# Hardware Acceleration of Sparse and Irregular Tensor Computations of ML Models: A Survey and Insights

Shail Dave, Student Member, IEEE, Riyadh Baghdadi, Member, IEEE, Tony Nowatzki, Member, IEEE, Sasikanth Avancha, Member, IEEE, Aviral Shrivastava, Senior Member, IEEE, and Baoxin Li, Senior Member, IEEE

Abstract-Machine learning (ML) models are widely used in many important domains. For efficiently processing these computational- and memory-intensive applications, tensors of these over-parameterized models are compressed by leveraging sparsity, size reduction, and quantization of tensors. Unstructured sparsity and tensors with varying dimensions yield irregular computation, communication, and memory access patterns; processing them on hardware accelerators in a conventional manner does not inherently leverage acceleration opportunities. This paper provides a comprehensive survey on how to efficiently execute sparse and irregular tensor computations of ML models on hardware accelerators. In particular, it discusses enhancement modules in the architecture design and the software support; categorizes different hardware designs and acceleration techniques and analyzes them in terms of hardware and execution costs; highlights further opportunities in terms of hardware/software/model co-design optimizations (inter/intra module). The takeaways from this paper include: understanding the key challenges in accelerating sparse, irregular-shaped, and quantized tensors; understanding enhancements in accelerator systems for supporting their efficient computations; analyzing trade-offs in opting for a specific design choice for encoding, storing, extracting, communicating, computing, and load-balancing the non-zeros; understanding how to map and compile models with sparse tensors on the accelerators; understanding recent design trends for efficient accelerations and further opportunities.

Index Terms—Machine learning, deep learning, deep neural networks, spatial architecture, dataflow, sparsity, compact models, pruning, quantization, dimension reduction, tensor decomposition, energy efficiency, hardware/software/model co-design, compiler optimizations, reconfigurable computing, VLSI.

#### I. INTRODUCTION

Machine learning (ML) models implement intelligence in computing systems. Different ML models are widely used in several important domains including computer vision (object classification [1]–[3] and detection [4]–[6]), natural language processing [7]–[9], media generation [10], recommendation

Shail Dave, Aviral Shrivastava, and Baoxin Li are with the School of Computing Informatics and Decision Systems Engineering at Arizona State University, Tempe, AZ, 85281 USA (e-mail: shail.dave@asu.edu; aviral.shrivastava@asu.edu; baoxin.li@asu.edu).

Riyadh Baghdadi is with the Computer Science and Artificial Intelligence Laboratory at Massachusetts Institute of Technology, Cambridge, MA 02139 USA (e-mail: baghdadi@mit.edu).

Tony Nowatzki is with the School of Computer Science at University of California, Los Angeles, CA 90095 USA (e-mail: tjn@cs.ucla.edu).

Sasikanth Avancha is with the Parallel Computing Lab at Intel Labs, Bangalore, India (email:sasikanth.avancha@intel.com).

systems [11], [12], medical diagnosis [13], large-scale scientific computing [14], embedded systems [15], mobile and edge processing [16], [17], and even for designing or optimizing hardware and software systems [18], [19]. Domaincustomized accelerators can significantly speed-up their execution in an energy-efficient manner [20]-[23]. However, the computational and memory requirements for processing these models have surged drastically [24]. Moreover, ML models can be deeper and larger which improves learning accuracy, but significant redundancy may exist in these often overparameterized models [25], [26]. Therefore, recent techniques for efficient learning and inference have proposed compressing tensors of ML models. Tensors are compressed by inducing and leveraging: (a) sparsity (zero values in tensors) [27]–[31], (b) size reduction (tensor decomposition, dimension reduction, and shape reduction) [3], [32]-[35], and (c) quantization (precision lowering and value sharing) [27], [36]. With significantly lowered computational, storage, and communication requirements, efficient processing of compressed tensors (sparse, size-reduced, and quantized) offers notable acceleration and energy efficiency opportunities [37]-[40].

Hardware accelerators can efficiently process tensor computations of ML models. In particular, coarse-grain spatial architectures are a common choice for hardware accelerator designs. They comprise of an array of processing elements (PEs) with local registers/memory and shared memory. These accelerators feature interconnects like mesh or multicast for communicating data to PEs and spatially reusing the data, which lowers the accesses to memory hierarchy. With simple PE designs and effective spatial and temporal management of the data and computations, such architectures achieve high speedups and energy-efficiency [20]–[22].

However, special mechanisms are needed to exploit the acceleration benefits due to tensor sparsity, size reduction, and quantization. Because, while hardware accelerators for ML can process low-precision tensors, they inherently cannot benefit from sparsity [41], [42]. They are designed for performing structured computations with regular memory accesses and communication patterns. Without special support for sparse tensors, they fetch all the data including zero values from memory and feed into PEs, thereby wasting the execution time. Sparsity, especially unstructured, induces irregularity in processing, since non-zeros (NZs) or blocks of NZs are scattered across tensors. So, leveraging sparsity necessitates additional

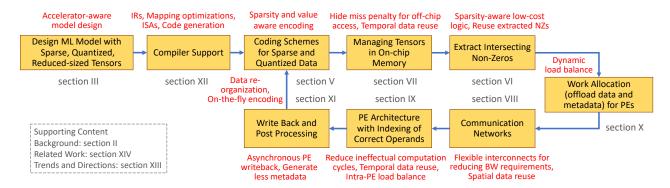


Fig. 1. Overview of the accelerator system for processing sparse and irregular tensor computations. (Section IV provides further discussion.)

mechanisms to store, extract, communicate, compute, and load-balance the NZs and the corresponding hardware and/or software support. The goal of exploiting sparsity is to exploit all forms of sparsity possible to considerably reduce computation, communication, and storage of zeros, while avoiding adding performance, power, and area overheads. Exploiting sparsity effectively depends on tailoring the data encoding and extraction, dataflow, memory banking structure, interconnect design, and write-back mechanisms. Further, it requires new representations and enables new opportunities for hardware/software/model co-designs. In this survey, we mainly discuss different accelerator designs that have leveraged sparsity of different tensors and different opportunities for performancegains and energy efficiency. Tensor decomposition and dimension reduction yield tensors of various sizes and asymmetric shapes [3], [43]. Dataflow mechanisms for executing layers of the models are typically optimized well for some commonly used layers (symmetric dimensions), and hence they often become ill-suited for processing tensors with reduced dimensions [43] and different functionality. So, we describe how configurable designs and and flexible dataflows can help achieving efficient execution. Sparse tensors quantized with value sharing require additional support to index a dictionary for obtaining shared values. The survey also discusses such techniques and accelerators that leverage value-similarity and support variable bit-widths of sparse tensors.

**Contributions:** This paper provides a comprehensive survey of different techniques for efficiently executing sparse and irregular tensor computations of the compact ML models on hardware accelerators. It describes corresponding enhancements in the hardware architecture and the required software support. In specific,

- For inference and training of different ML models, we summarize various sources of sparsity of the tensors.
- We highlight challenges in accelerating computations of sparse (especially, unstructured) and irregular-shaped tensors (e.g., dot product, convolution, and matrix multiplication) on spatial-architecture-based hardware accelerators that execute with dataflow mechanisms.
- We present an overview of the accelerator system along with the different hardware/software modules for sparse and irregular computations, their interfacing, and the execution flow. We provide an in-depth discussion for the need

- of each module, different design choices, and qualitative analysis of the different choices.
- We survey different accelerator systems and execution techniques for sparse tensors of ML models and provide taxonomies to categorize them based on the various hardware/software aspects of the designs.
- We analyze how various sparsity-levels and tensor shapes of different models impact the storage efficiency of different sparsity-encodings and the reuse of tensors.
- For designing these accelerator modules and overall accelerator system, we discuss recent trends and outline further opportunities for hardware/software/model co-designs.

#### Paper organization:

- Section II provides a brief background on different ML models, hardware accelerators for their tensor computations, and the need for further efficiency by reducing computation, storage, and communication requirements.
- Section III discusses tensor compression and opportunities due to sparse, size-reduced, and quantized tensors, and why their efficient processing requires a special support.
- Section IV provides an overview of the accelerator system
  with enhanced architectural modules and software support
  for sparse and irregular tensor computations (Fig. 1). Their
  in-depth discussions follow through sections V–XII. Opportunities for optimizing each module further are discussed at
  the end of corresponding sections or subsections.
- Section V illustrates common sparse data encodings, analyzes their implications in terms of storage and coding overheads, and describes group-wise encoding of tensors.
- Section VI discusses different techniques to extract matching NZs from tensors for computations. It analyzes advantages and limitations of the centralized and in-PE extractions.
- Section VII discusses managing non-coherent, multibanked, global scratchpad and hiding of the memory access latency behind computations. It also discusses data reuse of the sparse tensors and cross-layer reuse opportunities.
- Section VIII discusses interconnect designs for distributing data from memory and reducing partial outputs, their bandwidth requirements, spatial data reuse, and their configurability to support multiple dataflows for execution.
- Section IX describes sparsity-aware dataflows and pipelined PE architecture including tailoring function units for sparsity, bit-adaptive computing, and leveraging value similarity.

- Section X discusses sources of the inter-PE and intra-PE imbalance due to sparsity and their impact, software-directed balancing, and hardware structures for dynamic balancing.
- Section XI describes different write-back mechanisms for collecting data from PEs and assembling the data locally in PEs or on a central module. It also discusses data layout transformations and on-the-fly encoding of sparse outputs.
- Section XII discusses compiler support for targeting hardware accelerators including intermediate representations for deep learning models, compiler optimizations and their automation, and ISAs and code generation for accelerators.
- Section XIII describes recent trends and future directions in terms of developing tools and techniques for systematic exploration of hardware/software/model co-designs.
- Section XIV discusses relevant surveys that describe additional details (domain-specific models, tensor compression techniques, etc.) and can be useful to non-expert readers.

## II. BACKGROUND: NEED FOR EFFICIENT EXECUTION OF ML MODELS ON HARDWARE ACCELERATORS

#### A. Domain-Specific Machine Learning Models

Learning through ML models can be supervised (where labeled data is available), unsupervised (training samples are unlabeled), or semi-supervised. We refer non-expert readers to surveys [44], [45], and [46] for a detailed discussion on different learning approaches and inference and training process of various models. Discussions through this survey mainly focus on accelerating different *deep neural networks* (*DNNs*) that are commonly used in supervised learning.

Convolutional neural networks (CNNs) are commonly used for object classification and detection in image processing, video analysis, and autonomous vehicle systems; these models are usually trained through the supervised learning approach. CNNs majorly consist of many *convolution layers* (CONV) and a *few fully-connected* (FC) layers. Early CONV layers capture low-level features (e.g., edges and corners) from the images, which are used to construct high-level features (e.g., shapes) by subsequent layers. Finally, classifier aka FC layers determine the type of the objects [44].

**Sequence-to-sequence models** include recurrent neural networks (RNNs), gated recurrent units (GRU), long-short term memory (LSTM) [15], and attention mechanism [7], [8]. These models are used for *natural language processing (NLP)* and media processing tasks. They essentially use unidirectional or bidirectional recurrent cells at their core with processing of *multi-layer perceptrons (MLP)* aka FC structures.

Models for semantic segmentation and language translation use encoder-decoder structures with convolutions [5], [14] or recurrent cells/attention layers [8], respectively.

Generative adversarial networks (GANs) [10] are used by media generation applications. GANs use generator and discriminative networks that consist of convolution layers.

**Graph neural networks (GNNs)** and other graph learning models [47] are used for applications such as text classification and translation, node classification and link predictions in large social graphs, etc. They learn graph properties and infer about unforeseen information. To achieve this objective, each node

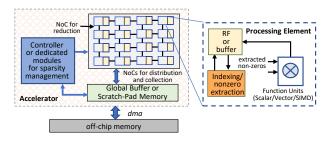


Fig. 2. Abstract accelerator design for processing sparse tensors of machine learning applications. Execution of applications require explicit management of computational, communication, and memory resources.

contains an embedding feature vector with the information mixture about own and neighborhood features. The nodes then recurrently aggregate features of local neighbors, perform neural network computations on aggregated data (e.g., MLP for down-scaling embeddings), and update their own embeddings.

**Recommendation system models** consist of embedding layers (look-ups and matrix operations) [12], CNNs for object detection and video understanding, and RNNs for processing language models [11].

Primitives like MLP or GEMM (general matrix multiply) and CONV are at the core of many models and dominate the execution. So, ML frameworks like PyTorch [48], TensorFlow [49], and Intel MKL [50] provide efficient implementations of these primitives for execution on commodity hardware (CPUs, GPUs, FPGAs) or even specialized accelerators. So, our discussions mainly focus on efficiently accelerating tensor computations of MLPs, CONVs, and RNNs.

#### B. Hardware Accelerators for Machine Learning

In the "new golden age of computer architecture", recent research efforts and commercial solutions have extensively demonstrated that domain-customized hardware accelerators significantly speed-up the execution of ML models in an energy-efficient way [20]-[22], [51]-[54]. Typically, these specialized solutions feature spatial architectures, which are those that expose low-level aspects of the hardware's interconnect and storage to the hardware-software interface. Spatial architectures can be coarse-grained or fine-grained. Coarse-grained architectures feature arrays of interconnected PEs, and finegrained designs are realized by programming FPGAs. Coarsegrained spatial architectures are a common implementation choice for designing hardware accelerators for ML [20]–[23], [55]. As Fig. 2 illustrates, the accelerator comprise of an array of PEs that contain private register files (RFs) and shared buffers or a scratchpad memory. PEs are much simple in design (function units with little local control), and the shared scratchpad is non-coherent with software-directed execution. Therefore, these accelerators are a few orders of magnitude more power-efficient than out-of-order CPU or GPU cores [20]–[22]. They lead to highly energy-efficient execution of ML models that are compute-intensive and memory-intensive. Since performance-critical tensor computations of ML models are relatively simple operations like element-wise or tensor additions and multiplications, they can be efficiently processed

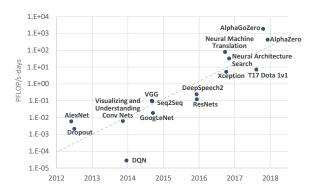


Fig. 3. Computation requirements for the training of AI algorithms almost double every few months (Figure adopted from [24]).

with structured computations on the PE-array. Moreover, private and shared memories of PEs enable high temporal reuse of the data [56], [57], and with efficient data management, PEs can be continuously engaged in tensor computations while the data is communicated via memories [20]. Additionally, interconnects like mesh or multicast enable data communication among PEs and spatial reuse of the data, lowering the accesses to off-chip memory. Thus, with minimized execution time, spatial-architecture-based hardware accelerators yield very high throughput and low latency for ML models.

#### C. Need for Further Efficient Execution

With recent advances in the development of ML models, their computational and memory requirements have increased drastically [18], [24]. Fig. 3 provides an overview of this dramatic surge. One major reason is the rise of deeper models. For example, for processing ImageNet images, AlexNet [1] contained five CONV and three FC layers (eight parameter layers) with the model size of 61M parameters (weights and bias) and computation of 724 MFLOPs. DNNs like ResNet-101 [2] achieved higher classification accuracy, but contained 100+ parameter layers and required processing about 7.6 GFLOPs per image. Memory requirements for NLP models have increased massively, e.g., from 50M–100M parameters (Transformer [7], 2017) to 175 billion (GPT-3 [9], 2020).

While deeper and larger models achieve high task efficiency for various applications [44], they consume high execution time, energy, and memory. Previous studies have shown that significant data redundancy exists in these often over-parameterized models [25], [26]. So, researchers have developed techniques that compress the tensors and obtain compact models, thereby significantly reducing computational, communication, and storage requirements.

## III. ACCELERATION OPPORTUNITIES DUE TO COMPACT MODELS AND THE NEED FOR SPECIAL SUPPORT

Efficiency of executing ML models can be improved further by drastically reducing computation, communication, and memory requirements. This can be achieved by compressing tensors of ML models. Tensors are compressed by inducing and leveraging: (a) sparsity (zero values) [27]–[30], (b) size reduction (tensor decomposition, dimension reduction, and

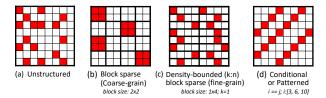


Fig. 4. Common sparsity structures (e.g., for a 75% sparse 8×8 matrix).

shape reduction) [3], [30], [32]–[35], and (c) quantization (precision lowering and value sharing) [27], [36]. Previous techniques have achieved highly compact models without incurring accuracy loss. For example, after applying pruning, quantization, and Huffman encoding, Deep Compression [27] reduced the model size of AlexNet and VGG-16 by  $35 \times 10^{13}$  and  $49 \times 10^{13}$  (e.g., from 552 MB to 11.3 MB), respectively. Similarly, accelerator-aware designs [38], [40] compress the model further. For AlexNet and GoogLeNet models, [40] pruned 91% and 66% of weights and reduced computational requirements by  $6.63 \times 10^{13}$  and 100 and

This section describes various sources of tensor sparsity which is either inherent or induced by model architecture or regularization. It describes how sparsity reduces computations, storage, and communication requirements. It also discusses techniques for reducing the size and quantization of the tensors, and how they offer advantages in terms of storage/performance/energy-efficiency. Then, it describes how compression techniques may induce irregularity in the processing and why special support is needed for efficiently processing the compressed tensors on hardware accelerators.

#### A. Opportunities Due to Sparse Tensors

1) Sparsity Structures: Inherent sparsity is usually unstructured (e.g., in activations, gradients, or tensors of scientific computing applications), where NZ elements are randomly scattered (shaded elements in Fig. 4a). Applying ReLU, dropout, quantization, or fine-grain pruning also induces unstructured sparsity in input activations (IA) or weights (W). For improving execution efficiency, pruning techniques or model operators induce structured sparsity. For example, weights can be pruned in coarse-grain blocks where block shape can vary from 1-D (vector) to n-D for an n-dimension tensor [28], [37], [58], [59]. Fig. 4b shows 4×4 blocks for a block-sparse tensor, where each block contains all zeros or all NZs. With larger blocks, techniques often prune entire dimensions (e.g., channels or filters in CNN models) [28]. Selection of the block size and shape depends on task accuracy requirements. Alternatively, tensors are sparsified with density bounded blocks (Fig. 4c), where each n-D block contains a fixed (k) number of NZs [60]–[62]. It equally scatters NZs throughout the tensor. NZs are located arbitrarily in the whole block or a fixed number of NZs can be induced across each dimension of the block. Values of k can be selected based on the sensitivity of the pruning to accuracy. For example, analysis of [60] showed that for VGG-16 and ResNet-50, about 12 out of 16 elements can be pruned without any accuracy loss, and about 10 out of 16 elements for compact models like MobileNetV1 and SqueezeNetV1. To preserve accuracy while achieving high sparsity, a mixture of blocks (with different block sizes or block sparsity) can be also introduced [63]. Lastly, tensors can be pruned in patterns or conditionally with sophisticated rules (e.g., diagonally as Fig. 4d shows).

- **2) Sources of Sparsity:** Tensors of different ML models can be sparse due to multiple reasons:
- CNNs typically use the ReLU activation function [1] which clamps negative values to zero. So, sparsity of input activations (IA sparsity) can be on average more than 40% in CNNs [64], and higher in later layers (about up to 70% [64], [65]). [64] reported that max-pooling can amplify it, e.g., up to 80% for VGG-16 layers. [66] showed that IA sparsity can eliminate about 40% and 55% of the multiply-and-accumulate (MAC) operations during CNN training and inference, respectively. For recent compact models like MobileNetV2 [32], IA sparsity can eliminate about 20% MACs.
- Neural networks use drop-out layers to avoid overfitting. After applying the drop-out, only partial activations are retained [26]. Dropping the activations induces sparsity [26].
- Pruning techniques remove unimportant weights and alleviate the overfitting of the model while maintaining the classification accuracy. Typically, weights with the least significant values can be safely pruned [25], [31] (in training or post-training). Pruning can bring regularity in the learning of the model and can even increase accuracy slightly [37], [60]. Pruning algorithms introduce significant sparsity, e.g., more than 60% weights of CONV and more than 90% of weights of FC layers can be removed [25] (W sparsity). For recent compact models like MobileNetV2 and EfficientNetB0, W-sparsity can be from 50%-93% (80%-85% in point-wise convolutions) [67], which reduces MACs by  $2.5 \times -4.2 \times$ . Similarly, more than 80% weights of RNN, GRU, or LSTMs can be pruned [39], [68], [69], especially for medium or large models, without significantly increasing error rate. For NLP models Transformers [7] and BERT [8], recent techniques induce 80% [70] and 93% [71] W-sparsity, which reduces total MACs by about  $4.8 \times$  and  $12.3 \times$ , respectively. Besides, regularization of the models (e.g., L1 or group-lasso based) can induce unstructured or structured W-sparsity [28].

Pruning of activations is also shown as effective [72]–[76]. DasNet [73] reported eliminating about 27% and 12% MACs by activation sparsification for AlexNet and MobileNet. It achieved 79% IA-sparsity for AlexNet FC layers along with pruning 81% weights, without dropping top-1 accuracy. Similarly, MASR [77] applied refactoring of the batch normalization, achieving about 60% IA-sparsity for RNNs.

- CNNs use Atrous (dilated) convolutions where filters are upsampled by inserting zeros between weights [5].
- GANs use transposed convolution in a degenerator network, where input data is first upscaled by inserting zeros between values, and then convolution is applied. [78] showed that for transposed convolutions in different GANs, about 60% of MACs are zero. Additional sparsity is introduced when GANs are forced to forget generating specific objects [79].

- Input data for object detection tasks can be inherently sparse, as only specific regions of frames are valid [80]. For example, object detection models of autonomous driving systems process 3D LiDAR data by constructing point clouds and projecting them from the bird's eye view (top view) [81], [82]. The resultant images are then fed to object detection algorithms for locating the regions of interest. Recent techniques have reported that sparsity of the input data for object detection can be 80% or more [80], [81].
- For efficient communication in distributed training, gradients (Grad) are sparsified and compressed. E.g., Grad-sparsity can be 99%+ for computer vision or language processing tasks [83] and 95%–99% for recommendation models [84].
- Input data for the tasks of recommendation systems (e.g., user-item matrix) can be inherently very sparse e.g., from 95% [85] to 99% [11]. Recommendation models compute dot products on dense-sparse or sparse-sparse data [84], [86].
- GNNs process large graphs, e.g., with thousands of vertices. Depending on the real-world interactions of objects (vertices), data contain high (e.g., 75%–99%) or hyper (99%+) unstructured sparsity [87], [88]. For example, in processing large graphs with GCNs, many features of vertices are local and lead to zeros in adjacency matrices for remote nodes [88]. GNN computations involve aggregation on sparse data, and multiplications of dense matrices with dense or sparse matrices [88], [89], which are often processed on separate modules of the accelerator (e.g., in HyGCN [87] and EnGN [90]).
- Text corpus in text analytics applications leads to high sparsity since each document contains only a fraction of the words from the vocabulary. Such analytics applications include PCA for dimensionality reduction of the sparse data, support vector machines and regression for classification, collaborative filtering for the recommendation, and k-means for clustering the data [30]. These operations involve multiplications of sparse matrices with dense or sparse vectors, where the matrix sparsity can vary from 67%–99% [30].

