

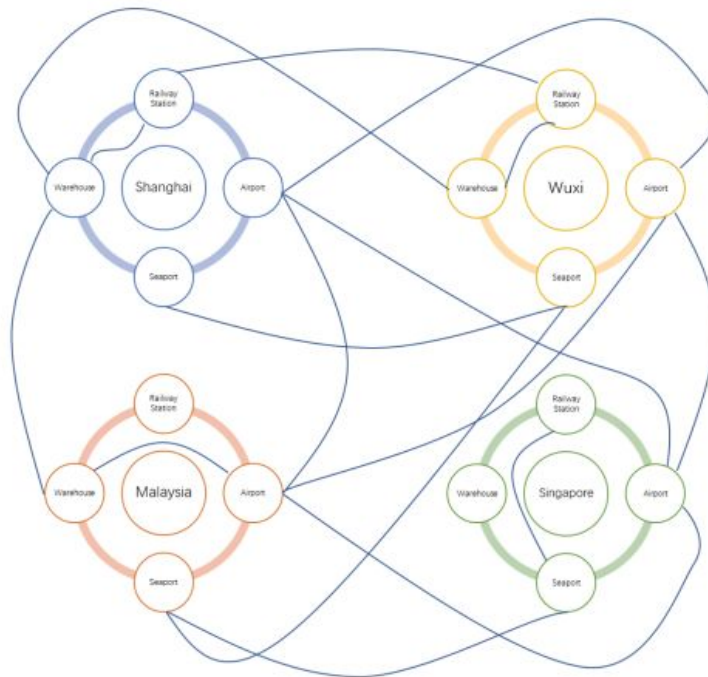
Experiment 8

Aim: Write a program to implement any kind of optimization on a multimodal dataset

Theory:

In this experiment, we would be using swarm algorithms to solve multi-modal transportation cost minimization in goods delivery and do the required optimization for better results.

In our simulated case, there are 8 goods, 4 cities/countries (Shanghai, Wuxi, Singapore, Malaysia), 16 ports and 4 transportation tools. The 8 goods originate from different cities and have different destinations. Each city/country has 4 ports, the airport, railway station, seaport and warehouse. There are in total 50 direct routes connecting different ports. Each route has a specific transportation tool, transportation cost, transit time and weekly schedule. Warehouses in each city allow goods to be deposited for a period of time so as to fit certain transportation schedules or wait for other goods to be transported together. All goods might have different order dates and different delivery deadlines. With all these criteria, how can we find out solution routes for all goods that minimize the overall cost?



Optimizing of routes using various swarm algorithms

Algorithm:

In order to make the criteria logic clearer and the calculation more efficient, we use the concept of the matrix to build the necessary components in the model. In our case, there are totally 4 dimensions:

1. Start Port: i

Indicating the start port of a direct transport route. The dimension length equals the total number of ports in the data.

2. End Port: j

Indicating the end port of a direct transport route. The dimension length equals the total number of ports in the data.

3. Time: t

Indicating the departure time of direct transport. The dimension length equals the total number of days between the earliest order date and the latest delivery deadline date of all goods in the data.

4. Goods: k

Indicating the goods to be transported. The dimension length equals the total number of goods in the data. All the variable or parameter matrices to be introduced in the later parts will have one or more of these 4 dimensions.

The objective of the model is to minimize the overall cost, which includes 3 parts, transportation cost, warehouse cost and tax cost. Firstly, the transportation cost includes container cost and route fixed cost. Container cost equals the number of containers used in each route times per container cost while route fixed cost equals the sum of the fixed cost of all routes.

