

Two Way ANOVA Calculator

Factorial ANOVA - Balanced design

Fixed effects, Mixed effects, Random effects and Mixed repeated measures

[Video](#) [Information](#) [One way ANOVA](#) [Levene's test](#)

Model:

Fixed effect (A-Fixed, B-Fixed) - no repeats

Significance level (α):

0,05

Effect:

Medium

Effect Size:

0,25

Step by step

Interaction

With interaction

Outliers:

Included

Effect type:

f^2

Digits:

4

- Enter raw data directly
- Enter raw data from excel

Enter sample data directly

Balanced two Factor ANOVA with Replication - several values per cell. The data should be separated by Enter or , (comma).
ANOVA without Replication - one value per cell.

The tool ignores empty cells or non-numeric cells.

Var A \ Var B	Conventional					Assertiveness-based						
Novice	4	2	4	14	4	24	2	1	2	16	2	12
Expert	5	5	7	16	5	55	2	1	3	20	3	11

[Calculate](#) [Insert column](#) [Delete column](#) [Insert row](#) [Delete row](#) [Clear](#) [Load example](#)

Enter sample data from excel

[Calculate](#) [Clear](#) [Validate](#) [Load example](#) [Load last run](#)

You may copy the data from Excel, Google sheets or any tool that separate the data with Tab and Line Feed. Copy the data, one block of consecutive columns includes the header, and paste. Click to see example:

[How to do with R?](#)

ANOVA table

Hover over the cells for formulas and calculation.

Source	DF	Sum of Square (SS)	Mean Square (MS)	F Statistic (df ₁ ,df ₂)	P-value
Factor A - rows (A)	1	23.181	23.181	0.7795 (1,1868)	0.3774
Factor B - columns (B)	1	30.2585	30.2585	1.0175 (1,1868)	0.3132
Interaction AB	1	14.1141	14.1141	0.4746 (1,1868)	0.4911
Error	1868	55548.7455	29.737		
Total	1871	55616.2991	29.7254		



Two sample ANOVA - fixed test, using F distribution (right-tailed)

Factor - A

1. H_0 hypothesis

Since the p-value > α , H_0 can not be rejected.

The averages of all groups assume to be equal.

In other words, the difference between the averages of all groups is not big enough to be statistically significant.

A non-significance result can not prove that H_0 is correct, only that the null assumption can not be rejected.

2. P-value

The p-value equals 0.3774, ($P(x \leq 0.7795) = 0.6226$). It means that the chance of type I error, rejecting a correct H_0 , is too high: 0.3774 (37.74%). The larger the p-value the more it supports H_0 .

3. Test statistic

The test statistic F_A equals 0.7795, which is in the 95% region of acceptance: $[-\infty : 3.8464]$.

4. Effect size

The observed effect size η^2 is **very small**, **0.00042**. This indicates that the magnitude of the difference between the average is very small.

Factor - B

1. H_0 hypothesis

Since the p-value > α , H_0 can not be rejected.

The averages of all groups assume to be equal.

In other words, the difference between the averages of all groups is not big enough to be statistically significant.

A non-significance result can not prove that H_0 is correct, only that the null assumption can not be rejected.

2. P-value

The p-value equals 0.3132, ($P(x \leq 1.0175) = 0.6868$). It means that the chance of type I error, rejecting a correct H_0 , is too high: 0.3132 (31.32%). The larger the p-value the more it supports H_0 .

3. Test statistic

The test statistic F_A equals 1.0175, which is in the 95% region of acceptance: $[-\infty : 3.8464]$.

4. Effect size

The observed effect size η^2 is **very small**, **0.00054**. This indicates that the magnitude of the difference between the average is very small.

Interaction AB

1. H_0 hypothesis

Since the p-value > α , H_0 can not be rejected.

The averages of all groups assume to be equal.

In other words, the difference between the averages of all groups is not big enough to be statistically significant.

A non-significance result can not prove that H_0 is correct, only that the null assumption can not be rejected.

