# University of California, Los Angeles Department of Computer Science

#### Computer Science 143

Prof. Ryan Rosario

# Homework 2

**Solutions** 

#### Please remember the following:

- 1. Homework is mostly graded on completion. We may grade a few parts, but it will never be the majority of the grade on the assignment. So try your best, and focus on solving the problems. Consider homework (and studying the solutions) as practice for the midterm.
- 2. Homework must be submitted digitally, on CCLE. We will not do any paper grading. You can use a text file, but if you use Word, a PDF is preferred rather than a DOC file.
- 3. If there are any exercises that are difficult to do digitally (such as diagrams or math), consider scanning your drawing or math, or using a graphics program (even a readable MS Paint is fine) or Equation Editor.
- 4. For the sanity of the grader we will ask you to run the queries and submit the result. You may lose points if you only provide a query.
- 5. Solutions will be posted.

# Part 1: Text, Joins and Subqueries

For some reason, your instructor has been scraping the Caltrans website every 15 minutes or so, since 2015, to get road conditions on all of the highways within California. The data is written to MySQL. Your version of the data is hourly, and only for 2017.

A Caltrans highway conditions report looks like the following and contains conditions for individual stretches of highway ("area") typically representing a coarse area of the state: Northern, Southern, Central, Sierra Nevada etc.

```
SR 120
[IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA]
IS CLOSED FROM CRANE FLAT TO 5 MI WEST OF THE JCT OF US 395 /TIOGA PASS/
(TUOLUMNE, MONO CO) - FOR THE WINTER - MOTORISTS ARE ADVISED TO USE AN
ALTERNATE ROUTE

[YOSEMITE NAT'L PARK]
FOR YOSEMITE NAT'L PARK ROAD INFORMATION CALL 209-372-0200
```

The schema for the caltrans table looks like the following:

```
CREATE TABLE caltrans (
    reported TIMESTAMP NOT NULL DEFAULT CURRENT_TIMESTAMP,
    highway VARCHAR(6) NOT NULL,
    area VARCHAR(255),
    text TEXT NOT NULL,
    hash VARCHAR(32) NOT NULL
);
```

reported is the time the data was scraped, highway is the highway the status pertains to prefixed by its type (i.e. US101, SR1, I405), area refers to a particular part of the state or highway, and text is the update itself. Since we cannot use text as a primary key, a hash column was added.







US Highway (US)

California State Route (SR)

Interstate (I)

#### Exercises

(a) Write a query that returns a list of all the highway stretches in 2017 that were closed due to snow at any point of the year, or were closed for the winter. Order them by highway and area and give us the top 20 results, both columns in descending order.

**Hint 1:** You don't need to do anything with dates to answer this question.

**Hint 2:** Before writing a query, look at the data.

First, look at the data. Run some exploratory queries before you write your final query. We want (stretches of) highway that were closed (first condition), due to snow or were closed entirely for the winter. So we should look for stretches of highway that have "closed" in the text and also contain either "snow" or "for the winter" (this is where data intuition and exploration is important). If you look at the data, you will notice that Caltrans road conditions follow a very standardized format (it is not obvious at first though).

One preferred query:

```
SELECT
DISTINCT
highway,
area AS stretch
FROM caltrans
WHERE text like '%CLOSED%' AND (
text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%'
) ORDER BY highway DESC, area DESC
LIMIT 20;
```

This exact query yields the following exact results, but variations may give different results. It is critical that your pattern has high *coverage*, which you can only get if you look at the data. As someone who has spent considerable time living in the Eastern Sierra and also in Southern California, any different answers should contain the following important highways:

- (a) Eastern Sierra: US 395, SR 89 (Monitor Pass), SR 88 (Carson Pass), SR 4 (Ebbetts Pass), SR 270 (Bodie), SR 267 (Lake Tahoe), SR 203 (Mammoth Mountain), SR 168 (Aspendell), SR 158 (June Lake Loop). SR 108 (Sonora Pass) may be further down your list.
- (b) Southern California, Angeles Crest National Forest, Big Bear: SR 330, SR 38, SR 18
- (c) Yosemite: SR 120 (Tioga Pass, East Yosemite) may be further down your list.

