

**OPTIMIZATION OF AN AXIALLY
COMPRESSED RING AND STRINGER
STIFFENED CYLINDRICAL SHELL
WITH A GENERAL BUCKLING
MODAL IMPERFECTION**

AIAA Paper 2007-2216

David Bushnell, Fellow, AIAA, retired

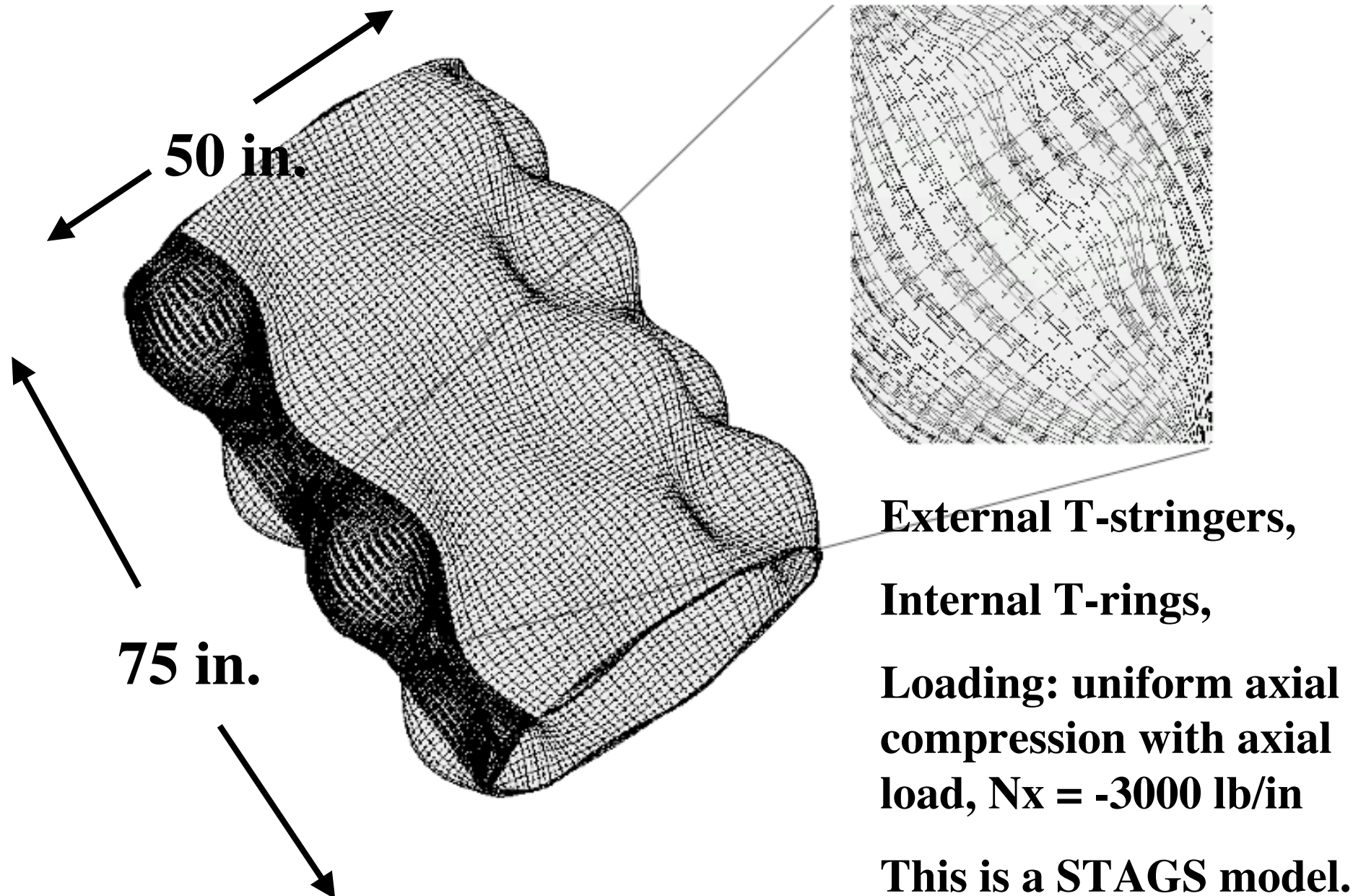
In memory of Frank Brogan, 1925 - 2006, co-developer of STAGS



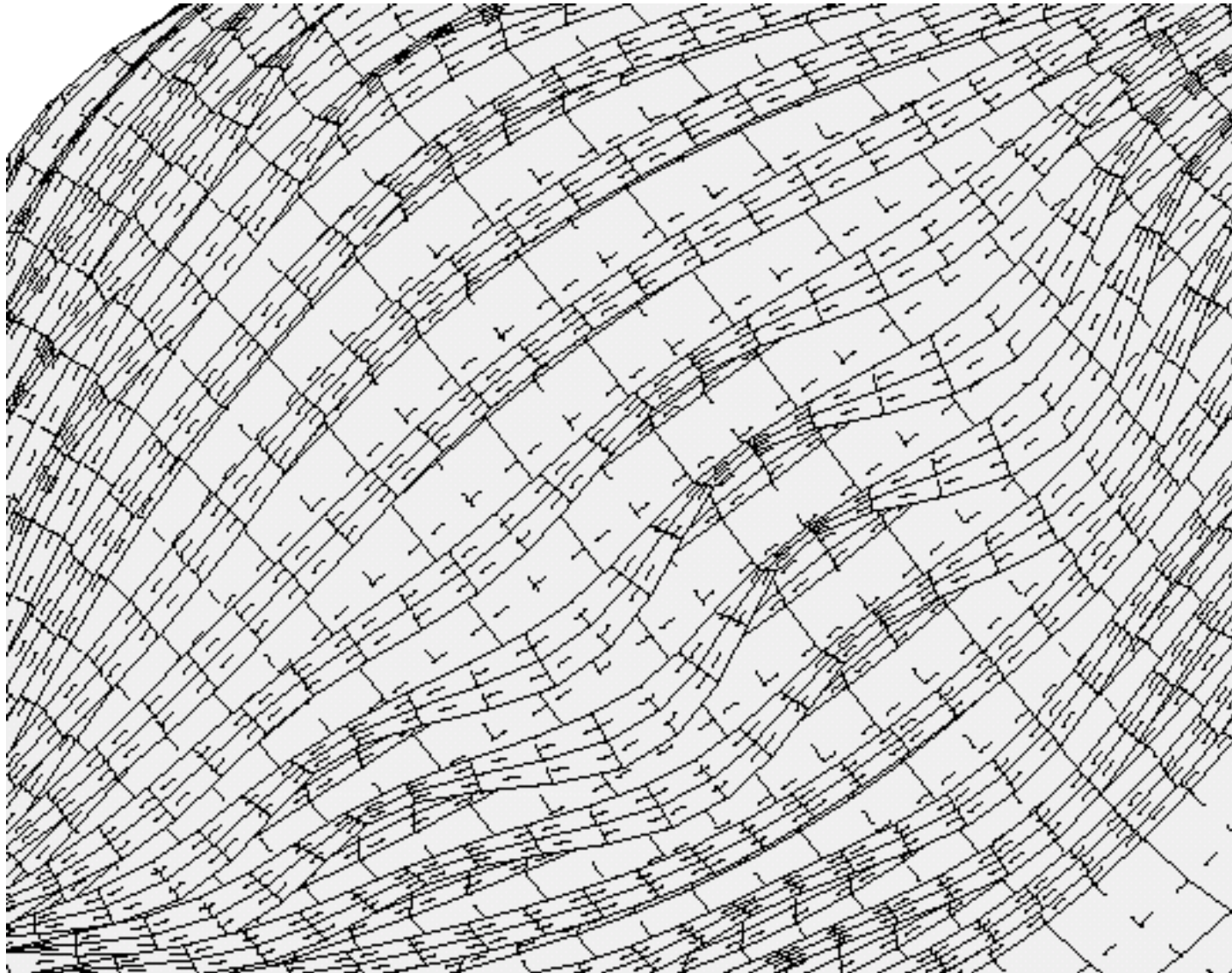
Summary of talk

- 1. The configuration studied here**
- 2. Two effects of a general imperfection**
- 3. PANDA2 and STAGS**
- 4. PANDA2 philosophy**
- 5. Seven cases studied here**
- 6. The optimization problem**
- 7. Buckling and stress constraints**
- 8. Seven cases explained**
- 9. How the shells fail**
- 10. Imperfection sensitivity**

General buckling mode from STAGS



Expanded region of buckling mode



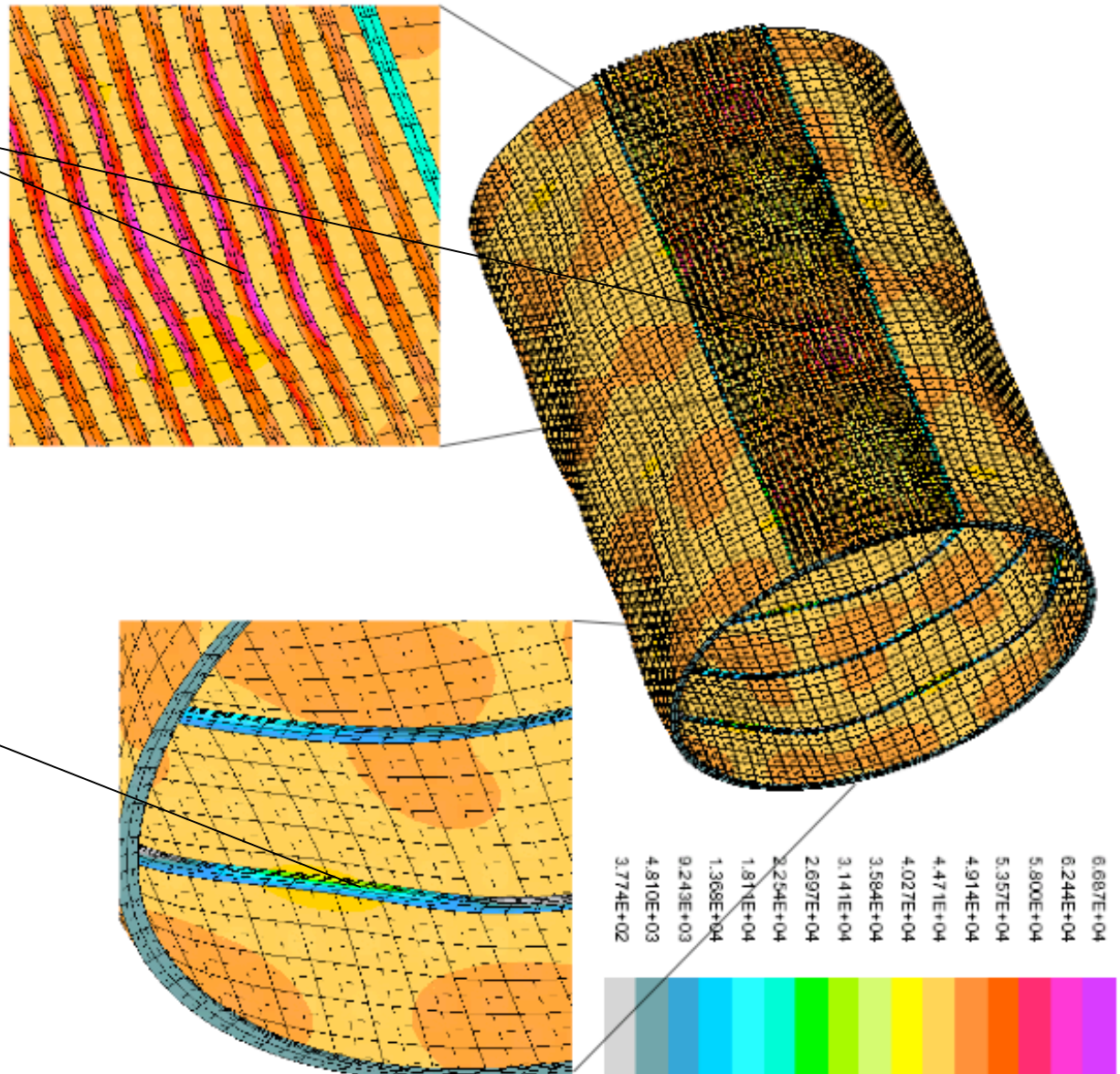
TWO MAJOR EFFECTS OF A GENERAL IMPERFECTION

1. The imperfect shell bends when any loads are applied. This “prebuckling” bending causes **redistribution of stresses** between the panel skin and the various segments of the stringers and rings.
2. The “**effective**” **radius of curvature** of the imperfect and loaded shell is larger than the nominal radius: “**flat**” **regions develop**.

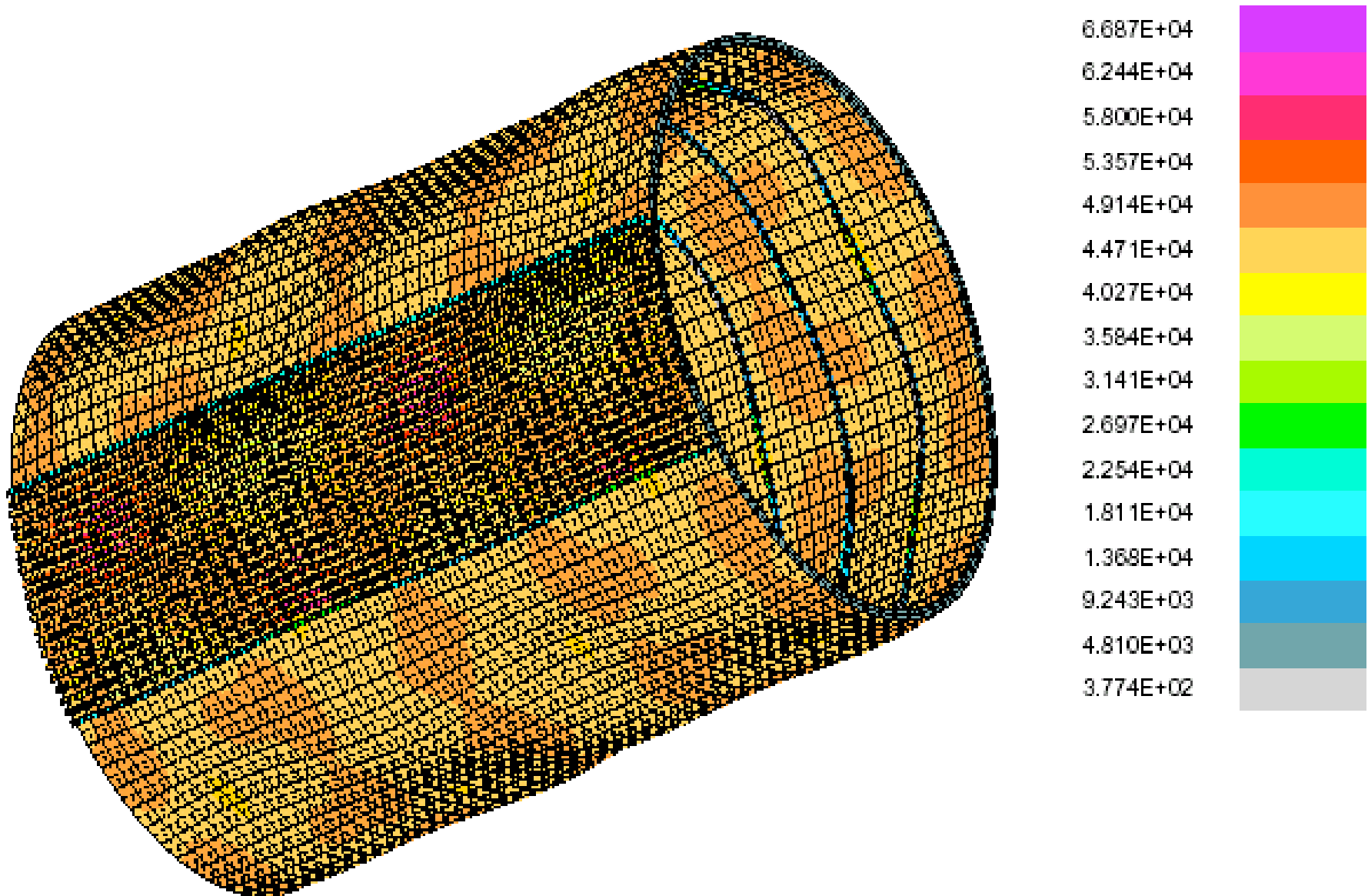
Loaded imperfect cylinder

**Maximum
stress,
 $\bar{s}(\max)$
=66.87 ksi**

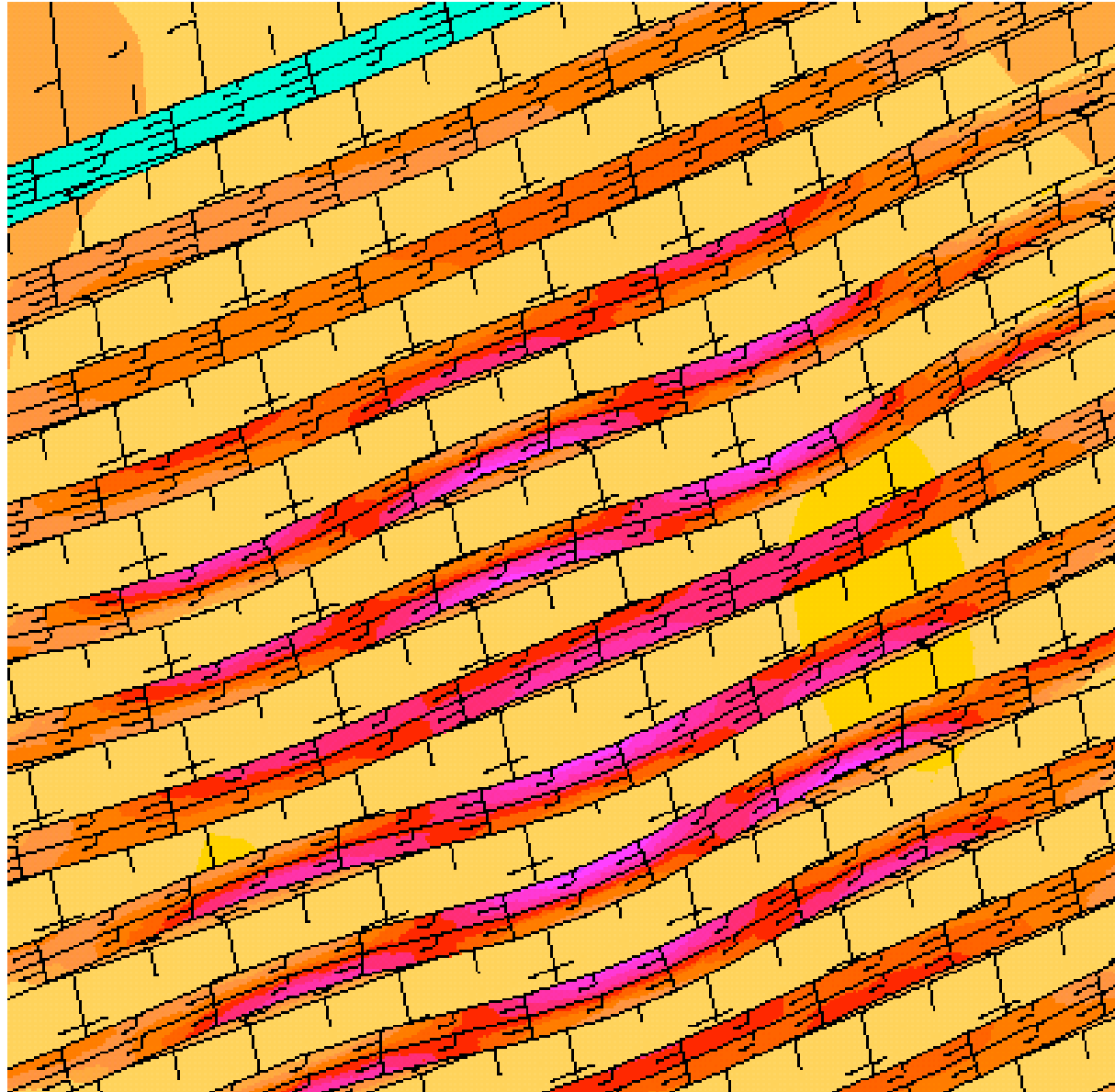
**“Flat”
region**



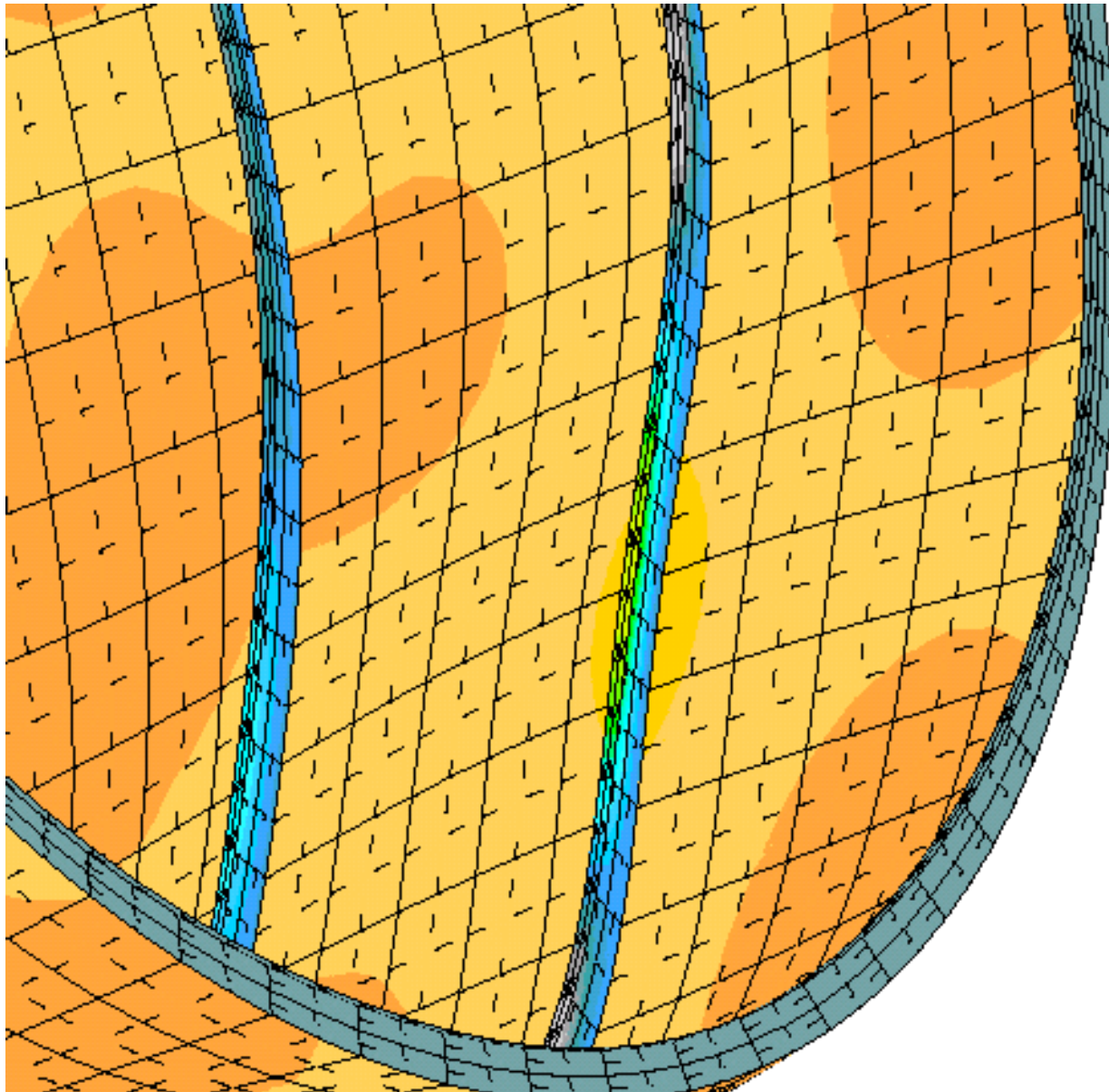
The entire deformed cylinder



The area of maximum stress



The “flattened” region



Computer programs **PANDA2** and **STAGS**

PANDA2 optimizes ring and stringer stiffened flat or cylindrical panels and shells made of laminated composite material or simple isotropic or orthotropic material. The shells can be perfect or **imperfect** and can be loaded by up to five combinations of **N_x , N_y , N_{xy}** .

