

Cornell University Team Reference Document

Contents

1	CopyFirst	2
1.1	template	2
2	Data Structures	2
2.1	fenwick	2
2.2	kdTree	2
2.3	rmq	3
2.4	rmq2D	3
2.5	segTree	4
2.6	segTree2D	4
2.7	segTreeLazy	4
2.8	treap	5
2.9	unionFind	6
3	Graph	6
3.1	2sat	6
3.2	bellman	6
3.3	biconnected	6
3.4	dijkstra	7
3.5	dinic	7
3.6	eulerCycle	8
3.7	flowMinCost	8
3.8	heavyPath	8
3.9	hungarian	9
3.10	lca	10
3.11	lcaLog	10
3.12	matching	10
3.13	royFloyd	11
3.14	strongConnected	11

4	Math	11
4.1	comb	11
4.2	fft	12
4.3	fftMOD	12
4.4	fraction	13
4.5	geom2D	13
4.6	geom3D	16
4.7	geomMisc	17
4.8	geomSphere	18
4.9	numberTheory	18
4.10	polynom	19
5	Misc	20
5.1	binSearch	20
5.2	dpOptim	20
5.3	gauss	20
5.4	matpow	21
5.5	parse	21
5.6	simplex	21
5.7	ternary	22
5.8	util	22
6	String	23
6.1	ahoCorasick	23
6.2	expresioneval	23
6.3	kmp	24
6.4	psepld	24
6.5	rabinquery	24
6.6	suffixAuto	24
6.7	suffixarray	25
6.8	zalgo	25

1 CopyFirst

1.1 template

```
typedef long long ll;
typedef vector<int> vi;
typedef pair<int,int> pii;
typedef pair<double, double> pdd;
#define pb push_back
#define mp make_pair
#define fs first
#define sc second
#define rep(i, from, to) for (int i = from; i < (to); ++i)
#define all(x) x.begin(), x.end()
#define sz(x) (int)(x).size()
#define FOR(i, to) for (int i = 0; i < (to); ++i)
typedef vector<vector<int> > vvi;
typedef vector<ll> vll;
typedef vector<vll> vvll;
typedef vector<pair<int, int> > vpi;
typedef pair<ll,ll> pll;
typedef vector<string> vs;
```

2 Data Structures

2.1 fenwick

```
int AIB[Nmax], N;
inline int zeros(int x) { return x & (-x); }
inline void add(int x, int q) {
    for (int i = x; i <= N; i += zeros(i)) AIB[i] += q;
}
inline int comp(int x) {
    int ret = 0;
    for (int i = x; i > 0; i -= zeros(i)) ret += AIB[i];
    return ret;
}
```

2.2 kdTree

```
// number type for coordinates, and its maximum value
typedef long long ntype;
const ntype inf = numeric_limits<ntype>::max();
struct point {
    ntype x, y;
    point(ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
};
bool operator==(const point &a, const point &b) {
    return a.x == b.x && a.y == b.y;
}
int cmpx(const point &a, const point &b) { return a.x < b.x; }
int cmpy(const point &a, const point &b) { return a.y < b.y; }
ntype dist(const point &a, const point &b) {
    ntype dx = a.x-b.x, dy = a.y-b.y;
    return dx*dx + dy*dy;
}
struct bbox { //bounding box
    ntype x0, x1, y0, y1;
    bbox() : x0(inf), x1(-inf), y0(inf), y1(-inf) {}
    void compute(const vector<point> &v) {
        for (int i = 0; i < v.size(); ++i) {
            x0 = min(x0, v[i].x); x1 = max(x1, v[i].x);
            y0 = min(y0, v[i].y); y1 = max(y1, v[i].y);
        }
    }
}
//distance between a point and this box, 0 if inside
ntype distance(const point &p) {
    if (p.x < x0) {
        if (p.y < y0) return dist(point(x0, y0), p);
        else if (p.y > y1) return dist(point(x0, y1), p);
        else return dist(point(x0, p.y), p);
    } else if (p.x > x1) {
        if (p.y < y0) return dist(point(x1, y0), p);
        else if (p.y > y1) return dist(point(x1, y1), p);
        else return dist(point(x1, p.y), p);
    } else {
        if (p.y < y0) return dist(point(p.x, y0), p);
        else if (p.y > y1) return dist(point(p.x, y1), p);
        else return 0;
    }
}
};
struct kdnode {
    bool leaf; point pt; //if only has one point
```

```

bbox bound;
kdnode *left, *right; // two children of this kd-node
kdnode() : leaf(false), left(0), right(0) {}
~kdnode() { if (left) delete left; if (right) delete right; }
ntype intersect(const point &p) { return bound.distance(p); }
void construct(vector<point> &vp) {
    bound.compute(vp);
    if (vp.size() == 1) {
        leaf = true; pt = vp[0];
    } else { // split on largest coord
        if (bound.x1-bound.x0 >= bound.y1-bound.y0) {
            sort(vp.begin(), vp.end(), cmpx);
        } else {
            sort(vp.begin(), vp.end(), cmpy);
        }
        int half = vp.size()/2;
        vector<point> vl(vp.begin(), vp.begin()+half);
        vector<point> vr(vp.begin()+half, vp.end());
        left = new kdnode(); left->construct(vl);
        right = new kdnode(); right->construct(vr);
    }
}
};

struct kdtree {
    kdnode *root;
    kdtree(const vector<point> &vp) {
        vector<point> v(vp.begin(), vp.end());
        root = new kdnode(); root->construct(v);
    }
    ~kdtree() { delete root; }
    ntype search(kdnode *node, const point &p) { // nearest neighbour
        if (node->leaf) {
            if (p == node->pt) return inf; // if not want dupl
            else return dist(p, node->pt);
        }
        ntype bleft = node->left->intersect(p);
        ntype bright = node->right->intersect(p);
        if (bleft < bright) {
            ntype best = search(node->left, p);
            if (bright < best) best = min(best, search(node->right, p));
            return best;
        } else {
            ntype best = search(node->right, p);
            if (bleft < best) best = min(best, search(node->left, p));
            return best;
        }
    }
};

```

```

    }
}
ntype nearest(const point &p) { return search(root, p); }
};

```

2.3 rmq

```

int rmq[log][Nmax], v[Nmax], lg[Nmax], N;
void genRmq() {
    for(int i=2; i<=N; ++i) lg[i] = lg[i/2] + 1;
    for(int i=1; i<=N; ++i) rmq[0][i] = v[i];
    for(int i=1; (1<<i)<=N; ++i) {
        for(int j=1; j+(1<<i)-1<=N; ++j) {
            rmq[i][j] = min(rmq[i-1][j], rmq[i-1][j+(1<<(i-1))]);
        }
    }
}
int query(int x, int y) {
    int l = lg[y-x+1], sh = y-x+1-(1<<l);
    return min(rmq[l][x], rmq[l][x+sh]);
}

```

2.4 rmq2D

```

int A[Nmax][Nmax], N, M;
int rmq[lmax][lmax][Nmax][Nmax], lg[Nmax];
void genRmq() {
    for(int i=2; i<=max(N,M); ++i) lg[i] = lg[i/2] + 1;
    for(int k=0; (1<<k)<=N; ++k) {
        for(int l=0; (1<<l)<=M; ++l) {
            for(int i=1; i+(1<<k)-1<=N; ++i) {
                for(int j=1; j+(1<<l)-1<=M; ++j) {
                    if(!k && !l) rmq[k][l][i][j] = A[i][j];
                    else if(!k) rmq[k][l][i][j] = min(rmq[k][l-1][i][j],
                                                         rmq[k][l-1][i][j+(1<<(l-1))]);
                    else rmq[k][l][i][j] = min(rmq[k-1][l][i][j],
                                                         rmq[k-1][l][i+(1<<(k-1))][j]);
                }
            }
        }
    }
}

```

```

}
int query(int xa, int ya, int xb, int yb) { //(xa,ya) topleft (xb,yb)
    bottomright
    int lx = lg[xb-xa+1], mx = xb+1-(1<<lx);
    int ly = lg[yb-ya+1], my = yb+1-(1<<ly);
    int ret1 = min(rmq[lx][ly][xa][ya], rmq[lx][ly][xa][my]);
    int ret2 = min(rmq[lx][ly][mx][ya], rmq[lx][ly][mx][my]);
    return min(ret1,ret2);
}

```

2.5 segTree

```

int t[4*Nmax];
void update(int nod, int st, int dr, int poz, int val) {
    if(st==dr) { t[nod]=val; return; }
    int mij = (st+dr)/2;
    if(poz<=mij) update(2*nod,st,mij,poz,val);
    else update(2*nod+1,mij+1,dr,poz,val);
    t[nod] = max(t[2*nod],t[2*nod+1]);
}
int getmax(int nod, int st, int dr, int l, int r) {
    if(l<=st && dr<=r) return t[nod];
    int ret = 0; int mij = (st+dr)/2;
    if(r>mij) ret = max(ret,getmax(nod*2+1,1+mij,dr,l,r));
    if(l<=mij) ret = max(ret,getmax(nod*2,st,mij,l,r)); return ret;
}

```

2.6 segTree2D

```

int N, val[4*Nmax];
vector<ll> AIB[4*Nmax];
vector<ll> v[4*Nmax];
inline int zeros(int x) { return x & (-x); }
inline void Add(int nod, int x, int q){
    for(int i=x ;i < AIB[nod].size(); i+= zeros(i)) AIB[nod][i] += q;
}
ll comp(int nod, int x){
    ll ret = 0;
    if(AIB[nod].size() == 0) return 0;
    for(int i=x;i>0;i-=zeros(i)) ret += AIB[nod][i];
    return ret;
}

```

```

}
void init(int nod, int st, int dr){
    if(dr - st == 0){
        v[nod].pb(val[st]);
        AIB[nod].resize(v[nod].size()+1);
        Add(nod,1,1);
    } else {
        int mij = (st+dr) / 2;
        init(nod*2, st, mij); init(nod*2+1, mij+1, dr);
        v[nod].resize(v[nod*2].size() + v[nod*2+1].size());
        merge(v[nod*2].begin(), v[nod*2].end(), v[nod*2+1].begin(),
            v[nod*2+1].end(),v[nod].begin());
        AIB[nod].resize(v[nod].size()+1);
        for(int i=1;i<AIB[nod].size();++i) Add(nod, i, 1);
    }
}
int getInd(int nod, int x){
    int ret = -1, st = 0, dr = v[nod].size() -1;
    while(st <= dr ){
        int mij = (st+dr)/2;
        if(v[nod][mij] <= x) { st = mij + 1; ret = mij; }
        else dr = mij - 1;
    }
    return ret+1;
}
int K; ll retV = 0; // calc between ist,idr and k,l
int calc(int nod,int ist, int idr, int st, int dr, int k, int l) {
    if (K == 0 && k > l) return 0;
    if(ist <= st && idr >= dr){
        retV += comp(nod,getInd(nod,l)) - comp(nod,getInd(nod,k-1));
    } else {
        int mij = (st+dr)/2;
        if (ist <= mij) calc(nod*2,ist,idr,st,mij,k,l);
        if (idr > mij) calc(nod*2+1,ist,idr,mij+1,dr,k,l);
    }
}
}