highway	stretch
US395	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR89	I IN THE NORTHERN CALIFORNIA AREA & SIERRA NEVADA
SR89	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR88	IN THE CENTRAL CALIFORNIA & SIERRA NEVADA
SR4	IN THE CENTRAL CALIFORNIA AREA
SR38	IN THE SOUTHERN CALIFORNIA AREA
SR330	IN THE SOUTHERN CALIFORNIA AREA
SR33	IN THE SOUTHERN CALIFORNIA AREA
SR3	IN THE NORTHERN CALIFORNIA AREA
SR270	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR267	IN THE NORTHERN CALIFORNIA AREA
SR203	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR20	IN THE NORTHERN CALIFORNIA AREA
SR2	IN THE SOUTHERN CALIFORNIA AREA
SR18	IN THE SOUTHERN CALIFORNIA AREA
SR172	IN THE NORTHERN CALIFORNIA AREA
SR168	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR158	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR138	IN THE SOUTHERN CALIFORNIA AREA
SR130	IN THE CENTRAL CALIFORNIA AREA
SR120	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
SR108	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA
I5	IN THE NORTHERN CALIFORNIA AREA

(b) For each highway stretch found in part (a), compute the percentage of days out of the year that it was closed. If a highway stretch was closed for only a partial day, it counts as a full day. There are at least three ways to solve this problem. Try to use a method that involves a join, and a method that does not. Report the highway, area/stretch, and the percentage of days it was closed in descending order by percentage, and only gives us the 5 highest percentages and the highways and areas they belong to. You may hardcode the number of days in the year (see the note below).

#### Method 0: No Subquery with DISTINCT

I typically use GROUP BY/COUNT instead of COUNT DISTINCT because it is more explicit to me; however, it is perfectly valid to use COUNT DISTINCT for this problem and as a bonus, you do not need a subquery!

```
SELECT

highway,
area,
COUNT(DISTINCT DAYOFYEAR(reported)) * 100 / 365 AS percentage_of_days_closed_365,
COUNT(DISTINCT DAYOFYEAR(reported)) * 100 / 353 AS percentage_of_days_closed_353

FROM caltrans
WHERE text LIKE '%CLOSED%DUE TO SNOW%' OR text LIKE '%CLOSED%FOR THE WINTER%'
GROUP BY highway, area
ORDER BY percentage_of_days_closed_365 DESC;
```

Special thanks to Allan Chen for pointing this out! This method is 0.23s, which is actually slower than Method 1, but it works fine for our purposes.

#### Method 1: Select within a Select

```
SELECT
highway,
stretch,
COUNT(1) AS days_closed,
100 * COUNT(1) / 365 AS pct_closed_365,
100 * COUNT(1) / 353 AS pct_closed_353
FROM (
SELECT
highway AS highway,
area AS stretch,
DATE(reported) AS closure
FROM caltrans
WHERE text LIKE '%CLOSED%' AND (
text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
GROUP BY highway, stretch, closure
) result GROUP BY highway, stretch ORDER BY pct_closed_365 DESC;
```

We get the following results. The percentage depends on if we used 365 or 353.