STAGS is a general-purpose program for the nonlinear elastic or elastic-plastic static and dynamic analyses. **I used STAGS to check the optimum designs obtained by PANDA2.**

PHILOSOPHY OF PANDA2

1. **PANDA2** obtains optimum designs through the use of **many relatively simple models**, each of which yields **approximate** buckling load factors (eigenvalues) and stresses.
2. Details about these models are **given in previous papers**. Therefore, they are **not repeated here**.
3. **“Global” optimum designs** can be obtained reasonably quickly and are not overly unconservative or conservative.
4. Because of the approximate nature of PANDA2 models, optimum designs obtained by **PANDA2** should be **checked** by the use of a general-purpose finite element computer program.
5. **STAGS** is a good choice because PANDA2 automatically generates input data for STAGS, and **STAGS has excellent reliable nonlinear capabilities**.

Example of PANDA2 philosophy

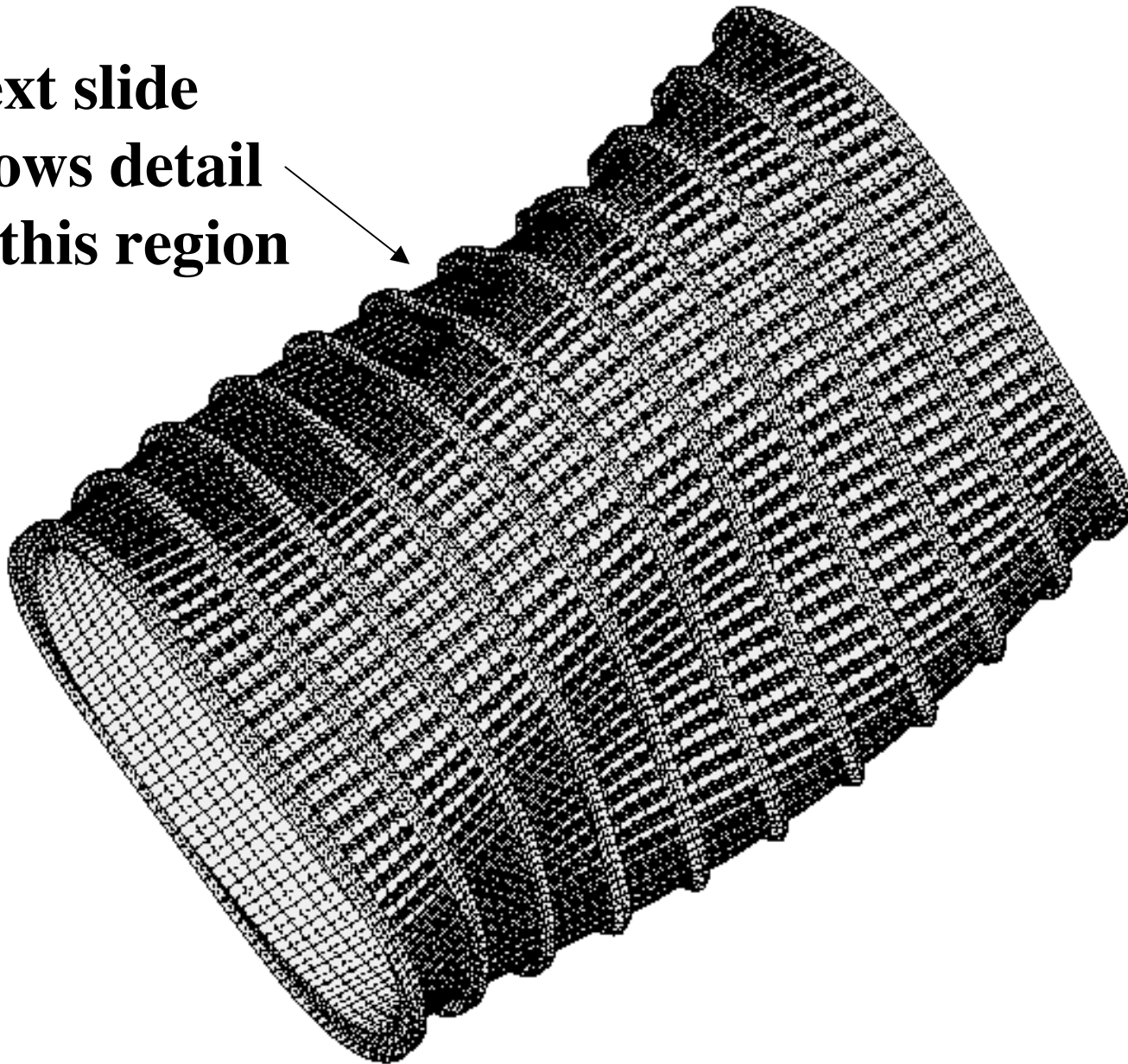
PANDA2 computes general buckling **from a simple closed-form model in which the stringers and rings are “smeared out”** as prescribed by Baruch and Singer (1963). [Bushnell (1987)]

Correction factors (knockdown factors) are computed to compensate for the inherent unconservativeness of this “smeared” model: one knockdown factor for “smearing” the stringers and another knockdown factor for “smearing” the rings.

The next several slides demonstrate **why a knockdown factor is needed** to compensate for the inherent unconservativeness of “smearing” the rings and **how this knockdown factor is computed.**

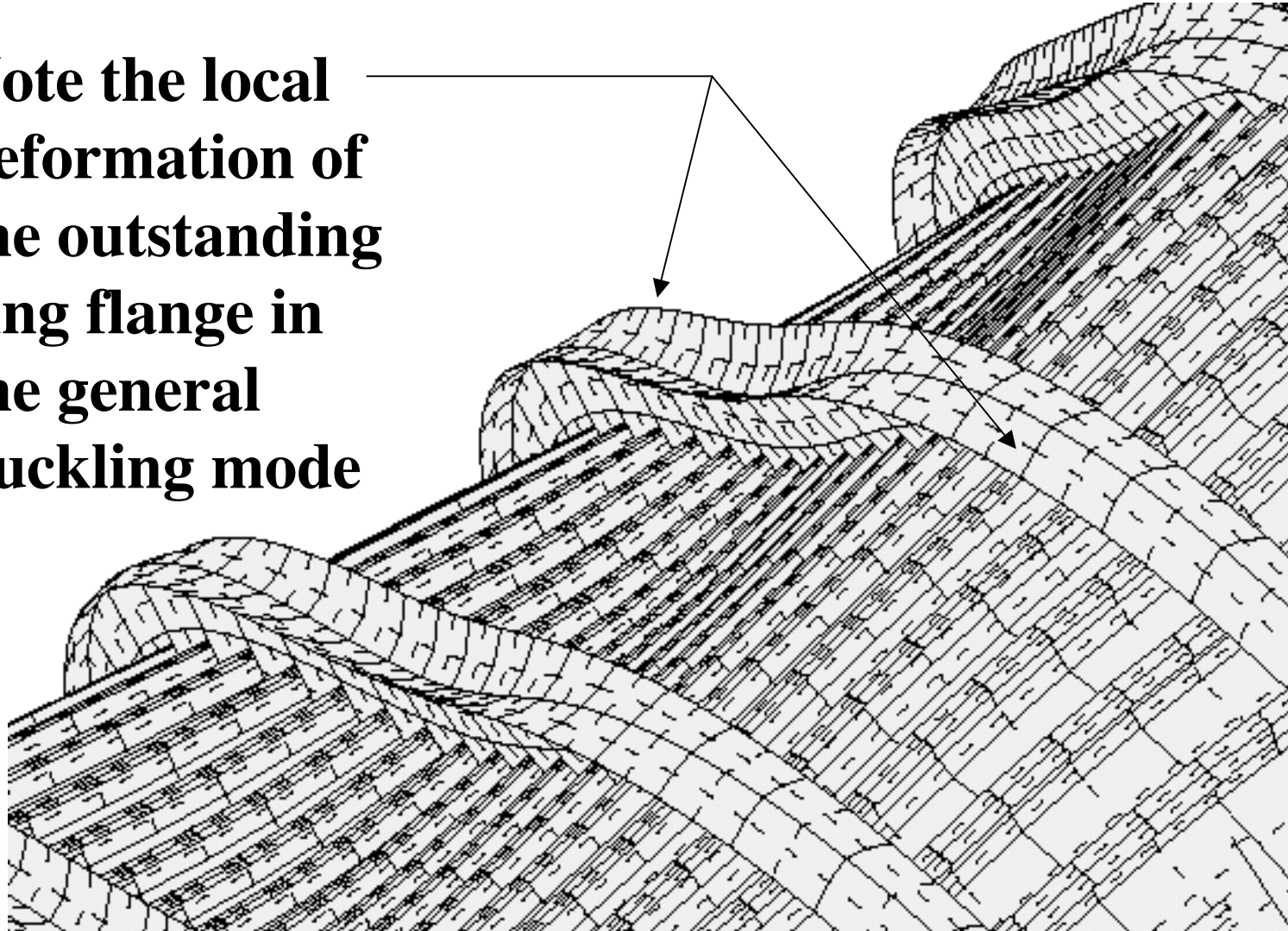
A general buckling mode from STAGS

**Next slide
shows detail
in this region**



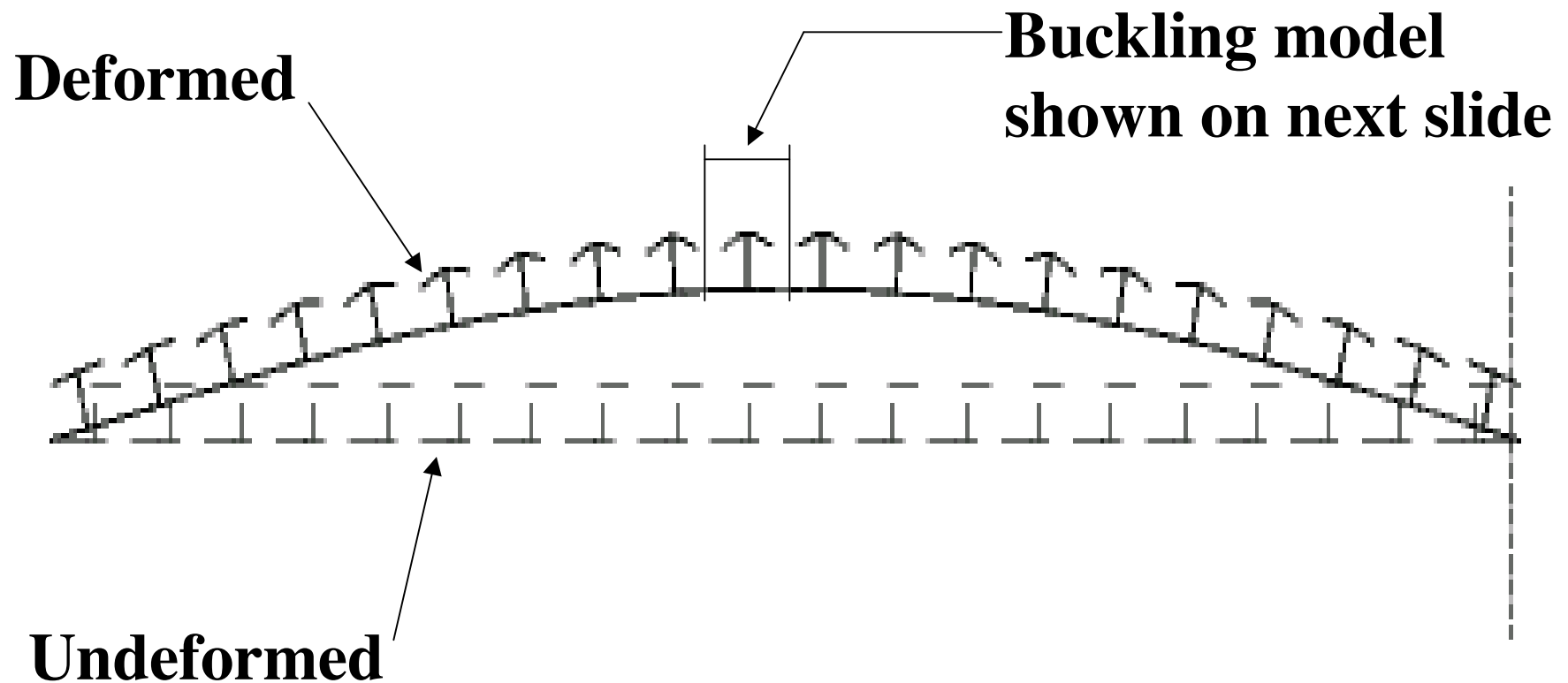
Detail showing local/global deformation in STAGS model

Note the local deformation of the outstanding ring flange in the general buckling mode

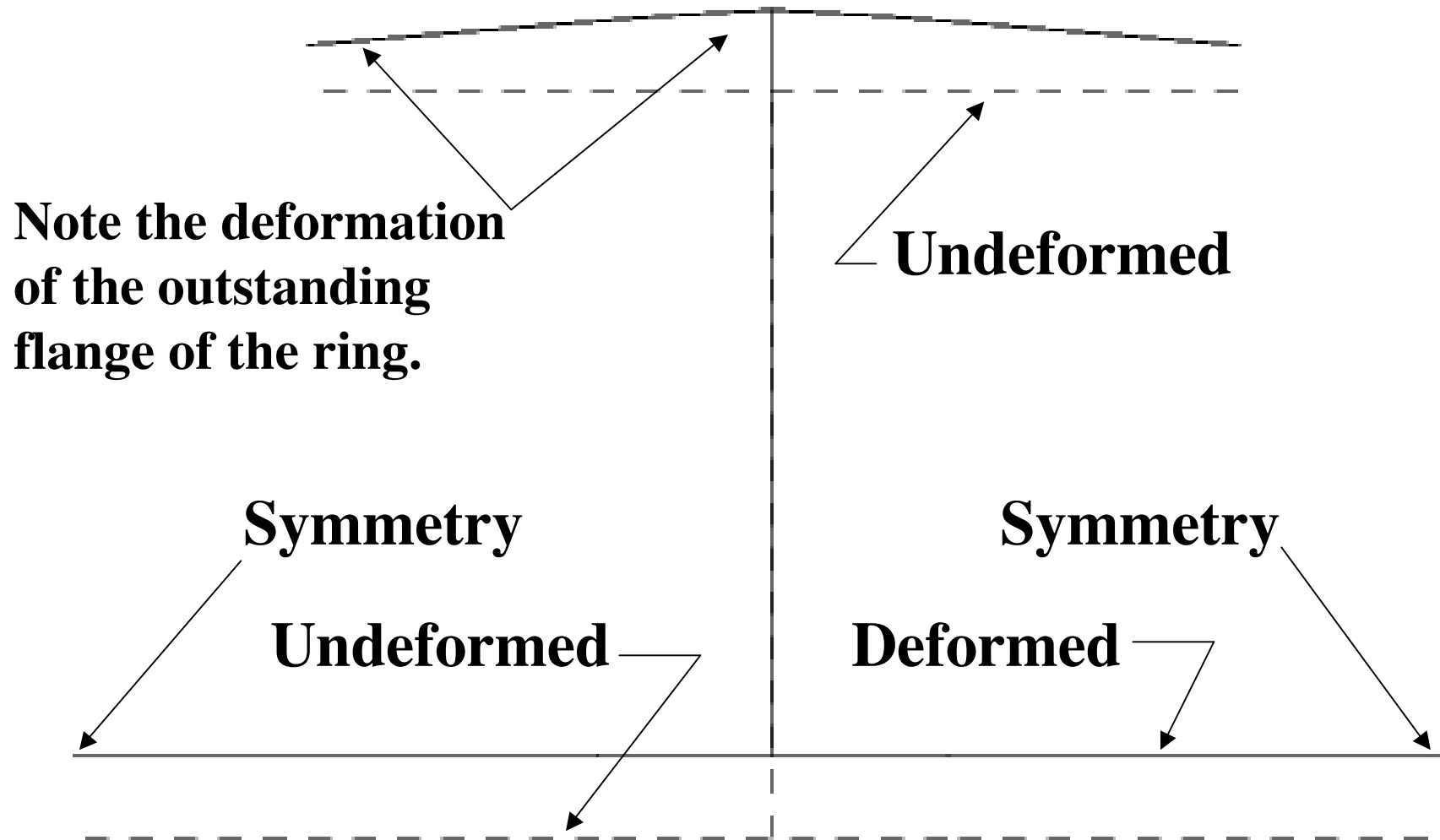


The same general buckling mode from
BIGBOSOR4 (Bushnell, 1999).

$n = 3$ circumferential waves



Approximate BIGBOSOR4 model of general buckling, $n = 3$



Knockdown factor to compensate
for inherent unconservativeness of
“smearing” rings

Ring knockdown factor =

(Buckling load from the BIGBOSOR4 model)/

(“Classical” ring buckling formula)

“Classical” ring buckling formula= $(n^2 - 1) EI/r^3$

SEVEN PANDA2 CASES IN TABLE 4 OF THE PAPER

Case 1: perfect shell, “no Koiter”, ICONSV=1

Case 2: imperfect, “no Koiter”, yes change imperf., ICONSV=-1

Case 3: imperfect, “no Koiter”, yes change imperf., ICONSV= 0

Case 4: imperfect, “no Koiter”, yes change imperf., ICONSV =1

Case 5: imperfect, “yes Koiter”, yes change imperf., ICONSV=1

Case 6: as if perfect, “no Koiter”, $N_x=-6000$ lb/in, ICONSV= 1

Case 7: imperfect, “no Koiter”, no change imperf., ICONSV= 1

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Decision variables for PANDA2 optimization

Stringer spacing **B(STR)**, Ring spacing **B(RNG)**, Shell skin thickness **T1(SKIN)**

T-stringer web height **H(STR)** and outstanding flange width **W(STR)**

T-stringer web thickness **T2(STR)** and outstanding flange thickness **T3(STR)**

T-ring web height **H(RNG)** and outstanding flange width **W(RNG)**

T-ring web thickness **T4(RNG)** and outstanding flange thickness **T5(RNG)**

OBJECTIVE =
MINIMUM WEIGHT

Global optimization: PANDA2

□ WEIGHT OF THE ENTIRE PANEL: 180 degrees of the circumference of the cylindrical shell

"Global" optimization of the perfect shell, Case 1 of Table 4

Objective,
weight

Each "spike" is a new
"starting" design,
obtained randomly.

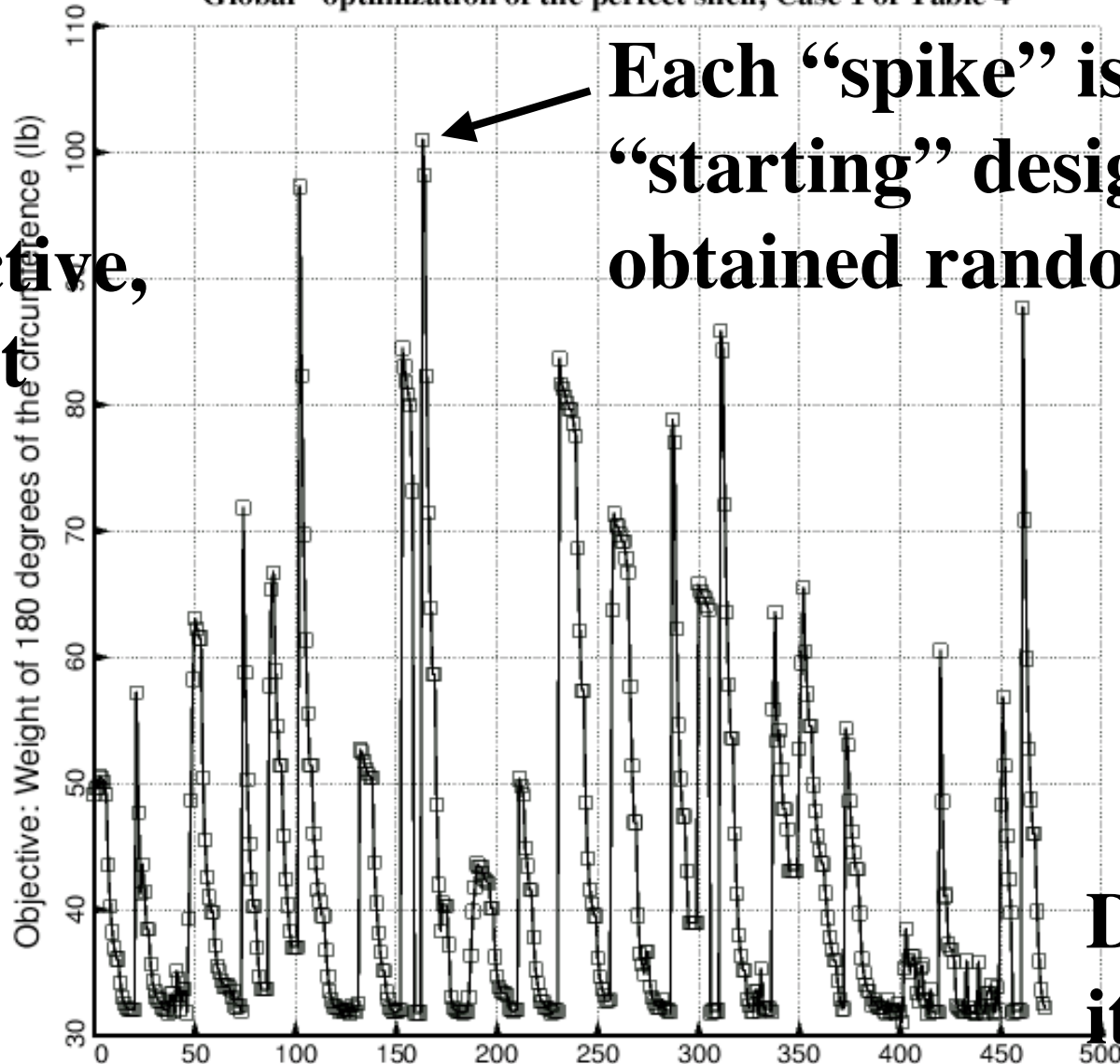


FIG. 3 Design iterations during the first SUPEROPT: Case 1, Table 4

CONSTRAINT CONDITIONS

Five classes of constraint conditions:

1. Upper and lower bounds of decision variables
2. Linking conditions
3. Inequality constraints
4. Stress constraints
5. Buckling constraints

DEFINITIONS OF MARGINS

Buckling margin= (buckling constraint) -1

(buckling constraint) =

(buckling load factor)/(factor of safety)

Stress margin = (stress constraint) - 1.0

(stress constraint) = (allowable stress)/

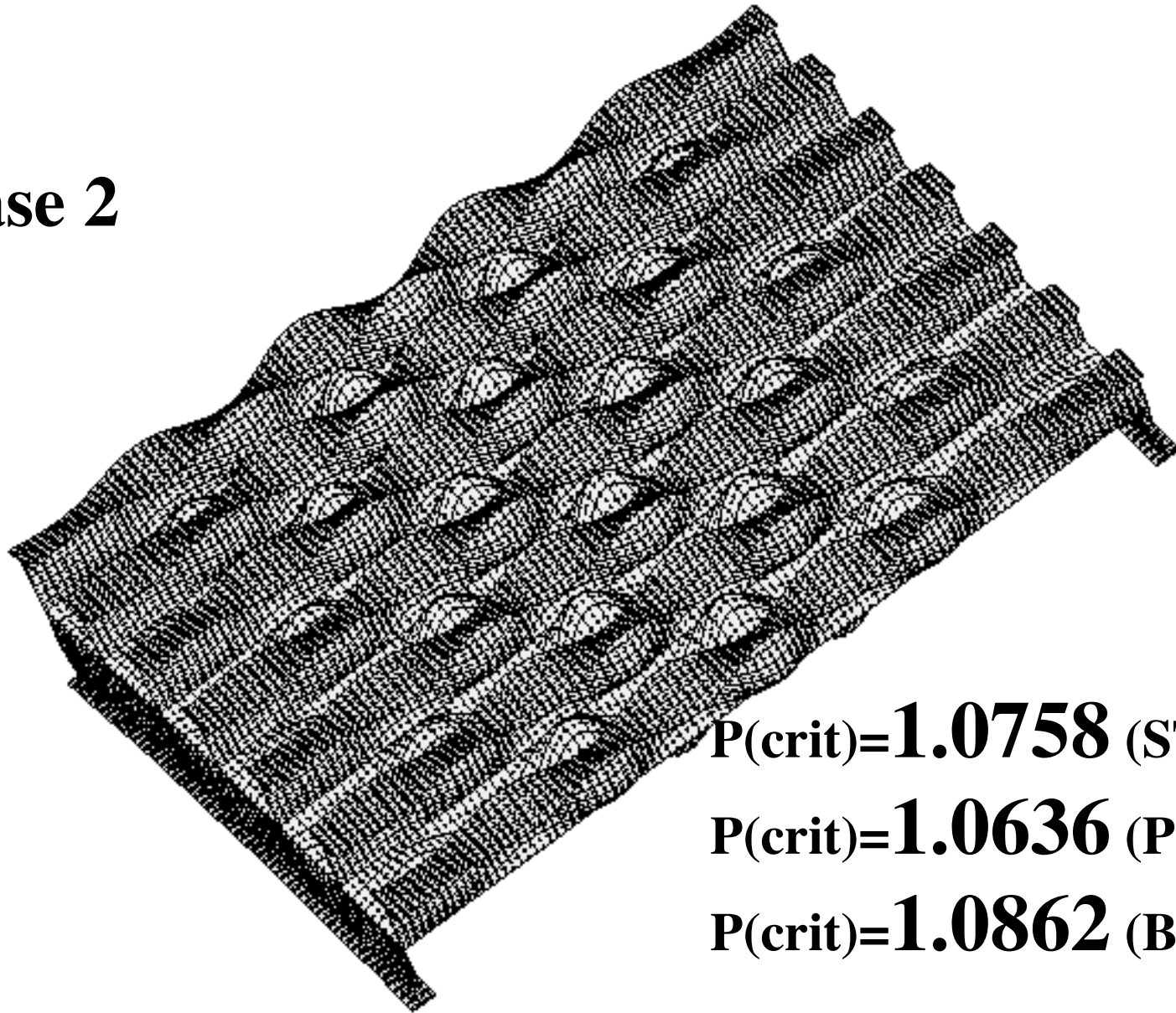
[(actual stress)x(factor of safety)]