```

2.7 segTreeLazy

```

int aint[Nmax*4], up[Nmax*4], v[Nmax];
inline void relax(int nod,int st,int dr) {
    if(!up[nod]) return; aint[nod] += up[nod];
    if(st!=dr) { up[2*nod]+=c; up[2*nod+1]+=c; }
}

```

```

    up[nod] = 0;
}
void update(int nod,int ist,int idr,int st,int dr,ll val) {
    relax(nod,st,dr);
    if(ist<=st&&idr>=dr) {
        up[nod] = val; relax(nod,st,dr);
    } else {
        int mij=(st+dr)/2;
        if(ist<=mij) update(2*nod,ist,idr,st,mij,val);
        if(idr>mij) update(2*nod+1,ist,idr,mij+1,dr,val);
        make(nod,st,dr);
    }
}
int calc(int nod,int ist,int idr,int st,int dr) {
    relax(nod,st,dr); int ret = 0;
    if(ist<=st && idr>=dr) ret += aint[nod];
    else {
        ll mij=(st+dr)/2;
        if(ist<=mij) ret += calc(2*nod,ist,idr,st,mij);
        if(idr>mij) ret += calc(2*nod+1,ist,idr,mij+1,dr);
        make(nod,st,dr);
    }
    return ret;
}
void init(int nod,int st,int dr){
    if(st != dr){
        int mij = (st+dr)/2;
        init(2*nod,st,mij); init(2*nod+1,mij+1,dr);
        make(nod,st,dr);
    } else {
        aint[nod] = v[st];
    }
}

```

2.8 treap

```

typedef struct item * pitem;
struct item {
    int cnt, value, prior, key; bool rev; pitem l, r;
    item(int prior, int value) : cnt(1), rev(false), prior(prior),
        value(value), l(NULL), r(NULL) {}
};
int cnt(pitem t) { return t ? t->cnt : 0; }

```

```

void upd_cnt(pitem it) { if (it) it->cnt = cnt(it->l) + cnt(it->r) + 1; }
void push(pitem it) {
    if (it && it->rev) {
        it->rev = false; swap(it->l, it->r);
        if (it->l) it->l->rev ^= true;
        if (it->r) it->r->rev ^= true;
    }
}
void merge(pitem &t, pitem l, pitem r) {
    push(l); push(r); if (!l || !r) t = l ? l : r;
    else if (l->prior > r->prior) merge(l->r, l->r, r), t = l;
    else merge(r->l, l, r->l), t = r; upd_cnt(t);
}
void split(pitem t, pitem &l, pitem &r, int key, int add = 0) {
    if (!t) return void (l = r = 0);
    push(t); int cur_key = cnt(t->l) + add;
    if (key <= cur_key) split(t->l, l, t->l, key, add), r = t;
    else split(t->r, t->r, r, key, add + cnt(t->l) + 1), l = t;
    upd_cnt(t);
}
void split (pitem t, int key, pitem &l, pitem &r) {
    if (!t) l = r = NULL; push(t);
    else if (key < t->key) split (t->l, key, l, t->l), r = t;
    else split (t->r, key, t->r, r), l = t; upd_cnt(t);
}
void reverse(pitem t, int l, int r) {
    if(l > r) return; pitem t1, t2, t3;
    split(t, t1, t2, l); split(t2, t2, t3, r-l+1);
    t2->rev ^= true; merge(t, t1, t2); merge(t, t, t3);
}
void output (pitem t) {
    if (!t) return; push(t); output (t->l);
    printf ("%d", t->value); output (t->r);
}
void erase (pitem &t, int key) {
    push(t); if (t->key == key) merge (t, t->l, t->r);
    else erase (key < t->key ? t->l : t->r, key); upd_cnt(t);
}
void insert (pitem &t, pitem it) {
    push(t); if (!t) { t = it; return;};
    if (it->prior > t->prior) split (t, it->key, it->l, it->r), t = it;
    else insert (it->key < t->key ? t->l : t->r, it);
}
pitem cur = new item(rand(), s[i] - 'a'); if (root) merge(root, root,
    cur);

```

```
else root = cur; reverse(root, x,y);
```

2.9 unionFind

```
int par[Nmax],h[Nmax]
int findx(int x) {
    int R = x, y; while(par[R] != R) R = par[R];
    while(par[x] != x) { y = par[x]; par[x] = R; x = y;}
    return R;
}
void unite(int x, int y) {
    x = findx(x); y = findx(y); if (x == y) return;
    if(h[x] > h[y]) { par[y] = x; h[x] += h[y]; }
    else { par[x] = y; h[y] += h[x]; }
}
```

3 Graph

3.1 2sat

```
int N,s[2*Nmax],curr,c[2*Nmax],sol[2*Nmax]; //value of i = sol[2*i]
vector<int> g[2*Nmax],gt[2*Nmax],v[2*Nmax];
int viz[2*Nmax],vz[2*Nmax];
void dfs(int x) {
    viz[x] = 1; for(auto y: g[x]) if(!viz[y]) dfs(y); s[++curr] = x;
}
void dfs2(int x, int comp) {
    viz[x] = 0; c[x] = comp; v[comp].push_back(x);
    for(auto y: gt[x]) if(viz[y]) dfs2(y,comp);
}
inline int ng(int x) { if(x%2) return x-1; return x+1;}
bool f(int x, int val) {
    vz[x] = 1;
    for(auto y: v[x]) {
        if(sol[y] && sol[y]!=val) return false; sol[y] = val;
    }
    for(auto y: v[x]) {
        y = ng(y); if(sol[y] && sol[y]!=3-val) return false;
        if(!sol[y]) return f(c[y],3-val);
    }
}
```

```
return true;
}
inline bool sat() {
    int comp = 0;
    for(int i=2;i<=2*N+1;++i) if(!viz[i]) dfs(i);
    for(int i=curr;i>=1;--i) if(viz[s[i]]) dfs2(s[i],++comp);
    for(int i=1;i<=comp;++i) if(!vz[i]) if(!f(i,1)) return false;
    return true;
}
inline void add_disj(int x, int sx, int y, int sy) { //s 0 normal,1
    negation
    g[2*x+(1-sx)].push_back(2*y+sy);
    g[2*y+(1-sy)].push_back(2*x+sx);
    gt[2*y+sy].push_back(2*x+(1-sx));
    gt[2*x+sx].push_back(2*y+(1-sy));
}
```

3.2 bellman

```
vector<pii> g[Nmax];
int N,cnt[Nmax],d[Nmax];
queue<int> q;
void bellman(int r) {
    for(int i=1;i<=N;++i) d[i] = inf; d[r] = 0; q.push(r);
    while(!q.empty()) {
        int x = q.front(); ++cnt[x];
        if(cnt[x] > N) return; q.pop();
        for(auto p: g[x]) {
            int y = p.fs, c = p.sc;
            if(d[y] > d[x] + c) { d[y] = d[x] + c; q.push(y); }
        }
    }
}
```

3.3 biconnected

```
int N,w[Nmax],low[Nmax],depth[Nmax],comp,viz[Nmax];
vector<pii> m; //edges stack
vector<vi> c; //result
vi g[Nmax], com; //adjacency list
void dfs(int x, int p, int dep) {
```

```

viz[x] = 1; depth[x]=dep; low[x]=dep;
for(auto y: g[x]) {
    if(!viz[y]) {
        m.pb(mp(x,y)); dfs(y,x,dep+1); low[x] = min(low[x],low[y]);
        if(low[y] >= depth[x]) {
            ++comp; com.clear();
            while(true) {
                int t = m.back().fs, u = m.back().sc;
                if(w[t] != comp) { w[t] = comp; com.pb(t); }
                if(w[u] != comp) { w[u] = comp; com.pb(u); }
                m.pop_back(); if(t==x && u==y) break;
            }
            c.pb(com);
        }
    } else if(y!=p) low[x]=min(low[x],depth[y]);
}
}
void biconnect() {
    for(int i=1;i<=N;++i) {
        if(!viz[i]) dfs(i,0,0);
    }
}

```

3.4 dijkstra

```

int N, d[Nmax], viz[Nmax];
vector<pii> g[Nmax];
priority_queue<pii> pq;
void dijkstra(int r) {
    for(int i=1;i<=N;++i) d[i] = inf;
    d[r] = 0; pq.push(mp(0,r));
    while(!pq.empty()) {
        int x = pq.top().sc; pq.pop(); viz[x] = 1;
        for(auto a: g[x]) {
            int y = a.fs, c = a.sc;
            if(!viz[y]) {
                if(d[y] > c + d[x]) {
                    d[y] = c + d[x]; pq.push(mp(-d[y],y));
                }
            }
        }
    }
}

```

3.5 dinic

```

struct Edge {
    int u, v; ll cap, flow; Edge() {}
    Edge(int u, int v, ll cap): u(u), v(v), cap(cap), flow(0) {}
};
int N; vector<Edge> E;
vi d, pt, g[Nmax]; //edge indices
inline void addEdge(int u, int v, int cap) {
    E.pb(Edge(u, v, cap)); g[u].pb(E.size() - 1);
    E.pb(Edge(v, u, 0)); g[v].pb(E.size() - 1);
}
inline int BFS(int S, int T) {
    queue<int> q; q.push(S);
    fill(d.begin(), d.end(), N + 1);
    d[S] = 0;
    while(!q.empty()) {
        int u = q.front(); q.pop();
        if (u == T) break;
        for (int k: g[u]) {
            Edge &e = E[k];
            if (e.flow < e.cap && d[e.v] > d[e.u] + 1) {
                d[e.v] = d[e.u] + 1; q.push(e.v);
            }
        }
    }
    return d[T] != N + 1;
}
ll DFS(int u, int T, ll flow = -1) {
    if (u == T || flow == 0) return flow;
    for (int &i = pt[u]; i < g[u].size(); ++i) {
        Edge &e = E[g[u][i]];
        Edge &oe = E[g[u][i]^1];
        if (d[e.v] == d[e.u] + 1) {
            ll amt = e.cap - e.flow;
            if (flow != -1 && amt > flow) amt = flow;
            if (ll pushed = DFS(e.v, T, amt)) {
                e.flow += pushed; oe.flow -= pushed; return pushed;
            }
        }
    }
    return 0;
}
ll MaxFlow(int S, int T) {
    ll total = 0; pt.resize(N); d.resize(N);

```

```

while (BFS(S, T)) {
    fill(pt.begin(), pt.end(), 0);
    while (ll flow = DFS(S, T)) total += flow;
}
return total;
}

```

3.6 eulerCycle

```

void dfs(int x) { //isD = isDeleted
    for(auto n : g[x]) {
        if(isD[n.sc]==0) { isD[n.sc]=1; dfs(n.fs); }
    }
    ret.pb(x);
} // fs = node, sc = edge num

