text{for } z \geq 0 \\ 0 & \text{for } z < 0 \end{cases}$$

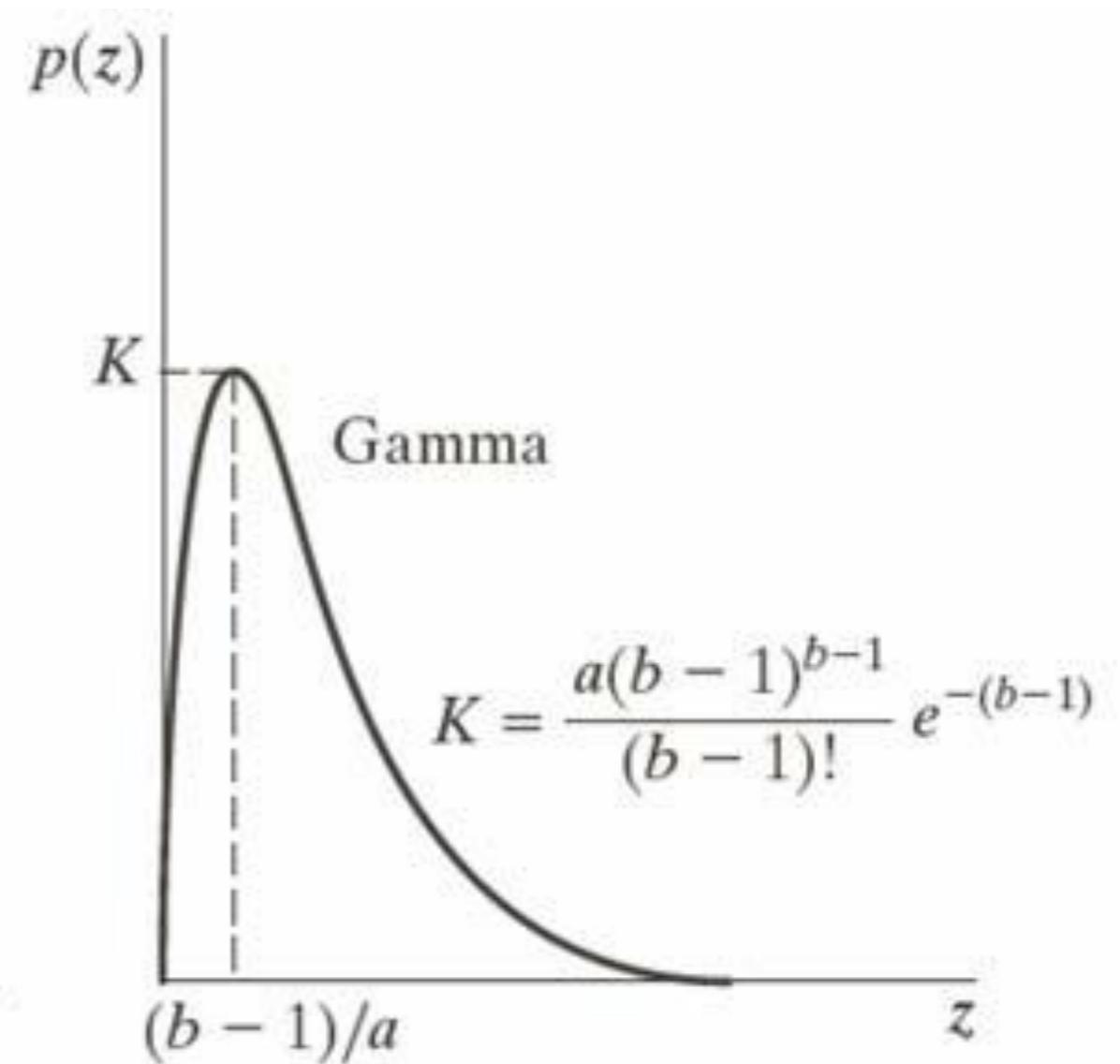
where

z represents intensity

$$\bar{z} = b / a$$

$$\sigma^2 = b / a^2$$

- $a > 0$, b is a positive integer



Noise Models

Exponential noise

- The PDF of exponential noise is given as:

$$p(z) = \begin{cases} ae^{-az} & \text{for } z \geq 0 \\ 0 & \text{for } z < 0 \end{cases}$$

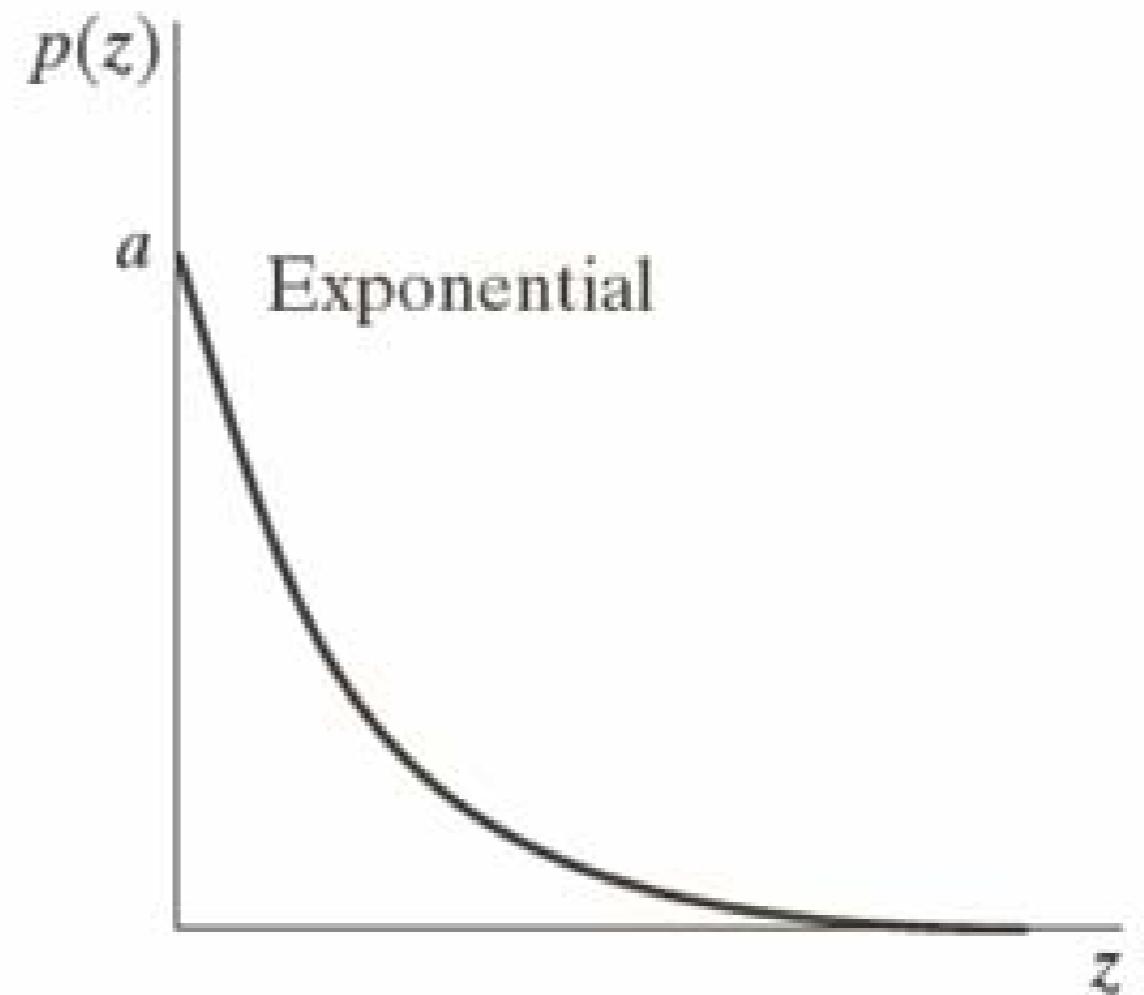
where

z represents intensity

$$\bar{z} = 1/a$$

$$\sigma^2 = 1/a^2$$

- $a > 0$
- This PDF is a special case of the Erlang PDF with $b=1$



Noise Models

Uniform noise

- The PDF of uniform noise is given as:

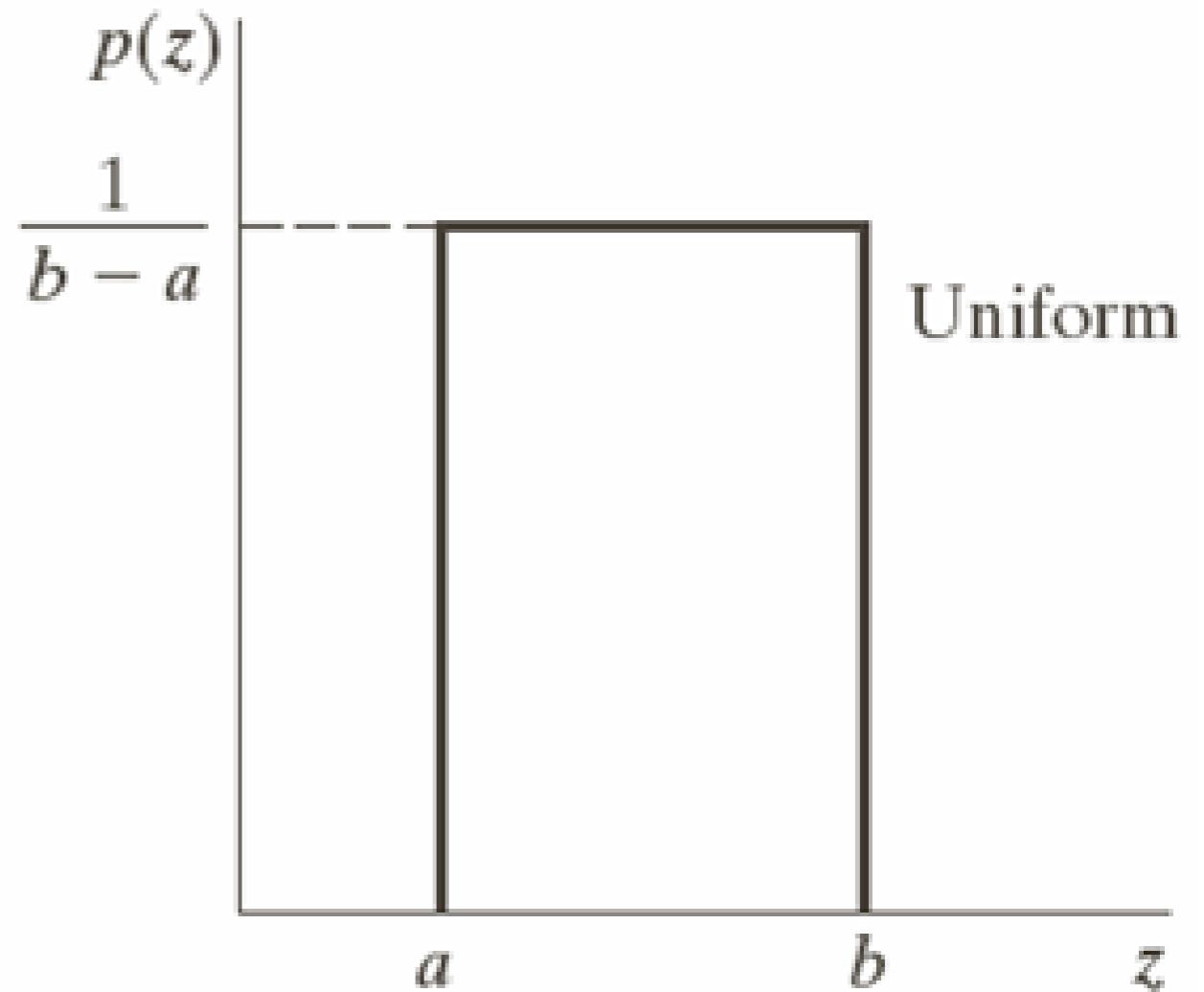
$$p(z) = \begin{cases} \frac{1}{b-a} & \text{if } a \leq z \leq b \\ 0 & \text{otherwise} \end{cases}$$

where

z represents intensity

$$\bar{z} = \frac{a+b}{2}$$

$$\sigma^2 = \frac{(b-a)^2}{12}$$



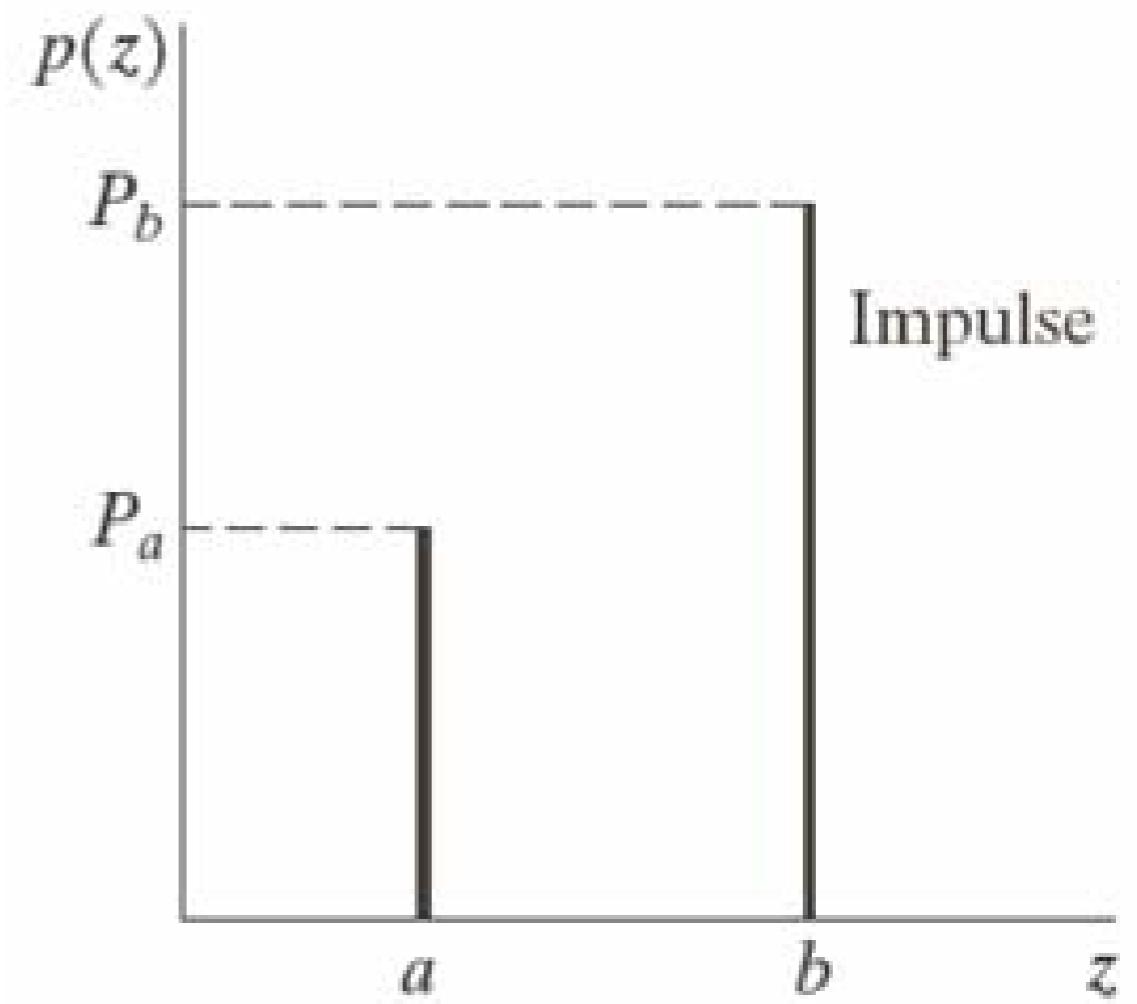
Noise Models

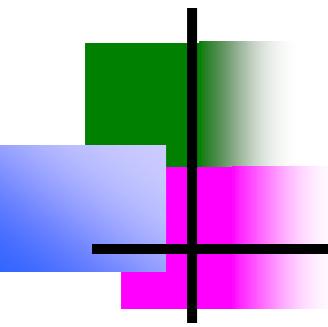
Impulse (salt-and-pepper) noise

- The PDF of (bipolar) impulse noise is given as:

$$p(z) = \begin{cases} P_a & \text{for } z = a \\ P_b & \text{for } z = b \\ 0 & \text{otherwise} \end{cases}$$