While we describe leveraging sparsity for ML models, applications of many domains including linear algebra, graph processing, and scientific computing [91], [92] can be accelerated by exploiting sparsity.

3) Advantages: Sparsity allows (i) eliminating ineffectual computations i.e., reduces execution time and energy by processing only NZs, (ii) reducing storage by encoding only NZ values, so more data fits in on-chip memory and off-chip memory accesses (extremely energy-consuming [42], [93]) are reduced, and (iii) improving speedup due to reduced communication requirements for data-intensive ML models.

#### B. Opportunities Due to Size-Reduced Tensors

Symmetric or high-dimensional tensors have large sizes and their processing requires more computation and memory. So, ML models are designed to reduce such requirements by using group or parallel operators [1], [94], 1×1 or pointwise convolutions (PW-CONV) [33], [95], or dimensionality reduction with PCA [30], [34]. Moreover, tensors can be decomposed with spatial factorization [34], [96], depth-wise

separation for convolutions [3], [32], or low-rank approximations [34]. Further, tensors can be ragged [35] to obviate the need of structured or rectangular shapes. While these transformations significantly reduce storage and computations, they make tensors irregular-shaped (asymmetric).

#### C. Opportunities Due to Quantized Tensors

Tensor quantization includes precision lowering [36] and leveraging value sharing or value similarity [27], [97], [98]. Precision lowering allows representing tensors (weights, activations, gradients, weight updates) at much lower bit-width (e.g., 8b or lower for inference and 8b/16b for learning). Moreover, elements with similar values can be clustered and approximated by sharing common values (centroids of clusters). In general, significant data redundancy exists in the tensor elements (particularly in the parameters of large models) and, a successfully trained model is generalized and immune to noisy data. So, when the precision is lowered, the error induced by quantization may often be tolerated by a welltrained model [99], and it can also obviate over-fitting caused otherwise by excessive precision, thereby bringing the generality in learning [100]. For compensating any accuracy drop due to quantization, learning algorithms fine-tune the model or use quantization-aware training [36]. Thus, quantization techniques typically do not degrade inference accuracy [66] or can even trade-off the accuracy with aggressive quantization [64], [101], [102].

Quantization significantly reduces storage requirements and accesses to off-chip memory. It offers additional advantages in terms of reduced area and power consumption. Because, for quantized tensors, function units can be simpler and energy-efficient (e.g., for a 45 nm process, int8 multiplier consumes  $20 \times$  less energy than FP32 multiplier [93]), and bandwidth requirements are reduced i.e., bus sizes can be smaller.

Thus, with sparse, size-reduced, and quantized tensors, compact models can achieve higher accuracy as models with uncompressed tensors, while becoming amenable for deployment at edge, mobile, or online-learning platforms [17], [27] due to scope for low latency, energy, and storage. So, leveraging such opportunities is crucial for further accelerations.

## D. Need for Special Support to Accelerate Sparse and Irregular Tensor Computations

While hardware accelerators efficiently process different models [21], [22], [103], they inherently cannot benefit from the sparsity. Because, all the data, including the zero values of activations, weights, and gradients still have to be fetched from the memory and communicated to PEs; PEs are also unable to skip ineffectual computations, wasting the execution time. Sparsity, especially unstructured, induces irregularity in processing, since NZs or blocks of NZs are scattered across the tensor. Therefore, leveraging sparsity necessitates additional mechanisms to store, extract, communicate, compute, and load-balance the NZs, and corresponding hardware and software support [41], [104]. The sparsity levels and patterns due to various sources lead to unique challenges and solutions in hardware/software co-design. Therefore, our discussions

throughout this survey mainly focus on exploiting tensor sparsity for accelerating compact models.

Tensor dimension reduction and tensor decomposition make tensors irregular-shaped (asymmetric), and they may also modify the functionality of the computational primitives e.g., depthwise convolution (DW-CONV). Since execution on hardware accelerators is typically well-optimized for processing symmetric tensors with specific dataflow mechanism, these shape transformations and supporting different functionality (e.g., DW-CONV, randomized or approximated matrix multiply [105]) may introduce irregularity in processing requirements. To sustain high utilization of computational resources, it requires additional support including configurable hardware architectures and flexible mappings of the functionality onto architectural resources [43], [104], [106].

Hardware accelerators have supported precision lowering by storing, communicating, computing tensors of low (typically fixed for a design) bit-widths, and even more recently, tensors with mixed precision [66]. However, when sparse tensors are quantized with value sharing, it requires indexing the codebook through indices for approximated elements [27]. Such irregular accesses are handled by implementing separate indirection tables in the hardware datapath in a pipelined manner [37], [42]. Moreover, value-similarity leads to reuse of computations by using memoized outputs, which requires additional processing. Further, supporting different bit-widths of various sparse tensors of different models require configurable architectures including bit-adaptive computing [107]–[109].

Thus, compressed tensors lead to sparse and irregular computations and their efficient accelerations require special support, which is described in the next section. Appendix describes that exploiting sparsity (especially, unstructured) is relatively hard for execution on CPUs and GPUs; with special support, hardware accelerators can achieve notable gains.

## IV. ACCELERATOR DESIGN FOR EFFICIENT SPARSE AND IRREGULAR TENSOR COMPUTATIONS

To efficiently process sparse and irregular tensor computations, designers of the accelerator systems can integrate special hardware or software modules. It enables orchestration of the structured computations while processing the tensors in compressed formats. Consequently, it can lead to efficient utilization of the accelerator resources and allows to conveniently exploit acceleration opportunities. Fig. 1 provides an overview of the accelerator system equipped with such modules. This section briefly describes these system modules.

Since sparse, size-reduced, and quantized tensors of ML models offer various opportunities for storage, performance, and energy-efficiency, several accelerators have provided marginal or comprehensive support and leveraged some or all the opportunities. Table I lists such common objectives and corresponding accelerator solutions that meet these objectives.

Different accelerators for inference and learning exploit only W-sparsity, IA-sparsity, or both, which impacts acceleration gains [129]. Several accelerators including Cambricon-X [41] exploit only static sparsity (Table II), e.g., when locations of zeros in weights are known beforehand for inference. Static

Objective	Techniques
Compress data in off-chip memory (storage)	[20], [30], [37], [41]–[43], [60], [65], [66], [68], [92], [104], [106], [108], [110]–[123]
Compress data	[30], [37], [41]–[43], [60], [65], [66],
in on-chip	[68], [72], [92], [104], [106], [110]–[118],
memory (storage)	[120], [122]–[124]
Skip processing	[20], [30], [37], [41]–[43], [60], [65], [66],
zeros	[68], [72], [92], [104], [106], [108], [112]–
(energy-efficiency)	[118], [120]–[132], [133]
Reduce ineffectual	[30], [37], [41]–[43], [60], [65], [66],
computation cycles	[68], [72], [92], [104], [106], [111]–[118],
(performance & energy)	[120], [122]–[124], [128], [129], [133]
Load balancing	[37], [42], [43], [60], [65], [66], [68],
(performance)	[115], [117], [122], [125], [126], [129]

sparsity allows offline encoding and data transformations for arranging structured computations (e.g., for systolic arrays [62], [125], [134]). Recent accelerators including ZENA [129], SNAP [106], and EyerissV2 [43] efficiently execute tensors with dynamic sparsity as well. It requires determining locations of intersecting NZs in both tensors at run-time to feed the function units, on-the-fly decoding (encoding) NZs, and often balancing the computations on PEs. Table II lists different accelerators that support static and dynamic sparsity of tensors. Now, we describe different hardware and software aspects of accelerator system that help in leveraging sparsity effectively.

**Sparsity encodings:** For efficient processing, sparse tensors are encoded using different formats, where only NZ values are stored in a "data" tensor and one or more "metadata" tensors encode locations of NZs. Section V discusses different formats and associated costs for encoding and decoding. For different sparsity levels, it analyzes their effectiveness in terms of storage efficiency. E.g., tensors can be compressed by 1.8× and 2.8× for 50% and 70% sparsity (bitmap or RLC-2), and by about  $7.6 \times$  and  $55 \times -60 \times$  for 90% (RLC-4) and 99% sparsity (CSC or RLC-7). Structured sparsity (coarse-grain block-sparse) can alleviate the overheads of metadata and finegrained data extraction by encoding indices for only large dense blocks. For accelerating ML models, sparse tensors are also quantized i.e., their precisions are lowered (typically int8 or int16 for inference [43], [114], [129] and FP16 for learning [66], [104]) and often approximated by clustering data of similar values [37], [42], [110]. Therefore, encoded sparse data contains quantized values of NZs.

NZ detection and data extraction: In processing sparse tensors of different primitives, corresponding elements of the weight and activation tensors are multiplied and accumulated. Depending on the sparsity, accelerators need to use data extraction logic that decodes compressed tensors, search within a window of NZs or index the buffer, and obtain matching pair of NZs to feed the function units for computation. Section VI provides a taxonomy of different data extraction mechanisms and analyzes their implications for various sparsity levels. Up to moderate IA-sparsity and high W-sparsity, these indexing or intersection based mechanisms efficiently extract sufficient NZs at every cycle for keeping function units engaged. For

efficient compute-bounded executions at such sparsity, accelerators reported achieving near-ideal speedups (e.g., about 80%–97% of the speedup corresponding to reduced operations i.e., *sparsity-speedup ratio*) [41], [42], [129]. However, extraction becomes challenging at high (e.g., 90%+) or hyper sparsity as NZs are scattered at distant locations [88] and execution is usually memory-bounded with low arithmetic intensity. Section VI also discusses sharing the data extraction mechanism among PEs or employing in PEs. Then, it discusses opportunities for further optimizations.

Memory management: Compressed tensors are often stored in the shared on-chip memory which is non-coherent, multi-banked, and often non-unified. For a pre-determined sequence of execution, a controller or PEs initiates the accesses between off-chip and on-chip memory; their latency needs to be hidden behind computations on PEs. Section VII discusses corresponding memory architectures and techniques for hiding of miss penalty for sparse tensors via double-buffering or asynchronous computation and memory accesses. It describes the data reuse opportunities for various sparsity and dimensions of tensors of common DNNs and how sparsity lowers the reuse. It also discusses techniques that leverage cross-layer reuse of intermediate output layers and reduce latency.

Communication networks: Once tensor blocks are fetched from memory, they are distributed to appropriate PEs via interconnect networks (often one per operand). Efficient designs ensure that sufficient data can be fed to PEs while they perform computations. Spatial reuse is leveraged by multicast or mesh networks that communicate common data blocks to multiple PEs. It lowers accesses to memory hierarchy and communication latency. However, depending on the sparsity, data extraction mechanism, and mapping of functionality on accelerator, spatial reuse opportunities vary considerably [43]. Section VIII discusses different designs for distributing sparse and quantized tensors and reducing partial outputs. It also describes challenges in executing inter-PE communications that may become unstructured due to sparsity and the temporal and spatial mechanisms for reduction/collection of the outputs. It describes how configurable designs supports different communication patterns for different sparsity, reuse, and functionality.

PE architecture: Several accelerators consist of scalar PEs with fused MAC units (e.g., EIE [42], LNPU [66], and Envision [108]). Others contain SIMD PEs (multiple function units) (e.g., EyerissV2 [43]) or vector PEs consisting of multiplier-arrays and adder-trees (e.g., Cambricon-X [41] and SNAP [106]). PE architectures either directly process pairs of matching NZs extracted from tensors or use hardware logic for data extraction or coordinate computation (Fig. 2). Effectively utilizing function units can be challenging for variations in sparsity, precisions, and functionality, and it may require configurable designs. Section IX provides corresponding discussions and describes sparsity-aware dataflow mechanisms (mapping of tensor computations on accelerator resources) used by different accelerators. It also describes how accelerators have leveraged value-sharing and value-similarity of tensors and the corresponding modifications in the PE architecture.

Load balancing: Depending on the distribution of zeros,

TABLE II
ACCELERATOR SYSTEMS LEVERAGING SPARSITY OF DIFFERENT TENSORS FOR DIFFERENT ML MODELS.

Dynamicity	Static	[41], [60], [62], [68], [111], [118], [121]–[123], [125], [126]	
of Sparsity	Dynamic	[20], [30], [37], [42], [43], [65], [66], [72], [92], [104], [106], [108], [110], [112]–[117], [120], [124] [127]–[132]	
	Weight	Unstructured [41], [111], [121]–[123], [126], [134]	
Tensors Treated	Weight	Structured [37], [58], [60], [61], [68], [117], [125], [62]	
as Sparse	Activation	[20], [66], [72], [110], [120], [124], [127], [132]	
	Both	[30], [37], [42], [43], [65], [92], [104], [106], [108], [112]–[118], [128], [129], [131], [133]	
	Matrix-Vector Multiply	[30], [37], [41]–[43], [60], [66], [92], [106], [113], [115], [118], [128], [132]	
Primitive	Matrix-Matrix Multiply	[41], [92], [104], [115], [125], [126], [131], [133]	
Operation	Convolution	[20], [37], [41], [43], [60], [65], [66], [72], [106], [108], [110]–[117], [120]–[123], [128]	
Operation	Recurrent Layer	[68], [77], [124], [127]	
Accelerators for Learning [66], [104]		[66], [104]	

the execution may end up with processing a different amount of NZs on different PEs or their function units, which creates inter-PE or intra-PE load imbalance. Section X analyzes such sources of the imbalance and introduces a taxonomy of different load balancing techniques. Different accelerators achieve load balance through either software techniques (e.g., structured pruning or data reorganization) or by providing a hardware module for dynamic work balance (through asynchronous execution or work sharing), which provides further accelerations. For example, ZENA [129] leveraged the sparsity of both activation and weight tensors for AlexNet and VGG-16 models and reported about 32% additional performance-gains through load balancing. Dynamic load balancing can provide notable speedups for high, unstructured sparsity [88].

Write-back and post-processing: Tensor elements produced by PEs need to be collected, post-processed for further operations, and written back to the memory. PEs in different accelerators either write back sequentially or asynchronously through a shared bus, or via point-to-point links. In addition, accelerators usually contain a post-processing unit which reorganizes the data (as per the dataflow mechanism of the current and next layer of the model) and encodes sparse output on-the-fly. Section XI discusses such mechanisms.

Compilation support: It is important to support the execution of various ML models on hardware accelerators and easier programming of models from ML libraries. Section XII discusses compiler support for sparse models and hardware accelerators. It discusses polyhedral and non-polyhedral intermediate representations and their implications on the compiler's ability to represent the code and apply code transformations. It describes challenges in supporting sparse tensors and DNN compilers that facilitate sparse tensor computations. Then, it discusses compiler optimizations including common loop optimizations and those specific to hardware intrinsics. It also describes semi-automatic optimizations for transforming the loops and data layout and automatic optimizations using the cost models. Finally, it discusses ISAs used by accelerators and their code generation by using library of high-level primitives.

#### V. ENCODINGS FOR COMPRESSING SPARSE TENSORS

Encoding format stores a sparse tensor in a compressed manner. It contains actual data (NZ values) and metadata (information about positions of NZs). Metadata is later used by the accelerator's data indexing logic to locate and extract

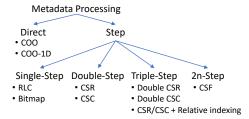


Fig. 5. A taxonomy for the required processing on the metadata during data extraction when a sparse tensor is encoded using different formats.

NZs. This section discusses commonly used encodings through a common example (Fig. V) and their implications on the storage and processing requirements. For different formats, Fig. 5 introduces a taxonomy for processing on metadata during data extraction, and Table III lists the corresponding storage overhead. Depending on the mapping of the layer of a model onto the accelerator, tensors are divided into blocks (per PE-wise work). We refer to such processing as a group-wise encoding, which is discussed later. Finally, this section briefly describes on-the-fly encoding and further opportunities.

#### A. Encoding Formats and Implications

1) Coordinate (COO): It stores absolute positions of NZs. As Fig. V(b) shows, all NZs of an uncompressed tensor T are stored in a data vector val, and vectors  $coord\_y$  and  $coord\_x$  indicate the coordinates of each NZ value. So, COO is a natural way to express sparse tensors and is commonly used (e.g., in PyTorch). Formats adopted by FROSTT [136] and matrix market [137] closely resemble COO.

The COO format stores all coordinates in the uncompressed format. E.g., as Fig. V(b) shows, the metadata for values '2' and '3' (same row) or '2' and '5' (same column) are not compressed, i.e., duplicate values of row and column indices exist in coordinate vectors. So, the overhead of storing n coordinates per NZ value is about  $\sum_{1}^{n} \lceil \log_2 d_i \rceil$  bits (vector d contains the tensor's dimensions). It makes COO inefficient for storing tensors with low or moderate sparsity.

Fig. 7 shows storage benefits for encoding 2 MB matrices of various sparsity in different formats. We calculated storage requirements with the analysis presented in Table III and normalized them to the matrix's size in dense format. We used Scipy library [138] for generating matrices of various sparsity and for encoding them in COO, CSR, and CSC formats. Fig. 7

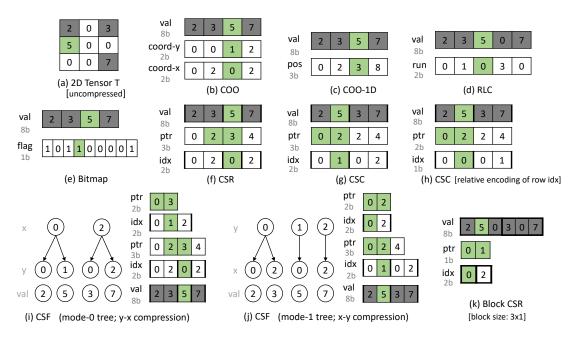


Fig. 6. Encodings to store sparse tensors in different formats. Elements with green shade encode the same NZ element. (Figure inspired by [135].)

shows that for a 2 MB matrix, COO achieves storage efficiency for 70%+ sparsity. However, COO may yield simple indexing logic, as both the data and metadata can be directly extracted.

- 2) COO-1D: For tile-wise processing of an encoded tensor, accelerators often process only a block of NZs at a time, where block elements vary across only single dimension. For example, Cnvlutin [72] process the input activations and weights across the channel direction. Therefore, the data block is encoded with COO-1D, which is just like COO, but there is only one *pos* vector for storing coordinates of NZs in the flattened block. For instance, if we flatten T to be considered as a block, then value '5' is indexed by position '3'.
- 3) Run-Length Coding (RLC): It compresses a sequence of values by replacing consecutive duplicate values with a single value and the number of repetitions (aka run). For RLC-encoded sparse tensor, 'run' indicates a total number of zeros before (after) an NZ. Fig. V(d) shows RLC encoding of T. Run values for '2' and '3' are '0' and '1', respectively. A few accelerators including Eyeriss [20] encode both the NZs and runs altogether in the same vector val. For example, T can be encoded as val: (0, 2, 1, 3, 0, 5, 4, 7).

RLC requires a step-processing on metadata, as run-length needs to be calculated by accumulating runs and preceding *number of NZs (NNZs)*, for determining position of an NZ. The storage overhead for RLC-B is NNZ  $\times$  B bits, where B is bitwidth of the run. If a vector d contains tensor dimensions, then B can be set as up to  $\lceil \log_2 \left(\prod_1^n d_i\right) \rceil$  bits for accommodating the number of leading zeros in a highly sparse tensor. When B is set lower, it cannot always capture the number of zeros as *run*. Fig. V(d) shows RLC-2b encoding, where leading zeros before '7' are four. This cannot be expressed by 2 bits. As a work-around, padding zeros [42] are inserted and treated as NZs. In this example, a padding zero is inserted between '5' and '7'; run values corresponding to the padding zero and '7' are '3' and '0', which contributes to the total run of four.

To accelerate CNNs with 30%–90% sparsity of tensors, designers have set B as 2 or 4 bits. In general, setting B as  $\lfloor \log_2(\frac{sparsity}{density}) \rfloor + 1$  bits can effectively compress tensors and provide a feasible bit-width to indicate leading zeros. sparsity and density are fractional numbers indicating the actual or anticipated number of zeros and non-zeros in the tensor, respectively. Thus, setting B as 1, 1, 1, 2, 4, and 7 efficiently encodes tensors with sparsity of 10%, 30%, 50%, 70%, 90%, and 99%, which is depicted in Fig. 7.

As RLC requires step-processing on metadata, the indexing logic needs an accumulator to determine the position of an NZ. When a tensor is not flattened or processed block-wise, but rather indexed by n-dimensions, the indexing logic may require performing division and modulo operations on the metadata. Alternatively, a multi-dimension representation can be processed where *run* for the coordinates of each dimension can be separately calculated and stored. The overall computational cost (arithmetic and logical operations realized in hardware) for such step processing can be low. Therefore, several accelerator designs including Eyeriss [20] and SCNN [114] used RLC encoding or its variant. As run indicates repetition of a value, CompAct [110] used an enhanced RLC format for encoding both the sparse and similar-value activations.

**4) Bitmap:** It stores all NZs in a tensor val along with a tensor flag which contains 1-bit flags for all elements of an uncompressed tensor T. As Fig. V(e) shows, a flag indicates whether an element is NZ (flag=1) or not (flag=0). Storage overhead for the bitmap (aka bit-mask) is  $\prod_{1}^{n} d_i$  bits (where vector d stores n dimensions of T) [120]. Therefore, bitmap is effective for compressing the tensors of low or moderate sparsity (e.g., tensors in several DNN layers). Since bitmap stores metadata for all elements, its storage efficiency over other formats reduces as sparsity increases.

Like RLC, decoding or indexing bitmap also requires stepprocessing. The data indexing logic to locate an NZ typically

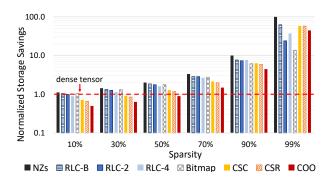


Fig. 7. Storage benefits for encoding a sparse tensor (512×2048 matrix with 16b elements) in different formats, normalized to the size of the fully dense tensor (Figure inspired by [104]).

consists of at least an adder and a comparator [41]. Due to overall low storage overhead and encoding/decoding cost, it is used by several accelerators including Cambricon-X [41], SparTen [115], and SIGMA [104], as shown in the Table IV.

5) Compressed Sparse Row (CSR): It compresses a matrix by processing each row as a sparse vector. In CSR-coded tensor, an array val contains all NZ values (ordered row-wise) and array idx stores their column indices [139]. Array ptr stores information about total NZs in each row i, which is obtained by calculating ptr[i+1] - ptr[i]. The last element of ptr equals to the total number of NZs in T. Row-wise compression enables random accesses to any row.