```

3.7 flowMinCost

```

int NRN, rez, d[Nmax], p[Nmax], viz[Nmax], inq[Nmax];
vector<pii> mc;
vi v, f, c, m[Nmax];
queue<int> q;
inline void add(int x) {
    if(inq[x]) return; inq[x] = viz[x] = 1; q.push(x);
}
inline int pop() {
    int x = q.front(); q.pop(); inq[x] = 0; // delete for bfs
    return x;
}
inline void reset_stuff(int S) {
    for(int i = 0; i <= NRN; ++i) {
        viz[i] = inq[i] = 0; d[i] = inf;
    } d[S] = 0;
}
inline void addEdge(int x, int y, int cap, int cost) {
    NRN = max(NRN, x); NRN = max(NRN, y);
    c.pb(cap); v.pb(cost); f.pb(0);
    m[x].pb(sz(mc)); mc.pb(mp(x, y));
    c.pb(0); f.pb(0); v.pb(-cost);
    m[y].pb(sz(mc)); mc.pb(mp(y, x));
}

```

```

inline int bfs(int S, int D) {
    reset_stuff(S); add(S);
    while(!q.empty()) {
        int x = pop(); if(x==D) continue;
        for(auto y : m[x]) {
            int ve = mc[y].sc;
            if(f[y] < c[y] && d[ve] > d[x] + v[y]) {
                add(ve); p[ve] = y; d[ve] = d[x] + v[y];
            }
        }
    }
    return viz[D];
}
pii update(int S, int D) {
    int ret = 0, retc = 0, flux = inf, curr = D;
    while(curr!=S) {
        int muc = p[curr], par = mc[p[curr]].fs;
        if(c[muc] - f[muc] < flux) flux = c[muc] - f[muc];
        if(!flux) break; curr = par;
    }
    curr = D;
    while(curr!=S) {
        int edg = p[curr], par = mc[p[curr]].fs;
        f[edg] += flux; f[edg^1] -= flux; curr = par;
    }
    ret += flux; retc += flux*d[D]; return mp(ret, retc);
}
pii flow(int S, int D) {
    int ret = 0, retc = 0;
    while(true) {
        if(!bfs(S, D)) break;
        pii u = update(S, D); ret += u.fs, retc += u.sc;
    }
    return mp(ret, retc);
}

```

3.8 heavyPath

```

int N, M, q, x, y, K;
int poz[Nmax], v[Nmax], nr[Nmax], l[Nmax], p[Nmax], cmp[Nmax], viz[Nmax];
vector<int> g[Nmax], c[Nmax];
//Segment tree stuff

```



```

vector<vector<int>> > t;
void update(int comp, int nod, int st, int dr, int c, int d) {
    if(st==dr) { t[comp][nod]=d; return; }
    int mij = (st+dr)/2;
    if(c<=mij) update(comp,2*nod,st,mij,c,d);
    else update(comp,2*nod+1,mij+1,dr,c,d);
    t[comp][nod] = max(t[comp][2*nod],t[comp][2*nod+1]);
}
int getmax(int comp, int nod, int st, int dr, int c, int d) {
    int ret = 0;
    if(c<=st && dr<=d) return t[comp][nod];
    int mij = (st+dr)/2;
    if(d>mij) ret = max(ret,getmax(comp,nod*2+1,1+mij,dr,c,d));
    if(c<=mij) ret = max(ret,getmax(comp,nod*2,st,mij,c,d));
    return ret;
}
inline int query_val(int comp, int st, int dr) {
    return getmax(comp, 1, 1, c[comp].size(), st+1, dr+1);
}
//Available queries
inline void update_val(int comp, int poz, int val) {
    update(comp, 1, 1, c[comp].size(), poz+1, val);
    v[c[comp][poz]] = val;
}
int find_max(int x, int y) {
    if(cmp[x] == cmp[y]) return
        query_val(cmp[x],min(poz[x],poz[y]),max(poz[x],poz[y]));
    int px = p[c[cmp[x]][0]], py = p[c[cmp[y]][0]];
    if(1[px] < 1[py]) { swap(x,y); swap(px,py); }
    int M = query_val(cmp[x],0,poz[x]);
    return max(M, find_max(px,y));
}
//Preprocessing
void dfs(int x) {
    viz[x] = 1; nr[x] = 1;
    int ind = -1, nrc = -1;
    for(auto y: g[x]) {
        if(viz[y]) continue;
        l[y] = l[x] + 1; p[y] = x; dfs(y);
        if(nr[y] > nrc) { ind = y; nrc = nr[y]; }
        nr[x] += nr[y];
    }
    if(nrc == -1) {
        vector<int> C; C.pb(x);
        ++K; c[K] = C; cmp[x] = K;
    }
}

```

```

    } else {
        c[cmp[ind]].pb(x); cmp[x] = cmp[ind];
    }
}
void heavy_path(int r) {
    l[r] = 1; dfs(r);
    for(int i=1;i<=K;++i) {
        reverse(c[i].begin(),c[i].end());
        for(int j=0;j<c[i].size();++j) poz[c[i][j]] = j;
    }
    t.resize(K+10);
    for(int i=1;i<=K;++i) t[i].resize(4*c[i].size()+10,0);
    for(int i=1;i<=N;++i) update_val(cmp[i],poz[i],v[i]);
}

```

3.9 hungarian

```

int hungarian() { //given a[n][m] matrix of costs
    vi u (n+1), v (m+1), p (m+1), way (m+1), ans(n+1);
    for (int i=1; i<=n; ++i) {
        p[0] = i; int j0 = 0;
        vi minv (m+1, INF), used (m+1, 0);
        do {
            used[j0] = 1; int i0 = p[j0], delta = INF, j1;
            for (int j=1; j<=m; ++j) {
                if (!used[j]) {
                    int cur = a[i0][j]-u[i0]-v[j];
                    if (cur < minv[j]) minv[j] = cur, way[j] = j0;
                    if (minv[j] < delta) delta = minv[j], j1 = j;
                }
            }
            for (int j=0; j<=m; ++j) {
                if (used[j]) u[p[j]] += delta, v[j] -= delta;
                else minv[j] -= delta;
            }
            j0 = j1;
        } while (p[j0] != 0);
        do {
            int j1 = way[j0]; p[j0] = p[j1]; j0 = j1;
        } while (j0);
    }
    for (int j=1; j<=m; ++j) ans[p[j]] = j;
    return -v[0];
}

```

}

3.10 lca

```
void dfs(int x, int lev) {
    e[++K] = x; L[K] = lev; poz[x] = K;
    for(auto y: g[x]) {
        dfs(y,lev+1); e[++K] = x; L[K] = lev;
    }
}
void preprocess_lca() {
    dfs(1,0);
    for(int i=2;i<=K;++i) Lg[i] = Lg[i/2]+1;
    for(int i=1;i<=K;++i) rmq[0][i]=i;
    for(int i=1;(1<<i) < K; ++i) {
        for(int j=1;j<=K-(1<<i);++j) {
            rmq[i][j] = rmq[i-1][j];
            if(L[rmq[i-1][j] + (1<<(i-1))] < L[rmq[i][j]]) {
                rmq[i][j] = rmq[i-1][j + (1<<(i-1))];
            }
        }
    }
}
int lca(int x, int y) {
    int a = poz[x], b = poz[y];
    if(a>b) swap(a,b);
    int l = Lg[b-a+1], sol = rmq[l][a];
    if(L[sol] > L[rmq[l][b - (1<<l) + 1]]) {
        sol = rmq[l][b - (1<<l) + 1];
    }
    return e[sol];
}
```

3.11 lcaLog

```
int par[Nmax][Lmax],N,M, lg[Nmax], lvl[Nmax];
vi g[Nmax];
void dfs(int nod, int lev){
    lvl[nod] = lev;
    for(auto x: g[nod])
        if(!lvl[x]) { par[x][0] = nod; dfs(x, lev+1); }
```

```
}
int lca(int x,int y){
    if(lvl[x] < lvl[y]) swap(x,y);
    int log1=1, log2=1;
    for(;(1<<log1) < lvl[x]; ++log1);
    for(;(1<<log2) < lvl[y]; ++log2);
    for(int k = log1; k >= 0; --k){
        if(lvl[x] - (1 << k) >= lvl[y]) x = par[x][k];
    }
    if (x == y) return x;
    for(int k=log2; k>=0 ;--k) {
        if(par[x][k] && par[x][k] != par[y][k]){
            x = par[x][k]; y = par[y][k];
        }
    }
    return par[x][0];
}
void preprocessLca() {
    dfs(1,1);
    for(int k=1; (1<<k) <= N; ++k){
        for(int i=1;i<=N;++i){
            par[i][k] = par[par[i][k-1]][k-1];
        }
    }
}
```

3.12 matching

```
int N,M,L,R,K,v[Nmax],p;
vi g[Nmax];
int l[Nmax],r[Nmax],u[Nmax],was[Nmax],S;
int match(int q) {
    if(was[q]) return 0; was[q]=1;
    for(auto x : g[q]) {
        if(!r[x]) { l[q]=x; r[x]=q; return 1;}
    }
    for(auto x: g[q]) {
        if(match(r[x])) { l[q]=x; r[x]=q; return 1; }
    }
    return 0;
}
void matching() { //edges i,l[i] if l[i]>0
    int ok = 1; while(ok) {
```

```

    ok = 0; for(int i=0;i<=L;++i) was[i]=0;
    for(int i=1;i<=L;++i) { if(!l[i]) ok|= match(i); }
}
}

```

3.13 royFloyd

```

FOR(k,N) FOR(i,N) FOR(j,N) {
    if(best[i][k] && best[k][j] && i!=j &&
        (best[i][k]+best[k][j]<best[i][j] || !best[i][j])) {
        best[i][j]=best[i][k]+best[k][j];
    }
}

```

3.14 strongConnected

```

vi g[Nmax],stack,viz,low,iss,aux;
vector<vi> comp;
int k,index=1,N,M,x,y;
void df(int x){
    viz[x] = index; low[x] = index;
    stack[++k] = x; iss[x] = 1; ++index;
    for(auto n : g[x]){
        if(viz[n] == 0){
            df(n); low[x] = min(low[x],low[n]);
        } else if(iss[n]) low[x] = min(low[x],low[n]);
    }
    if(low[x] == viz[x]){
        aux.clear();
        do {
            aux.pb(stack[k]); iss[stack[k]] = 0; --k;
        } while(stack[k+1] != x);
        comp.pb(aux);
    }
}
void init(){
    stack.resize(N+10); viz.resize(N+10);
    iss.resize(N+10); low.resize(N+10);
    for(int i=1;i<=N;++i) {
        if(!viz[i]) df(i);
    }
}

