

云南大学数学与统计学院

《算法图论实验》上机实践报告

课程名称：算法图论实验	年级：2015 级	上机实践成绩：
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一、实验目的

1. 理解广度优先搜索算法的具体步骤；
2. 学会读开源的代码库，并逐步学会使用这些代码库完成扩展性的实验。

二、实验内容

1. 用形式化伪代码表示图的广度优先搜索算法；
2. 借助开源代码库，完成高质量的广度优先搜索算法编程。

三、实验平台

Windows 10 Pro 1809;
MacOS Mojave 10.14.2;
Python 2;

四、算法设计

本次理论课上所讲的 Searching 算法在图论中一般被称为广度优先的图遍历算法（Breath First Searching, BFS）。在一定规则下循环地使用这个算法可以对一个图进行遍历，并得到所有的连通子图（连通分支）。这个算法十分重要，它是 Dijkstra 算法以及更一般的 Prim 算法的基础与原型。下面对 Searching 算法（广度优先图遍历算法）进行形式化描述。

Algorithm 图的反圈遍历算法，记此算法为SEARCH

Input 图 $G = (V, E)$ ，并假定图 G 是无向图；
图 G 中的某个起点 v

Output 自 v_1 出发所有有路可到达的点以及路过的边所构成的诱导子图，记之为 ε -CLOSURE = SEARCH(G, v_1)

Begin

Step 1 // 初始化染色
for each vertex $u \in (V - \{v\})$:

$u.\text{color} = \text{White}$

$u.\mathbf{d} = \infty$

$u.\pi = \text{NIL}$

Step 2 *// 初始化给定的起点*

$v.\text{color} = \text{Gray}$

$v.\mathbf{d} = 0$

$v.\pi = \text{NIL}$

$Q = \emptyset$

ENQUEUE(Q, v)

Step 3 **while** $Q \neq \emptyset$:

$u = \text{DEQUEUE}(Q)$

for each vertex $x \in \Phi_G(u)$:

if $x.\text{color} == \text{White}$:

 ENQUEUE(Q, x)