2. P-value

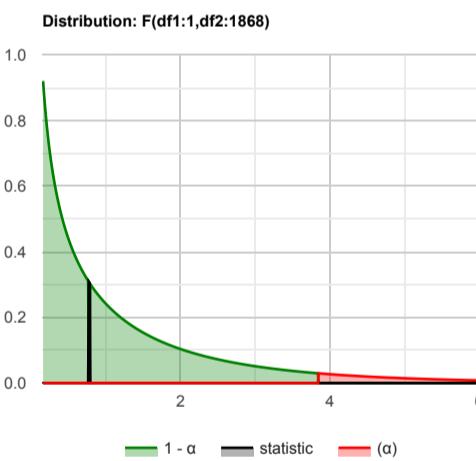
The p-value equals 0.491, ($P(x \leq 0.4746) = 0.509$). It means that the chance of type I error, rejecting a correct H_0 , is too high: 0.491 (49.1%). The larger the p-value the more it supports H_0 .

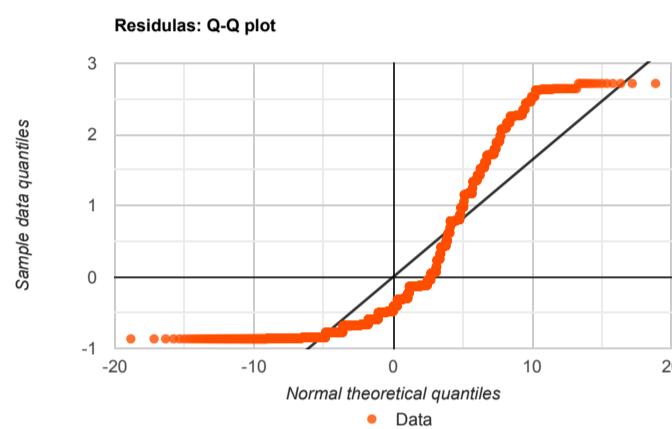
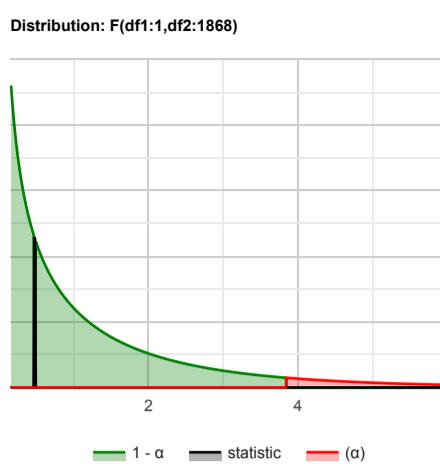
3. Test statistic

The test statistic F_A equals 0.4746, which is in the 95% region of acceptance: $[-\infty : 3.8464]$.

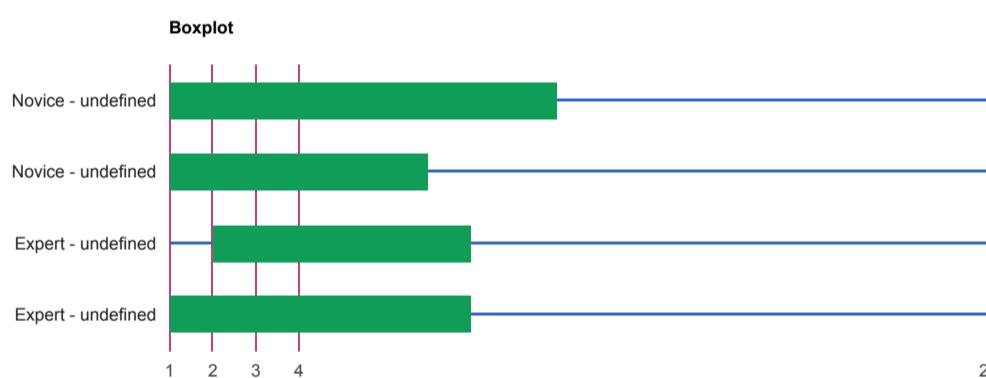
4. Effect size

The observed effect size η^2 is **very small**, **0.00025**. This indicates that the magnitude of the difference between the average is very small.





Right click on: [Save image](#), (please use 'save link as...' or 'open link in new tab').



Right click on: [Save image](#), (please use 'save link as...' or 'open link in new tab').

/alidation

Outliers

[Outliers'](#) detection method: Tukey Fence, $k=1.5$.

Residuals doesn't contain outliers. The **two way ANOVA** test is robust to the presence of outliers.