TYPICAL BUCKLING MARGINS

- 1. Local buckling from discrete model**
- 2. Long-axial-wave bending-torsion buckling**
- 3. Inter-ring buckling from discrete model**
- 4. Buckling margin, stringer segment 3**
- 5. Buckling margin, stringer segment 4**
- 6. Buckling margin, stringer segments 3 & 4 together**
- 7. Same as 4, 5, and 6 for ring segments**
- 8. General buckling from PANDA-type model**
- 9. General buckling from double trig. series expansion**
- 10. Rolling only of stringers; of rings**

Example of local buckling: STAGS

Case 2

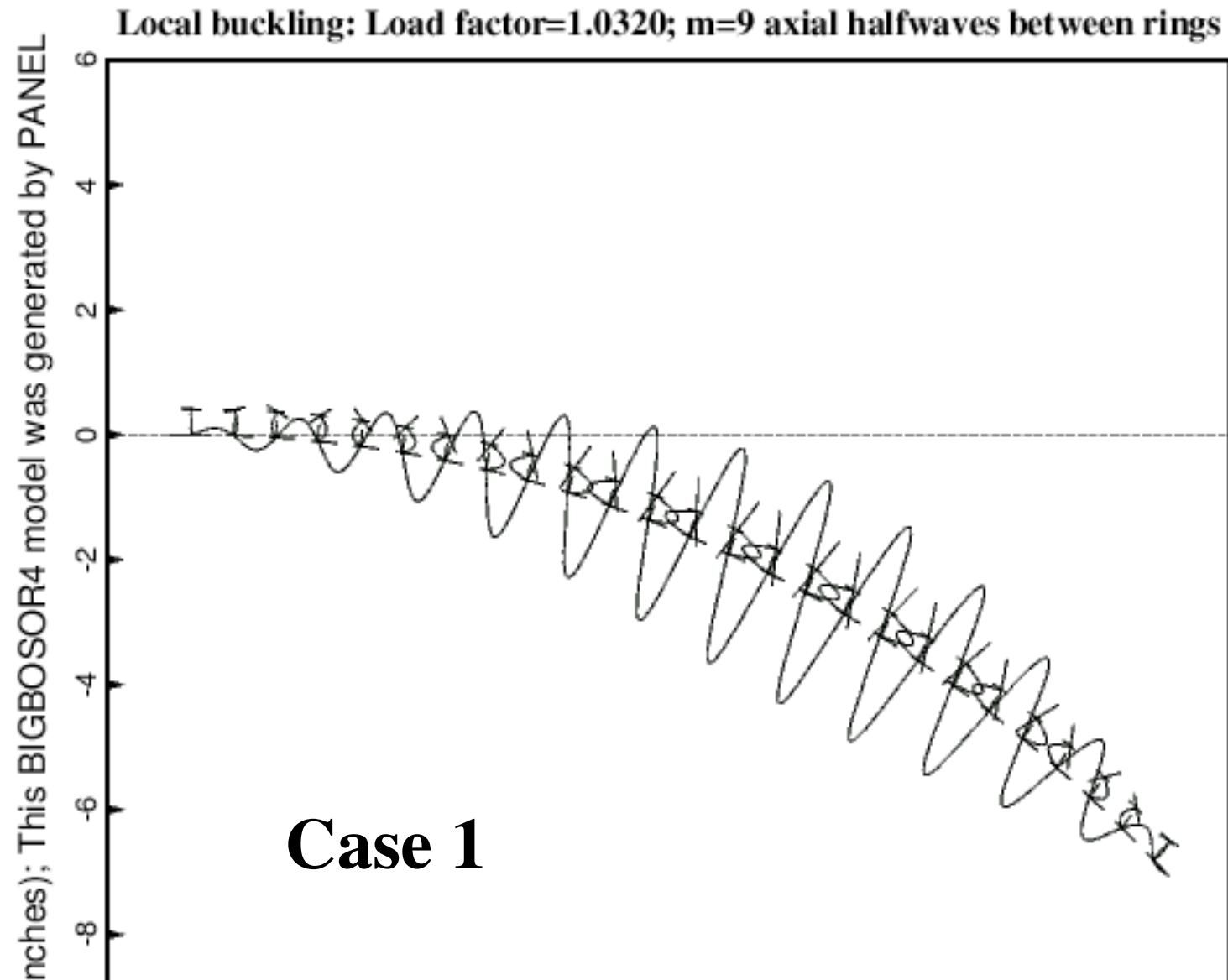


$P(\text{crit})=1.0758$ (STAGS)

$P(\text{crit})=1.0636$ (PANDA2)

$P(\text{crit})=1.0862$ (BOSOR4)

Example of local buckling: BIGBOSOR4

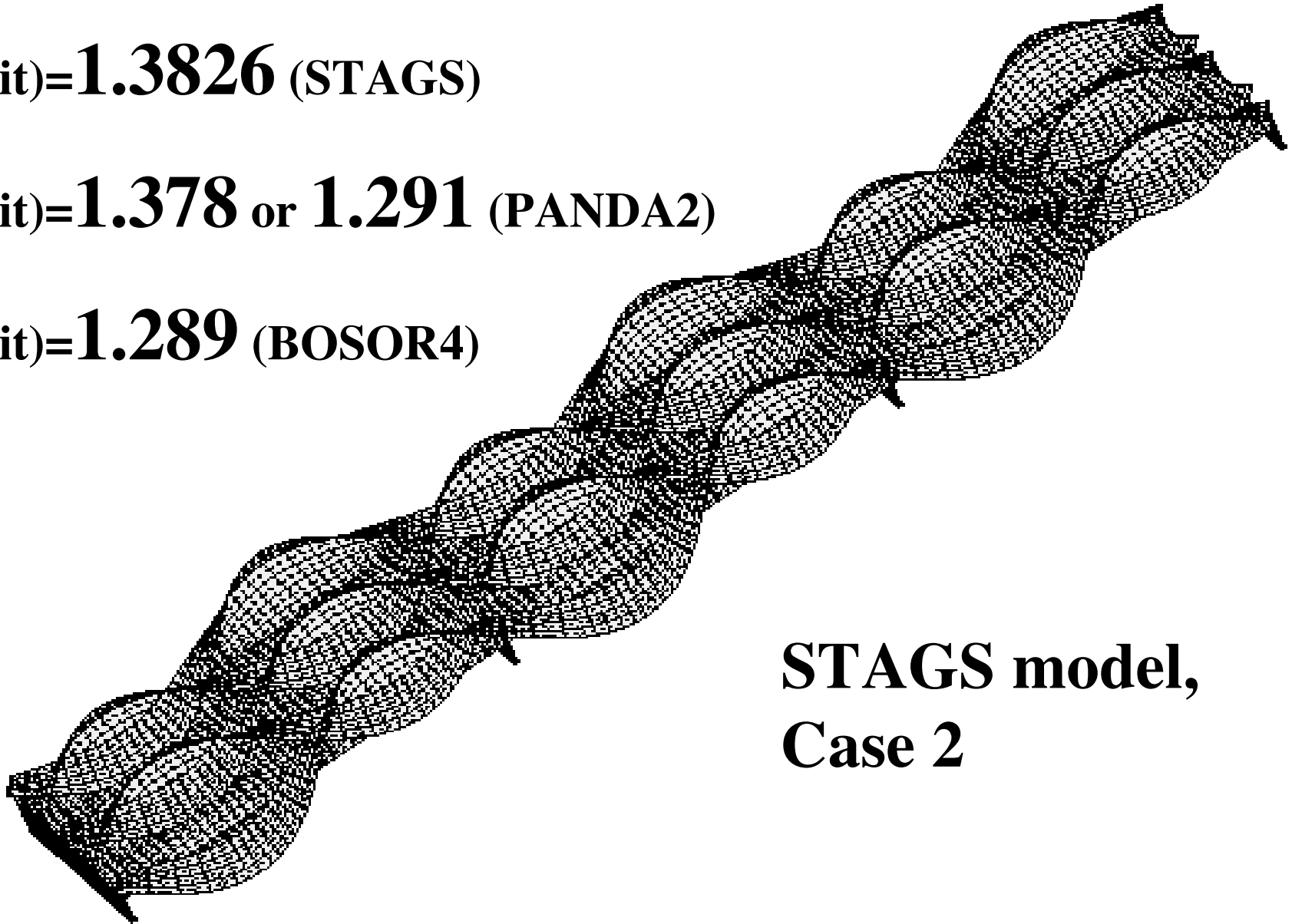


Example of bending-torsion buckling

$P(\text{crit})=1.3826$ (STAGS)

$P(\text{crit})=1.378$ or 1.291 (PANDA2)

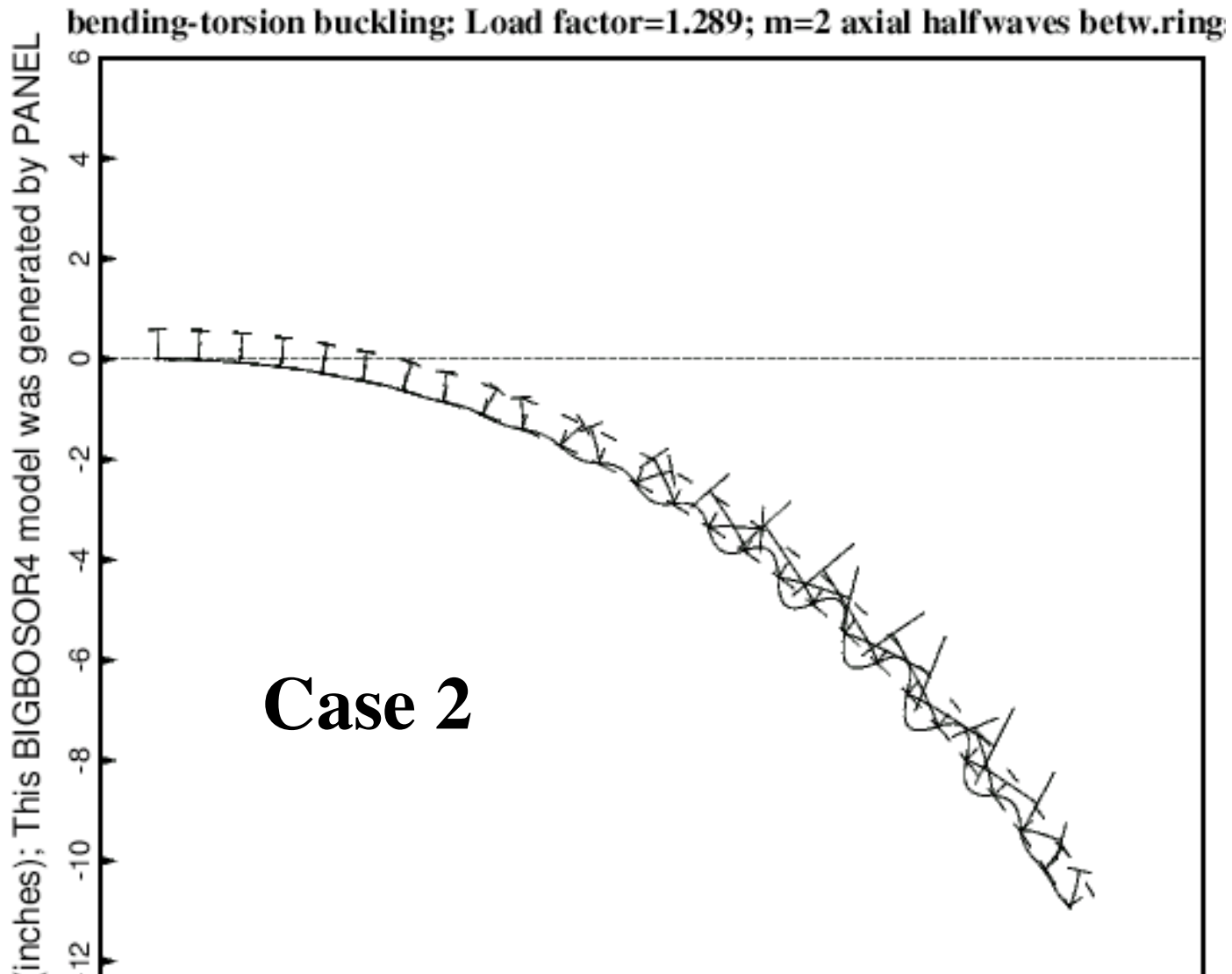
$P(\text{crit})=1.289$ (BOSOR4)



**STAGS model,
Case 2**

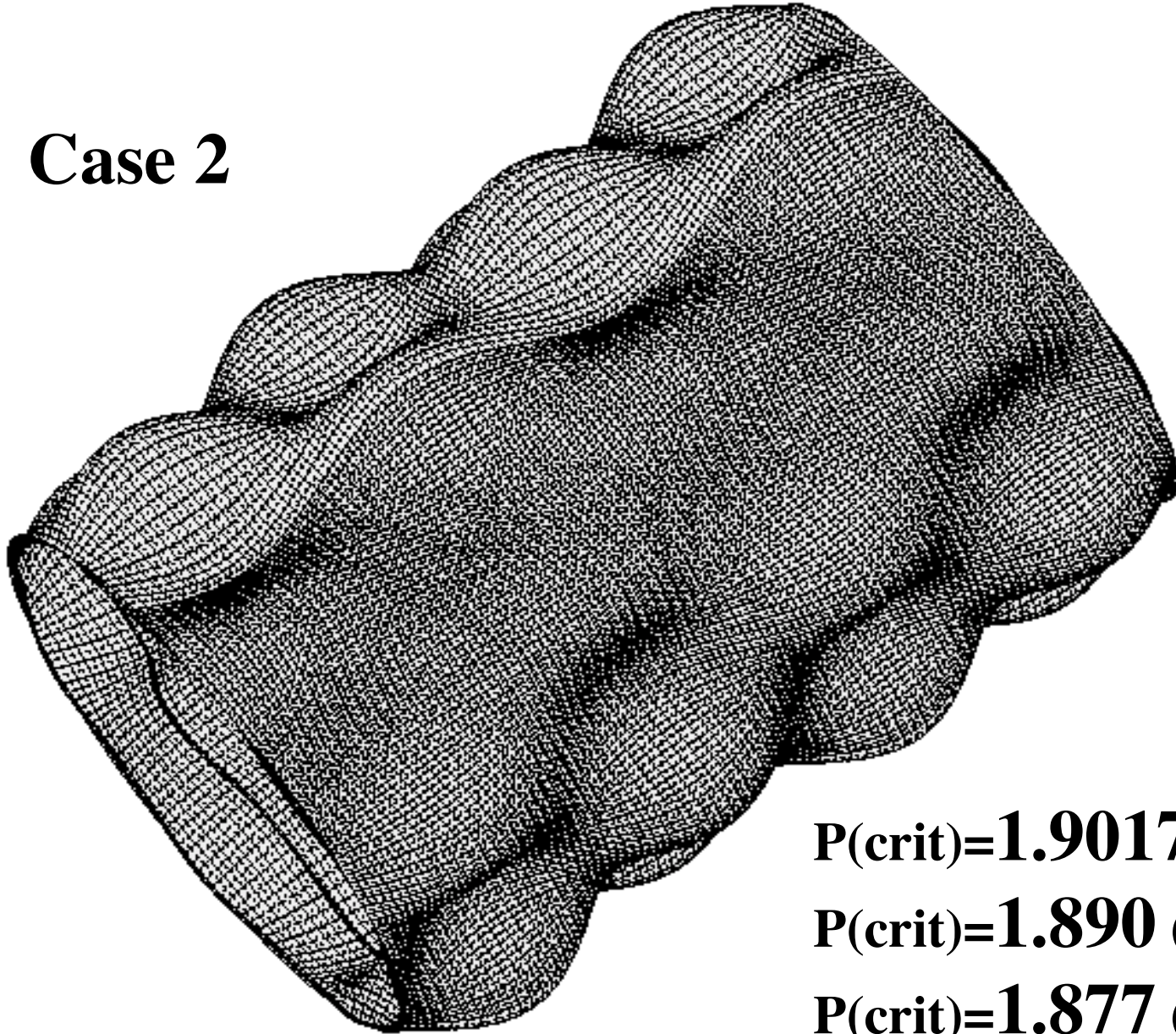
Bending-torsion buckling: BIGBOSOR4

- Undeformed: An arc of the stiffened cylindrical shell is modeled as a huge torus [26].
- Deformed: bending-torsion buckling; PANDA2 gets 1.291 in subcase 2; This is Case 2 in Table 4



Example of general buckling: STAGS

Case 2



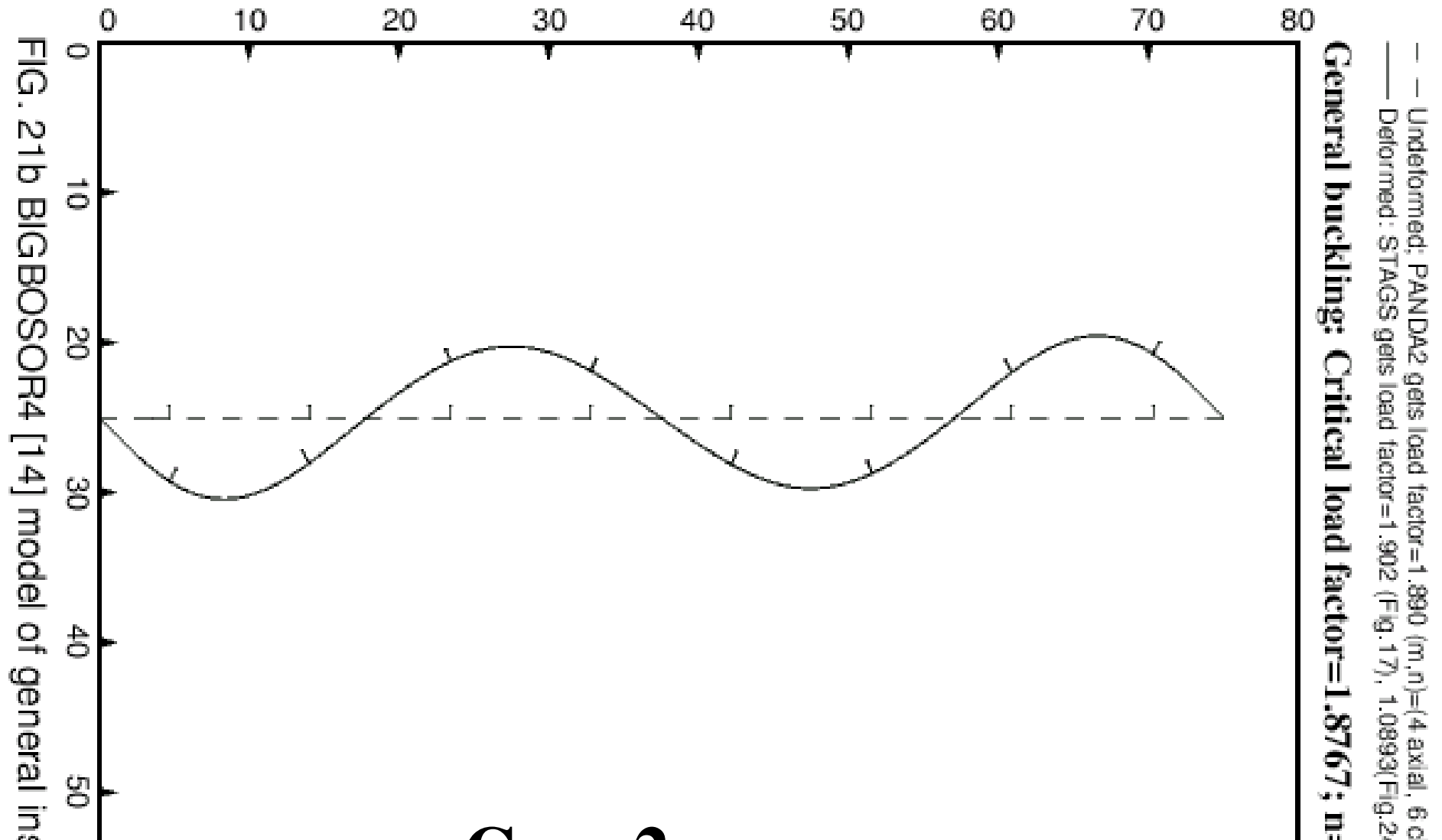
$P(\text{crit})=1.9017$ (STAGS)

$P(\text{crit})=1.890$ (PANDA2)

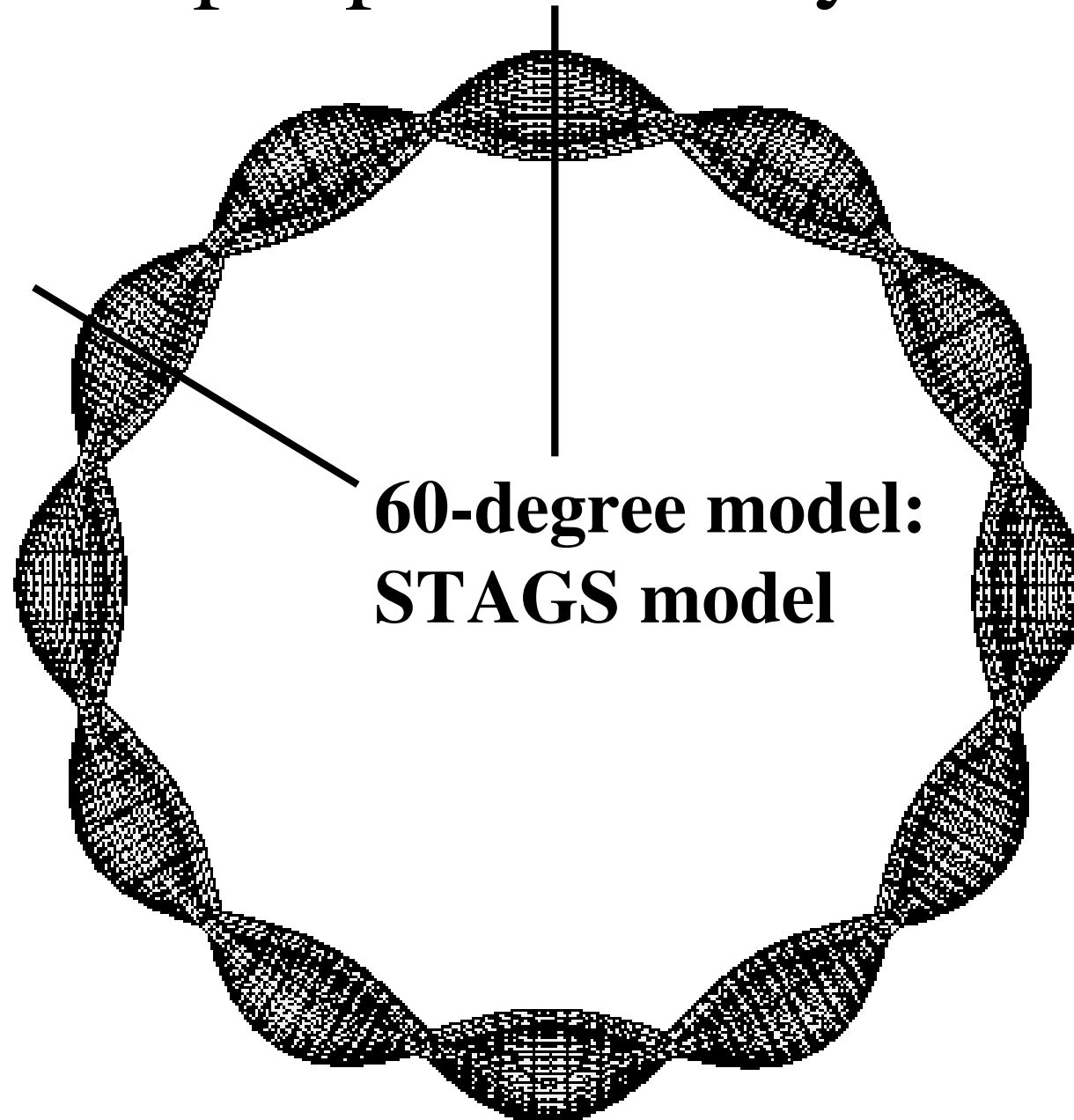
$P(\text{crit})=1.877$ (BOSOR4)