- If $b>a$ then any pixel with intensity b will appear as a light dot in the image
- Pixels with intensity a will appear as a dark dot

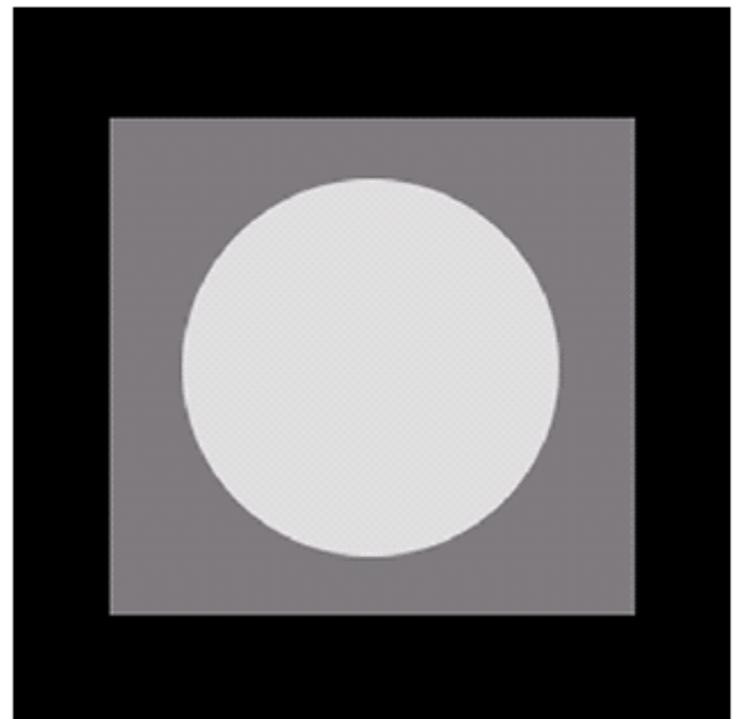




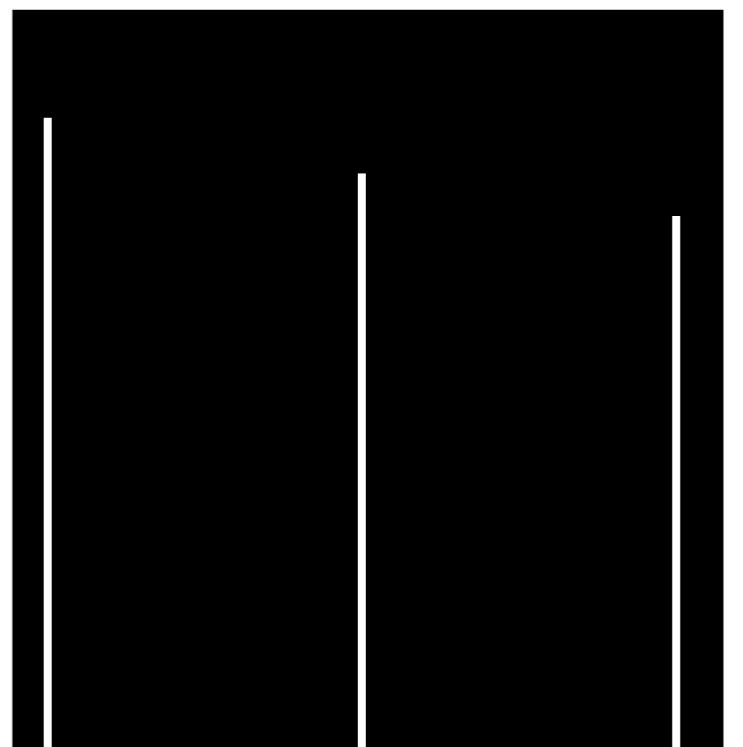
Noise Example

The test pattern to the right is ideal for demonstrating the addition of noise

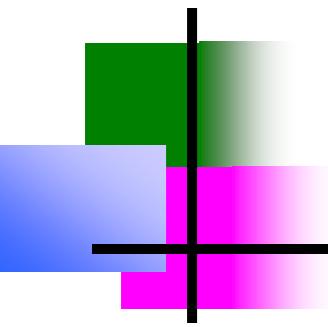
The following slides will show the result of adding noise based on various models to this image



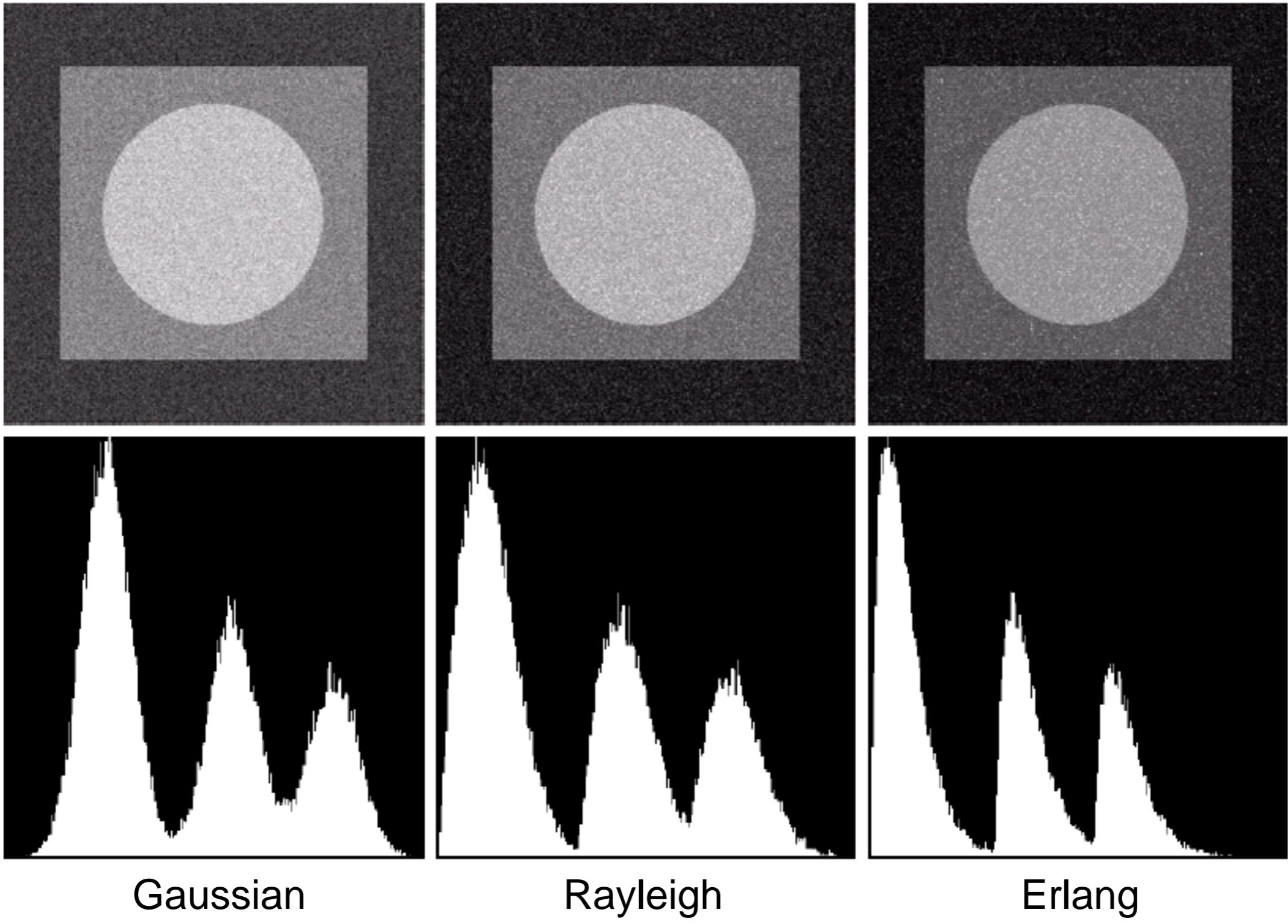
Image

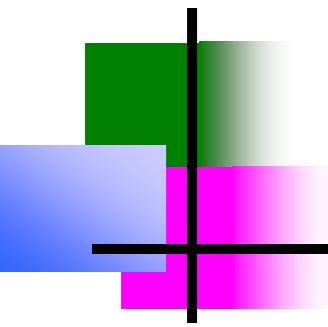


Histogram

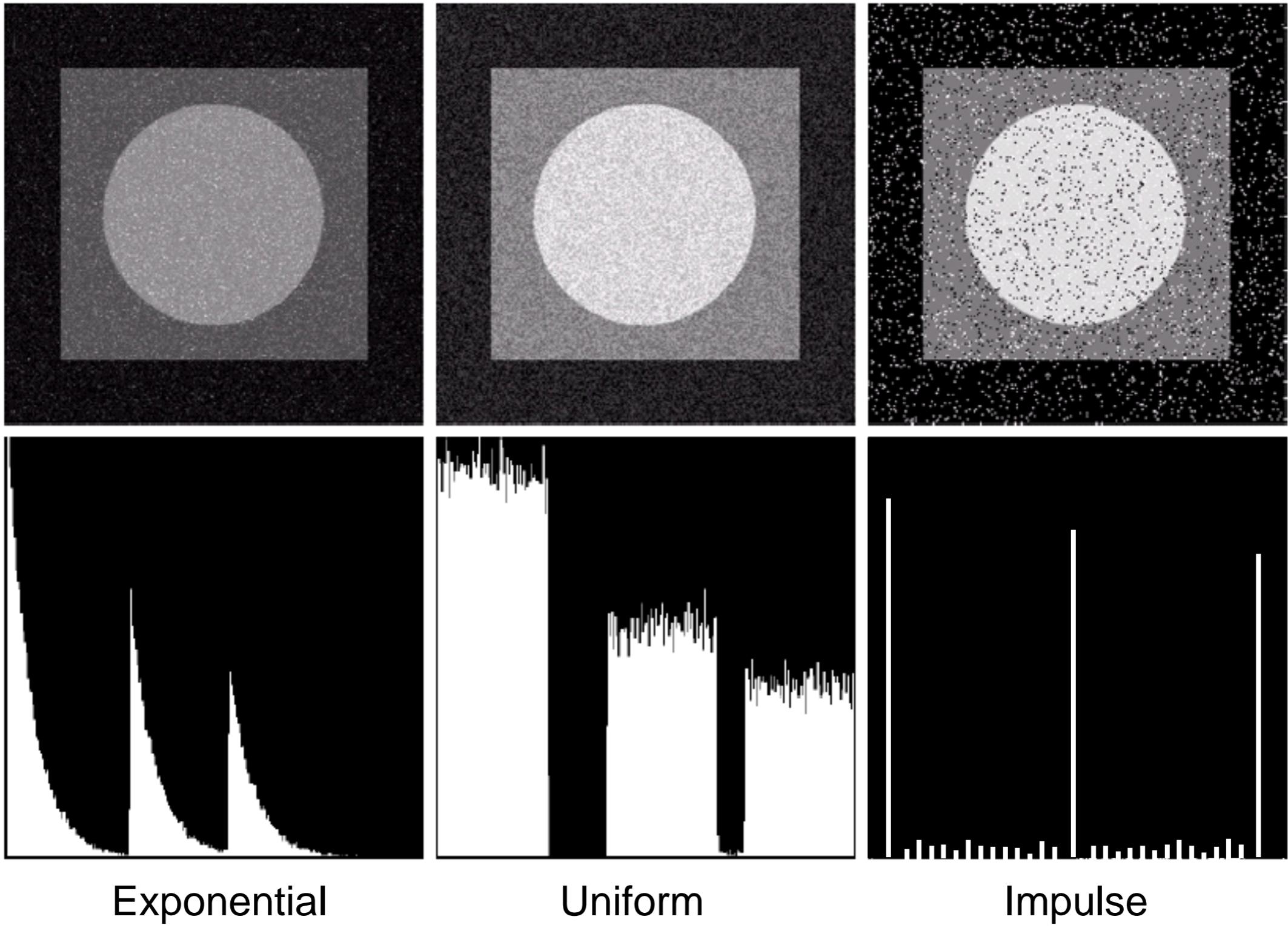


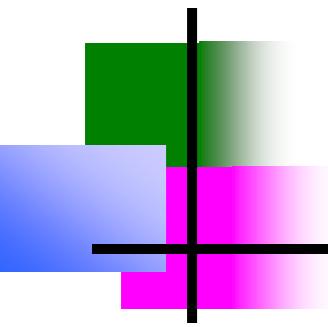
Noise Example (cont...)





Noise Example (cont...)



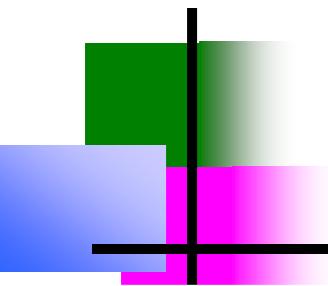


Noise Models

Estimation of noise parameters (continued)

- If only a set of images already generated by a sensor are available, estimate the PDF function of the noise from small strips of reasonably constant background intensity
- Consider a subimage (S) and let
$$p_s(z_i), i=0,1,2, \dots, L-1$$
- denote the probability estimates of the intensities of the pixels in S .
- L is the number of possible intensities in the image
- The mean and the variance of the pixels in S are given by:

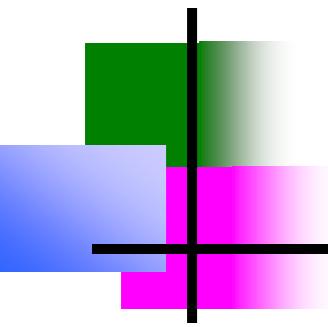
$$\bar{z} = \sum_{i=0}^{L-1} z_i p_s(z_i) \text{ and } \sigma^2 = \sum_{i=0}^{L-1} (z_i - \bar{z})^2 p_s(z_i)$$



Noise Models

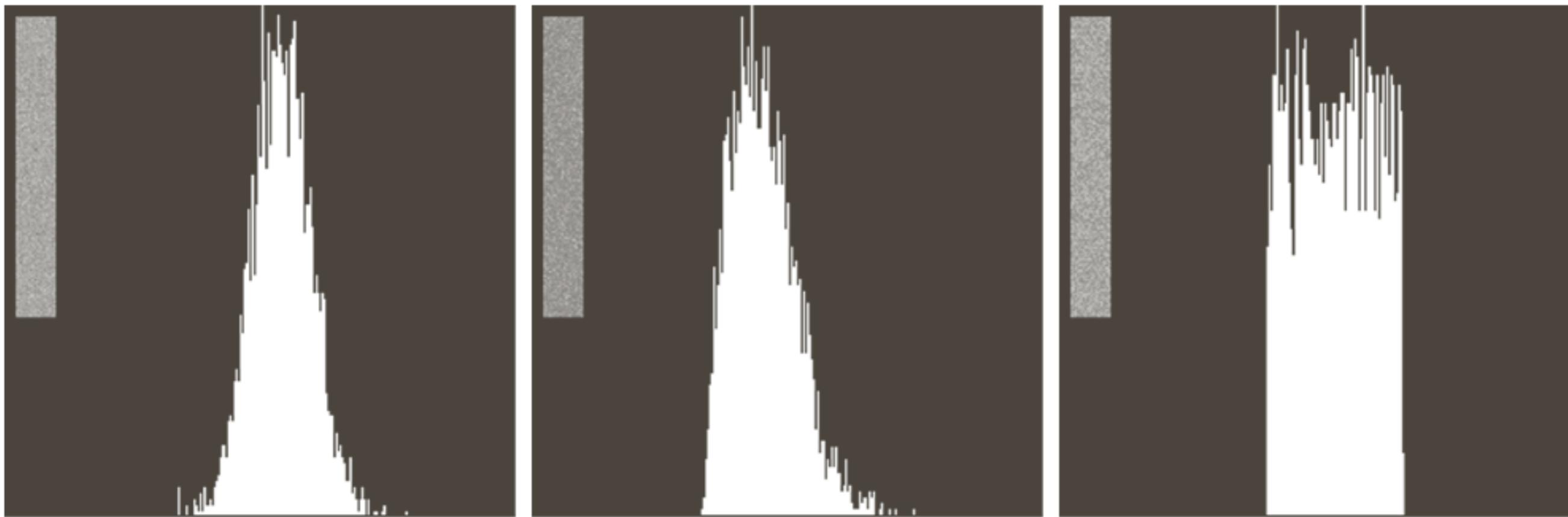
Estimation of noise parameters (continued)

- The shape of the noise histogram identifies the closest PDF match
 - If the shape is Gaussian, then the mean and variance are all that is needed to construct a model for the noise (i.e. the mean and the variance completely define the Gaussian PDF)
 - If the shape is Rayleigh, then the Rayleigh shape parameters (a and b) can be calculated using the mean and variance
 - If the noise is impulse, then a constant (with the exception of the noise) area of the image is needed to calculate P_a and P_b probabilities for the impulse PDF



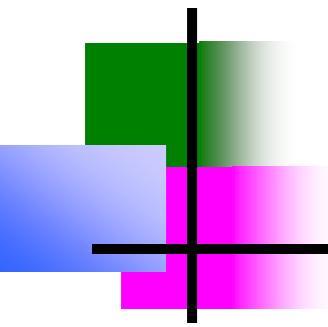
Noise Models

Histograms from noisy strips of an area of an image



a | b | c

FIGURE 5.6 Histograms computed using small strips (shown as inserts) from (a) the Gaussian, (b) the Rayleigh, and (c) the uniform noisy images in Fig. 5.4.