Normality

The assumption was checked based on the [Shapiro-Wilk Test](#). ($\alpha=0.05$)

It is assumed that **the residuals does not** follow a normal distribution (p-value is 0).

The test is considered robust for moderate violation of the normality assumption.

Test power: Factor - A

The test priori power is strong 1

Test power: Factor - B

The test priori power is strong 1

Test power: Interaction

The test priori power is strong 1

Balanced design

undefined

Tukey HSD / Tukey Kramer

Count

Var A \ Var B	undefined	undefined	Total
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Novice	414	414	828
Expert	522	522	1044
Total	936	936	1872

Average

Var A \ Var B	undefined	undefined	Total
Novice	5.6787	5.2295	5.4541
Expert	5.728	5.6284	5.6782
Total	5.7062	5.4519	5.5791

Variance

Var A \ Var B	undefined	undefined	Total
Novice	34.3493	33.2329	33.8008
Expert	24.4902	28.5564	26.5003
Total	28.8195	30.6308	29.7254

Mean confidence interval (CL:0.95)

Var A \ Var B	undefined	undefined	Total
Novice	[-5.7944,17.1519]	[-6.0557,16.5146]	[-5.9339,16.8421]
Expert	[-3.9621,15.4181]	[-4.8353,16.092]	[-4.4066,15.7629]
Total	[-4.81,16.2224]	[-5.3897,16.2936]	[-5.104,16.2621]

Differential effects

Var A \ Var B	undefined	undefined	Total
Novice	0.0975	-0.0975	-0.125
Expert	-0.07733	0.07733	0.0991
Total	0.1271	-0.1271	0

Cells - the differential effects of the interactions.For example, the effect of the interactions of the categories **undefined** and **Novice** is **0.0975**.**Totals** - the differential effects of factor A (right column) and factor B (bottom row).For example, the effect of factor B category **undefined** is **0.1271**.Residuals

A	B	Y _{i,j,k}	Formula: Y _{i,j,k} - Ŷ _{i,j}	Residual
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	15	15 - 5.679	9.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	15	15 - 5.679	9.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	17	17 - 5.679	11.3213
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	17	17 - 5.679	11.3213
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	17	17 - 5.679	11.3213
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	7	7 - 5.679	1.3213

Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	6	6 - 5.679	0.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	9	9 - 5.679	3.3213
Novice	undefined	15	15 - 5.679	9.3213
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	10	10 - 5.679	4.3213
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	15	15 - 5.679	9.3213
Novice	undefined	9	9 - 5.679	3.3213
Novice	undefined	6	6 - 5.679	0.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	6	6 - 5.679	0.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	6	6 - 5.679	0.3213
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	14	14 - 5.679	8.3213
Novice	undefined	7	7 - 5.679	1.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	19	19 - 5.679	13.3213
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	19	19 - 5.679	13.3213
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Novice	undefined	1	1 - 5.679	-4.6787
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	2	2 - 5.679	-3.6787

Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	20	20 - 5.679	14.3213
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	20	20 - 5.679	14.3213
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
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Novice	undefined	4	4 - 5.679	-1.6787
Novice	undefined	20	20 - 5.679	14.3213
Novice	undefined	3	3 - 5.679	-2.6787
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	20	20 - 5.679	14.3213
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Novice	undefined	20	20 - 5.679	14.3213
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Novice	undefined	2	2 - 5.679	-3.6787
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Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	5	5 - 5.679	-0.6787
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Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	13	13 - 5.679	7.3213
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Novice	undefined	1	1 - 5.679	-4.6787
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Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	2	2 - 5.679	-3.6787
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Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	2	2 - 5.679	-3.6787
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Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	18	18 - 5.679	12.3213
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	1	1 - 5.679	-4.6787
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Novice	undefined	4	4 - 5.679	-1.6787
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	2	2 - 5.679	-3.6787