```

```

}

```

4 Math

4.1 comb

```

ll MOD, inv[Nmax], fact[Nmax], ifact[Nmax];
ll c[nmax][nmax];
void make_comb(int N) { // N ~ 10^3
    for(int i=0;i<=N;++i) {
        c[i][0] = 1;
        for(int j=1;j<=i;++j) c[i][j] = (c[i-1][j] + c[i-1][j-1]) % MOD;
    }
}
void make_fact(int N) { // N ~ 10^6
    inv[1] = fact[0] = fact[1] = ifact[0] = ifact[1] = 1;
    for(int i=2;i<=N;++i) {
        inv[i] = (MOD - (MOD/i) * inv[MOD%i] % MOD) % MOD;
        fact[i] = (fact[i-1]*i) % MOD;
        ifact[i] = (ifact[i-1]*inv[i]) % MOD;
    }
}
ll comb(ll a, ll b) { // a,b ~ 10^6
    ll ret = (fact[a] * ifact[b]) % MOD;
    return (ret * ifact[a-b]) % MOD;
}
ll vp(ll x) { //exponent of MOD in x!
    ll z = MOD, ret = 0;
    while(z <= x) { ret += x/z; z *= MOD; }
    return ret;
}
ll f(ll x) { // x! % MOD if we ignore the MOD factors
    if(x < MOD) return fact[x];
    ll z = 1, k = 0;
    do { z *= MOD; ++k; } while (z <= x/MOD);
    ll ret = (fact[x/z] * f(x%z)) % MOD;
    if(k%2 && t%2) return (MOD-ret)%MOD;
    else return ret;
}
ll getComb(ll A, ll B) { // A, B ~ 10^18
    if(vp(A) > vp(B) + vp(A-B)) return 0;
    if(MOD==2) return 1;
}

```

```

    return (((f(A)*inv[f(B)])%MOD)*inv[f(A-B)])%MOD;
}

```

4.2 fft

```

const int MAX = 1<<20;
typedef int value;
typedef complex<double> comp;
int N, p[MAX];
comp omega[MAX], omega_tmp[MAX], a1[MAX], a2[MAX], z1[MAX], z2[MAX];
void fft(comp *a, comp *z) {
    FOR(i, N) z[i] = a[p[i]]; int t = N;
    for (int size = 1; size < N; size *= 2) {
        t /= 2; FOR(j, size) omega_tmp[j] = omega[j*t];
        for (int i = 0; i < N; i += 2*size) {
            FOR(j, size) {
                comp c = omega_tmp[j] * z[i+j+size];
                z[i+j+size] = z[i+j] - c; z[i+j] += c;
            }
        }
    }
}
void mult(value *a, value *b, value *c, int len) {
    N = 2*len; while (N & (N-1)) ++N;
    p[0] = 0; int k = 0, t = -1;
    while ((1 << k) < N) ++k;
    for(int i = 1; i < N; ++i) {
        if ((i&(i-1)) == 0) ++t;
        p[i] = p[i^(1<<t)]; p[i] |= 1 << (k-t-1);
    }
    FOR (i, N) { a1[i] = 0; a2[i] = 0; }
    FOR (i, len) { a1[i] = double(a[i]); a2[i] = double(b[i]); }
    FOR (i, N/2) {
        omega[i] = polar(1.0, 2*M_PI/N*i);
        omega[N-i-1] = conj(omega[i]);
    }
    fft(a1, z1); fft(a2, z2);
    FOR (i, N) omega[i] = conj(omega[i]);
    FOR (i, N) a1[i] = z1[i] * z2[i] / comp(N, 0);
    fft(a1, z1);
    FOR (i, 2*len) c[i] = value(round(z1[i].real()));
}

```

4.3 fftMOD

```

#define Pmax 19
#define MOD 5767169 //magic: MOD-1 must be multiple of 2^Pmax
#define GEN1 177147 //magic: root of order 2^Pmax mod MOD
#define GEN2 5087924 //magic: inverse of GEN1
#define Nmax 530000
vi v1,v2,B; int k=1, z[2][Nmax], b[Nmax];
int powy(int x, int y) {
    if(!y) return 1; int z = powy(x,y/2);
    z = (1LL*z*z) % MOD; if(y%2) z = (1LL*z*x) % MOD;
    return z;
}
//start: index, inc: divisions, rev0 fft , rev1 reverse fft
void fft(vector<int> &v, int start, int inc, int rev) {
    if(inc==k) return; //we done
    fft(v,start,inc*2,rev); //compute first half
    fft(v,start+inc,inc*2,rev); //compute second half
    int nr = k/inc, Z = 1, zN = z[rev][nr];
    for(int i=0;i<nr/2;++i) {
        int x = (1LL*Z*v[start + (2*i+1)*inc]) % MOD;
        b[start+i*inc] = (v[start + 2*i*inc] + x) % MOD;
        b[start+(i+nr/2)*inc] = (v[start + 2*i*inc] - x + MOD) % MOD;
        Z = (1LL*Z*zN)%MOD; //Z is current root
    }
    for(int i=0;i<nr;++i) {
        v[start+i*inc] = b[start+i*inc];
    }
}
void preprocess_fft(vector<int> &v1, vector<int> &v2) {
    int pw = 0; //smallest power of 2 greater than degree
    int N = v1.size(), M = v2.size(), deg = M+N;
    while(k<deg) { k*=2; ++pw; } //smallest pw2 >= final degree
    for(int i=N;i<k;++i) v1.pb(0);
    for(int i=M;i<k;++i) v2.pb(0);
    int r1 = GEN1, r2 = GEN2; //square until roots of order 2^pw
    for(int i=pw;i<Pmax;++i) {
        r1 = (1LL*r1*r1) % MOD; r2 = (1LL*r2*r2) % MOD;
    }
    for(int nr=k;nr>=1;nr/=2) { //primitives 2^nr
        z[0][nr] = r1; z[1][nr] = r2; // 1 / z0
        r1 = (1LL*r1*r1) % MOD; r2 = (1LL*r2*r2) % MOD;
    }
}
vector<int> multiply(vector<int> &v1, vector<int> &v2) {

```

```

preprocess_fft(v1, v2);
vi ret;
fft(v1,0,1,0); fft(v2,0,1,0);
for(int i=0;i<k;++i) ret.pb((1LL*v1[i]*v2[i])%MOD);
fft(ret,0,1,1);
int inv = powy(k,MOD-2);
for(int i=0;i<k;++i) ret[i] = (1LL*ret[i]*inv) % MOD;
return ret;
}

```

4.4 fraction

```

pll contToFrac(vector<ll> &a, int start) {
    if(start >= a.size()-1) return mp(a[start],1);
    pll p = contToFrac(a,start+1);
    return reduce(a[start] * p.fs + p.sc, p.fs);
}
vector<ll> fracToCont(pll frac) {
    vector<ll> ret; ll A = frac.fs, B = frac.sc;
    while(true) {
        if(B == 0 || (A < B && ret.size() != 0) ) break; ret.pb(A/B);
        ll newA = B, newB = A%B; A = newA; B = newB;
    }
    return ret;
}

```

4.5 geom2D

```

#define PI 3.141592653589793
#define eps 0.00000001
int cmp(double a, double b) {
    if(a + eps <= b) return -1; if(a < b + eps) return 0; return 1;
}
int cmp(pdd a, pdd b) {
    int t = cmp(a.fs, b.fs); if(t) return t; return cmp(a.sc, b.sc);
}
pdd in = mp(INFINITY, INFINITY); //no solution
pdd operator+(pdd a, pdd b) { return mp(a.fs+b.fs, a.sc+b.sc); }
pdd operator-(pdd a, pdd b) { return mp(a.fs-b.fs, a.sc-b.sc); }
pdd operator*(pdd a, double t) { return mp(a.fs*t, a.sc*t); }
pdd operator/(pdd a, double t) { return mp(a.fs/t, a.sc/t); }

```

```

double operator*(pdd a, pdd b) { return a.fs*b.fs + a.sc*b.sc; }
double operator%(pdd a, pdd b) { return a.fs*b.sc - a.sc*b.fs; }
bool operator<(pdd a, pdd b) { return cmp(a,b) < 0; }
bool operator==(pdd a, pdd b) { return cmp(a,b) == 0; }
double norm(pdd a) { return sqrt(a*a); }
double arg(pdd a) { return atan2(a.sc,a.fs); }
inline double dist(pdd p, pdd q) { return norm(p-q); }
inline int ccw(pdd a, pdd b, pdd c) { return cmp((a-c)*(b-c),0); }
inline double angle(pdd a, pdd b, pdd c) { //[-PI/2, PI/2]
    pdd u = a - b, v = c - b; return atan2(u % v, u * v);
}
inline int between(pdd p, pdd q, pdd r) {
    return ccw(p,q,r) == 0 && cmp((p-q)*(r-q),0) <= 0;
}
int segInters(pdd p, pdd q, pdd r, pdd s) {
    pdd A = q-p, B = s-r, C = r-p, D = s-q;
    int a = cmp(A%C,0) + 2*cmp(A%D,0);
    int b = cmp(B%C,0) + 2*cmp(B%D,0);
    if(a==3 || a==3 || b==3 || b==3) return false;
    if (a || b || p == r || p == s || q == r || q == s) return true;
    int t = (p<r) + (p<s) + (q<r) + (q<s);
    return t!=0 && t!=4;
}
double distToSeg(pdd p, pdd q, pdd r) { // from r to pq
    pdd A = r - q, B = r - p, C = q - p;
    double a = A * A, b = B * B, c = C * C;
    if (cmp(b, a + c) >= 0) return sqrt(a);
    else if (cmp(a, b + c) >= 0) return sqrt(b);
    else return abs(A % B) / sqrt(c); //ONLY THIS IF WHOLE LINE
}
int inPoly(pdd p, vector<pdd> &T) { // -1 border, 0 outside, 1 inside
    double a = 0; int N = T.size();
    for (int i = 0; i < N; i++) {
        if (between(T[i], p, T[(i+1) % N])) return -1;
        a += angle(T[i], p, T[(i+1) % N]);
    }
    return cmp(a,0) != 0;
}
pdd lineInters(pdd p, pdd q, pdd r, pdd s) {
    if(cmp(p-q,s-r) == 0 || cmp(p-q,r-s) == 0) return mp(INFINITY,INFINITY);
    pdd a = q - p, b = s - r, c = mp(p % q, r % s);
    return mp(mp(a.fs, b.fs) % c, mp(a.sc, b.sc) % c) / (a % b);
}
pdd foot(pdd P, pdd A, pdd B) {
    pdd dir = B-A; pdd x = P-A;

