```
machine Mach PartProc Trans
 refines Mach Part Trans sees Ctx PartProc Trans
variables processes
           processes of partition
           partition_mode process_state
invariants
  @inv proc processes \in \mathbb{P}(PROCESSES)
  @inv_proc_state process_state ∈ processes → PROCESS_STATES
  @inv proc of part processes of partition ∈ processes → PARTITIONS
  @inv readyrunsuspproc onlyin normalpart \forall p (p \in PARTITIONS \land partition mode(p) \neq PM NORMAL \Rightarrow
                                               \forall proc \cdot (proc \in processes\_of\_partition \sim [\{p\}] \Rightarrow
                                               process state(proc) \( \neq \begin{array}{c} PS \\ Ready \\ \neq \\ process \\ state(proc) \( \neq \end{array} \)
PS Running ∧ process state(proc) ≠PS Suspend))
  @inv readyrunsusp proc imply normalpart \forall proc (proc \in processes \land (process state(proc) = PS Ready \lor processes)
process state(proc)=PS Running v process state(proc)=PS Suspend)
                                               ⇒ partition_mode(processes_of_partition(proc)) = PM_NORMAL)
  @inv noproc imply notnormal \forall part \in PARTITIONS \land part \in ran(processes of partition) \land
card(processes of partition\sim[{part}])=0 \Rightarrow partition_mode(part) \neq PM_NORMAL)
  @inv normalmode imply procs \forall part \in PARTITIONS \land partition mode(part) = PM NORMAL \Rightarrow part \in
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ran(processes_of_partition) \( \card(processes_of_partition \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \( \card(processes_of_partition \) \) \( \card(processes_of_partition \) \( \card(processes_of_par
                  @inv idlemode imply noproc \forall part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow part \in PARTITIONS \land partition mode(part) = PM IDLE \Rightarrow PM IDL
ran(processes_of_partition))
                  @inv part mode partition mode ∈ PARTITIONS → PARTITION MODES
 events
                 event INITIALISATION
                                 then
                                                    @act01 partition mode = PARTITIONS × {PM COLD START}
                                                    @act00 processes = Ø
                                                    @act02 process state = Ø
                                                    @act03 processes of partition = Ø
                  end
                  event process_schedule
                                 any part proc
                                 where
                                                    @grd01 part ∈ PARTITIONS
                                                    @grd02 proc ∈ processes
                                                    @grd03 processes_of_partition(proc) = part
                                                    @grd04 partition mode(part) = PM NORMAL
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@grd05 process_state(proc) = PS_Ready v process_state(proc) = PS_Running
   then
                                         (process_state~[{PS_Running}] × {PS_Ready}))
     @act1 process_state = (process_state
                                                                                         {proc →
PS_Running}
 end
 event create_process
   any part proc
   where
     @grd01 part ∈ PARTITIONS
     @grd02 proc ∈ PROCESSES \ processes
     @grd03 partition mode(part)=PM COLD START v partition mode(part)=PM WARM START
   then
     @act01 processes = processes U {proc}
     @act02 processes_of_partition(proc) = part
     @act03 process state(proc) = PS Dormant
 end
  event partition mode transition to idle refines partition mode transition
   any part newm procs
   where
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@grd01 part ∈ PARTITIONS
     @grd02 newm ∈ PARTITION MODES
     @grd03 partition_mode(part) = PM_COLD_START v partition_mode(part) = PM_WARM_START v
partition_mode(part) = PM_NORMAL
     @grd04 newm = PM IDLE
     @grd07 procs = processes_of_partition~[{part}]
   then
     @act01 partition_mode(part) = newm
     @act22 processes = processes \ procs
     @act23 process_state = procs ← process_state
     @act24 processes of partition = procs ← processes of partition
 end
 event partition mode transition to normal refines partition mode transition
   any part newm procs procsstate
       procs2
   where
     @grd01 part ∈ PARTITIONS
     @grd02 newm ∈ PARTITION MODES
     @grd03 partition_mode(part) = PM_COLD_START v partition_mode(part) = PM_WARM_START
     @grd04 newm = PM NORMAL
```

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@grd08 card(processes_of_partition~[{part}]) > 0
     @grd09 procs = processes of partition~[{part}] \cap process state~[{PS Waiting}]
     @grd10 procs2 = processes_of_partition~[{part}] \cap process_state~[{PS\_WaitandSuspend}]
     @grd101 \ procsstate \in procs \rightarrow \{PS \ Waiting, PS \ Ready\}
   then
     @act01 partition_mode(part) = newm
     @act22 process state = (process state
                                              procsstate)
                                                             (procs2 ×{PS Suspend})
 end
  event partition_modetransition_to_coldstart
 refines partition_mode_transition
   any part newm procs
   where
     @grd01 part ∈ PARTITIONS
     @grd02 newm ∈ PARTITION_MODES
     @grd04 newm = PM COLD START
     @grd03 partition_mode(part) = PM_COLD_START v partition_mode(part) = PM_WARM_START v
partition_mode(part) = PM_NORMAL
     @grd08 procs = processes of partition~[{part}]
   then
     @act01 partition mode(part) = newm
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```