$x.\text{color} = \text{Gray}$

$x.\mathbf{d} = u.\mathbf{d} + 1$

$x.\pi = u$

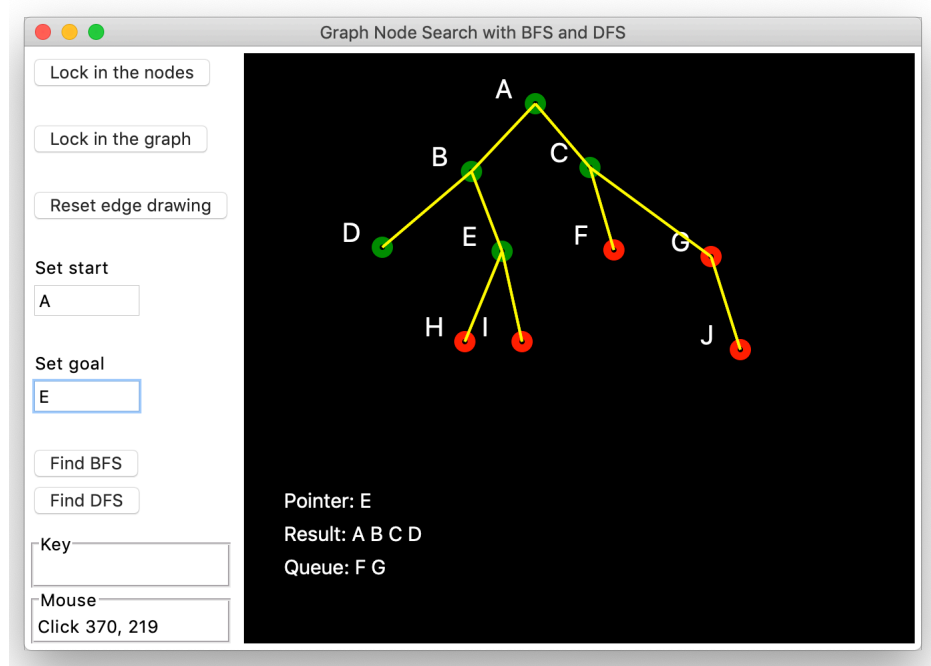
$u.\text{color} = \text{Black}$

End

根据这个算法，可以很快写出图的极大连通分支搜索算法SUB-GRAPH(G)、图的连通性判断算法IS-CONNECTED(G)等。

五、 程序代码

由于染色的时候，黑白色在白底纹的显示屏上很不突出，而把底纹改成其他颜色的话纸质打印有会出现涂抹现象，所以代码中把染色变为了具有高对比度的红绿色。



可以在下图中看出，求 A 到 E 的路时，队列有如命令行中所示的变化。

```

graph-bfs-dfs-gui — ~/graph-bfs-dfs-gui — Python source/BFS_DFS_GUI.py — 76x44
newton@newton-pc-4 ~/graph-bfs-dfs-gui
$ python2 source/BFS_DFS_GUI.py
The nodes are now locked in!
node1: A
node2: B
node3: C
node4: D
node5: E
node6: F
node7: G
node8: H
node9: I
node10: J
Graph is now set!
Start: A
Goal: E

BFS starts here:

Pointer: A
Result: A
Queue: B C

Pointer: B
Result: A B
Queue: C D E

Pointer: C
Result: A B C
Queue: D E F G

Pointer: D
Result: A B C D
Queue: E F G

Pointer: E
SUCCESS!

```

5.1 程序代码

由于 C 语言的 GUI 代码库太复杂，这里采用 Python 的 simpleGUItk 进行编程。核心语言还是 Python 2。

```

1  """
2      Title: A graph node search program in Python with the application of
3              bread first and depth first search algorithms.
4      Author: Ryan Gilera
5  """
6
7
8  import simplegui as simplegui
9
10 # Constants
11 HEIGHT = 400
12 WIDTH = 500
13 NODE_SPACE_ALLOWANCE = 20
14 EDGE_COLOR = "Yellow"
15 EDGE_SIZE = 2

```

```

16  NODE_LABEL_COLOR = "White"
17  NODE_COLOR = "Red"
18  NODE_MARK_COLOR = "Green"
19
20  # Global variables
21  start = 0
22  goal = 0
23  placeNodes = True
24  setNodesRelation = False
25  draw_relations = False
26  draw_mark_relations = False
27  setGoal = False
28  setStart = False
29  displayResult = False
30  lock_nodes = False
31  nodes = []
32
33  pos1 = [0,0]
34  pos2 = [0,0]
35  pos_lock = False
36  indx = 0
37  letter_label_default = '@'
38  letter_pos = 1
39  current_node_letters_low = []
40  current_node_letters_up = []
41
42
43  class Point:
44      def __init__(self, pos, node_colour, node_mark_colour):
45          self.pos = pos
46          self.children = []
47          self.radius = 5
48          self.colour = node_colour
49          self.mark_colour = node_mark_colour
50          self.index = 0
51          self.is_mark = False
52          self.label = '@'
53
54      def draw(self, canvas):
55          if self.is_mark == False:
56              canvas.draw_circle(self.pos, self.radius, 6, self.colour)
57          else:
58              canvas.draw_circle(self.pos, self.radius, 6, self.mark_colour)
59
60
61
62  def mouseclick(pos):
63      global pos1, pos2, pos_lock, indx, draw_relations, draw_mark_relations, nodes, indx_mark_color
64      global letter_label_default, letter_pos
65
66      # Creates new instance of point(node) if the last position of
67      # the mouseclick is not on top of a previous node
68      allow_place_node = True
69
70      if placeNodes == True:
71          if nodes: # Checks if the nodes are not empty
72              for p, location in enumerate(nodes):
73                  if ((pos[0] >= (nodes[p].pos[0]-NODE_SPACE_ALLOWANCE) and pos[0] <= (nodes[p].pos[0]+NODE_SPACE_ALLOWANCE)) and