Source Code:

multi.py

```
from
docplex.mp.model
import Model
from itertools import product
import numpy as np
import cvxpy as cp
import pandas as pd
import json
class MMT:
    """a Model class that solves the multi-model transportation optimization problem."""
    def __init__(self, framework='DOCPLEX'):
        self.portSpace = None
        self.dateSpace = None
        self.goods = None
        self.indexPort = None
```

```
self.portIndex = None
self.maxDate = None
self.minDate = None
self.tranCost = None
self.tranFixedCost = None
self.tranTime = None
self.ctnVol = None
self.whCost = None
self.kVol = None
self.kValue = None
self.kDDL = None
self.kStartPort = None
self.kEndPort = None
self.kStartTime = None
self.taxPct = None
self.transitDuty = None
self.route_num = None
self.available_routes = None
# decision variables
self.var = None
self.x = None
self.var_2 = None
self.y = None
self.var_3 = None
self.z = None
# result & solution
self.xs = None
self.ys = None
self.zs = None
self.whCostFinal = None
self.transportCost = None
self.taxCost = None
self.solution_ = None
self.arrTime_ = None
self.objective_value = None
# helping variables
self.var_location = None
self.var_2_location = None
self.var_3_location = None
```

```
if framework not in ['CVXPY', 'DOCPLEX']:
```

```
        raise ValueError('Framework not supported, the model only supports CVXPY and  
DOCPLEX')
```

```
    else:
```

```
        self.framework = framework
```

```
def set_param(self, route, order):
```

```
    """set model parameters based on the read-in route and order information."""
```

```
        bigM = 100000
```

```
        route = route[route['Feasibility'] == 1]
```

```
        route['Warehouse Cost'][route['Warehouse Cost'].isnull()] = bigM
```

```
        route = route.reset_index()
```

```
        portSet = set(route['Source']) | set(route['Destination'])
```

```
        self.portSpace = len(portSet)
```

```
        self.portIndex = dict(zip(range(len(portSet)), portSet))
```

```
        self.indexPort = dict(zip(self.portIndex.values(), self.portIndex.keys()))
```

```
        self.maxDate = np.max(order['Required Delivery Date'])
```

```
        self.minDate = np.min(order['Order Date'])
```

```
        self.dateSpace = (self.maxDate - self.minDate).days
```

```
        startWeekday = self.minDate.weekday() + 1
```

```
        weekday = np.mod((np.arange(self.dateSpace) + startWeekday), 7)
```

```
        weekday[weekday == 0] = 7
```

```
        weekdayDateList = {i: [] for i in range(1, 8)}
```

```
        for i in range(len(weekday)):
```

```
            weekdayDateList[weekday[i]].append(i)
```

```
        for i in weekdayDateList:
```

```
            weekdayDateList[i] = json.dumps(weekdayDateList[i])
```

```
        source = list(route['Source'].replace(self.indexPort))
```

```
        destination = list(route['Destination'].replace(self.indexPort))
```

```
        DateList = list(route['Weekday'].replace(weekdayDateList).apply(json.loads))
```

```
        self.goods = order.shape[0]
```

```
        self.tranCost = np.ones([self.portSpace, self.portSpace, self.dateSpace]) * bigM
```

```
        self.tranFixedCost = np.ones([self.portSpace, self.portSpace, self.dateSpace]) * bigM
```

```
        self.tranTime = np.ones([self.portSpace, self.portSpace, self.dateSpace]) * bigM
```

```
        for i in range(route.shape[0]):
```

```
            self.tranCost[source[i], destination[i], DateList[i]] = route['Cost'][i]
```

```
            self.tranFixedCost[source[i], destination[i], DateList[i]] = route['Fixed Freight  
Cost'][i]
```

```
            self.tranTime[source[i], destination[i], DateList[i]] = route['Time'][i]
```

```
        self.transitDuty = np.ones([self.portSpace, self.portSpace]) * bigM
```

```
        self.transitDuty[source, destination] = route['Transit Duty']
```

```

# make the container size of infeasible routes to be small enough, similar to bigM
self.ctnVol = np.ones([self.portSpace, self.portSpace]) * 0.1
self.ctnVol[source, destination] = route['Container Size']
self.ctnVol = self.ctnVol.reshape(self.portSpace, self.portSpace, 1)
self.whCost = route[['Source', 'Warehouse Cost']].drop_duplicates()
self.whCost['index'] = self.whCost['Source'].replace(self.indexPort)
self.whCost = np.array(self.whCost.sort_values(by='index')['WarehouseCost'])
self.kVol = np.array(order['Volume'])
self.kValue = np.array(order['Order Value'])
self.kDDL = np.array((order['Required Delivery Date'] - self.minDate).dt.days)
self.kStartPort = np.array(order['Ship From'].replace(self.indexPort))
self.kEndPort = np.array(order['Ship To'].replace(self.indexPort))
self.kStartTime = np.array((order['Order Date'] - self.minDate).dt.days)
self.taxPct = np.array(order['Tax Percentage'])

# add available route indexes
self.route_num = route[['Source', 'Destination']].drop_duplicates().shape[0]
routes = route[['Source', 'Destination']].drop_duplicates().replace(self.indexPort)
self.available_routes = list(zip(routes['Source'], routes['Destination']))

# localization variables of decision variables in the matrix
var_location = product(self.available_routes, range(self.dateSpace), range(self.goods))
var_location = [(i[0][0], i[0][1], i[1], i[2]) for i in var_location]
self.var_location = tuple(zip(*var_location))
var_2_location = product(self.available_routes, range(self.dateSpace))
var_2_location = [(i[0][0], i[0][1], i[1]) for i in var_2_location]
self.var_2_location = tuple(zip(*var_2_location))
self.var_3_location = self.var_2_location

def build_model(self):
    """overall function to build up model objective and constraints"""
    if self.framework == 'CVXPY':
        self.cvxpy_build_model()
    elif self.framework == 'DOCPLEX':
        self.cplex_build_model()

def cvxpy_build_model(self):
    """build up the mathematical programming model's objective and constraints using CVXPY
    framework."""
    # 4 dimensional binary decision variable matrix
    self.var = cp.Variable(self.route_num * self.dateSpace * self.goods, boolean=True,
name='x')