While COO redundantly stores row-coordinates of NZs in the same row, CSR compresses such metadata by storing NZs row-wise [135]. For example, in Fig. V(b) (COO), *coordy* stores row indices '0' and '0' for NZs '2' and '3'. This redundancy is removed in the CSR coding of Fig. V(f), as ptr stores only total NZs in each row. For compressing an M×N matrix using CSR, the total storage overhead is NNZ  $\times \lceil \log_2 N \rceil$  (for idx) + (M + 1)  $\times \lfloor \log_2 N NZ + 1 \rfloor$  (for ptr). Due to high storage overhead (proportional to NNZs and size of the row), CSR coding is efficient for high sparsity [41], [104], e.g., 90% or higher (Fig. 7).

Decoding a CSR-encoded tensor can require a two-step processing of metadata. The first step locates NZs of a row by iterating over ptr, and the next step locates an NZ element in the NZs of the row through the column index. Accelerators efficiently process CSR-coded matrices row-wise such that ptr is accessed once for fetching each row and then a decoder iterates through idx (to locate column positions).

CSR variants can improve the efficiency further. For example, ptr stores duplicate values when consecutive rows are zero. Doubly CSR (DCSR) [140] eliminates this redundancy and achieves additional compression for hyper-sparse matrices. Block CSR (BCSR) [141] stores a block of elements in val, if the block contains at least one NZ. As Fig. V(k) shows, in BCSR, idx indicates column index of a block and ptr informs about the number of dense blocks located in the same rows. BCSR avoids storing blocks of all zeros and populates dense regions, and hence suitable for encoding block-sparse structured weight tensors. Thus, BCSR-coded tensors can be efficiently executed not only on conventional processors

Format	Storage Overhead (bits)	
COO	$NNZ \times \sum_{1}^{n} \lceil \log_2 d_i \rceil$	
COO-1D	$NNZ \times \lceil \log_2 \prod_{1}^n d_i \rceil$	
RLC	$NNZ \times B$	
Bitmap	$\prod_{1}^{n} d_{i}$	
CSR	$NNZ \times \lceil \log_2 d_1 \rceil + (d_0 + 1) \times \lfloor \log_2 NNZ + 1 \rfloor$	
CSC	$NNZ \times \lceil \log_2 d_0 \rceil + (d_1 + 1) \times \lfloor \log_2 NNZ + 1 \rfloor$	

DIMENSIONS OF A TENSOR THAT CONTAINS NNZ non-zero elements.

but also on hardware accelerators (which requires additional support for appropriately indexing dense regions e.g., [125]).

6) Compressed Sparse Column (CSC): CSC is similar to CSR, except that NZs are stored column-wise [139]. As Fig. V(g) shows, an array val contains NZs (organized columnwise); idx stores their row indices; ptr informs about the total NZs in each column. The storage overhead and hardware cost for encoding/decoding tensors in CSC format are similar to those for CSR. Accelerators including EIE [42] and Sticker [116] processed high-sparsity tensors with CSC format.

To alleviate high storage overhead of CSR or CSC formats due to storing idx and ptr arrays, a few accelerators further encode the metadata idx or ptr. For example, EIE [42] and EyerissV2 [43] encode idx in RLC such that elements in idx indicate zeros between column indices of NZs (similar to run in RLC for NZ values). Fig. V(h) shows CSC encoding with such RLC-encoded row index array. Values '2' and '5' have column index of '0' and '1', respectively, which can be encoded as '0' and '0' because there are no leading zeros before NZs '2' and '5'. Similarly, if the first column of T is (0, 2, 0, 0, 5), then the row indices for '2' and '5' can be encoded as '1' and '2'. ptr can be encoded likewise. (store NZs per column instead of a cumulative number). However, encoding positions relatively requires additional step-processing on the metadata. Therefore, decoding a CSR or CSC encoded matrix with RLC-coded metadata can require triple-step processing on metadata (additional hardware cost).

7) Compressed Sparse Fiber (CSF): CSF [142] provides a generalization of CSR for higher-order (n-dimensional) tensors by forming a tree (with n levels). Nodes at level l contain indices for lth mode (dimension) of an uncompressed tensor T. Path from a root to a leaf node encodes different coordinates of an NZ, which are stored in the nodes throughout the path; each leaf node stores an NZ value. So, the height of the tree is the total dimensions of T; the width is NNZs in T.

Fig. V(i) illustrates a mode-0 tree and corresponding arrays of index pointers. Root nodes represent the major mode (0 or y), and their child nodes represent the consecutive dimension (1 or x). Like CSR, ptr informs about a group of indices corresponding to a dimension. For instance, ptr array at the beginning informs that one group of three coordinates corresponds to the mode 0 (coordinates stored in idx). Similarly, the next ptr array informs about three different groups of coordinates for the next mode (dimension 1) (corresponding to the three parent nodes from previous mode 0). The corresponding idx array stores the coordinates for mode 1, separated into three groups (marked by thick outer vertical borders).

TABLE IV
COMMONLY USED SPARSITY ENCODINGS BY ACCELERATORS

COO	[92], [116]
COO-1D	[60], [72], [106], [113], [123], [124], [128], [131]
RLC	[20], [65], [66], [110], [111], [114], [145], [146]
Bitmap	[37], [41], [62], [104], [108], [110], [112], [115]– [117], [119], [120], [129]
CSR	[30]
CSC	[30], [42], [43], [68], [118], [122], [147]
CSF	[92]

Layering the arrays of index pointers reduces duplication of indices [143]. Each time when a node directs to children, it eliminates duplicating indices for the corresponding mode. Storage benefits increase with the increase in dimensions and redundancy among coordinates of NZs. Organization of the data also impact the storage efficiency. For example, Fig. V(j) shows the other possible ordering, which eliminates storing redundant column (mode 1) coordinates, achieving fewer nodes. For an n-mode CSF tensor, the storage overhead corresponds to storing more than NNZ+n-1 coordinates and typically much less than  $n \times NNZ$  coordinates. [142], [143] provide further details about managing higher-order tensors with CSF format. Processing metadata at each dimension-level require two-step processing (just like processing ptr and idxin CSR), thereby up to 2n-step processing for an n-dimensional tensor. So, accelerator designers may opt for CSF format when processing high-dimensional tensors with high sparsity.

- 8) Huffman coding: It is typically applied for compressing sparse tensors once they are quantized using precision lowering or value sharing. After quantization, values of the reduced range appear with different frequency and can be compressed further with Huffman encoding [27]. For example, Deep Compression [27] pruned and quantized weights of AlexNet [1] and VGG-16 [144], achieving 8b/5b indices with a codebook of 256/32 weights for CONV/FC layers. With Huffman encoding, it compressed the models further by 22% and 36% (total compression of  $35\times$  and  $49\times$  vs. uncompressed).
- 9) Other formats: To improve efficiency of compressing or accessing sparse tensors (for high-performance and scientific computing) for execution on CPUs/GPUs, a variety of encoding formats have been proposed. They include compressed sparse blocks (CSB) [148], libsvm [149], ELLPACK [150], diagonal (DIA) [151], dynamic CSR [152], delta-coded CSR [153], and mode-generic and mode-specific formats [154]. Prior works including [135], SPARSKIT [139], and [143], [155]–[157] surveyed them along with additional formats and discussed their implications. Different libraries that provide support for encoding the tensors and for sparse tensor computations on CPUs or GPUs include MATLAB tensor toolbox [158], Intel MKL [50], SciPy [138], and cuSPARSE [159].
- 10) Encodings for tensors with structured sparsity: Density-bounded blocks (Fig. 4c) are encoded similarly as tensor blocks with unstructured sparsity, e.g., with bitmap [62], COO-1D [60], or RLC. So, for the same sparsity and block size, the overhead is similar as tile-wise processing of a tensor with unstructured sparsity. It is low usually, as block sizes are small (e.g.,  $8 \times 1$  [62],  $1 \times 4$  in NVIDIA A100 Tensor

Core GPU [61]), and position of each NZ is indicated by one or few bits. Coarse-grain block sparse tensors (Fig. 4b) can be encoded at block-granularity, which can significantly reduce the metadata size (almost eliminated for dimension pruning [160]). Cambricon-S [37] used bitmap to indicate the presence of each 1×16 dense block with a single bit. Similarly, ERIDANUS [125] used few bytes to process each 8×8 dense block on systolic arrays. Such encodings require indicating position of a dense block across rows and/or columns, and additional indices for higher dimensions that indicate dense blocks packed per dimension, e.g., in block CSR (Fig. V-k).

#### B. Group-wise Encoding

One way of processing sparse tensors is to encode the whole tensor. Then, the accelerator's data management logic extracts an appropriate tile (optionally decodes it) and communicates to the PEs. In contrast, for group-wise encoding, tensor tiles are encoded separately, based on pre-determined per-PE work. Depending on the mapping, each tile is typically communicated to a unique PE (or a PE-group) during execution. Thus, the encoding considers the mapping of the tensor computations onto PEs. So, its applicability depends on the dataflow mechanism (that determines which PEs process what data, discussed in section IX-B), fetching of tensors from memory, and communicating tensors between PEs and memory via interconnect. Group-wise encoding can make the decoding and data extraction easier, as each group corresponds to execution on a distinct PE. Accelerators including EIE [42], Cambricon-X [41], and CompAct [110] used group-wise encoding.

#### C. On-the-fly Encoding

Accelerator designers often target static sparsity of weights and encode them off-line, e.g. DNN inference accelerators including EIE [42], Cambricon-X [41], and [111]. However, on-the-fly encoding is required for efficiently processing dynamically sparsified tensors (sparse activations in the inference and tensors in training the models). Therefore, accelerators including CompAct [110], SCNN [114], NullHop [120], Cn-vlutin [72], and Sticker [161] employ an on-the-fly encoder. Typically, before encoding a tensor, the data is re-organized as per requirements of the group-wise encoding and dataflow mechanism for processing the subsequent layer. So, on-the-fly encoding is often combined with assembling the outputs from PEs (section XI-D provides further details).

#### D. Optimization Opportunities

(i) Tailoring encoding formats for sparsity levels and patterns: Various layers of deep learning models exhibit a wide range of sparsity for weight/activation tensors (inter-layer, intratensor sparsity variation). Moreover, even within a DNN layer, sparsity among tensors can be different (intra-layer, inter-tensor sparsity variation). Accelerators need to support such different sparsity-levels effectively without incurring significant overheads for storage, encoding, and indexing. When sparsity range or pattern of multiple tensors is diverse, designers can opt for the separate encoding of different tensors

 $\label{thm:table V} TABLE\ V$  Classification of NZ Data Extraction Techniques

Target Sparsity	PE Arch- itecture	Function Unit Operation	Accelerators
One	Scalar	MAC	[30], [68], [111], [120]
Tensor	SIMD/	Sc-Vec-Mul	[60], [66], [72]
Telisoi	Vector	Vec-Vec-Mul	[41], [60], [122]
	Scalar	MAC	[30], [42], [92], [113],
Both	Scalai	WIAC	[115], [118], [129]
Tensors	SIMD/	Sc-Vec-Mul	[43], [112]
	Vector	Vec-Vec-Mul	[37], [104], [106]

Location of Extraction Units	Accelerators	
Centralized / Shared	[30], [37], [41], [42], [65], [66], [104], [106], [112], [118], [120]	
In-PE	[42], [43], [60], [68], [72], [92], [111], [113]–[115], [117], [122], [129], [133]	

(e.g., [116]). These different sparsity-codings can be utilized for off-chip storage, zero-guarding the PEs, or for reducing the latency of on-chip extraction and obviating the ineffectual cycles to locate intersecting NZs. When using different formats for performance improvements, accelerator should provide hardware logic for decoding of the tensors that are stored in different formats (and support for any on-the-fly encoding). Such decoding logic may use existing data intersection mechanisms (e.g., comparators or skip mechanisms) but, it will require separate logic for each of the multiple formats to fetch absolute position of an NZ in a vector/tensor (e.g., different circuitry for decoding tensors encoded with RLC, CSC, or block-sparsity).

## VI. EXTRACTION OF MATCHING DATA FOR COMPUTATIONS ON NON-ZEROS

Tensors in accelerator's memory are typically in the compressed format. Therefore, locations of the NZs that need to be computed are determined from the metadata. Once a matching pair (elements of two tensors that need to be added or multiplied) is extracted, a PE can proceed for computations. Identifying effective NZs is the primary step towards eliminating ineffectual computations due to sparsity. By leveraging sparsity of CNNs AlexNet [1] and VGG-16 [144], MACs can be reduced by  $3.3\times$  and  $4.8\times$ , respectively  $(1.5\times$  and  $1.6\times$  for only IA sparsity and  $2.4\times$  and  $3\times$  for only W sparsity) [25]. CNN accelerators including Cnvlutin [72] and Cambricon-X [41] demonstrated similar speedups by leveraging sparsity of activations or weights, and ZENA [129] and Cambricon-S [37] showed achieving high collective speedup. E.g., ZENA accelerated CONV layers of AlexNet and VGG-16 by about  $3.3 \times$  and  $4 \times$ , as compared to its baseline architecture processing dense tensors. When leveraging higher sparsity (e.g., 92% sparse weights [71] of NLP model BERT-baseuncased [8]), accelerators can reduce computational cycles further and achieve even more speedups depending on their data extraction schemes. This section describes different data extraction mechanisms (Table V provides a taxonomy), their management in PEs or as central/shared modules, and their trade-offs. Then, it discusses further acceleration opportunities to effectively leverage various sparsity levels.

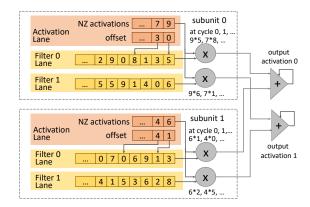


Fig. 8. Data extraction in subunits of Cnvlutin PE (Figure adopted from [72]).

#### A. Non-Zero Detection and Extraction Mechanisms

A data extraction mechanism needs to feed functional units of PEs every cycle. So, based on their processing of scalars or vectors of NZs, Table V categorizes the corresponding extraction mechanisms as (i) MAC operation on scalars, (ii) scalar-vector multiplication, and (iii) vector-vector multiplication.

1) Indexing dense tensors by indices of NZs of a sparse tensor: Depending on sparsity, only one tensor may be treated as sparse and compressed (e.g., activations by Cnvlutin [72] and NullHop [120] or weights by Cambricon-X [41]). So, the position of an NZ can be used to index the other (i.e., dense) tensor to extract the corresponding value.

Sc-Sc MAC: Data is extracted for a scalar PE by indexing a dense tensor with positions of NZs of a sparse tensor. Consider the activation lane and filter lane 0 of subunit 0 in Fig. 8, which can be visualized as processing on a scalar PE. For an NZ streaming from the activation lane, matching weight can be looked-up and provided to the multiplier or MAC unit.

For COO-1D encoded tensor blocks, absolute positions of NZs can be obtained directly from the metadata. Otherwise, absolute positions of NZs need to be computed explicitly. So, Cambricon-X [41] and [111] used similar NZ extraction schemes but required decoding of the metadata (bitmap, CSC, or RLC format) through simple combinational logic consisting of AND gates, multiplexers, and adders.

Sc-Vec Mul: For SIMD processing, multiple data arrays are indexed with the position of an NZ. Fig. 8 shows one such mechanism used in Cnvlutin PEs [72] for indexing matching weights of filters. Each of 16 subunits in Cnvlutin PE subunit featured an activation lane (streamed an input channel vector), 16 multipliers, and 16 synapse lanes (stored filters). A common NZ activation was fetched from the neuron lane, and its position was used to look up in all 16 synapse lanes to obtain corresponding weights for multiplication.

Vec-Vec Mul: PEs of some accelerators spatially process vectors at every cycle (e.g., an array of 16 multipliers and an adder tree in Cambricon-X [41]). Corresponding data extraction logic uses multiplexers for a parallel look-up [41], [60]. Based on positions of NZs of a vector, a combinational logic with multiplexers can select matching data elements to feed the arithmetic units. Fig. 9 shows one such mechanism used by Cambricon-X. An associated challenge is the overheads

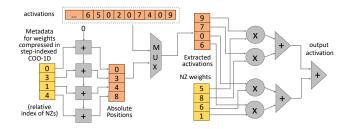


Fig. 9. Data extraction via central indexing module in Cambricon-X [41] accelerator. The indexing module decodes weights encoded in step-indexed COO-1D format to obtain the absolute positions of NZs. Then, it extracts the activations via a parallel look-up, which are later communicated to a PE via fat-tree NoC for a vector-vector multiplication. (Figure adopted from [41].)

of parallel look-up. For high sparsity, larger multiplexers need to be used for indexing the dense tensor, since the positions of scattered NZs are likely distant. E.g., a sensitivity analysis was performed for area and power of Cambricon-X by varying search length of multiplexers from 32 (supports 50% sparsity for fetching 16 elements) to 512 (96.88% sparsity). With the search length set as 256, a central indexing module occupied about 31% and 35% of total on-chip area and power, respectively (exceeded total power of all 16 PEs).

2) Compare metadata of sparse tensors for extracting matching pairs of NZs: For processing multiple compressed tensors (moderate or more sparsity), the extraction logic determines pairs of NZs (intersections) for effectual computations. Matching operands are determined by comparing indices either from streams of metadata or in multi-stage indexing.

Sc-Sc MAC: Circuitry for extracting NZ scalars can consist of one or more comparators (or AND gates for comparing bitmaps) and an additional indexing logic (e.g., in ZENA [129] and SparTen [115]). The comparators match positions of NZs and the indexing logic utilizes their outputs to extract the leading pair. Due to diverse sparsity of tensors, the positions of NZs may not match during comparison. Therefore, the detection logic uses several comparators for searching within a large window, which can usually provide at least one pair at every cycle. When using multiple comparators, priority encoders are used to obtain the leading n-pairs for feeding n computational units (n=1 for scalar PEs). The data extraction unit can use skip mechanisms (e.g., in ExTensor [92]) to quickly navigate through the lanes.

Alternatively, multi-stage indexing logic is used for extracting the pair. The first stage obtains a position of an NZ from one tensor for indexing another tensor. The later stage checks if there is a corresponding NZ in another tensor and extracts it upon matching of the positions. For example, in EIE [42], each PE loads an NZ activation from a queue; when it does not have any matching weights, it fetches the next activation from the queue in the next cycle. Depending on the sparsity level and pattern, the indexing based design occasionally cannot find the matching data, wasting the execution cycles (e.g., subsequent cycles) for functional units in the pipeline.

Sc-Vec Mul: PEs in EyerissV2 [43] use multi-stage extraction. Each SIMD PE fetches an CSC-coded activation and its position, and checks positions of NZ weights. Upon match, it

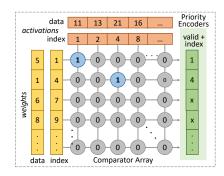


Fig. 10. Associative index matching in SNAP (Figure adopted from [106]).

forwards the activation and weights to two MAC units.

Vec-Vec Mul: The data extraction logic to feed multiple arithmetic units of a vector PE requires multiple comparators followed by priority encoders or multiplexers. For example, in SNAP architecture [106], an associate index matching module (AIM, Fig. 10) determines the positions of NZs in case of valid matches. Each PE of a row is interfaced with a shared AIM. By using comparison outcomes from AIM, a sequencer in each PE determines leading pairs of matching data, which are then fed to three multipliers within the PE. Similar extraction logic is used by Cambricon-S [37]. However, with bitmap encoding of tensors, the comparator array gets simplified as ANDing of the bits. Outputs of the comparisons are used to extract the leading pairs of NZs for vector-vector multiplications on PEs.

## 3) Eliminating extraction of intersecting NZs: Some accelerators do not require extracting fine-grained NZs.

Orchestrating structured computations: A few techniques targeted high sparsity of single tensor (DNN weights). They proposed data pruning or transformations and achieved coarsegrained sparsity, so that each PE can process a dense region of NZs. ERIDANUS [125] proposed a pruning algorithm to cluster the weights (Fig. 11a). Then, the blocks of NZ weights were dispatched to PEs of systolic arrays for conventional processing. Fig. 11(c) shows that block of weights is streamed over time and corresponding activations are kept stationary. Partial products computed by each row of PEs are added on a separate adder tree. In general, when structured pruning can ensure that the block width is set as the height/width of the systolic array, dot products can be accumulated linearly over systolic array itself. Thus, structured sparsity enables structured computations and allows to execute dense data blocks conventionally on the accelerators that are suited for dense tensor processing, with an additional support to index

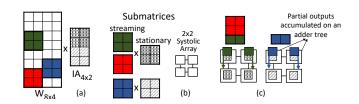


Fig. 11. Computation of locally dense regions in ERIDANUS (Figure adopted from [125]). (a) matrix multiplication of block-sparse weights (b) Sub-matrices for processing on a 2×2 systolic array. (c) Multiplication of streaming blocks (NZs) with stationary data.

the blocks and communicate them. Adaptive tiling [126] used a column-combining approach. For a sparse GEMM, NZ weights were statically combined such that each column of the systolic array could process multiple columns of input activations. Thus, it obviated the run-time data extraction and reduced total invocations of the systolic array by  $2\times-3\times$  for processing point-wise CONV layers of MobileNet. Techniques like CirCNN [162] and C-LSTM [163] proposed executing DNN operators as FFT (Fast Fourier Transform) on smaller block-circulant matrices.

Coordinate computation unit: Accelerators like SCNN [114] and SqueezeFlow [65] perform unit-strided convolutions as Cartesian product where all elements of two blocks of tensors should be multiplied together. Due to all-to-all multiplication, no special support is required for extracting matching pairs of NZs. However, index computation is still required to determine which partial-sums should be accumulated with partial products. This calculation is performed in a "coordinate computation unit" that processes metadata (indices of NZs) and determine indices of outputs. These approaches require conflict detection in hardware, since it can't be pre-determined which accumulators would be accessed in any cycle. Since coordinate computation unit facilitates direct processing on compressed tensors, it may be also used for computing block-level indices for processing a coarse-grain block-sparse tensor.

#### B. Centralized vs. Distributed Management

1) Centralized: Data extraction unit can be either centralized (and shared among PEs) or within pipeline of PEs. Advantages of central mechanisms are: (i) PEs can be directly provided effective NZs for useful computations [41]. It can also be used as a pre-processing unit for a PE-array that process structured computations, e.g., systolic arrays or neardata accelerators. (ii) Centralized extraction in some architectures (e.g., Cambricon-X [41]) duplicates hardware for concurrent extractions for PEs. However, the module can be time-shared by multiple PEs (e.g., in Cambricon-S [37], SNAP [106]), which can reduce area and power. In fact, by leveraging structured W-sparsity, the module in Cambricon-S shares extracted indices among all PEs. (iii) Centralized logic extracts work for multiple PEs and it is often coupled with a controller that allocates data to PEs. So, it can enable runtime load balancing. However, a major challenge is to maintain spatial data reuse. Because, it mostly extracts data on a per-PE basis for communication to a unique PE. So, the common data for multiple PEs cannot be multi-cast. SNAP overcomes this limitation by sharing a module with a row of PEs and multicasting data to PEs. The multicast occurs first, followed by PEs communicating their metadata to the extraction unit. Then, extracted indices are streamed back to a PE which uses them to obtain data from its local RF for computations.