```

```

74         (pos[1] >= (nodes[p].pos[1]-NODE_SPACE_ALLOWANCE) and pos[1] <= (nodes[p].pos[1]+NODE_SPACE_ALLOWANCE))):
75         print "Warning: Cannot create node on top of another node!"
76         allow_place_node = False
77         break
78     # Creates new instance of Point class if no nodes detected in
79     # the vicinity of mouseclick position
80     if allow_place_node == True:
81         nodes.append(Point(pos,NODE_COLOR,NODE_MARK_COLOR))
82         nodes[-1].label = chr(ord(letter_label_default) + letter_pos)
83         letter_pos += 1
84     # Else creates a node for first time
85     else:
86         nodes.append(Point(pos,NODE_COLOR,NODE_MARK_COLOR))
87         nodes[-1].label = chr(ord(letter_label_default) + letter_pos)
88         letter_pos += 1
89
90     # Sets up the edges or links
91     if setNodesRelation == True:
92
93         # If mouseclick pos is on top of a current node mark that node
94         for i, position in enumerate(nodes):
95             if ((pos[0] >= (nodes[i].pos[0]-NODE_SPACE_ALLOWANCE) and pos[0] <= (nodes[i].pos[0]+NODE_SPACE_ALLOWANCE)) and
96                 (pos[1] >= (nodes[i].pos[1]-NODE_SPACE_ALLOWANCE) and pos[1] <= (nodes[i].pos[1]+NODE_SPACE_ALLOWANCE))):
97                 if pos_lock == False:
98                     pos1[0] = pos[0]
99                     pos1[1] = pos[1]
100
101                     indx = i
102                     indx_mark_color = i
103                     pos_lock = True
104                     draw_mark_relations = True
105                     break
106
107             else:
108                 # If it is the second node that is not the same of
109                 # the first marked node, then creates a new relation/edge
110                 if i != indx:
111                     pos2[0] = pos[0]
112                     pos2[1] = pos[1]
113                     nodes[indx].children.append(i)
114                     nodes[i].children.append(indx)
115
116                     pos_lock = False
117                     draw_relations = True
118                     draw_mark_relations = False
119                     break
120             else:
121                 print "Warning: Recursion or self loop is not allowed."
122
123
124 def button_refresh_new_relation():
125     global pos_lock, pos1, pos2, nodes, draw_relations, draw_mark_relations
126
127     if lock_nodes == False and setNodesRelation == True:
128         pos_lock = False
129         draw_mark_relations = False
130         draw_relations = False
131         pos1[0] = 0
    
```

```

132     pos1[1] = 0
133     pos2[0] = 0
134     pos2[1] = 0
135
136     # This empties the list of children attribute of Point class
137     for i, child in enumerate(nodes):
138         del nodes[i].children[:]
139     else:
140         print "Warning: This action is not allowed."
141
142
143 def button_lock_nodes():
144     global placeNodes, setNodesRelation, current_node_letters_up, nodes, current_node_letters_low
145
146     # Can only lock nodes if the set-up is right
147     # Prevents locking nodes later in the program
148     if placeNodes == True and setNodesRelation == False and setStart == False and setGoal == False:
149         placeNodes = False
150         setNodesRelation = True
151
152         # Fills two new lists of all node labels(letters)
153         # for later use in input start and goal
154         if nodes:
155             for n, obj in enumerate(nodes):
156                 current_node_letters_up.append(nodes[n].label)
157
158             for let in current_node_letters_up:
159                 current_node_letters_low.append(let.lower())
160
161         print "The nodes are now locked in!"
162     else:
163         print "Warning: This action is not allowed."
164
165 def button_lock_graph():
166     global placeNodes, setNodesRelation, nodes, lock_nodes
167
168     if setNodesRelation is True:
169         placeNodes = False
170         setNodesRelation = False
171         lock_nodes = True
172
173         # Sets the index of nodes list and apply it to each index attribute of Point class
174         # for index/element reference only, for later use in BFS and DFS functions
175         for d, dot in enumerate(nodes):
176             nodes[d].index = d
177             print "node"+str(d+1)+":", nodes[d].label
178
179         # This is important
180         # This sorts the elements of children attribute list in ascending order
181         nodes[d].children.sort()
182
183         print "Graph is now set!"
184     else:
185         print "Warning: This action is not allowed."
186
187
188 def input_start_handler(start_string):
189     global start, nodes, setStart