```

```

self.x = np.zeros((self.portSpace, self.portSpace, self.dateSpace,
self.goods)).astype('object')
self.x[self.var_location] = list(self.var)

# 3 dimensional container number matrix
self.var_2 = cp.Variable(self.route_num * self.dateSpace, integer=True, name='y')
self.y = np.zeros((self.portSpace, self.portSpace, self.dateSpace)).astype('object')
self.y[self.var_2_location] = list(self.var_2)

self.var_3 = cp.Variable(self.route_num * self.dateSpace, boolean=True, name='z')
self.z = np.zeros((self.portSpace, self.portSpace, self.dateSpace)).astype('object')
self.z[self.var_3_location] = list(self.var_3)
# warehouse related cost
warehouseCost, arrTime, stayTime = self.warehouse_fee(self.x)
transportCost = np.sum(self.y * self.tranCost) + np.sum(self.z * self.tranFixedCost)
transitDutyCost = np.sum(np.sum(np.dot(self.x, self.kValue), axis=2) * self.transitDuty)
taxCost = np.sum(self.taxPct * self.kValue) + transitDutyCost
objective = cp.Minimize(transportCost + warehouseCost + taxCost)

constraints = []
constraints += [np.sum(self.x[self.kStartPort[k], :, :, k]) == 1 for k in range(self.goods)]
constraints += [np.sum(self.x[:, self.kEndPort[k], :, k]) == 1 for k in range(self.goods)]

constraints += [np.sum(self.x[:, self.kStartPort[k], :, k]) == 0 for k in range(self.goods)]
constraints += [np.sum(self.x[self.kEndPort[k], :, :, k]) == 0 for k in range(self.goods)]

for k in range(self.goods):
    for j in range(self.portSpace):
        if (j != self.kStartPort[k]) & (j != self.kEndPort[k]):
            constraints.append(np.sum(self.x[:, j, :, k]) == np.sum(self.x[j, :, :,
k]))

constraints += [np.sum(self.x[i, :, :, k]) <= 1 for k in range(self.goods)
for i in range(self.portSpace)]
constraints += [np.sum(self.x[:, j, :, k]) <= 1 for k in range(self.goods)
for j in range(self.portSpace)]
constraints += [stayTime[j, k] >= 0 for j in range(self.portSpace) for k in
range(self.goods)]

numCtn = np.dot(self.x, self.kVol) / self.ctnVol
constraints += [self.y[i, j, t] - numCtn[i, j, t] >= 0 \
for i in range(self.portSpace) for j in

