

5.4

5.4 An NMOS transistor that is operated with a small v_{DS} is found to exhibit a resistance r_{DS} . By what factor will r_{DS} change in each of the following situations?

- (a) V_{OV} is doubled.
- (b) The device is replaced with another fabricated in the same technology but with double the width.
- (c) The device is replaced with another fabricated in the same technology but with both the width and length doubled.
- (d) The device is replaced with another fabricated in a more advanced technology for which the oxide thickness is halved and similarly for W and L (assume μ_n remains unchanged).

(a)

$$r_{DS} = \frac{1}{g_{DS}}$$

$$g_{DS} = k_n v_{OV}$$

$$\Rightarrow r_{DS} = \frac{1}{k_n v_{OV}}$$

$$\frac{r_{DS_{new}}}{r_{DS}} = \frac{1/(k_n 2v_{OV})}{1/(k_n v_{OV})} = \frac{1}{2}$$

r_{DS} is halved.

(b)

The device width is proportional to the MOSFET transconductance parameter, k_n . So,

$$k_{n_{new}} = 2k_n.$$

As in (a),

$$\frac{r_{DS_{new}}}{r_{DS}} = \frac{1/(2k_n v_{OV})}{1/(k_n v_{OV})} = \frac{1}{2}.$$

r_{DS} is halved.

(c)

Since the aspect ratio stays the same, the MOSFET transconductance parameter, stays the same. Therefore,

r_{DS} stays the same.

(d)

As per (c), the aspect ratio stays the same and hence we will disregard the width, W , and length, L , for the total effect on r_{DS} .

The thickness of the oxide layer will have an effect on r_{DS} . The MOSFET transconductance parameter is proportional to the process transconductance parameter. The thickness of the oxide layer is inversely proportional to the process transconductance parameter. So, the MOSFET transconductance parameter, k_n , is inversely proportional to the thickness of the oxide layer, t_{ox} . We can relate this proportionality to r_{DS} :

$$k_n \propto t_{ox}^{-1}$$

$$r_{DS} \propto k_n^{-1}$$

$$\Rightarrow r_{DS} \propto t_{ox}.$$

Since t_{ox} is halved, r_{DS} is halved.

5.8

5.8 Consider an NMOS transistor operating in the triode region with an overdrive voltage V_{OV} . Find an expression for the incremental resistance

$$r_{ds} \equiv 1 / \left. \frac{\partial i_D}{\partial v_{DS}} \right|_{v_{DS}=V_{DS}}$$

Give the values of r_{ds} in terms of k_n and V_{OV} for $V_{DS} = 0$, $0.2V_{OV}$, $0.5V_{OV}$, $0.8V_{OV}$, and V_{OV} .

If $V_{DS} \ll V_{OV}$, then,

$$i_D = k_n V_{OV} V_{DS}$$

However, as V_{DS} rises,

$$i_D = k_n \left(V_{OV} - \frac{1}{2} V_{DS} \right) V_{DS}$$

where $V_{OV} - \frac{1}{2} V_{DS}$ replaces V_O due to tapering from an increase in holes at the drain.

So,

$$r_{DS} = \left[\frac{\delta i_D}{\delta v_{DS}} \right]^{-1}$$

becomes,

$$\begin{aligned} r_{DS} &= \left[\frac{1}{\delta v_{DS}} \left(k_n \left(V_{OV} - \frac{1}{2} V_{DS} \right) V_{DS} \right) \right]^{-1} \\ &= \left[k_n \left(V_{OV} \frac{1}{\delta v_{DS}} V_{DS} - \frac{1}{2} \frac{1}{\delta v_{DS}} V_{DS}^2 \right) \right]^{-1} \\ &= [k_n (V_{OV} - V_{DS})]^{-1} \end{aligned}$$

case $V_{DS} = 0$:

$$r_{DS} = \frac{1}{k_n V_{OV}}$$

case $V_{DS} = 0.2V_{OV}$:

$$r_{DS} = \frac{1}{k_n \cdot 0.8V_{OV}}$$

case $V_{DS} = 0.5V_{OV}$:

$$r_{DS} = \frac{1}{k_n \cdot 0.5V_{OV}}$$

case $V_{DS} = 0.8V_{OV}$:

$$r_{DS} = \frac{1}{k_n \cdot 0.2V_{OV}}$$

case $V_{DS} = V_{OV}$:

$$r_{DS} = \infty$$

5.24

5.24 When the drain and gate of a MOSFET are connected together, a two-terminal device known as a “diode-connected transistor” results. Figure P5.24 shows such devices obtained from MOS transistors of both polarities. Show that

(a) the i - v relationship is given by

$$i = \frac{1}{2} k' \frac{W}{L} (v - |V_t|)^2$$

(b) the incremental resistance r for a device biased to operate at $v = |V_t| + V_{ov}$ is given by

$$r \equiv 1 / \left[\frac{\partial i}{\partial v} \right] = 1 / \left(k' \frac{W}{L} V_{ov} \right)$$

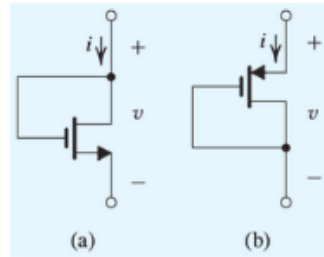


Fig. P5.24

(a)

Since $V_{DS} = V_{OV}$, the NMOS is saturated and the current through the transistor is,

$$i = \frac{1}{2} k_n (v - |V_t|)^2$$

where $i = i_{DS}$ and $v = V_{GS} = V_{DS}$.