highway	stretch	•		pct_closed_353	
SR89	IN THE NORTHERN CALIFORNIA AREA & SIERRA NEVADA	I 242	66.3014	68.5552	Lassen National Park (Tehama/Shasta Co) & Lake Tahoe
SR120	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	225	61.6438	63.7394	Tioga Pass (Yosemite East Entrance, Mono County)
SR203	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	224	61.3699	63.4561	Mammoth Mountain (Mono County)
SR108	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	l 203	55.6164	57.5071	Sonora Pass (Mono/Tuolumne/Alpine County Line)
SR4	IN THE CENTRAL CALIFORNIA AREA	200	54.7945	56.6572	Ebbetts Pass (Alpine County)
SR168	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	149	40.8219	42.2096	Aspendell/Bishop Creek (Inyo County)
SR270	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	145	39.7260	41.0765	Bodie Ghosttown (Mono County)
SR89	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	127	34.7945	35.9773	Monitor Pass (Alpine County)
SR2	IN THE SOUTHERN CALIFORNIA AREA	117	32.0548	33.1445	Angeles Crest Highway (LA/San Bernardino Co)
SR158	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	l 91	24.9315	25.7790	June Lake Loop (Mono County)
SR172	IN THE NORTHERN CALIFORNIA AREA	l 66	18.0822	18.6969	Lassen National Forest (Tehama County)
SR88	IN THE CENTRAL CALIFORNIA & SIERRA NEVADA	15	4.1096	4.2493	Carson Pass (Alpine County)
SR3	IN THE NORTHERN CALIFORNIA AREA	13	3.5616	3.6827	Trinity Alps Wilderness (Trinity County)
SR130	IN THE CENTRAL CALIFORNIA AREA	1 7	1.9178	1.9830	Diablo Range/Mt. Hamilton (Santa Clara County)
SR33	IN THE SOUTHERN CALIFORNIA AREA	l 4	1.0959	1.1331	Ojai (Ventura/Santa Barbara Co)
I5	IN THE NORTHERN CALIFORNIA AREA	J 3	0.8219	0.8499	Grapevine (Los Angeles/Kern County Line)
US395	IN THE CENTRAL CALIFORNIA AREA & SIERRA NEVADA	J 3	0.8219	0.8499	Eastern Sierra (Lee Vining to Bridgeport, Mono County)
SR18	IN THE SOUTHERN CALIFORNIA AREA	1 2	0.5479	0.5666	Big Bear (San Bernardino County)
SR267	IN THE NORTHERN CALIFORNIA AREA	1	0.2740	0.2833	Truckee/Lake Tahoe (Placer County)
SR330	IN THE SOUTHERN CALIFORNIA AREA	1	0.2740	0.2833	Big Bear/Running Springs (San Bernardino County)
SR20	IN THE NORTHERN CALIFORNIA AREA	1	0.2740	0.2833	Yuba Pass/Emigrant Gap (Placer County)
SR138	IN THE SOUTHERN CALIFORNIA AREA	1	0.2740	0.2833	Crestline (San Bernardino County)
SR38	IN THE SOUTHERN CALIFORNIA AREA	1 1	0.2740	0.2833	Big Bear (San Bernardino County)

0.17s

We could add another outermost query to reduce some redundancy, but it is not necessary. If we do not want to hardcode the number of days, we can use a scalar subquery by replacing 365 or 353 with the scalar subquery, but there are a host of other issues we need to deal with so we use our best judgment and hardcode using 365, or the number of days represented in the data (353). If each highway was recorded on a different number of days, we would even need to use a join. Let's not go there.

#### Method 2: Join as a Filter

We can use a join. We join the **caltrans** table with a subset of itself to filter out highway stretches that were never closed for snow or for the winter.

```
SELECT
   highway,
   stretch,
   COUNT(1) AS days_closed,
   100 * COUNT(1) / 365 AS pct_closed_365,
   100 * COUNT(1) / 353 AS pct_closed_353
FROM (
    SELECT
       c.highway AS highway,
        c.area AS stretch,
       DATE(c.reported) AS closure
   FROM caltrans c
    JOIN (
        SELECT
            DISTINCT
            highway,
            area
        FROM caltrans
        WHERE text like '%CLOSED%' AND (
           text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO NOW%')
    ) snow_highways ON c.highway = snow_highways.highway
    WHERE text like '%CLOSED%' AND (
       text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
   GROUP BY highway, stretch, closure
) closures
GROUP BY highway, stretch
ORDER BY pct_closed_365 DESC;
```

This query is slower (0.33s) than method 1 because of the join. This mimics a *left semijoin* except that a semijoin technically uses a WHERE EXISTS some\_subquery instead of the JOIN syntax. We did not discuss the semijoin in class, but we see here that we can compute one using the tools we already learned. We did not even need to know it was called a semijoin! A left semijoin is actually an inner join where matches are dictated by the table on the lefthand side of the join. Usually LEFT implies OUTER but this is not the case with the semijoin. One reason we do not cover it: it's too confusing.

