



AVT-331, L2 Problem (Sea Vehicle): DTMB 5415 Hull-shape Optimization for Resistance Minimization in Calm Water

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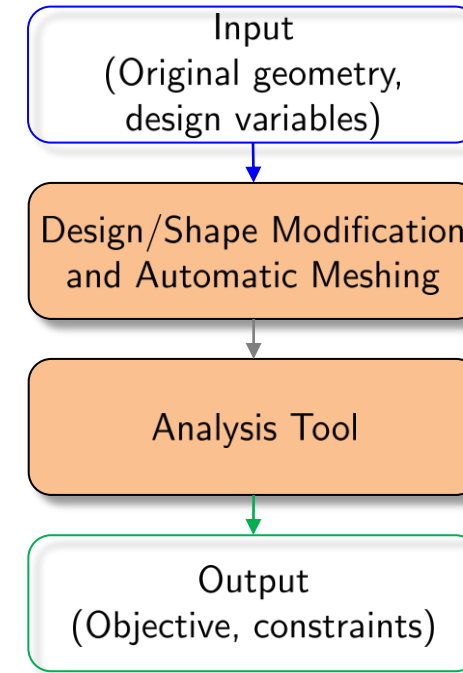
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28/09/2021

The Tool and the L2 Benchmark

□ Tool components:

- Numerical solver based on linear potential flow
- Geometry modification
- Automatic meshing
- Variable-fidelity capability given by
 - Variable computational grid
 - Variable coupling (between hydro loads and rigid body equations of motion, 2DoFs)



□ L2 problem:

- Hull: DTMB 5415
- Objective: Resistance reduction in calm water at $Fr=0.28$
 - Even keel
- Constraints: geometrical equalities and inequalities



L2 problem: DTMB 5415 Hull-shape Optimization

Objective

- Model-scale resistance reduction in calm water at $Fr=0.28$ (20kn in full scale)

Constraints

- Fixed length between perpendiculars (L_{pp})
- Fixed displacement (∇)
- $\pm 5\%$ variation of beam (B) and draft (T)
- Reserved volume (V) for the sonar in the dome

$$\begin{aligned} &\text{minimize} && R_T(\mathbf{x}) && \text{with } \mathbf{x} \in \mathbb{R}^N \\ &\text{subject to} && L_{pp}(\mathbf{x}) = L_{pp0} \\ &\text{and to} && \nabla(\mathbf{x}) = \nabla_0, \\ & && |\Delta B(\mathbf{x})| \leq 0.05 B_0, \\ & && |\Delta T(\mathbf{x})| \leq 0.05 T_0, \\ & && V(\mathbf{x}) \geq V_0, \\ & && -1 \leq x_i \leq 1 && \forall i = 1, \dots, N \end{aligned}$$



Arleigh Burke-class destroyer (from military.com)