Example of general buckling: BIGBOSOR4

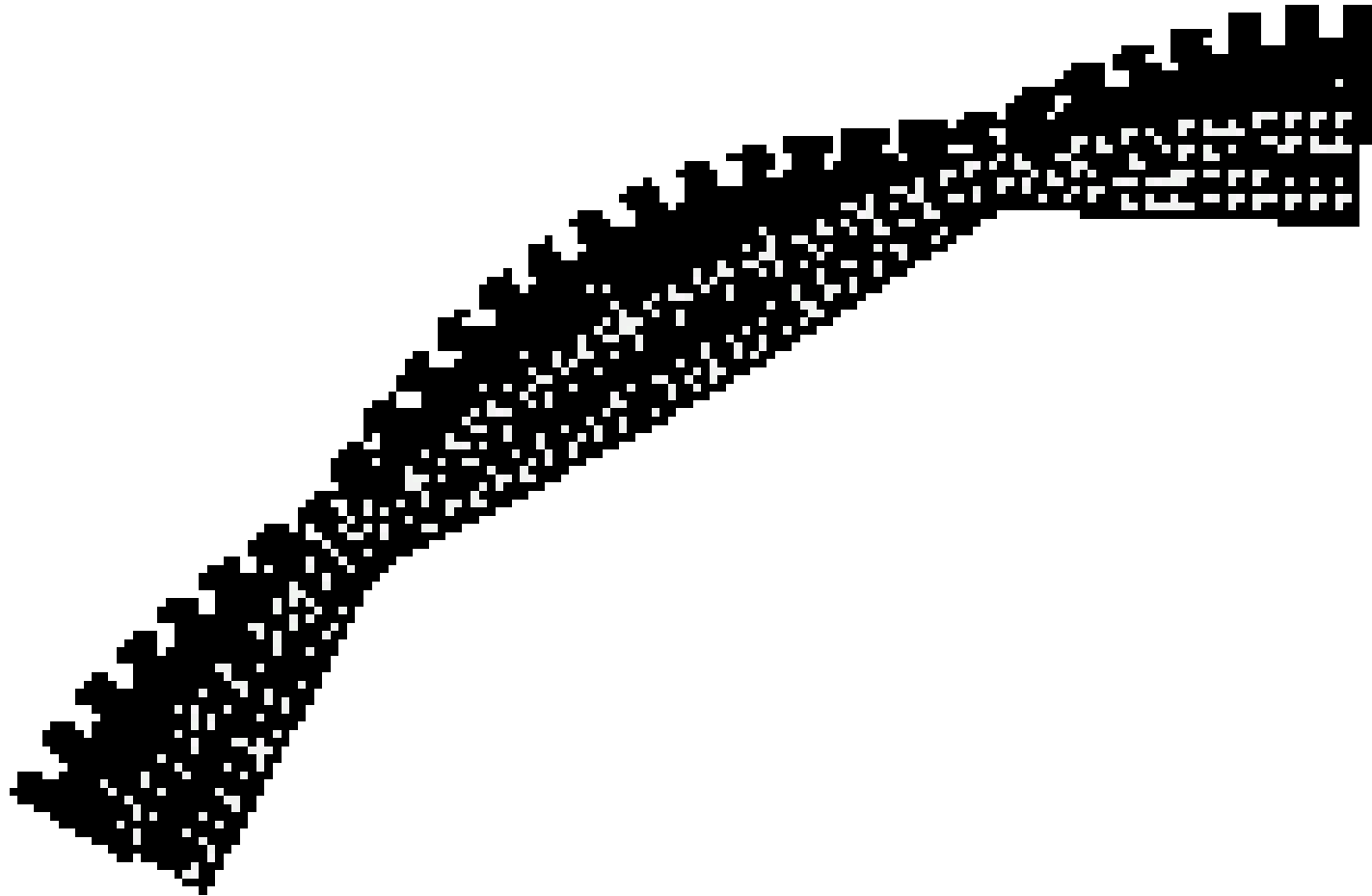
Axial Station (inches); This BIGBOSOR4 model was generated by PANEL2



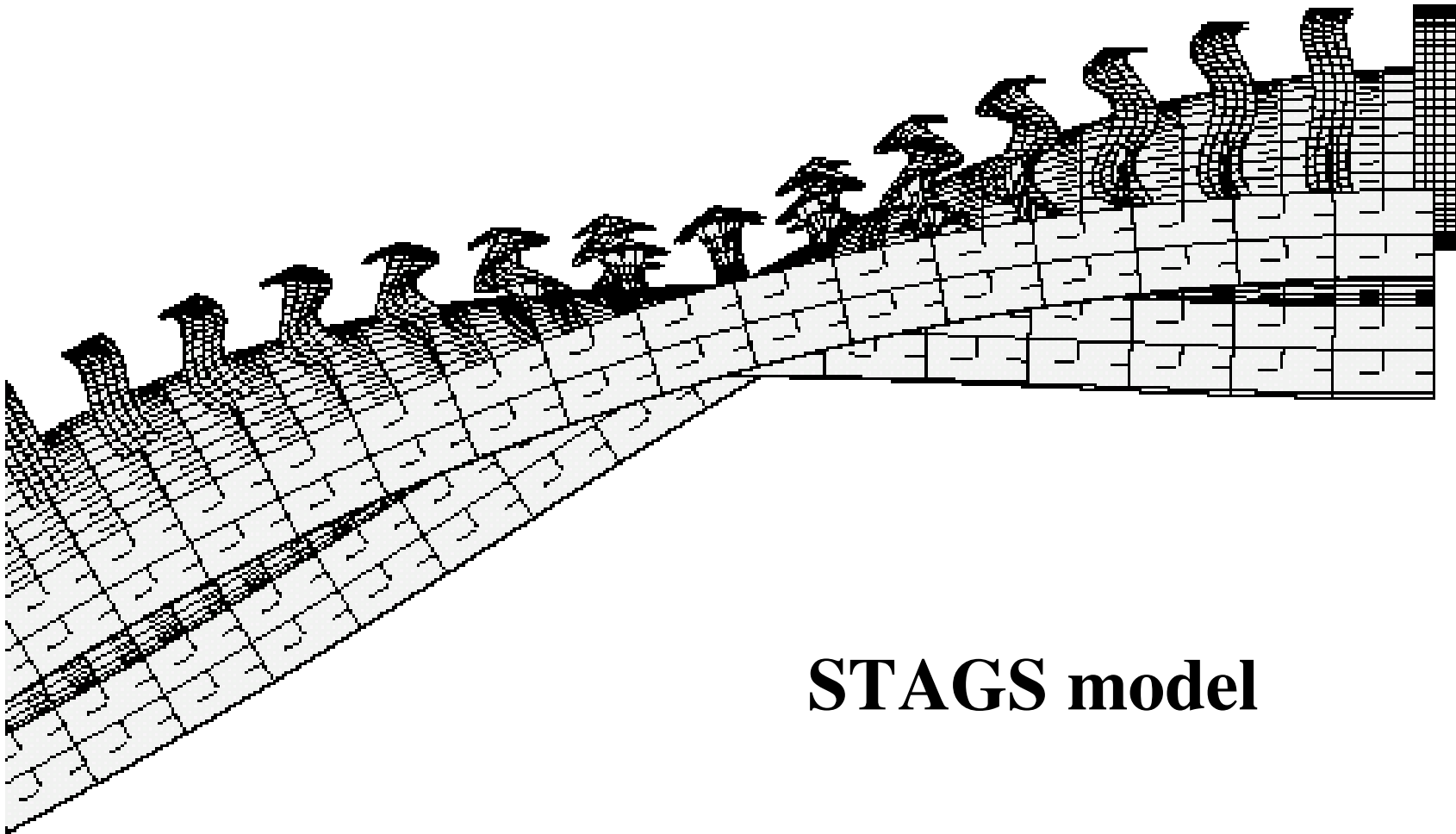
Multiple planes of symmetry



60-degree STAGS model: End view



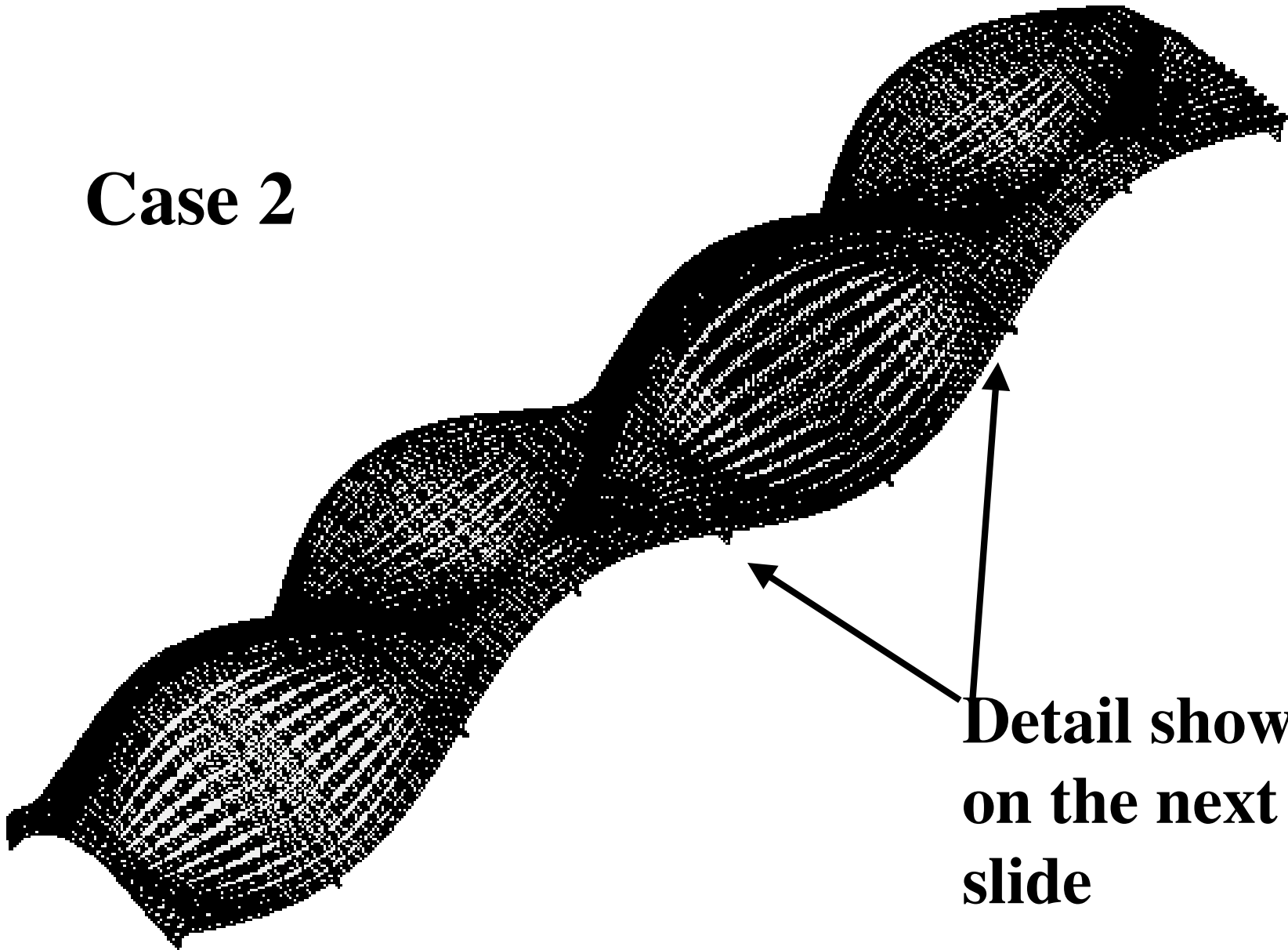
Close-up view of part of 60-deg. model



STAGS model

60-degree STAGS model

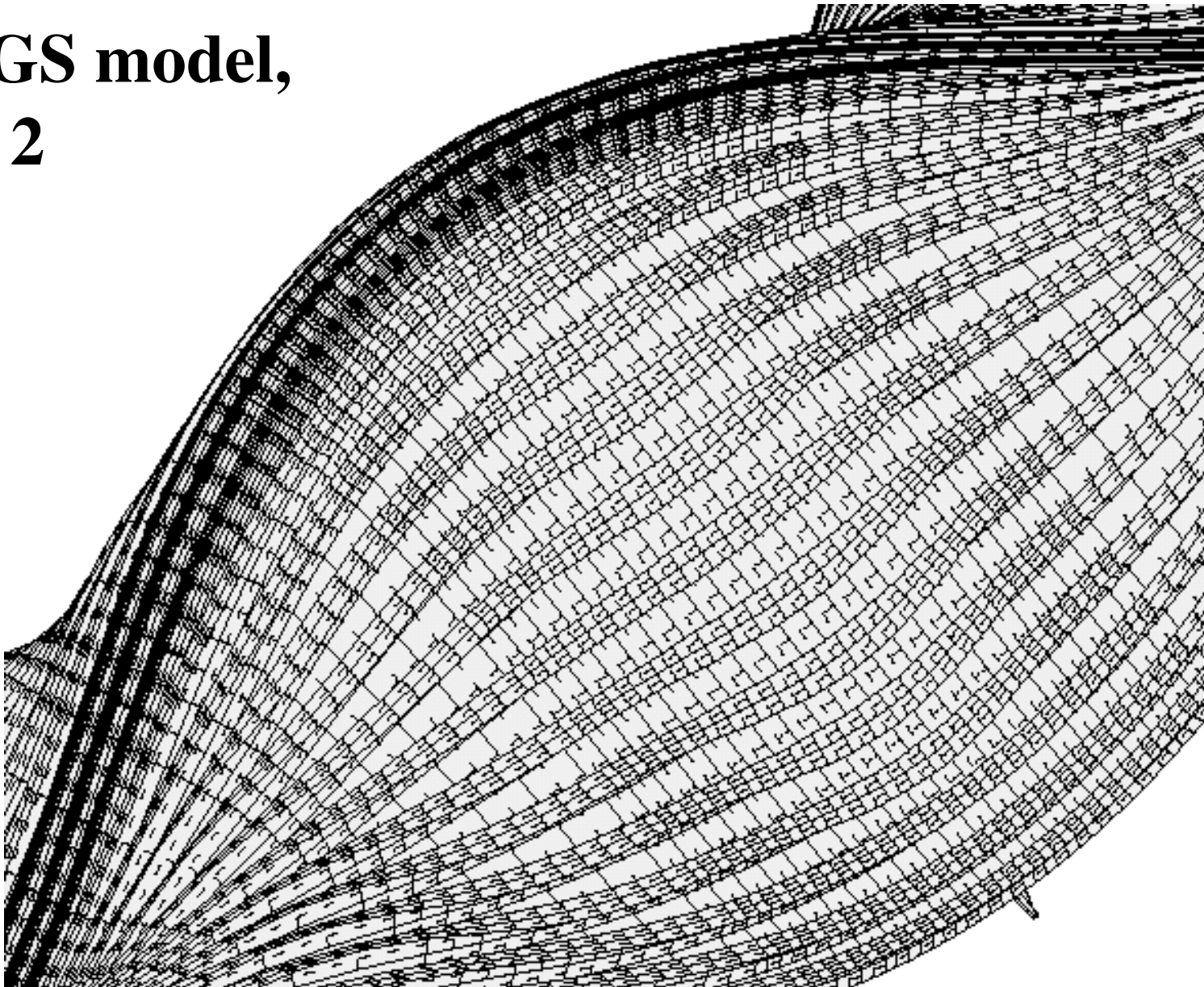
Case 2



**Detail shown
on the next
slide**

Detail of general buckling mode

**STAGS model,
Case 2**



TYPICAL STRESS MARGINS

1. Effective stress, material x, location y,
computed from SUBROUTINE
**STRTHK (locally post-buckled
skin/stringer discretized module)**
2. Effective stress, material x, location y,
computed from SUBROUTINE
**STRCON (No local buckling. Stresses
in rings are computed)**

Buckling and stress margins in PANDA2 design sensitivity study

↑
**Design
margins**

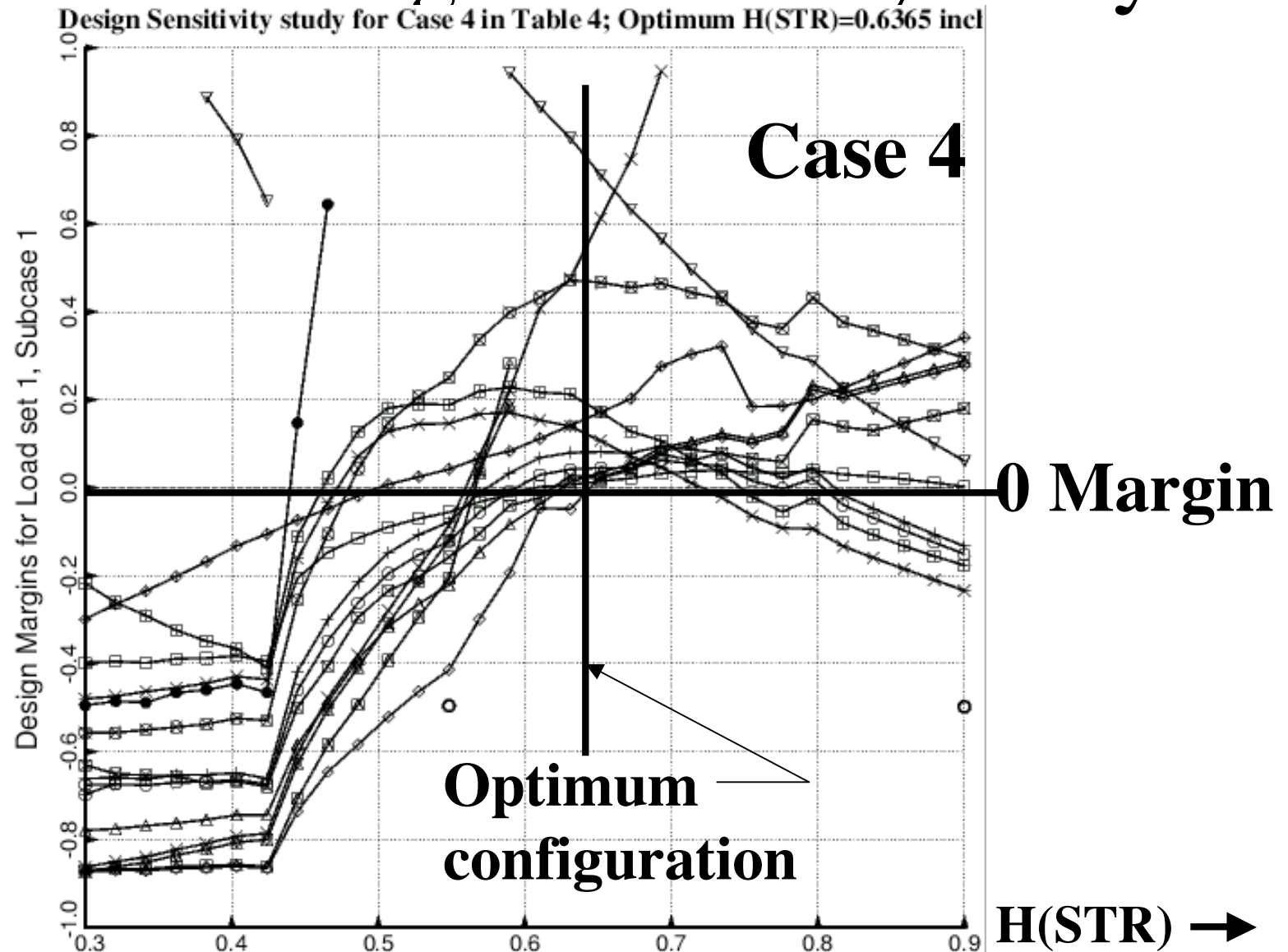


FIG. 44 PANDA2 design sensitivity study: Design Parameter, $H(\text{STR})$, inches

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THE MEANING OF “ICONSV”

ICONSV = 1 (the recommended value):

- 1. Include the Arbocz theory for imperfection sensitivity.**
- 2. Use a conservative knockdown for smearing stringers.**
- 3. Use the computed knockdown factor for smearing rings.**

ICONSV = 0:

- 1. Do not include the Arbocz theory.**
- 2. Use a less conservative knockdown for smearing stringers.**
- 3. Use the computed knockdown factor for smearing rings.**

ICONSV = -1:

Same as ICONSV=0 except the knockdown factor for smearing rings is 1.0 and 0.95 is used instead of 0.85 for ALTSOL.