2) In-PE: PEs of several accelerators including Cnvlutin [72], ZENA [129], and EyerissV2 [43] extracts appropriate data. It allows a controller to multicast or broadcast tensor elements for the spatial reuse. Because, in-PE logic can then extract the data. However, the challenges are: (i) in-PE logic may cause ineffectual computation cycles for extracting NZ

values, and (ii) employing inter-PE load-balancing in the hardware may be infeasible, as the actual work carried out by different PEs is unknown at the time of offloading compressed tensors to PEs (until data extraction in the PE datapath).

#### C. Optimization Opportunities

Based on the sparsity levels of applications, a few opportunities may be explored for further acceleration:

(i) Sparsity-adaptive low-cost data extraction mechanisms: Encodings of sparse tensors are often selected with a focus on storage benefits. However, the computational overhead and hardware cost for encoding and decoding tensors should be also reduced, since they affect the performance and energy consumption. When the data extraction cannot feed n pairs of NZs to n computational units of a PE at every cycle, achieved speedup can reduce notably from the peak. Sustaining the acceleration can be challenging for various sparsity of tensors, as different extraction schemes may be cost-effective for only a certain sparsity range and patterns. For example, for similar sparsity, extraction logic with a few comparators may easily locate a pair of NZs. However, an indexing based mechanism may be more effective, when one tensor is highly sparse and another is dense. Moreover, when positions of NZs in the two tensors can be considerably distant (e.g., for diverse sparsity levels or for hyper-sparse tensors), the extraction logic need to use several comparators or multiplexers for parallel lookup, so that it can extract at least one pair to feed each computational unit. Therefore, the extraction module needs to be configurable or use (and select among) multiple mechanisms so that it can exploit various sparsity at modest hardware cost. For the latter, it can select partial features for desired sparsity levels/patterns and power-gated otherwise for energy efficiency.

(ii) Tightening integration with load balance mechanism: Central data extraction module can enable dynamic load balancing of work among PEs (e.g., data-driven dynamic work dispatch in GraphDynS [164]). As section X discusses, inter-PE imbalance can be severe due to irregular distribution of NZs in the tensor blocks that are allocated to PEs. Its mitigation by structuring the data may not be always possible (e.g., for activations/weights of some models or for applications beyond deep learning). Consequently, accelerators may attain low speedup and ineffective utilization of PEs. Although some recent accelerators used hardware modules to dynamically balance the work, further efficient designs may be achieved by enhancing the central/shared data extraction module with additional low-cost logic. Because, it already keeps the track of the data provided to PEs, which can lead to the information about the number of operations performed by different PEs.

#### VII. MEMORY MANAGEMENT OF COMPRESSED TENSORS

Accelerators contain multi-banked scratchpads, which are usually shared among PEs. Either the scratchpad is unified [23] or separate buffers store different tensors [110], [129]. Their size varies from several tens of KBs [37], [43] to several MBs [22], [72]. Effective data management for shared and local memory highly reuses data and hides memory access latency behind computations on PEs. This section discusses how

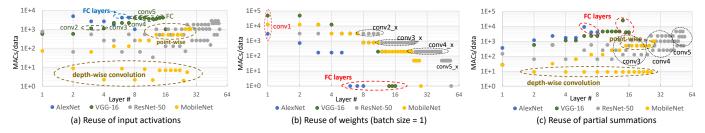


Fig. 12. Data reuse opportunities for executing different CNN layers (dense tensors) on hardware accelerators (Figure inspired by [43]).

sparsity and reduced shapes of tensors lower reuse. However, compressed tensors help achieving better speedups and energy-efficiency as more data fits in on-chip memory, reducing off-chip accesses. This section also describes how unstructured accesses (e.g., arbitrating output activations) makes bank management challenging. Then, it discusses reusing intermediate outputs via fused-layer executions and how sparsity affects it.

#### A. Leveraging Data Reuse Opportunities

1) Reuse characteristics: Depending on the functionality of layers, there can be significant reuse of tensors. Fig. 12 depicts reuse opportunities for processing different layers (early CONV layers, later CONV layers, MLPs, DW-CONVs, PW-CONVs). For each tensor, the data reuse is calculated as the total number of MACs per data element. For better visualization, reuse factors and layers are plotted on a logarithmic scale. Input activations: For CNNs, reuse of input activations increases with going deeper in the model, because the number of filters increases significantly. DW-CONVs are an exception and present very low reuse as there is only one filter. High reuse of input activations in FC layers or MLPs depends on the sizes of weight matrices (i.e., sizes of output tensors). Weights: Since 2D feature maps in CNNs are usually much larger than 2D weights, weight reuse can be higher by an order of magnitude. With going deeper in CNNs, feature maps get shrunk spatially, which lowers the reuse. There is no weight reuse for MLPs, but increasing the batch size linearly improves weight reuse. Video processing applications use 3D CNNs (e.g., c3d [6]), which can further increase the reuse opportunities [165] for input activations and weights due to additional processing steps on consecutive frames. Partial summations: Input channels are increased as we go deeper in CNNs, which improves the reuse of partial summations. MLPs also provide high reuse due to larger input vectors. DW-CONVs show very low reuse because partial summations are not accumulated across input channels.

2) Impact of sparsity on reuse: Increase in sparsity can lead to lower reuse. To determine the impact of sparsity, we considered evaluations by Han et al. [25] for pruned AlexNet and VGG-16 models. Then, we calculated the reuse as NZ MACs per NZ of a tensor. Fig. 13 plots the reuse opportunities for both dense and sparse tensors of CNN layers. It shows that while reuse characteristics are preserved (e.g., increase/decrease in the reuse of activations/weights as we go deeper), the reuse factor decreases for almost all layers and all the three tensors, as compared to processing

dense tensors. Primarily, this is due to the reduced number of effectual MACs. For example, for MLPs, weight reuse can drop below one. It means that even if a weight matrix consists of NZs, some of them are never used due to the unavailability of matching NZs in input activations. Similarly, the reuse of partial summations decreases because effectual MACs per partial summation decreases with sparsity. Note that each output activation element still needs to be populated or assembled before ReLU/encoding. Even if sparsity reduces the reuse, the available reuse can be still high for some layers (up to 1E+04) and should be leveraged for efficient accelerations.

3) Temporally reusing data through shared on-chip memory: Data reuse can be leveraged temporally (repeatedly accessing the data from memory without accessing lower-level memory) and spatially (providing the same data to multiple PEs without repeatedly accessing memory). Like CPUs, accelerators have memory hierarchies because applications have different working set sizes. When temporal reuse is high, the highest energy gets spent in upper-level buffers [23], [44].

#### B. Hiding Miss Latency Behind Computations

1) Management of tiled data in double-buffered memory: On-chip buffers are typically not large enough to accommodate all tensors. Therefore, loops are tiled for reusing some tensors from buffers, while repeatedly accessing other tensors from the off-chip memory [20], [114]. Since scratchpads are non-coherent and their management is software-directed, data is transferred by direct memory accesses (DMA) [22], [56]. PEs are engaged in useful computations by interleaving computations with memory accesses. Such objective is usually achieved by double-buffering (aka ping-pong buffers) [37], [129]. Loop optimization techniques, like loop tiling and ordering, can determine sizes of tensor blocks to be managed in memories and sequence of memory accesses for high reuse and reduced accesses to lower-level memory [23], [56].

2) Asynchronous communication: Some accelerators hide the latency of communicating data to the shared/local memory with an asynchronous mechanism which refills the memory after some data has been consumed (e.g., in Cambricon-X [41]). For such execution, PEs and DMA controller may simultaneously produce/consume data either through different banks or at the granularity of small blocks in the same bank. Similarly, when accessing shared memories via configurable communication networks [43], PEs can execute in dataflow fashion and request for partially refilling their memory with new data. Such mechanisms for asynchronous communication

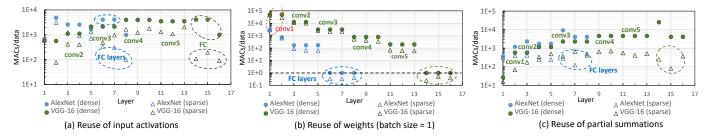


Fig. 13. Impact of sparsity on data reuse opportunities for accelerating CNN layers.

and computations can alleviate work imbalance among PEs that is caused by leveraging unstructured sparsity.

3) Impact of sparsity on latency of memory accesses and speedup: For memory-bounded execution (e.g., MLPs), even with effective prefetching, miss penalty may be significant, which restricts accelerators to achieve peak performance [22]. When tensors are sparse, the amount of the data that needs to be transferred from off-chip reduces significantly, leading to substantial performance gains. For example, Cambricon-S reported up to 59.6× speedup of FC layers for hyper-sparse weights. However, higher sparsity of activations did not provide such performance gains (speedup saturated at about  $14\times$ ), since the total execution time was dominated by the latency for accessing weights. Note that for processing high sparsity (e.g., 90%+) and low reuse, it becomes challenging to keep functional units engaged in effectual computations, because with low arithmetic intensity, the data required for effectual operations may not be prefetched at available bandwidth.

#### C. Management of Multi-Bank Memory

- 1) Concurrent accesses to memory banks:: On-chip memories are often partitioned into smaller banks [43], [114], [166]. For mapping a layer onto the accelerator, each bank is usually allocated to only one tensor (e.g., in EyerissV2 [43]). Banked buffers provide multiple read and write ports, allowing simultaneous accesses to different tensors stored in different banks [20], [167]. Although single-bank memory can be easier to manage, it is infeasible to provide multiple ports for the PEarray with just one bank [168]. Moreover, multi-port unified memory consumes very high power and longer latency [169]. Sometimes, a data layout reorganization is required before loading into memory banks. Such transformation is done after loading it from DRAM or before writing outputs to the DRAM, which can increase the execution time and energy consumption. However, for reduced memory traffic with compressed tensors, such transformation can be done along with the data encoding [110], which can alleviate overheads.
- 2) Arbitration and conflict management: Depending on the indexing logic and interconnect between memory and PEs, managing application data may require additional compilation support or hardware logic for data arbitration and conflict management [114], [161]. For regular memory accesses (e.g., computations on dense or block-sparse data), bank-allocation and accesses to the banks can be determined for mappings of layers. However, computations on unstructured sparse data can

lead to arbitrary bank accesses and require special support. E.g., outputs from PEs may need to be written to different banks. Moreover, accelerators contain accumulator-buffers [114], where PEs or their function units are connected with memory banks via a crossbar. The crossbar arbitrates write-back of outputs to appropriate bank [65], [114]. Since these partial outcomes can correspond to non-contiguous elements in an output tensor, bank conflicts are possible during arbitration, i.e., multiple outputs need to be simultaneously handled by the same bank [114], [161]. To obviate conflicts, buffer contains more banks (e.g.,  $2\times N$  banks for storing outputs from N sources in SCNN [114]). It helps alleviating the collision in hashing irregular outputs into different memory banks. So, the crossbar can require higher bandwidth and significant on-chip area (e.g., 21% for a  $16\times32$  crossbar in each SCNN's PE).

#### D. Reusing Intermediate Tensors

- 1) Reusing intermediate tensors from large on-chip memory: Intermediate feature map in DNNs is an output of a layer that serves as input to next layers. It can be maintained as stationary and reused from on-chip memory to reduce off-chip traffic. Such reuse is amplified when input is same for multiple layers due to residual connections [2] or high cardinality [94]. Leveraging such reuse can be important for latency-bounded real-time applications. Sparsity-encoding and quantization significantly reduces storage requirements, which makes such reuse opportunities more feasible. Large memories (hundreds of KBs) of accelerators (e.g., SCNN, Cnvlutin, CompAct) can enable such reuse.
- 2) Overcoming static bank assignment: Many accelerators process models layer-by-layer and do not leverage cross-layer reuse, i.e., write outputs for layer L in DRAM and load them back later as inputs for layer L+1. It is more prevalent among accelerators with small memories. Moreover, bank assignment for each tensor is often fixed at design time [167], which enforces write-back of outputs and reloading them later in other banks as inputs while processing next layers. Thus, in both cases, output activations are not reused on-chip, causing excessive off-chip memory traffic. To address this problem and exploit cross-layer reuse, shortcut-mining [167] used a flexible architecture with decoupled physical-logical buffers.

For pre-known sparsity, prior techniques for statically determining the data allocation to memory banks may work well by estimating sizes of encoded tensors. However, for dynamic sparsity, conservative estimations may lead to inefficient uti-

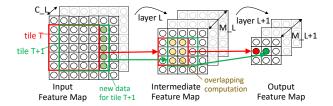


Fig. 14. Fusing the execution of layers can significantly reuse intermediate activations [170] (Figure adopted from [170]).

lization of banks, and efficient banking for non-conflicting accesses can be also challenging.

3) Fused-layer execution: Fused-layer CNNs [170] leveraged cross-layer reuse by processing small tile of activations such that outputs for few layers can be computed alongside while retaining the corresponding data in the on-chip memory. Fig. 14 shows an example for processing an input tile of  $5\times5$  activations ( $C_L$  input channels) for layer L and finally obtaining  $1 \times 1$  output activations  $(M_L + 1)$  output channels) for layer L+1. Apart from reusing intermediate outputs for obtaining the output tile, corresponding tiles of intermediate activations and filters are maintained in the memory and partially reused for processing next tiles (striding execution in the spatial direction). [170] reported reducing off-chip transfers of input feature maps by 28% for the first two layers of AlexNet and by 95% for first five layers of VGG-19. Since the cascading by storing all the filters and input channels (dense tensors) requires high memory, [170] applied it to only early layers. However, sparsity-encoded tensors and further tiling across filters/channels allows fitting tensors for multiple layers in the small memory, making such reuse opportunities more feasible. The tile size and number of layers that can be fused are bounded by memory capacity. So, fusion parameters depend on the actual/anticipated sparsity levels. For efficient executions, fusion parameters need to be explored systematically with sparsity-aware dataflows.

#### E. Techniques for Further Energy-Efficiency

- 1) Look-ahead snoozing: Depending on the sparsity, encoding of tensors, and mapping of the layer, several banks can be unused or inactive for certain time intervals. Accelerators achieve further energy efficiency by power gating unused or inactive banks. For example, look-ahead snoozing in CompAct [110] targeted reducing the leakage power of large on-chip SRAMs. Each bank of its activation SRAM can be powergated. Unutilized banks for execution of a layer were put in the deep sleep mode (maximal savings in leakage power, while not preserving any data in unused banks). Further, based on the data movement schedule, period of active cycles for each bank was determined. Then, inactive banks were snoozed during execution (i.e., connecting the bank to the data retention voltage for consuming lower leakage power).
- 2) Skipping memory hierarchy: Some layers (MLPs, without batch processing) do not provide significant reuse. Data reuse is also lowered due to sparsity and architectural choice for extracting or communicating NZs. Therefore, a few

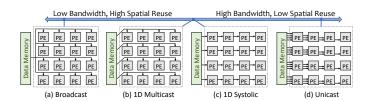


Fig. 15. Common NoC designs (Figure adopted from [43]).

accelerators (e.g., EIE [42] and Cambricon-X [41]) obviate storing non-reusable data (weights for MLPs) in the shared memory and directly feed it to appropriate PEs.

#### F. Optimization Opportunities

(i) Hardware/software designs for managing both data and metadata in unified memory: Accelerators often contain separate buffers for metadata (positions of NZs) and codebook (shared values) or indirection tables for leveraging value-similarity. Although such designs are easy to manage for processing tensors of some models encoded in a specific format, it may not scale well across different levels of sparsity and value-similarity, as storage requirements can vary significantly. So, designers can explore unified memory architectures (partitioning, banking, port requirements) for managing both data and metadata and their trade-offs. Such trade-off analysis can help tailoring coarse-grain designs for FPGA-based accelerators.

## VIII. INTERCONNECTS FOR DISTRIBUTING NON-ZEROS AND REDUCING PARTIAL OUTPUTS

Network-on-chip or NoC is required to efficiently distribute data to PEs, exchange data between PEs e.g., for reducing partial outputs, and collect distinct outputs back from PEs. For processing data-intensive ML models, accelerators employ multiple high-bandwidth interconnects for simultaneous communication of different tensors between PEs and buffers. At first, this section describes NoCs for distribution of operands, which vary in terms of bandwidth and spatial reuse of the data. With efficient NoC design, PEs can be engaged in processing data from input FIFOs and/or local memory, which gets interleaved with communication of another set of data via NoC. This section also discusses configurable NoC designs that can support various bandwidth requirements and spatial reuse opportunities due to variations in sparsity and tensor shapes. In processing sparse tensors, unstructured reduction of partial outputs among PEs can be challenging. This section describes different mechanisms for accumulating the outputs temporally and/or spatially at PE-level and PE-array level. It also discusses configurable mechanisms for efficient asymmetric accumulation of variable-sized partial outputs.

#### A. Mechanisms for Distribution of Operands

Fig. 15 shows some common NoC designs for distributing the operands along with NoC bandwidth and achievable spatial reuse [43]. Data can be spatially reused by distributing it to multiple PEs or function units. For layers with high reuse opportunities (Fig. 12), it lowers communication and helps

TABLE VI NOC DESIGNS FOR DISTRIBUTION OF SPARSE TENSORS

	Fat-width /	[41], [65], [72], [92], [111], [113], [114],	
	Unicast	[120]–[122]	
Topology	Multicast	[92], [106], [120]	
Topology	Broadcast	[37], [42], [60], [65], [66], [68], [72],	
		[106], [111]–[116], [121], [122], [129]	
	Mesh [110], [125], [126], [133]		
	Configurable	[43], [104], [172]	
	Activations	[37], [42], [43], [60], [66], [68], [72],	
Spatial		[104], [106], [111]–[113], [115]–[117],	
Reuse		[120]–[122], [129], [161]	
	Weights	[43], [65], [104], [106], [114], [116],	
	Weights	[129], [161]	

hiding the communication latency. Most accelerators leverage spatial reuse with multicast or broadcast NoC. They consist of configurable buses or trees that multicast the data to PEs (often in single cycle) [20], [104]. In contrast, the mesh interconnect (e.g., in systolic arrays) or 1D buses spatially reuse and communicate the data with store-and-forward mechanism [22], [110]. Low-reuse tensors are distributed with unicast NoCs.

The communication requirements vary significantly depending on the sparsity of tensors, available reuse, and adopted dataflow mechanism. [171] provides a detailed analysis of different NoC topologies and [172] characterize the NoC bandwidth required for different dataflows. Similarly, analytical tools including [57] model implications of different dataflows on communication requirements and execution time.

- 1) Broadcast: Accelerators including Cnvlutin [72], EIE [42], and Cambricon-S [37] use broadcast NoC to reuse activations for processing CONVs or MLPs. Similarly, in SCNN [114], weights are broadcast to PEs for executing unit-strided convolutions with input stationary dataflow. For sparsity-encoded tensors, their NZs (and positions) can be broadcast for spatial reuse, as long as the NZs are indexed or extracted afterwards (e.g., in-PE extraction in Cnvlutin and EIE). In Cambricon-S, positions of intersecting NZs are extracted centrally prior to broadcast, but due to structured sparsity, the extracted positions are same for all PEs. So, NZ activations are broadcast to all PEs. Accelerators often employ multiple broadcast NoCs for simultaneously broadcasting different data to their corresponding PE-groups. For instance, Sticker [161] broadcasts different blocks of activations and weights to different columns and rows of PEs, respectively.
- 2) Multicast: Eyeriss [20], ZENA [129], and SNAP [106] use multicast NoC to spatially reuse multiple operands. For example, Eyeriss processed tensors with row-stationary dataflow where PEs of a same row processed same spatial rows of filters and diagonal PEs processed same spatial row of feature maps. Eyeriss facilitated such multicasting through its configurable NoCs, which consisted of row-wise and columnwise interconnect controllers for 2D PE-array. Each controller could be configured with a pre-determined tag value, which was compared at run-time with the row-wise or column-wise tag of a packet. Upon matching the tags, a row-wise controller forwarded the packet to associated column-wise controllers, and a column-wise controller forwarded it to associated PE. Similarly, for processing bitmap-coded tensors in ZENA [129],

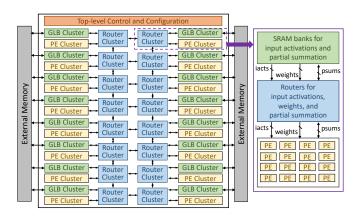


Fig. 16. EyerissV2 accelerator architecture [43] (Figure adopted from [43]).

a block of activation tensor was broadcast to a row of PEs, and a block of weights was multicast to PEs of the same column.

- 3) Mesh: A few accelerators including Compact [110], ERIDANUS [125], and [126] use systolic arrays with mesh interconnects. Since the same data is forwarded among PEs in the same row or column, such interconnects achieve the same amount of spatial reuse as multicast NoCs. But, it makes difficult for efficiently executing sparse tensors. Therefore, preprocessing is required to cluster appropriate NZs or index appropriate block of structured-sparse tensor before feeding PEs of the systolic array [104], [125], [134].
- 4) Unicast: SCNN [114], Cambricon-X [41], and Squeeze-Flow [65] use unicast NoC or point-to-point links. Such NoCs concurrently feed different elements to various PEs. They are used when tensor cannot be spatially reused, e.g., weights in MLPs, NZs are extracted beforehand, due to dataflow requirements, or for simultaneous collection of outputs (section XI-A). With high bandwidth, they reduce communication latency [41], but can incur high area and power.
- 5) Configurable: Communication requirements vary with different dataflows that are effective for some DNN layers (section IX-B and Table 25). Further, while communication may be visualized as gather, scatter, forward, or reduction patterns [172], [173], efficient execution may demand a combination of these patterns or even non-uniform patterns including multi-hop communications among PEs [23]. Therefore, configurable NoC designs are required, which can be flexibly programmed for executing various communication patterns amenable to different reuse and sparsity. Recent designs including EyerissV2 [43], microswitch-NoC [172], and SIGMA [104] address some of these challenges.

EyerissV2 [43] uses a novel hierarchical-mesh NoC, which is illustrated in Fig. 16. EyerissV2 contains 16 clusters (8×2 array) of PEs and global buffers (GLBs). Each PE-cluster contains 3×4 PEs, and each 12 kB GLB-cluster contains seven banks for input and output activations. At the top-level, router clusters are connected through a 2D mesh and enables communication among different PE-clusters and GLB-clusters. For local communication among each PE-cluster and GLB-cluster, a router-cluster with ten routers is used. Each router connects PEs with a port of the GLB cluster for accessing

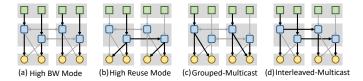


Fig. 17. Different configuration modes of hierarchical mesh network in EyerissV2 architecture [43] (Figure adopted from [43]).

GLB bank or off-chip memory (three, three, and four routers for managing input activations, weights, partial summations). As Fig. 16 shows, an all-to-all NoC connects all PEs of a PEcluster to all routers of the adjacent router-cluster. As Fig. 17(a)–(d) illustrates, the all-to-all NoC for local communication facilitates multiple communication patterns including multicast, broadcast, and unicast of the tensors. 2D mesh topology enables inter-cluster communications, allowing an interleaved-multicast or broadcast to a different cluster.