Arleigh Burke-class destroyer model: DTMB 5415

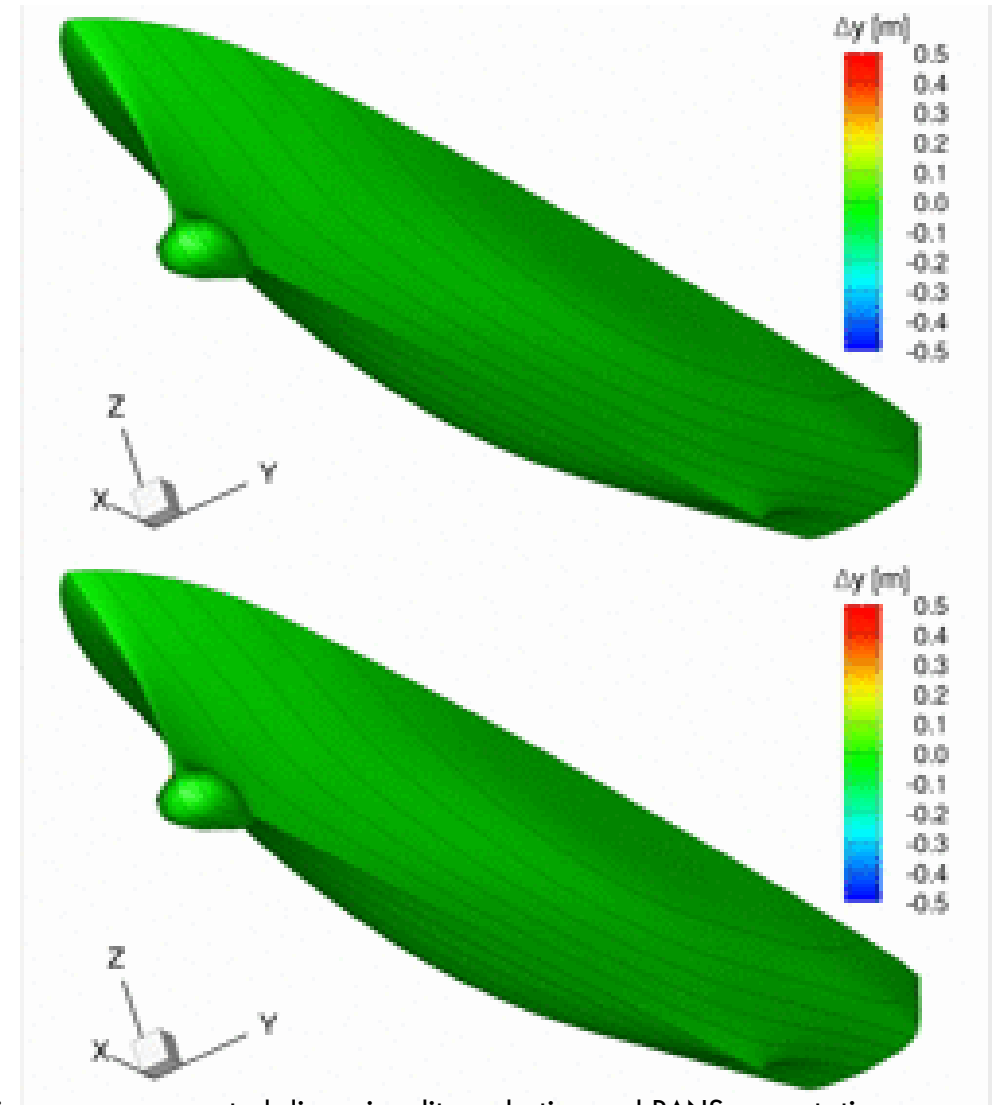
Hull-shape Modification

- ❑ Shape modification based on an original design space composed by $M=27$ global modification functions
- ❑ Optimization on a reduced design space based on **physics-informed/augmented dimensionality reduction** providing $N=14$ orthogonal basis functions (ψ)

$$\begin{array}{c} \text{Modified} \\ \text{geometry} \end{array} = \begin{array}{c} \text{Shape} \\ \text{modification} \\ \text{vector} \end{array} \begin{array}{c} \text{Original} \\ \text{geometry} \end{array} + \delta(\mathbf{u}, \mathbf{x}) \longrightarrow \delta(\mathbf{u}, \mathbf{x}) = \sum_{i=1}^N x_i \psi_i(\mathbf{u})$$

Physics-informed dimensionality reduction

Shape modification examples



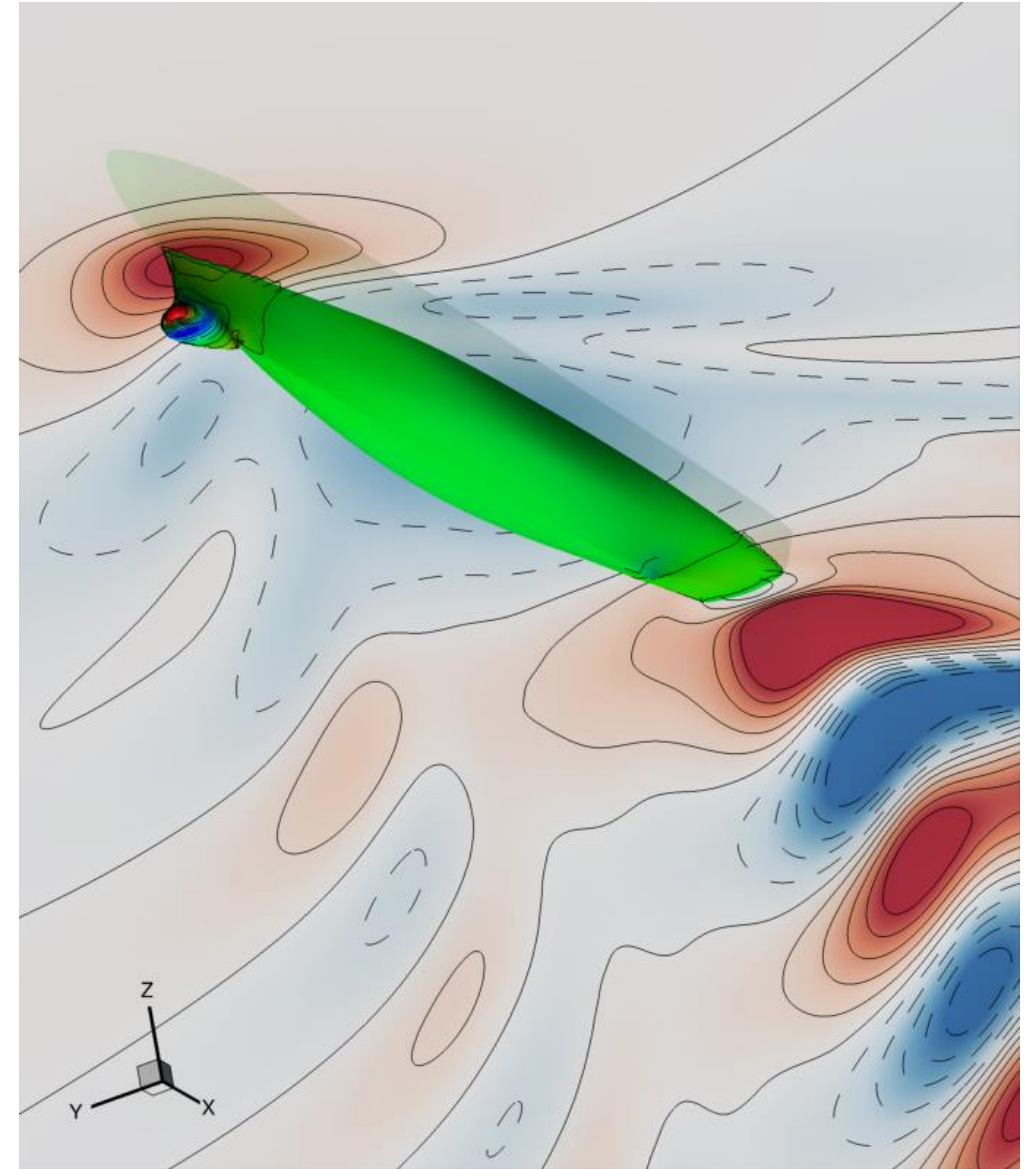
- ❖ Serani, A., Diez, M., Wackers, J., Visonneau, M., & Stern, F. (2019). Stochastic shape optimization via design-space augmented dimensionality reduction and RANS computations. In AIAA Scitech 2019 Forum (p. 2218).
- ❖ Serani, A., Stern, F., Campana, E. F., & Diez, M. (2021). Hull-form stochastic optimization via computational-cost reduction methods. *Engineering with Computers*, 1-25.