```

```

range(self.portSpace) for t in
                                range(self.dateSpace) if not isinstance(self.y[i, j, t] -
numCtn[i, j, t] >= 0, bool)]

constraints += [self.z[i, j, t] >= (np.sum(self.x[i, j, t, :]) * 10e-5) \
for i in range(self.portSpace)
for j in range(self.portSpace)
for t in range(self.dateSpace)
if not isinstance(self.z[i, j, t] >= (np.sum(self.x[i, j, t, :]) * 10e-5),
bool)]

constraints += [np.sum(arrTime[:, self.kEndPort[k], :, k])
<= self.kDDL[k]
for k in range(self.goods)
if not isinstance(np.sum(arrTime[:, self.kEndPort[k], :, k]) <= self.kDDL[k], bool)]
model = cp.Problem(objective, constraints)
self.objective = objective
self.constraints = constraints
self.model = model

def cplex_build_model(self):
    """build up the mathematical programming model's objective and constraints using DOCPLEX
    framework."""
    model = Model()

    self.var = model.binary_var_list(self.route_num * self.dateSpace * self.goods, name='x')
    self.x = np.zeros((self.portSpace, self.portSpace,
self.dateSpace, self.goods)).astype('object')
    self.x[self.var_location] = self.var

    # 3 dimensional container number matrix
    self.var_2 = model.integer_var_list(self.route_num * self.dateSpace, name='y')
    self.y = np.zeros((self.portSpace, self.portSpace, self.dateSpace)).astype('object')
    self.y[self.var_2_location] = self.var_2

    self.var_3 = model.binary_var_list(self.route_num * self.dateSpace, name='z')
    self.z = np.zeros((self.portSpace, self.portSpace, self.dateSpace)).astype('object')
    self.z[self.var_3_location] = self.var_3
    warehouseCost, arrTime, stayTime = self.warehouse_fee(self.x)
    transportCost = np.sum(self.y * self.tranCost) + np.sum(self.z * self.tranFixedCost)
    transitDutyCost = np.sum(np.sum(np.dot(self.x, self.kValue), axis=2) * self.transitDuty)
    taxCost = np.sum(self.taxPct * self.kValue) + transitDutyCost
    model.minimize(transportCost + warehouseCost + taxCost)