# Method 3: Using an IN Subquery as a Filter

We replace the join with a WHERE clause that tests whether or not the stretch of highway is in the set of highways with snow or winter closures. Again this simulates left semijoin.

```
SELECT
   highway,
   stretch,
   COUNT(1) AS days_closed,
    100 * COUNT(1) / 365 AS pct_closed_365,
   100 * COUNT(1) / 353 AS pct_closed_353
FROM (
   SELECT
        c.highway AS highway,
        c.area AS stretch,
               DATE(c.reported) AS closure
   FROM caltrans c
    WHERE (highway, area) IN (
       SELECT
        DISTINCT
            highway,
            area
        FROM caltrans
        WHERE text like '%CLOSED%' AND (
           text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
   ) AND text LIKE '%CLOSED%' AND (text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
   GROUP BY highway, stretch, closure
) closures
GROUP BY highway, stretch
ORDER BY pct_closed_365 DESC;
```

This is slightly the slowest (0.65s) because a bunch of irrelevant rows are produced, which are then filtered out using the IN. The set containment also may require more time to process.

**Important Note:** The results should match exactly, but when there are ties, the query processor seems to slightly alter the ordering. This only affects the last few records, so we will ignore these when grading.

#### Method 4: Formal Left Semijoin

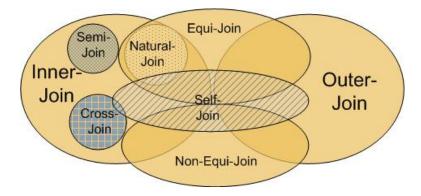
We can replace methods 2 and 3 with the formal left semijoin syntax. A left semijoin is actually an inner join where matches are dictated by the table on the lefthand side of the join. Usually LEFT implies LEFT OUTER but this is not the case with the semijoin. This is one reason we do not cover it – it is too confusing.

```
SELECT
   highway,
    stretch,
   COUNT(1) AS days_closed,
   100 * COUNT(1) / 365 AS pct_closed_365,
   100 * COUNT(1) / 353 AS pct_closed_353
FROM (
    SELECT
        c.highway AS highway,
        c.area AS stretch,
        DATE(c.reported) AS closure
    FROM caltrans c
    WHERE EXISTS (
        SELECT
            1
       FROM caltrans
        WHERE text like '%CLOSED%' AND (
            text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
    ) AND text LIKE '%CLOSED%' AND (text LIKE '%FOR THE WINTER%' OR text LIKE '%DUE TO SNOW%')
   GROUP BY highway, stretch, closure
) closures
GROUP BY highway, stretch
ORDER BY pct_closed_365 DESC;
0.16s
```

If we replace EXISTS with NOT EXISTS (or NOT IN in method 3) we get an antijoin.

Interestingly, this is the **fastest** method along with Method 1. Thus, for filtering records, we can use a subquery, or a semijoin. While a normal join and set containment works, they are slower. The COUNT DISTINCT method is also not the fastest, but it is darn simple to write, so there are tradeoffs to consider.

Part 2: Join Definitions



#### Exercises

(a) Your instructor almost included the above Venn Diagram in his lecture slides to show how different types of joins are related, but he noticed that it was wrong in at least one way. Explain at least one thing that is wrong about the diagram.

A natural join is not an inner join!!! It is not a subset of inner joins either! Yes, in MySQL the syntax NATURAL JOIN yields an INNER JOIN if there are columns in common (and a CROSS JOIN otherwise), but the concepts are not the same!

It is also unclear why the author classified a CROSS JOIN as an INNER JOIN.

Finally, outer join and inner join should overlap because an OUTER join keeps the same matches that an INNER join does, except it handles *mismatches* differently.

Overall, this Venn diagram is a mess.