Hydrodynamic Solver

Wave Resistance Program (WARP)

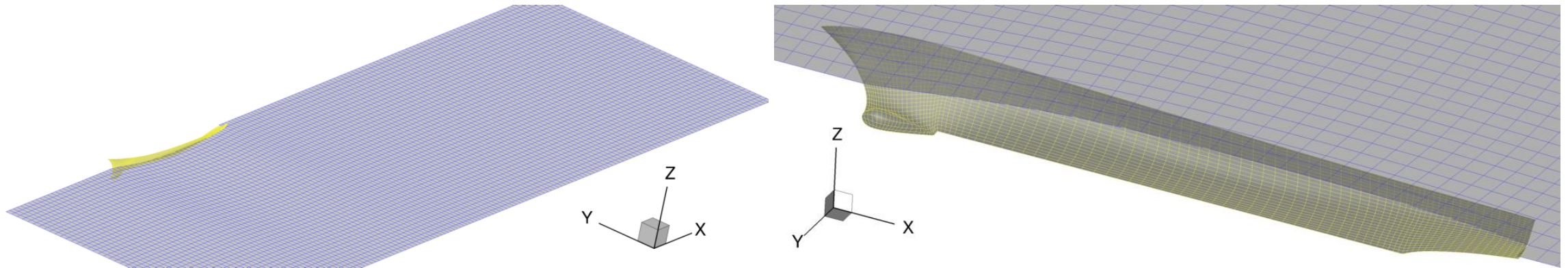
- ❑ Developed at CNR-INM (former CNR-INSEAN)
- ❑ Linear potential flow
- ❑ Dawson (double-model) linearization
- ❑ Pressure integral for wave resistance
- ❑ Flat-plate approximation for frictional resistance, based on local Reynolds number
- ❑ Coupling with body equation of motions (2 DoF) given a fixed tolerance

❖ Bassanini, P., Bulgarelli, U., Campana, E. F., and Lalli, F., “The wave resistance problem in a boundary integral formulation,” *Surveys on Mathematics for Industry*, Vol. 4, 1994, pp. 151–194.