```

```

    return (dir*((P-A)*dir))/(dir*dir) + A;
}
// Perp in Q on PQ at distance d
pair<pdd,pdd> disppt(pdd P, pdd Q, double d) {
    pdd dir = P - Q; pdd r = pdd(dir.sc, -dir.fs);
    pdd k = r * (d/norm(r)); return mp(Q + k, Q - k);
}
double area(vector<pdd> &v) {
    double ret = 0; int N = v.size();
    for(int i=0;i<N;++i) { ret += v[i].v[(j+1)%N]; }
    return abs(ret)/2;
}
double getX(pdd v1, pdd v2, double t) { // find (x,t) on (v1,v2)
    return (t - v1.sc)*(v1.fs - v2.fs) / (v1.sc - v2.sc) + v1.fs;
}
double getY(pdd v1, pdd v2, double t) { // find (t,y) on (v1,v2)
    return (t - v1.fs)*(v1.sc - v2.sc) / (v1.fs - v2.fs) + v1.sc;
}
vector<pdd> polygIntersect(vector<pdd> &P, vector<pdd> &Q) {
    vector<pdd> R, nope;
    int m = Q.size(), n = P.size(); if (m == 0 || n == 0) return nope;
    int a = 0, b = 0, aa = 0, ba = 0, inflag = 0;
    while ((aa < n || ba < m) && aa < 2*n && ba < 2*m) {
        pdd p1 = P[a], p2 = P[(a+1) % n], q1 = Q[b], q2 = Q[(b+1) % m];
        pdd A = p2 - p1, B = q2 - q1;
        int cross = cmp(A % B, 0), ha = ccw(p2, q2, p1), hb = ccw(q2, p2, q1);
        if (cross == 0 && ccw(p1, q1, p2) == 0 && cmp(A * B, 0) < 0) {
            if(between(p1, q1, p2)) R.pb(q1); if(between(p1, q2, p2)) R.pb(q2);
            if(between(q1, p1, q2)) R.pb(p1); if(between(q1, p2, q2)) R.pb(p2);
            if (R.size() < 2) return nope; inflag = 1; break;
        } else if (cross != 0 && segInters(p1, p2, q1, q2)) {
            if (inflag == 0) aa = ba = 0;
            R.pb(lineInters(p1, p2, q1, q2));
            inflag = (hb > 0) ? 1 : -1;
        }
        if (cross == 0 && hb < 0 && ha < 0) return R;
        bool t = cross == 0 && hb == 0 && ha == 0;
        if (t ? (inflag == 1) : (cross >= 0) ? (ha <= 0) : (hb > 0)) {
            if (inflag == -1) R.pb(q2); ba++; b++; b %= m;
        } else {
            if (inflag == 1) R.pb(p2); aa++; a++; a %= n;
        }
    }
    if (inflag == 0) {
        if (inPoly(P[0], Q)) return P; if (inPoly(Q[0], P)) return Q;
    }
}

```

```

    }
    R.erase(unique(R.begin(), R.end()), R.end());
    if (R.size() > 1 && R.front() == R.back()) R.pop_back();
    return R;
}
/***** CONVEX HULL CCW *****/
pdd V; int cmpv(pdd a, pdd b) { return ccw(V,a,b) > 0; }
vector<pdd> hull(vector<pdd> &a) { //graham
    vector<pdd> b; sort(a.begin(), a.end()); V = a[0];
    sort(a.begin()+1, a.end(), cmpv);
    for(int i = 0; i < a.size(); ++i) {
        while(b.size() >= 2 && ccw(b[b.size()-2], b[b.size()-1], a[i]) <= 0) {
            b.pop_back();
        }
        b.pb(a[i]);
    }
    return b;
}
vector<pdd> hull2 (vector<pdd> &a) {
    if (a.size() == 1) return a;
    sort (a.begin(), a.end()); pdd p1 = a[0], p2 = a.back();
    vector<pdd> up, down, b; up.pb (p1); down.pb (p1);
    for (int i=1; i<a.size(); ++i) {
        if (i==a.size()-1 || ccw (p1, a[i], p2) < 0) { //<= > for colin
            while (up.size()>=2 && ccw(up[up.size()-2], up[up.size()-1], a[i])
                >= 0) {
                up.pop_back();
            }
            up.pb(a[i]);
        }
        if(i==a.size()-1 || ccw (p1, a[i], p2) > 0) { //>= < for colin
            while (down.size()>=2 && ccw(down[down.size()-2],
                down[down.size()-1], a[i]) <= 0) {
                down.pop_back();
            }
            down.pb (a[i]);
        }
    }
    for (size_t i=0; i<down.size(); ++i) b.pb(down[i]);
    for (size_t i=up.size()-2; i>0; --i) b.pb(up[i]);
    return b;
}
/***** CIRCLES *****/
int between(pdd o, double r, pdd A, pdd B, pdd C) { //is B on arc AC (ccw)
    double a = arg(A - o), b = arg(B - o), c = arg(C - o);
    if(cmp(a,c) == -1) return cmp(a,b) <= 0 && cmp(b,c) <= 0;
}

```

```

    else return cmp(a,b) <= 0 || cmp(b,c) <= 0;
}
pair<pdd,pdd> circInters(pdd o1, double r1, pdd o2, double r2) {
    pdd dir = o2 - o1; double d = norm(dir);
    if(cmp(r1 + r2, d) == 0 || cmp(d + r2, r1) == 0 || cmp(d + r1, r2) ==
        0) {
        return mp(o1 + dir * r1/(r1 + r2), in); //tangent
    }
    if(cmp(r1 + r2, d) == -1 || cmp(d + r2, r1) == -1 || cmp(d + r1, r2) ==
        -1) {
        return mp(in, in); // too far, 2nd inside 1st, 1st inside 2nd
    }
    double x = (d*d - r2*r2 + r1*r1)/(2*d); //2 intersections
    return disppt(o1, o1 + dir * x/d, sqrt(r1*r1 - x*x));
}
pair<pdd,pdd> circLine(pdd o, double r, pdd a, pdd b){
    pdd h = foot(o, a, b); double d = norm(h - o);
    if(cmp(d,0) == 0) { //line through center
        return mp( (a - o)*r/norm(a-o) + o, (b - o)*r/norm(b - o) + o);
    }
    if(cmp(d*d, r*r) == 0) return mp(h, in); //tangent
    if(cmp(d*d, r*r) == 1) return mp(in, in); //no inters
    return disppt(o, h, sqrt(r*r - d*d));
}
pdd cinv(pdd o, double r, pdd p) { //inversion of p
    pdd p0 = p - o; return o + p0 * (r*r/(p0 * p0));
}
bool inCircle(pdd o, double r, pdd p) {
    return cmp((p - o)*(p - o), r*r) <= 0;
}
pdd circumcenter(pdd p, pdd q, pdd r) {
    pdd a = p - r, b = q - r, c = mp(a * (p + r) / 2, b * (q + r) / 2);
    return mp(c % pdd(a.sc, b.sc), pdd(a.fs, b.fs) % c) / (a % b);
}
pair<pdd,double> SpanningCircle(vector<pdd>& T) {
    int N = T.size(); random_shuffle(T.begin(),T.end());
    pair<pdd,double> C = mp(mp(0,0), 0);
    for (int i = 0; i < N; ++i) {
        if(inCircle(C.fs,C.sc,T[i])) continue;
        C = mp(T[i], 0);
        for (int j = 0; j < i; ++j) {
            if (inCircle(C.fs,C.sc, T[j])) continue;
            C = mp((T[i] + T[j]) / 2, norm(T[i] - T[j]) / 2);
            for (int k = 0; k < j; k++) {
                if (inCircle(C.fs,C.sc, T[k])) continue;

```

```

                pdd o = circumcenter(T[i], T[j], T[k]);
                C = mp(o, norm(o - T[k]));
            }
        }
    }
    return C;
}
pair<pdd, pdd> getTangents(pdd o, double r, pdd p) {
    if(inCircle(o,r,p)) return mp(in,in);
    double d = sqrt( (p-o)*(p-o) - r*r );
    double ang = arg(o-p); double ofs = atan(r/d);
    pdd dir1 = mp(cos(ang+ofs),sin(ang+ofs));
    pdd dir2 = mp(cos(ang-ofs),sin(ang-ofs));
    return mp(p + dir1*d, p + dir2*d);
}
/***** ax + by + c = 0 *****/
pair<pdd,double> getLine(pdd p1, pdd p2) { //points to ax+by+c=0
    double a = (p2.sc - p1.sc), b = (p1.fs - p2.fs);
    double n = sqrt(a*a+ b*b); a /= n; b /= n; //only if normalize
    double c = -(a*p1.fs + b*p1.sc); return mp(mp(a,b),c);
}
double dist(pdd p, pair<pdd,double> line) {
    double ret = abs(line.fs.fs*p.fs + line.fs.sc*p.sc + line.sc);
    ret /= norm(ret); return ret;
}
pdd lineInters(pair<pdd,double> l1, pair<pdd,double> l2) {
    double a1=l1.fs.fs, b1=l1.fs.sc, c1 = l1.sc;
    double a2=l2.fs.fs, b2=l2.fs.sc, c2 = l2.sc;
    double x, y;
    if(cmp(a1,0) == 0) {
        y = -c1 / b1;
        if(cmp(a2,0) != 0) x = (- c2 - b2*y) / a2;
        else return mp(INFINITY,INFINITY); //both vertical
    } else if(cmp(a2,0) == 0) {
        y = -c2 / b2; x = (- c1 - b1*y) / a1;
    } else {
        b1 /= a1; b2 /= a2; c1 /= a1; c2 /= a2;
        if(cmp(b1,b2)==0) return mp(INFINITY,INFINITY); //parallel
        else y = (c2 - c1) / (b1 - b2); x = -c1 - b1*y;
    }
    return mp(x,y);
}

```

4.6 geom3D

```

struct point {
    double x, y, z; point(){};
    point(double _x, double _y, double _z){ x=_x; y=_y; z=_z; }
    point operator+ (point p) { return point(x+p.x, y+p.y, z+p.z); }
    point operator- (point p) { return point(x-p.x, y-p.y, z-p.z); }
    point operator* (double c) { return point(x*c, y*c, z*c); }
    point operator/ (double c) { return point(x/c, y/c, z/c); }
    point operator-() const { return point(-x, -y, -z); }
    point operator%(point p) {
        return point(y*p.z-z*p.y, z*p.x-x*p.z, x*p.y-y*p.x);
    }
    double operator* (point p) { return x*p.x + y*p.y + z*p.z; }
};
inline double dist(point a, point b) { return (a-b)*(a-b); }
void makePlane(point p1, point p2, point p3, double& a, double& b,
    double& c, double& d) {
    point normal = cross(p2-p1, p3-p1);
    a = normal.x; b = normal.y; c = normal.z; d = -a*p1.x-b*p1.y-c*p1.z;
}
point planeProj(point p, double a, double b, double c, double d) {
    double l = (a*p.x+b*p.y+c*p.z+d)/(a*a+b*b+c*c);
    return point(p.x-a*l, p.y-b*l, p.z-c*l);
}
double planeDist(point p, double a, double b, double c, double d){
    return fabs(a*p.x + b*p.y + c*p.z + d) / sqrt(a*a + b*b + c*c);
}
double planePlaneDist(double a, double b, double c, double d1, double d2){
    return fabs(d1 - d2) / sqrt(a*a + b*b + c*c); //only if parallel
}
// square distance between point and line(0), ray(2) or segment(1)
double pointLineDist(point s1, point s2, point p, int type){
    double pd2 = dist(s1, s2); point r; if(pd2 == 0) r = s1;
    else {
        double u = (p-s1)*(s2-s1) / pd2;
        r = s1 + (s2 - s1)*u;
        if(type != 0 && u < 0.0) r = s1;
        if(type == 1 && u > 1.0) r = s2;
    }
    return dist(r, p);
}
// Squared distance between lines ab and cd
double lineLineDistance(point a, point b, point c, point d) {
    point v1 = b-a, v2 = d-c, cr = cross(v1, v2);