For an N-PE accelerator, an array of microswitches (Fig. 18a) contains  $\log_2 N + 1$  levels with N micro-switches at each level. Each microswitch contains a small combinational logic for configuration and up to two FIFOs for buffering the data during routing conflict. With small logic and storage, data traverses through several microswitches within each cycle [172]. All microswitches contain gather and scatter units, and bottom microswitches (level  $\log_2 N$ ) also contain local units for inter-PE communication. In top microswitches (level 0), scatter unit connects to memory banks, and gather unit uses round-robin-based priority logic for arbitrating the incoming data in a pipelined manner. In middle microswitches, scatter units forward data to desired lower-level links, and gather units stream the data back. In bottom microswitches, scatter and gather units stream the data, and local units connect adjacent PEs. Fig. 18(b)–(d) shows how configurable microswitches can enable various communication patterns.

SIGMA [104] used Benes topology with configurable switches (Fig. 19a). For N source and destinations, the interconnect contains  $2\log_2 N + 1$  levels, each with N number of  $2\times 2$  switches. Each switch receives two control signals to determine whether to forward data vertically and/or diagonally. After combining communication requirements for distributing all elements to desired multipliers, switches can be configured

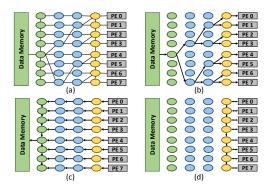


Fig. 18. (a) Microswich network [172]. NoC configurations: (b) multicast (c) gather (d) local communication. (Figure adopted from [172].)

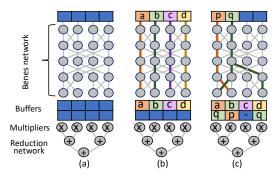


Fig. 19. (a) Flexible dot product engine in SIGMA accelerator [104] features a data distribution NoC with configurable switches interconnected via Benes topology. (b)–(c): Configuration of the interconnect facilitates different unicast and multicast communication patterns. (Figure adopted from [104].)

to forward the data, as shown in Fig. 19(b)–(c).

#### B. Mechanisms for Reduction of Partial Outputs

Computation primitives of ML models require reduction (accumulation) of partial outputs from PEs or their function units. It can be done temporally and/or spatially (Table VII).

1) **Temporal:** All the reductions for computing an output scalar are performed on a single PE (or a function unit) during different cycles. Accumulations are done temporally when different PEs compute distinct outputs, e.g., for output stationary dataflow. Temporal reduction makes processing of sparse tensors simple, because PEs update partial outputs in their private memory or registers, without communicating to other PEs via an additional interconnect. Therefore, it is adopted by many accelerators including EIE [42], ZENA [129], and SparTen [115]. However, temporal accumulation requires indexing the memory/buffer for reading/writing partial outputs or by accumulating computations in the output register (of MAC unit). So, it involves register/memory read and write operations which consume higher energy, as compared to integer arithmetic [23], [44]. Besides, using local accumulator buffers for vector/SIMD function units (e.g., in SCNN) require support for arbitration of partial outputs.

2) Spatial: Partial outputs can be reduced spatially for an output scalar. It can be done by either the function units within a PE (e.g., adder-trees in Cambricon-X/S that processes partial products from multipliers) or inter-PE communication via a separate interconnect for reduction (e.g., forwarding in systolic arrays). Inter-PE spatial reduction usually requires communication among neighboring PEs and is typically achieved through a mesh or similar topology [20], [110], [126]. Spatial reduction obviates buffer accesses and improves energyefficiency (e.g., by  $2\times-3\times$  [128], as compared to temporal reduction on scalar PEs). However, a major challenge for spatial (and spatiotemporal) reduction is the need for efficient and flexible mechanisms for asymmetric reductions. Because, when adapting to high sparsity, tensor shape, or target functionality (e.g., DW-CONV), an efficient dataflow may require some of the function units or PEs to compute distinct output elements, for keeping them engaged. Hence, all partial outputs cannot be reduced altogether (linearly in a systolic fashion, or

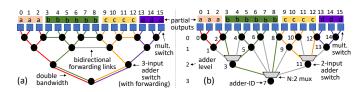


Fig. 20. Configurable spatial reduction trees: (a) Augmented reduction tree in MAERI (Figure adopted from [174].) (b) Forwarding adder network in SIGMA (Figure adopted from [104].)

via a reduction-tree). Hence, it requires configurable interconnects that provide flexibility for asymmetric and asynchronous reductions of different partial outputs. However, function units of PEs are usually kept simpler (e.g., conventional multiplierarray and adder-tree or MAC units) and they perform structured computations. Hence, for high or hyper sparsity, they cannot be fed enough NZs and are not utilized effectively. Note that structured sparsity can alleviate imbalance by inducing patterns such that all PEs (or function units) process the same number of NZs. However, configurable mechanisms may be still required to support flexible dataflows that differently process the variations in functionalities or tensor shapes.

- 3) Spatio-temporal: Partial outputs can be reduced both spatially and temporally, and both locally (within PEs) and globally (across PEs). Whether PEs reduce outputs temporally and/or spatially depends on mapping of the computation graph onto PEs [56]. In spatiotemporal reduction, different PEs or their functional units compute partial outputs at every cycle or a few, and reduce them first spatially. The resultant partial output is then reduced temporally by updating the previous partial output in the memory. E.g., when data streams through PEs of a systolic array, there is an inter-PE spatial reduction of partial outputs (via PEs of each column), and then, the bottom PE-row provides the reduced partial outputs to accumulator buffers (CompAct [110], TPU [22]). PEs of SNAP [106] perform spatiotemporal accumulation locally, where partial products are first spatially accumulated through a configurable adder-tree, and then accumulated in PE's memory over time.
- 4) **Temporo-spatial:** In temporospatial reduction, different PEs or their function units compute partial outputs and reduce them locally over time. Then, they are collected later and accumulated spatially via interconnect before further processing (e.g., write-back, encoding, or other operations). For example, PEs of each row in EyerissV2 [43] first locally accumulate partial summations for rows of output feature maps. Then, partial outputs are accumulated across vertically connected PEs. SCNN [114] PEs compute output tiles corresponding to distinct input feature maps stored in their buffers. Outputs are temporally reduced by indexing the accumulator buffers. Then, overlapping fractions of incomplete outputs are exchanged among neighboring PEs for reduction. SNAP [106] also performs temporospatial reduction at PE-array (core) level. Its PEs accumulate outputs locally over time, which are reduced spatially along horizontal/diagonal PEs by a core-level reducer.
- 5) Configurable: MAERI [174] and SIGMA [104] employ configurable reduction trees for efficient and asymmetric spatial reduction of partial outputs. So, it can be useful for spatial

TABLE VII
MECHANISMS FOR ACCUMULATIONS OF PARTIAL OUTPUTS

Temporal	[42], [66], [68], [92], [111], [113], [115], [117], [120]–[122], [129], [132], [133]
Spatial (intra-PE)	[37], [41], [104]
Spatial (inter-PE)	[65], [66], [104], [174]
Spatio-temporal	[106], [110], [128]
Temporo-spatial	[43], [106], [114]
Configurable	[104], [106], [174]

processing of unstructured sparsity and variable-sized vectors for dot products. Augmented reduction tree in MAERI (Fig. 20a) allows asymmetric reduction on partial outputs with its configurable adder switches and bidirectional forwarding links. Each 3-input adder switch can receive two partial outputs from previous level and one via a forwarding link, and it can add and/or forward them. Plus, upper-levels of the tree (near root) have double bandwidth than lower-levels, which allows simultaneous collection of multiple reduced outputs. Forwarding adder network in SIGMA (Fig. 20b) enables similar configurable reduction, but at reduced area and power. Instead of 3-input adders, it uses 2-input adders and N:2 mux for selecting the inputs. Also, adders at 0<sup>th</sup> level allows bypassing of partial products to the next level.

#### C. Optimization Opportunities

i) Low-cost flexible interconnects for accommodating spatial reuse opportunities, dynamic communication requirements, and various sparsity and precision: Sparse tensors of different layers exhibit various levels of reuse (Fig. 13), which is affected by sizes of tensors, the functionality of the layer (e.g., stride, separable execution), batch size, and sparsity of tensors. The communication mechanism needs to leverage such reuse by supporting various multicast and unicast patterns [43], [172]. Moreover, depending on the load balancing and inter-PE synchronization employed, distribution of unique chunks of sparse data to PEs, inter-PE communication for accumulating sparse tensors, and writing the outputs back from PEs to shared memory can be done asynchronously and concurrently. This requires the interconnect switches to support dynamic communication (including low-cost logic for priority and congestion management). Furthermore, communication among distance PEs may be required (e.g., for store-and-forward or exchange of outputs during sparse computations). Finally, depending on the sparsity and precision of tensors, the bitwidth of the metadata and NZ value can differ significantly. Communication of different numbers of data and metadata elements can be facilitated by designing the configurable interconnect buses and their interfacing with PEs and memory. For instance, in EyerissV2 [43], a 24-bit bus can supply PEs either three 8b uncompressed values or 8b NZs and 4b metadata. Thus, various configurable interconnect topologies should be explored for effectively serving such communication requirements for different reuse scenarios, dynamicity, and bitwidth of the NZ data and metadata. When execution of target models necessitate supporting a wide range of communication patterns and bit-width, FPGAs can be leveraged for designing accelerators with tailored interconnect topologies.

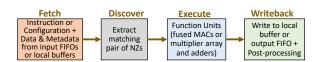


Fig. 21. Overview of the PE pipeline for processing sparse and value-approximated tensors (Figure adopted from [106]).

ii) Programming support for configurable interconnects and design exploration: While configurable interconnects can support various communication patterns and dynamic data movement of sparse computations, the compilation support is required for programming configurable switches of the interconnect for facilitating such execution for various dataflows. This is because, configurable interconnects often employ parameterized multi-level switches and switches with many-tomany links between source and destination switches (e.g., [104], [172]). Depending on the interconnect topology and optimized dataflow, the compiler may need to select efficient paths for distributing data from source to destination switches. Additionally, the underlying topology (e.g., lack of multi-hop connectivity) may not support some dataflows (e.g., spatiotemporal accumulation of partial outputs that are produced by distant PEs). Further, systematic methodology for mapping communication flow onto interconnect topology can enable design space exploration of efficient interconnects that are required for accelerating required ML models, with the minimum overhead of run-time reconfiguration of the interconnect switches to support various dataflows.

#### IX. PE ARCHITECTURE DESIGN

PE architecture consists of function units, local memory (RFs or SRAMs), and local control (instruction buffer or finite state machine). Fig. 21 shows pipeline stages for processing sparse and value-approximated tensors. Depending upon PE's interface, it either gets data from the interconnect (typical) or directly accesses off-chip memory via DMA transfer. At every cycle or few, a PE processes an instruction or events based on its state [127], [161], [175], fetches data from local memory (or interconnect), computes tensor elements via function unit, stores the intermediate result into local memory, or writes the data back (to lower memory or interconnect). Application-specific PE designs may also contain special-function modules (e.g., for ReLU or sigmoid computations [68], [114]).

Processing compressed tensors can impose significant maneuvering efforts for PE design. For example, reusing tensors temporally through local memory (e.g., in EyerissV2 [43], SNAP [106]) alleviates overheads of repeatedly accessing compressed tensors via memory hierarchy and decoding them. However, it requires that data is communicated to PEs before indexing NZs for effectual computation. Thus, the PE may require additional hardware for extracting NZs or correctly indexing the data (section VI). Additionally, selection of function units is affected by the number of NZs that can be fed for various sparsity of tensors, support for mixed-precision, and functionality of the layers. For different layers of the models, dimensions of tensors [3], functionality, and sparsity can vary significantly; a single dataflow may not

TABLE VIII
PE ARCHITECTURES FOR ACCELERATING SPARSE TENSOR
COMPUTATIONS

Scalar	[20], [30], [42], [65], [66], [68], [92], [108], [111], [113], [115], [116], [118], [120], [121], [127], [129], [132]
SIMD /	[37], [41], [43], [60], [72], [104], [106], [112], [114],
Vector	[117], [122], [124], [128]

be always effective [43], [176] and can lead to significant acceleration loss. Therefore, PE datapath needs to be adaptive for supporting multiple dataflows optimized for different layers and sparsity. Further, techniques for leveraging computation reuse due to value similarity often require enhancements in the design. PEs may also post-process outputs or generate additional metadata for communicating outputs. So, efficient pipeline needs to hide pre-processing and post-processing latency.

#### A. Function Units

1) Scalar PEs: Table VIII lists accelerators based on their function units for scalar, SIMD, or vector processing. Several architectures including EIE [42] and SparTen [115] contain an array of scalar PEs; PE datapath contains a pipelined MAC unit. With scalar PEs, data extraction and communication for keeping MAC units engaged can be easy.

2) SIMD/Vector PEs: PEs of Cnvlutin [72] and Cambricon-S [37] contain multiplier arrays and adder trees for vectorvector multiply at every cycle. Such designs can deliver high throughput. Moreover, accumulation through adder-trees spatially reuses data, which lowers energy consumption (by  $2\times-3\times$  [128]) as compared to temporal accumulation on scalar PEs by reading and writing partial summations via local memory. However, a major challenge is inefficient utilization of multipliers and adders, which often leads to ineffectual computation cycles and the acceleration loss. Because, for high sparsity, enough NZs may not be extracted to feed all multipliers at every cycle. For example, a sensitivity analysis by [41] determined that for high W-sparsity, Cambricon-X accelerated convolutions by about  $8 \times$  (vs.  $16 \times$  peak speedup). Similarly, utilization of the multiplier array in SNAP [106] can fall below 80% for moderate sparsity and up to 20% for 90% sparsity of tensors. So, the utilization may be improved by employing larger indexing modules or more comparators (increased on-chip area and power). Alternatively, PEs can be designed with a fewer multipliers to sustain the scalability and efficiency over a wide sparsity range.

While SIMD or vector PEs achieve spatial reuse, due to fixed designs, they are poorly utilized while executing some functionalities like DW-CONV. Efficiency of SIMD PEs is further affected by high sparsity, as computational units of the PE require synchronization and there may not be enough effectual computations to feed all of them. Configurable designs of function units can overcome such limitations. For example, PEs of SNAP architecture [106] use a configurable adder-tree. It processes inputs from three multipliers and computes different combinations of partial summations. With multiple adders

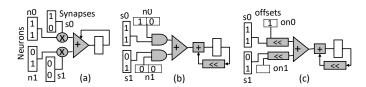


Fig. 22. Bit-serial processing of sparse activations in Pragmatic [107]. (a) Bit-parallel unit. (b) Bit-serial unit. (c) Bit-serial unit in Pragmatic for processing only essential bits. (Figure adopted from [107]).

and multiplexers, the PE can concurrently process different partial summations (vs. gather in adder-tree), while eliminating the need for high-bandwidth crossbars (in scatter networks). Such configurable designs make the architecture amenable to flexibly support different and novel DNN operators or tensors of different shapes, e.g., DW-CONVs.

- 3) Multiplier-free PEs: Accelerators including ZENA [129] and [111] use multiplier-free PEs for high energy efficiency. These PEs process tensors of very low-precision (binary or ternary values) or logarithmic quantization. So, they replace multipliers with simpler arithmetic like 2's complement (inverters and adders or subtractors) [111], [177] or bit-wise shift and additions [102], [178]. However, one challenge is to maintain accuracy of DNNs, as aggressive quantization often drops top-1 and top-5 accuracy, e.g., by 0.1% [178] 5% [102]. By trading off the flexibility with simple hardware, supporting various models on such accelerators can be challenging.
- 4) Bit-adaptive computing: Precision requirements for targeted accuracy can vary for different models [107], [179], which can be supported by PEs with bit-adaptive computing.

**Bit-serial computing:** Albericio et al. [107] showed that zero bits in NZ activations (8b or 16b precision) can be more than 50% and proposed Pragmatic accelerator for leveraging sparsity of activation bits. Fig. 22(b) shows bit-serial computation of an inner product with an array of AND gates, adder tree, and bit-wise shift of partial output. AND gates are serially fed 1b activations (variable precision) and bit-parallel 16b weights (fixed precision). Fig. 22(c) shows processing of only NZ activations in Pragmatic (essential bits indicated by their positions). Laconic [180] achieved further accelerations by processing only NZ bits of both activations and weights.

**Bit-composable computing:** Bit-fusion [181] employed fusion units consisting of an array of BitBricks. The fusion units can be configured for processing multiplications of 2b, 4b, 8b, or 16b operands. For processing NZs, PEs of CNN accelerator Envision [108] used a single-cycle N-subwordparallel multiplier, followed by a N×48b/N reconfigurable adder. The subword-parallel design allowed configuration of MAC units for processing the data of 4b, 8b, or 16b. SPU architecture [109] employed DGRA, a decomposable CGRA, for efficiently processing stream-join accesses. The DGRA PE and interconnect switches enabled decomposing up to four 16b sub-word operands. DGRA also supported accessing sub-word data from the scratchpad. For DNN training with mixed-precision and sparse tensors, PEs of LNPU contained configurable MAC units that can process either FP8 or FP16 tensors. Table IX lists precisions of sparse tensors that are supported by different accelerators. The precision indicates

TABLE IX
PRECISION OF SPARSE TENSORS SUPPORTED BY ACCELERATORS

binary/ternary	[111], [133]
int8	[110], [115]
int16	[20], [37], [41], [42], [65], [68], [72], [106],
litto	[112]–[114], [120], [122], [124], [126], [132]
logarithmic	[129], [131]
bit-adaptive	[107]–[109], [180], [182]
FP8	[66]
FP16	[66], [121], [133]
FP32	[30], [104], [133]
FP64	[92], [118]

the bit-width of input operands (activations and weights). For MAC operations, accumulators usually produce high-precision output which can be down-scaled or truncated afterward.

5) Clock-gated PEs: PEs can be clock-gated when not used for executing a layer and for ineffectual computations. For example, Eyeriss [20], Thinker [127], and Minerva [74] use zero detection for clock gating the datapath in the PE pipeline. PEs check whether the value being read is zero (or compare with a threshold, e.g., in MNNFast [130]), and based on the comparator output, their clock gating logic prevent the MAC datapath from switching in the consecutive cycle and reduce energy (e.g., saved power consumption of Eyeriss PE by 45%). Zero-skipping through flags in Envision [108] and Sticker [161] achieved similar savings.

#### 6) Optimization opportunities:

(i) Exploring efficient designs of function units for various sparsity range/patterns and functionality: Utilization of vector/SIMD units can drop significantly due to unstructured sparsity [106] and for accelerating tensor computations beyond dot-products e.g., DW-CONV. Therefore, for exploring design hyperparameters such as number of computational units (e.g., multipliers), designers need to consider the impacts of sparsity, data extraction mechanism, required synchronization among computational units, and configurations required to support various functionalities. Moreover, for low sparsity, designs should deliver performance at par with a sparsity-oblivious design. For example, for processing dense tensors, SCNN [114] achieved 79% of the performance and consumed 33% higher energy as compared to baseline accelerator for processing dense tensors. So, designers may ensure that additional features for exploiting sparsity and configurable components do not increase the critical path latency and are power-gated if not used.

#### B. Dataflow Mechanisms

1) Background: The efficiency of executing a layer of a model onto hardware accelerator depends on the computational, communication, and memory access patterns, which are commonly referred to as dataflow mechanisms [44], [56]. A dataflow refers to the spatiotemporal execution of a model layer (nested loop) on architectural resources [23], [56]. Here, spatial execution corresponds to how PEs exploits parallelism in the computation graph and processes different subsets of tensors. Temporal execution drives the data accessed throughout memory hierarchy and data communication via

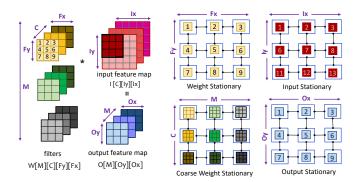


Fig. 23. Commonly used dataflow mechanisms for executing convolution layers on hardware accelerators.

interconnects. Thus, depending on the functionality and tensor dimensions, dataflow can significantly impact the utilization of resources, data reuse, and latency hiding for memory accesses and data communication, and consequently, the execution time and energy consumption [43], [44], [56], [57], [183].

One way to classify dataflows is by what data is kept "stationary" in registers or local memory of PEs (and reused fully before eviction), while other data is being iterated over. Some commonly used dataflow mechanisms are output stationary, weight stationary, input stationary, row stationary, and no local reuse. Fig. 23 shows an example of convolution and the layout of the stationary data for mapping the convolution with these dataflows. In weight stationary dataflow, each weight (of a 2D filter) remains stationary on a unique PE, and reused many times, during processing activations (corresponding to the same input channel C). By processing a unique weight, each PE produces partial summations for output activations, which are communicated by PEs and accumulated before outputs are written back to the memory hierarchy. Thus, input and output activations are accessed from off-chip memory (via shared scratchpad and PE's local memory) several times, while weights are continuously reused. After reuse, a new set of weights is loaded from the memory, and the execution repeats. Weight reuse is higher in processing larger feature maps (CNNs) and multi-folded for processing data in a batch (e.g., images for CNNs, tokens of sentences for NLP models). Fig. 25 lists such characteristics of different layers.

Dataflows can be applied at coarser-level, where PEs process a data block or plane (1D/2D/3D). In a coarse weight stationary approach [23], each PE processes weights of an entire 2D filter (dimensions C and/or M are laid out spatially on PEs). Rows and columns of PEs process the data corresponding to unique input and output channels, respectively. So, activations need to be multicast to the PEs of a row, different weights need to be provided to each PE, and partial summations for output channels can be accumulated vertically [23]. Similarly, in an input stationary dataflow, unique activations (or blocks of input feature maps) remain stationary and are reused. In an output stationary dataflow, each PE produces a unique output activation (corresponding to the the same or different output channel) [44]. By processing spatial data and input channels first, partial summations are accumulated and reused via memory of each PE. With temporal accumulation

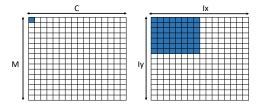


Fig. 24. Low utilization of a  $16 \times 16$  PE-array in (a) coarse weight stationary dataflow when executing depth-wise layers and (b) input stationary dataflow for executing later layers of deep CNN models (Figure inspired by [43]).

of outputs on PEs, the output stationary dataflow does not need to reduce partial outputs spatially by collecting them from appropriate PEs, which is otherwise challenging for unstructured sparse data (section VIII-B). Therefore, many accelerators opt for such dataflow. In no local reuse dataflow, input operands are streamed to PEs, but they are not stored in PE's memory [22], [44]. In row stationary dataflow, PEs of the same row process the same weights (a row of a filter), diagonal PEs process the same row of input activations, and partial summations for rows of the output feature map are accumulated through vertically connected PEs [20]. Thus, different dataflows uniquely exploit the spatial parallelism and reuse of different tensors.