Filtering to Remove Noise

We can use spatial filters of different kinds to remove different kinds of noise

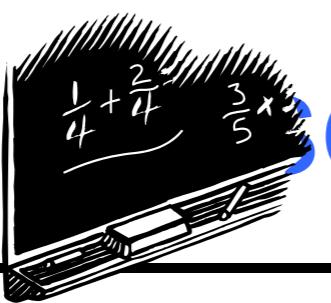
The *arithmetic mean* filter is a very simple one and is calculated as follows:

$$\hat{f}(x, y) = \frac{1}{mn} \sum_{(s,t) \in S_{xy}} g(s, t)$$

$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$

This is implemented as the simple smoothing filter

Blurs the image to remove noise



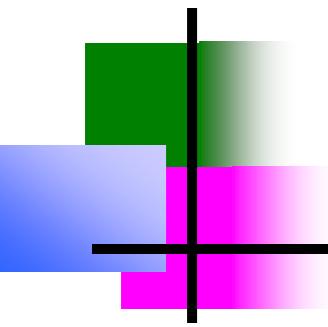
Noise Removal Example

Original Image

<i>Image $f(x, y)$</i>						
54	52	57	55	56	52	51
50	49	51	50	52	53	58
51	204	52	52	0	57	60
48	50	51	49	53	59	63
49	51	52	55	58	64	67
148	154	157	160	163	167	170
151	155	159	162	165	169	172

Filtered Image

<i>Image $f(x, y)$</i>						



Other Means

There are different kinds of mean filters all of which exhibit slightly different behaviour:

- Geometric Mean
- Harmonic Mean
- Contraharmonic Mean

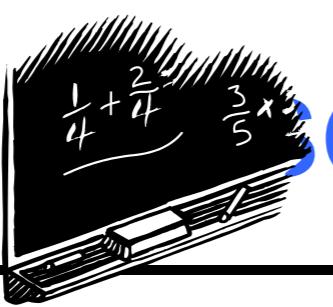
Other Means (cont...)

There are other variants on the mean which can give different performance

Geometric Mean:

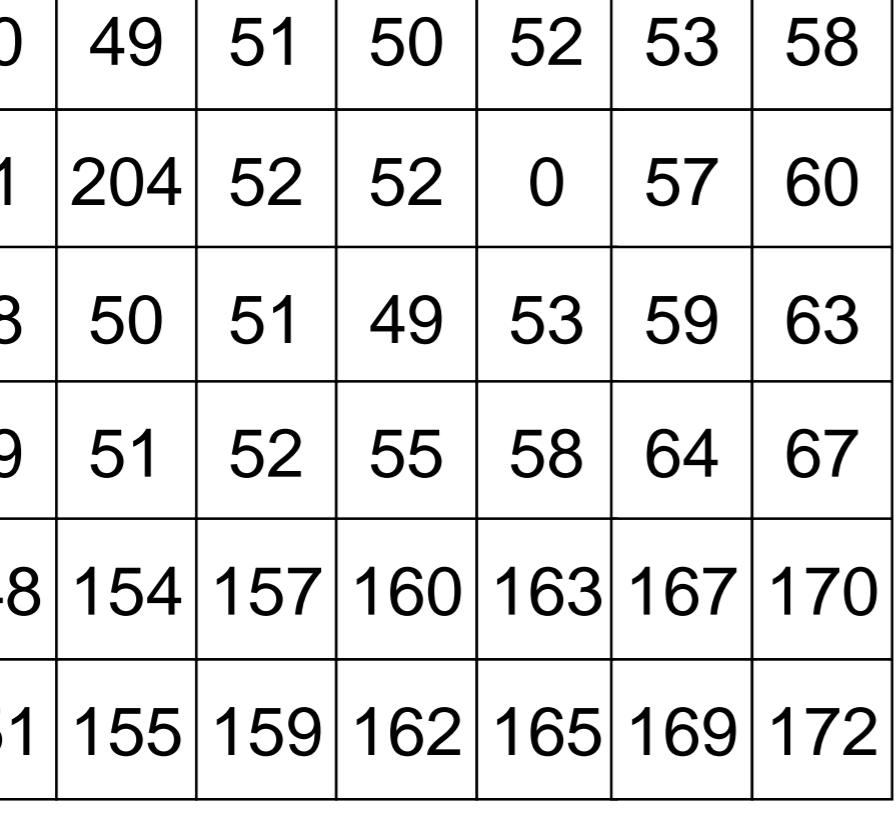
$$\hat{f}(x, y) = \left[\prod_{(s,t) \in S_{xy}} g(s, t) \right]^{\frac{1}{mn}}$$

Achieves similar smoothing to the arithmetic mean, but tends to lose less image detail



e Removal Example

Original Image



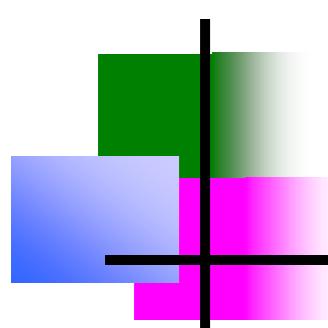
A 7x7 grid of numerical values, representing a 2D image $f(x, y)$. The grid is bounded by a thick blue line. A horizontal blue arrow points to the right along the top edge, and a vertical blue arrow points downwards along the left edge.

54	52	57	55	56	52	51
50	49	51	50	52	53	58
51	204	52	52	0	57	60
48	50	51	49	53	59	63
49	51	52	55	58	64	67
148	154	157	160	163	167	170
151	155	159	162	165	169	172

Image $f(x, y)$

Filtered Image

A 7x7 grid representing an image $f(x, y)$. The grid has a blue vertical axis on the left and a blue horizontal axis at the top.



Other Means (cont...)

Harmonic Mean:

$$\hat{f}(x, y) = \frac{mn}{\sum_{(s,t) \in S_{xy}} \frac{1}{g(s, t)}}$$

Works well for salt noise, but fails for pepper noise

Also does well for other kinds of noise such as Gaussian noise

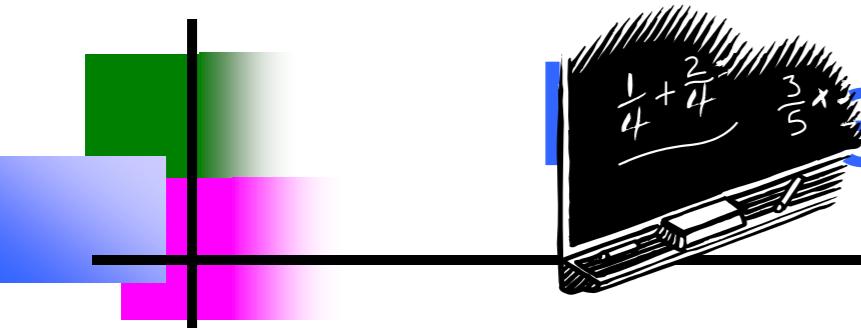


Image Corruption Example

Original Image

	x						
	54	52	57	55	56	52	51
	50	49	51	50	52	53	58
	51	204	52	52	0	57	60
	48	50	51	49	53	59	63
	49	51	52	55	58	64	67
	50	54	57	60	63	67	70
	51	55	59	62	65	69	72

Image $f(x, y)$

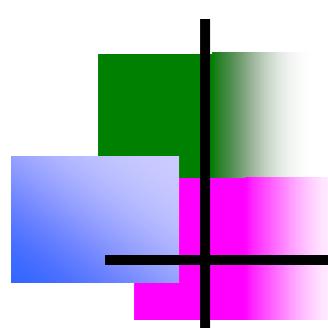
y

Filtered Image

	x						

Image $f(x, y)$

y



Other Means (cont...)

Contraharmonic Mean:

$$\hat{f}(x, y) = \frac{\sum_{(s,t) \in S_{xy}} g(s, t)^{Q+1}}{\sum_{(s,t) \in S_{xy}} g(s, t)^Q}$$

Q is the *order* of the filter and adjusting its value changes the filter's behaviour

Positive values of Q eliminate pepper noise

Negative values of Q eliminate salt noise



Image Corruption Example

Original Image

<i>Image $f(x, y)$</i>						
54	52	57	55	56	52	51
50	49	51	50	52	53	58
51	204	52	52	0	57	60
48	50	51	49	53	59	63
49	51	52	55	58	64	67
50	54	57	60	63	67	70
51	55	59	62	65	69	72

Filtered Image

<i>Image $f(x, y)$</i>						

Noise Removal Examples

Original
Image

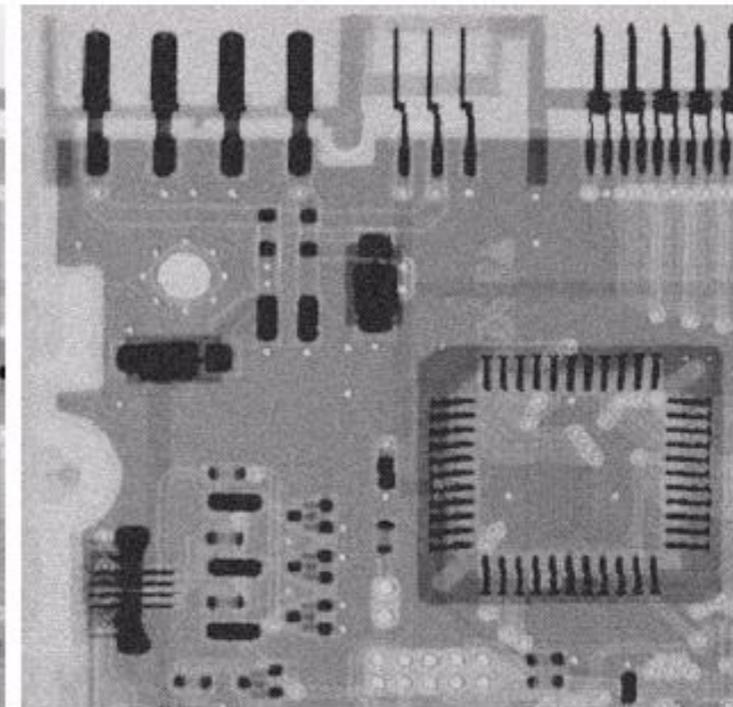
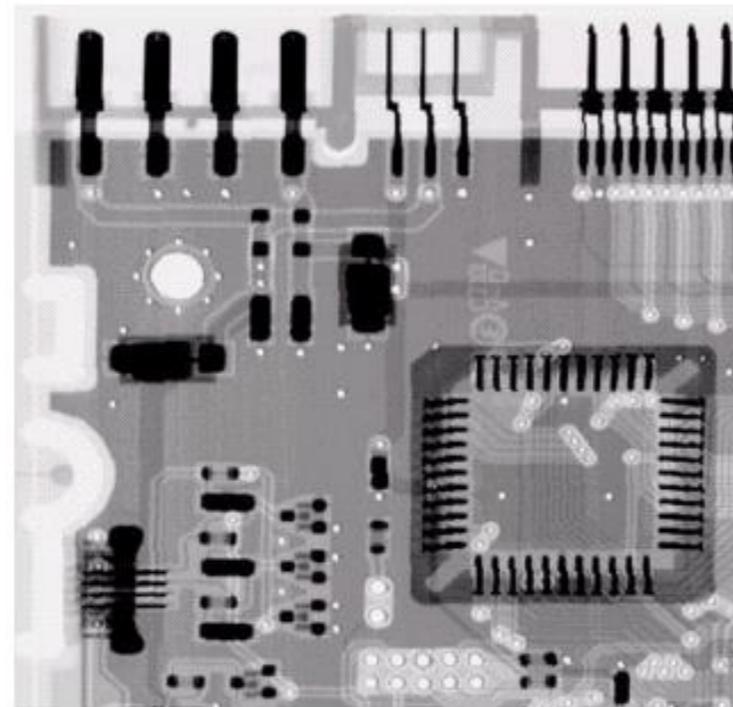
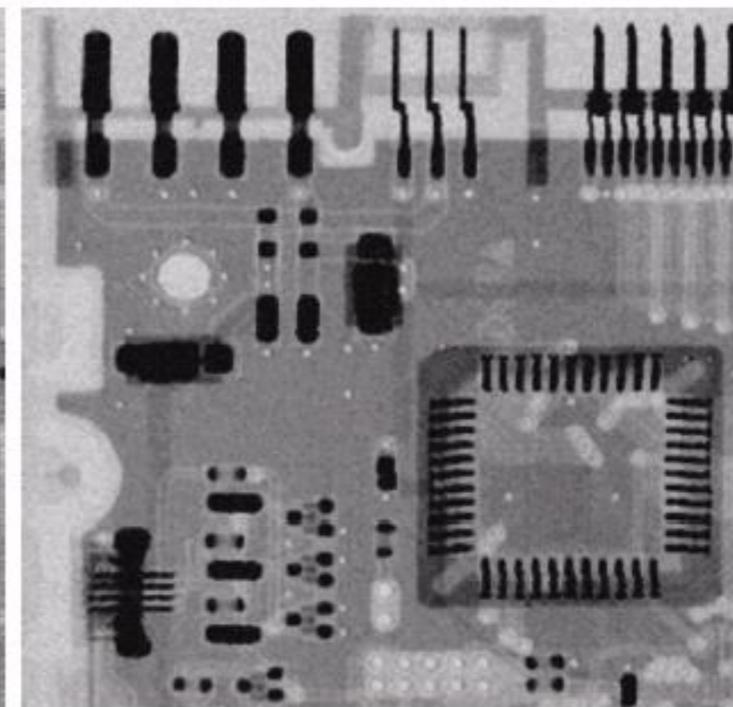
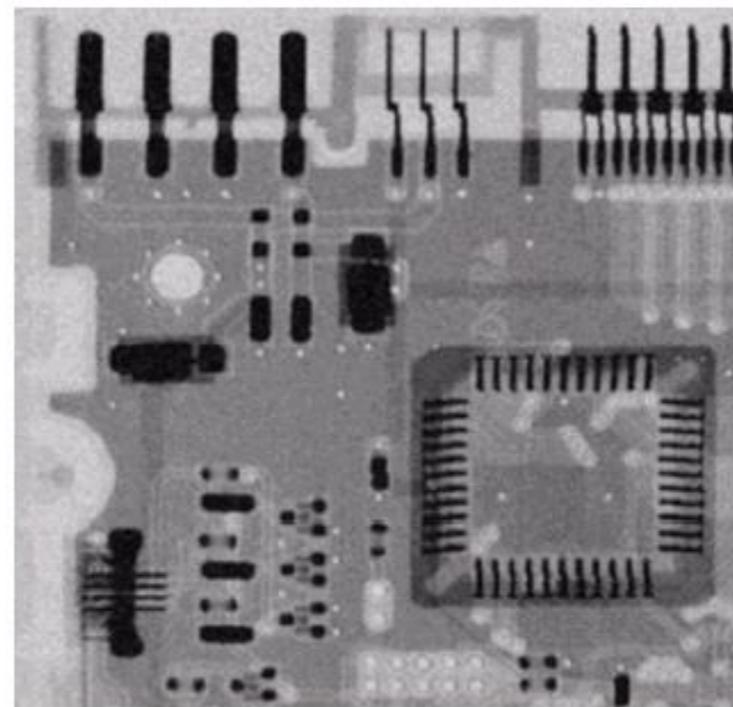


