

**MATHS EXAM**  
**(COMPLEX NUMBER, QUADRATIC**  
**EQUATION, LINEAR INEQUALITIES)**

TIME = 60MINS

FM=25

**1. EXPRESS IN THE FORM  $a + ib$**

a.  $i^{-39}$  (1)

b.  $[(1/3 + i7/3) + (4 + i1/3)] - (-4/3 + i)$   
(2)

c.  $(3 + i\sqrt{5})(3 - i\sqrt{5})/(\sqrt{3} + \sqrt{2}i) - (\sqrt{3} - i\sqrt{2})$   
(2)

**2. SOLVE THE FOLLOWING**

$$x^2 + x/\sqrt{2} + 1 = 0 \quad (2)$$

3. If  $x - iy = \sqrt{(a - ib)/(c - id)}$  prove that  
 $(x^2 + y^2)^2 = (a^2 + b^2)/(c^2 + d^2)$  (3)

**4. LET  $Z_1 = 2 - i$ ,  $Z_2 = -2 + i$  (2x2=4)**

$$\operatorname{Re}(Z_1 Z_2 / \bar{Z}_1)$$

$$\operatorname{Im}(1/z_1 \bar{Z}_1)$$

5. If  $(x + iy)^3 = u + iv$ , then show that  
$$u/x + v/y = 4(x^2 - y^2) \quad (3)$$

6. **SOLVE THE FOLLOWING SYSTEM OF INEQUALITIES GRAPHICALLY (4)**

$$3x + 2y \leq 150, \quad x + 4y \leq 80, \quad x \geq 0, \quad y \geq 0$$

7. **EVALUATE: (4)**  
 $\sqrt{16-30i}$