@act22 processes = processes > processes
   @act23 process_state = procs ◀ process_state
   @act24 processes_of_partition = procs ← processes_of_partition
end
event partition_modetransition_to_warmstart
refines partition mode transition
 any part newm procs
 where
   @grd01 part ∈ PARTITIONS
   @grd02 newm ∈ PARTITION MODES
   @grd04 newm = PM WARM START
   @grd09 partition_mode(part) = PM_WARM_START v partition_mode(part) = PM_NORMAL
   @grd08 procs = processes of partition~[{part}]
 then
   @act01 partition mode(part) = newm
   @act22 processes = processes \ procs
   @act23 process_state = procs ← process_state
   @act24 processes of partition ⊨ processes of partition
end
```

```
event partition_modetransition_idle_to_warmstart
refines partition mode transition
 any part newm
 where
   @grd01 part ∈ PARTITIONS
   @grd02 newm ∈ PARTITION_MODES
   @grd04 newm = PM_WARM_START
   @grd07 partition_mode(part) = PM_IDLE
 then
   @act01 partition_mode(part) = newm
end
event partition_modetransition_idle_to_coldstart
refines partition_mode_transition
 any part newm
 where
   @grd01 part ∈ PARTITIONS
   @grd02 newm ∈ PARTITION_MODES
   @grd04 newm = PM COLD START
   @grd07 partition_mode(part) = PM_IDLE
 then
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@act01 partition mode(part) = newm
  end
  event process state transition
   any part proc newstate
   where
      @grd01 part ∈ PARTITIONS
      @grd02 proc ∈ processes
      @grd03 newstate ∈ PROCESS STATES
     @grd06 processes_of_partition(proc) = part
      @grd07 partition mode(part) = PM NORMAL v partition mode(part) = PM WARM START v
partition_mode(part) = PM_COLD_START /*partition_mode(part) ≠ PM_IDLE*/
      @grd20 ((partition mode(part) = PM COLD START \vee partition mode(part) = PM WARM START) \wedge
process state(proc) = PS Dormant) ⇒ newstate = PS Waiting
      @grd21 ((partition mode(part) = PM COLD START \vee partition mode(part) = PM WARM START) \wedge
process state(proc) = PS Waiting) \Rightarrow (newstate = PS Dormant \lor newstate = PS WaitandSuspend)
      @grd29 ((partition mode(part) = PM COLD START \vee partition mode(part) = PM WARM START) \wedge
process state(proc) = PS WaitandSuspend) \Rightarrow (newstate = PS Dormant \lor newstate = PS Waiting)
      @grd22 (partition mode(part) = PM NORMAL \land process state(proc) = PS Dormant) \Rightarrow (newstate =
PS Ready v newstate = PS Waiting)
      @grd23 (partition mode(part) = PM NORMAL \land process state(proc) = PS Ready) \Rightarrow (newstate =
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PS Dormant v newstate = PS Suspend)
      @grd24 (partition mode(part) = PM NORMAL \land process state(proc) = PS Waiting) \Rightarrow (newstate =
PS Dormant \lor newstate = PS WaitandSuspend \lor newstate = PS Ready)
      @grd25 (partition mode(part) = PM NORMAL \land process state(proc) = PS Suspend) \Rightarrow (newstate =
PS Dormant v newstate = PS Ready)
      @grd28 (partition mode(part) = PM NORMAL \land process state(proc) = PS WaitandSuspend) \Rightarrow
(newstate = PS Waiting v newstate = PS Suspend v newstate = PS Dormant)
      @grd27 (partition mode(part) = PM NORMAL \land process state(proc) = PS Running) \Rightarrow (newstate =
PS Running v newstate = PS Ready v newstate = PS Waiting v newstate = PS Suspend v newstate =
PS Dormant)
   then
      @act01 process state(proc) = newstate
  end
  event process_state_transition2
   any part procs newstates
   where
      @grd01 part ∈ PARTITIONS
     @grd02 procs ⊆ processes
      @grd03 newstates ∈ procs → PROCESS_STATES
      @grd06 procs ⊆ processes of partition~[{part}]
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@grd07 partition mode(part) = PM NORMAL v partition mode(part) = PM WARM START v
partition_mode(part) = PM_COLD_START /*partition_mode(part) ≠ PM IDLE*/
      @grd20 \forall proc((proc \in procs \land (partition mode(part) = PM COLD START \lor partition mode(part) =
PM WARM START) \land process state(proc) = PS Dormant) \Rightarrow newstates(proc) = PS Waiting)
      @grd21 \forall proc ((proc \in procs \land (partition mode(part) = PM COLD START \lor partition mode(part) =
PM WARM START) \land process state(proc) = PS Waiting) \Rightarrow (newstates(proc) = PS Dormant \lor newstates(proc)
= PS WaitandSuspend))
      @grd29 \forall proc((proc \in procs \land (partition mode(part) = PM COLD START \lor partition mode(part) =
PM WARM START) \land process state(proc) = PS WaitandSuspend) \Rightarrow (newstates(proc) = PS Dormant \lor
newstates(proc) = PS Waiting))
      @grd22 \forall proc (proc \in procs \land (partition mode(part) = PM NORMAL \land process state(proc) =
PS Dormant) ⇒ (newstates(proc) = PS Ready ∨ newstates(proc) = PS Waiting))
      @grd23 \forall proc (proc \in procs \land (partition_mode(part) = PM_NORMAL \land process_state(proc) = PS_Ready)
\Rightarrow (newstates(proc) = PS Dormant \lor newstates(proc) = PS Suspend))
      @grd24 \forall proc (proc \in procs \land (partition\_mode(part) = PM\_NORMAL \land process\_state(proc) =
PS Waiting) \Rightarrow (newstates(proc) = PS Dormant \lor newstates(proc) = PS WaitandSuspend \lor newstates(proc) =
PS Ready))
      @grd25 \forall proc (proc \in procs \land (partition\_mode(part) = PM\_NORMAL \land process\_state(proc) =
PS Suspend) \Rightarrow (newstates(proc) = PS Dormant \lor newstates(proc) = PS Ready))
      @grd28 \forall proc (proc \in procs \land (partition\_mode(part) = PM\_NORMAL \land process\_state(proc) =
PS WaitandSuspend) \Rightarrow (newstates(proc) = PS Waiting \lor newstates(proc) = PS Suspend\lor newstates(proc) =
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