Dataflow optimization: Dimensions of tensors are often large, and so many ways exist for spatiotemporally executing a layer onto computational and memory resources of an accelerator. Optimization of the dataflow is important as it can significantly impact the performance and energy consumption [23], [56], [57]. For instance, mappings with similar performance can consume an order of magnitude higher energy [183] or vice versa. Further, as Fig. 25 shows, reuse characteristics, tensor dimensions, functionality, and sparsity can vary significantly for different DNN layers. Hence, a single dataflow may not be always effective for acceleration. Fig. 24 provides two such examples that lead to low PE-array utilization. The coarse weight stationary dataflow processes different 2D filters on different PEs. So, it is inefficient for DW-CONV. Similarly, output-stationary or input-stationary dataflows can result in low utilization of PEs for processing later layers of deep CNNs. With the vast space of execution methods and growing development of the new models (with variations in tensor dimensions), it becomes hard for non-experts to figure out optimized execution methods and designs. Therefore, many optimization tools have been proposed recently including Timeloop [183], dMazeRunner [56], MAESTRO [57], and Interstellar [23]. They analytically model execution of accelerators to estimate execution metrics and evaluate a set of mappings from the pruned space of various dataflows.

2) Sparsity-aware dataflows: Dataflows for processing sparse tensors are typically similar to those for dense tensors, while processing the data in compressed format. For correct functionality, dataflow executions are facilitated by extraction/orchestration of NZs, which is done either in PEs [43], [114], on a different module [37], or by a separate controller. For example, SCNN [114] used a novel PT-IS-CP dataflow. It processed planar tiles of feature maps with input stationary

Layers	Examples	Characteristics	Implications on Execution	
		Large H/W of feature maps	High weight reuse	
Early CONV	AlexNet CONV1, MobileNet	Less filters	Low input reuse	
		Less channels	Low reuse of partial summations	
	CONV1	Low sparsity of weight		
		and activations		
	ResNet-50	Small H/W of feature maps	Low weight reuse	
	CONV4_x &	More filters	High input reuse	
Last CONV	CONV5_x, VGG-16	More channels	High reuse of partial summations	
	CONV4	High weight sparsity and		
	& CONV5	moderate activation sparsity		
		Smaller activation vectors	No weight reuse (batch size=1)	
MLP	AlexNet FC, VGG-16 FC, NeuralTalk	Large weight matrix	execution is memory-bounded or communication-bounded	
		High weight sparsity and low/ moderate activation sparsity		
		Single filter	Low input reuse	
		, and the second	Low reuse of partial	
Depth-		No channel-wise reduction	summations	
wise	MobileNet d/w		Low computation and	
CONV	Xception		high communication	
			requirements	
		No/low sparsity due to non- pruning of few parameters		
	MobileNet s/1,		Reduced reuse of	
		nception 1x1 convolution kernel	weights & activations	
Point-	module in		limits structured	
wise	GoogLeNet,		sparsity to channel and	
CONV	CONV Fire module in SqueezeNet		filter direction	
		Low/moderate sparsity due to few parameters		
Residual Layers	ResNet-50, U-Net	Concatenation of outputs	additional accesses to off-chip memory	
			opportunity for on-chip	
		additional inputs from previous layers	reuse of intermediate	
			feature maps	
Group CONV	ResNeXt Aggregation Blocks	Parallel paths due to cardinality	opportunity for input reuse with fused executions	
3D CNN	C3D	Temporal processing across frames	heavy computations, increased data reuse	

Fig. 25. Characteristics of different DNN layers pertaining to hardware execution (Figure inspired by [43], [57]).

TABLE X
DATAFLOW MECHANISMS OF ACCELERATORS

Input Stationary	[104], [111], [114]
Output Stationary	[30], [37], [41], [42], [60], [65], [66], [68], [72], [92], [106], [108], [112], [115]–[117], [121], [122], [132], [133]
Weight Stationary	[126], [104], [125]
Coarse Weight Stationary	[72], [113]
Row Stationary	[20], [43]

dataflow. PT-IS-CP-sparse dataflow extended the PT-IS-CP, and processed only NZ activations and weights in compressed format while accessing them from memory and performing computations on PEs. The coordinate computation module in each PE ensured that partial products generated by all-to-all multiplications of NZ inputs and weights were accumulated correctly and stored in appropriate buffers. Table X lists sparsity-aware dataflow mechanisms used by accelerators.

EyerissV2 [43] used an enhanced row-stationary dataflow. Using statically known sparsity of weights, more NZ weights were allocated in local memories and global scratchpads. For example, each PE can store up to 192 NZ weights. Mappings

of CONV and FC layers of AlexNet with row-stationary dataflow allocated 64–174 NZ weights, which corresponded to a total of 132–480 weights in the dense format. With in-PE data extraction logic, each PE only processed NZ values from CSC-encoded data. Thus, sparsity-aware dataflow can be optimized with the pre-known (or expected bounds of) sparsity-levels and the degree of value sharing.

#### 3) Optimization opportunities:

(i) Dataflow optimizations accounting for storage and computational overheads for metadata and codebooks: Sparse and value-shared tensors are processed along with metadata (indicates positions of NZs) and code-book (common values shared among tensor elements), respectively. It requires additional processing, e.g., buffer management, communication via interconnect, and indexing of appropriate values. Depending on the dataflow, such additional management can considerably increase the execution cost. Existing tools for optimizing dataflows target dense tensor computations. Similarly, accelerators like EIE, SCNN, and Cambricon-S process sparse tensor computations but, with customized dataflows. Frameworks for mapping and design explorations need to consider the sparsity and value sharing of tensors and their variations across layers/models. To facilitate such support, such tools can include include costs for corresponding storage, communication, extraction, and computational overheads (due to metadata, codebook, precision variations, etc.) in their analytical models. Explorations supporting multiple dataflows can help achieving efficient designs for handling different functionality and variations in sparsity, shapes, and quantizations of tensors.

(ii) Sparsity-aware resource partitioning: Acceleration of deep learning models is scaled by simultaneously processing multiple layers. It is done either by partitioning resources [166] of a scaled-up accelerator or on multiple accelerators (scale-out) by leveraging model-parallelism or data-parallelism [184]. Techniques for resource partitioning aim to reduce data movements and highly reuse data from on-chip memory of accelerators. It involves evaluating many-to-many mappings between layers and accelerators. Such optimizations can be crucial for several applications that require low-latency, real-time processing or high frame rates (e.g., processing the frames on multiple object detection models of an autonomous vehicle system). Exploiting sparsity can provide further opportunities due to less computation, communication, and storage.

#### C. Leveraging Value-Similarity and Computation Reuse

Several techniques have leveraged value similarity and computation reuse for accelerating DNNs (Table XI). Video frames exhibit high similarity spatially (among neighboring pixels) and temporally (over consecutive frames) [98], [185]. After precision lowering, values of limited range repeat frequently [27], [97], which are further compressed by maintaining a codebook of unique values [42]. With repetition of values, computation can be reused, either partially during processing a layer [97], [98] (fine-grain) or by skipping processing of a whole layer [145] (coarse-grain). This subsection describes such techniques and corresponding hardware enhancements.

TABLE XI
LEVERAGING VALUE SIMILARITY AND REDUCED COMPUTATIONS.

Value similarity	Weights	[37], [42], [97], [116], [186]					
value similarity	Activations	[98], [187]					
Computation reuse	Partial	[97], [98], [124], [186]–[189]					
and memoization	Full	[145], [185], [190]					
Computation reduction with		[191]–[193]					
early termin	ation	[191]-[193]					

1) Weight similarity: Prior studies have shown that weights can be approximated with a small set of values. Hegde et al. [97] showed that for 8b weights of DNNs, each NZ value mostly repeated for more than 10 times and for more than 100 times in later layers of AlexNet and ResNet-50 models. Han et al. [27] showed that pruned weights of DNNs can be quantized with k-means clustering for value sharing. Then, the unique values can be represented with 4 or 5 bits and shared among all elements, without dropping classification accuracy. Local quantization (applying clustering separately over different subtensors) can achieve even smaller codebooks [37]. Leveraging the weight similarity can compress pruned models further by up to an order of magnitude [27], [37].

Value-shared weights are processed by augmenting the PE datapath with a weight decoder (e.g., in EIE [42]). For processing NZ weights, the PE provides the encoded index of the weight to the decoder and obtains shared value. Depending on the lookup mechanism and total bits to be extracted at every cycle, the decoder can incur considerable area and power costs (e.g., for Cambricon-S [37], 32.56% and 3.98% of the total on-chip area and power, respectively).

2) Input similarity: Audio or video frames can contain high similarity spatially or temporally. Because, a speech signal can be quasi-stationary for a short interval. Also, successive executions of DNNs process overlapping windows of audio frames for context extraction [98]. Feature maps for CNNs exhibit high spatial correlation [187]. High input similarity enables storing only unique values and reusing computations with a differential processing of non-similar data.

Riera et al. [98] showed that after uniform linear quantization of inputs of DNNs (e.g., C3D [6], EESEN [194], CNN for self-driving cars [195]), about 61% of input activations are same as previous execution and 66% of the computations can be avoided. Their accelerator maintains centroids of quantized inputs and corresponding index for each input element. Then, consecutive frames are processed layer-wise with differential computing. For example, for each activation of an FC layer (of a new frame), the accelerator calculates centroid and index, and then it compares calculated centroid to memoized centroid. If the difference is zero, then output from the previous execution is reused and next activation is processed. Otherwise, new value of the index is updated in the buffer and new values for output activations are computed by accumulating multiplications of weights with the difference.

3) Computation reuse (partial during processing a layer): UCNN [97] leverages repetition of weights by forming activation groups (summations of activations) that share the same weight. It also reuses activation sub-groups i.e., memoize partial summations of activations that can repeatedly

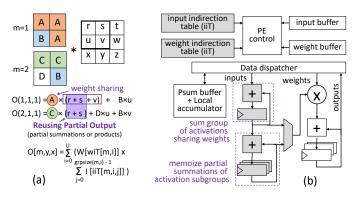


Fig. 26. (a) Leveraging weight similarity and reuse of partial outputs [97]. (b) Modifications in UCNN PE architecture (shaded blocks) for buffering indirection tables, partial summations of activation groups, and memoization of partial outputs. (Figure adopted from [97].)

appear across different filters. Fig. 26(a) illustrates an example. Weights A and C can be shared among corresponding activation groups. For producing activation groups, subgroups like (r+s) can be reused with memoization. So, an output activation is calculated by indexing unique weight value and corresponding activation groups. Indirection tables provide indices of the unique weight and grouped activations. Fig. 26(b) shows corresponding modifications in the PE datapath. UCNN reported up to 24% area overhead for a PE and  $1.8 \times$  speedup for CNNs as compared to execution on a baseline accelerator without exploiting weight repetition.

Silfa et al. [188] showed that for RNNs (e.g., DeepSpeech2 [196], EESEN [194]), relative difference between the output activations over consecutive frames was about 23%. Leveraging temporal similarity of outputs saved about 24% computations with negligible accuracy loss. To predict whether an output activation leads to a similar value as previous output, their technique extended each RNN layer with a binary neural network (BNN). With BNN outputs correlating to actual outputs, execution of much smaller BNN layers led to an efficient prediction of the temporal output similarity.

4) Computation reuse (completely skipping layer execution): A few techniques predict outputs based on previous computations and skip heavy computations of some layers. [185] showed that about 18%–81% of computations in AlexNet CONV layers can be reused due to spatial (intraframe) and temporal (inter-frame) redundancy of the inputs. They leveraged such reuse with memory look-ups and avoided execution of CONV layers. For DNNs like YOLO-v3 [4], it processed only 22%-32% of the frames with a negligible accuracy loss. [145] proposed to skip heavy processing of some CNN layers for several frames (predicted) and executing precise computations periodically for remaining (key) frames. For predicted frames, their algorithm estimated motion in the input frame and used the result to incrementally update output saved from last key frame. Unlike some of the value similarity techniques that incur changes in PE datapath, such techniques can be efficiently executed on a separate module (e.g., EVA<sup>2</sup> [145]) or co-processor, while other modules of the same or different accelerator computes sparse tensors of DNN layers. EVA<sup>2</sup> identified 78%–96% of the frames for AlexNet and 40%–71% of the frames for Faster-RCNN as predicted frames while processing YouTube-BoundingBoxes dataset [197].

5) Early termination of computations by predicting outputs: Accelerators including SnaPEA [191], SparseNN [192], and CompEND [193] reduce ineffectual computations by early prediction of the usefulness of outputs. They check whether computations contribute to the effective inputs for the subsequent layer (e.g., ReLU or max-pooling). If not, their PEs terminate such computations. To reduce computations corresponding to output sparsity, [191] statically re-ordered weights based on their signs. PEs of its SnaPEA architecture contained prediction activation units (with each MAC) which checked sign-bit of the partial summation and raised termination signal to notify the controller as the sign-bit was set.

#### 6) Optimization opportunities:

(i) Joint exploration of spatial and temporal similarity of inputs, weights, and outputs: Depending on model's configurations (depth, layer dimensions, cardinality) and domain-specific data, opportunities for value sharing and computation reuse (at both fine-grain and coarse-grain levels) in processing activations and weights can vary considerably. A joint exploration for different tensors can help to identify storage-Opsaccuracy trade-offs for efficient acceleration.

(ii) Leveraging value similarity through separate processing: Determining value similarity and leveraging computation reuse often demands modifications in PE-array, and can increase the accelerator's area, latency, or power. Designers may obviate it by providing a separate and compact module for differential computing that handles necessary pre-processing or post-processing and can be interfaced with the PE-array and on-chip memory. Upon requirement, it can trigger execution on PE-array for structured computations. Further, algorithms expressing the functionality of ML layers/models may be defined in terms of differential computing (i.e., execution is conditional to the input mismatch, reused otherwise). With efficient hardware/model codesigns for differential processing of tensors, accelerators can attain structured effectual computations with less overheads of metadata or memoization.

#### X. LOAD BALANCING OF EFFECTUAL COMPUTATIONS

Depending on the distribution of zeros, the inter-PE or intra-PE imbalance can cause low utilization of PEs or their function units, which increases execution time and energy consumption. This section summarizes sources of such imbalance, and then it discusses different software-directed techniques or hardware designs for balancing the computations. Table XII categorizes these techniques. Software-based techniques facilitate structured computations by forming local regions of dense elements, sorting the data by combining same-sparsity tensor blocks, or regularizing models with structured pruning. Although requiring low/no additional hardware, they are often limited to static W-sparsity. Accelerators dynamically balance computations by prefetching work in FIFOs or memory, which obviates fine-grained synchronization of computations on PEs. Some accelerators achieve further run-time balance across PEs by a central hardware module for work-sharing.

TABLE XII
CLASSIFICATION OF LOAD BALANCING TECHNIQUES

Software - Directed -	Data Clustering	[65], [125], [126], [134]					
	Data Reorganization	[115], [122], [129]					
	Model Regularization	[37], [60]–[62], [68], [117]					
Hardware	Prefetching of Work	[41], [42], [68]					
Module	Work Sharing	[66], [129]					

#### A. Sources and Impact of Imbalance

1) Inter-PE imbalance: Zeros in different tensors can be scattered and their positions may not be deterministic statically (e.g., W-sparsity due to pruning coarse-grain blocks and unstructured IA-sparsity). For most of the accelerators, work allocation is determined statically; so, extraction and communication mechanisms feed the data for a fixed set of computations to each PE. Also, executions with conventional dataflows usually require synchronization among PEs (e.g., in SCNN [114], Cnvlutin [72]), which is achieved by barriers implemented in software via instructions or in hardware via PE architecture or controller logic. With unstructured NZs, computations per PE during each execution pass can vary drastically (inter-PE load imbalance). So, many PEs may finish their computations early, get stalled, and wait for the next set of data due to synchronized execution, while other PEs still process the previously allocated data. Such imbalance lowers average PE utilization and increases energy consumption. [129] analyzed the distribution of NZ weights in AlexNet CONV3 filters and showed that in an execution pass, NZs processed by the leading and trailing PEs differed by up to 6.5×. Similarly, up to 40% cycles were idle for executions of PEs in SCNN architecture [114]. Sensitivity analysis for EIE showed that without any support for load balance, about 47% of the cycles were idle for a 64-PE accelerator [42].

2) Intra-PE imbalance: For SIMD or vector PEs, intra-PE load imbalance can also contribute to a significant acceleration loss. With unstructured sparsity of one or more tensors, enough NZs may not be extracted to feed all the function units (e.g., multipliers and subsequent adders in the datapath) within PEs, which causes intra-PE load imbalance. Sensitivity analysis for SNAP accelerator showed that with moderate sparsity, utilization of multipliers can fall below 80%, and up to 20% for 90% sparsity [106]. Similarly, SCNN [114] reported below 80% utilization of multipliers for all GoogLeNet [95] layers and 20% for the last two inception modules. Moreover, a few architectures use PE designs with multiple subunits in each PE; each subunit consists of multiplier arrays and may need to be in synchronization with other subunits of the same PE e.g., in Cnvlutin [72], [60], and [112]. With unstructured sparsity of the either tensor, multipliers and accumulators in some subunits can be often idle, while trailing subunits process computations.

#### B. Software Directed Load Balance

1) Clustering NZs for populating dense data regions: As described in section VI-A, a few techniques targeted high W-sparsity. They proposed structured pruning or data

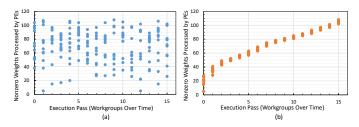


Fig. 27. Distribution of NZ weights for executing CONV1 of AlexNet [198] with coarse weight stationary dataflow on a  $4\times3$  PE-array. Distribution shows NZ weights in different workgroups (each workgroup contains NZs for 12 PEs): (a) without load balance (b) after sorting. (Figure inspired by [129].)

combining approaches for clustering the tensor elements in locally dense regions that are dispatched to PEs for processing in a conventional manner [125], [126]. Thus, they achieve high PE utilization and lower invocations to accelerator resources. However, such techniques may not be effective when algorithms cannot generate or pack structured sparse data (e.g., for dynamic unstructured sparsity).

Concise convolution rules (CCR) [65] partitioned sparse convolutions into effective and ineffective sub-convolutions for processing locally dense regions of filters and input feature maps. It eliminated most of the ineffective computations and their storage (for VGG-16, achieving reduction of about 79% and 51%, respectively) [65]. Sub-convolutions after CCR transformation were executed on the SqueezeFlow accelerator [65]. However, with PEs performing only all-to-all multiplications, it may not support generic tensor operations; it can be challenging to extend CCR methodology for other algorithms.

2) Data reorganization prior to work allocation: In ZENA [129], each PE processed a different set of filters for processing a sub-workgroup. To balance computations among these PEs, filters were sorted by sparsity and allocated to PEs such that all PEs executed filters of similar sparsity.

To determine efficacy of such sorting, we considered AlexNet [198] for ImageNet classification. We obtained the pruned model through neural network distiller [199] with the pruning algorithm similar to Han et al. [25]. For accelerating AlexNet [198] CONV1 layer with coarse weight stationary dataflow, Fig. 27 presents distributions of NZs in filters before and after reorganization. For processing 64 filters of size  $3\times11\times11$  on  $4\times3$  PEs, we consider execution through 16 different workgroups. Each workgroup contains NZ weights for concurrent processing of four different filters and three different channels on 12 PEs (up to 11×11 on a PE). To leverage high weight reuse, next workgroup can be initiated only after all PEs process previously allocated weights completely. Fig. 27(a) shows that before data re-organization, the total NZ weights allocated to PEs within workgroups differed by up to  $21.4 \times$  (5 vs. 107 for  $11 \times 11$  filters) and on average by  $6.09 \times$ . Fig. 27(b) shows that after sorting the weights (both filter-wise and input channel-wise), it leads to almost equal number of NZs for computations onto 12 PEs during each workgroup. And, the total allocated NZ weights differed by only  $1.36 \times$ .

After static sorting, ZENA achieved about 20%–32% more acceleration for CONV layers of AlexNet and VGG-16 [129]. Depending on the sparsity, distribution of NZs, and achievable

sorting granularity, the work allocated to PEs may differ considerably even after sorting. Moreover, such transformations are usually feasible only statically. So, ZENA also used dynamic work sharing, which we discuss in section X-C.

3) Accelerator-aware regularization of the model: Recent accelerators including Sparse Tensor Cores in NVIDIA Ampere architecture [61], [60], and [117] execute models pruned with k:n block-sparsity (density bounded blocks). Their PEs contain multiplexers that use indices of k NZ weights to select k values from n dense activations. Extracted values are then provided to function units. Like k:n block-sparsity, ESE [68] used a load-balance aware pruning for RNNs, which considered sub-matrices to be processed by different PEs and induced the same sparsity into all sub-matrices.

In many accelerator designs, all PEs receive the same set of NZ activations and process them with their unique weights, and produce distinct output activations. One such architecture is Cambricon-S [37] which used a coarse-grained pruning of weights. The block size for pruning depends on total number of PEs (16). The pruning was done such that all connections between an input activation and all (16) output activations in local regions were removed altogether. So, when PEs processed output neurons, they processed the same number of NZ input activations and weights for computing MACs.

#### C. Load Balancing with Hardware Structures

1) Facilitating asynchronous computations by prefetching of allocated work: One way to improve PE utilization (in the presence of load imbalance) is to prefetch the allocated work for PEs and avoid their fine-grain synchronization. So, even if there is a different amount of work (e.g., MACs per input activation), all the PEs may perform effectual computations (e.g., work on different activations) at the same time. Thus, each PE can be engaged in performing some computations, before it runs out of the available data. This can be achieved by offloading more data into FIFO or memory of each PE. For example, in EIE [42], activations are broadcast to FIFOs of all PEs. Once a PE finishes multiplying an activation to corresponding NZ weights or does not find any matching weights, it processes the next activation from its queue. FIFO size of 8 or higher ensured each PE almost having an NZ activation to process (during 87%–91% of computation cycles) and lowered idle time of PEs from about 47% to 13% [42].

Cambricon-X [41] allows asynchronous communication of weights to PEs. A centralized data extraction mechanism provides NZ activations to each PE via a unicast network, and compressed weights are loaded in the memory of each PE (2 KB). The memory access port is assigned to each PE for short period where it fetches several chunks of weights via DMA transfer. Depending on the prefetching interval and unstructured sparsity, each PE may be engaged in (asynchronous) computations throughout most of the execution cycles.

While asynchronous execution improves utilization of PEs, the work allocated to PEs is still fixed. Plus, in-PE data fetching mechanisms may restrict PEs to find out the work pending

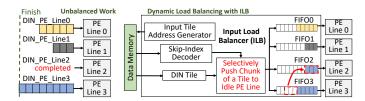


Fig. 28. Load balance mechanism in LNPU [66] (Figure adopted from [66]).

in other PEs and from work-sharing. For highly imbalanced computations, straggling PEs can still be the bottleneck.