(b)

$$\begin{aligned} r &= \left[\frac{\partial i}{\partial v} \right]^{-1} \\ &= \frac{1}{2k' \frac{W}{L} (v - V_t)} \\ &= \frac{1}{k'_n \frac{W}{L} V_{OV}} \end{aligned}$$

5.28

5.28 The NMOS transistor in Fig. P5.28 has $V_t = 0.4$ V and $k'_n(W/L) = 1$ mA/V². Sketch and clearly label i_D versus v_G with v_G varying in the range 0 to +1.8 V. Give equations for the various portions of the resulting graph.

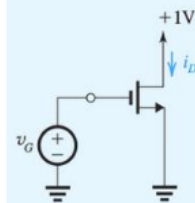


Figure P5.28

graph i_D vs V_G

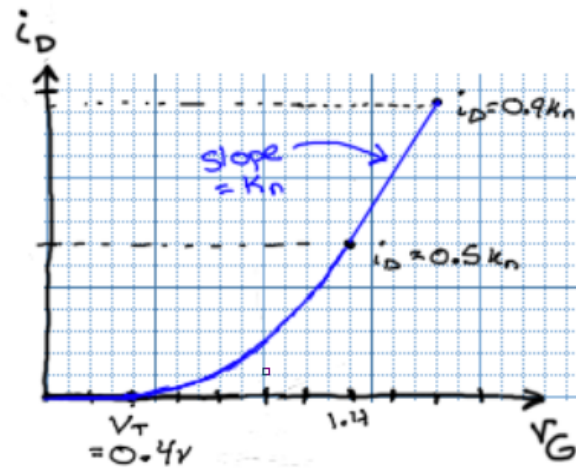


Figure 1: Note that $k_n = k'_n \frac{W}{L} = 1\text{mA}$ and represents the MOSFET transconductance parameter.

case $0V \leq V_G \leq V_t = 0.4V$

The NMOS is off since $V_G < V_t$. So,

$$i_D = 0\text{mA}$$

case $V_t = 0.4V < V_G \leq V_t + V_{DS} = 1.4V$

The NMOS is saturated since $V_{DS} \geq V_G - V_t$.

$$i_D = \frac{1}{2}k_n V_{OV}^2 = \frac{1}{2} \cdot 1\text{mA} \cdot (V_G - 0.4V)^2$$

case $V_t + V_{DS} = 1.4V \leq V_G \leq 1.8V$

The NMOS is operating in the triode region.

$$i_D = k_n \left(V_{OV} - \frac{1}{2}V_{DS} \right) V_{DS} = 1\text{mA} \cdot (V_G - 0.9)$$

5.39

5.39 A p -channel transistor for which $|V_t| = 0.8\text{ V}$ and $|V_A| = 40\text{ V}$ operates in saturation with $|v_{GS}| = 3\text{ V}$, $|v_{DS}| = 4\text{ V}$, and $i_D = 3\text{ mA}$. Find corresponding signed values for v_{GS} , v_{SD} , V_t , V_A , λ , and $k'_p(W/L)$.

$$v_{GS} = -3V$$

$$v_{SG} = 3V$$

$$v_{DS} = -4V$$

$$v_{SD} = 4V$$

$$V_t = -0.8V$$

$$V_A = -40V$$

$$\lambda = \frac{1}{V_A} = -25\text{mV}$$

$$i_D = \frac{1}{2}k_p(V_{GS} - V_t)^2(1 + \lambda v_{DS})$$

$$3\text{mA} = \frac{1}{2}k_p(-3 + 0.8)^2(1 + .025 \cdot 4)$$

$$\rightarrow k_p = 1.13\text{mA/V}^2$$

5.44

D 5.44 Design the circuit of Fig. P5.44 to establish a drain current of 0.1 mA and a drain voltage of +0.3 V. The MOSFET has $V_t = 0.5$ V, $\mu_n C_{ox} = 400 \mu\text{A/V}^2$, $L = 0.4 \mu\text{m}$, and $W = 5 \mu\text{m}$. Specify the required values for R_S and R_D .

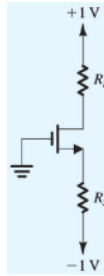


Fig. P5.44

find R_D

We know the voltage drop across R_D and the branch current. So,

$$R_D = \frac{1\text{V} - 0.3\text{V}}{0.1\text{mA}} = \boxed{7\text{k}\Omega}$$

find R_S

We need to know the voltage at the NMOS source, V_S , to figure out the voltage drop across R_S .

$$k_n = \mu_n C_{OX} \frac{W}{L} = 0.4\text{mA/V}^2 \cdot \frac{5\mu\text{m}}{0.4\mu\text{m}} = 5\text{mA/V}^2$$

Since $V_D > V_G$, the NMOS is saturated. So,

$$i_D = \frac{1}{2}k_n v_{OV}^2$$

$$0.1\text{mA} = \frac{1}{2} \cdot 5\text{mA/V}^2 \cdot v_{OV}^2$$

$$v_{OV} = 0.2\text{V}$$

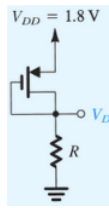
$$V_{GS} = v_{OV} + V_t = 0.2 + 0.5 = 0.7\text{V}$$

$$V_S = -0.7\text{V}$$

$$R_S = \frac{V_S - (-1\text{V})}{i_D} = \frac{-0.7 + 1}{0.1\text{mA}} = \boxed{3\text{k}\Omega}$$

5.49

D 5.49 The PMOS transistor in the circuit of Fig. P5.49 has $V_t = -0.5$ V, $\mu_p C_{ox} = 100 \mu\text{A/V}^2$, $L = 0.18 \mu\text{m}$, and $\lambda = 0$. Find the values required for W and R in order to establish a drain current of $180 \mu\text{A}$ and a voltage V_D of 1 V.



5.51

5.56

5.58