```

```

    if (cr * cr < eps) return pointLineDist(a,b, c, 0); //parallel
    else {
        point n = cr / sqrt(cr * cr); //direction
        return n * (c - a);
    }
}
point lineLineInters(point a, point b, point c, point d) {
    if(lineLineDistance(a,b,c,d) > eps) return point(); //don't intersect
    point v1 = b-a, v2 = d-c, v3 = c-a, cr = cross(v1, v2);
    double s = (cross(v3,v2) * cr) / (cr*cr);
    return a + (b-a)*s;
}
double signedTetrahedronVol(point A, point B, point C, point D) {
    double A11 = A.x - B.x, A12 = A.x - C.x, A13 = A.x - D.x;
    double A21 = A.y - B.y, A22 = A.y - C.y, A23 = A.y - D.y;
    double A31 = A.z - B.z, A32 = A.z - C.z, A33 = A.z - D.z;
    double det = A11*A22*A33 + A12*A23*A31 +
        A13*A21*A32 - A11*A23*A32 - A12*A21*A33 - A13*A22*A31;
    return det / 6;
}

/***** HULL *****/
struct twoset {
    void insert(int x) { (a == -1 ? a : b) = x; }
    bool contains(int x) { return a == x || b == x; }
    void erase(int x) { (a == x ? a : b) = -1; }
    int size() { return (a != -1) + (b != -1); } int a, b;
} E[MAXN][MAXN];
struct face { point norm; double disc; int I[3]; };
face make_face(int i, int j, int k, int inside_i) {
    E[i][j].insert(k); E[i][k].insert(j); E[j][k].insert(i);
    face f; f.I[0] = i; f.I[1] = j; f.I[2] = k;
    f.norm = (A[j] - A[i]) % (A[k] - A[i]); f.disc = f.norm * A[i];
    if(f.norm * A[inside_i] > f.disc) {
        f.norm = -f.norm; f.disc = -f.disc;
    }
    return f;
}
vector<face> hull3(vector<point> &A) {
    vector<face> faces; face f; memset(E, -1, sizeof(E));
    FOR(i,4) for(int j=i+1;j<4;j++) for(int k=j+1;k<4;k++) {
        faces.pb(make_face(i, j, k, 6 - i - j - k));
    }
    for(int i = 4; i < N; i++) {
        for(int j = 0; j < faces.size(); j++) {

```



```

    f = faces[j];
    if(f.norm * A[i] > f.disc) {
        E[f.I[0]][f.I[1]].erase(f.I[2]);
        E[f.I[0]][f.I[2]].erase(f.I[1]);
        E[f.I[1]][f.I[2]].erase(f.I[0]);
        faces[j--] = faces.back();
        faces.resize(faces.size() - 1);
    }
}
int nfaces = faces.size();
for(int j = 0; j < nfaces; j++) {
    f = faces[j];
    for(int a = 0; a < 3; a++) for(int b = a + 1; b < 3; b++) {
        int c = 3 - a - b;
        if(E[f.I[a]][f.I[b]].size() == 2) continue;
        faces.pub(make_face(f.I[a], f.I[b], i, f.I[c]));
    }
}
return faces;
}

```

4.7 geomMisc

```

/***** CLOSEST POINTS *****/
vector<pair<pll,int>> v,x,y;
ll INF = 4e18;
ll dist(pll a, pll b) {
    return (a.fs - b.fs) * (a.fs - b.fs) + (a.sc - b.sc) * (a.sc - b.sc);
}
pair<ll,pii> solve(int st, int dr) {
    if (st >= dr - 1) return mp(INF,mp(0,0));
    if (dr - st == 2) {
        if (y[st] > y[st + 1]) swap(y[st], y[st + 1]);
        return mp(dist(x[st].fs, x[st + 1].fs),mp(x[st].sc, x[st+1].sc));
    }
    int mij = (st + dr) / 2;
    pair<ll,pii> ret = min(solve(st,mij),solve(mij,dr));
    merge(y.begin() + st, y.begin() + mij, y.begin() + mij, y.begin() + dr,
        v.begin());
    copy(v.begin(), v.begin() + (dr - st), y.begin() + st);
    int nr = 0;
    for (int i=st; i<dr; ++i) {

```

```

        if (abs(y[i].fs.sc - x[mij].fs.fs) < ret.fs) v[nr++] = y[i];
    }
    for(int i=0;i<nr;++i) {
        for (int j=i+1; j<nr && j<=i+7; ++j) {
            ll d = dist(v[i].fs,v[j].fs);
            if(d < ret.fs) ret = mp(d,mp(v[i].sc,v[j].sc));
        }
    }
    return ret;
}
pair<ll,pii> closest_points() {
    int N = x.size(); sort(x.begin(), x.end()); v.resize(N);
    for(ll i=0;i<N;++i) y.pb( mp(mp(x[i].fs.sc, x[i].fs.fs), x[i].sc));
    return solve(0,N);
}
/***** MAX AREA *****/
pair<pdd,pair<pdd,pdd>> getMaxArr(vector<pdd> &v) {
    v = convex_hull(v);
    int A = 0, B = 1, C = 2, N = v.size();
    double S = 0; pdd a,b,c;
    while(true) {
        double T = arr(v[A],v[B],v[C]);
        if(T > S) {a = v[A], b = v[B], c = v[C]; S = T;}
        while(true) {
            while(T <= arr(v[A], v[B], v[(C+1) %N])) {
                C = (C+1) %N; T = arr(v[A],v[B],v[C]);
                if(T > S) {a = v[A], b = v[B], c = v[C]; S = T;}
            }
            if(T < arr(v[A], v[(B+1) %N], v[C])) {
                B = (B+1) %N; T = arr(v[A],v[B],v[C]);
                if(T > S) {a = v[A], b = v[B], c = v[C]; S = T;}
            } else break;
        }
        A = (A+1) % N; if(A == 0) break;
        if(A == B) B = (B+1) %N; if(B == C) C = (C+1) %N;
    }
    return mp(a,mp(b,c));
}
/***** FARTHEST POINTS *****/
pair<pdd,pdd> farthestPoints(vector<pdd> &v) {
    v = convex_hull(v); vector<pair<pdd,pdd>> A; //antipodal
    int k = 1, M = v.size();
    while(area(v[0],v[k+1],v[M-1]) > area(v[0],v[k],v[M-1])) ++k;
    int i = 0, j = k;
    //If want farthest point from each edge, do j<2*M and double array

```

```

while(i<=k && j<M) {
    A.pb(mp(v[i],v[j]));
    while(j<M-1 && area(v[i+1],v[j+1],v[i]) > area(v[i+1],v[j],v[i])) {
        A.pb(mp(v[i],v[j])); ++j;
    }
    ++i;
}
pair<pdd,pdd> ret = mp(v[0],v[0]);
for(auto p: A) {
    if(dist(p.fs,p.sc) > dist(ret.fs,ret.sc)) ret = p;
}
return ret;
}
/***** TRANSFORMATIONS AND ELLIPSE *****/
double rot[3][3] = {{cos(a),-sin(a),0},{sin(a),cos(a),0},{0,0,1}};
double rotx[4][4] = {{1,0,0,0},{0,cos(a),-sin(a),0},
{0,sin(a),cos(a),0},{0,0,0,1}};
double roty[4][4] = {{cos(a),0,sin(a),0},{0,1,0,0},
{-sin(a),0,cos(a),0},{0,0,0,1}};
double rotz[4][4] = {{cos(a),-sin(a),0,0},{sin(a),cos(a),0,0},
{0,0,1,0},{0,0,0,1}};
long double ellipseInt(long double x) {
    return b*(x*sqrt(a*a - x*x) + a*a*atan(x / sqrt(a*a - x*x))) / (2*a);
}

```

4.8 geomSphere

```

#define PI 3.14159265358979
double R = 6370.0; //earth
double rad(double x) { return x * PI / 180.0; }
double ang(double x) { return x * 180.0 / PI; }
double dist(pdd a, pdd b) {
    if(a == b) return 0;
    double v = sin(a.fs)*sin(b.fs) + cos(a.fs) * cos(b.fs) * cos(a.sc -
        b.sc);
    return acos(v);
}
struct cel {
    double x,y,z;
    cel(double lat, double lon) {
        x = cos(lat) * cos(lon); y = cos(lat) * sin(lon); z = sin(lat);
    }
    cel(double a1, double a2, double a3) { x = a1, y = a2, z = a3; }
}

```

```

inline cel operator^(cel c1) { //cross
    return cel(y*c1.z - c1.y * z, c1.x * z - c1.z * x, c1.y * x - c1.x *
        y);
}
inline cel operator*(double cx) { return cel(cx*x,cx*y,cx*z); }
double mag() { return sqrt(x*x + y*y + z*z); }
pdd rev() {
    double lat = asin(z); double tmp = cos(lat);
    double sgn = asin(y/tmp); double lon = acos(x / tmp);
    if(sgn < 0) lon = 2 * PI - lon; return mp(lat,lon);
}
};
int inside(pdd a, pdd b, pdd c) {
    return abs(dist(a,b) + dist(a,c) - dist(b,c)) <= 0.000001;
}
pdd inter(pdd a, pdd b, pdd c, pdd d) {
    cel p1(a.fs,a.sc); cel p2(b.fs,b.sc);
    cel p3(c.fs,c.sc); cel p4(d.fs,d.sc);
    cel v1 = p1 ^ p2; cel v2 = p3 ^ p4;
    v1 = v1 * (1.0 / v1.mag()); v2 = v2 * (1.0 / v2.mag());
    cel d1 = v1 ^ v2; d1 = d1 * (1.0 / d1.mag());
    cel d2 = d1 * (-1);
    pdd x1 = d1.rev(), x2 = d2.rev();
    if(inside(x1,a,b) && inside(x1,c,d)) return x1;
    if(inside(x2,a,b) && inside(x2,c,d)) return x2;
    return mp(inf,inf);
}

```

4.9 numberTheory

```

int lcm(int a, int b) { return a / __gcd(a,b) * b; }
int gcd(int a, int b, int &x, int &y) {
    if(!b) { x=1; y=0; return a; }
    else {
        int x0, y0, d = gcd(b,a%b,x0,y0);
        x = y0; y = x0 - a/b * y0; return d;
    }
}
pair<int,int> euclid(int a, int b, int c) { //ax - by = c;
    int x, y, sol1, sol2; int d = gcd(a,b,x,y);
    if(c%d) return mp(0,0); //no sol
    } else { sol1 = (c/d)*x; sol2 = -(c/d)*y; }
    //only if want minimal
}