2) Centralized load balance: In some accelerators, data is multicast to one or more rows (or columns) of PEs. A central logic processes the metadata (indices) of the tensor tiles to be distributed along with control signals from PE-rows and finds out work distribution. Then, it feeds the fast-acting rows/lanes of PEs and facilitates work-sharing. For instance, ZENA [129] allocates work dynamically through down counters. Different PE-groups (e.g., PE-rows) process the same filters with different activation tiles. A central distribution mechanism contains down counters that store the number of remaining activation tiles for each PE-group. When a leading PE-group finishes its work (counter is zero), it obtains an activation tile from a straggling group (has biggest count value) and then continues processing output activations. This work-sharing improved acceleration by about 10% for CONV layers of AlexNet and VGG-16 [129]. Memory port contention may occur when multiple leading groups simultaneously attempt to fetch the same set of input activation tiles. ZENA's execution mechanism overcomes this problem by reassigning only one activation tile at a time (to leading group) and performing reassignments only during bus idle time.

LNPU [66] uses an input load balancer (ILB) which is shared among PE-rows. As Fig. 28 shows, ILB contains address generator units to determine the indices of the compressed elements that need to be fetched. Once ILB fetches them, the skip-index decoder unit determines the appropriate indices for data extraction and pushes them along with the NZ values into the FIFO of a PE-row. It also calculates bitmaps, which are used to push the data (indices and NZs) selectively into FIFOs of PE-rows at run time. Due to ILB, PE utilization in LNPU was increased by 2%–26% for 10%–90% sparsity of the inputs (activations or their gradients) [66]. Thus, centralized load balancing mechanisms can leverage the information about data allocation for PEs and provide equal work to PEs or feed the fast-acting PEs during run-time.

#### D. Optimization Opportunities

(i) Software-level or hardware/software/model co-design optimizations for low-cost load balance: Most accelerators lack special support to balance the computations among PEs, e.g., to avoid area and power overheads due to a special hardware logic. One software-directed technique is to reorganize the data [115], [129]. But, it can only exploit the static W-sparsity for inference at no/low hardware cost. So, we may require additional co-design optimizations for regularizing/leveraging dynamic sparsity. For pre-known or estimated sparsity range and

pattern, sparsity-aware mapping optimizations for accelerators may identify dataflows that can sustain high PE utilization, while exploiting data reuse and parallelism. When models or hardware logic can induce/regularize sparsity (e.g., for many DNNs), the hardware/model co-design can induce the balance. This can be done either via structurally pruning the elements (e.g., activations, in hardware or during training) or refactoring the functions for nonlinear activations, batch normalization [77], or quantization of outputs. Consequently, the co-designs may achieve structured computations for both activations and weights at an extent, leading to further accelerations.

#### XI. WRITE-BACK AND POST-PROCESSING

Once PEs process allocated data, they write (partial) outputs back via interconnect. For unstructured sparsity, managing write-backs (WBs) can be challenging because different PEs can produce outputs of different size at different time. Moreover, operations like ReLU, pooling, and batch-normalization need to be performed on outputs. They are usually not performance-critical like CONV or MLP and can be either executed on PEs before WBs of outputs (in SCNN [114], Cambricon-S [37], and EIE [42]) or post-processed on central modules (in MAERI [174], ZENA [129], and SqueezeFlow [65]). Central modules often assemble the outputs collected from PEs, transform data as per processing requirements for the next layer, and encode sparse outputs on-the-fly.

#### A. Write-Back from PEs

- 1) Simultaneous WB: Cambricon-X [41] and SCNN [114] use fat-tree networks or point-to-point links, which allows simultaneous WBs from multiple PEs, whenever ready, PEs can execute in a dataflow manner and immediately write outputs back once done with computations. This is important for processing unstructured sparsity because, different PEs may process different number of NZs and produce different amounts of output values for WB at different time intervals. With such high bandwidth, communication time can be reduced and interleaved with computations, which is important for processing models with low arithmetic intensity. These PEs either WB to a central module for post-processing (e.g., in Cambricon-X [41]), or directly to the on-chip memory [41] or off-chip memory (e.g. in SCNN [114]). Although simultaneous WBs are faster, such a fat-tree network can incur considerable overhead due to increased bandwidth and inefficient bandwidth utilization in some scenarios. So, accelerator designs can instead use a common bus that is time-shared among multiple PEs; PEs can write the data back turn-wise or asynchronously.
- 2) Sequential WB: PEs in several accelerator designs operate in a lock-stepped manner, where data blocks common to PEs are broadcast to them, and all PEs synchronize for processing the outputs (idle when done). Synchronized execution can allow to WB in a specific sequence (e.g., a PE with the lowest PE-index writes the data first and so forth). It makes programming of the accelerator easier. It also obviates

overheads of specialized hardware/software support, which is required otherwise for asynchronous WB.

3) Asynchronous WB: With unstructured sparsity, PEs process a different amount of data and can asynchronously request WB during the execution. To facilitate such support, accelerator designs can employ additional hardware logic. For example, ZENA [129] used a common bus that was used to multicast/broadcast blocks of filters or feature maps to PEs and for collecting the output. Output buffers of PEs were flushed to the memory during the idle period of the bus, which avoided bus contention between broadcasting activations from memory and WB of partial summations. For prioritizing the requests from PEs to access the bus for WB, it determined the PE groups with a high number of pending output tiles.

#### B. Data Assembling

PEs often process large output tiles. So, they perform finegrained assembling of outputs locally. For example, SCNN [114] PEs use a coordinate computation unit which determines appropriate indices for arbitrating partial outputs to local accumulator buffer. In other accelerators, PEs produce metadata and supplies it with outputs for correctly indexing the memory (e.g., in ZENA [129]) or assembling outputs on a central module (e.g., in Cambricon-X [41], CoNNA [113]). The central module uses the metadata (e.g., output coordinates) from PEs or pre-known indices of PEs in a workgroup to assemble collected outputs, before encoding the data or WB to the global scratchpad or DRAM. In some designs, data assembling is done by global accumulators that reduce partial summations and update outputs in appropriate memory banks (e.g., SNAP [106]). The data assembling logic typically also handles data layout transformation (e.g., in [110], [113]), which is required for processing the subsequent layer.

#### C. Data Layout Transformations

- 1) Data reorganization (NWHC): Accelerators are often designed for efficient vector or matrix multiplications. So, for processing convolutions, they (e.g., CompAct [110], Cnvlutin [72]) require data layout in NHWC (channels-first) format [200], which is also used for processing on CPUs and GPUs. Fig. 29(b) shows data reorganization for striding execution of the convolution of Fig. 29(a). It shows iterative processing of the spatial data with channels-first processing. For example, an output activation 1A can be processed by fetching a block containing all channels of the first filter and ifmap. The output 1A can be computed by processing for four spatial inputs either iteratively on a vector PE or concurrently on multiple PEs. Sparse data blocks are also processed similarly, but with computations on appropriate NZs.
- 2) Transformations to Toeplitz matrix: Processing with NHWC format allows executing CONVs as iterative vector-vector multiplications, but it requires hardware support to fetch appropriate blocks. So, for processing CONVs as sparse GEMMs, a few accelerators including ERIDANUS [125] and [126] transform sparse feature maps into Toeplitz matrix with *im2col* transformation [201]. Once transformed matrices are

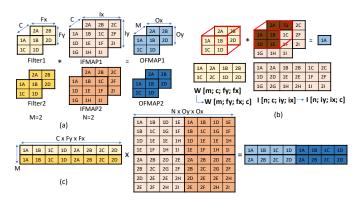


Fig. 29. Data layout transformation for executing convolution. (a) Convolution of two  $2\times3\times3$  feature maps with two  $2\times2\times2$  filters. (b) Reorganizing data for striding execution. (c) Transforming feature maps into Toeplitz matrix.

obtained and sparsity-encoded, accelerators compute sparse matrix multiplication. Fig. 29(c) illustrates the transformation for tensors of Fig. 29(a). It shows that neighborhood values for computing an output with a 2D CONV are combined as a vector. For multiple input channels of ifmaps or filters, corresponding elements are stacked in column-vectors or row-vectors. However, transforming ifmap into Toeplitz matrix duplicates neighborhood data and yields storage overhead (Fy×Fx times higher memory for unit-strided CONV).

#### D. On-the-fly Encoding

Several accelerators including SparTen [115], SqueezeFlow [65], Eyeriss [20], and CompAct [110] use an encoding module. Such module encodes blocks of output tensor on-thefly, and typically before writing them back to on-chip buffer or DRAM. It reduces accesses to off-chip memory significantly [20], [65]. On-the-fly encoding allows efficient processing of dynamically sparsified tensors, i.e., sparse activations for DNN inference and tensors in the training of models. It typically consumes low on-chip area and power, e.g., 2.5% and 3.06% for RLC encoder-decoder unit in SqueezeFlow [65] and 0.3% of total on-chip area for RLC coding unit in Eyeriss. The complexity of the hardware logic required for encoding depends on the coding format (section V). For example, single-step processing for bitmap, RLC, or COO-1D incurs low overhead. A central bitmap-encoder in SparTen consisted of comparators (XNOR gates) for determining NZs and additional logic for shifiting NZs to populate data vector. The encoding overhead may be lowered for block-sparse tensors, which require indicating only positions of blocks and each block contains several NZs.

Sticker [116] facilitates sparsity-aware encoding. It uses three modes to encode DNN tensors of high, medium, or low sparsity with COO, bitmap, and dense format. The three modes are controlled by two threshold values. Since weights can be processed offline for DNN inference, they are pre-encoded in appropriate formats. For encoding activations online, Sticker uses a sparsity adaptor module consisting of a sparsity detector, a 4 kB buffer, an encoder, and a controller. Sparsity detector contains counters that count zeros in activations of consecutive 16 channels. After the detector processes output

activations (obtained after ReLU), they are stored in the buffer. Then, the controller determines the encoding mode with which the encoder can encode the data in the buffer.

#### XII. COMPILER SUPPORT

This section provides an overview of the compiler support for sparse deep learning accelerators. It focuses on:

- Intermediate representations (IRs). They determine what type of code the compiler can support and what kind of compiler transformations it can perform.
- Support for sparse tensors. This subsection discusses challenges in supporting sparse deep learning in compilers and compilers developed to overcome these challenges.
- Compiler optimizations. This subsection provides an overview of state-of-the-art techniques that allow the compiler to apply advanced optimizations and generate the most efficient code from high-level neural network descriptions.
- Accelerator ISAs and code generation. This subsection focuses on accelerator ISAs (e.g., instruction set for high-level tensor operations) and the compiler support for machine code generation for accelerators.

#### A. Intermediate Representations

IR determines which types of code can be represented by the compiler, whether it can support sparse tensor computations, the types of code transformations that can be done, and even the scalability of the compiler.

- 1) Need for high-level representations: A common example of low-level IR is LLVM IR which is well suited for low-level code optimizations such as register allocation, but not for many high-level code optimizations needed for optimizing sparse deep learning. This is mainly because low-level IRs do not preserve information about loop structures and data layouts and reconstructing such information is not trivial [202]. This is why many deep learning compilers such as TVM [203], Tiramisu [202], and Halide [204] apply many code optimizations on a high-level IR (an IR that has loops and represents multi-dimensional tensors). This is also one of the motivations for creating MLIR [205], which serves as a high level-IR for low-level compilers like LLVM.
- 2) Mathematical abstractions of code: While previous IRs have focused on representing program statements and program structure, many compilers use an additional mathematical representation (abstraction) to represent iteration domains and array accesses of statements. These mathematical representations are usually used in conjunction with the IR to simplify iteration domain and array access transformations. This subsection presents two major families of mathematical representations and compares their strengths and weaknesses.
- **2.A. Polyhedral representation.** It is a unified mathematical representation for the iteration domains of statements, code transformations, and dependencies. It relies on two main concepts: *integer sets* and *maps. Integer sets* represent iteration

domains. *Maps* are used for representing memory accesses and transforming iteration domains and memory accesses.

An integer set is a set of integer tuples described using affine constraints. An example of a set of integer tuples is

$$\{(1,1);(2,1);(1,2);(2,2);(1,3);(2,3)\}$$

Instead of listing all the tuples, we can describe the set by using affine constraints over loop iterators and symbolic constants as follows:

$$\{S(i,j): 1 \leq i \leq 2 \land 1 \leq j \leq 3\}$$

where i and j are the dimensions of the tuples in the set.

A map is a relation between two integer sets. For example,

$$\{S1(i,j)\rightarrow S2(i+1,j+1): 1\leq i\leq 2 \land 1\leq j\leq 3\}$$

is a map between tuples in the set S1 and tuples in the set S2. More details about the polyhedral model and formal definitions can be found in [206]–[208].

**Polyhedral compilers:** Notable polyhedral compilers for deep learning include Tiramisu [202], Tensor Comprehensions [209], Diesel [210], and TensorFlow XLA [211] (through affine MLIR dialect [205]). General-purpose compilers that support deep learning include PENCIL [208], Pluto [212], Polly [213], PolyMage [214], AlphaZ [215], and CHiLL [216].

#### Strengths of the polyhedral representation:

- Unified representation: It eliminates friction within compiler IRs and greatly simplifies design of code transformations.
- Instance-wise representation: The representation granularity
  is instances of statement executions where each instance is
  a single execution of a statement during one loop iteration.
  Instance-wise representation includes iteration domains, data
  dependencies, data accesses, and code transformations,
  which allows the compiler to have a precise representation.
- Support for the whole class of affine transformations: It allows applying any affine transformation on iteration domain and data accesses. An example of a complex affine transformation is iteration space skewing, which allows extracting parallelism from multi-layer recurrent neural networks to increase hardware occupancy.
- Non-rectangular iteration domains: The representation allows compilers to naturally express non-rectangular iteration domains (i.e., iteration domains with an affine conditional).

#### Weaknesses of the polyhedral representation:

- Limited support for non-affine code: The polyhedral model mainly represents code and transformations using sets and maps described using affine constraints. This means that it does not naturally support code that leads to non-affine constraints. This includes code with non-affine loop bounds, non-affine array accesses, and non-affine conditional. While the classical polyhedral model does not support non-affine constraints, recent work has extended the polyhedral representation to support non-affine array accesses, non-affine loop bounds, non-affine conditionals [217], and parametric tiling [218]. Efficiency of these techniques has been demonstrated in practice by PENCIL [219] and Tiramisu [202].
- Slower compilation: While polyhedral operations are precise, they are computationally expensive. So, polyhedral compilers are slower than non-polyhedral compilers. Recent techniques reduce the number of statements by clustering groups of statements into macro-statements and scheduling

<sup>&</sup>lt;sup>1</sup>The iteration domain of loop iterators in a loop is all possible values that loop iterators can take.

macro-statements instead of individual statements [220], reducing the compilation time notably.

**2.B Non-polyhedral representation.** A common non-polyhedral representation used in deep learning compilers is *interval*-based representation. It uses intervals and interval arithmetic to represent iteration domain and code transformations, respectively. Using intervals, N-dimensional loops are represented with N-dimensional boxes, e.g., iteration domain of a loop nest can be represented as:  $(i, j) \in ([0, N], [2, M-2])$ .

**Non-polyhedral DNN compilers:** Their examples include TVM [203], Halide [204], DLVM [221], and Latte [222].

#### Strengths of interval-based representations:

- Better support for non-affine code: Non-polyhedral compilers can naturally support non-affine code transformations such as parametric tiling (loop tiling with parametric tile size). Because, the interval based representation does not rely on using affine sets and affine relations to represent the code or dependencies. However, non-polyhedral compilers also have limited support for non-affine code (e.g., indirect memory accesses) and code transformations.
- Faster compilation: Operations on intervals are computationally less expensive than polyhedral equivalent operations on sets of integer points, which yields faster compilation.

#### Weaknesses of interval-based representations:

- Limited expressiveness: Interval-based non-polyhedral compilers cannot naturally represent non-rectangular iteration spaces (e.g., when bounds of loop iterators depends on a condition). It is also hard to perform certain complex affine transformations such as iteration space skewing.
- Lack of support for programs with cyclic data-flow graphs: To simplify checking the legality of a schedule, many interval-based compilers assume that the program has an acyclic dataflow graph. This prevents users from expressing many programs with cyclic dataflow. For example, when a value produced by a loop is read by another loop, Halide [204] does not allow fusion of the two loops by using compute\_with command. While it avoids illegal fusion, it prevents legal loop fusions in many common cases. Polyhedral compilers avoid these over-conservative constraints by using dependence analysis [223] to check for the correctness of code transformations, which enables more possible schedules. While interval-based compilers can also implement non-polyhedral dependence analysis (by computing dependence distance vectors [224]), it is not as precise as polyhedral dependence analysis [223].

#### B. Support for Sparse Tensors

1) Challenges in supporting sparse tensors: While compiler support is needed in general for targeting ML hardware accelerators with diverse features, sparse tensor computations with various dataflows specially need further support. The code for manipulating sparse tensors exhibits non-static loop bounds, non-static array accesses, and conditionals, which is difficult to analyze at compile time. The following pseudocode shows one example of a direct convolution with sparse tensors (bounds of *j* and accesses of *in* are non-static).

```
for each output channel c_o
    for j in (W.row_ptr[c_o], W.row_ptr[c_o + 1])
    {
       coeff = W.value[j]
       offset = W.col_idx[j]
       for y in (0, out_H)
            for x in (0, out_W)
            out[c_o][y][x] += coeff*in[y*out_W+x+offset]
    }
```

2) DNN compilers supporting sparsity: Their examples include Tiramisu [202], Acorns [80], and Taichi [225].

Tiramisu supports W-sparsity by extending the polyhedral model in a way similar to [217]. For example, a non-affine conditional is transformed into a predicate that is attached to computation. The list of accesses of the computation is the union of the accesses of the computation in the two branches of the conditional, which is an over-approximation. During code generation, a pre-processing step inserts the conditional back into generated code. Non-static loop bounds and tensor accesses are represented as parameters in the polyhedral model. Statements that define those parameters are inserted just before the original statements that have non-static code. These techniques introduce approximations in the compiler. Their efficiency was demonstrated by [217] and confirmed by PENCIL [219] and Tiramisu [202].

Acorns [80] optimizes the CNNs with *IA*-sparsity. It fuses operators in a computation graph of a deep CNN, followed by sparse layout conversion (which ensures that dense/sparse tensors produced by each operator are compatible with the next operation), followed by code optimization and code generation. Acorns introduces a data layout for exploiting the sparsity structure of input data in certain domains (face detection, Li-DAR, etc.) where only certain data regions are NZs. For code optimization and generation, the compiler processes a set of template codes for CNN operators (e.g., convolution, pooling) and applies optimizations such as loop tiling, vectorization, and weight packing. It does not implement advanced loopnest optimizations like iteration space skewing.

TACO [226] uses a specific representation (iteration graphs) to generate code for sparse tensor operations and uses a scheduling language to guide the code optimization.

#### C. Compiler Optimizations

To generate efficient code for NN operators, a compiler has to apply a large set of complex code optimizations. It includes operator fusion; multi-level tiling and register blocking which improve data reuse; loop reordering, array packing [227] and data prefetching; loop skewing which enables extraction of wavefront parallelism from multi-layer RNNs; parallelization; loop unrolling; vectorization; full/partial tile separation; tuning optimization parameters to the target architecture (e.g., tile sizes or loop unrolling factors). There are two major families of optimizing compilers: compilers that allow semi-automatic code optimization and fully automatic compilers.

1) Compilers with semi-automatic code optimization (scheduling languages): The main idea in these compilers is to separate the algorithm from optimizations. A program, in this case, has two parts: The first part specifies the algorithm without specifying how it is optimized. The second part specifies how the algorithm is optimized (transformed). This is done

through a set of high-level scheduling commands for common optimizations. Halide [204], Tiramisu [202], and TVM [203] are examples of compilers that allow semi-automatic optimization. The main advantage of this approach is to allow a user to have full control over how code should be optimized. This is important because fully automatic optimization techniques do not always succeed in providing the best performance.

Semi-automatic deep learning compilers usually provide a library of highly optimized deep learning operators. The compiler then only needs to decide automatically whether to apply certain optimizations such as operator fusion. All other optimizations are encoded manually in the library using scheduling commands. This minimizes the number of automatic decisions that the compiler needs to make and thus guarantee the best possible performance. Note that semi-automatic compilers usually also have automatic optimization modules, but such modules can be disabled if necessary.

2) Fully automatic compilers: Tensor Comprehensions [209] and Diesel [210] are examples of fully automatic compilers for deep learning. Other examples of fully automatic compilers include PENCIL [208], [219], Pluto [212], and Polly [213]. All of them use Pluto [212] algorithm to automatically optimize code (choosing the schedule of statements). The main idea of Pluto algorithm is to use integer linear programming to model the problem of automatic code optimization where constraints are dependencies of the program and the objective function is the minimization of the distance between producer and consumer statements. Other compilers such as PolyMage [214] use custom algorithm for automatic optimization.

All of these compilers do not have a scheduling language and therefore do not allow the user to have fine-grain control over optimizations. Although fully automatic compilers provide productivity, they may not always obtain the best performance. This sub-optimal performance is due to the fact that they do not have a precise cost-model to decide which optimizations are profitable. For instance, the Pluto [212] algorithm does not consider the redundant computations, data layout, or the complexity of the control-flow of generated code.

Cost models for automatic code optimization: The goal of an automatic code optimization pass in a compiler is to find the best combination of code optimizations that minimizes the execution time. This can be modeled as a search problem where the search-space is a set of combinations of code optimizations. Then, the compiler needs a search technique and a cost model to evaluate each combination. Classical compilers use hand-tuned cost models [228], while others use machine learning to build cost models [229]. Both of these models do not precisely capture hardware complexity (different memory hierarchies, out-of-order execution, hardware prefetching, communication latency, etc.). Instead, state-ofthe-art models are built using deep learning for better accuracy [230], [231]. For example, Ithemal [231] is a cost model that predicts the throughput of a basic block of x86 instructions and gets less than half the error of state-of-the-art hand-tuned models (llvm-mca in LLVM [232] and Intel's IACA).

#### D. Accelerator ISAs and Code Generation

Accelerators including Cambricon-X [41], Scaledeep [233], Thinker [127], and DnnWeaver [181] expose a high-level ISA where some instructions perform tensor operations (e.g., dot product, matrix-matrix multiplication, convolution, pooling, and sigmoid). They simplify compiler's mission, because it can invoke high-level operations instead of generating and optimizing a low level-code. However, it still has to manage data copies automatically. This subsection describes such high-level ISAs used by accelerators and machine code generation.

1) Instruction sets: For tensor computations on hardware accelerators, ISAs typically feature instructions for arithmetic, logical, and data transfer operations with matrix, vector, and scalar data. Layers of ML models feature loops iterating thousands of times; dynamic instances of repetitive instructions can significantly increase the bandwidth requirements for delivering them to PEs at each cycle and the energy consumption. To mitigate such overheads, accelerators are designed with an array of vector or SIMD PEs. It allows PEs to process a single instruction for performing multiple computations on the blocks of tensors. Alternatively, PEs contain additional control logic such that they process an instruction once, but repeatedly perform the sequence of execution for a certain interval.