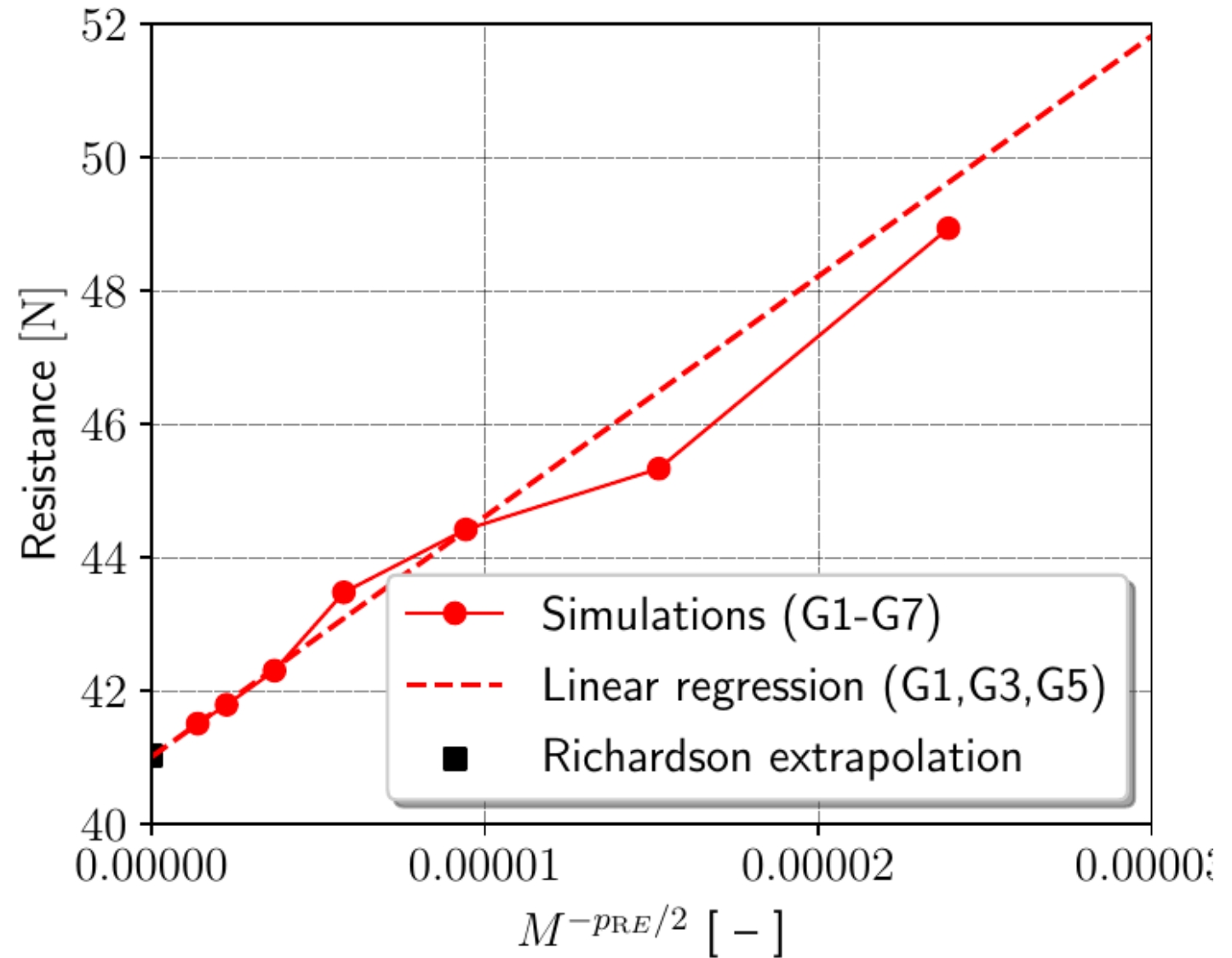
Free-surface and hull discretization

Grid/fidelity level	Refinement ratio	Free-surface	Hull	Number of elements (N)
G1	$2^{0.25}$	150 x 50	180 x 50	16.5k
G2		126 x 42	151 x 42	11.6k
G3		106 x 35	127 x 35	8.2k
G4		89 x 29	107 x 29	5.7k
G5		76 x 25	90 x 25	4.2k
G6		64 x 21	76 x 21	2.9k
G7		54 x 18	64 x 18	2.1k