Novice	undefined	6	6 - 5.679	0.3213
Novice	undefined	2	2 - 5.679	-3.6787
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	4	4 - 5.679	-1.6787
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Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	13	13 - 5.679	7.3213
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	11	11 - 5.679	5.3213
Novice	undefined	5	5 - 5.679	-0.6787
Novice	undefined	13	13 - 5.679	7.3213
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	3	3 - 5.679	-2.6787
Novice	undefined	11	11 - 5.679	5.3213
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Novice	undefined	13	13 - 5.679	7.3213
Novice	undefined	10	10 - 5.679	4.3213
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	18	18 - 5.679	12.3213
Novice	undefined	10	10 - 5.679	4.3213
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	10	10 - 5.679	4.3213
Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	12	12 - 5.679	6.3213
Novice	undefined	18	18 - 5.679	12.3213
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Novice	undefined	1	1 - 5.679	-4.6787
Novice	undefined	10	10 - 5.679	4.3213
Novice	undefined	1	1 - 5.679	-4.6787
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Novice	undefined	10	10 - 5.679	4.3213
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Novice	undefined	2	2 - 5.679	-3.6787
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Novice	undefined	15	15 - 5.679	9.3213
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Novice	undefined	15	15 - 5.679	9.3213
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Novice	undefined	15	15 - 5.679	9.3213
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Novice	undefined	5	5 - 5.229	-0.2295
Novice	undefined	17	17 - 5.229	11.7705
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Novice	undefined	2	2 - 5.229	-3.2295
Novice	undefined	17	17 - 5.229	11.7705
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Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	7	7 - 5.728	1.272
Expert	undefined	20	20 - 5.728	14.7705
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Expert	undefined	1	1 - 5.728	-4.2295
Expert	undefined	2	2 - 5.728	-3.2295
Expert	undefined	5	5 - 5.728	-0.2295
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Expert	undefined	3	3 - 5.728	-2.728
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Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728

Expert	undefined	18	18 - 5.728	12.272
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Expert	undefined	3	3 - 5.728	-2.728
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Expert	undefined	17	17 - 5.728	11.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	16	16 - 5.728	10.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	17	17 - 5.728	11.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	17	17 - 5.728	11.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	17	17 - 5.728	11.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	17	17 - 5.728	11.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	3	3 - 5.728	-2.728

Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	10	10 - 5.728	4.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	18	18 - 5.728	12.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	19	19 - 5.728	13.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	19	19 - 5.728	13.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	19	19 - 5.728	13.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	13	13 - 5.728	7.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	13	13 - 5.728	7.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	13	13 - 5.728	7.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272

Expert	undefined	13	13 - 5.728	7.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	7	7 - 5.728	1.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	7	7 - 5.728	1.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	7	7 - 5.728	1.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	2	2 - 5.728	-3.728
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Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	10	10 - 5.728	4.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	14	14 - 5.728	8.272
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	14	14 - 5.728	8.272
Expert	undefined	6	6 - 5.728	0.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	3	3 - 5.728	-2.728

Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
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Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	16	16 - 5.728	10.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	15	15 - 5.728	9.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	16	16 - 5.728	10.272
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	15	15 - 5.728	9.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	16	16 - 5.728	10.272
Expert	undefined	4	4 - 5.728	-1.728
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Expert	undefined	3	3 - 5.728	-2.728
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Expert	undefined	5	5 - 5.728	-0.728
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Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	10	10 - 5.728	4.272
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Expert	undefined	3	3 - 5.728	-2.728
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Expert	undefined	6	6 - 5.728	0.272

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Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	20	20 - 5.728	14.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	20	20 - 5.728	14.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	3	3 - 5.728	-2.728
Expert	undefined	20	20 - 5.728	14.272
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Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	16	16 - 5.728	10.272
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Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	16	16 - 5.728	10.272
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Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	14	14 - 5.728	8.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	4	4 - 5.728	-1.728
Expert	undefined	14	14 - 5.728	8.272
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Expert	undefined	2	2 - 5.728	-3.728
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Expert	undefined	2	2 - 5.728	-3.728

Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	5	5 - 5.728	-0.728
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Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	9	9 - 5.728	3.272
Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	12	12 - 5.728	6.272
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Expert	undefined	8	8 - 5.728	2.272
Expert	undefined	1	1 - 5.728	-4.728
Expert	undefined	11	11 - 5.728	5.272
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Expert	undefined	3	3 - 5.728	-2.728
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Expert	undefined	11	11 - 5.728	5.272
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Expert	undefined	11	11 - 5.728	5.272
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Expert	undefined	14	14 - 5.728	8.272
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Expert	undefined	5	5 - 5.728	-0.728
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Expert	undefined	14	14 - 5.728	8.272
Expert	undefined	7	7 - 5.728	1.272
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	13	13 - 5.728	7.272
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Expert	undefined	2	2 - 5.728	-3.728
Expert	undefined	14	14 - 5.728	8.272
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Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	5	5 - 5.728	-0.728
Expert	undefined	18	18 - 5.728	12.272
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Expert	undefined	5	5 - 5.728	-0.728
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Expert	undefined	16	16 - 5.628	10.3716
Expert	undefined	3	3 - 5.628	-2.6284
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	6	6 - 5.628	0.3716
Expert	undefined	5	5 - 5.628	-0.6284
Expert	undefined	8	8 - 5.628	2.3716
Expert	undefined	16	16 - 5.628	10.3716
Expert	undefined	3	3 - 5.628	-2.6284
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	12	12 - 5.628	6.3716
Expert	undefined	5	5 - 5.628	-0.6284
Expert	undefined	8	8 - 5.628	2.3716
Expert	undefined	17	17 - 5.628	11.3716
Expert	undefined	3	3 - 5.628	-2.6284
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	4	4 - 5.628	-1.6284
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	6	6 - 5.628	0.3716
Expert	undefined	15	15 - 5.628	9.3716
Expert	undefined	7	7 - 5.628	1.3716
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	8	8 - 5.628	2.3716
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	6	6 - 5.628	0.3716
Expert	undefined	15	15 - 5.628	9.3716
Expert	undefined	7	7 - 5.628	1.3716
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	8	8 - 5.628	2.3716
Expert	undefined	1	1 - 5.628	-4.6284
Expert	undefined	6	6 - 5.628	0.3716
Expert	undefined	14	14 - 5.628	8.3716
Expert	undefined	7	7 - 5.628	1.3716
Expert	undefined	1	1 - 5.628	-4.6284

Information

Models

There are many possible models, this calculator deal currently only with the following balanced models:

- **Fixed effect model (A-Fixed, B-Fixed), no repeats** - both factors are fixed.
- **Mixed effect model (A-Random, B-Fixed), no repeats** - factor A is random, factor B is fixed, each subject is measured only once.
- **Mixed effect model (A-Fixed, B-Random), no repeats** - factor A is fixed, factor B is random, each subject is measured only once.
- **Random effect model (A-Random, B-Random), no repeats**
- **Mixed repeated measures (A-Fixed, B-Repeated)** - factor A is fixed, factor B uses the same subject for all the categories.

You may use data with replications, or data without replications.

What is balanced model?

The balanced design has the same number of observations in each cell - each combination of factor.

Currently this calculator supports only the balanced design.

When the model is **unbalanced**, it causes correlation between the factors and the interaction if it is proportional, and also between the factors if it is unbalance but not proportional. hence you don't know how to divide the shared sum of squares between the two factors.

There are several methods how to deal with the shared sum of squares.

Type I - sequenceial, the first some of squares (SS) you calculate get the shared some of squares, in this case the order is matter!

Type II - conservative, it assumes there is no interaction between the factors, it ignores the shared SS between the factors. Type III - it assumes there is interaction between the factors, it ignores all the shared SS between the factors and between the factors and the intercation.

Targets

The two way ANOVA test checks the following targets using sample data.

- Checks if the difference between **Factor A** averages of two or more categories is significant
- Checks if the difference between **Factor B** averages of two or more categories is significant
- Checks if there is an interaction between **Factor A** and **Factor B**

When performing ANOVA test, we try to determine if the difference between the averages reflects a real difference between the groups, or is due to the random noise inside each group.

The F statistic represents the ratio of the variance between the groups and the variance inside the groups. Unlike many other statistic tests, the smaller the F statistic the more likely the averages are equal.

Right-tailed F test, for ANOVA test you can use only the right tail. [Why?](#)

Hypotheses

Factor A: $H_0: \mu_1 = \dots = \mu_a$

There is no difference in the means of variable A categories.

Factor B: $H_0: \mu_1 = \dots = \mu_b$

There is no difference in the means of variable B categories.