```

```

190
191     setStart = False
192     if start_string.isdigit():
193         # Allows number as input for starting node
194         # 1 for A, 2 for B and so on and so forth
195         temp_start = int(start_string) - 1
196         for element, num in enumerate(nodes):
197             if temp_start == element:
198
199                 # Minus one because node label starts at 1 not zero(index)
200                 start = temp_start
201                 print "Start:", chr(start+65)
202                 setStart = True
203                 break
204         if setStart == False:
205             print "Warning: This number is outside of the nodes!"
206     else:
207         # Allows letter as input for starting node
208         if start_string in current_node_letters_up:
209             start = ord(start_string) - 65
210             setStart = True
211             print "Start:", chr(start+65)
212         else:
213             if start_string in current_node_letters_low:
214                 start = ord(start_string) - 97
215                 setStart = True
216                 print "Start:", chr(start+65)
217             else:
218                 print "Warning: Unknown input. Enter a number or the node letter."
219
220
221 def input_goal_handler(goal_string):
222     global goal, nodes, setGoal
223
224     setGoal = False
225     if goal_string.isdigit():
226
227         # Allows number as input for goal node
228         # 1 for A, 2 for B and so on and so forth
229         temp_goal = int(goal_string) - 1
230         for element, num in enumerate(nodes):
231             if temp_goal == element:
232                 #minus one because node label starts at 1 not zero(index)
233                 goal = temp_goal
234                 print "Goal:", chr(goal+65)
235                 setGoal = True
236                 break
237         if setGoal == False:
238             print "Warning: This number is outside of the nodes!"
239     else:
240         # Allows letter as input for goal node
241         if goal_string in current_node_letters_up:
242             goal = ord(goal_string) - 65
243             setGoal = True
244             print "Goal:", chr(goal+65)
245         else:
246             if goal_string in current_node_letters_low:
247                 goal = ord(goal_string) - 97

```



```

248         setGoal = True
249         print "Goal:", chr(goal+65)
250     else:
251         print "Warning: Unknown input. Enter a number or the node letter."
252
253
254 def button_breadth_first_search():
255     global nodes, displayResult, result_string, queue_string, pointer_string
256     displayResult = False
257     pointer_string = ""
258
259     # Resets all nodes markings (color)
260     for d, marking_obj in enumerate(nodes):
261         nodes[d].is_mark = False
262
263     in_queue_result = False
264
265     if placeNodes == False and setNodesRelation == False and setStart == True and setGoal == True:
266         print " "
267         print "BFS starts here:"
268
269         # Checks queue if defined,
270         # if it is, then go to else and empty the list; otherwise create a new list
271         try:
272             queue
273         except:
274             queue = []
275         else:
276             del queue[:]
277
278         queue.append(nodes[start])
279         queue[0].is_mark = True
280
281         try:
282             result
283         except:
284             result = []
285         else:
286             del result[:]
287
288         while queue:
289             pointer = queue[0]
290             queue.pop(0)
291
292             pointer.is_mark = True
293             print " "
294             print "Pointer:", pointer.label
295
296             if pointer.index == goal:
297                 pointer_string = "Pointer: " + pointer.label
298                 result_string = "Result: "
299                 queue_string = "Queue: "
300
301                 for obj in result:
302                     result_string += str(obj.label)
303                     result_string += " "
304                 for objt in queue:
305                     queue_string += str(objt.label)

```

```

306         queue_string += " "
307
308         displayResult = True
309         print "SUCCESS!"
310         break
311     else:
312         result.append(pointer)
313
314         for neighbor in pointer.children:
315             in_queue_result = False
316             for i in queue:
317                 #print "neighbor:", neighbor+1, "queue:", i.index+1
318                 if neighbor == i.index:
319                     in_queue_result = True
320
321             for j in result:
322                 #print "neighbor:", neighbor+1, "result:", j.index+1
323                 if neighbor == j.index:
324                     in_queue_result = True
325
326             if in_queue_result == False:
327                 for object in nodes:
328                     if object.index == neighbor:
329                         queue.append(nodes[object.index])
330
331         result_string = "Result: "
332         queue_string = "Queue: "
333         for obj in result:
334             result_string += str(obj.label)
335             result_string += " "
336         print result_string
337
338         for objt in queue:
339             queue_string += str(objt.label)
340             queue_string += " "
341         print queue_string
342
343 def button_depth_first_search():
344     global nodes, displayResult, result_string, queue_string, pointer_string
345     displayResult = False
346     pointer_string = ""
347
348     # Resets all nodes markings (color)
349     for d, marking_obj in enumerate(nodes):
350         nodes[d].is_mark = False
351
352     in_queue_result = False
353
354     if placeNodes == False and setNodesRelation == False and setStart == True and setGoal == True:
355         print " "
356         print "DFS starts here:"
357
358         # Checks queue if defined,
359         # if it is, then go to else and empty the list; otherwise create new list
360         try:
361             queue
362         except:
363             queue = []