Image
Corrupted
By Gaussian
Noise

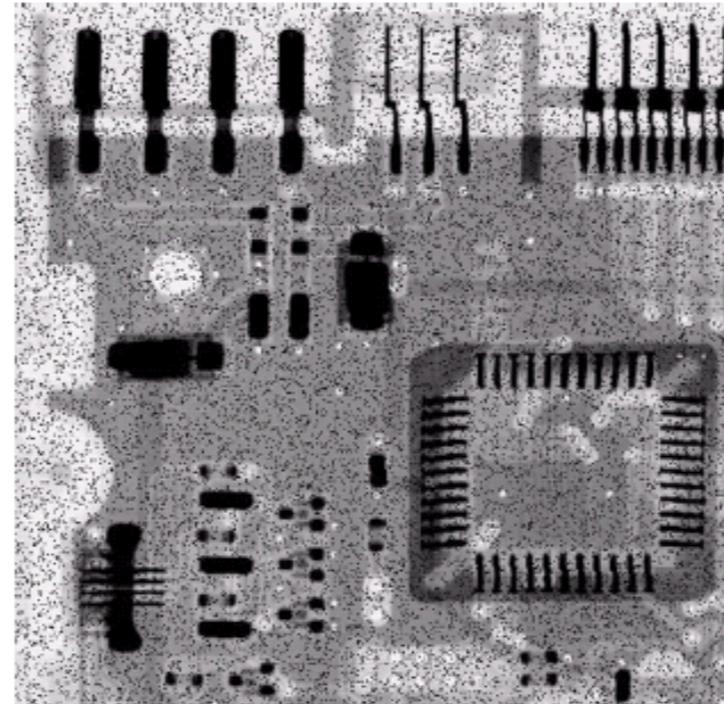
After A 3*3
Arithmetic
Mean Filter



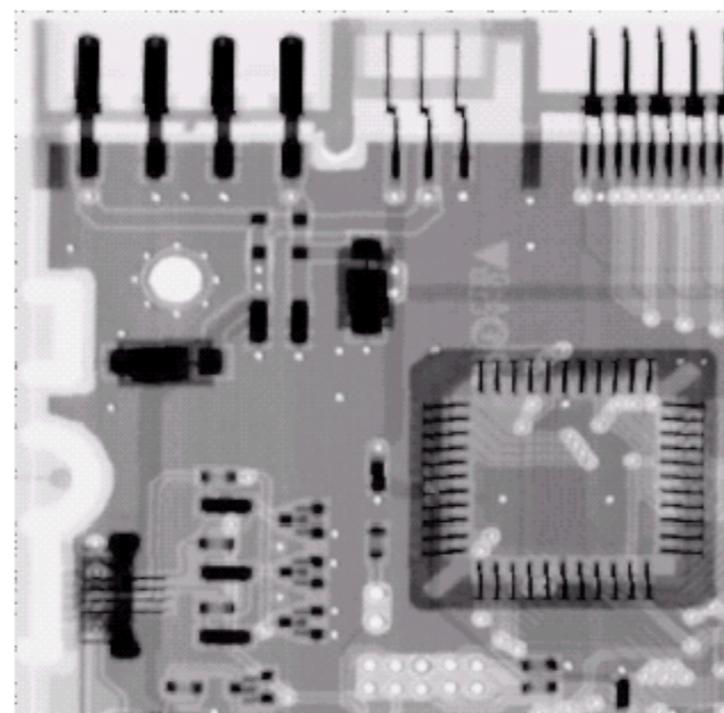
After A 3*3
Geometric
Mean Filter

Noise Removal Examples (cont...)

Image
Corrupted
By Pepper
Noise



Result of
Filtering Above
With 3*3
Contraharmonic
 $Q=1.5$



Noise Removal Examples (cont...)

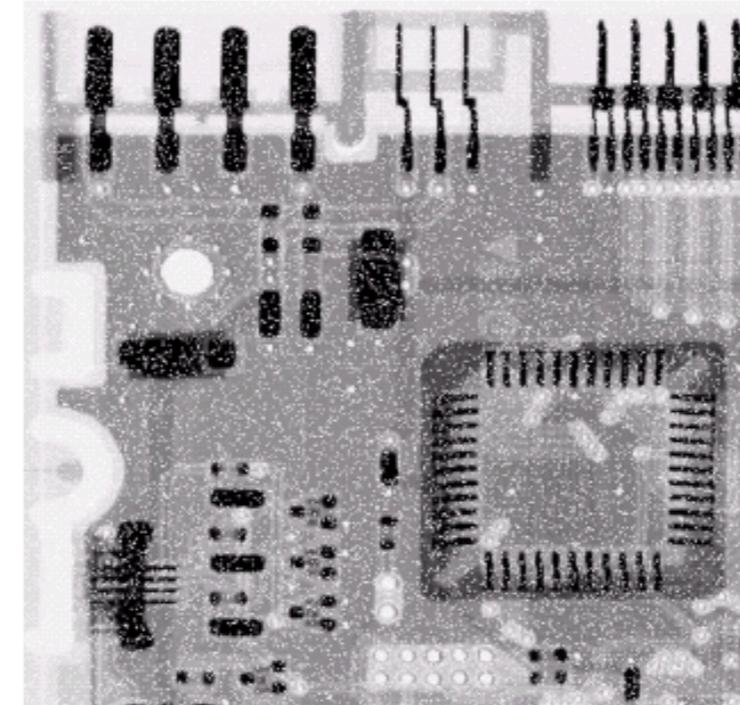
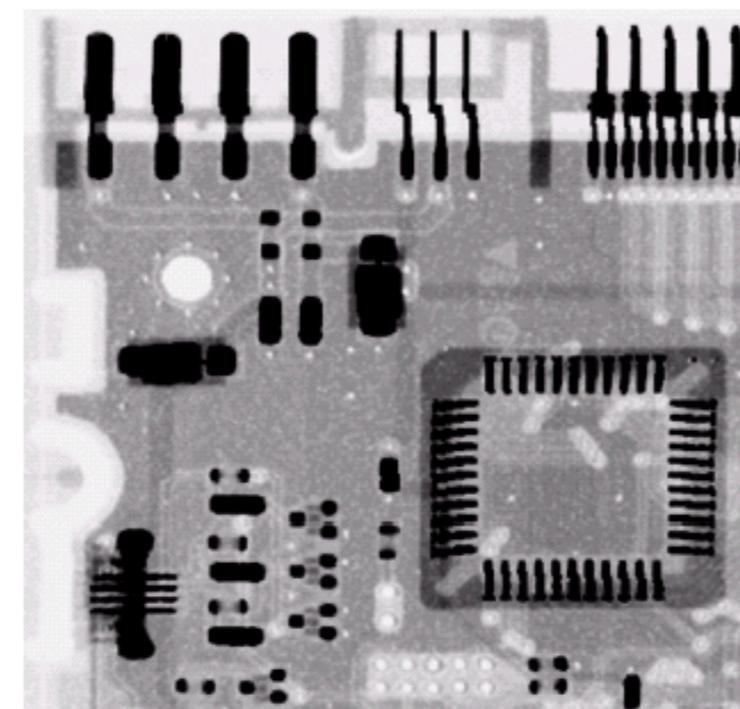


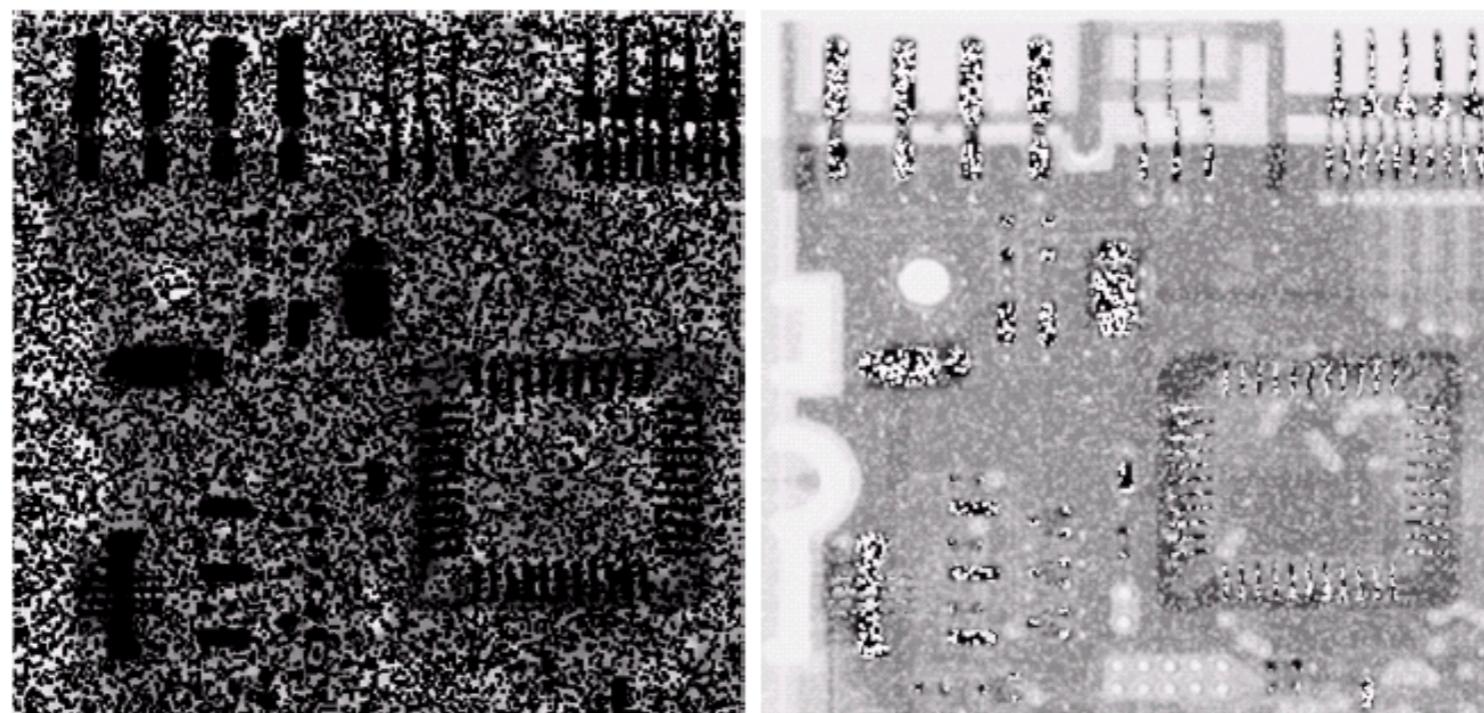
Image
Corrupted
By Salt
Noise

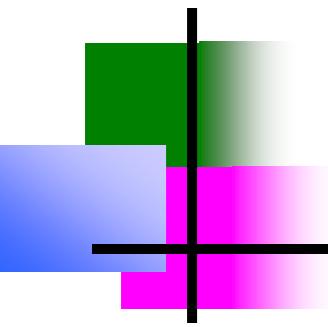


Result of
Filtering Above
With 3×3
Contraharmonic
 $Q = -1.5$

Contraharmonic Filter: Here Be Dragons

Choosing the wrong value for Q when using the contraharmonic filter can have drastic results



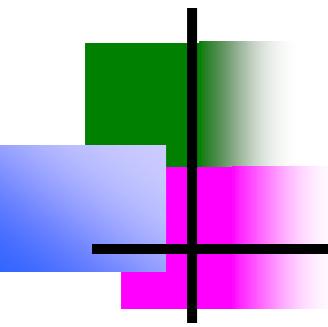


Order Statistics Filters

Spatial filters that are based on ordering the pixel values that make up the neighbourhood operated on by the filter

Useful spatial filters include

- Median filter
- Max and min filter
- Midpoint filter
- Alpha trimmed mean filter



Median Filter

Median Filter:

$$\hat{f}(x, y) = \text{median}\{g(s, t)\}$$

Excellent at noise removal, without the smoothing effects that can occur with other smoothing filters

Particularly good when salt and pepper noise is present

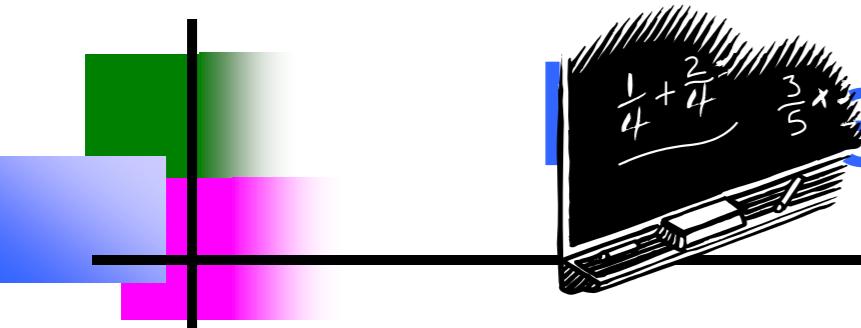


Image Corruption Example

Original Image

	x						
	54	52	57	55	56	52	51
	50	49	51	50	52	53	58
	51	204	52	52	0	57	60
	48	50	51	49	53	59	63
	49	51	52	55	58	64	67
	50	54	57	60	63	67	70
	51	55	59	62	65	69	72

Image $f(x, y)$

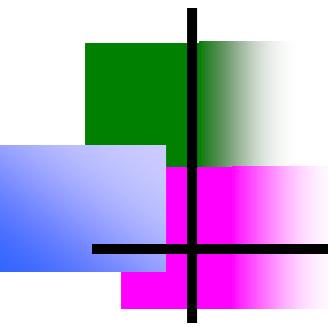
y

Filtered Image

	x						

Image $f(x, y)$

y



Max and Min Filter

Max Filter:

$$\hat{f}(x, y) = \max_{(s,t) \in S_{xy}} \{g(s, t)\}$$

Min Filter:

$$\hat{f}(x, y) = \min_{(s,t) \in S_{xy}} \{g(s, t)\}$$

Max filter is good for pepper noise and min is good for salt noise

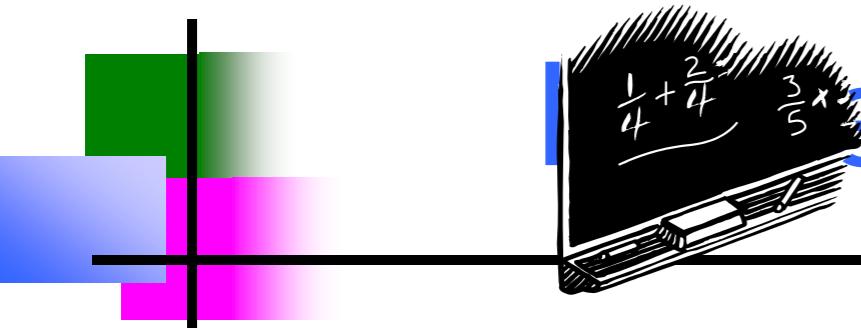


Image Corruption Example

Original Image

	x						
	54	52	57	55	56	52	51
	50	49	51	50	52	53	58
	51	204	52	52	0	57	60
	48	50	51	49	53	59	63
	49	51	52	55	58	64	67
	50	54	57	60	63	67	70
	51	55	59	62	65	69	72