Numerical Grids – Resistance Grid Convergence

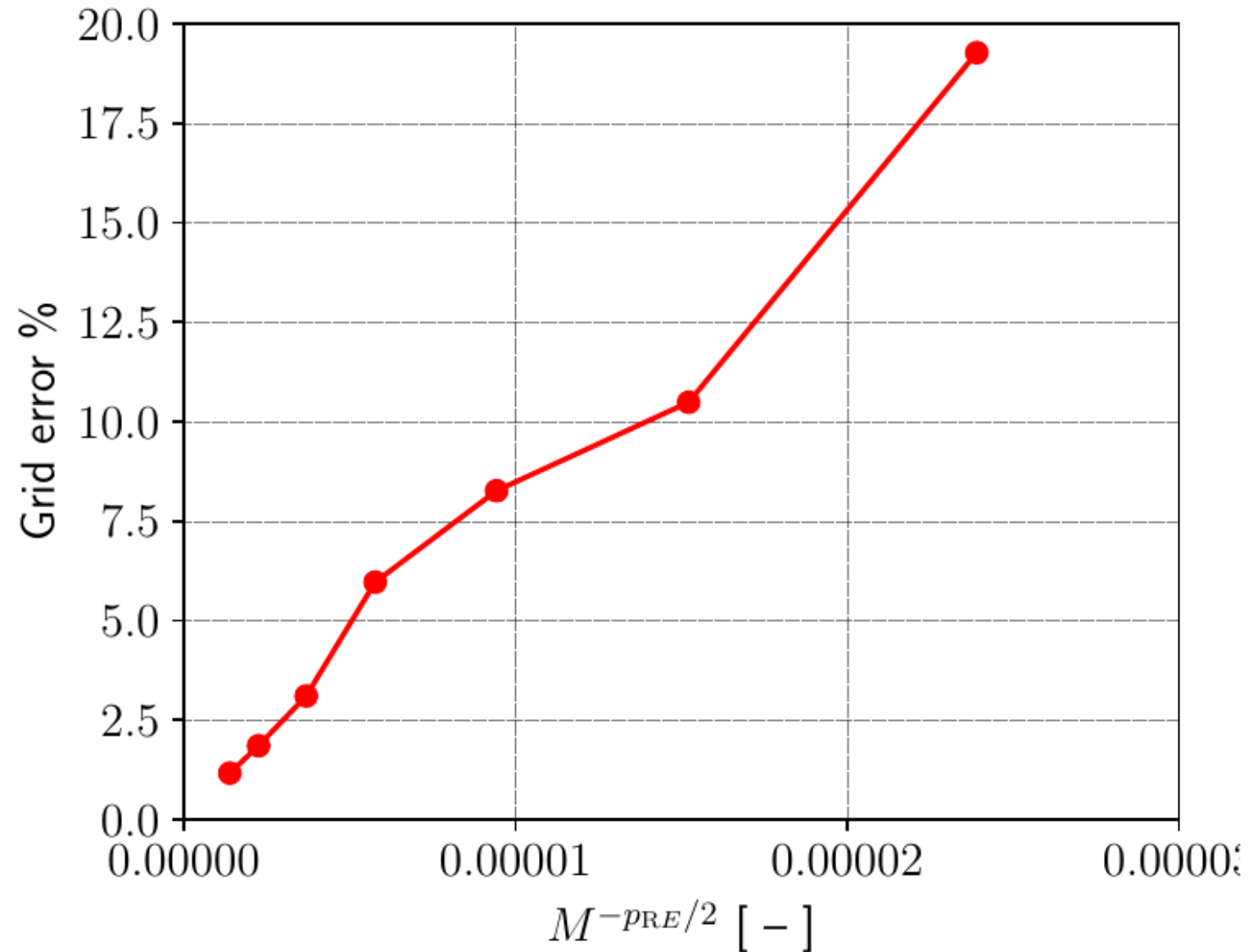
- Grid convergence is in the asymptotic range
- Coarser grids (G6, G7) are far from the linear regression
- The use of extra-coarse grids have to be done carefully