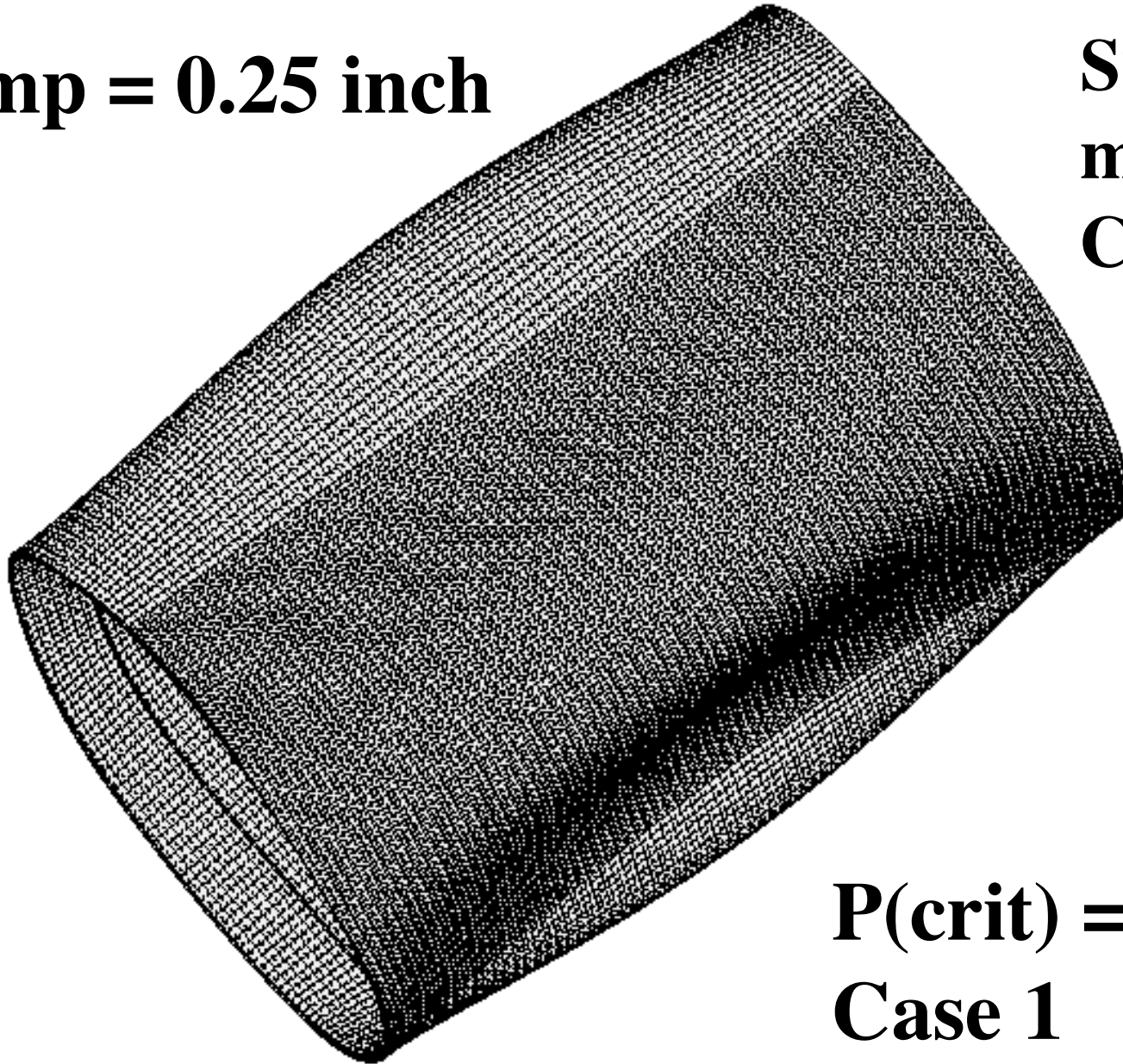
THE MEANING OF “YES CHANGE IMPERFECTION”

The general buckling modal
imperfection **amplitude** is made
**proportional to the axial
wavelength of the critical
general buckling mode shape.**

A simple general buckling modal imperfection

Wimp = 0.25 inch

**STAGS
model:
Case 1**

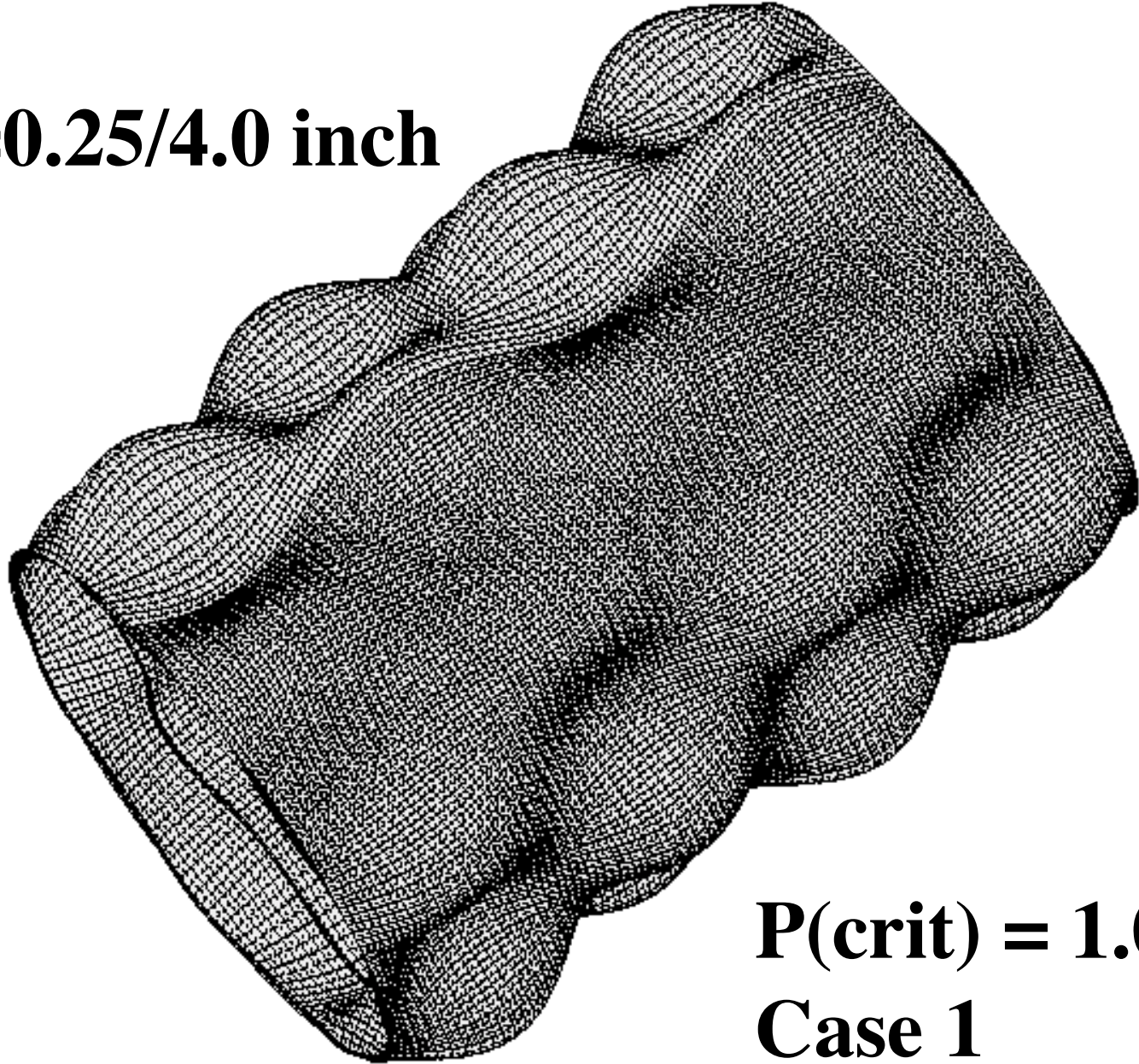


**$P(\text{crit}) = 1.090$,
Case 1**

A “complex” general buckling modal imperfection

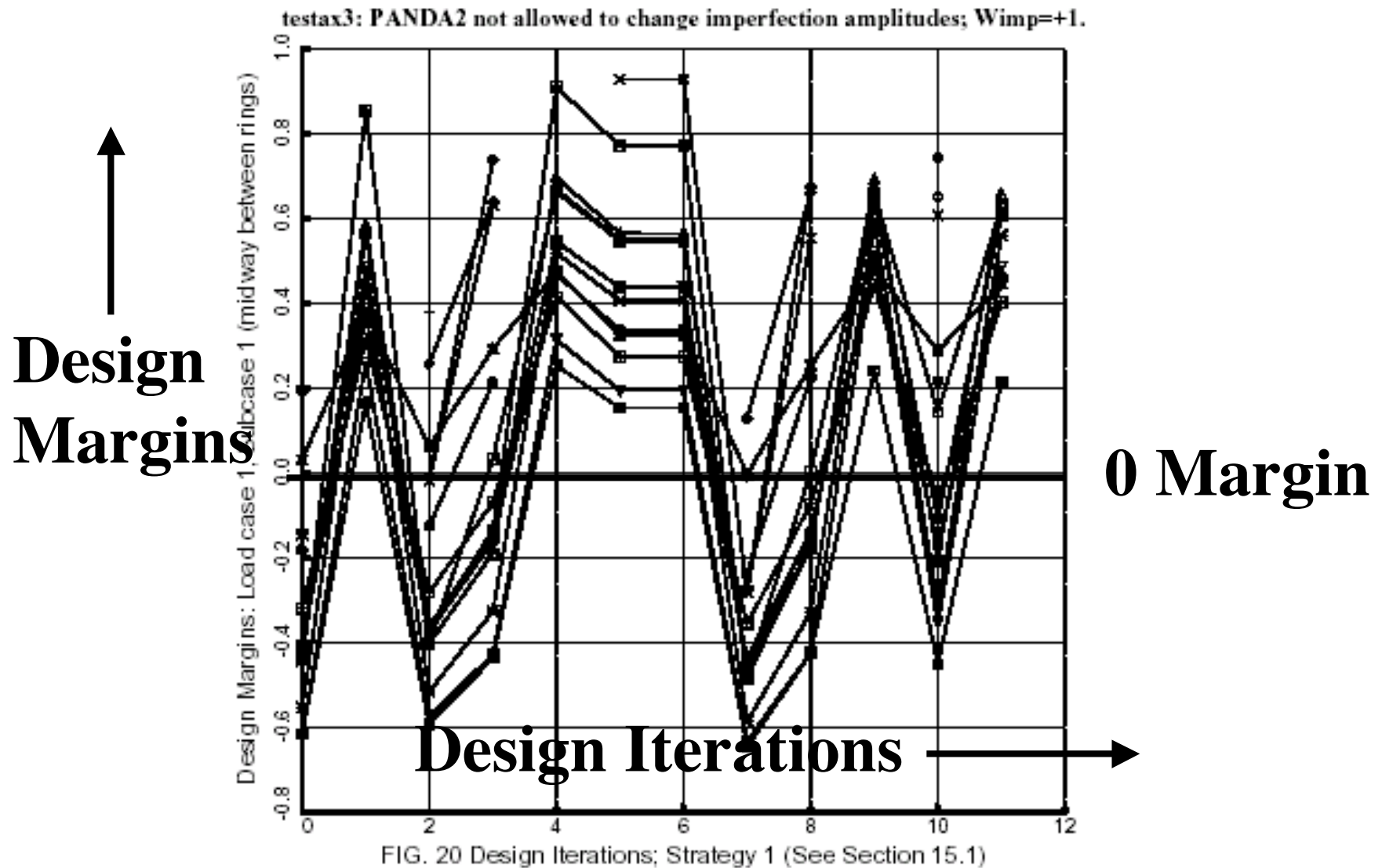
Wimp = 0.25/4.0 inch

Case 1

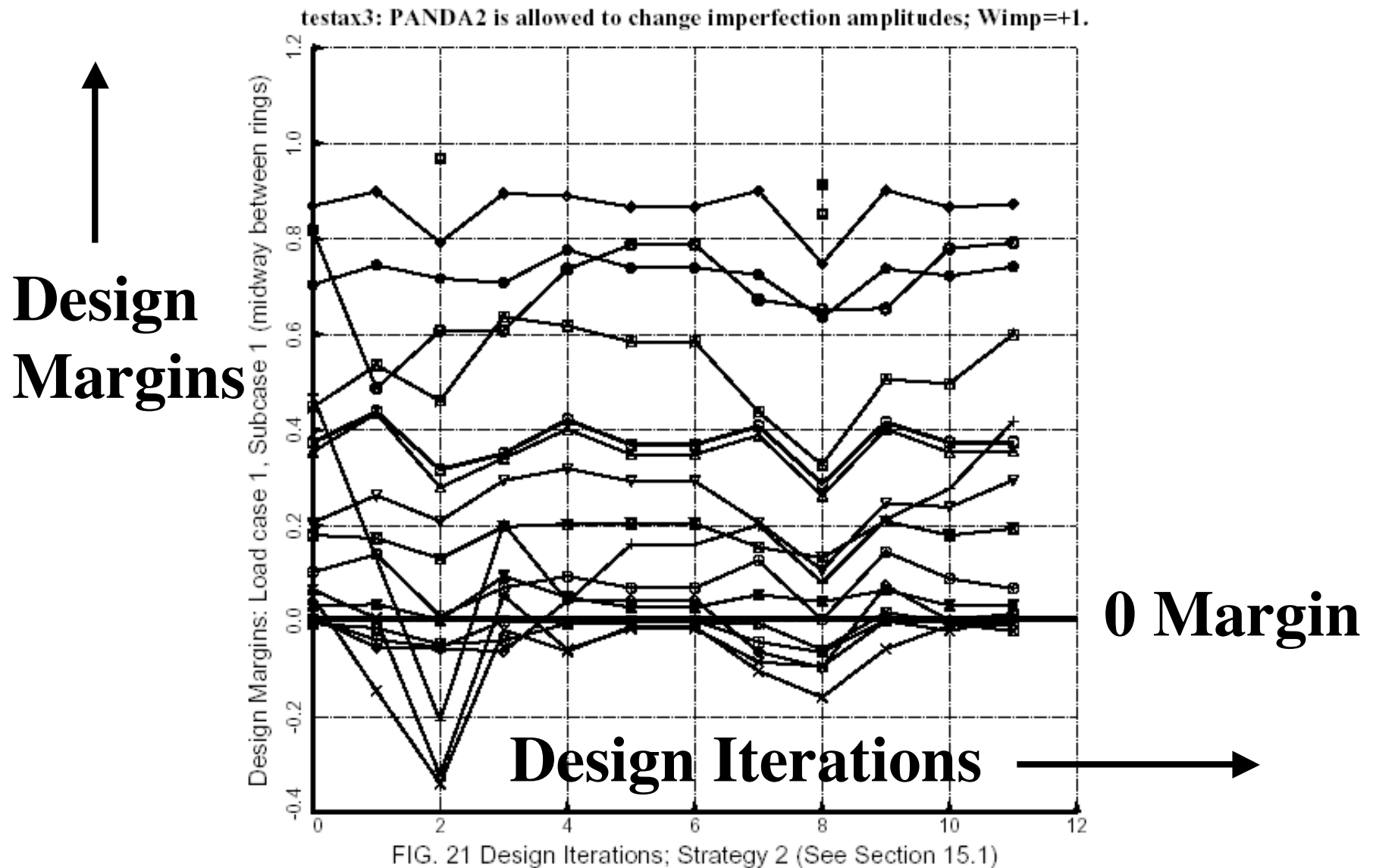


**$P(\text{crit}) = 1.075,$
Case 1**

“Oscillation” of margins with “no change imperfection” option



“Oscillation” of margins with “yes change imperfection” option



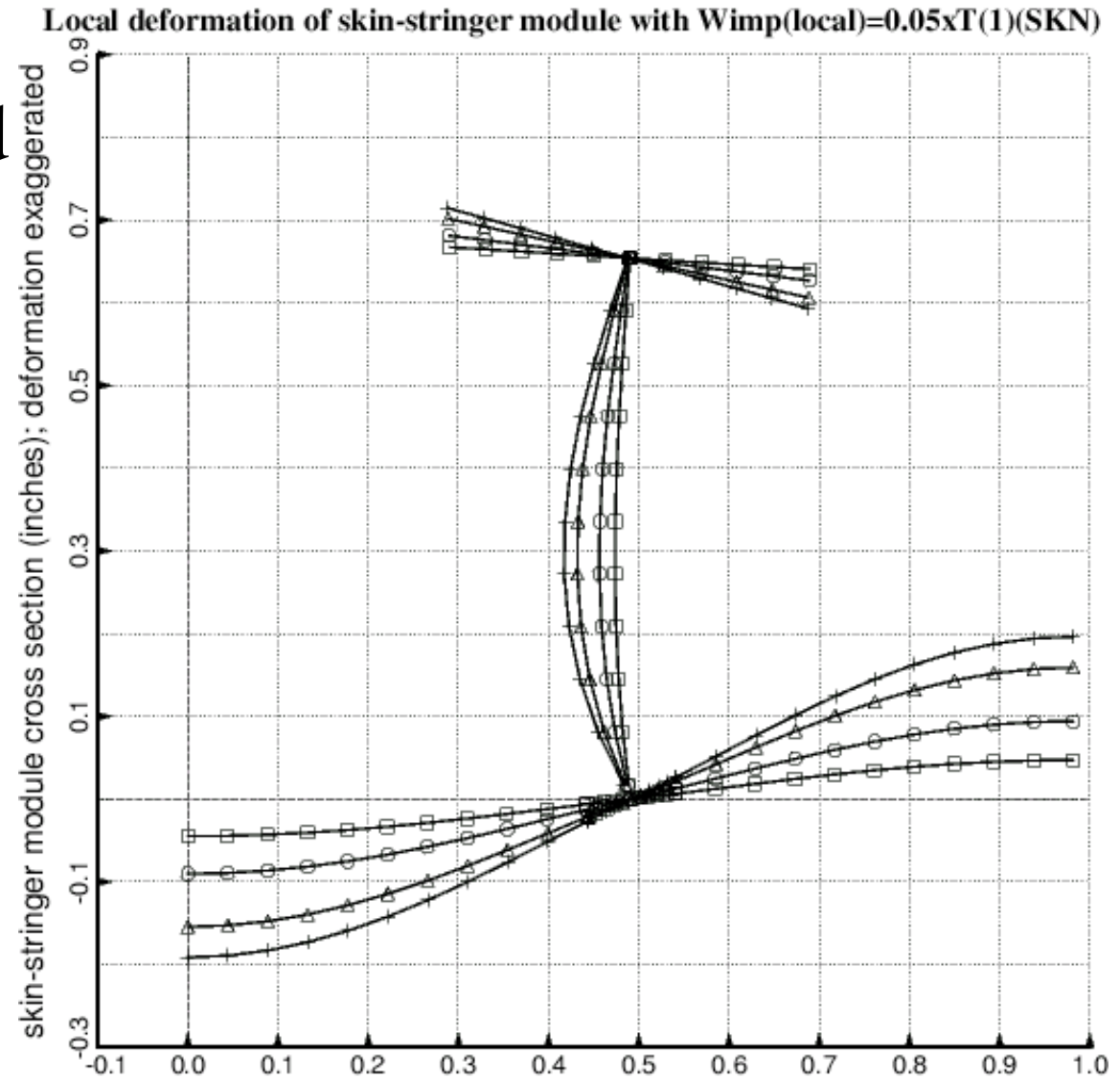
THE MEANING OF “NO” AND “YES KOITER”

“NO KOITER” = no local postbuckling state is computed.

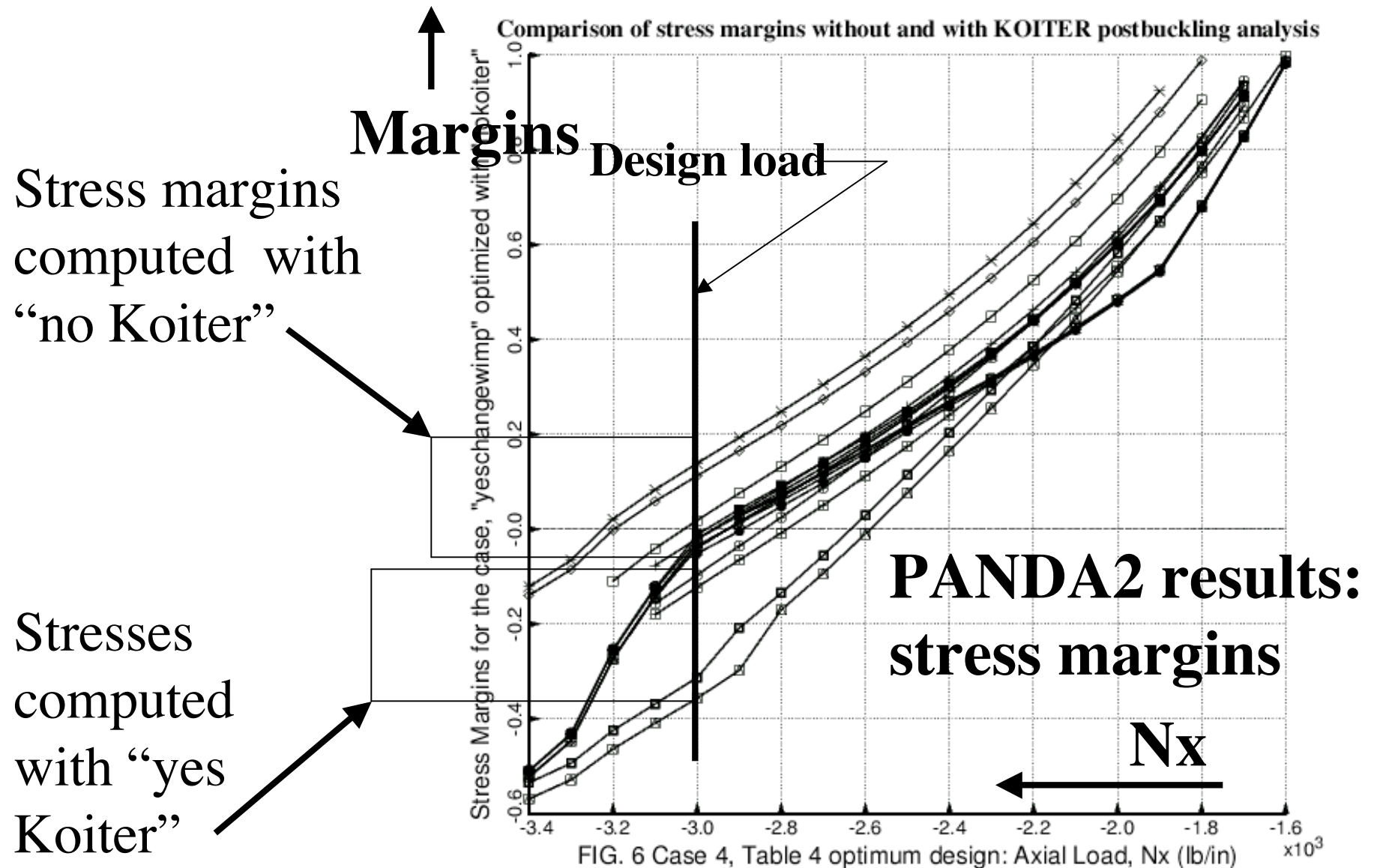
“YES KOITER” = the local postbuckling state is computed. A modified form of the nonlinear theory by KOITER (1946), BUSHNELL (1993) is used.

Local postbuckling: PANDA2

A single discretized skin-stringer module model (BOSOR4-type model) of the Case 4 optimum design as deformed at four levels of applied axial compression, N_x .