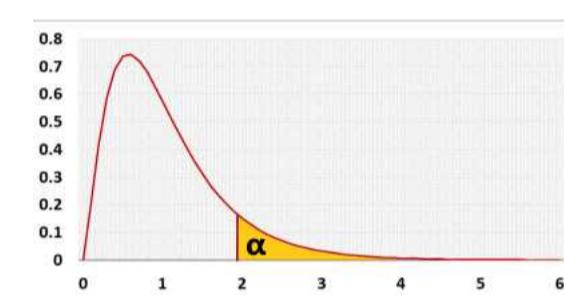
H₀: Interaction(A_iB_j) = 0 ($\forall i = 1 \text{ to } a, j = 1 \text{ to } b$)

There is no interaction between variable A and variable B, i.e., for all the cells, the effect of variable A on the cells' means is not depend on the effect of variable B, and vice versa.

Test statistic

Fixed Model	Mixed Model	Random Model	Mixed Repeated
$F_A = \frac{MS_A}{MS_E}$	$F_A = \frac{MS_A}{MS_{AB}}$	$F_A = \frac{MS_A}{MS_{AB}}$	$F_A = \frac{MS_A}{MS_{SWA}}$
$F_B = \frac{MS_B}{MS_E}$	$F_B = \frac{MS_B}{MS_E}$	$F_B = \frac{MS_B}{MS_{AB}}$	$F_B = \frac{MS_B}{MS_{BSWA}}$
$F_{AB} = \frac{MS_{AB}}{MS_E}$	$F_{AB} = \frac{MS_{AB}}{MS_E}$	$F_{AB} = \frac{MS_{AB}}{MS_E}$	$F_{AB} = \frac{MS_{AB}}{MS_{BSWA}}$

F distribution



Assumptions

- The dependent variable is continuous (ratio or interval)
- Two categorical independent variables
- Independent observations (no repeated measure)
- The residuals distribution is normal
- Homogeneity of variances, a similar variance for each cell

Required Sample Data

Sample data from all compared groups

Parameters

a - the number of categories in variable A, number of rows.

b - the number of categories in variable B, number of columns.

n_i - sample size of category i of variable A (row i).

n_j - sample size of category j of variable B (column j).

n_{i,j} - sample size of cell i,j (row i, column j). In the balance $n_{i,j} = n / (a * b)$.

n - overall sample size, includes all the groups ($\sum n_{i,j}$, $i=1 \text{ to } a$, $j=1 \text{ to } b$).

Ȳ_i - average of all the observations of category i of variable A (row i).

Ȳ_j - average of all the observations of category j of variable B (column j).

Ȳ - overall average ($\sum Y_{i,j,k} / n$, $i=1 \text{ to } a$, $j=1 \text{ to } b$, $k=1 \text{ to } n_{i,j}$).

Repeated measures ANOVA

s - represent the order of subject in category i (subject 1 in category 1 is different than subject 1 in category 2)

sub - number of subjects per cell, cell is one combination of variable A and variable B. For the balance design: $N=a*b*sub$.

Ȳ_{i,s} - subject's average, $\sum Y_{i,j,s}$ for subject i,s ,the average of all the observations of subject s of category j of variable B (column j).

Ȳ - overall average ($\sum Y_{i,j,s} / n$)

Results calculations

Sum of squares

The sum of squares accumulates the squared differences related to the effect we try to estimate.

SS_A - the squared differences related to the effect of variable A. You compare the average of every category to the total average. The same value as the sum of squares between groups in one way ANOVA.

SS_B - the same as SS_A for variable B.

SS_{AB} - the squared differences related to the effect of the combination of variable A and variable B in each cell, Since we try to understand the influence of the interaction AB, the interaction of the specific value of variable A and the specific value of variable B, we take the average of each cell, remove the influence of variable A and variable B, and compare to the total average.

A effect = $\bar{Y}_i - \bar{Y}$

B effect = $\bar{Y}_j - \bar{Y}$

AB effect = Cell average - A effect - B effect - Total average.

$$= \bar{Y}_{i,j} - (\bar{Y}_i - \bar{Y}) - (\bar{Y}_j - \bar{Y}) - \bar{Y}$$

$$= \bar{Y}_{i,j} - \bar{Y}_i - \bar{Y}_j + \bar{Y}$$

Take the square of each difference

$$\bar{Y}_{i,j} - \bar{Y}_i - \bar{Y}_j + \bar{Y}$$

Count the square differences of each value in the cell, hence multiply by the sample size of each cell ($n_{i,j}$).

$$SS_{AB} = \sum_i^a \sum_j^b n_{i,j} (\bar{Y}_{i,j} - \bar{Y}_i - \bar{Y}_j + \bar{Y})^2$$

Fixed and Random Effects

The fixed and random effects are related to the independent variables () .