```

```

        model.add_constraints(np.sum(self.x[self.kStartPort[k], :, :, k]) == 1 for k in
range(self.goods))
        model.add_constraints(np.sum(self.x[:, self.kEndPort[k], :, k]) == 1 for k in
range(self.goods))
        model.add_constraints(np.sum(self.x[:, self.kStartPort[k], :, k]) == 0 for k in
range(self.goods))
        model.add_constraints(np.sum(self.x[self.kEndPort[k], :, :, k]) == 0 for k in
range(self.goods))

    for k in range(self.goods):
        for j in range(self.portSpace):
            if (j != self.kStartPort[k]) & (j != self.kEndPort[k]):
                model.add_constraint(np.sum(self.x[:, j, :, k]) == np.sum(self.x[j, :, :, k]))

        model.add_constraints(np.sum(self.x[i, :, :, k]) <= 1 for k in range(self.goods) for i in
range(self.portSpace))
        model.add_constraints(np.sum(self.x[:, j, :, k]) <= 1 for k in range(self.goods) for j in
range(self.portSpace))
        # 5.transition-out should be after transition-in
        model.add_constraints(stayTime[j, k] >= 0 for j in range(self.portSpace)
for k in range(self.goods))
        # 6.constraint for number of containers used
        numCtn = np.dot(self.x, self.kVol) / self.ctnVol
        model.add_constraints(self.y[i, j, t] - numCtn[i, j, t] >= 0 \
for i in range(self.portSpace) for j in
range(self.portSpace) for t in
range(self.dateSpace) if not isinstance(self.y[i, j,
t] - numCtn[i, j, t] >= 0, bool))
        # 7. constraint to check whether a route is used
        model.add_constraints(self.z[i, j, t] >= (np.sum(self.x[i, j, t, :]) *
10e-5) \
for i in range(self.portSpace) for j in range(self.portSpace) for t in range(self.dateSpace)
if not isinstance(self.z[i, j, t] >= (np.sum(self.x[i, j, t, :]) * 10e-5), bool))
            model.add_constraints(np.sum(arrTime[:, self.kEndPort[k], :, k])
<=self.kDDL[k] for k in range(self.goods)
            if not isinstance(np.sum(arrTime[:, self.kEndPort[k], :, k]) <= self.kDDL[k], bool))
        self.objective = model.objective_expr
        self.constraints = list(model.iter_constraints())
        self.model = model

```

```

def solve_model(self, solver=cp.CBC):

```



```

try:
    if self.framework == 'CVXPY':
        self.objective_value = self.model.solve(solver)
        self.xs = np.zeros((self.portSpace, self.portSpace,
self.dateSpace, self.goods))
        self.xs[self.var_location] = self.var.value
        self.ys = np.zeros((self.portSpace, self.portSpace,
self.dateSpace))
        self.ys[self.var_2_location] = self.var_2.value
        self.zs = np.zeros((self.portSpace, self.portSpace,
self.dateSpace))
        self.zs[self.var_3_location] = self.var_3.value
    elif self.framework == 'DOCPLEX':
        ms = self.model.solve()
        self.objective_value = self.model.objective_value
        self.xs = np.zeros((self.portSpace, self.portSpace,
self.dateSpace, self.goods))
        self.xs[self.var_location] = ms.get_values(self.var)
        self.ys = np.zeros((self.portSpace, self.portSpace,
self.dateSpace))
        self.ys[self.var_2_location] = ms.get_values(self.var_2)
        self.zs = np.zeros((self.portSpace, self.portSpace,
self.dateSpace))
        self.zs[self.var_3_location] = ms.get_values(self.var_3)
    except:
        raise Exception('Model is not solvable, no solution will be provided')
        nonzeroX = list(zip(*np.nonzero(self.xs)))
        nonzeroX = sorted(nonzeroX, key=lambda x: x[2])
        nonzeroX = sorted(nonzeroX, key=lambda x: x[3])
        nonzeroX = list(map(lambda x: (self.portIndex[x[0]], self.portIndex[x[1]],
\
(self.minDate + pd.to_timedelta(x[2],
unit='days')).date().isoformat(),
x[3]), nonzeroX))
        self.whCostFinal, arrTime, _ = self.warehouse_fee(self.xs)
        self.transportCost = np.sum(self.ys * self.tranCost) + np.sum(self.zs *
self.tranFixedCost)
        self.taxCost = np.sum(self.taxPct * self.kValue) + \
np.sum(np.sum(np.dot(self.xs, self.kValue), axis=2) *
self.transitDuty)
        self.solution_ = {}
        self.arrTime_ = {}