Cambricon ISA for machine learning [234] contains instructions for matrix and vector processing with arithmetic and logic operations, control (conditional branch and jump), and data transfer. Each operand of instruction is either an immediate value or one of the 64 32b general-purpose registers. The registers are used for temporarily storing scalars or register-indirect addressing of the on-chip scratchpad memory. The tensor blocks are communicated between computational units from the on-chip scratchpad which is made transparent to the compiler and programmers. The instructions support commonly used primitives in various ML models, e.g., multiplication, addition, subtraction, and division operations on matrices and vectors. It also supports max-pooling with a vector-greater-than-merge instruction and provides dedicated instruction for random vector generation with uniform distribution of values within [0, 1]. To support weight update during the training of DNNs, Cambricon provides additional instructions such as outer product, scalar-matrix multiplication, and matrix-matrix-addition. However, it lacks support for managing data in the local memory of PEs and configuring NoC for communication in various dataflows. Moreover, it does not provide specific instructions for handling sparsity, e.g., predicated execution of encoded sparse data.

The instruction set for Sticker [161] consists of instructions for high-level operations. For processing each layer, one of the instructions is executed only once. It configures instruction registers and common control signals that correspond to the sparsity levels and tensor dimensions. Then, at a certain time interval, a dynamic 32b instruction executes for computing convolution over data blocks on PE-array. Meanwhile, the accelerator controller distributes the next instruction, if there is no collision between the current and the next instruction. It allows hiding the execution of other dynamic instructions including the write-back and encoding of outputs and trans-

ferring data between on-chip and off-chip memory.

- 2) Finite state machines (FSMs): Some accelerators use FSMs for PE executions. The parameters of FSMs or PE's control logic correspond to tensor shapes and target functionality, and they are configured once (e.g., through bitstreams [20]) before executing a model or a layer. Accelerator controllers (which usually initiate the data movement between on-chip and off-chip memory and configure PEs and NoC) can also contain FSMs. For example, in Thinker architecture [127], a finite-state controller is used for configuring the accelerator at three levels, i.e., PE-array level, model layer level, and PE level. Configuration word for PE-array level handles partitioning of the PE-array, and it points to the memory address of configurations for model layers. Each configuration word for a layer contains information about tensor dimensions and their memory addresses. Lastly, layer configurations for PEs correspond to PE functionality and the interval (loop iterations) of computations and idle time.
- 3) Library support and code generation: The instructions for cycle-level executions or primitives are usually obtained off-line. Accelerator system designers often provide users a template library that defines high-level primitives such as model layers or low-level primitives such as vector/matrix operations. Using these primitives, users can construct the model of their interest. Then, the low-level code is obtained automatically by the compiler or using the pre-defined optimized code [233], [235]. For example, Zhang et al. [41] programmed Cambricon-X accelerator with a set of library functions (written in C/C++) for primitives like convolution and matrix/vector multiplication and addition. Chen et al. [234] proposed a programming framework consisting of assembly language, an assembler, and run-time support for executing ML models with their Cambricon ISA. For executing common layers, it also replaced the primitives with pre-defined code blocks.

TVM [203] supports defining custom back-ends for accelerators, which was demonstrated using a vanilla accelerator with a matrix-multiply engine. For executing primitives on accelerators, TVM enables Tensorization [203], i.e., decoupling the target hardware intrinsic from the schedule while mapping ML operators. To demonstrate code generation for the vanilla accelerator, TVM enabled a driver library and runtime support that constructs the instructions and offloads them to the accelerator. Its code generation module translated the program into appropriate function calls of the runtime API. Moreau et al. [236] leveraged TVM stack and proposed a JIT compiler and a runtime system to generate code for programmable VTA accelerator.

It is important that the accelerator can support multiple front-ends corresponding to different ML frameworks such as TensorFlow [49], PyTorch [48], and MXNet [237]. Integration of the programming, compilation, and runtime environment with the common frameworks for ML application development is necessary for supporting different compact ML models. Leveraging the existing system stack (e.g., TVM) can provide such opportunities to accelerator system developers. Note that although TVM supports defining custom accelerator backends and can lower optimized mappings to accelerator-specific

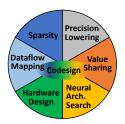


Fig. 30. Co-designs can enable efficient accelerations of compact models.

code, it currently does not provide support for sparse tensors.

#### XIII. TRENDS AND FUTURE DIRECTIONS

- A. Hardware/Software/Model Co-designs
- 1) Hardware-aware compression techniques: The framework for exploring efficient model compression (either of quantization, value sharing, pruning, and size reduction) should be aware of hardware features and provide directed search accordingly. For example, bit-widths of tensors that can be efficiently processed by different hardware platforms vary considerably (e.g., from multiple of 8-bits to arbitrary bitwidths). Accelerators typically support only uniform widths of tensors (activations and weights) and many accelerators do not support value sharing. Also, when hardware only supports widths that are multiple of 4 or 8 bits, quantization with other bit-widths require zero-padding, which incurs inefficient storage and processing. Instead, the compression algorithm can opt for improving the accuracy, increasing sparsity, or trading off the bit-widths among layers of a model such that higher hardware-friendly compression and acceleration is achieved. Similarly, depending on the hardware support for fine-grained or block-sparsity (block size, direction), hardware-aware pruning can better achieve the compression objectives (model exploration time, performance, and energy-efficiency, while meeting target accuracy). Efficiency can be further improved when compression techniques leverage execution models of hardware accelerators (e.g., energy-aware pruning [40]). Relatively simple logic modules of hardware accelerators have enabled recent techniques to estimate execution metrics through analytical cost models. Accommodating such cost models (including for different sparsity levels/patterns, precisions) enables the compression algorithms to select effective pruning ratios/structures, tensor shapes, and tensor precisions, which can help achieving desired accelerations.
- 2) Joint and automated exploration of sparsity, precision, and value-similarity: Recent compression techniques typically employ structured or fine-grained data pruning during training with a fixed precision of tensors. Techniques for adaptive quantization often do not explore pruning. Joint explorations of the pruning and quantization may achieve high compression due to the interplay of these compression mechanisms. For instance, quantization can increase sparsity considerably [120], as more values can be represented as zero after compressing the range [31]. Likewise, pruning may reduce bit-widths further, since fewer non-zero values in the pruned model may be expressed with a much lower numeric

range and precision. Moreover, such compression techniques do not leverage temporal and spatial value-similarity in inputs, outputs, or weights. So, joint exploration algorithms may be developed that use multiple compression strategies during training and automatically explore combinations that compress the model further. Recent techniques for automated explorations include CLIP-Q [238], [58], and [239]. Exploring a wide range of compression combinations during the training may not be feasible and necessary. Therefore, model designers may reduce the space of compression choices by limiting effective options before beginning resource-extensive training and, if required, further limiting the search-space by quick evaluations with a pre-trained model and fine-tuning.

Compression benefits achieved through joint explorations needs to be translated into efficient hardware accelerations. So, the exploration heuristic should not preclude experts from expressing a directed search for hardware-friendly executions, e.g., specifying pruning with 1D or k:n block-sparsity, constraints for bit-widths, tolerable accuracy loss, etc. Moreover, the heuristic should also provide automated optimization/exploration of hyperparameters (including using cost models of accelerators), because the compression algorithm needs to adjust the strategy of the pruning or quantization and corresponding hyperparameters. For instance, pruning algorithm needs to find out the pruning ratio for each iteration (epoch); pruning mechanism (which values to prune, e.g., below a certain threshold); pruning pattern (fine-grain, block-structured); bit-widths of tensors (quantization). All such hyperparameters or strategies need to be adjusted automatically (at possible extent) such that the memory footprint or computations are greatly reduced, with no or tolerable accuracy loss.

3) Value-aware neural architecture search (NAS) and hardware/model co-designs: Techniques for NAS or AutoML can automatically obtain efficient models that surpass the accuracy of models devised by human developers. However, there remains scope for considerably improving NAS for obtaining highly compact models. Recent techniques [240]–[243] have explored hardware/model co-designs that support quantized models and layers of different shapes. However, the efficiency can be further amplified by including the sparsity and adaptive bit-widths of model layers and analytically considering their implications on hardware accelerators.

A major challenge faced by the model search techniques and automated hardware/model co-designs is the vast search-space. As Fig. 30 shows, explorations can be performed for (i) ML models (i.e., NAS) [31], (ii) compression strategies (e.g., automated pruning and quantization) [244], (iii) mappings of models on accelerators [176], [183], and (iv) specifications of hardware accelerators [57], [176]. The explorations of (i) and (ii) directly impact compression and accuracy, while search optimizations for (iii) and (iv) affect performance and energy-efficiency of the accelerator for given models. Among these exploration spaces, NAS can be significantly time-consuming (several GPU days [31]), followed by the automated model compression (e.g., [244]). Therefore, the resultant joint space for value-aware NAS and hardware/model co-designs is many-folded. So, it may require notable efforts for developing

automated joint search and co-design process that can obtain extremely efficient and hardware-friendly compact models.

4) Facilitating structured computations of sparse tensors: Designers may opt for accelerators that are effective for structured computations of dense tensors, e.g., systolic arrays as near-data accelerators or coupled to processor cores or inmemory processing with resistive crossbars. While sparsity or size reduction of tensors may need to be leveraged for execution on such accelerators, significant design modifications are often infeasible due to design requirements (area/power budgets) or increasing complexity of the system stack. Therefore, techniques for pre-processing can be developed that can arrange structured dense regions for feeding underlying engines or achieve structured data through sparsification/reorganization at almost no accuracy loss. Such pre-processing can be done on additional hardware modules or the host processor that handles the non-performance-critical tasks. Such disjoint mechanisms can obviate heavy design modifications in systolic arrays (e.g., [126]) or in-memory/near-data processing engines (e.g., Re-Com [245], SNNrram [246]) while leveraging various sparsity and value-similarity opportunities across different models.

#### B. Design Tools and Frameworks

1) Framework for analyzing performance-gains of accelerators due to sparsity: Given that tensors of several ML models are sparse, it is important to design accelerator systems that can exploit performance-gains for multiple models through low-cost hardware modules and enhanced software support. As we discussed in sections V-XII, each enhancement presents multiple implementation choices at hardware and/or software level. Although crafting a cycle-level simulation infrastructure for such a wide design space may be infeasible, a data-driven quantitative model can be significantly helpful for design explorations. It can processes the actual data (or discover distributions of zeros), provide high-level modeling of common choices, and estimate the performance-gains for each combination of the implementation choices. For newer models or functionality, hardware designers can run through a set of implementation choices in an early design phase. They can explore the performance implications for the desired choice of encoding, data extraction logic, function units, NoC, load balancing, and dataflow mechanism. Such a sparse-datadriven analytical framework can also inform about the bandwidth requirements for communication, reuse opportunities, and storage and computation requirements.

2) Accelerator design frameworks for compact models: Several frameworks for developing and simulating FPGA or ASIC based accelerators have recently been proposed, including DNNWeaver [181], DNNBuilder [252], T2S-Tensor [253], and HeteroCL [254] for FPGAs and NVDLA [119], VTA [236], MAGNet [255], MAERI [174], and AutoDNNChip [173] for specialized accelerators. Similarly, hardware construction languages or representations such as Chisel [256] and  $\mu$ IR [257] enable expressing microarchitectural features through high-level primitives. Such infrastructures are key for the community since they can serve as a good learning

TABLE XIII

RELATED LITERATURE FOR HARDWARE, SOFTWARE, AND ALGORITHM DESIGNS TO ACCELERATE COMPACT MODELS CONSISTING OF SPARSE,

IRREGULAR-SHAPED, AND QUANTIZED TENSORS.

			This work	[44]	[31]	[247]	[45]	[248]	[249]	[250]	[251]
	ML / DL Models			<b>√</b>	<b>√</b>		<b>√</b>	<b>√</b>			
		ML Frameworks		<b>√</b>			$\checkmark$	<b>√</b>			
Model							$\checkmark$	<b>√</b>			
Design for				<b>√</b>			<b>√</b>	<b>√</b>			
Application					<b>√</b>	<b>√</b>					<b>√</b>
Domain		sor Quantization		<b>√</b>	<b>√</b>	<b>√</b>					<b>√</b>
	Tenso	Tensor Size Reduction			<b>√</b>	<b>√</b>					
	Neural	Architecture Search			<b>√</b>						
	Spat	ial Architectures	<b>√</b>	<b>√</b>							
Accelerator Hardware	Sparse	Enodings and Data Extraction	✓		✓						
	Tensor	Sparsity-aware Dataflows	<b>√</b>								
	Computations	Memory Management and Communication	✓								
		Load Balancing	<b>√</b>								
	Quantized	Bit-adaptive Computing	<b>√</b>		<b>√</b>	<b>√</b>			<b>√</b>	<b>√</b>	<b>√</b>
	Tensors	Leverage Value-similarity	<b>√</b>	<b>√</b>							$\checkmark$
	Irregular-shaped Tensors Benchmarking		<b>√</b>							<b>√</b>	
										<b>√</b>	
Software	Mapping Optimizations		<b>√</b>	<b>√</b>					<b>√</b>		
Stack	Compiler Support		<b>√</b>								
Co-design	Hardware/Software/Model		<b>√</b>	<b>√</b>	<b>√</b>						

resource for training of the new professionals and provide a kick-starter baseline for developing new design features.

However, most frameworks support designs for dense tensors of fixed bit-widths and lack support for sparsity-tailoring features. Such frameworks can provide some pre-built modules for encoding/extracting sparse data (e.g., with common formats like RLC, bitmap, or for block-sparse tensors), dynamic load balancing or data reorganization, configurable function units and interconnects for sparse and bit-adaptive computing, etc. Even with limited support for compressed tensors, they may serve as reusable logic that can be leveraged by designers for quick prototyping and design explorations. Further, abstractions and specifications for constructing sparsity-tailored hardware and dataflows can enable automated and efficient design explorations and easier programming of accelerators.

#### C. Accelerating Training of ML Models

While there have been significant advances in performing inference on hardware accelerators, efficient training of the models on hardware accelerators has received relatively little attention. Training has been done in high-performance computing environments containing CPU and GPU platforms and more recently, FPGA and TPU accelerators. Hardware accelerators can offer significant benefits to the model training in both edge and datacenter-scale computing environments, and it can notably improve performance and energy efficiency, respectively. In particular, they are promising for enabling online learning on edge devices through compact models.

Accelerator including [21], ScaleDeep [233], and HyPar [184] have been proposed for efficiently training the models. However, they either do not leverage sparsity, or may not be efficiently utilized for irregular-shaped tensors, or lack support for various precisions of weights activations, gradients,

and weight updates. This presents further opportunities for performance-gains and energy-efficiency. Additionally, designers can leverage cross-layer optimizations (e.g., by reusing the data of gradients during back-propagation) and support mixed-precision of tensors during training of compact models.

#### D. Applying Sparsity Techniques to Other Domains

In this work, we considered a wide variety of techniques that leverage sparsity for the machine learning domain, which represents an enormous research effort. Many other domains face similar challenges in exploiting sparsity, and accelerators have been proposed for some of the more processing-intensive domains; this includes graph processing [258], [259], database operations [260], genomics [261], [262], and compression [263]. In some cases, computation primitives even extend across domains. For example, the problem of finding intersecting non-zeros is analogous to joins in a database context [109]. Applying the lessons learned from extensive research on sparsity in an ML context can likely speed innovation in a broader context.

#### XIV. RELATED WORK

**Deep learning models and their applications:** Surveys [45], [46] described different deep learning models along with different frameworks and datasets. [264] discussed applications of CNNs in computer vision and language processing. Recent surveys have also discussed applications of deep learning in medical image analysis [13], biomedical applications [265], wireless and networking [16], and embedded systems [15]. [266] surveyed techniques for neural architecture search.

**Compact models:** [267] surveyed techniques for parameter pruning and low-rank factorization. [247] surveyed techniques for pruning, precision lowering, weight sharing, low-

rank factorization, and knowledge distillation. [31] described techniques to obtain compact models including sparsification, quantization, tensor decomposition, and joint-way compression. Table XIII summarizes related surveys about ML models, hardware accelerators, and software optimizations.

Hardware accelerators for dense ML models: [268] surveyed FPGA accelerators for processing dense tensor computations of deep learning applications. [250] discussed different CNN-to-FPGA toolchains and described their hardware architectures, design space exploration techniques, and support for different precisions of tensors. They also compared execution metrics of the designs obtained with various toolchains and that with the previously proposed FPGA accelerators for CNNs. [44] presented a survey about efficiently executing DNNs on hardware accelerators. It described different DNNs, different compression techniques for compact models, and optimized dataflows for spatial architectures. [269] benchmarked executions of different ML accelerators. [270] discussed different ML frameworks and compilers for deep learning models.

Hardware accelerators for compact ML models: [249] surveyed execution of compact models including BNNs on FP-GAs. It also discussed processing convolutions with Winograd algorithm and executions on multiple FPGAs. [31] surveyed hardware accelerators that support bit-adaptive computing and the designs of data extraction modules for leveraging sparsity of inputs, weights, or outputs. [251] recently proposed Min-MaxNN system for dynamically switching NN models. They surveyed techniques for designing self-aware NN systems (which can continuously sense information from the environment and dynamically react) including leveraging sparsity and tensor quantization. [247] surveyed hardware implementations for processing tensors of lower precisions (binary, ternary, and logarithmic quantizations). [271] benchmarked executions of quantized deep learning models on mobile AI accelerators.

In contrast to the above surveys, this work highlights sources of sparsity and size reduction of tensors in ML models and challenges in efficiently executing them on hardware accelerators. Then, it surveys and discusses the corresponding hardware and software support including encodings and extraction of sparse data, sparsity-aware dataflows, memory management and on-chip communication of sparse tensors while leveraging data reuse, load balancing of computations, and compiler support. It also discusses techniques for computations of mixed-precision and value-shared sparse tensors.

#### XV. SUMMARY

For efficient and hardware-friendly processing, compact deep learning models have been designed. They consume less storage/computation/energy and consist of tensors with considerable sparsity, asymmetric shapes, and variable precision. While these compact models can be efficiently accelerated on hardware accelerators, it requires special hardware and software support. We have highlighted challenges in efficiently accelerating their sparse and irregular tensor computations. Leveraging sparsity, especially unstructured, requires significant redesign to store, extract, communicate, compute, and load-balance only non-zeros. Moreover, the sparsity levels and

patterns due to various sources lead to unique challenges and solutions in hardware/software/model co-designs.

In this article, we have discussed how exploiting sparsity effectively depends on tailoring the data encoding and extraction, dataflow, memory bank structure, interconnect design, and write-back mechanisms. We have provided an overview of corresponding enhancements in accelerator designs and their effectiveness in exploiting sparsity. Categorization of different techniques inform whether they leveraged structured/unstructured sparsity of weight and/or activations during learning or inference of ML models for storage/performance/energyefficiency. Analysis of sparsity-encodings describe their storage efficiency for various sparsity-levels and the decoding requirements. We have introduced a taxonomy for non-zero extraction techniques that are used to feed the function units of PEs. We also discuss how structured sparsity (e.g., with coarsegrain blocks) can alleviate overheads of metadata for encoding, simplify data extraction, and facilitate balanced computations.

Data reuse opportunities for processing common DNNs can vary significantly, and sparsity lowers the data reuse due to less effectual computations. However, compressed tensors allows to fit and reuse more data in on-chip memory, which reduces accesses to off-chip memory and overall latency. We have discussed techniques for the memory bank management to support unstructured accesses for sparse computations and hiding of the memory access latency. Different accelerator designs have used various interconnects for distribution of operands, reduction of partial outputs, and collecting the outputs. They vary in terms of the bandwidth requirement and exploiting spatial data reuse. Configurable interconnects, however, can efficiently support different DNNs of diverse sparsity, functionality, and tensor shapes, as they can be configured to support a mix of communication patterns.

Processing compressed tensors can impose significant maneuvering efforts in the PE architecture design, including configurable designs of function units for efficient scalar, SIMD, or vector processing and flexible sparsity-aware dataflows for high utilization across variations in sparsity and functionality of different layers. Sparse tensor computations that are allocated to different PEs can be highly imbalanced. We have surveyed different techniques that sustain the acceleration by balancing the work through hardware modules for asynchronous computations or work-sharing or by softwaredirected regularization. The survey has also described mechanisms for asynchronous or simultaneous write-backs from PEs and on-the-fly sparsity-aware encodings. Compilation for the accelerators requires the ability to efficiently express sparsity in intermediate representations, flexibly apply different compiler optimizations, and emit efficient accelerator-specific code. The survey has discussed different techniques that enable such support.

Hardware/model co-designs can efficiently leverage various precision and value-similarity of different tensors and induce sparsity for accelerator-friendly executions. Automated and joint explorations of hardware-aware compression algorithms can advance acceleration opportunities further. We have highlighted future directions for such co-designs and the system stack development. We have also discussed further

opportunities for tailoring different hardware and software enhancements for sparsity. While our discussions focused on designs that leveraged sparsity for processing ML models, efficient designs for exploiting diverse sparsity can also aid efficient processing of applications of other domains.

In conclusion, while different accelerators and compression algorithms have been proposed for efficiently processing compact ML models, it remains an active research frontier. In particular, hardware/software/model co-designs and automated and joint explorations of tensor sparsity, adaptive quantization, shape reductions, and dataflow will likely provide further opportunities for innovations across the system. With a boost in energy-efficient accelerations of the learning and inference at the cloud and edge, they can be anticipated to further improve the intelligence of various systems or applications.

## APPENDIX HARDWARE ACCELERATORS CAN EXPLOIT SPARSITY BETTER

Exploiting acceleration opportunities due to sparsity (especially, unstructured) is relatively hard for execution on CPUs and GPUs [37], [41], [104]. The performance of ML models can even degrade, as compared to the execution with dense data (e.g., for a GEMM, when unstructured W-sparsity is below 70% [272]). For executing AlexNet layers on GPUs, [28] analyzed speedup for processing CSR-encoded matrices with cuSPARSE and dense matrices with cuBLAS. Their experiments showed obtaining limited speedups (below  $1.4\times$ ) or even slowdowns for high sparsity. This is because unstructured sparsity may yield poor data locality for scattered effectual NZs. Plus, it is challenging to skip ineffectual computations and equally distribute the work among multiple threads or compute units of processor cores. [41] analyzed performance benefits of executing sparse models (LeNet, AlexNet, and VGG-16) on CPU (with sparse BLAS) and GPU (with cuS-PARSE) platforms, as compared to processing dense models (with Caffe [201]). For average sparsity of 90.94%, they reported geomean speedup of only 23.34% for GPU and 110% more time on CPU. In their sparsity-sensitivity analysis, CPU and GPU showed marginal speedup only at moderate or high sparsity due to non-trivial costs of sparse data processing. But, for Cambricon-X [41], performance gains were reported for 5% or more sparsity due to its design tailored for sparse tensor computations. For hyper sparsity, it achieved high speedups (e.g.,  $15.5 \times$  for CONV and  $48.5 \times$  for FC layer), as compared to executing dense tensors [41]. Thus, with special support for sparse and irregular tensor computations, hardware accelerators can achieve notable speedups and efficiency.

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