#### Part 3: More Joins and Subqueries

In Homework 1, we did several things with the Bird Scooter use case, but we did not have any data to practice writing queries with. Suppose we now have trip data in the following two tables:

- trip\_starts;
- trip\_ends;

#### Exercises

(a) Write a query that computes the elapsed time of each trip. If something happened and a trip end was not recorded, the elapsed time shall be 24 hours, per Bird's policy. Print your results as trip\_id, user\_id, and trip\_length. Only show the first 5, without any special ordering.

```
SELECT
    l.trip_id,
    l.user_id,
    IFNULL(CEILING(TIMESTAMPDIFF(SECOND, l.time, r.time) / 60), 1440) AS trip_length
FROM trip_starts l
LEFT JOIN trip_ends r
ON l.trip_id = r.trip_id and l.user_id = r.user_id;
```

```
trip_id | user_id | trip_length |
-----
         20685 I
     0 |
                        2 |
     2 |
         34808
                        3 |
     3 I
         25463 l
                     1440 l
     4
         26965
                        2 |
     5 I
                        1 |
           836 l
```

(b) Write a query that computes the charge to the user for each trip. The charge is calculated as follows: \$1 flat rate per trip plus 15 cents per minute. All fractional minutes are rounded up to the next minute. Assume we did not store the results of the query from part (a). Print the first 5 results (no ordering) as trip\_id, user\_id and trip\_charge.

In the next problem, we cap the maximum daily charge is \$100. We also make the assumption that the user is billed monthly, not by ride. Unfortunately, this is not clear until reading the next part.

So, for this part, it is fine to have charges above \$100. We get the following results:

trip_id	user_id	   trip_charge
0   2   3   4   5	20685   34808   25463   26965   836	
+	-+	++

(c) Putting it all together: Suppose we bill the user at the end of the month rather than at the end of each trip. Write a query that computes the monthly charge for trips in March 2018 for each user assuming we did not store the results from parts (a) or (b). Print your results: user\_id and monthly\_total for the first five users (no ordering). In particular, how much does user\_id = 2 owe?

Answers will vary depending on where you chose to put the, well, WHERE clause. Typically, we want to filter filter filter as much as possible before doing an inner join, but we have to *very* careful when using outer joins, and it's best do filtering after the join. **Think about why.** MySQL's query processor creates a fairly efficient query plan regardless of where we put the WHERE in this case (as long as it is outside of the join), but the difference in execution time can be dramatic in systems like Hive. There are at least three different places we can put the WHERE clause.

Also, students were to cap the daily charge at \$100, but this seems to have been inadvertently deleted somewhere in my edits.

Regardless of method, we get the following results:

4	++
user_id	monthly_total
0   1   2   3   4	4.05     314.05
+	++

If we do not cap at \$100, we may get the following which is also accepted. We can see the difference between the total and the capped total.

+	user_id	+   trips	monthly_total	month_total_capped
	0 1 2		4.05   665.05	4.05   314.05
	3 4	8   10	11.90     444.55	11.90     210.55

#### Method 1: WHERE in Same Subquery as LEFT JOIN

```
SELECT
    user_id,
   SUM(daily_total) AS monthly_total
FROM (
   SELECT
        LEAST(100, SUM(trip_charge)) AS daily_total
   FROM (
        SELECT
           trip_id,
            user_id,
            time.
           trip_length * 0.15 + 1.00 AS trip_charge
        FROM (
           SELECT
                1.trip_id AS trip_id,
               1.user_id AS user_id,
               DATE(1.time) AS time,
               IFNULL(CEILING(TIMESTAMPDIFF(SECOND, 1.time, r.time) / 60), 1440) AS trip_length
            FROM trip_starts 1
            LEFT JOIN trip_ends r
            ON 1.trip_id = r.trip_id and 1.user_id = r.user_id
            WHERE MONTH(1.time) = 3 AND YEAR(1.time) = 2018
            -- right side time is NULL, so don't use it to filter!
        ) durations
   ) charges
   GROUP BY user_id, DATE(time)
) daily
GROUP BY user_id;
```