← Numerical accuracy

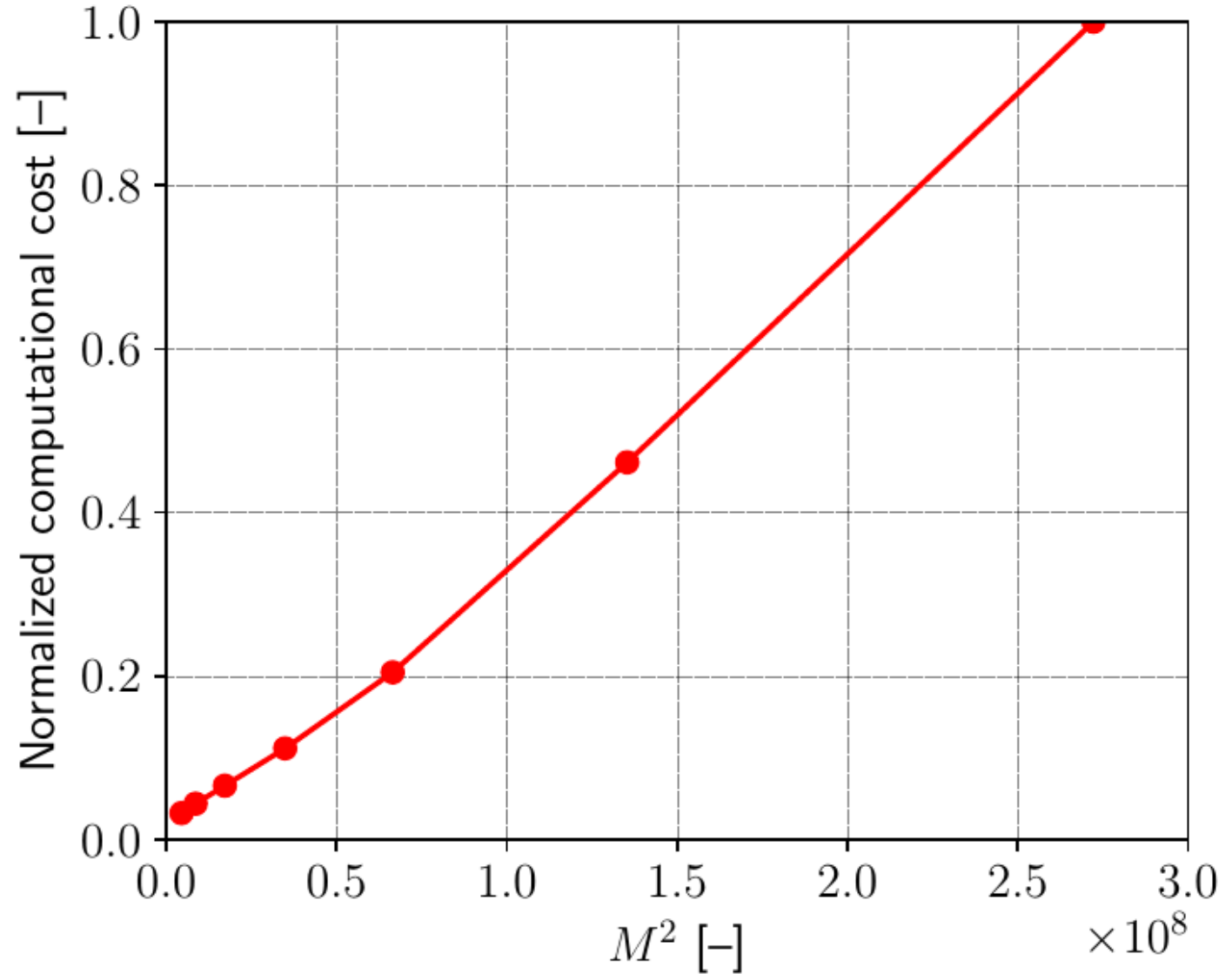
Numerical Grids – Resistance Grid Error

- Reference solution is estimate via Richardson extrapolation (RE) of G1, G3, G5 triplet
- Grid levels error are evaluated with respect to RE
- Grid errors go from 20 (G7, coarsest) to 1% (G1, finest)



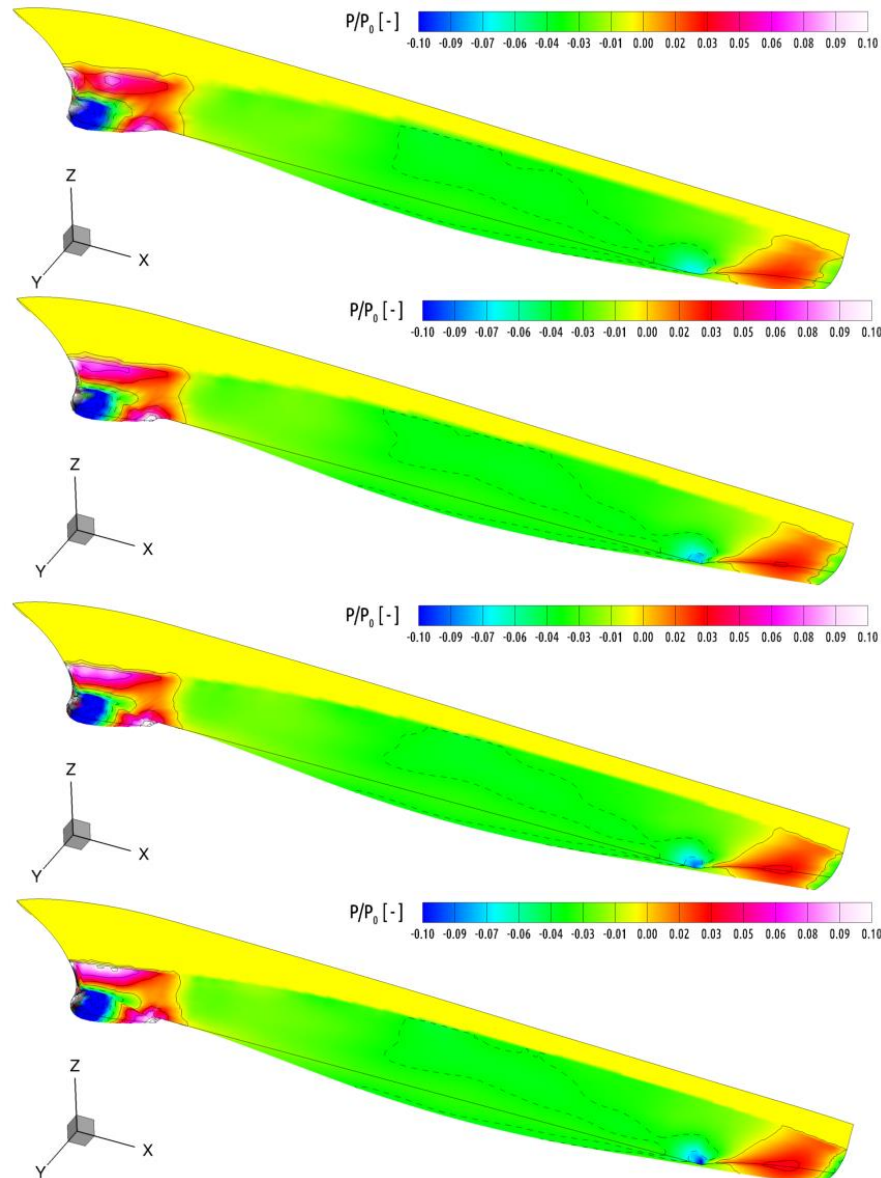
Numerical Grids – Normalized CPU Time Convergence

