
Algorithm 1 Metropolis-Hastings Algorithm

Generate samples from $p(x) \propto p^*(x)$ given proposal density $q(x^* | x)$ in I iterations

Require: $I > 0$, $p^*(x)$, and $q(x^* | x^{(i-1)})$

$x^{(0)} \leftarrow x_0; \forall x_0 \in \mathbf{X}$

for $i = 1$ to I **do**

 sample x^* from $q(x | x^{(i-1)})$

$\alpha \leftarrow \min\left(\frac{p^*(x^*)}{p^*(x^{(i-1)})} \times \frac{q(x^{(i-1)} | x^*)}{q(x^* | x^{(i-1)})}, 1.0\right)$

 sample u from $\mathcal{U}[0, 1]$

if $u < \alpha$ **then**

$x^{(i)} \leftarrow x^*$

else

$x^{(i)} \leftarrow x^{(i-1)}$

end if

end for

Algorithm 2 Gelman-Rubin Diagnostic

TODO

Require: $M \geq 2$

for chain = 1 to M **do**

 run MCMC algorithm for chain, for length $2n$ with different initial values

 discard the first n draws in chain

$B \leftarrow \frac{n}{M-1} \sum_{i=1}^M (\bar{\theta}_i - \sum_{i=1}^M \bar{\theta}_i) //$ between-chain variance

$W \leftarrow \frac{1}{M} \sum_{i=1}^M s_i^2 //$ within-chain variance

 calculate potential scale reduction factor

end for