# Method 2: WHERE in Subquery Outside LEFT JOIN

```
SELECT
   user_id,
   SUM(daily_total) AS monthly_total
FROM (
       LEAST(100, SUM(trip_charge)) AS daily_total
   FROM (
       SELECT
           trip_id,
           user_id,
           time.
           trip_length * 0.15 + 1.00 AS trip_charge
        FROM (
           SELECT
               1.trip_id AS trip_id,
               1.user_id AS user_id,
               DATE(1.time) AS time,
               IFNULL(CEILING(TIMESTAMPDIFF(SECOND, 1.time, r.time) / 60), 1440) AS trip_length
            FROM trip_starts 1
           LEFT JOIN trip_ends r
           ON 1.trip_id = r.trip_id and 1.user_id = r.user_id
        ) durations
        WHERE MONTH(time) = 3 AND YEAR(time) = 2018
    ) charges
   GROUP BY user_id, DATE(time)
) daily
GROUP BY user_id;
```

# Method 3: WHERE in Outermost Query

```
SELECT
   user_id,
   COUNT(trip_id) AS trips,
   SUM(trip_charge) AS monthly_total
FROM (
    SELECT
       trip_id,
       user_id,
       start_time,
       LEAST(100.00, trip_length * 0.15 + 1.00) AS trip_charge
       SELECT
           1.trip_id AS trip_id,
           1.user_id AS user_id,
           1.time AS start_time,
           IFNULL(CEILING(TIMESTAMPDIFF(SECOND, 1.time, r.time) / 60),
               1440) AS trip_length
       FROM trip_starts 1
       LEFT JOIN trip_ends r
       ON 1.trip_id = r.trip_id and 1.user_id = r.user_id
) charges
WHERE MONTH(start_time) = 3 AND YEAR(start_time) = 2018
GROUP BY user_id;
```

# Wrong Method 1: Including the End Date in a Filter

If you got a charge of \$14.05 for user\_id = 2, you likely did this, or used the wrong join type. Remember that when there is no end time, the attributes in the result from the left join related to the right hand table will be NULL. So, by applying a filter with month and year on end\_time we remove all of the mismatches because MONTH(NULL)  $\neq$  3! So, the user gets charged for the completed trips, but never gets charged for the trips that did not have an end time.

```
SELECT
    user_id,
    SUM(daily_total) AS monthly_total
    SELECT
        user_id,
        LEAST(100, SUM(trip_charge)) AS daily_total
    FROM (
        SELECT
           trip_id,
            user_id,
           time,
            trip_length * 0.15 + 1.00 AS trip_charge
        FROM (
            SELECT
               1.trip_id AS trip_id,
                1.user_id AS user_id,
                DATE(1.time) AS time,
               IFNULL(CEILING(TIMESTAMPDIFF(SECOND, 1.time, r.time) / 60), 1440) AS trip_length
            FROM trip_starts 1
            LEFT JOIN trip_ends r
            ON 1.trip_id = r.trip_id and 1.user_id = r.user_id
            WHERE MONTH(1.time) = 3 AND MONTH(r.time) = 3
               AND YEAR(1.time) = 2018 AND YEAR(r.time) = 2018
            -- right side time is NULL, so don't use it to filter!
       ) durations
   ) charges
   GROUP BY user_id, DATE(time)
) daily
GROUP BY user_id LIMIT 5;
```

#### Wrong Method 2: Using ON Instead of WHERE in OUTER Join

We get the wrong answer if we do this. Why? Think about how the join will differ when the filter is carried out *before* the outer join. This should work fine for inner join though.

```
ON 1.trip_id = r.trip_id AND 1.user_id = r.user_id AND
    MONTH(1.time) = 3 AND YEAR(1.time) = 2018
```

Note that we can place some WHERE restrictions in the ON and in some systems this makes a difference for efficiency; however, it does not work well for an OUTER join.

(d) In the solution set for Homework 1, it was mentioned that another way we can record starts and ends of trips was to use one table, 2 rows per trip: one row representing the start and a second row representing the end of the trip. We would then have an ENUM or BIT that specifies whether the row refers to a start or an end. If we wanted to use this one single table as the basis to charge users, what type of join would we need to compute?

Self left [outer] equijoin.