Fixed Effect

The effect is constant across individuals.

- The categories of the variable contains the entire categories' list
 - The effect of this variable is interesting. The difference between the categories is important
 - There is no known pattern on the difference between the categories

Random Effect

The effect vary across individuals, the individuals may be people, products.

- The categories' list is only a sample from the entire categories' list
 - The effect of this variable is not interesting by itself. The difference between the categories is not important
 - There is no known pattern on the difference between the categories

Example: collecting data from several schools.

A sample from the entire groups' population.

There is no pattern about the difference between the schools, and if there will be a pattern, it will be another factor, like school's size.

Each school is not important by itself.

When you change the **interaction field** or the **model**, the following ANOVA table and diagram will be adjusted.

ANOVA table - with interaction

Source	Degrees of Freedom (DF)	Sum of Squares (SS)	Mean Square (MS)	F statistic	p-value
Factor A (rows) Between the categories of factor A	$DF_A = a - 1$	$SS_A = \sum_i^a n_i (\bar{Y}_i - \bar{Y})^2$	$MS_A = SS_A / DF_A$	$F_A = MS_A / MS_E$	$P(x > F_A)$
Factor B (Columns) Between the categories of factor B	$DF_B = b - 1$	$SS_B = \sum_j^b n_j (\bar{Y}_j - \bar{Y})^2$	$MS_B = SS_B / DF_B$	$F_B = MS_B / MS_E$	$P(x > F_B)$
Interaction AB Between the cells after reducing factor A and factor B effects	$DF_{AB} = (a - 1)(b - 1)$	$SS_{AB} = \sum_i^a \sum_j^b n_{i,j} (\bar{Y}_{i,j} - \bar{Y}_i - \bar{Y}_j + \bar{Y})^2$	$MS_{AB} = SS_{AB} / DF_{AB}$	$F_{AB} = MS_{AB} / MS_E$	$P(x > F_{AB})$
Error Within the cells	$DF_E = n - a*b$	$SS_E = \sum_i^a \sum_j^b \sum_k^n n_{i,j,k} (Y_{i,j,k} - \bar{Y}_{i,j})^2$	$MS_E = SS_E / DF_E$		
Total All the deviations from the average	$DF_T = n - 1$	$SS_T = \sum_i^a \sum_j^b \sum_k^n n_{i,j,k} (Y_{i,j,k} - \bar{Y})^2$ $SS_T = \text{Sample Variance} * (n-1)$ $SS_T = SS_A + SS_B + SS_{AB} + SS_E$	$MS_E = S^2 = SS_T / (n - 1)$		

Sum of squares diagram - with interaction

In the following diagram you may see the differences per each observation $Y_{i,j,k}$ that used to calculate the sum of squares.

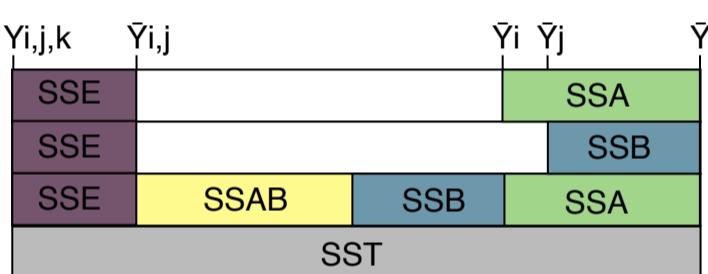
A effect: $\bar{Y}_i - \bar{Y}$.

B effect: $\bar{Y}_i - \bar{Y}_j$

Interaction effect (AB): $Y_{ijkl} = \bar{Y}_i + \bar{Y}_j + \bar{Y}_{ij} + \bar{Y}_{ijkl}$

