

An in-depth study of the syntactic analysis of graph search  
matching algorithms, to the degree of sub graphs

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August 3, 2015

# 1 Graph Basics

A Graph in Mathematics and Computer Science is a pair  $G = (V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, formed by pairs of vertices with each other. Figure 1 demonstrates the structural attributes of a simple graph graph.

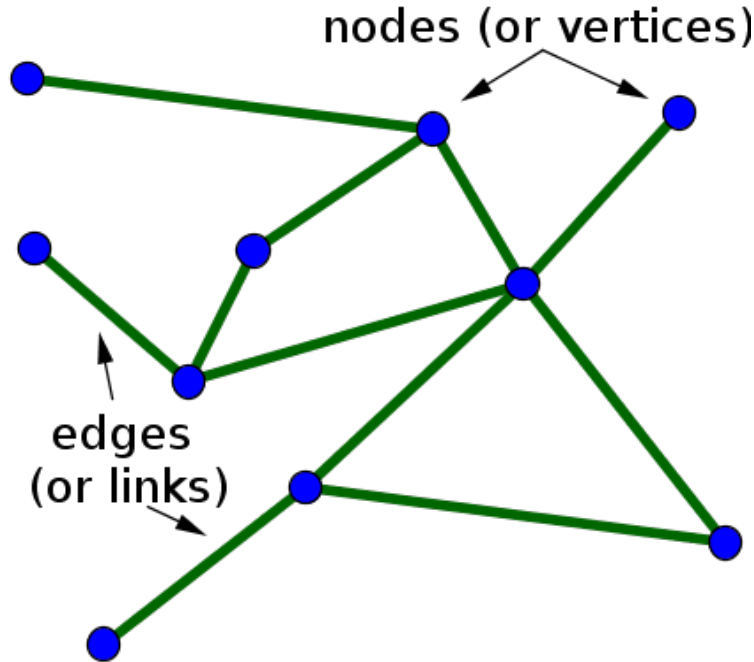


Figure 1: Representation of a graph

Graphs can either be directed or they can be undirected. This means that the edges in the graph could have an absence of direction as in the figure above, or they could have a direction showing from which vertex the edge is coming from, and to which vertex the edge is going to. The figure below demonstrates a directed graph, commonly known as a digraph. This characteristic is demonstrated by the edge 1, that goes from node a to node b, and also by edges 3 that goes from node c to node a. Note that the undirected graph mentioned above is commonly referred to as a bigraph because the direction of its edges could be perceived as going in both directions as it is not specified.

In this paper, the focus is primarily on directed graphs, and they shall be referred to as digraphs from here onward.

## 1.1 Digraph

A Digraph in mathematics is defined as a pair of vertices and edges  $(V, E)$  that are disjoint, and their respective mappings that comprise of two components, namely the initial vertex and terminal

vertex of each edge i.e. each edge has a initial vertex:  $E_i \rightarrow V_i$  and a terminal vertex  $V_j \rightarrow E_j$  for some vertices  $V_i, V_j$  in  $V$  and edges  $E_i, E_j$  in  $E$ [7], refer to the figure above.

## 1.2 Graph representation

Graphs are represented in a variety of ways, from adjacency lists, incident matrices and adjacency matrices. The algorithms that are studied in this paper make use of adjacency matrices and adjacency list representations of graphs.

### 1.2.1 Adjacency matrices

An adjacency matrix is a  $n \times n$  matrix  $A$ , with  $A(i,j) = 1$  iff  $(i,j) \in E$ [9]. This means that wherever there is an edge in the graph, it is denoted by a 1 in the matrix, places in the matrix  $A$  where there is an absence of an edge  $E$  are denoted by 0.

Figure 4 depicts the association between a graph and its adjacency matrix.

### 1.2.2 Adjacency list

An Adjacency list is vertices of a graph, of which each vertex is connected to the list. The vertices in an adjacency list point to their own list of edges that they are connected to (i.e. the list contains the edges that connect them to other vertices). Figure 4 depicts an example of an adjacency list.

## 1.3 Supergraphs and subgraphs

Let  $G_A$  be a graph defined as follows  $G_A = (V_A, E_A)$  and let  $G_B$  be another graph that is defined as follows  $G_B = (V_B, E_B)$  where  $V_A, V_B$  are sets of vertices and  $E_A, E_B$  are sets of edges. In graph theory, a graph  $G_A$  is said to be a subgraph of graph  $G_B$ , and graph  $G_B$  is said to be a supergraph of graph  $G_A$  if all the vertices and edges that are in graph  $G_A$  are also in graph  $G_B$ , that is [3]

- (1)  $V_A \subseteq V_B$ , and
- (2) Every edge of  $G_A$  is also an edge in  $G_B$ .