



Fig. 188 Elastic-plastic analysis of the **optimized unstiffened equivalent ellipsoidal shell with the thick apex with  $t(\text{apex}) = 0.4$  inch;  $W_{\text{imp}}=0.2$  inch; the optimum design is listed in Table 78.** Collapse of the imperfect shell with three different kinds of imperfections. trace 1= imperfection is a residual dent caused by a single concentrated load (Fig. 171); traces 2 and 3 = imperfections are residual dents caused by a “ $\cos(\theta)$ ” distribution of concentrated loads along a circumferential line from  $\theta = 0$  to 90 degrees (Figs. 184 and 186), and trace 4 = a linear buckling modal imperfection with  $n=1$  circumferential wave (Fig. 190). Notice the similarity between traces 2 and 4. These two curves differ mostly by a horizontal shift of  $w = 0.2$  inch, which represents the depth of the residual dent created by the “ $\cos(\theta)$ ” distribution of concentrated loads. The “ $\cos(\theta)$ ” residual dent is just as harmful as the  $n=1$  buckling modal imperfection.