```

```

while(sol1 < 0 || sol2 < 0) { sol1 += b/d; sol2 += a/d;}
while(sol1 >= b/d || sol2 >= a/d) { sol1 -= b/d; sol2 -= a/d;}
return mp(sol1,sol2);
}
int inversmod(int a, int b) { //inverse of a mod b
    int x,y; gcd(a,b,x,y);
    if(x<0) { int k = (-x-1)/b + 1; x += k*b;}
    return x%b;
}
ll mulmod(ll a,ll b,ll c) { // a*b mod c
    ll x = 0, y=a%c;
    while(b > 0){ if(b%2 == 1) x = (x+y)%c; y = (y*2)%c; b /= 2; }
    return x%c;
}
int fi[Nmax],sp[Nmax]; //sp = smallest prime
void makeSieve(int lim) {
    for(int i=2;i<=lim;++i) {
        if(!sp[i]) {
            for(int j=i;j<=lim;++j) { if(!sp[j]) sp[j] = i;}
            sp[i] = i;
        }
    }
}
void makeFi(int lim) {
    fi[1] = 1; for(int i=2;i<=lim;++i) fi[i] = i-1;
    for(int i=2;i<=lim;++i) {
        for(int j=2;j<=lim;++j) fi[i*j] -= fi[i];
    }
}
vector<int> linSolver(int a, int b, int c) { //ax = b (mod c)
    vector<int> sol; int d = __gcd(a,c);
    pair<int, int> e = euclid(a,c,d);
    int x = e.fs, y = e.sc;
    if(b%d == 0) {
        x = ((b/d * x) % c + c) % c;
        for(int i=0;i<d;++i) {
            sol.pb(((x + c/d * i)%c + c)%c );
        }
    }
    return sol;
}
// x = a1 mod m1, x = a2 mod m2
pair<int,int> crt(int a1, int m1, int a2, int m2) {
    int d = gcd(m1,m2);
    pair<int,int> p = euclid(m1,m2,d);

```

```

    int s = p.fs, t = -p.sc;
    if (a1 % d != a2 % d) return make_pair(0, -1);
    int x = (s * a2 * m1 + t * a1 * m2) % (m1*m2);
    x = (x + m1*m2) % (m1*m2);
    return mp(x/d, m1*m2/d);
}
// x = a[i] (mod m[i]) also returns period (lcm)
pair<int,int> chinese(vector<int> &a, vector<int> &m) {
    pair<int,int> ret = mp(a[0], m[0]);
    for (int i = 1; i < a.size(); ++i) {
        ret = crt(ret.fs, ret.sc, a[i], m[i]); if (ret.sc == -1) break;
    }
    return ret;
}

```

4.10 polynomial

```

typedef complex<double> cdouble;
typedef vector<cdouble> pol;
int cmp(double a, double b) { //same as geom2d
    if(a + eps <= b) return -1; if(a <= b + eps) return 0; return 1;
}
int cmp(cdouble x, cdouble y = 0) { return cmp(abs(x), abs(y));}
pol deriv(pol &a) {
    int N = a.size(); pol ret(N-1);
    for(int i=1;i<N;++i) ret[i-1] = a[i]*cdouble(i); return ret;
}
pair<pol, cdouble> ruffini(pol &a, cdouble z) { // divide by (x-z)
    int N = a.size(); pol ret;
    if (N == 0) return mp(ret, 0); if (N == 1) return mp(ret, a[0]);
    ret.resize(N-1); ret[N-2] = a[N-1];
    for(int i=N-2;i>0;--i) ret[i-1] = ret[i]*z + a[i];
    return mp(ret, ret[0]*z + a[0]);
}
cdouble getVal(pol &a, cdouble z) { return ruffini(a,z).sc; }
cdouble find_one_root(pol &a, cdouble x) {
    pol a1 = deriv(a); pol a2 = deriv(a1);
    int N = a.size(), m = 1000;
    while (m--) {
        cdouble y0 = getVal(a,x);
        if(cmp(y0) == 0) break;
        cdouble G = getVal(a1,x) / y0;
        cdouble H = G * G - getVal(a2,x) / y0;
    }
}

```

```

    cdouble R = sqrt(cdouble(N-1) * (H * cdouble(N) - G * G));
    cdouble D1 = G + R, D2 = G - R;
    cdouble A = cdouble(N) / (cmp(D1, D2) > 0 ? D1 : D2);
    x -= A; if (cmp(A) == 0) break;
}
return x;
}

```

5 Misc

5.1 binSearch

```

int binary_search(int val) { //array A of size N
    int i, step;
    for (step = 1; step < N; step <= 1);
    for (i = 0; step; step >= 1) {
        if (i + step < N && A[i + step] <= val) i += step;
    }
    return i;
}

```

5.2 dpOptim

```

/* 1. best[i] = max(best[i] + a[i]*b[j]) a increasing, b decreasing
max:q(a[i]),add(b[i],best[i]); min: q(-a[i]),add(b[i],-best[i])
2. best[i][j] = max(best[i-1][k] + b[k]*a[j]), a increasing, b decreasing
Do independently for each i
max:q(a[j]),add(b[j],best[i-1][j]);min:q(-a[j]),add(b[j],-best[i-1][j]) */
int cnt; pll h[Nmax]; //stores the lines
pll operator-(pll a, pll b) { return mp(a.fs-b.fs, a.sc-b.sc); }
inline int cw(pll a, pll b, pll c) {
    pll x = a-c, y = b-c; return x.fs*y.sc <= x.sc*y.fs; //Beware overflow
}
void add(pll a, pll b) { // Add ax+b (decreasing order of a)
    h[cnt++] = mp(a,b);
    while(cnt > 2 && cw(h[cnt-3],h[cnt-2],h[cnt-1])) {
        h[cnt-2] = h[cnt-1]; --cnt;
    }
}
long long query(long long x) { //return max ax+b

```

```

int st = 0, dr = cnt - 2, ret = cnt-1;
while(st <= dr) {
    int mij = (st+dr)/2;
    if(h[mij].fs * x + h[mij].sc > h[mij+1].fs*x + h[mij+1].sc) {
        ret = mij; dr = mij-1;
    } else st = mij+1;
}
return h[ret].fs * x + h[ret].sc;
}
/*KNUTH: d[i][j] = min(d[i][k] + d[k][j] + c[i][j])
DIVCONQ: d[i][j] = min(d[i-1][k] + c[k][j]), c[i][j] <= c[i][j+1]
compute(j, l, r, optL, optR) m = (l+r)/2; brut(m,optL,optR);
compute(j,l,m-1,optL, opt[m][j]); compute(j,m+1,r, opt[m][j], optR);
*/

```

5.3 gauss

```

double A[Nmax][Nmax], X[Nmax];
int k, N, M; // A[i][1] * X[1] + ... + A[i][M] * X[M] = A[i][M+1]
void gauss() {
    int i=1,j=1;
    while(i<=N && j<=M) {
        int k;
        for(k=i;k<=N;++k) if( A[k][j]<-EPS || A[k][j]>EPS) break;
        if(k==N+1) { ++j; continue; }
        if(k!=i) for(int q=1;q<=M+1;++q) swap(A[i][q],A[k][q]);
        for(int q=j+1;q<=M+1;++q) A[i][q] /= A[i][j];
        A[i][j] = 1;
        for(int u=i+1;u<=N;++u) {
            for(int q=j+1;q<=M+1;++q) A[u][q] -= A[u][j]*A[i][q];
            A[u][j]=0;
        }
        ++i; ++j;
    }
    for(int i=N;i>0;--i) {
        for(int j=1;j<=M+1;++j) {
            if(A[i][j]>EPS || A[i][j]<-EPS) {
                if(j==M+1) {} //HANDLE NO SOLUTION
                X[j] = A[i][M+1];
                for(int k=j+1;k<=M;++k) X[j] -= X[k]*A[i][k];
                break;
            }
        }
    }
}

```

```

    }
}

```

5.4 matpow

```

vvll mul(vvll &a, vvll &b) {
    int N = sz(a), M = sz(a[0]), P = sz(b[0]);
    vvll ret(N, vll(P,0));
    FOR(i,N) FOR(j,P) FOR(k,M)
        ret[i][j] += a[i][k]*b[k][j]; ret[i][j] %= MOD;
    return ret;
}
vvll matpw(vvll &v, long long k) {
    int N = sz(v); vvll ret(N, vll(N,0));
    for(int i=0;i<N;++i) ret[i][i] = 1;
    for(int i=0;(1LL<<i) <= k; ++i) {
        if((1LL<<i)&k) ret = mul(ret, v); v = mul(v,v);
    }
    return ret;
}

```

5.5 parse

```

#define BUFFER_SIZE 1234
char buff[BUFFER_SIZE];
int buffIt;
inline int getNumber() {
    int ret = 0;
    while (buff[buffIt] < '0' || buff[buffIt] > '9')
        if (++buffIt == BUFFER_SIZE)
            fread(buff, BUFFER_SIZE, 1, stdin), buffIt = 0;
    while (buff[buffIt] >= '0' && buff[buffIt] <= '9') {
        ret = ret * 10 + buff[buffIt] - '0';
        if (++buffIt == BUFFER_SIZE) {
            buffIt = 0; fread(buff, BUFFER_SIZE, 1, stdin);
        }
    }
    return ret;
}
for(int i=1;i<=M;++i) {
    if(!getline(cin, s)) break;

```

```

    if (s == "") { --i; continue; }
    stringstream ss; ss << s;
    int x; while(ss >> x) { g[i].push_back(x+M+1); }
}

```

5.6 simplex

```

// maximize cx, Ax <= b and x >= 0, A = Mxy, b size M, c size y
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
DOUBLE inf = -numeric_limits<DOUBLE>::infinity();
const DOUBLE EPS = 1e-9;

struct LPSolver {
    int m, n;
    VI B, y; //slack variables, actual variables
    VVD D; //canonical form
    LPSolver(const VVD &A, const VD &b, const VD &c) {
        m = b.size(); n = c.size(); y = VI(n+1);
        B = VI(m); D = VVD(m+2,VD(n+2));
        for (int i = 0; i < m; i++) {
            for (int j = 0; j < n; j++) D[i][j] = A[i][j];
        }
        for (int i = 0; i < m; i++) {
            B[i] = n + i; D[i][n] = -1; D[i][n + 1] = b[i];
        }
        for (int j = 0; j < n; j++) {
            y[j] = j; D[m][j] = -c[j];
        }
        y[n] = -1; D[m + 1][n] = 1;
    }
    void Pivot(int r, int s) {
        double inv = 1.0 / D[r][s];
        for (int i = 0; i < m + 2; i++) {
            if (i == r) continue;
            for (int j = 0; j < n + 2; j++) {
                if (j == s) continue;
                D[i][j] -= D[r][j] * D[i][s] * inv;
            }
        }
        for (int j = 0; j < n + 2; j++) {