- CPU time normalized by the highest-fidelity (G1) CPU time cost
- Computational cost increase with a quadratic trend
- Computational cost ratio:
 - 1.00, 0.46, 0.20, 0.11, 0.07, 0.04, 0.03



Numerical accuracy

Numerical Grids – Hull Pressure Field and Wave Elevation Patterns



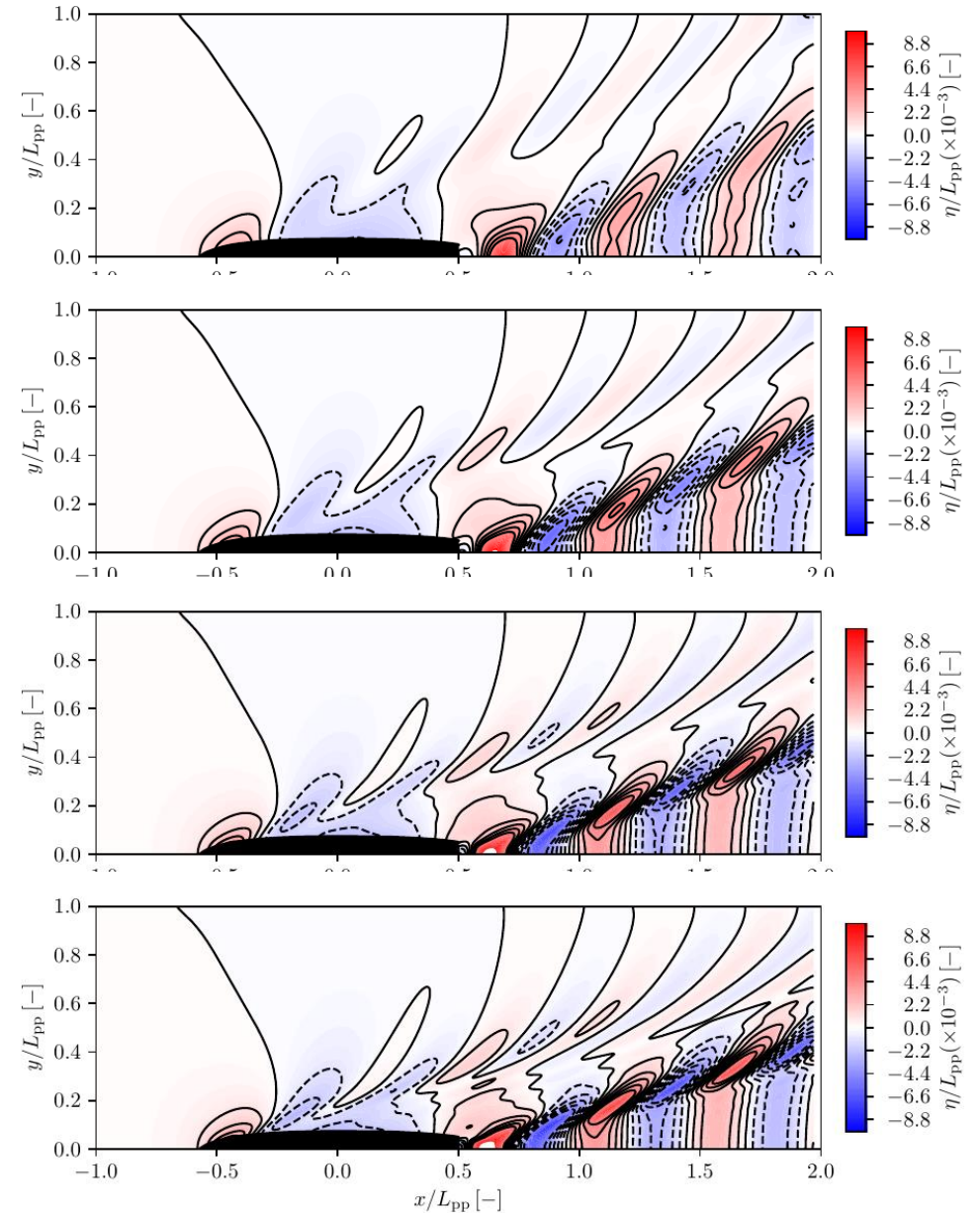
G7

G5

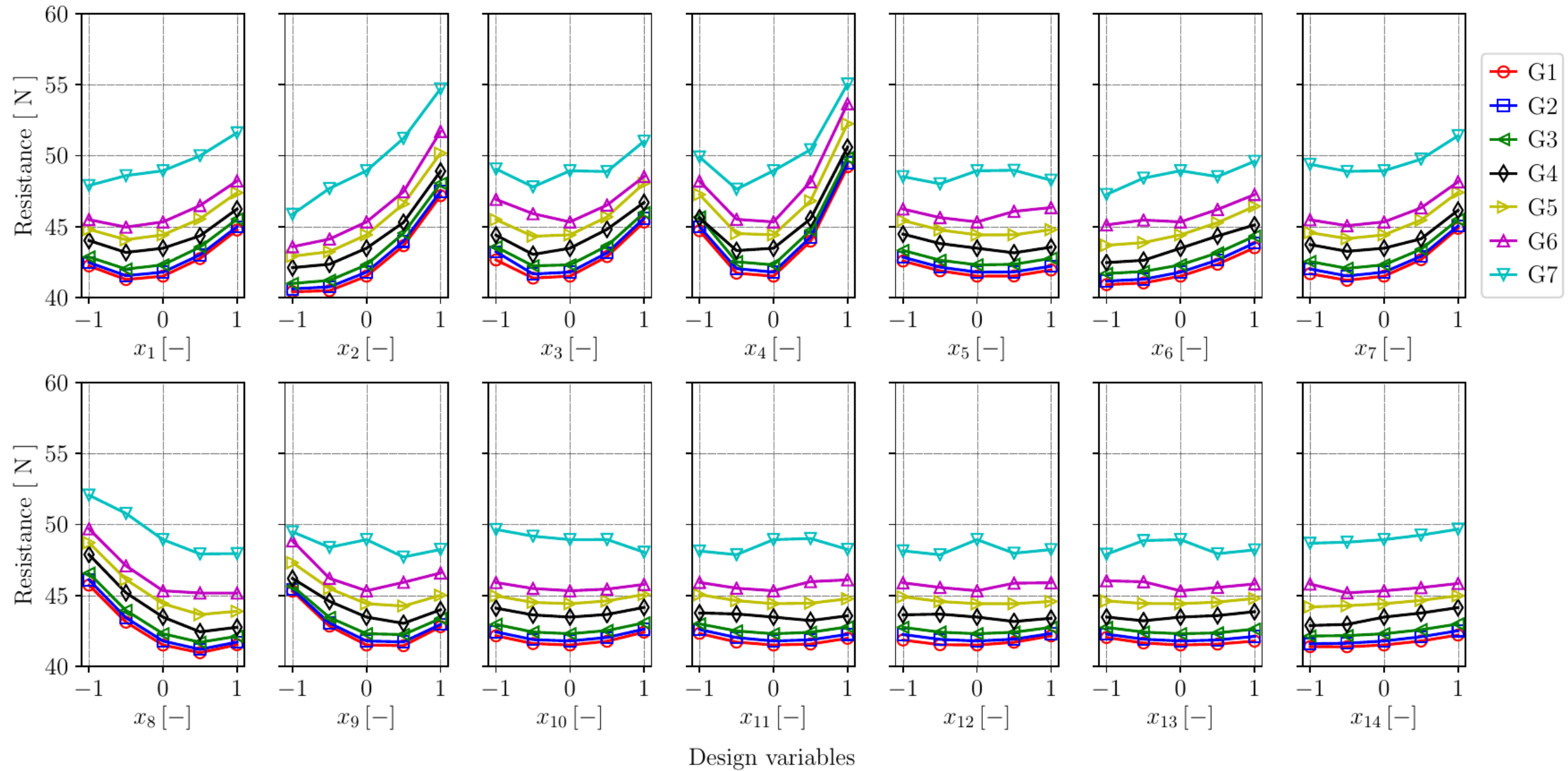
G3

G1

Numerical accuracy



Sensitivity Analysis – 0 DoF



Distributed Package

❑ Compiled fortran code (tested on **Linux and Windows Linux Subsystem**)

- Compiled with both *gfortran* and *ifort*
- External libraries needed:
 - *lapack* and *blas* (for GNU compiler)
 - *mkl* or *lapack* and *blas* (for Intel compiler)
 - *openMP* (not mandatory)

❑ Source code with makefile

❑ For use:

- Input namelist (SBDF.nml) needs to be edited
 - Fidelity level can be defined selecting the grid level and/or the coupling accuracy
- Design variables file (variables.inp)

Package to be Distributed and Timeline

- **Package uploaded on GitLab repository**

➤ <https://gitlab.com/qudo046/avt-331-benchmarks/-/tree/master/sea>

The screenshot shows the GitLab interface for the 'AVT-331 Benchmarks' repository. The left sidebar contains navigation links: 'Project overview', 'Repository', 'Files', 'Commits', 'Branches', 'Tags', 'Contributors', 'Graph', and 'Compare'. The main content area shows the repository path 'Domenico Quagliarella > AVT-331 Benchmarks > Repository'. Below this, there's a breadcrumb 'master > avt-331-benchmarks / sea /' and buttons for 'History', 'Find file', 'Web IDE', 'Clone', and a download icon. A commit message 'Uploaded L2 Sea problem package with compiled binaries (both Intel and GNU) along with source files' by 'Andrea Serani' is shown. Below this is a table of commits:

Name	Last commit	Last update
..		
.gitkeep	L2 sea benchmark folder created	1 hour ago
NATO-AVT-331-Sea-L2_problem.zip	Uploaded L2 Sea problem package with compiled binaries (b...	1 hour ago