Error: $\bar{Y}_{1..n} - \bar{Y}_{1..}$

Error: $Y_{i,j,k} - \bar{Y}_{i,j}$



R Code

The following R code should produce the same results

```

c(10,1,2,18,5,1,10,1,2,18,5,1,1,1,1,19,1,1,1,1,1,19,1,1,1,1,1,19,1,1,8,5,8,13,8,10,8,5,8,13,8,10,7,5,5,9,4,6,7,5,5,9,4,6,7,5,5,9,4,6,8,2,10,10,5,2,8,2,10,10,5,2,6,5,5,14,6,1,6,5,5,14,6,1,6,5,14,6,1,3,3,5,8,3,2,3,3,
DV3 =
c(5,5,5,18,5,1,5,5,5,18,5,1,5,5,18,5,1,5,1,5,13,5,1,5,1,5,13,5,1,5,1,5,13,5,1,2,1,2,16,2,1,2,1,2,17,2,1,2,1,2,17,2,1,3,3,5,17,3,1,5,5,5,14,3,3,7,5,8,17,4,4,5,1,5,16,5,4,9,1,7,17,9,4,11,2,8,15,13,7,2,3,3,20,3,2,3,3,3,19,2,2,2,2,2,20,2,2,2,1,1,1
DV4 =
c(3,1,3,18,1,2,1,1,5,14,2,2,1,1,5,14,2,2,1,1,5,14,2,1,8,13,1,14,2,1,5,13,1,14,4,1,5,17,2,6,4,1,11,17,2,6,4,1,4,17,2,6,2,3,3,12,5,13,2,3,3,12,5,13,5,3,3,12,5,13,8,1,10,18,8,1,8,1,10,16,8,1,8,1,13,18,8,1,7,2,2,13,2,5,7,2,1,13,2,5,
DV5 =
c(3,1,1,20,1,1,2,1,1,20,1,1,5,1,5,12,2,2,3,1,5,12,2,2,3,1,5,12,2,10,1,2,18,5,1,10,3,2,18,5,1,10,3,2,18,5,1,1,3,1,19,1,1,1,1,1,19,1,1,1,1,1,19,1,1,6,4,8,15,8,10,6,4,8,15,8,10,9,5,5,12,4,6,7,5,5,12,4,6,9,5,5,12,4,6,8,2,13,12,3,2,8,
DV6 = c(5,8,1,12,4,3,5,8,1,12,4,3,5,8,1,13,4,3,13,10,3,13,5,5,13,10,3,14,5,5,13,10,3,13,5,5,6,5,4,16,3,1,6,5,8,16,3,1,12,5,8,17,3,1,4,1,6,15,7,1,8,1,6,15,7,1,8,1,6,14,7,1)
DV = c(DV0,DV1,DV2,DV3,DV4,DV5,DV6)
ID0 =
c(0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,67,68,69,70,71,72,73,74
ID1 =
c(300,301,302,303,304,305,306,307,308,309,310,311,312,313,314,315,316,317,318,319,320,321,322,323,324,325,326,327,328,329,330,331,332,333,334,335,336,337,338,339,340,341,342,343,344,345,346,347,348
ID2 =
c(600,601,602,603,604,605,606,607,608,609,610,611,612,613,614,615,616,617,618,619,620,621,622,623,624,625,626,627,628,629,630,631,632,633,634,635,636,637,638,639,640,641,642,643,644,645,646,647,648
ID3 =
c(900,901,902,903,904,905,906,907,908,909,910,911,912,913,914,915,916,917,918,919,920,921,922,923,924,925,926,927,928,929,930,931,932,933,934,935,0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,
ID4 =
c(264,265,266,267,268,269,270,271,272,273,274,275,276,277,278,279,280,281,282,283,284,285,286,287,288,289,290,291,292,293,294,295,296,297,298,299,300,301,302,303,304,305,306,307,308,309,310,311,312
ID5 =
c(564,565,566,567,568,569,570,571,572,573,574,575,576,577,578,579,580,581,582,583,584,585,586,587,588,589,590,591,592,593,594,595,596,597,598,599,600,601,602,603,604,605,606,607,608,609,610,611,612
ID6 =
c(864,865,866,867,868,869,870,871,872,873,874,875,876,877,878,879,880,881,882,883,884,885,886,887,888,889,890,891,892,893,894,895,896,897,898,899,900,901,902,903,904,905,906,907,908,909,910,911,912
ID = c(ID0, ID1, ID2, ID3, ID4, ID5, ID6)
df1 <- data.frame(A,B,DV,ID)
Model1 <- aov(DV ~ A + B + A:B, data=df1)
summary(Model1)
res=residuals(object = Model1)

```