Image $f(x, y)$

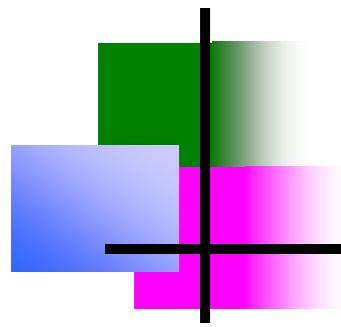
y

Filtered Image

	x						

Image $f(x, y)$

y



Midpoint Filter

Midpoint Filter:

$$\hat{f}(x, y) = \frac{1}{2} \left[\max_{(s,t) \in S_{xy}} \{g(s,t)\} + \min_{(s,t) \in S_{xy}} \{g(s,t)\} \right]$$

Good for random Gaussian and uniform noise



Image Corruption Example

Original Image

	x						
	54	52	57	55	56	52	51
	50	49	51	50	52	53	58
	51	204	52	52	0	57	60
	48	50	51	49	53	59	63
	49	51	52	55	58	64	67
	50	54	57	60	63	67	70
	51	55	59	62	65	69	72

Image $f(x, y)$

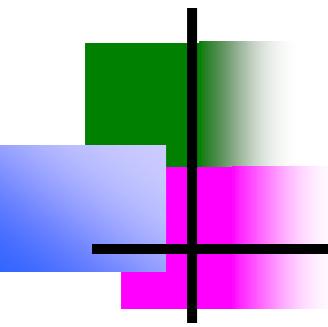
y

Filtered Image

	x						

Image $f(x, y)$

y



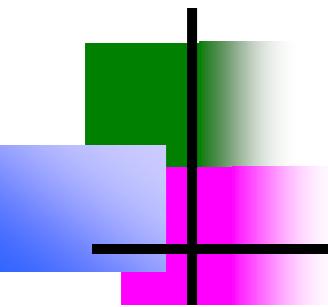
Alpha-Trimmed Mean Filter

Alpha-Trimmed Mean Filter:

$$\hat{f}(x, y) = \frac{1}{mn - d} \sum g_r(s, t)$$

We can delete the $d/2$ lowest and $d/2$ highest grey levels

So $g_r(s, t)$ represents the remaining $mn - d$ pixels



Alpha-Trimmed Mean Filter

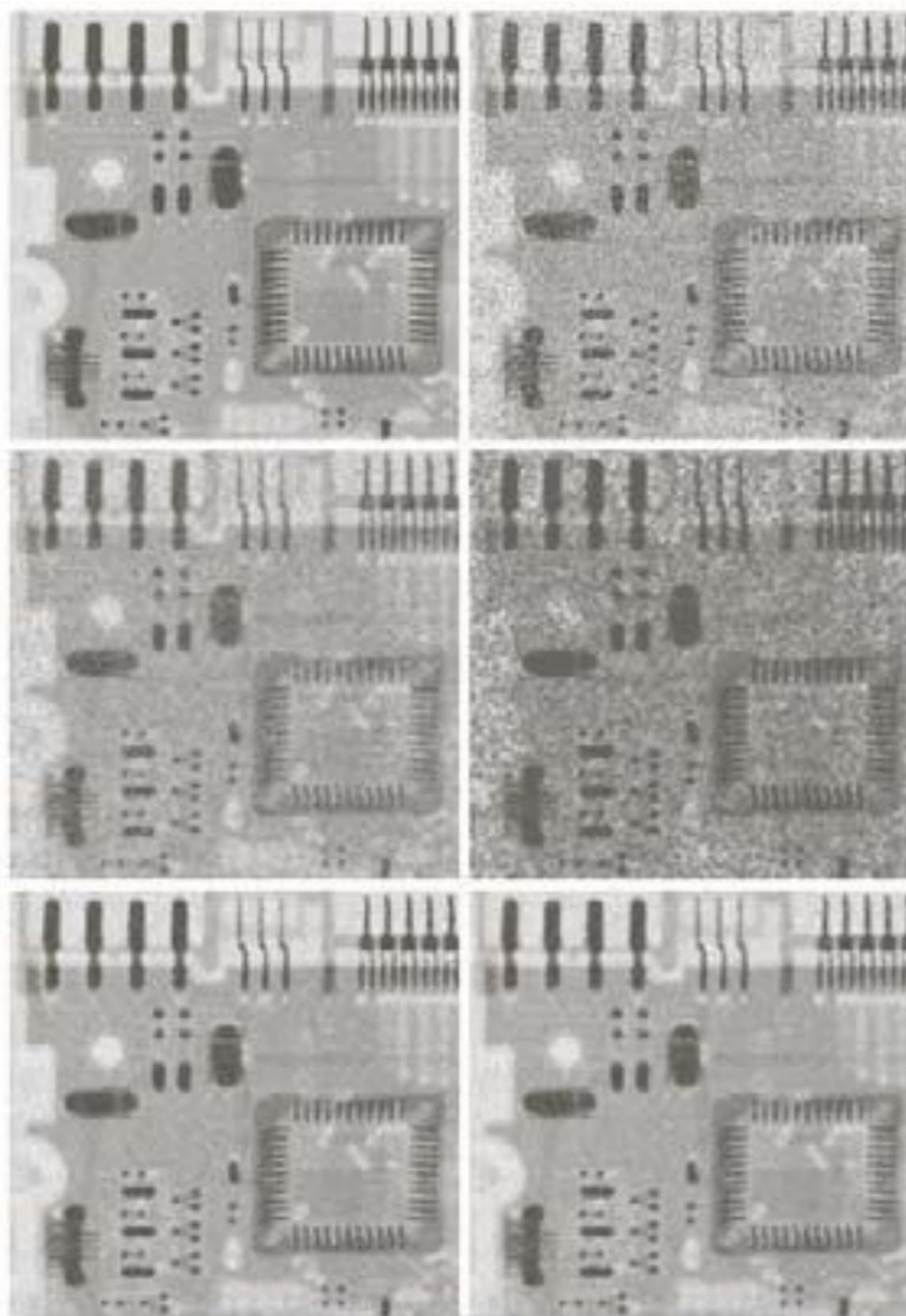
Alpha-trimmed mean filter

- If we delete the $d/2$ lowest and the $d/2$ highest intensity values from a neighborhood $g(s,t)$ of size $m*n$ and let $g_r(s,t)$ represent the remaining $mn-d$ pixels, the average of the remaining pixels is called an *alpha-trimmed mean* filter and is given by:

$$\hat{f}(x,y) = \frac{1}{mn-d} \sum_{(s,t) \in S_{x,y}} g_r(s,t)$$

- d can vary from 0 to $mn-1$
- If $d=0$ the filter becomes the arithmetic mean filter
- If $d=mn-1$, the filter reduces to a median filter

Alpha-Trimmed Mean Filter



a	b
c	d
e	f

FIGURE 5.12

- (a) Image corrupted by additive uniform noise.
(b) Image additionally corrupted by additive salt-and-pepper noise.
Image (b) filtered with a 5×5 ;
(c) arithmetic mean filter;
(d) geometric mean filter;
(e) median filter;
and (f) alpha-trimmed mean filter with $d = 5$.

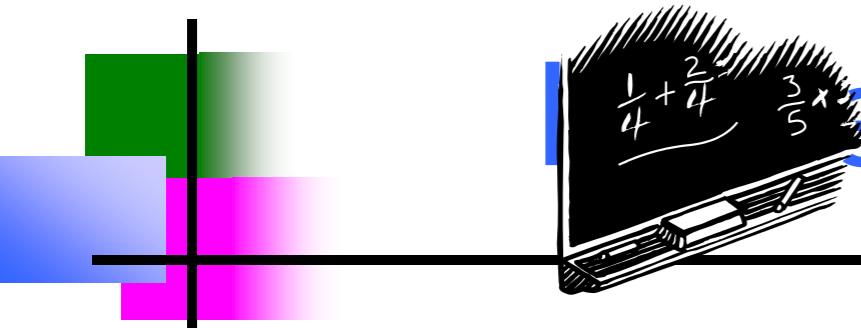


Image Corruption Example

Original Image

	x						
	54	52	57	55	56	52	51
	50	49	51	50	52	53	58
	51	204	52	52	0	57	60
	48	50	51	49	53	59	63
	49	51	52	55	58	64	67
	50	54	57	60	63	67	70
	51	55	59	62	65	69	72

Image $f(x, y)$

y

Filtered Image

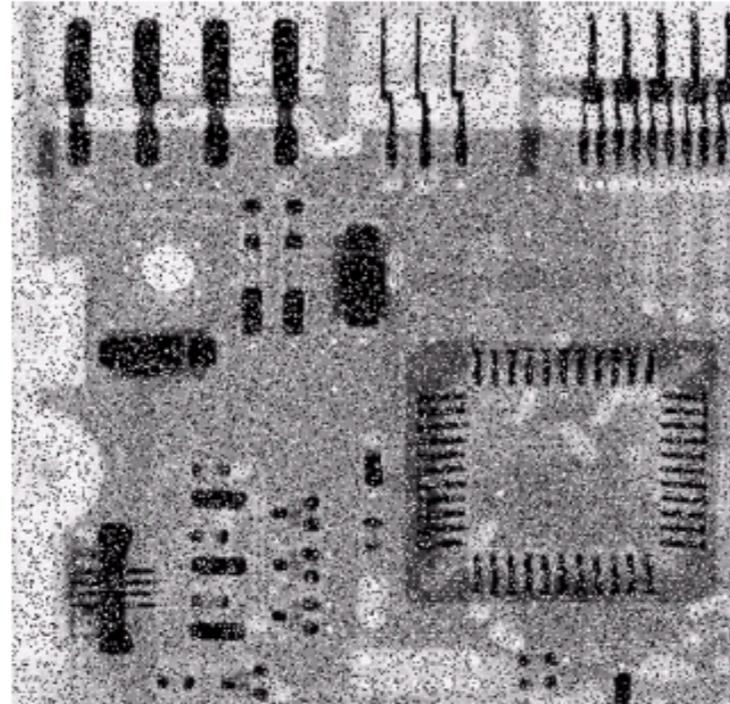
	x						

Image $f(x, y)$

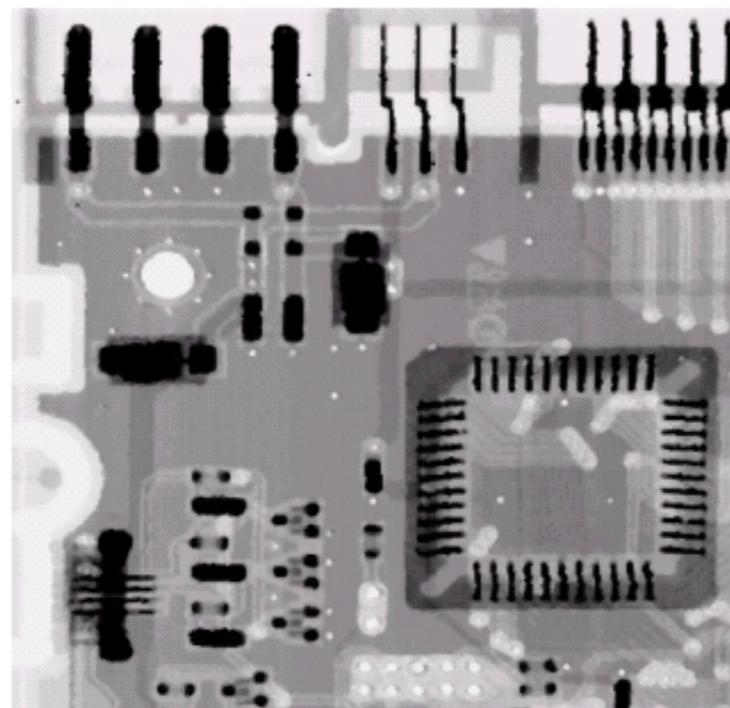
y

Noise Removal Examples

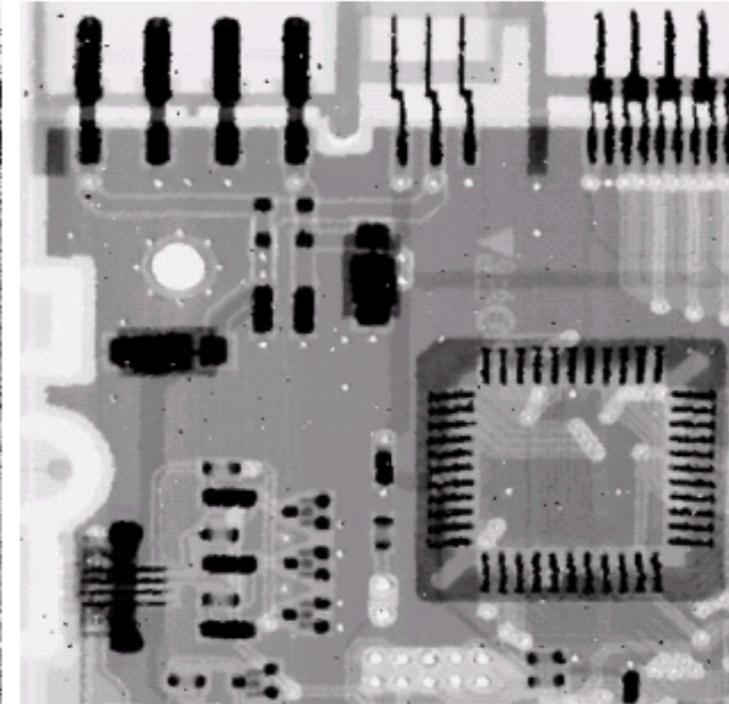
Image
Corrupted
By Salt And
Pepper Noise



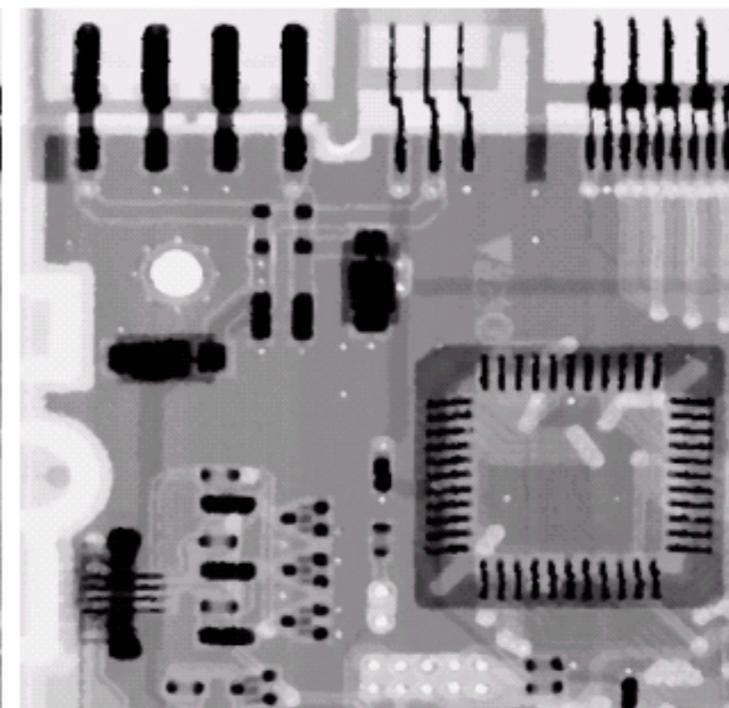
Result of 2
Passes With
A 3×3 Median
Filter



Result of 1
Pass With A
 3×3 Median
Filter

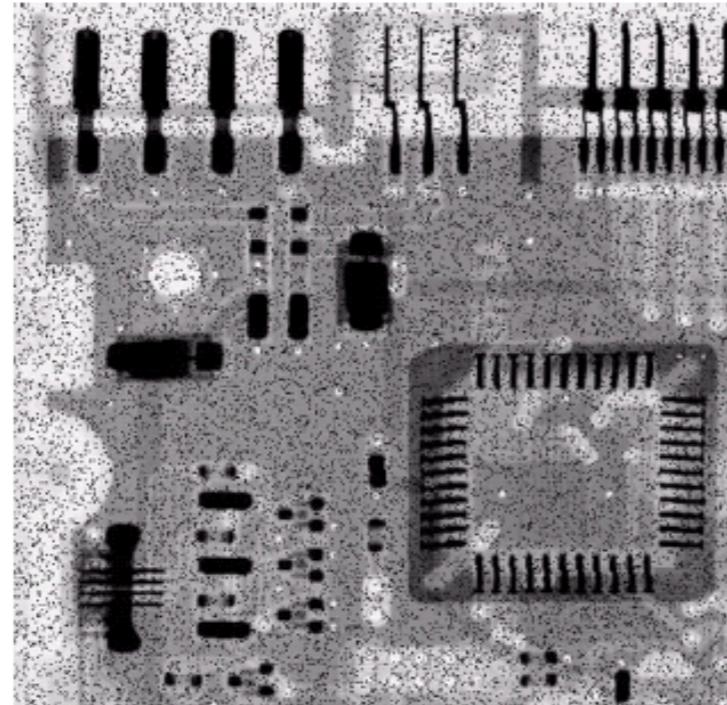


Result of 3
Passes With
A 3×3 Median
Filter



Noise Removal Examples (cont...)