```

```

364     else:
365         del queue[:]
366
367     #print queue
368     queue.append(nodes[start])
369     queue[0].is_mark = True
370     #print "queue:", queue
371     try:
372         result
373     except:
374         result = []
375     else:
376         del result[:]
377
378
379     try:
380         temp_list
381     except:
382         temp_list = []
383     else:
384         del temp_list[:]
385
386
387     while queue:
388         pointer = queue[0]
389         queue.pop(0)
390         #print "pointer is", pointer
391         pointer.is_mark = True
392         print " "
393         print "Pointer:", pointer.label
394
395
396         if pointer.index == goal:
397             pointer_string = "Pointer: " + pointer.label
398             result_string = "Result: "
399             queue_string = "Queue: "
400
401             for obj in result:
402                 result_string += str(obj.label)
403                 result_string += " "
404             for objt in queue:
405                 queue_string += str(objt.label)
406                 queue_string += " "
407
408             displayResult = True
409             print "SUCCESS!"
410             break
411         else:
412             result.append(pointer)
413             del temp_list[:]
414
415             for neighbor in pointer.children:
416                 in_queue_result = False
417
418                 for i in queue:
419                     #print "neighbor:", neighbor+1, "queue:", i.index+1
420                     if neighbor == i.index:
421                         in_queue_result = True

```

```

422
423         for j in result:
424             #print "neighbor:", neighbor+1, "result:", j.index+1
425             if neighbor == j.index:
426                 in_queue_result = True
427
428             if in_queue_result == False:
429                 for obj in nodes:
430                     if obj.index == neighbor:
431                         temp_list.append(nodes[obj.index])
432
433             if temp_list:
434                 queue[0:0] = temp_list
435
436             result_string = "Result: "
437             queue_string = "Queue: "
438             for obj in result:
439                 result_string += str(obj.label)
440                 result_string += " "
441             print result_string
442
443             for objt in queue:
444                 queue_string += str(objt.label)
445                 queue_string += " "
446             print queue_string
447
448
449 def draw_handler(canvas):
450     global result_string, queue_string, pointer_string
451     global placeNodes, setNodesRelation, setStart, setGoal, pos1
452
453     # Draws nodes
454     if draw_mark_relations == True and setNodesRelation == True:
455         canvas.draw_circle(nodes[indx_mark_color].pos, 15, 3, "Yellow", "Black")
456
457     if nodes:
458         for i, vertex in enumerate(nodes):
459             nodes[i].draw(canvas)
460             canvas.draw_text(nodes[i].label, (nodes[i].pos[0]-30, nodes[i].pos[1]), 20, NODE_LABEL_COLOR)
461
462     # Draws edges
463     if draw_relations == True:
464         for n, point in enumerate(nodes):
465             if nodes[n].children:
466                 for child in nodes[n].children:
467                     canvas.draw_line(nodes[n].pos, nodes[child].pos, EDGE_SIZE, EDGE_COLOR)
468
469     # Display results
470     if displayResult == True:
471         canvas.draw_text(pointer_string, (30, 345), 15, NODE_LABEL_COLOR)
472         canvas.draw_text(result_string, (30, 370), 15, NODE_LABEL_COLOR)
473         canvas.draw_text(queue_string, (30, 395), 15, NODE_LABEL_COLOR)
474
475
476     # Creates the frame window
477     frame = simplegui.create_frame("Graph Node Search with BFS and DFS", WIDTH, HEIGHT)
478
479     frame.set_mouseclick_handler(mouseclick)

```

```
480 frame.set_draw_handler(draw_handler)
481
482 # Button, input and label controls for the frame window
483 button1 = frame.add_button('Lock in the nodes', button_lock_nodes)
484 label1 = frame.add_label(' ')
485
486 button2 = frame.add_button('Lock in the graph', button_lock_graph)
487 label2 = frame.add_label(' ')
488
489 button3 = frame.add_button('Reset edge drawing', button_refresh_new_relation)
490 label3 = frame.add_label(' ')
491
492 input_start = frame.add_input('Set start', input_start_handler, 50)
493 label4 = frame.add_label(' ')
494
495 input_goal = frame.add_input('Set goal', input_goal_handler, 50)
496 label5 = frame.add_label(' ')
497
498 button4 = frame.add_button('Find BFS', button_breadth_first_search)
499 button5 = frame.add_button('Find DFS', button_depth_first_search)
500
501
502 # Program starts here
503 frame.start()
```

六、参考文献

- [1] 林锐. 高质量 C++/C 编程指南 [M]. 1.0 ed., 2001.
- [2] 算法精解: C 语言描述: <https://github.com/yourtion/LearningMasteringAlgorithms-C>
- [3] <https://github.com/Daytron/graph-bfs-dfs-gui>