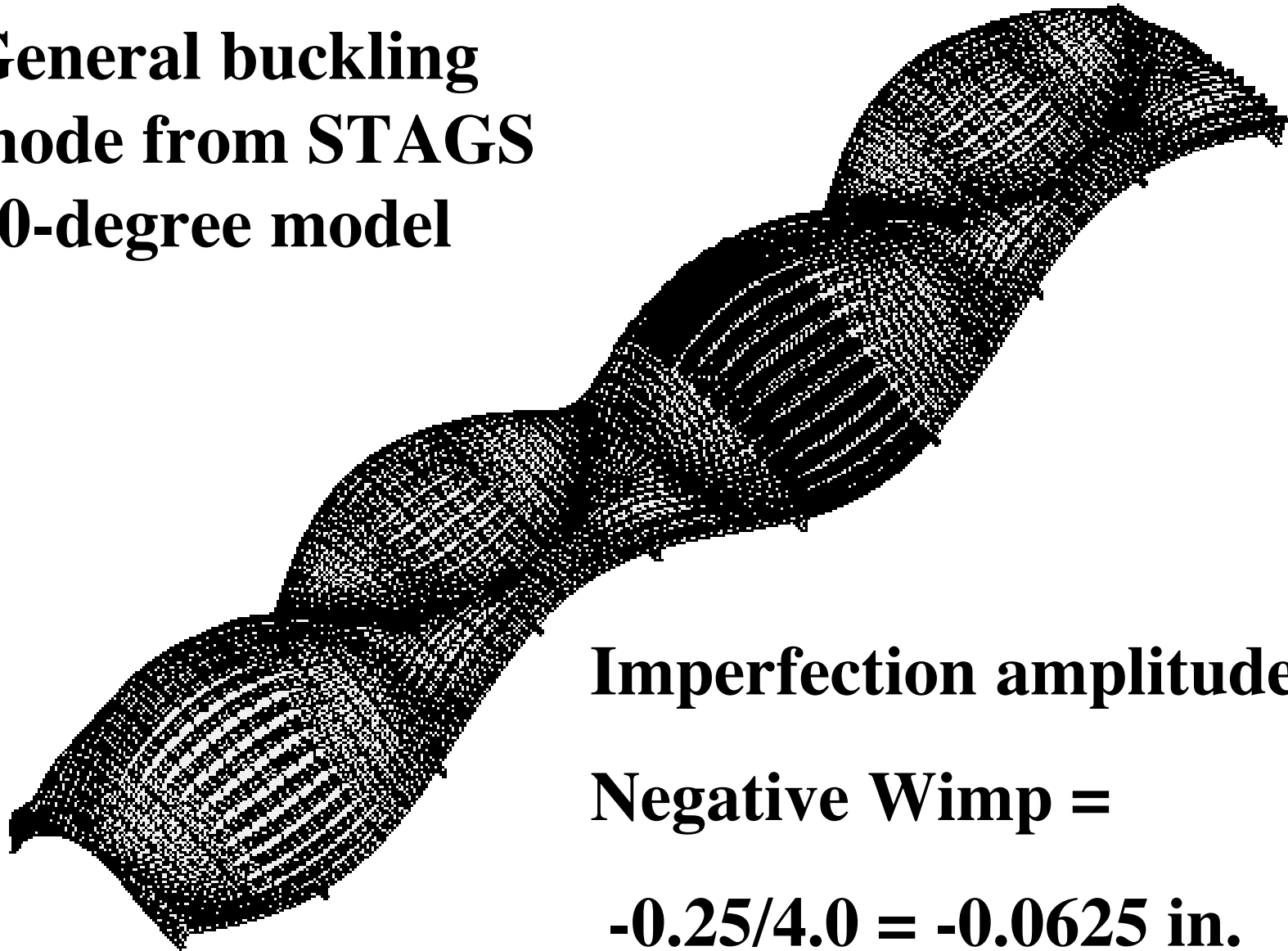


Case 4 with “no Koiter” and with “yes Koiter”



Case 4: Initial imperfection shape

**General buckling
mode from STAGS
60-degree model**



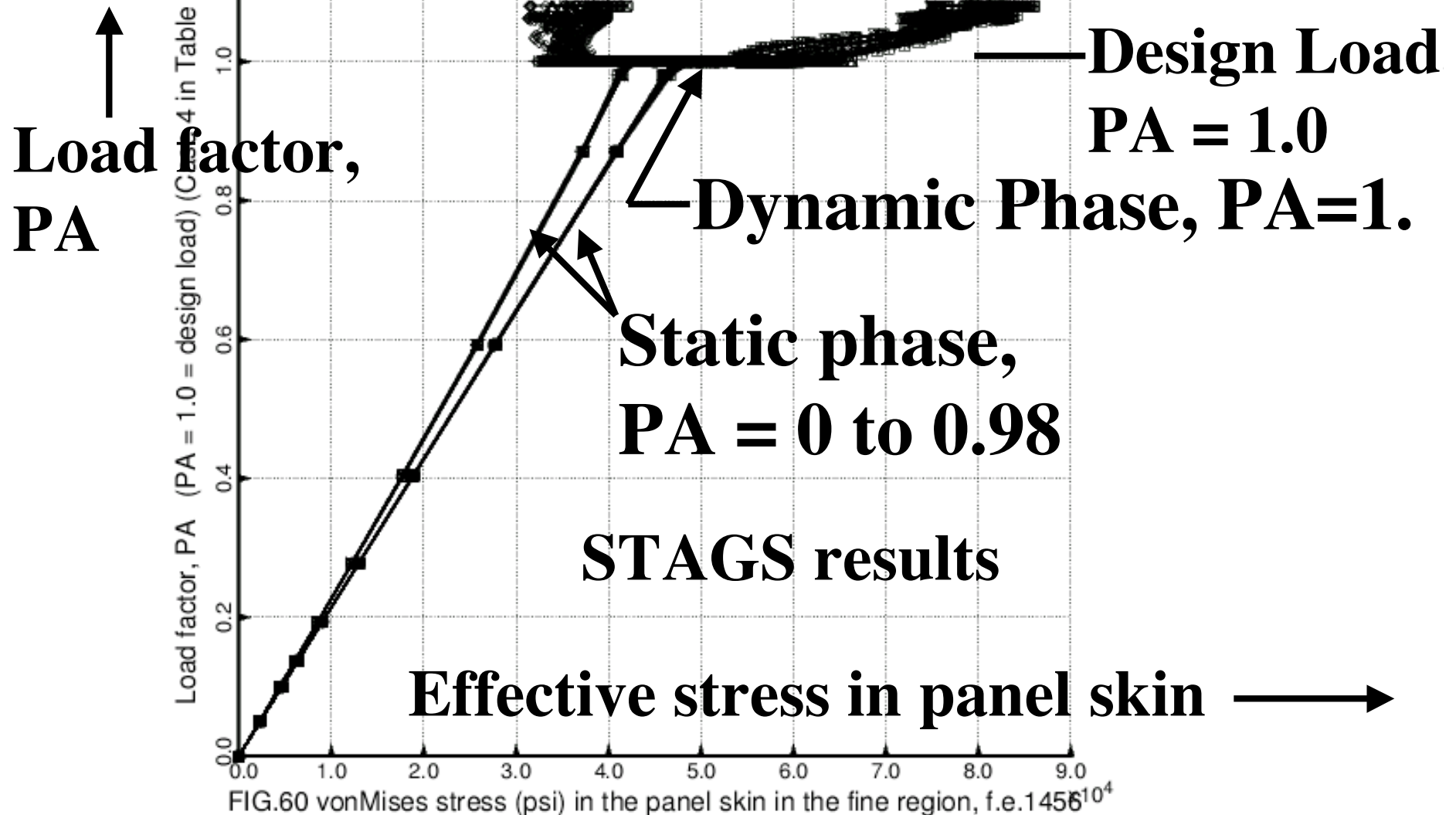
Imperfection amplitude,

Negative Wimp =

$$\mathbf{-0.25/4.0 = -0.0625\ in.}$$

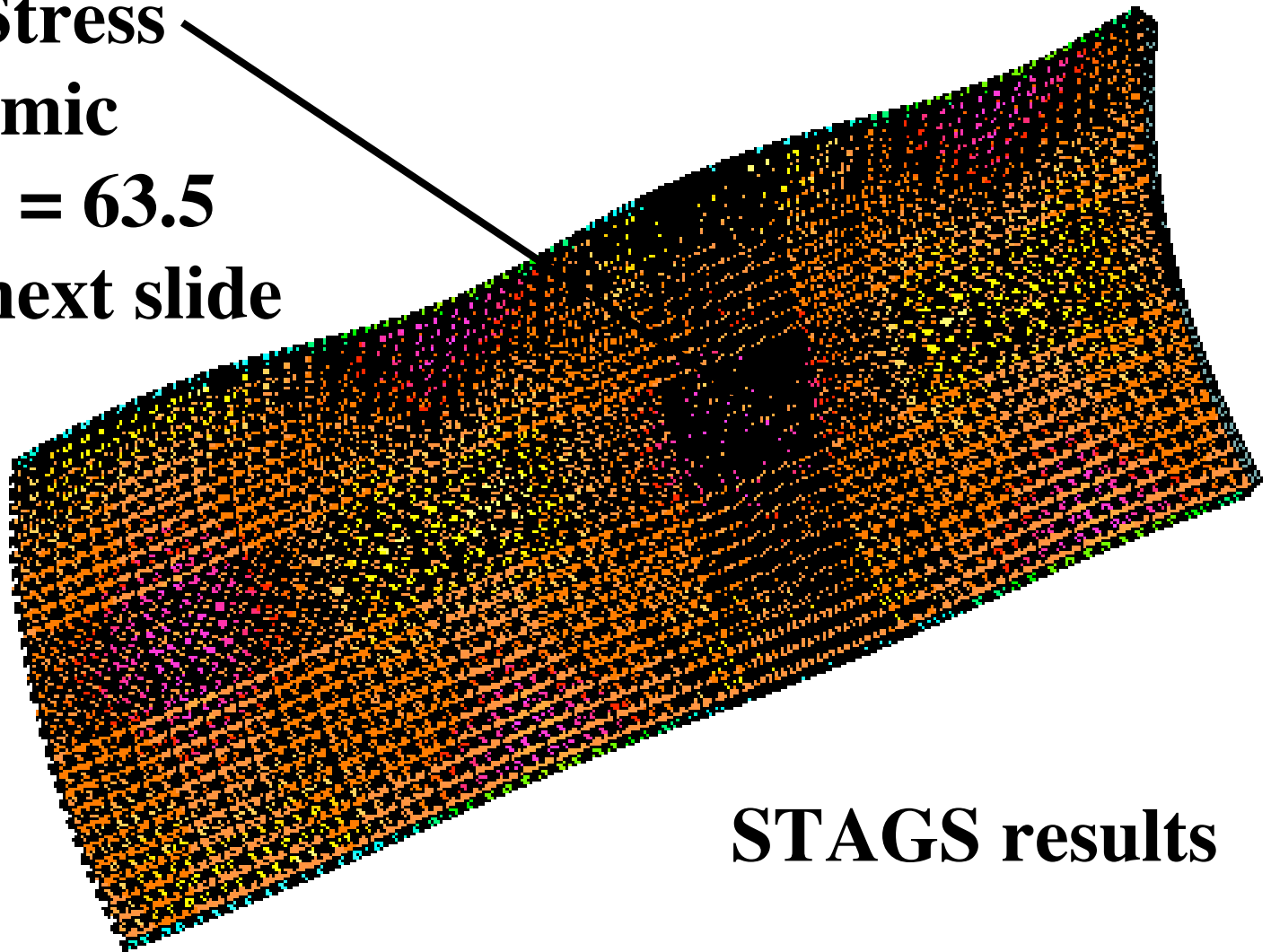
Load-stress curve: static & dynamic

f.e.1456 is in panel skin between stringers 12 & 13, 18 elements from the left of fine region



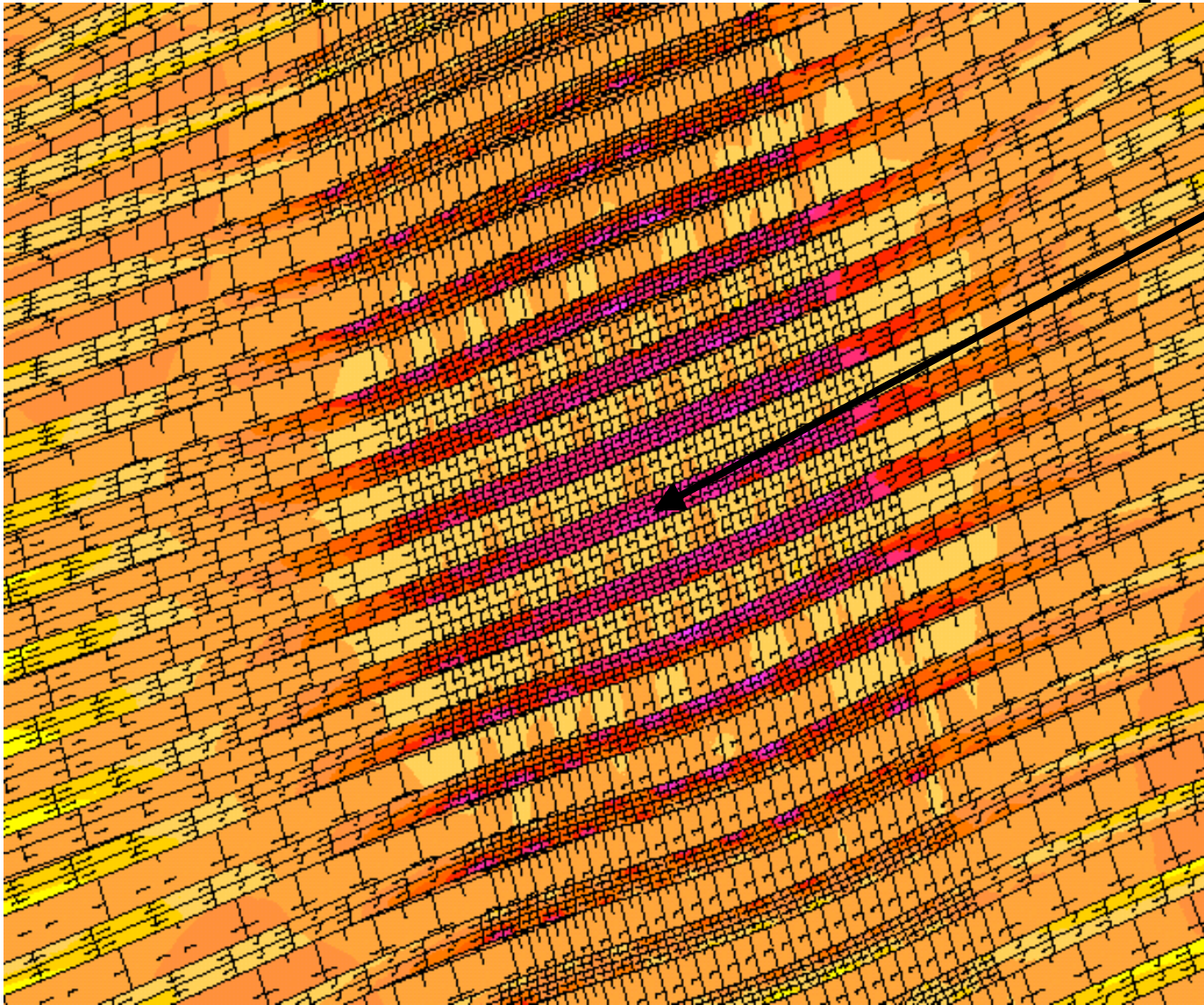
Deformed panel at $PA=0.98$

**Maximum Stress
before dynamic
STAGS run = 63.5
ksi See the next slide
for detail.**



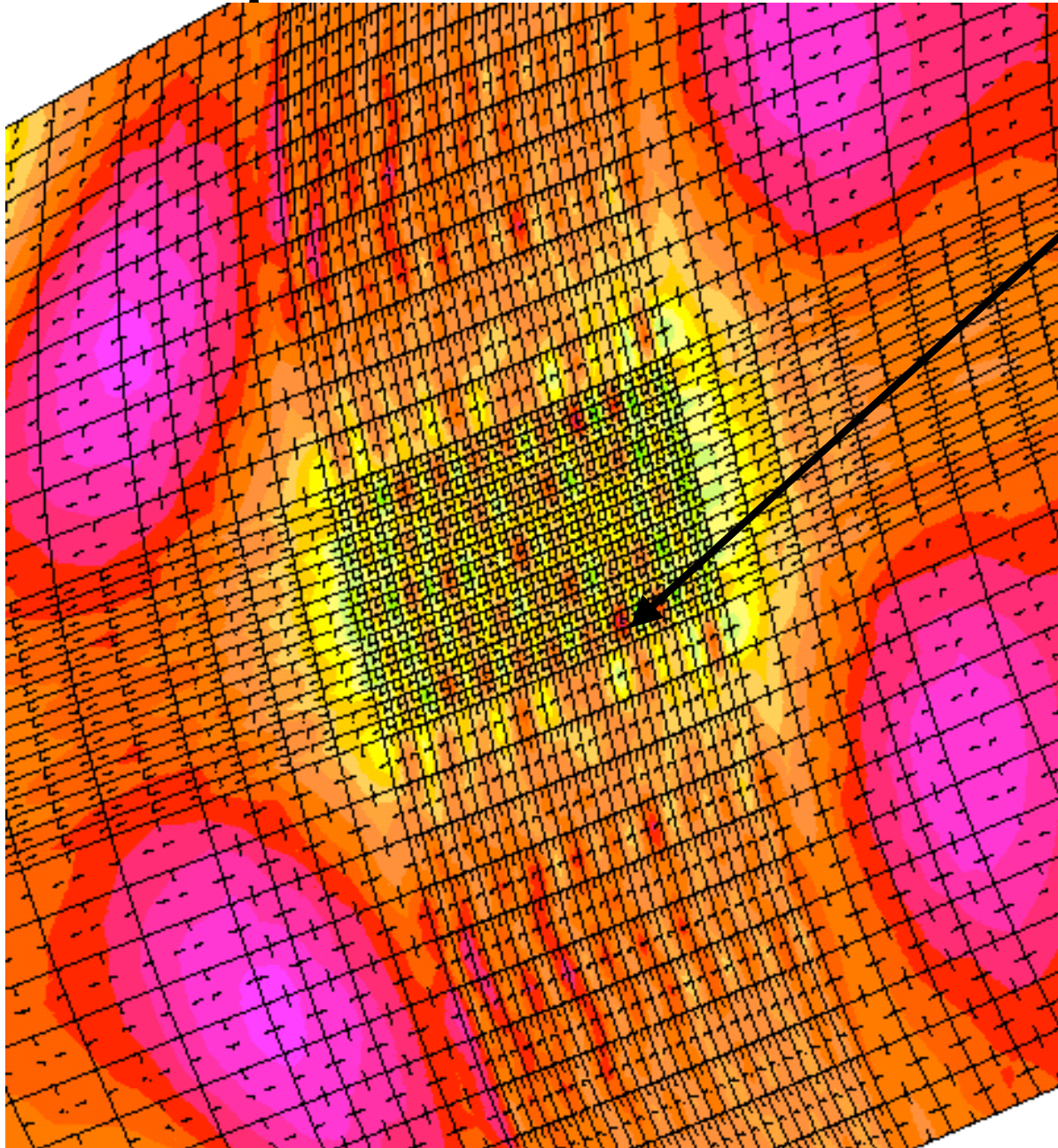
STAGS results

Example 1 of stress in the imperfect panel



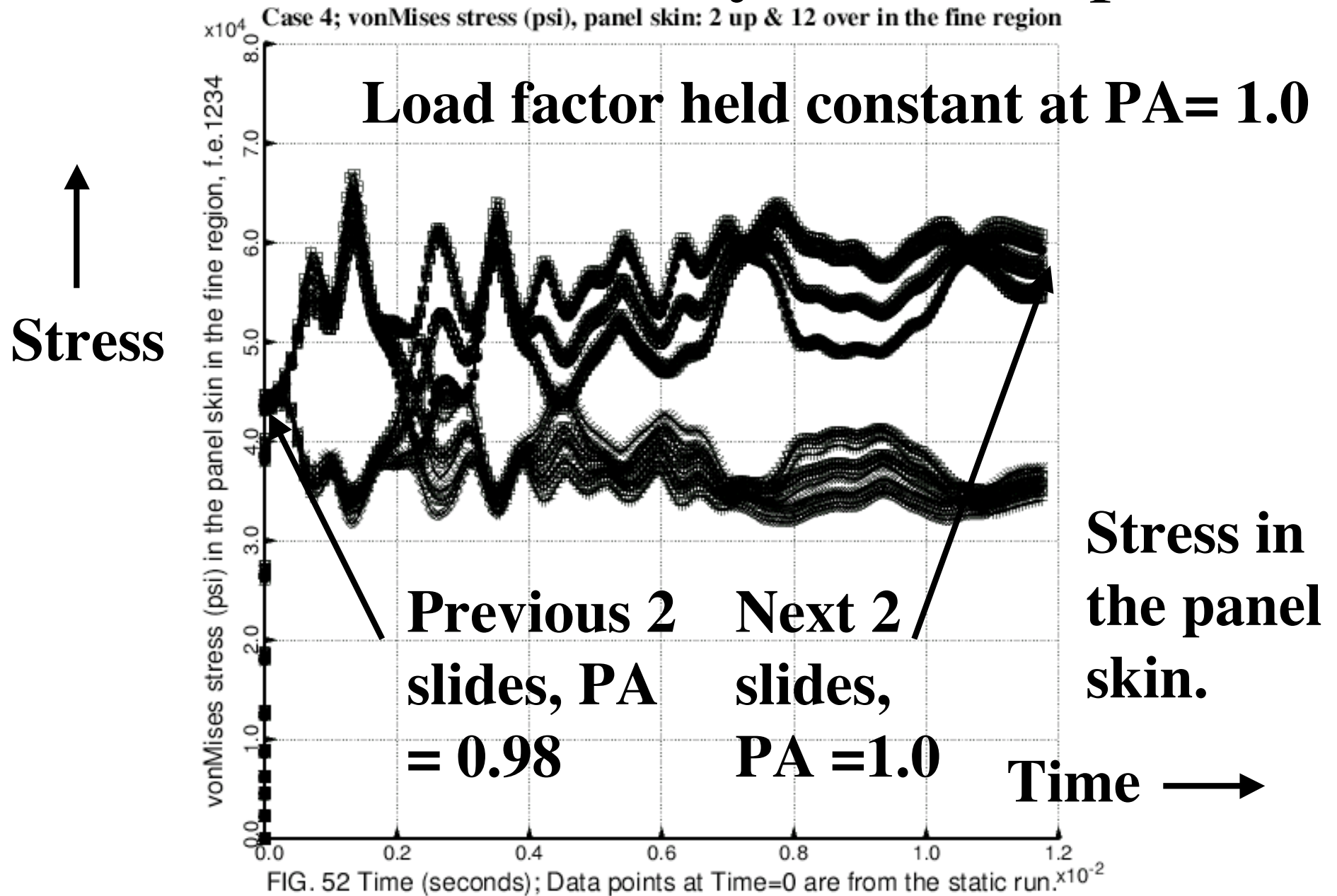
Maximum effective (von Mises) stress in the entire panel, 63.5 ksi. (Case 4 nonlinear STAGS static equilibrium at load factor, $PA = 0.98$, before the STAGS dynamic run)

Example 1 of stress in the panel skin

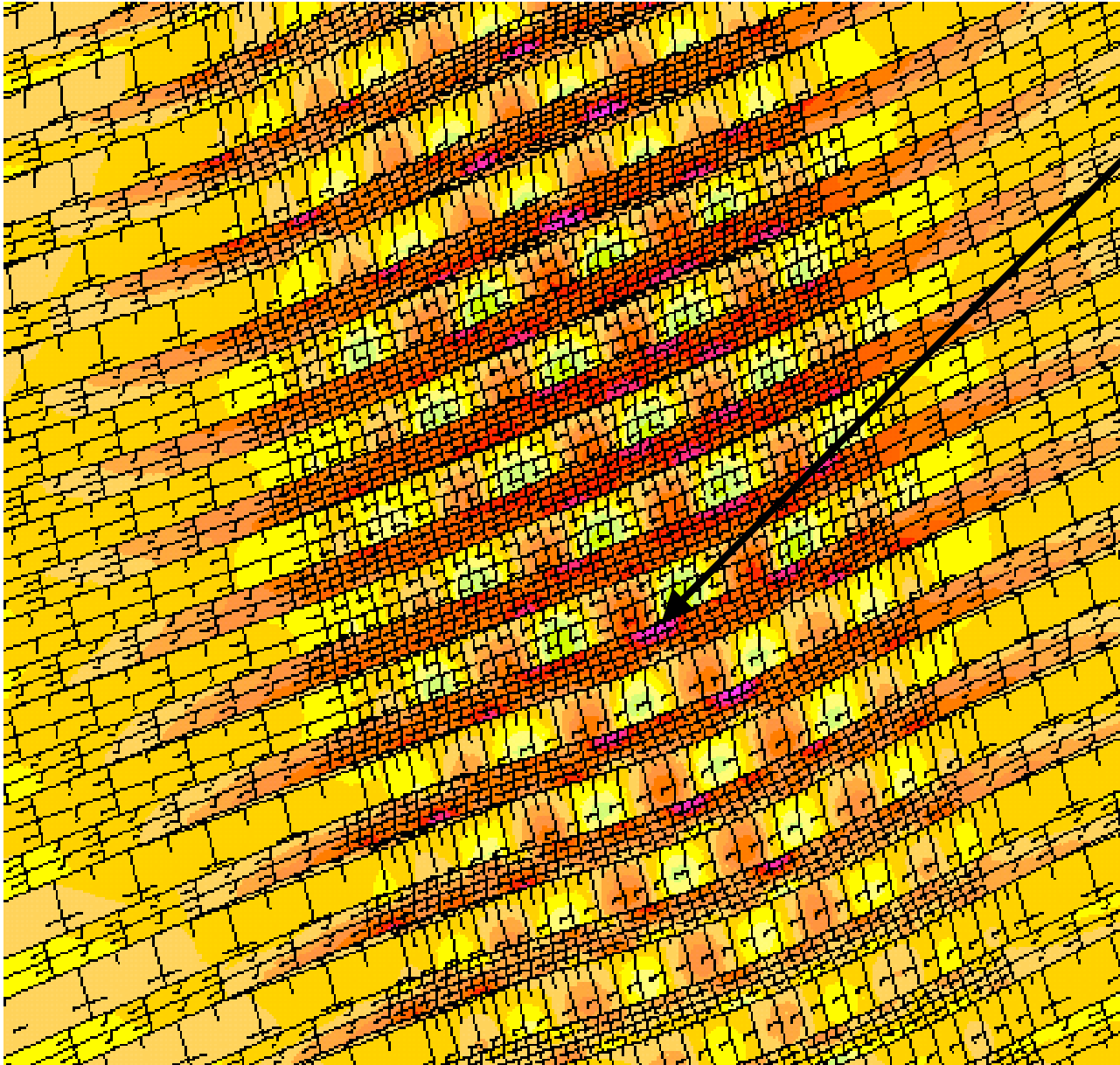


Maximum effective (von Mises) stress in the panel skin= 47.2 ksi (Case 4 nonlinear STAGS static equilibrium at load factor, PA = 0.98, before the STAGS dynamic run)