Image
Corrupted
By Pepper
Noise



Result Of
Filtering
Above
With A 3×3
Max Filter

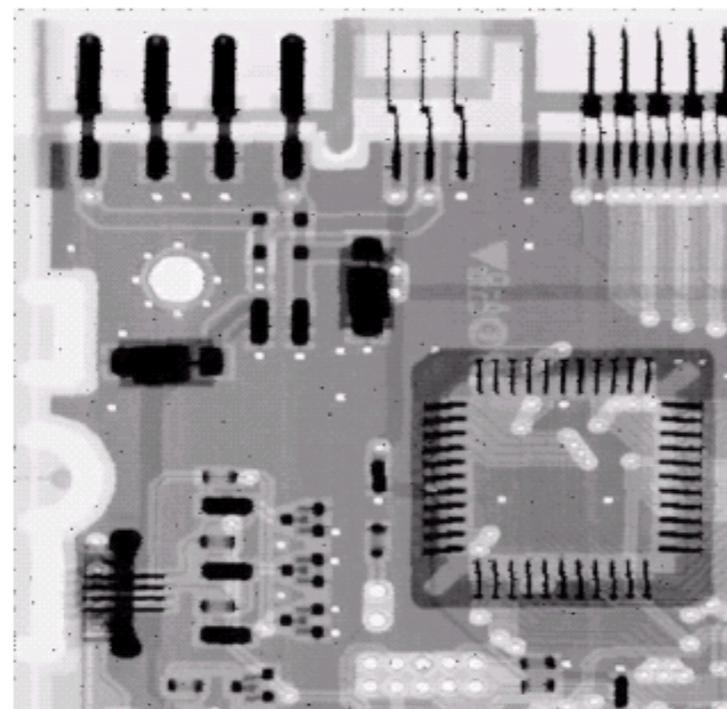
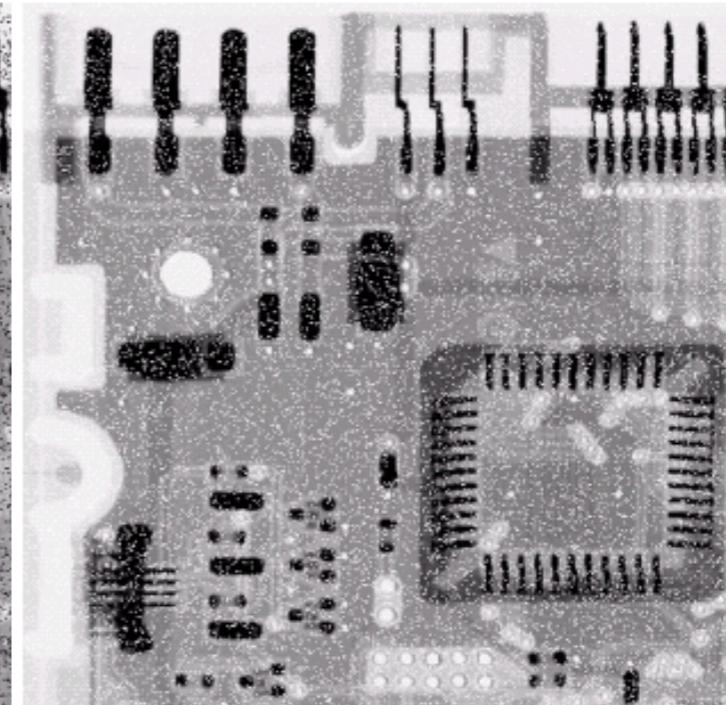
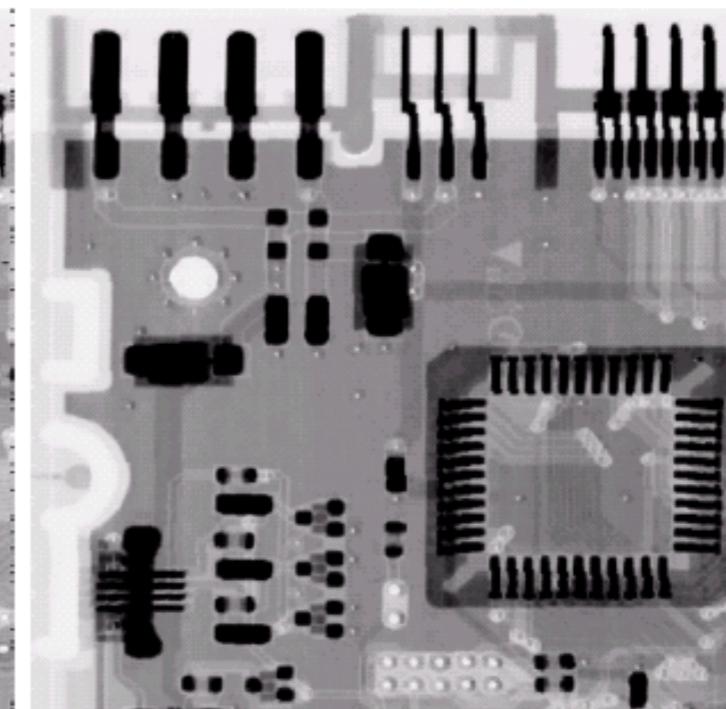


Image
Corrupted
By Salt
Noise



Result Of
Filtering
Above
With A 3×3
Min Filter



Noise Removal Examples (cont...)

Image
Corrupted
By Uniform
Noise

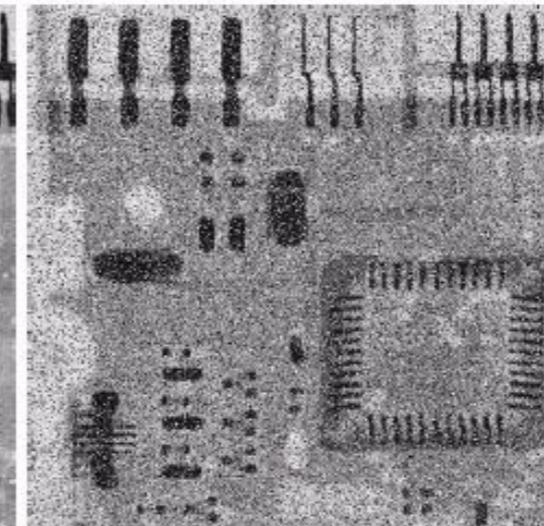
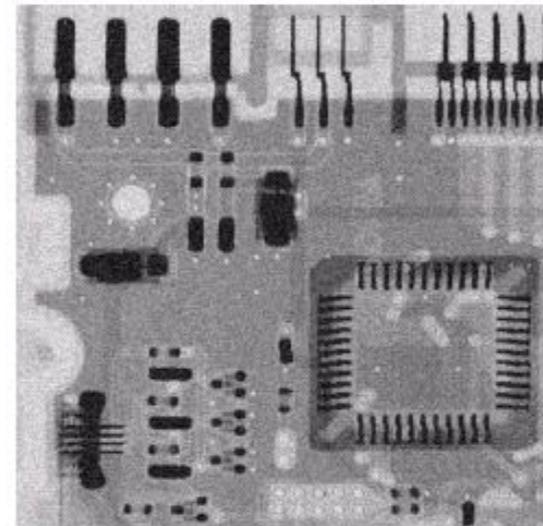
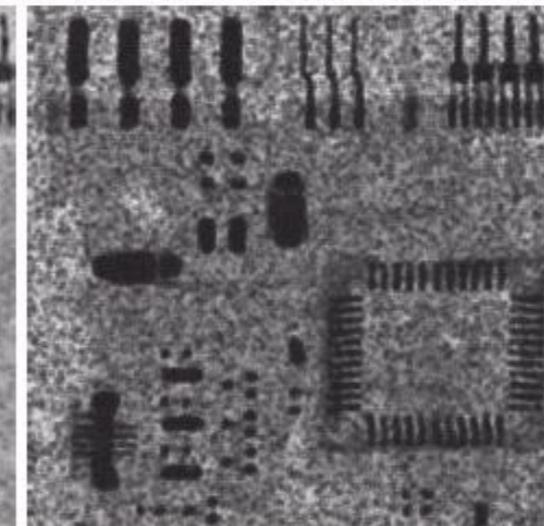
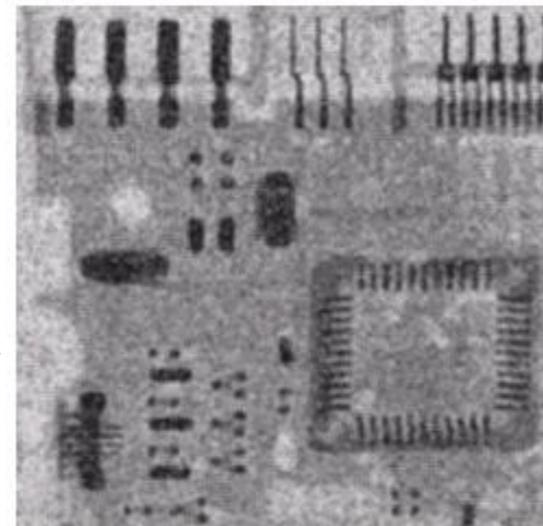


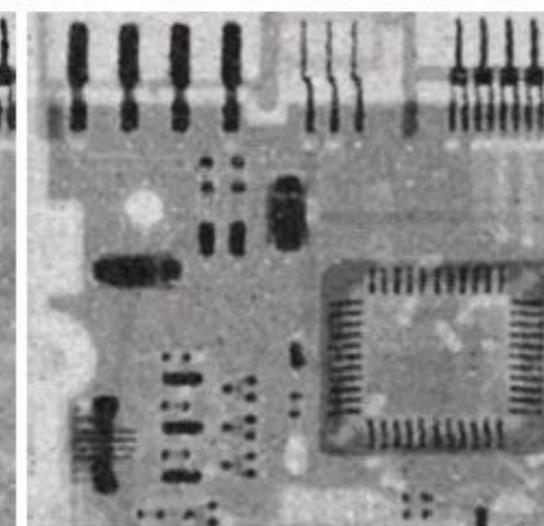
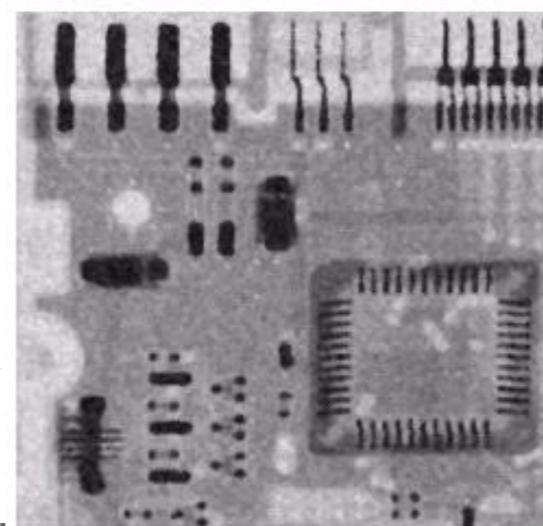
Image Further
Corrupted
By Salt and
Pepper Noise

Filtered By
 5×5 Arithmetic
Mean Filter

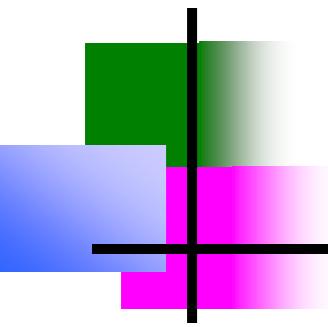


Filtered By
 5×5 Geometric
Mean Filter

Filtered By
 5×5 Median
Filter



Filtered By
 5×5 Alpha-Trimmed
Mean Filter

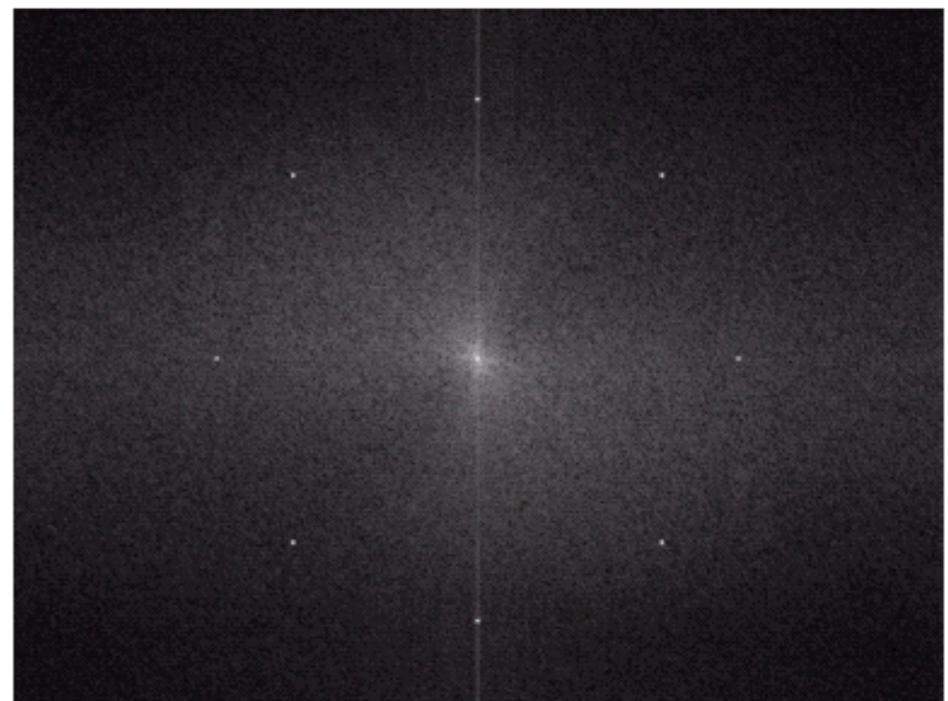
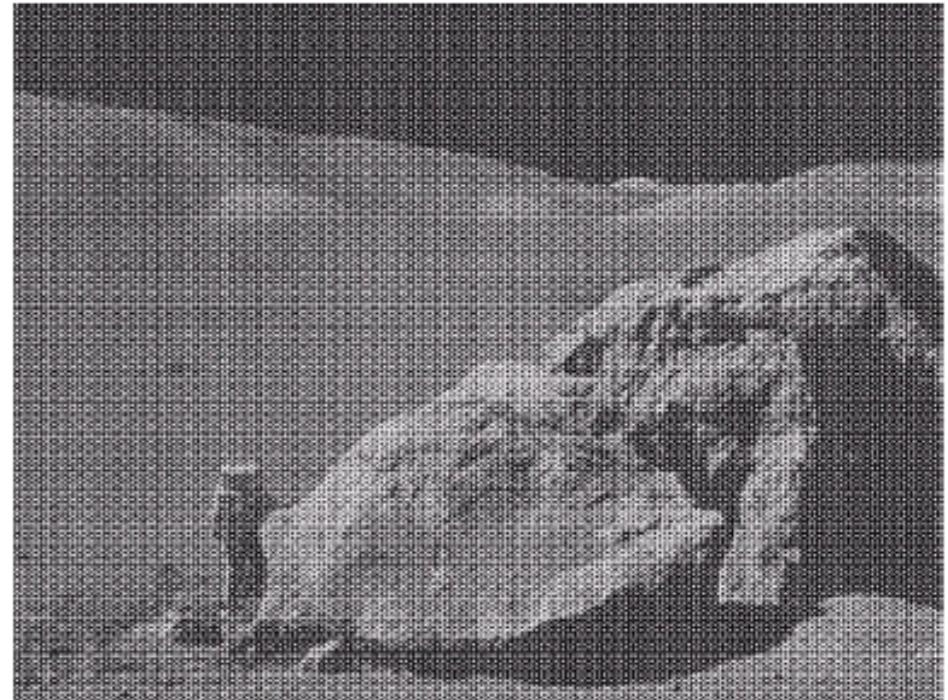


