Queer uses for probability theory

 \leftarrow Back to Chapters

Exercise 5.3

From 5.31 we want x > y but

$$\log \frac{x}{1-x} + \log \frac{a_x}{b_x} < \log \frac{y}{1-y} + \log \frac{a_y}{b_y}$$

i.e.

$$\log \frac{x}{1-x} - \log \frac{y}{1-y} < \log \frac{a_y}{b_y} - \log \frac{a_x}{b_x}$$

or, multiplicatively

$$\frac{x(1-y)}{y(1-x)} < \frac{a_y b_x}{a_x b_y}.$$

This is of course very possible. It means simply that the level of trust of N is sufficiently different between X and Y that the the difference of evidence perceived by X and Y from the announcement is bigger than their prior difference of evidences.

Exercise 5.5

Everything in this exercise is conditional on I.

If the "graphical model" assumption $C \to B \to A$, is true (meaning that A and C are independent conditional on B), then 5.43 becomes

$$P(A|CI) = qP(A|BI) + (1 - q)P(A|\overline{B}I)$$

and since $P(A|\overline{B}I)$ is bounded by 1, as $q \to 1$ we do have $P(A|CI) \to P(A|BI)$.

In general, however, even q = 1 does not imply closeness of P(A|BI) and P(A|CI). Suppose we have a fair 4 sided die. Let C be the event "4 is rolled", B the event "the result is even", A the event "the result is 1 or 2". Then q = P(B|C) = 1, but P(A|C) = 0 while P(A|B) = 1/2.

By taking more-sided dice we can even make P(A|B) arbitrarily small while keeping the other implications.

An example "from life": B ="I'm in San Francisco" implies that the probability that A"It is snowing around me" conditional on B is very low. However, if I know C ="I'm in San Francisco and the date is February 5, 1976" then I am certain of B|C (so q=1), but also certain of A|C.