

POKHARA UNIVERSITY

Level: Bachelor

Semester – Spring

Year: 2020

Program: BE

Full Marks: 70

Course: Engineering Mathematics I

Pass Marks: 31.5

Time: 2 hrs.

Candidates are required to answer in their own words as far as practicable. The figures in the margin indicate full marks.

Group - A: Attempt all questions (5×10=50)

- Q. N. 1 a) Suppose that f is an even function of x . Does knowing that $\lim_{x \rightarrow 2^-} f(x) = 7$ tell you anything about either $\lim_{x \rightarrow -2^-} f(x)$ or $\lim_{x \rightarrow -2^+} f(x)$? Give reasons for your answer. 3.5+3.5+3
- b) For what values of x , if any y' is positive? zero? negative?
- c) Show that the function
$$f(x) = \begin{cases} x & \text{for } x < 1 \\ 2 - x & \text{for } 1 \leq x < 2 \\ -2 + 3x - x^2 & \text{for } x \geq 2 \end{cases}$$
 is continuous at $x = 1$ but not differentiable at $x = 1$.

OR

- a) State Mean Value Theorem, using it find the values of a , m , and b of the function
$$f(x) = \begin{cases} 3 & x = 0 \\ -x^2 + 3x + a & 0 < x < 1, \text{ where } f(x) \text{ satisfied the} \\ mx + b & 1 \leq x \leq 2 \end{cases}$$
 conditions of MVT in $[0, 2]$. 4+3+3
- b) Suppose that f is differentiable on $[0, 1]$ and that its derivative is never zero. Show that $f(0) \neq f(1)$.
- c) Suppose that f is differentiable on $[a, b]$ and that $f(b) < f(a)$. Can you then say anything about the values of f' on $[a, b]$?
- Q. N. 2 a) Define conic section and classify them with respect to eccentricity. 2+1+3+4
- b) For what value of e the ellipse reduces to the circle?
- c) Derive standard equation of hyperbola.
- d) The foci of the hyperbola coincide with the foci of the ellipse $\frac{x^2}{25} + \frac{y^2}{9} = 1$. Find the equation of hyperbola with eccentricity 2.
- Q. N. 3 a) What is definite and indefinite integral? 1+2+3+4
- b) How does the method of substitution work for definite integrals? Give examples.

c) Verify the integral $\int_0^1 \frac{\log(1+x)dx}{1+x^2} = \frac{\pi}{8} \log 2$.

d) Show that $\int_0^\pi 2 \sin^2 x \, dx = \pi$. How close do you come to this value by using trapezoidal rule with $n=6$? Simpson's rule with $n=6$?

Q. N. 4 a) Find the area of the propeller –shaped region enclosed by the curves $x - y^{\frac{1}{3}} = 0$ and the line $x - y^{\frac{1}{5}} = 0$. 5+5

b) Find the volume of the solid generated by revolving the region bounded by the parabola $y = x^2$ and the line $y=1$ about
i) the line $y=1$; ii) the line $y=2$; iii) the line $y = -1$.

Q. N. 5 a) How you define the term indeterminate form. Justify with the fact that 1^∞ is an indeterminate form. 2+4+4

b) Find the asymptotes of the curve:

$$x^3 + 3x^2y - xy^2 - 3y^3 + x^2 - 2xy + 3y^2 + 4x + 5 = 0$$

c) Define the physical meaning of the curvature. Find the radius of curvature at origin of the following curve as; $x^4 + y^2 = 6a(x + y)$.

Group - B: (1×20=20)

Q. N. 6 a) Let \vec{v} be a vector in the plane not parallel to the y-axis. How is the slope of \vec{v} related to the slope of \vec{v} ? Give reasons for your answer. 5+5+5+5

b) Explain briefly how the value of scalar triple product of three vector is zero if all the vectors are co-planer.

c) Find a plane through the origin that meets the plane M; $2x+3y+z=12$ in a right angle. How do you know that your plane is perpendicular to M?

d) In the line $x= 1-2t$, $y=2+5t$, $z=-3t$ parallel to the plane $2x+y-z =8$? Give reasons for your answer.