Periodic Noise

Typically arises due to electrical or electromagnetic interference

Gives rise to regular noise patterns in an image

Frequency domain techniques in the Fourier domain are most effective at removing periodic noise



Band Reject Filters

Removing periodic noise from an image involves removing a particular range of frequencies from that image

Band reject filters can be used for this purpose

An ideal band reject filter is given as follows:

$$H(u, v) = \begin{cases} 1 & \text{if } D(u, v) < D_0 - \frac{W}{2} \\ 0 & \text{if } D_0 - \frac{W}{2} \leq D(u, v) \leq D_0 + \frac{W}{2} \\ 1 & \text{if } D(u, v) > D_0 + \frac{W}{2} \end{cases}$$

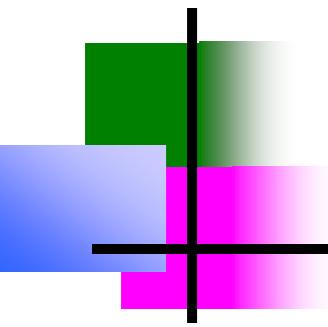
Band Reject Filters

Similarly, a Butterworth bandreject filter of order n is given by the expression

$$H(u, v) = \frac{1}{1 + \left[\frac{D(u, v)W}{D^2(u, v) - D_0^2} \right]^{2n}} \quad (5.4-2)$$

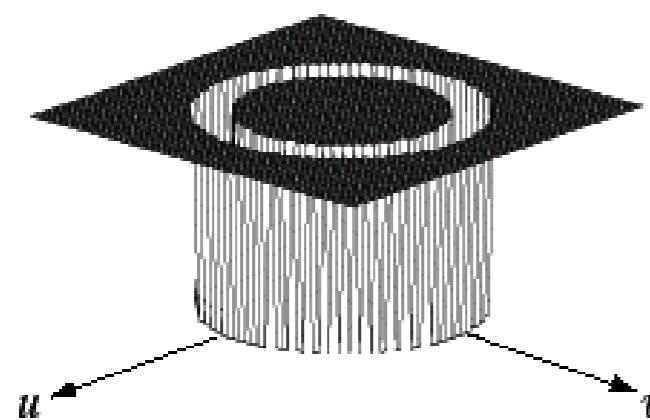
and a Gaussian bandreject filter is given by

$$H(u, v) = 1 - e^{-\frac{1}{2} \left[\frac{D^2(u, v) - D_0^2}{D(u, v)W} \right]^2}. \quad (5.4-3)$$

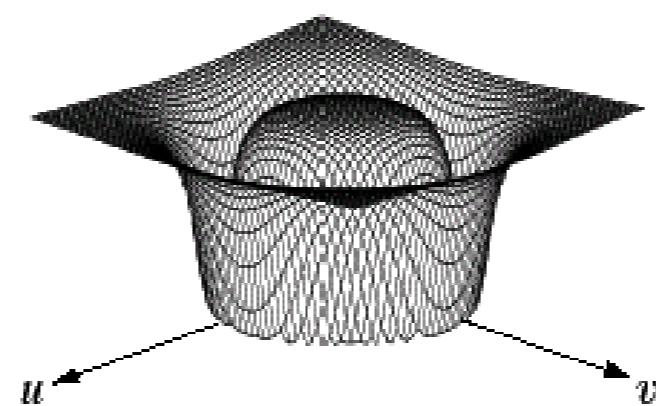


Band Reject Filters (cont...)

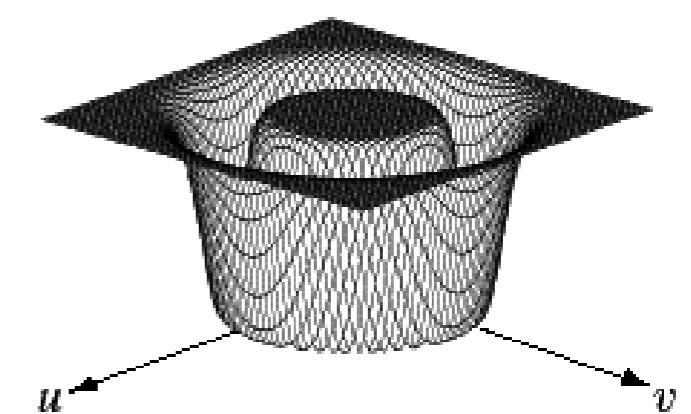
The ideal band reject filter is shown below, along with Butterworth and Gaussian versions of the filter



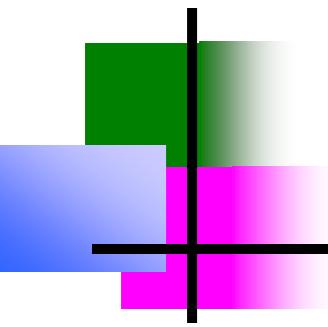
Ideal Band
Reject Filter



Butterworth
Band Reject
Filter (of order 1)

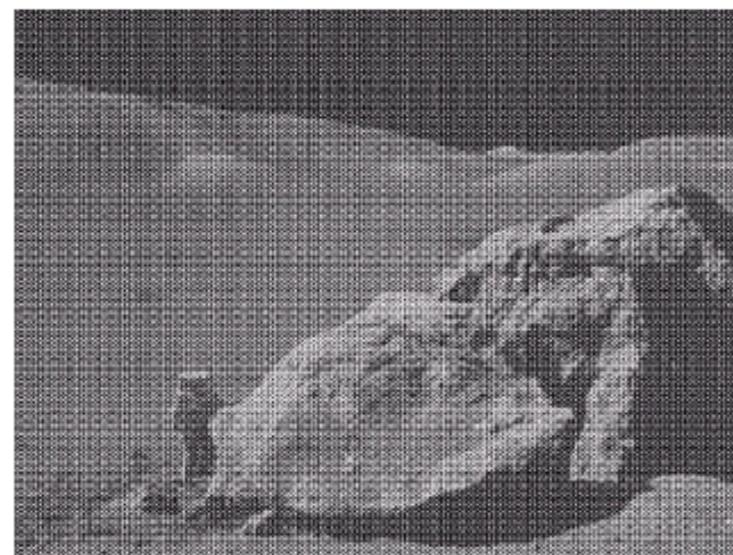


Gaussian
Band Reject
Filter

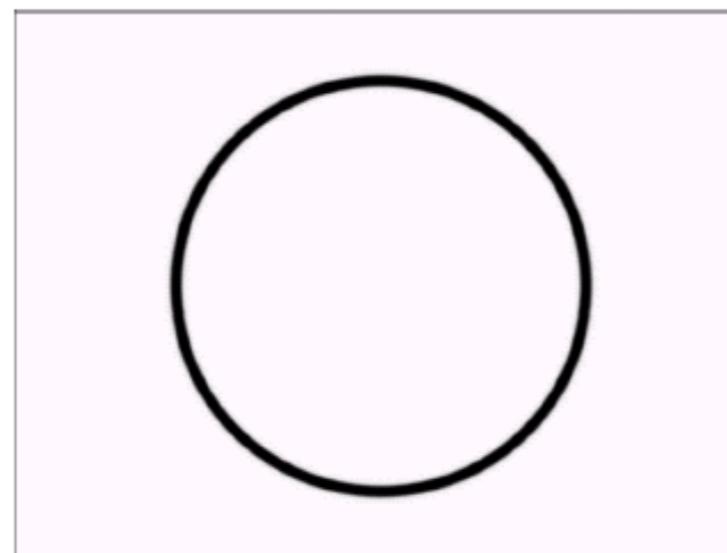


Band Reject Filter Example

Image corrupted by sinusoidal noise



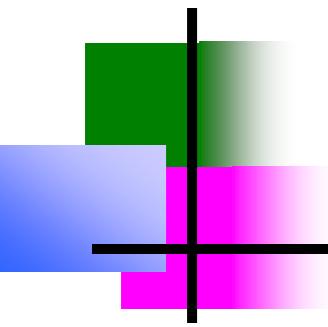
Fourier spectrum of corrupted image



Butterworth band reject filter



Filtered image



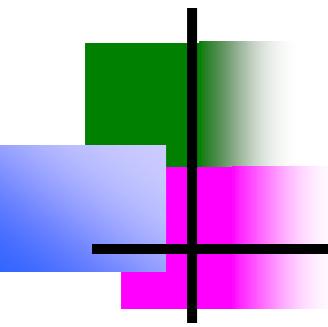
Summary

In this lecture we will look at image restoration for noise removal

Restoration is slightly more objective than enhancement

Spatial domain techniques are particularly useful for removing random noise

Frequency domain techniques are particularly useful for removing periodic noise

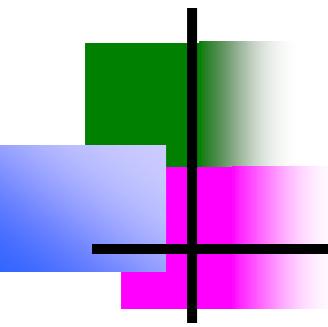


Adaptive Filters

The filters discussed so far are applied to an entire image without any regard for how image characteristics vary from one point to another

The behaviour of **adaptive filters** changes depending on the characteristics of the image inside the filter region

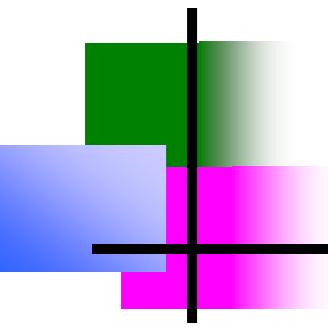
We will take a look at the **adaptive median filter**



Adaptive Filters

Adaptive filters

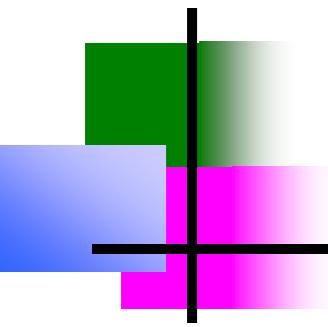
- All filters considered thus far are applied to an image without regard for how image characteristics may vary from one point to another in the image
- An *adaptive* filter is one whose behavior can change based on statistical characteristics of an area within the image
 - This is typically the $m \times n$ filter region in the $S_{x,y}$ window
- Generally provides superior performance at the cost of increased filter complexity



Adaptive Filters

Adaptive, local noise reduction filter

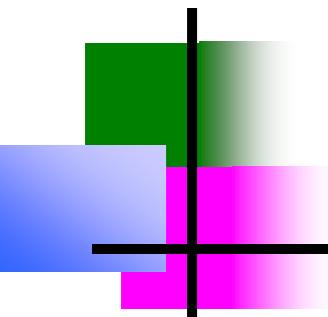
- The *mean* and *variance* are reasonable parameters upon which to base a simple adaptive filter
 - They are closely related to image properties
 - The *mean* gives the average intensity over a region
 - The *variance* gives a measure of the contrast in a region
- A simple filter will operate on a local region $S_{x,y}$ with the response at any point (x,y) base on four quantities:
 - The value of the noisy image at (x,y) : $g(x,y)$
 - The variance of the noise corrupting $f(x,y)$ to form $g(x,y)$: σ^2_η
 - The local mean of the pixels in $S_{x,y}$: m_L
 - The local variance of the pixels in $S_{x,y}$: σ^2_L



Adaptive Filters

Adaptive, local noise reduction filter algorithm

- If $\sigma_{\eta}^2 = 0$, return the value $g(x,y)$
 - This is the zero-noise case where $g(x,y) = f(x,y)$
- If the local variance (σ_L^2) is high relative to σ_{η}^2 , return a value close to $g(x,y)$
 - A high local variance is generally associated with image features (i.e. an edge, etc.) and should be preserved
- If $\sigma_L^2 = \sigma_{\eta}^2$, return the arithmetic mean of the pixels in $S_{x,y}$
 - This occurs if the local area has the same properties as the overall image. Local noise is reduced by averaging.



Adaptive Filters

Adaptive, local noise reduction filter equation

- An adaptive expression may be written as:

$$\hat{f}(x, y) = g(x, y) - \frac{\sigma_\eta^2}{\sigma_L^2} [g(x, y) - m_L]$$

- The only quantity that must be known is σ_η^2
- Everything else can be computed from $S_{x,y}$
- An assumption here is that $\sigma_\eta^2 \leq \sigma_L^2$
 - This is generally reasonable given that the noise we are considering is additive and position independent
 - If this is not true then a simple test could set the ratio of the variances to one if $\sigma_\eta^2 > \sigma_L^2$

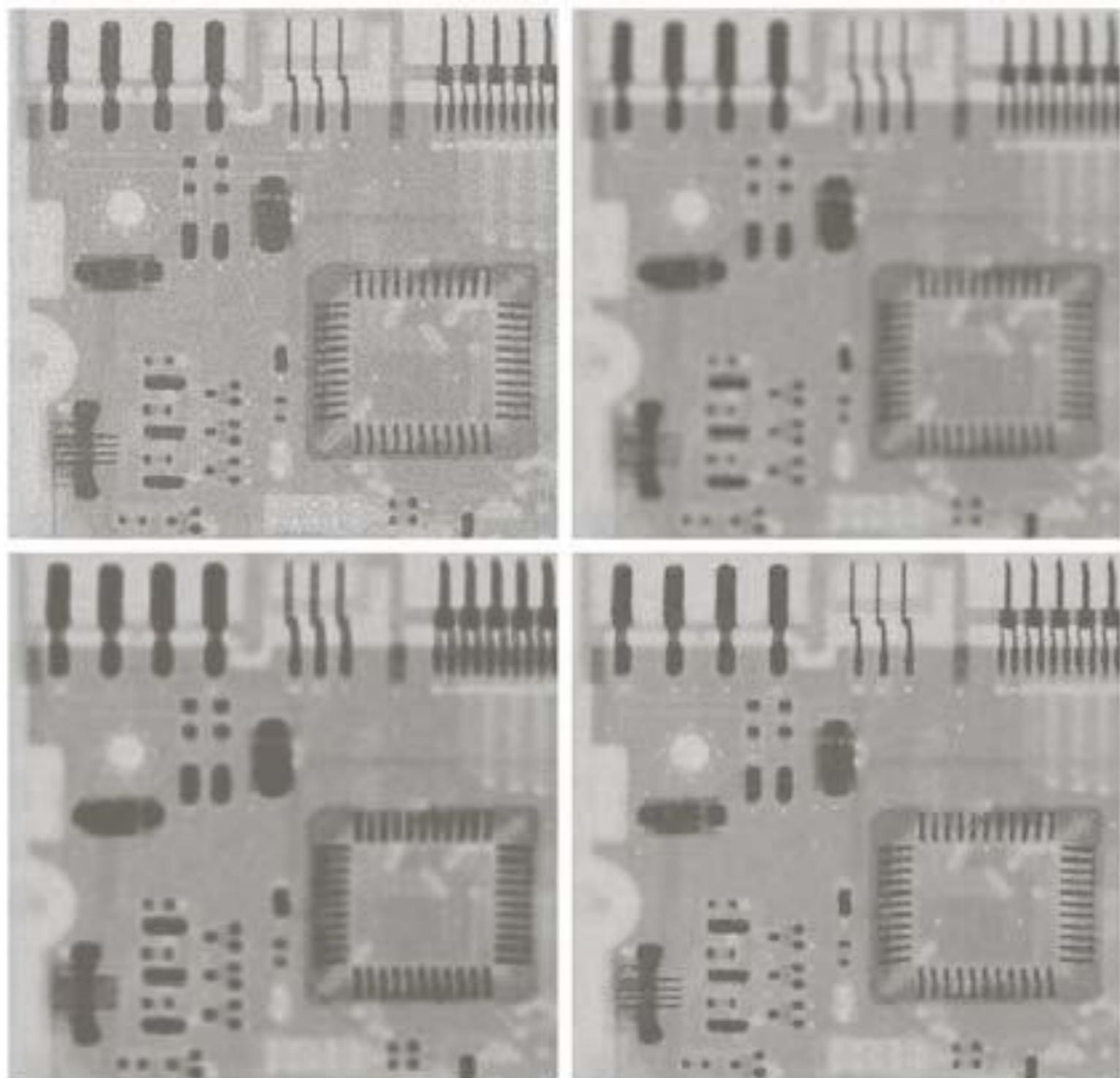
Adaptive Filters

Adaptive, local noise reduction filter example

a
b
c
d

FIGURE 5.13

- (a) Image corrupted by additive Gaussian noise of zero mean and variance 1000.
(b) Result of arithmetic mean filtering.
(c) Result of geometric mean filtering.
(d) Result of adaptive noise reduction filtering. All filters were of size 7×7 .