STAGS nonlinear dynamic response

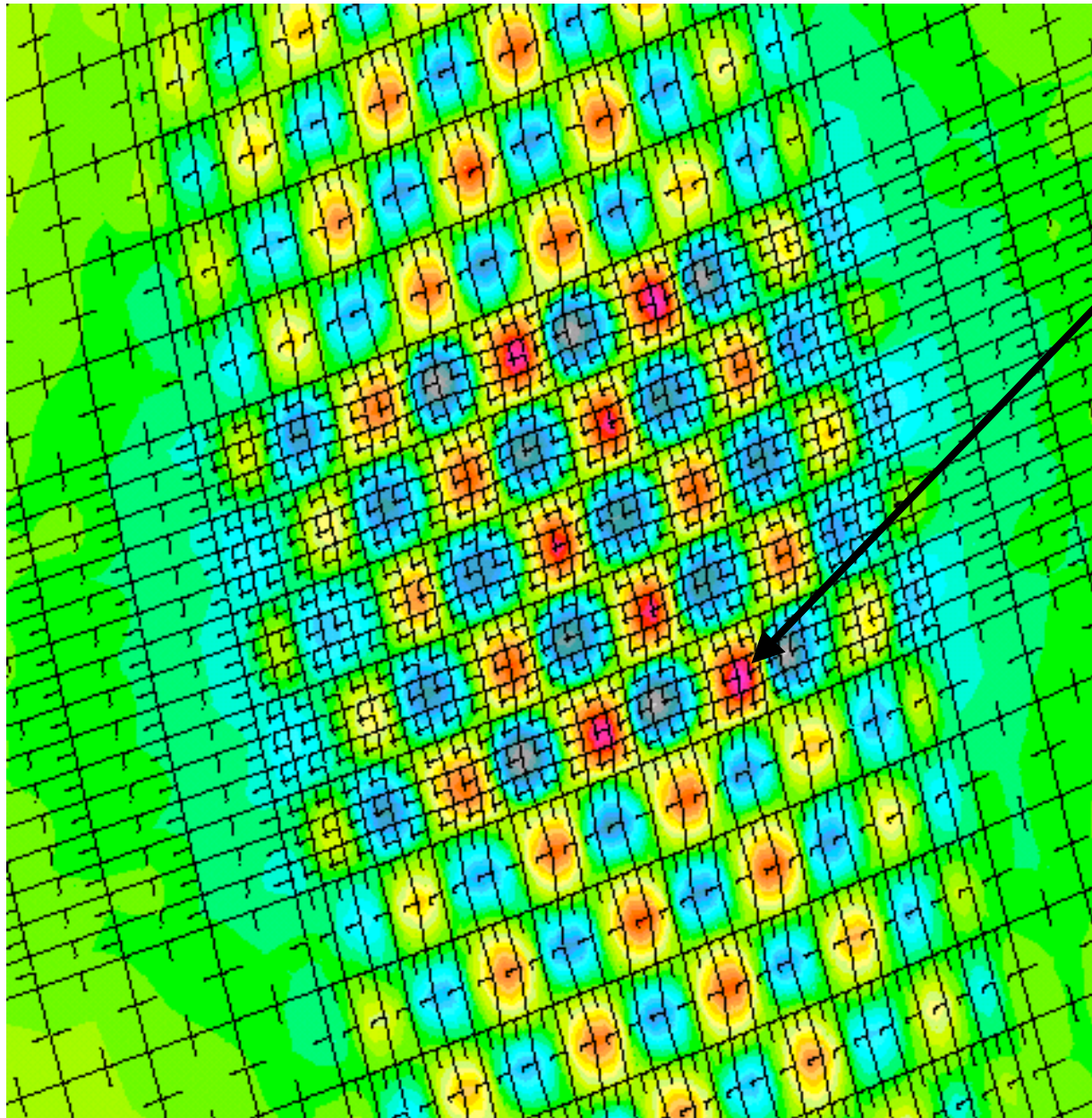


Example 2 of stress in the imperfect panel



**Maximum
effective (von
Mises) stress in
the entire panel,
70.38 ksi (Case 4
STAGS
nonlinear static
equilibrium after
the dynamic
STAGS run at
load factor, $PA =$
1.00)**

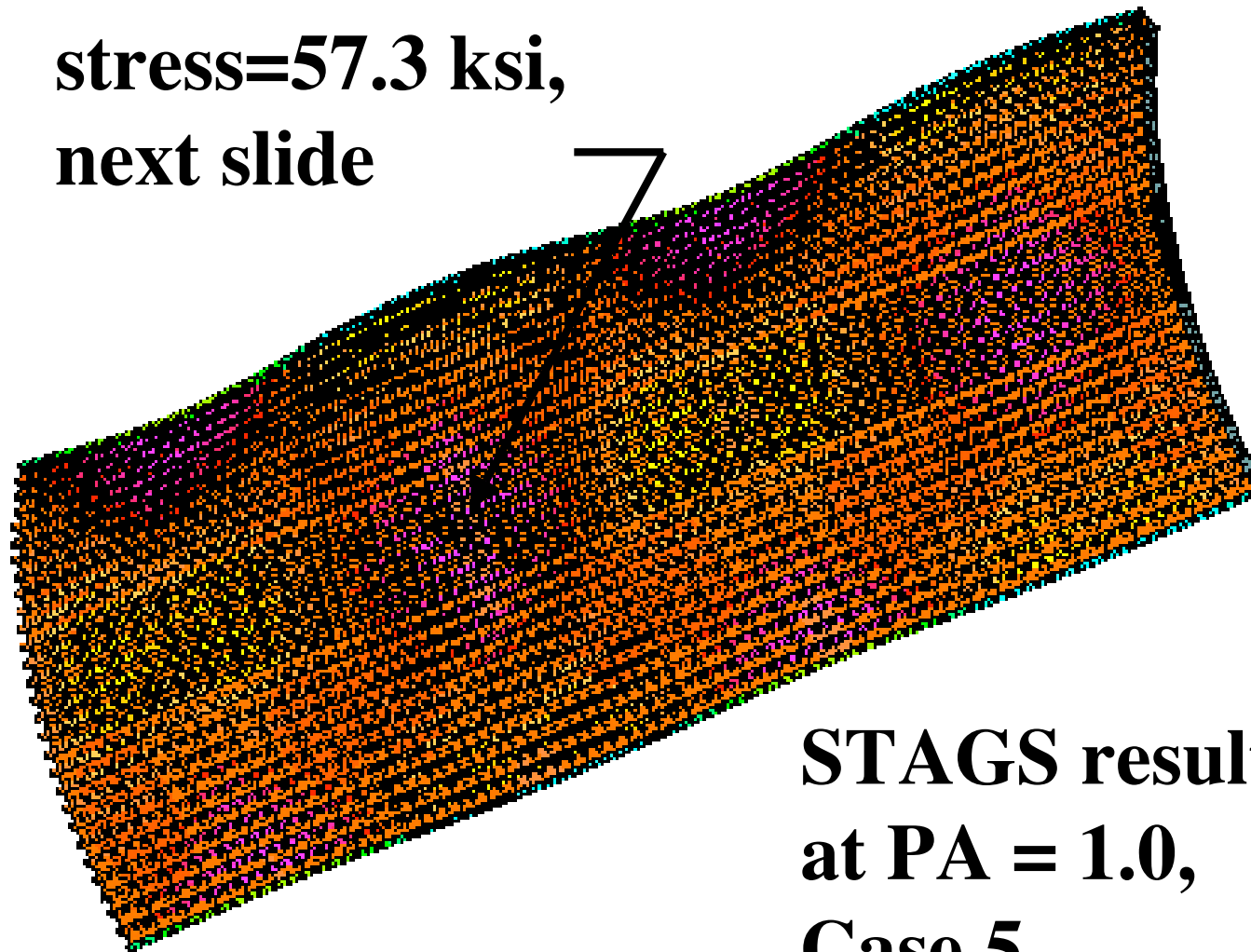
Example 2 of stress in the panel skin



**Maximum
effective (von
Mises) stress
in the panel
skin=60.6 ksi
(Case 4
nonlinear
STAGS static
equilibrium
after dynamic
STAGS run at
load factor,
 $PA = 1.00$)**

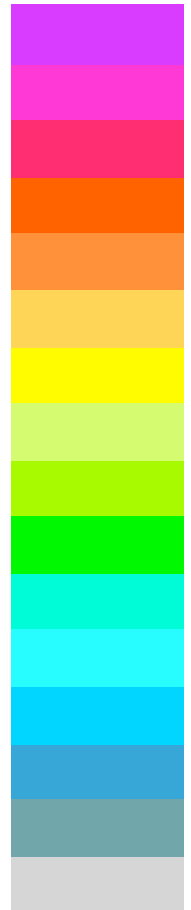
Shell optimized with “yes Koiter”

**Maximum
stress=57.3 ksi,
next slide**



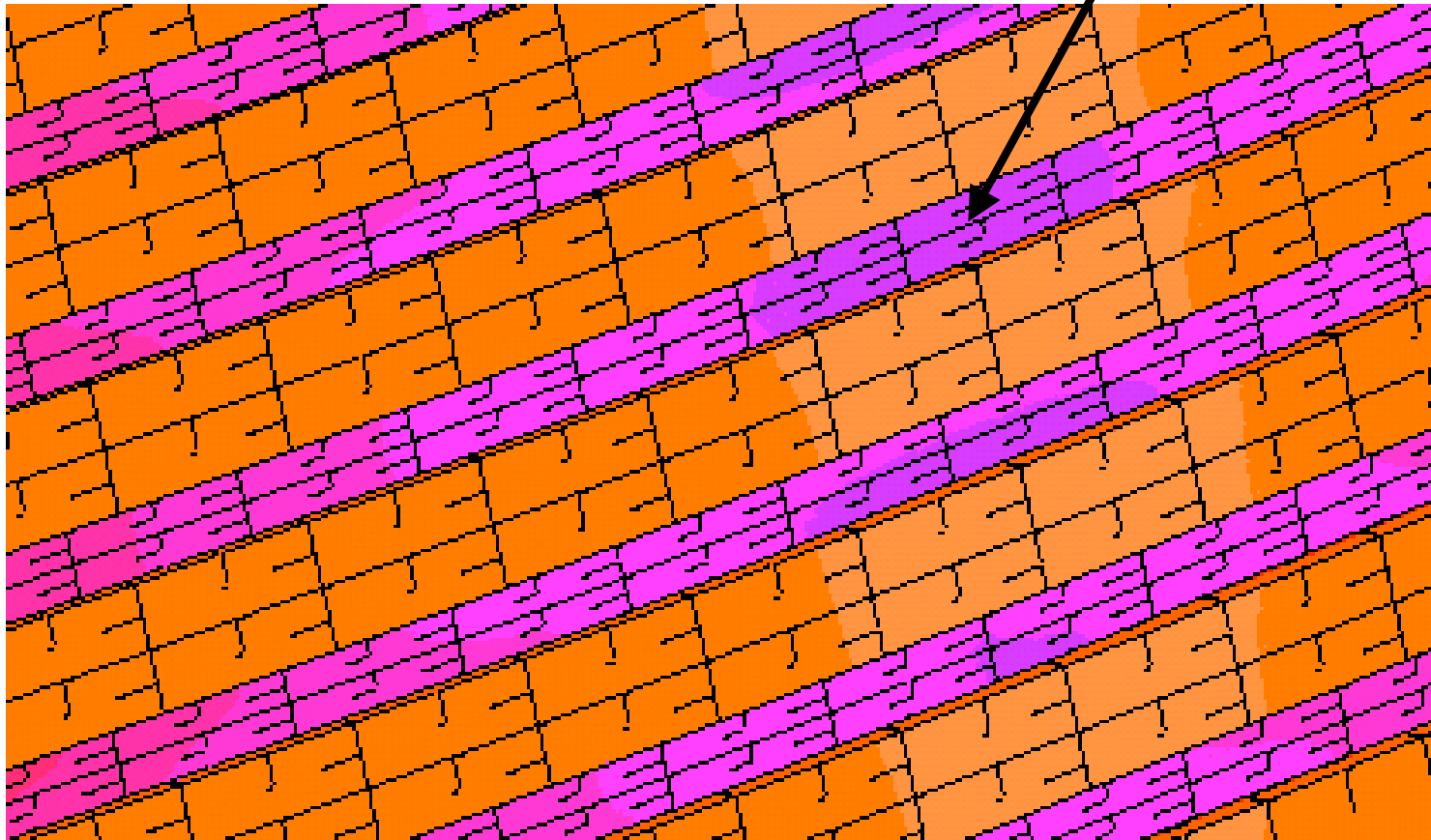
**STAGS result
at PA = 1.0,
Case 5**

5.727E+04
5.348E+04
4.970E+04
4.592E+04
4.213E+04
3.835E+04
3.457E+04
3.078E+04
2.700E+04
2.321E+04
1.943E+04
1.565E+04
1.186E+04
8.079E+03
4.296E+03
5.118E+02



Detail from previous slide: $PA = 1.0$

Maximum stress=57.3 ksi



OPTIMIZED WEIGHTS FOR CASES 1 - 7: PANDA2

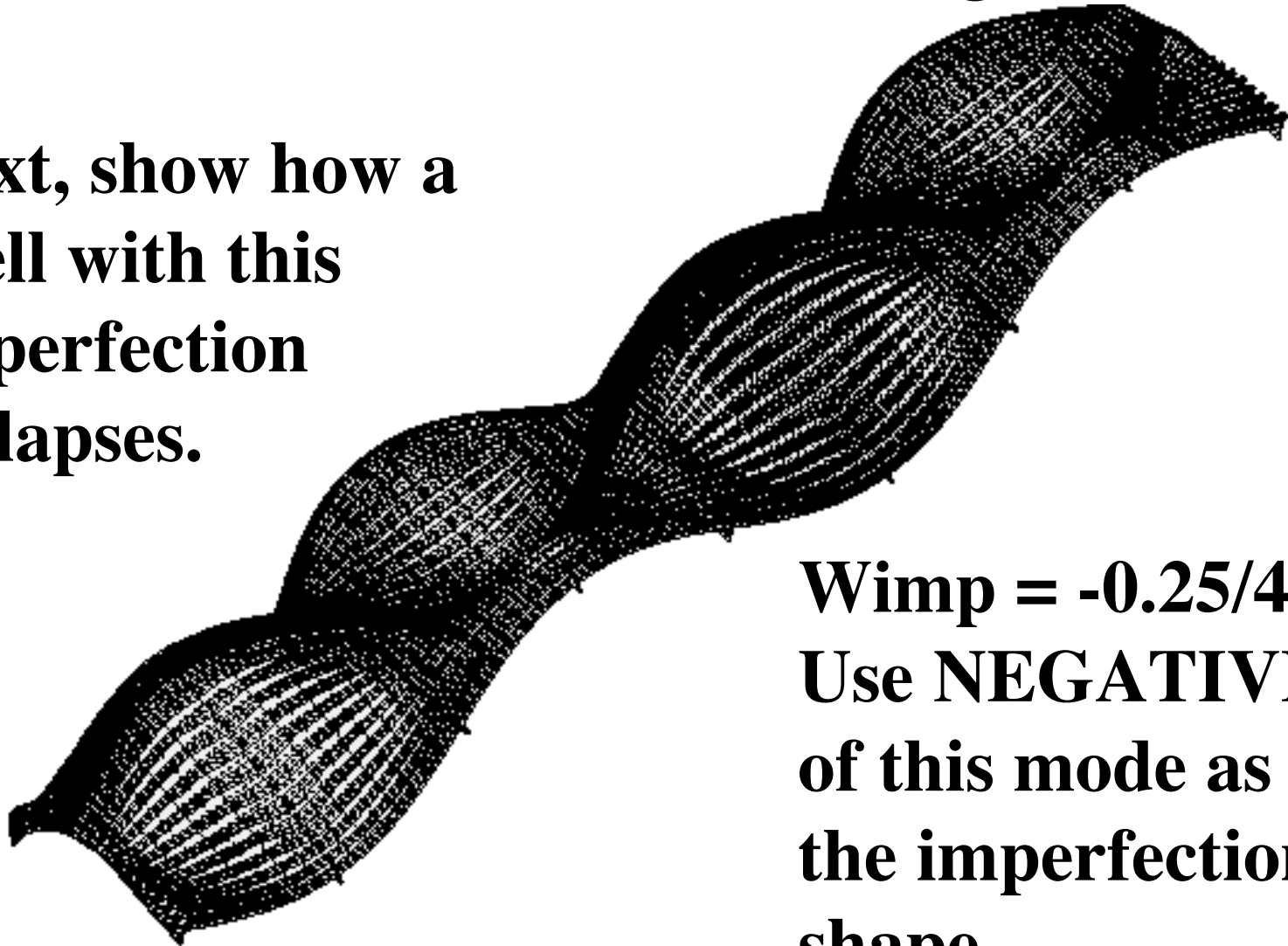
| CASE | WEIGHT(lb) | COMMENT |
|------|--------------|--|
| 1 | 31.81 | perfect shell, no Koiter, ICONSV=1 |
| 2 | 39.40 | imperfect, no Koiter, yes change imp., ICONSV=-1 |
| 3 | 40.12 | imperfect, no Koiter, yes change imp., ICONSV= 0 |
| 4 | 40.94 | imperfect, no Koiter, yes change imp., ICONSV= 1 |
| 5 | 41.89 | imperfect, yes Koiter, yes change imp., ICONSV= 1 |
| 6 | 46.83 | as if perfect, no Koiter, $N_x = -6000$ lb/in, ICONSV= 1 |
| 7 | 56.28 | imperfect, no Koiter, no change imperf., ICONSV=1 |

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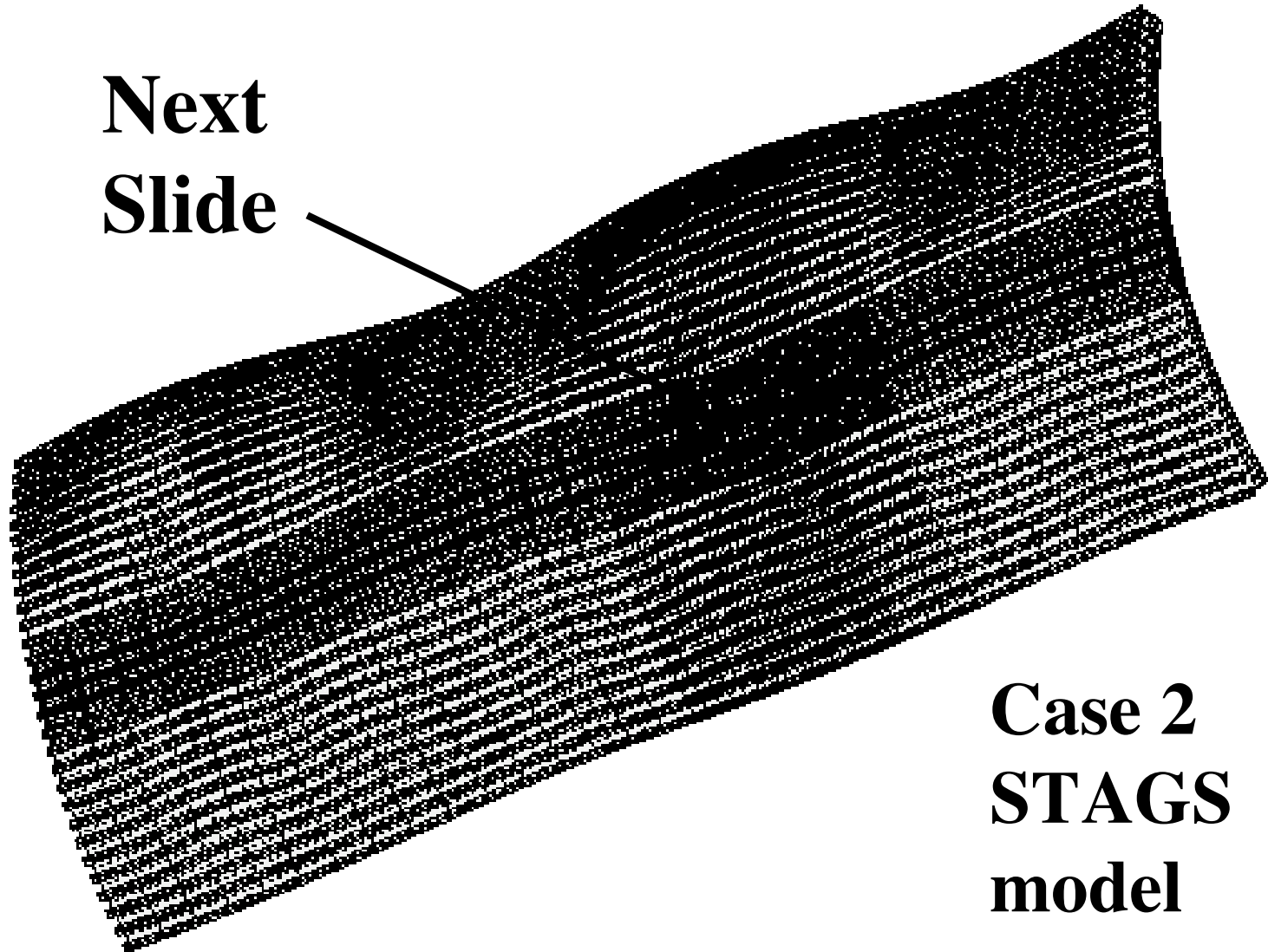
60-degree STAGS model of Case 2: General buckling mode