```

```

    if (j != s) D[r][j] *= inv;
}
for (int i = 0; i < m + 2; i++) {
    if (i != r) D[i][s] *= -inv;
}
D[r][s] = inv; swap(B[r], y[s]);
}
bool Simplex(int phase) {
    int x = phase == 1 ? m + 1 : m;
    while (true) {
        int s = -1;
        for (int j = 0; j <= n; j++) {
            if (phase == 2 && y[j] == -1) continue;
            if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && y[j] <
                y[s]) s = j;
        }
        if (D[x][s] > -EPS) return true;
        int r = -1;
        for (int i = 0; i < m; i++) {
            if (D[i][s] < EPS) continue;
            if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
                (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] <
                B[r]) r = i;
        }
        if (r == -1) return false;
        Pivot(r, s);
    }
}
DOUBLE Solve(VD &x) {
    int r = 0;
    for (int i = 1; i < m; i++) {
        if (D[i][n + 1] < D[r][n + 1]) r = i;
    }
    if (D[r][n + 1] < -EPS) {
        Pivot(r, n);
        if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return inf;
        for (int i = 0; i < m; i++) if (B[i] == -1) {
            int s = -1;
            for (int j = 0; j <= n; j++) {
                if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && y[j] <
                    y[s]) {
                    s = j;
                }
            }
        }
        Pivot(i, s);
    }
}

```

```

    }
}
if (!Simplex(2)) return inf;
x = VD(n);
for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
return D[m][n + 1];
}
};

```

5.7 ternary

```

// F is some concave function
double ternarySearch(double left, double right) { // finds max
    while (abs(right - left) > EPS) {
        long double lt = left + (right - left) / 3.0;
        long double rt = right - (right - left) / 3.0;
        if (F(lt) < F(rt)) left = lt;
        else right = rt; // reverse if convex and min
    }
    return (left + right) / 2.0;
}

```

5.8 util

```

struct cmp {
    bool operator()(piii a, piii b) { return a.fs > b.fs; }
};
priority_queue<piii, vector<piii>, cmp> pq;
namespace std {
    template <>
    struct hash<pii> {
    public:
        size_t operator()(pair<int, int> x) const throw() {
            size_t h = x.fs + x.sc * 1145; return h;
        }
    };
}
for (int news=state; news; news=state&(news-1)) // all subsets of state

```

6 String

6.1 ahoCorasick

```

int tr[Nmax], nw[Nmax], NR, term[Nmax], len[Nmax], to[Nmax][sigma],
    link[Nmax], sz = 1;
void add(string s) { // doesn't handle dups
    int cur = 0;
    for(auto c: s) {
        if(!to[cur][c - 'a']) {
            to[cur][c - 'a'] = sz++;
            len[to[cur][c - 'a']] = len[cur] + 1;
        }
        cur = to[cur][c - 'a'];
    }
    term[cur] = cur; tr[cur] = ++NR;
}

void push_links() {
    queue<int> Q; Q.push(0);
    while(!Q.empty()) {
        int V = Q.front(); Q.pop(); int U = link[V];
        if(!term[V]) term[V] = term[U];
        for(int c = 0; c < sigma; c++) {
            if(to[V][c]) {
                link[to[V][c]] = V ? to[U][c] : 0;
                Q.push(to[V][c]);
            } else to[V][c] = to[U][c];
        }
    }
}

void match(string s) {
    int cur = 0;
    for(auto c : s) {
        cur = to[cur][c-'a']; int f = cur;
        while(f) {
            if(tr[f]) tr[f]; // match on tr[f]
            if(f == term[f]) f = term[link[f]];
            else f = term[f];
        }
    }
}

```

6.2 expresioneval

```

string gb; vector<vector<string>> ops;
// is operation op, at location loc, when the string is st,dr
int is(string op, int loc,int st,int dr) {
    if(loc + op.size() - 1 > dr) return 0;
    int ok = 1;
    for(int i=0;i<op.size() && ok;++i) {
        if(gb[i+loc] != op[i]) ok = 0;
    }
    return ok;
}

int make(string op,int x,int y) { // make the operations
    if(op == "+") return x+y; return 0;
}

// evals substring(st,dr), when we should only check lvl forward
int eval(int st,int dr, int lvl) {
    for(int t = lvl;t<ops.size();++t) {
        int par = 0;
        for(int i = dr;i>=st;--i) {
            if(gb[i] == '(') ++ par; if(gb[i] == ')') -- par;
            if(par) continue;
            for(auto op : ops[t]) {
                if(is(op,i,st,dr)) {
                    return make(op,eval(st,i-1,t),eval(i+op.size(),dr,t));
                }
            }
        }
    }
    if(gb[st] == '(') return eval(st+1,dr-1,0);
    return getnum(st,dr);
}

void init() { //add operations in order, call at main start
    ops.pb(vector<string>({"+", "-"}));
    ops.pb(vector<string>({"/", "%", "*"}));
}

int eval(string &s) {
    gb = s;
    for(auto c : s) if(c != ' ') gb.pb(c);
    int ret = eval(0,gb.size()-1,0);
    return ret;
}

```

6.3 kmp

```
void make() {
    int k = -1; nx[0] = -1;
    for(int i=1;i<sz(s1);++i) {
        while(k >= 0 && s1[k+1] != s1[i]) k = nx[k];
        if(s1[k+1] == s1[i]) ++k; nx[i] = k;
    }
}

void match() {
    int k=-1;
    for(int i=0;i<sz(s2);++i) {
        while(k >= 0 && s1[k+1] != s2[i]) k = nx[k];
        if(s1[k+1] == s2[i]) ++k;
        if(k==sz(s1)-1) k = nx[k]; // match on i - sz(s1)
    }
}
```

6.4 pscpld

```
char s[2010000], s1[2010000];
int val[2020201],maxind,maxVal,N;
void make_sir(){
    s1[0]='*';
    for(int i=1;i<=N;++i) { s1[i*2-1]=s[i]; s1[i*2]='*';}
}

ll pscpld (char *s) {
    ll S = 0; N = strlen(s+1); make_sir();
    for(int i=1;i<2*N;++i) {
        if(maxVal >= i) {
            int loc = maxind - (i-maxind);
            val[i] = min(val[loc],maxVal-i);
        }
        while((i - val[i] >= 0) && (i + val[i] <= 2*N) &&
            (s1[i-val[i]] == s1[i+val[i]])) {
            ++val[i];
            if(i + val[i] > maxVal){
                maxVal = i + val[i]; maxind = i;
            }
        }
    }
    for(int i=1;i<2*N;++i){
        S += (val[i]+1)/2; if(s1[i]=='*') --S;
    }
```

```
}
return S;
}
```

6.5 rabinquery

```
#define Nmax 101010
#define p1 47
#define p2 149
#define MOD1 666013
#define MOD2 991777
int nr1[Nmax],pow1[Nmax],pow2[Nmax],nr2[Nmax],nrfin;
char car[Nmax]; // string we want to hash, STARTING FROM 1
int N,M;
void make() {
    pow1[0]=1,pow2[0]=1;
    for(int i=1;i<=N;++i) {
        pow1[i]=(1LL*pow1[i-1]*p1)%MOD1;
        pow2[i]=(1LL*pow2[i-1]*p2)%MOD2;
        nr1[i]=((1LL*nr1[i-1]*p1)%MOD1 + car[i])%MOD1;
        nr2[i]=((1LL*nr2[i-1]*p2)%MOD2 + car[i])%MOD2;
    }
}

int query(int x,int y,int x1,int y1,int debug) {
    int sol1,sol2,sol12,sol22;
    sol1=1LL*(nr1[y]-(1LL*pow1[y-x+1]*nr1[x-1])%MOD1+MOD1)%MOD1;
    sol2=1LL*(nr1[y1]-(1LL*pow1[y1-x1+1]*nr1[x1-1])%MOD1+MOD1)%MOD1;
    sol12=(nr2[y]-(1LL*pow2[y-x+1]*nr2[x-1])%MOD2+MOD2)%MOD2;
    sol22=(nr2[y1]-(1LL*pow2[y1-x1+1]*nr2[x1-1])%MOD2+MOD2)%MOD2;
    if(sol1==sol2 && sol12 == sol22) return 1; return 0;
}
```

6.6 suffixAuto

```
unordered_map<char, int> h[200100];
int len[200100],lnk[200100],last,curr,nr;
long long add_char(char c) {
    long long ret = 0;
    curr = ++nr; len[curr] = len[last] + 1; int p = last;
    while(p != -1 && !h[p][c]){h[p][c] = curr; p = lnk[p];}
    if(p == -1) {
```



```

    lnk[curr] = 0; ret += len[curr];
} else {
    int q = h[p][c];
    if(len[q] == len[p]+1) {
        lnk[curr] = q; ret += (len[curr] - len[q]);
    } else {
        int clone = ++nr;
        len[clone] = len[p] + 1; lnk[clone] = lnk[q];
        ret += (len[clone] - len[lnk[q]]); h[clone] = h[q];
        while(p!=-1 && h[p][c] == q) {
            h[p][c] = clone; p = lnk[p];
        }
        ret -= (len[q] - len[lnk[q]]); lnk[q] = clone;
        ret += (len[q] - len[lnk[q]]); lnk[curr] = clone;
        ret += (len[curr] - len[clone]);
    }
}
last = curr; return ret;
}
void suffix_automaton(string &s) {
    last = 0, curr = 0, nr = 0; len[0] = 0; lnk[0] = -1;
    for(auto c: s) add_char(c); //also counts new suffixes
}

```

6.7 suffixarray

```

struct entry {
    int nr[2], p;
} L[Nmax];
int P[LMax][Nmax], N, i, stp, cnt;
bool cmp(const entry &a, const entry &b) {
    return a.nr[0] == b.nr[0] ? (a.nr[1] < b.nr[1]) : (a.nr[0] < b.nr[0]);
}
int lcp(int x, int y) {
    int k, ret = 0; if (x == y) return N - x;
    for (k = stp - 1; k >= 0 && x < N && y < N; --k) {
        if (P[k][x] == P[k][y]) {
            x += 1 << k; y += 1 << k; ret += 1 << k;
        }
    }
    return ret;
}
void suffArr(string A) {

```

```

    int N = a.size();
    for(int i=0;i<N;++i) P[0][i] = A[i] - 'a';
    for (stp = 1, cnt = 1; cnt >> 1 < N; ++stp, cnt <= 1) {
        for (i = 0; i < N; ++i) {
            L[i].p = i; L[i].nr[0] = P[stp - 1][i];
            L[i].nr[1] = i + cnt < N ? P[stp - 1][i + cnt] : -1;
        }
        sort(L, L + N, cmp);
        for (i = 0; i < N; ++i)
            P[stp][L[i].p] = i > 0 && L[i].nr[0] == L[i - 1].nr[0] &&
                L[i].nr[1] == L[i - 1].nr[1] ? P[stp][L[i - 1].p] : i;
    }
}

```

6.8 zalgo

```

// z -> int array, s2 -> char array, N, it's length. At the end have z[i]
int left=0, right=0;
for(int i=1;i<N;++i) {
    if( i > right) {
        left = i, right = i;
        while (right < N && s2[right-left] == s2[right]) ++right;
        z[i] = right - left; --right;
    } else {
        int k = i - left; if(z[k] < right-i+1) z[i] = z[k];
        else {
            left=i;
            while (right < N && s2[right - left] == s2[right]) ++right;
            z[i] = right-left; --right;
        }
    }
}
}
}

```