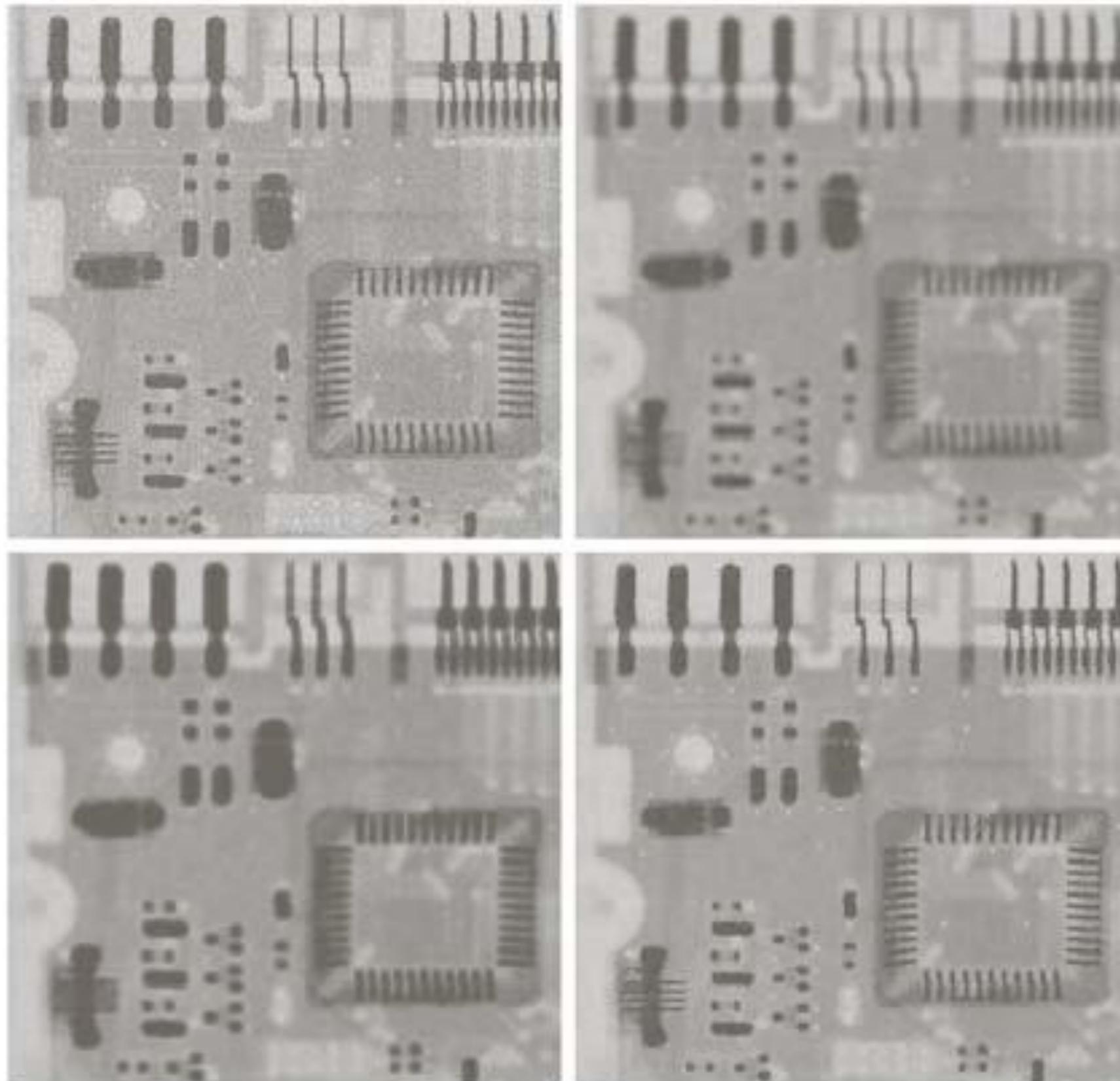


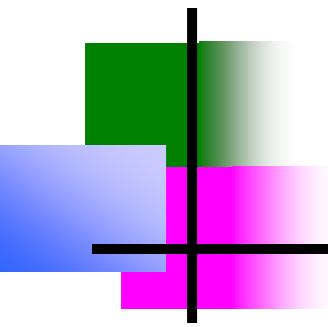
Adaptive Filters

a b
c d

FIGURE 5.13

- (a) Image corrupted by additive Gaussian noise of zero mean and variance 1000.
(b) Result of arithmetic mean filtering.
(c) Result of geometric mean filtering.
(d) Result of adaptive noise reduction filtering. All filters were of size 7×7 .

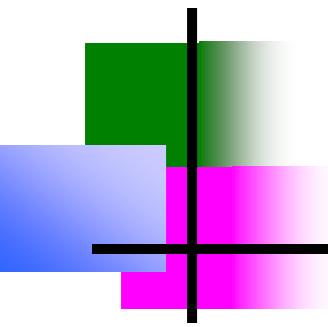




Adaptive Median Filtering

Adaptive median filter

- A median filter works well in the spectral density of the impulse noise is not large
 - A P_a and P_b less than 0.2 is a good general rule of thumb
- An adaptive median filter can handle noise with probabilities greater than these
- An additional benefit is that the adaptive median filter attempts to preserve detail while smoothing the impulse noise
- The adaptive median filter works in a rectangular window area $S_{x,y}$
 - The size of $S_{x,y}$ is not fixed
- The output of the filter is a single value that will be used to replace the center value of $S_{x,y}$



Adaptive Median Filtering

The median filter performs relatively well on impulse noise as long as the spatial density of the impulse noise is not large

The adaptive median filter can handle much more spatially dense impulse noise, and also performs some smoothing for non-impulse noise

The key insight in the adaptive median filter is that the filter size changes depending on the characteristics of the image

Adaptive Median Filtering (cont...)

Remember that filtering looks at each original pixel image in turn and generates a new filtered pixel

First examine the following notation:

$-z_{min}$ = minimum grey level in S_{xy}

$-z_{max}$ = maximum grey level in S_{xy}

$-z_{med}$ = median of grey levels in S_{xy}

$-z_{xy}$ = grey level at coordinates (x, y)

$-S_{max}$ = maximum allowed size of S_{xy}

Adaptive Median Filtering (cont...)

Level A:

$$A1 = z_{med} - z_{min}$$

$$A2 = z_{med} - z_{max}$$

If $A1 > 0$ and $A2 < 0$, Go to level B

Else increase the window size

If window size \leq repeat S_{max} level A

Else output z_{med}

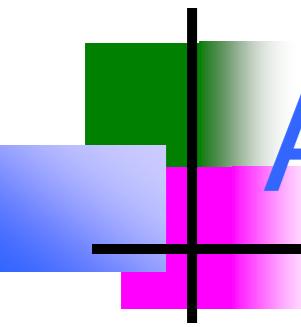
Level B:

$$B1 = z_{xy} - z_{min}$$

$$B2 = z_{xy} - z_{max}$$

If $B1 > 0$ and $B2 < 0$, output z_{xy}

Else output z_{med}



Adaptive Median Filtering (cont...)

The key to understanding the algorithm is to remember that the adaptive median filter has three purposes:

- Remove impulse noise
- Provide smoothing of other noise
- Reduce distortion

Adaptive Filtering Example

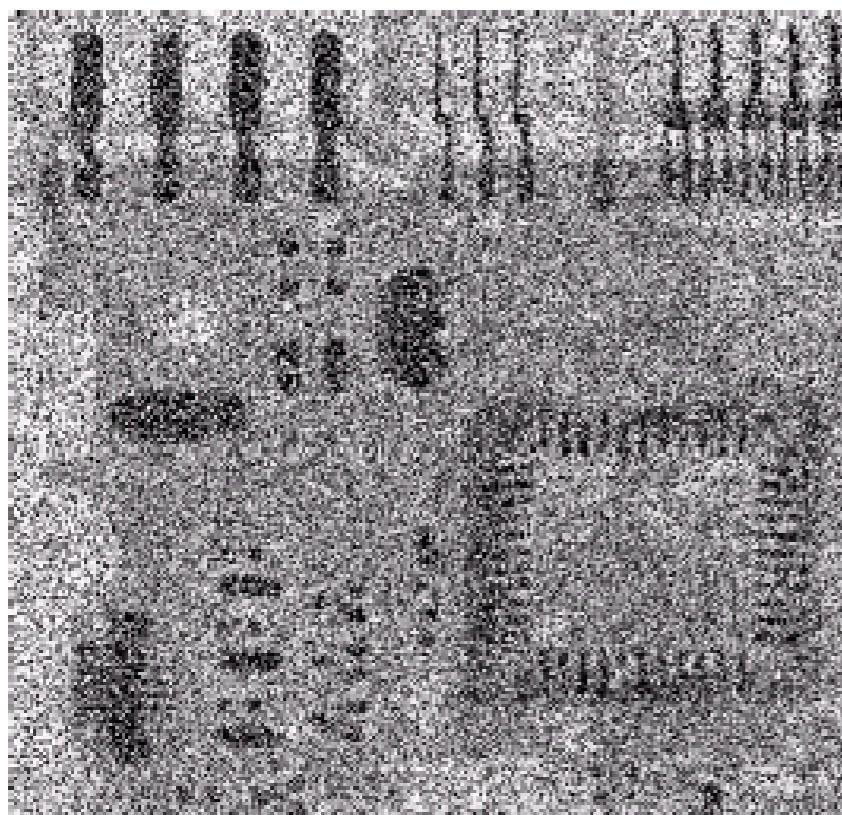
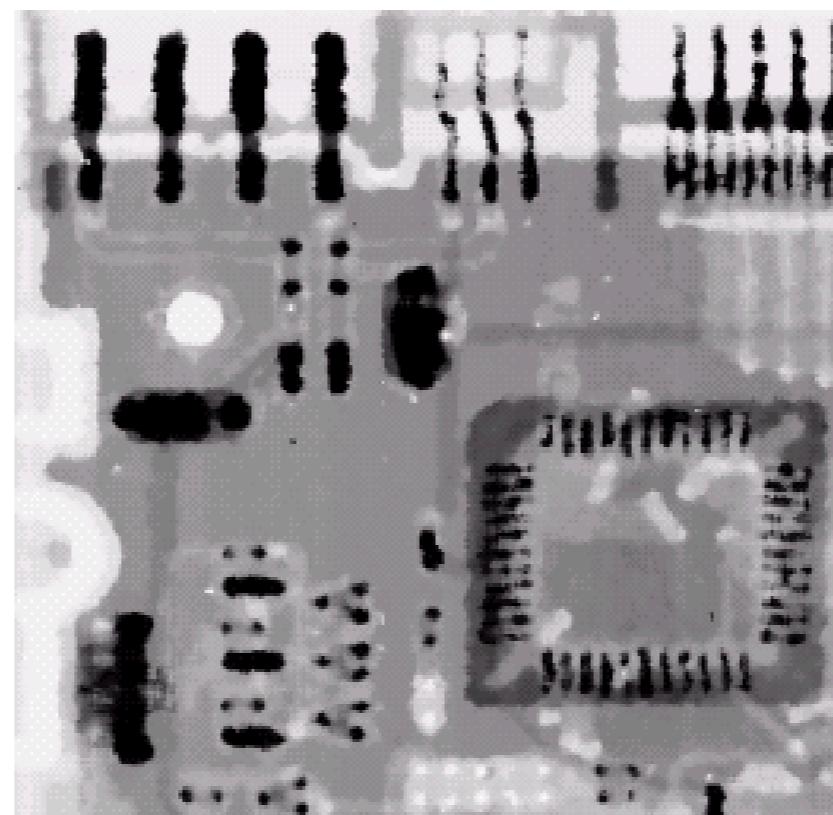
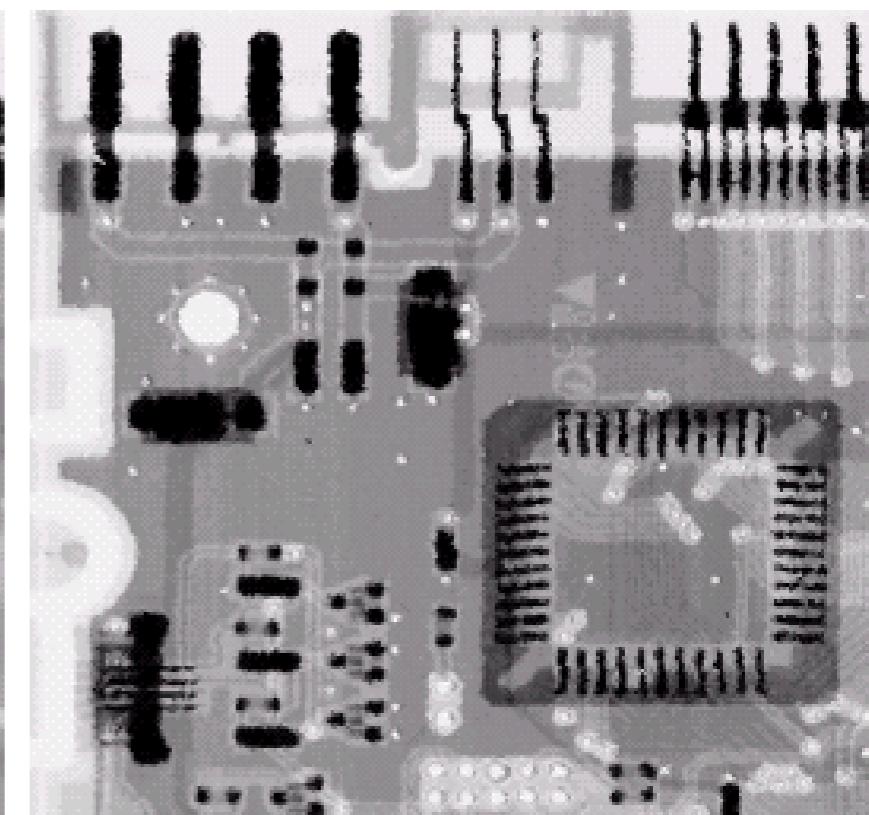


Image corrupted by salt
and pepper noise with
probabilities $P_a = P_b = 0.25$

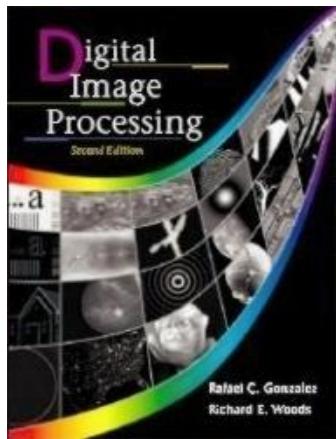


Result of filtering with a 7
* 7 median filter



Result of adaptive median
filtering with $i = 7$

References

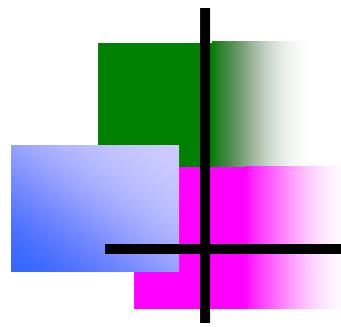


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Thank you !!!