EM - Expectation Maximisation Algorithm

Assignment 1

E-step deduction: Please see attachment E-step.pdf

M-step deduction of the item a): Please see attachment M-step.pdf

Assignment 2

K-Means error: 16.4192 %GMM error: 11.9911 %

Both approaches were evaluated on the full set of images and the final result was obtained as an arithmetic mean.

Better result was given by GMM approach. This result is probably caused by better segmentation of the pixels where in GMM every pixel has a probability that it belongs to one of the segments. But in K-Means there are no probabilities, only hard assignemnts to one segment. Another reason can be that Gaussian distribution is more flexible in the shape. K-Means is just circle around the center.

Assignment 3

• EM error: 1.0645 %

Comparing to the baseline models the EM algorithm has a better error. This value can be further improved. The final value was obtained by using condition to end the main cycle.

The final shape model is clearer than segmentations from the baseline models.

The final errors for each image:

- hand 00: 1.3577854671280276 %
- hand 01: 1.1737024221453287 %
- hand 02: 0.6131487889273356 %
- hand 03: 1.645674740484429 %
- hand 04: 0.8899653979238755 %
- hand 05: 1.582006920415225 %
- hand 06: 0.546712802768166 %
- hand 07: 0.9411764705882352 %
- hand 08: 1.0740484429065744 %
- hand 09: 1.4062283737024222 %
- hand 10: 0.22422145328719725 %
- hand 11: 1.3923875432525952 %
- hand 12: 0.584083044982699 %

- hand 13: 0.7003460207612457 %
- hand 14: 1.0325259515570935 %
- hand 15: 1.015916955017301 %
- hand 16: 1.6235294117647059 %
- hand 17: 1.6069204152249132 %
- hand 18: 1.5349480968858131 %
- hand_19: 0.4221453287197232 %
- hand 20: 0.6463667820069204 %
- hand 21: 0.7944636678200692 %
- hand 22: 1.3301038062283737 %
- hand 23: 1.1294117647058823 %
- hand 24: 1.346712802768166 %
- hand 25: 1.4214532871972319 %
- hand 26: 0.9231833910034601 %
- hand 27: 1.5847750865051902 %
- hand 28: 1.0878892733564014 %
- hand 29: 1.6498269896193771 %
- hand 30: 1.678892733564014 %
- hand 31: 1.0961937716262975 %
- hand 32: 1.2470588235294118 %
- hand 33: 0.93840830449827 %
- hand 34: 0.3875432525951557 %
- hand 35: 0.754325259515571 %
- hand 36: 1.6027681660899653 %
- hand_37: 0.3889273356401384 %
- hand 38: 0.560553633217993 %
- hand 39: 1.511418685121107 %
- hand 40: 0.43737024221453286 %
- hand 41: 0.6048442906574395 %
- hand 42: 0.39031141868512115 %
- hand 43: 0.9176470588235295 %
- hand_44: 0.754325259515571 %
- hand 45: 1.5875432525951558 %
- hand 46: 1.87681660899654 %
- hand 47: 1.835294117647059 %
- hand 48: 1.0768166089965396 %
- hand 49: 0.3003460207612456 %