**Next, show how a
shell with this
imperfection
collapses.**

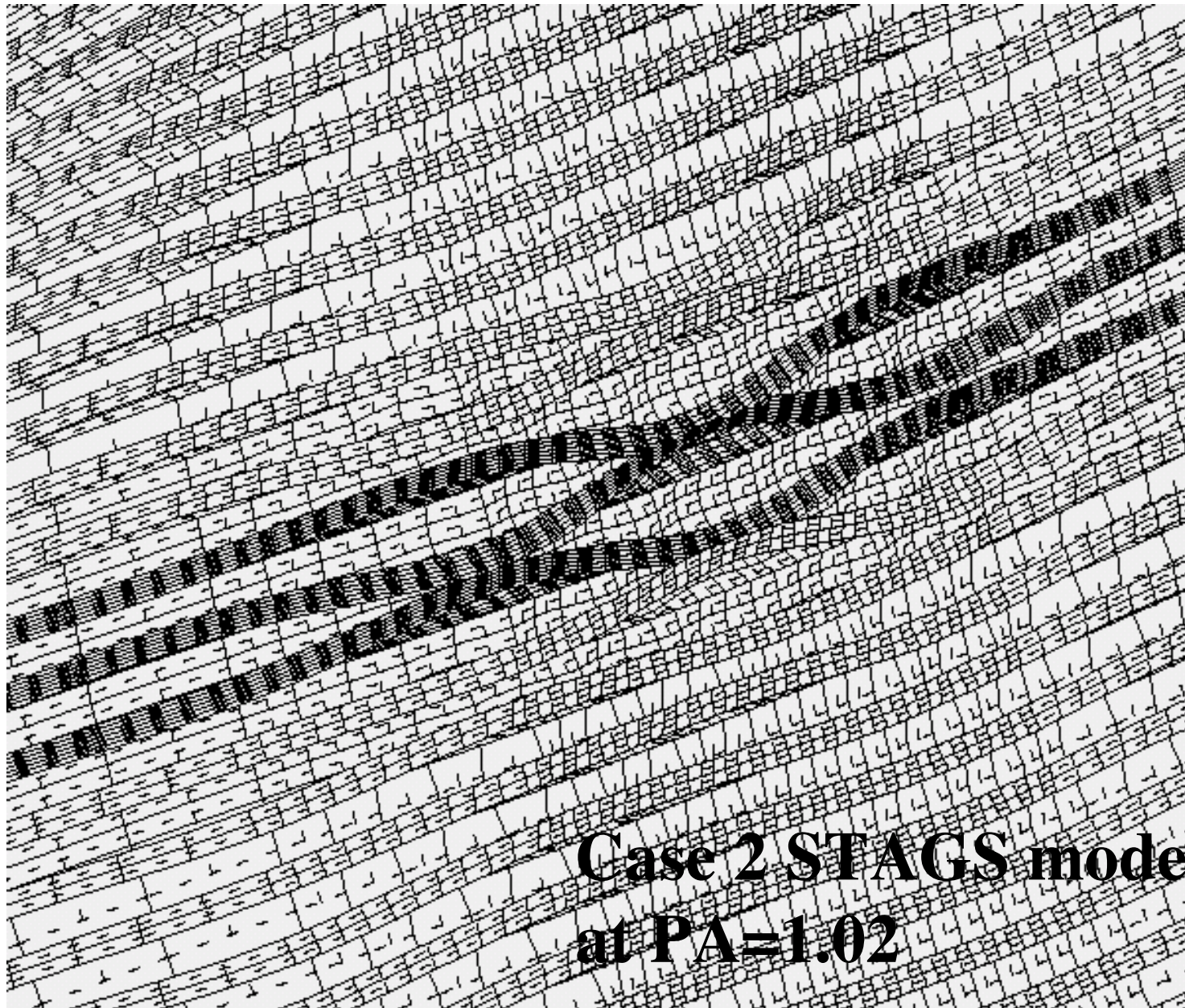


**Wimp = -0.25/4.0
Use **NEGATIVE**
of this mode as
the imperfection
shape.**

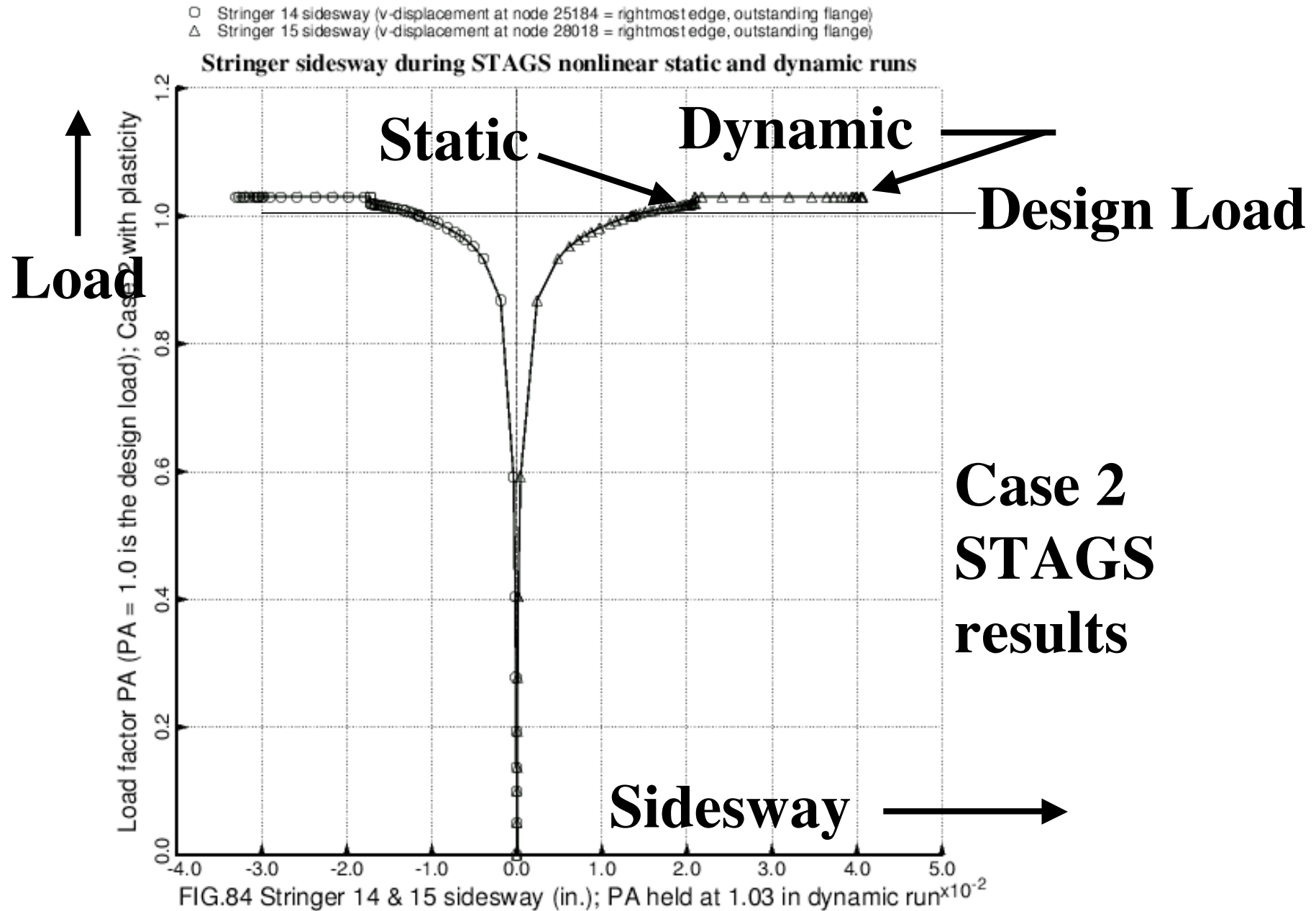
Deformed shell at $PA=1.02$ with
negative of general buckling mode



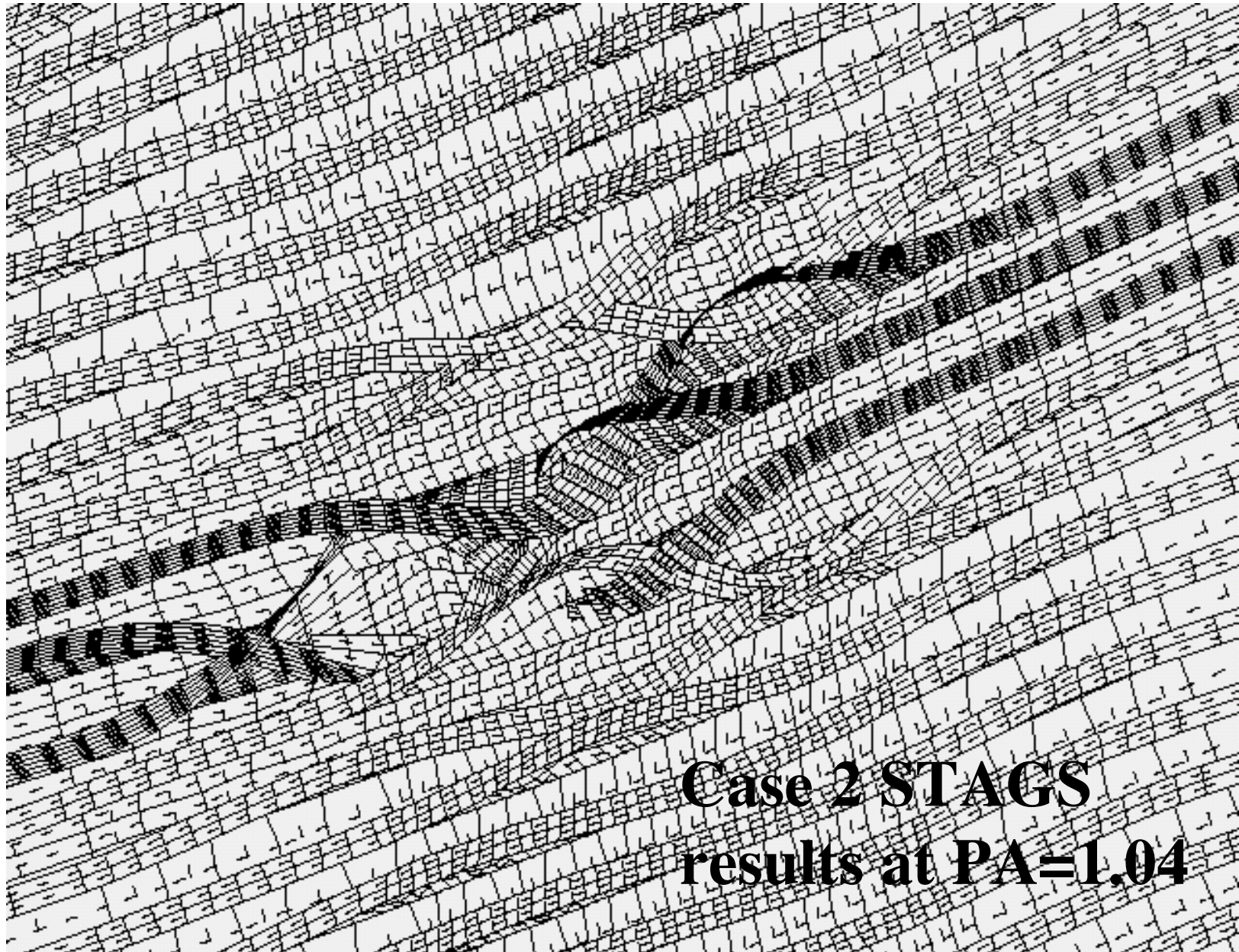
Enlarged view of collapsing zone



Sidesway of central stringers vs PA



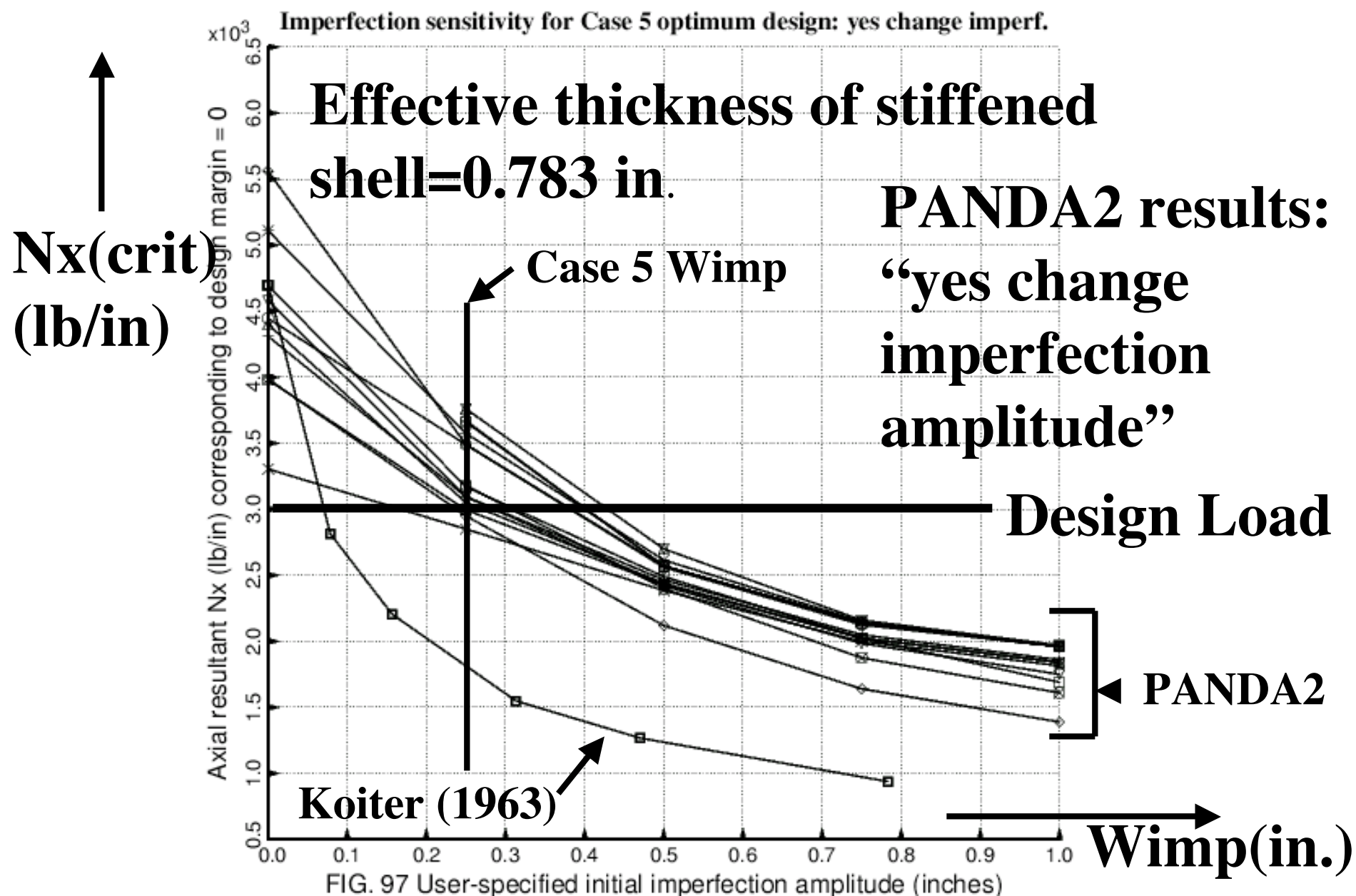
Deformation after dynamic run



Summary of talk

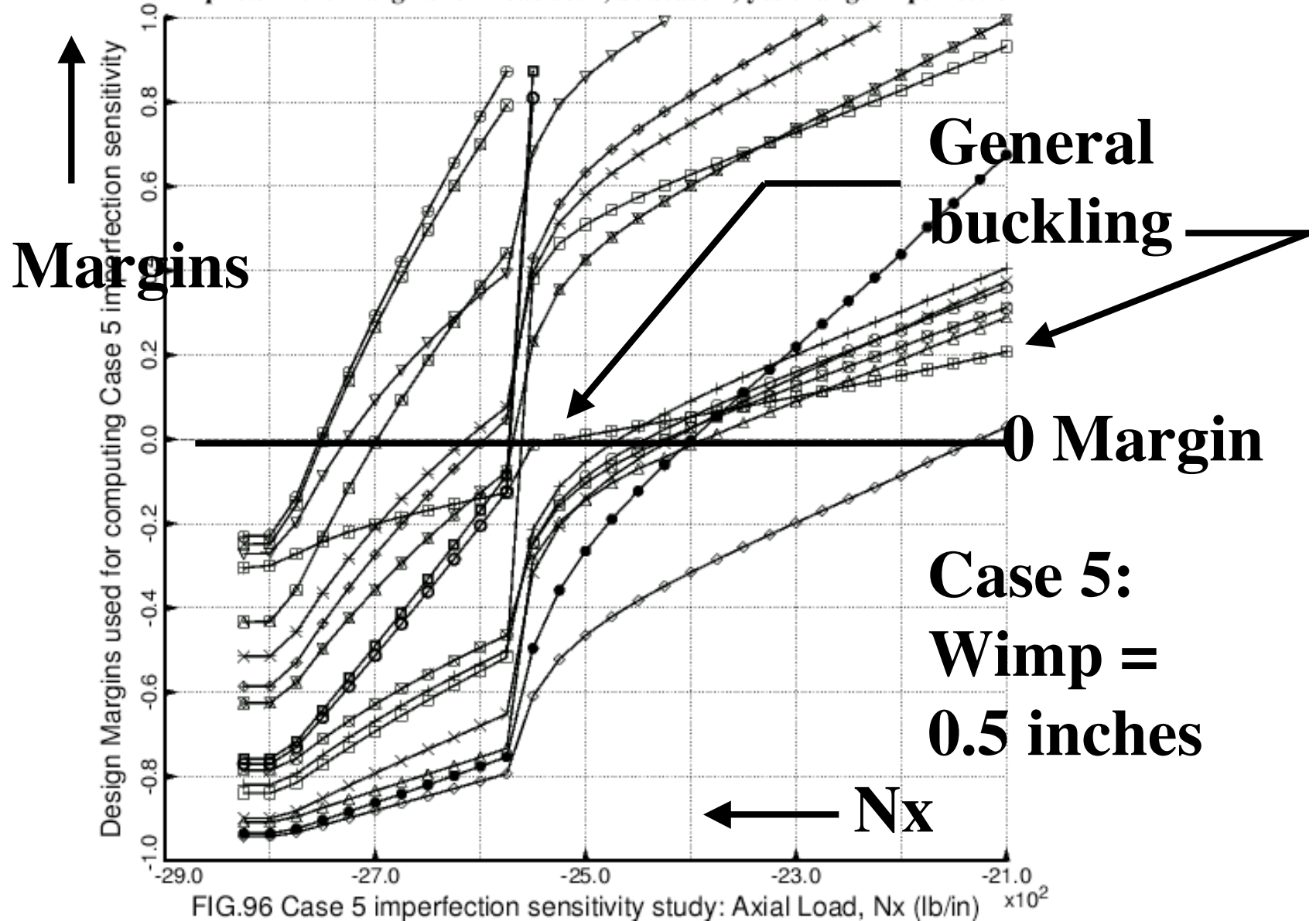
- 1. The configuration studied here**
- 2. Two effects of a general imperfection**
- 3. PANDA2 and STAGS**
- 4. PANDA2 philosophy**
- 5. Seven cases studied here**
- 6. The optimization problem**
- 7. Buckling and stress constraints**
- 8. Seven cases explained**
- 9. How the shells fail**
- 10. Imperfection sensitivity**

Imperfection sensitivity, Case 5

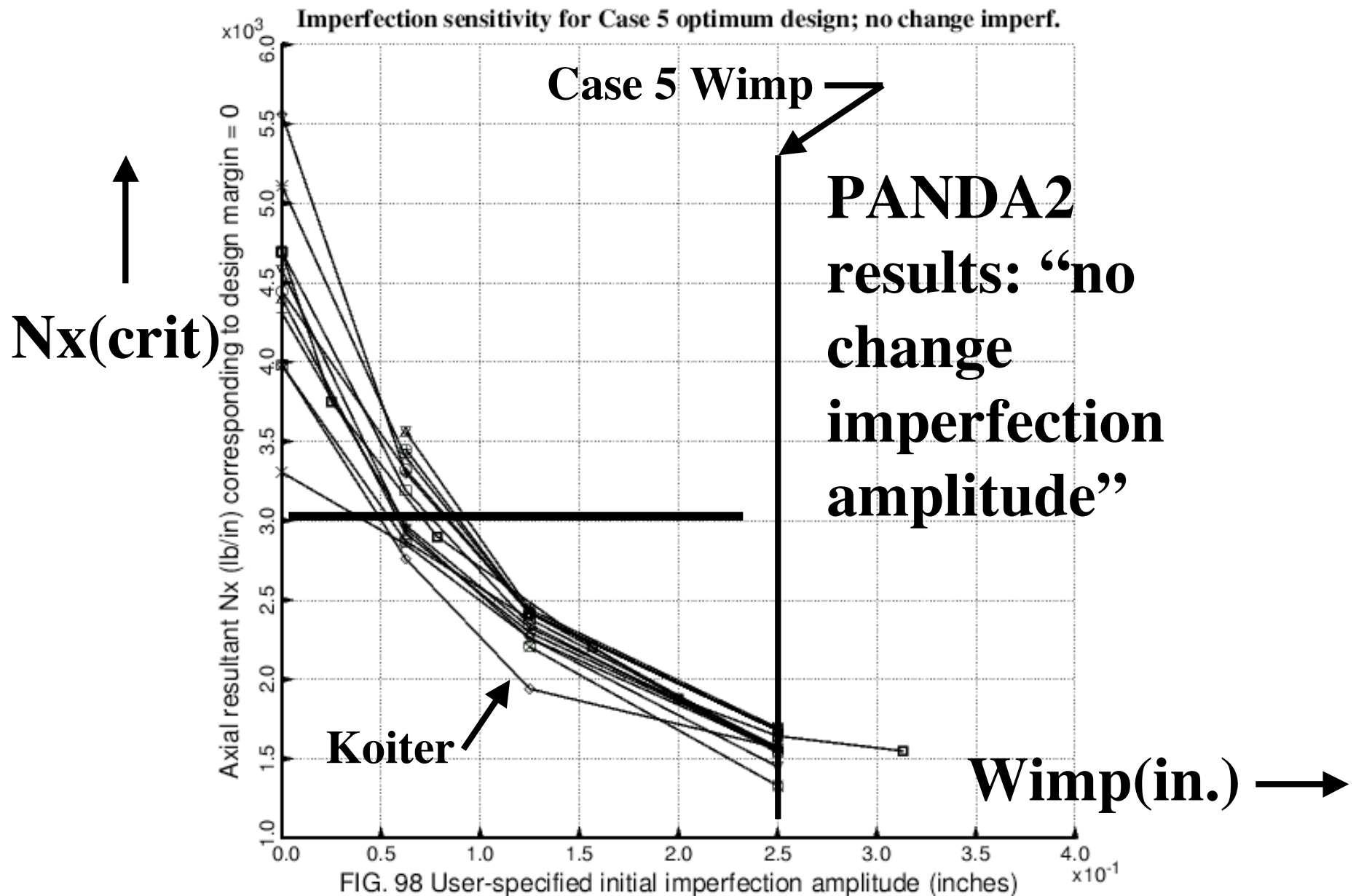


Margins from PANDA2 vs N_x

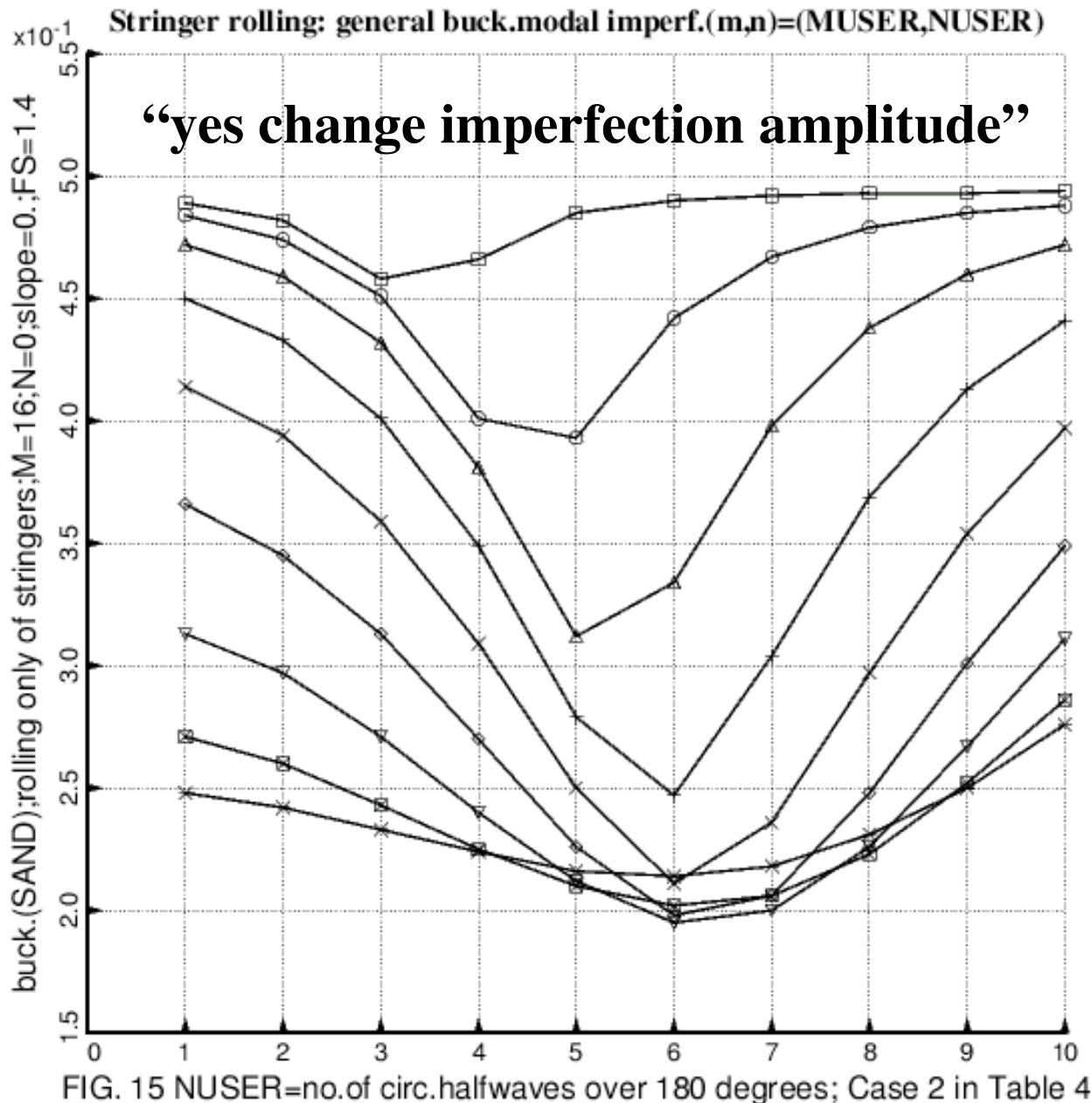
Wimp=0.5 inch: Margins for Load set 1, Subcase 1; yes change imperfection



Imperfection sensitivity: Case 5



Results of survey of Wimp(m,n)



Case 2
stringer
rolling
margin as
function of
general
buckling
modal
imperfection
shape, $A(m)$
x wimp(m,n)

Conclusions

- 1. There is reasonable agreement of PANDA2, STAGS, & BIGBOSOR4**
- 2. Use “Yes Koiter” option to avoid too-high stresses.**
- 3. Use “Yes change imperfection” option to avoid too-heavy designs.**
- 4. There are other conclusions listed in the paper.**