```

```

        for i in range(self.goods):
            self.solution_['goods-' + str(i + 1)] = list(filter(lambda x: x[3] ==
i, nonzeroX))
            self.arrTime_['goods-' + str(i + 1)] = (self.minDate + pd.to_timedelta
\
            (np.sum(arrTime[:, self.kEndPort[i], :, i]),
            unit='days')).date().isoformat()

def get_output_(self):
    return self.objective_value, self.solution_, self.arrTime_

def warehouse_fee(self, x):
    startTime = np.arange(self.dateSpace).reshape(1, 1, self.dateSpace, 1) * x
    arrTimeMtrx = startTime + self.tranTime.reshape(self.portSpace, \ self.portSpace,
self.dateSpace, 1) * x
    arrTime = arrTimeMtrx.copy()
    arrTimeMtrx[:, self.kEndPort.tolist(), :, range(self.goods)] = 0
    stayTime = np.sum(startTime, axis=(1, 2)) - np.sum(arrTimeMtrx, axis=(0, 2))
    stayTime[self.kStartPort.tolist(), range(self.goods)] -= self.kStartTime
    warehouseCost = np.sum(np.sum(stayTime * self.kVol, axis=1) * self.whCost)
    return warehouseCost, arrTime, stayTime

def txt_solution(self, route, order):
    """transform the cached results to text."""
    travelMode = dict(zip(zip(route['Source'], route['Destination']), route['Travel Mode']))
    txt = "Solution"
    txt += "\nNumber of goods: " + str(order['Order Number'].count())
    txt += "\nTotal cost: " + str(self.transportCost + self.whCostFinal + self.taxCost)
    txt += "\nTransportation cost: " + str(self.transportCost)
    txt += "\nWarehouse cost: " + str(self.whCostFinal)
    txt += "\nTax cost: " + str(self.taxCost)
    for i in range(order.shape[0]):
        txt += "\n-----"
        txt += "\nGoods-" + str(i + 1) + " Category: " + order['Commodity'][i]
        txt += "\nStart date: " + pd.to_datetime(order['Order Date']) \ .iloc[i].date().isoformat()
        txt += "\nArrival date: " + str(self.arrTime_['goods-' + str(i + 1)])
        txt += "\nRoute:"
        solution = self.solution_['goods-' + str(i + 1)]
        route_txt = ""
        a = 1
        for j in solution:
            route_txt += "\n(" + str(a) + ")Date: " + j[2]

```

```

        route_txt += " From: " + j[0]
        route_txt += " To: " + j[1]
        route_txt += " By: " + travelMode[j[0], j[1]]
        a += 1
        txt += route_txt
    return txt

```

```

def transform(filePath):
    order = pd.read_excel(filePath, sheet_name='Order Information')
    route = pd.read_excel(filePath, sheet_name='Route Information')
    order['Tax Percentage'][order['Journey Type'] == 'Domestic'] = 0
    route['Cost'] = route[route.columns[7:12]].sum(axis=1)
    route['Time'] = np.ceil(route[route.columns[14:18]].sum(axis=1) / 24)
    route = route[list(route.columns[0:4]) +
                   ['Fixed Freight Cost', 'Time', \ 'Cost', 'Warehouse Cost', 'Travel Mode',
'Transit Duty']] + list(
        route.columns[-9:-2])
    route = pd.melt(route, id_vars=route.columns[0:10], value_vars=route.columns[-7:] \ ,
var_name='Weekday', value_name='Feasibility')
    route['Weekday'] = route['Weekday'].replace({'Monday': 1, 'Tuesday': 2, 'Wednesday': 3,
\ 'Thursday': 4, 'Friday': 5, 'Saturday': 6, 'Sunday': 7})
    return order, route

if __name__ == '__main__':
    order, route = transform("model data.xlsx")
    m = MMT()
    m.set_param(route, order)
    m.build_model()
    m.solve_model()
    txt = m.txt_solution(route, order)
    with open("Solution.txt", "w") as text_file:
        text_file.write(txt)

```

Output:

Solution

Number of goods: 8
Total cost: 196959.0
Transportation cost: 6645.0
Warehouse cost: 1410.0
Tax cost: 188904.0

Goods-1 Category: Honey

Start date: 2018-02-01

Arrival date: 2018-02-12

Route:

(1)Date: 2018-02-01 From: Singapore Warehouse To: Malaysia Warehouse By: Truck
(2)Date: 2018-02-02 From: Malaysia Warehouse To: Malaysia Port By: Truck
(3)Date: 2018-02-03 From: Malaysia Port To: Shanghai Port By: Sea
(4)Date: 2018-02-10 From: Shanghai Port To: Shanghai Warehouse By: Truck
(5)Date: 2018-02-11 From: Shanghai Warehouse To: Wuxi Warehouse By: Truck

Goods-2 Category: Furniture

Start date: 2018-02-02

Arrival date: 2018-02-11

Route:

(1)Date: 2018-02-02 From: Malaysia Warehouse To: Malaysia Port By: Truck
(2)Date: 2018-02-03 From: Malaysia Port To: Shanghai Port By: Sea
(3)Date: 2018-02-10 From: Shanghai Port To: Shanghai Warehouse By: Truck

Goods-3 Category: Paper plates

Start date: 2018-02-03

Arrival date: 2018-02-15

Route:

(1)Date: 2018-02-03 From: Singapore Warehouse To: Malaysia Warehouse By: Truck
(2)Date: 2018-02-06 From: Malaysia Warehouse To: Malaysia Port By: Truck
(3)Date: 2018-02-07 From: Malaysia Port To: Shanghai Port By: Sea
(4)Date: 2018-02-14 From: Shanghai Port To: Shanghai Warehouse By: Truck

Goods-4 Category: Pharmaceutical drugs

Start date: 2018-02-04

Arrival date: 2018-02-15

```

Route:
(1)Date: 2018-02-04 From: Singapore Warehouse To: Malaysia Warehouse By: Truck
(2)Date: 2018-02-06 From: Malaysia Warehouse To: Malaysia Port By: Truck
(3)Date: 2018-02-07 From: Malaysia Port To: Shanghai Port By: Sea
(4)Date: 2018-02-14 From: Shanghai Port To: Shanghai Warehouse By: Truck
-----
Goods-5 Category: Cigarette
Start date: 2018-02-05
Arrival date: 2018-02-15
Route:
(1)Date: 2018-02-05 From: Wuxi Warehouse To: Shanghai Warehouse By: Truck
(2)Date: 2018-02-06 From: Shanghai Warehouse To: Shanghai Port By: Truck
(3)Date: 2018-02-07 From: Shanghai Port To: Malaysia Port By: Sea
(4)Date: 2018-02-14 From: Malaysia Port To: Malaysia Warehouse By: Truck
-----
Goods-6 Category: Apple
Start date: 2018-02-06
Arrival date: 2018-02-16
Route:
(1)Date: 2018-02-06 From: Shanghai Warehouse To: Shanghai Port By: Truck
(2)Date: 2018-02-07 From: Shanghai Port To: Malaysia Port By: Sea
(3)Date: 2018-02-14 From: Malaysia Port To: Malaysia Warehouse By: Truck
(4)Date: 2018-02-15 From: Malaysia Warehouse To: Singapore Warehouse By: Truck
-----
Goods-7 Category: Durian
Start date: 2018-02-07
Arrival date: 2018-02-08
Route:
(1)Date: 2018-02-07 From: Malaysia Warehouse To: Singapore Warehouse By: Truck
-----
Goods-8 Category: Furniture
Start date: 2018-02-08
Arrival date: 2018-02-09
Route:
(1)Date: 2018-02-08 From: Wuxi Warehouse To: Shanghai Warehouse By: Truck

```

Finding and Learnings:

We have successfully implemented the optimization Algorithm on a multimodal dataset in python.