

Rhythms

Introduction (Part 1)

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Brain rhythms

Introduction

What are they?

Where do they come from?

What do they do?

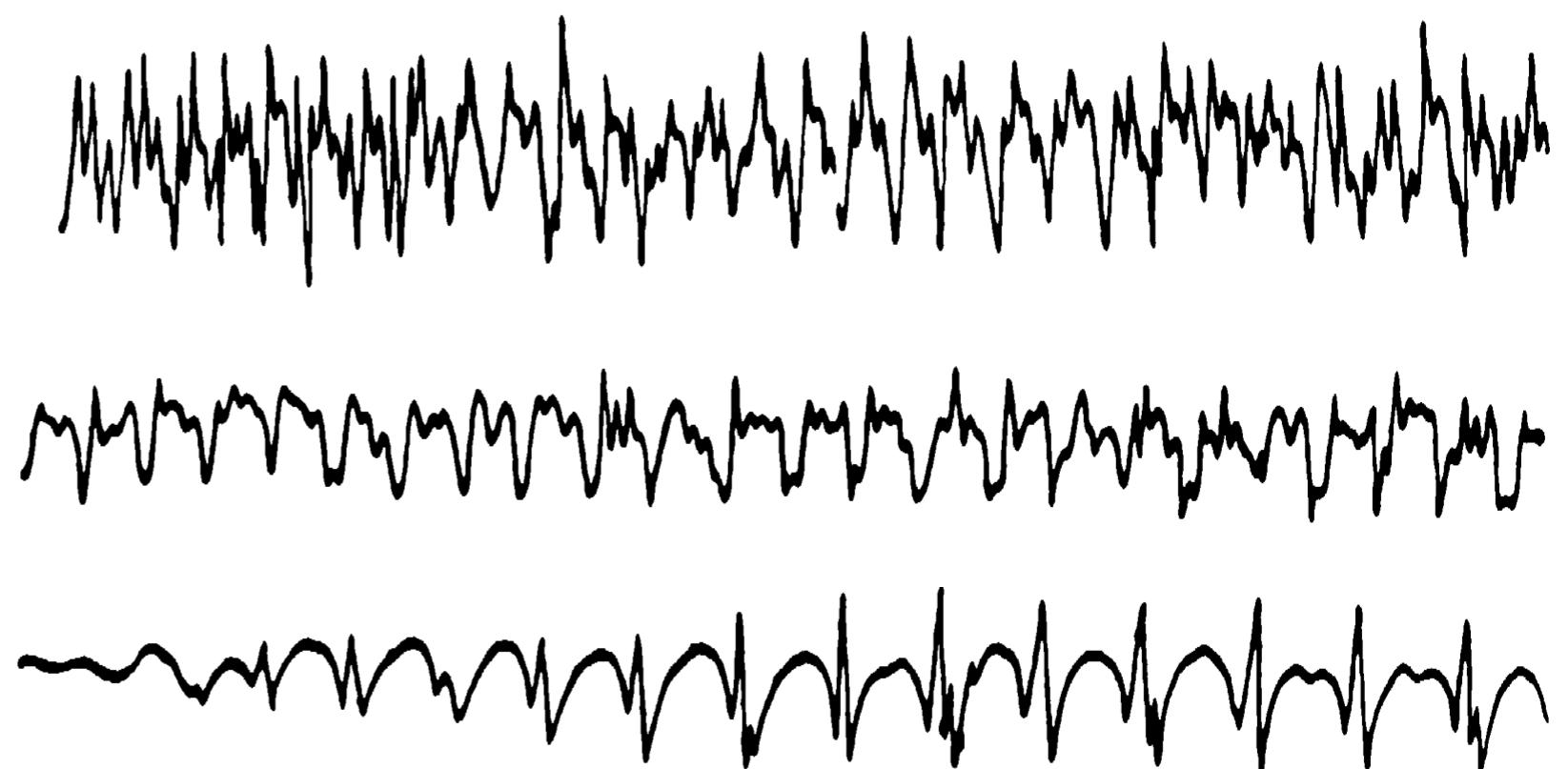
Method of analysis

Brain rhythms

Fact: The brain can generate rhythmic activity.

Ex: Scalp electroencephalogram (EEG)

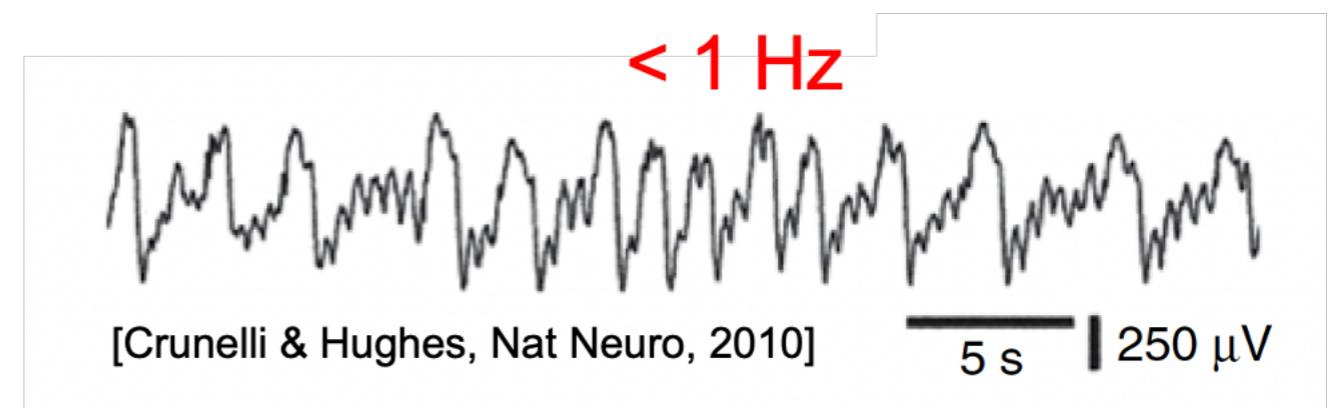
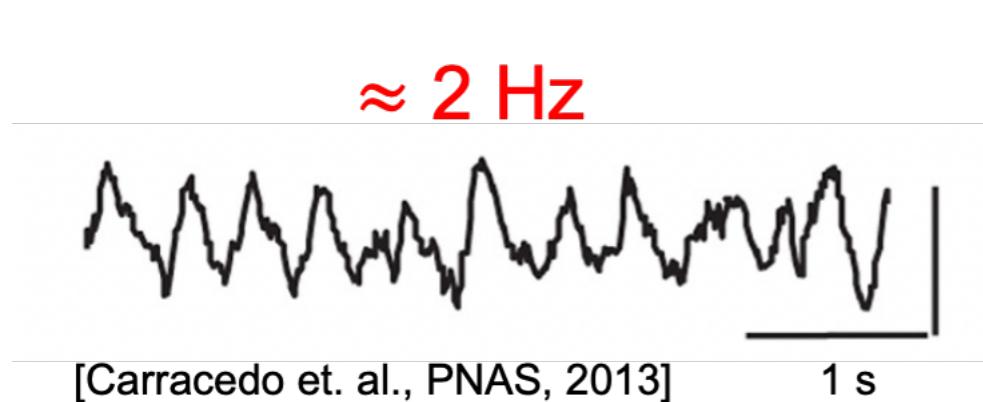
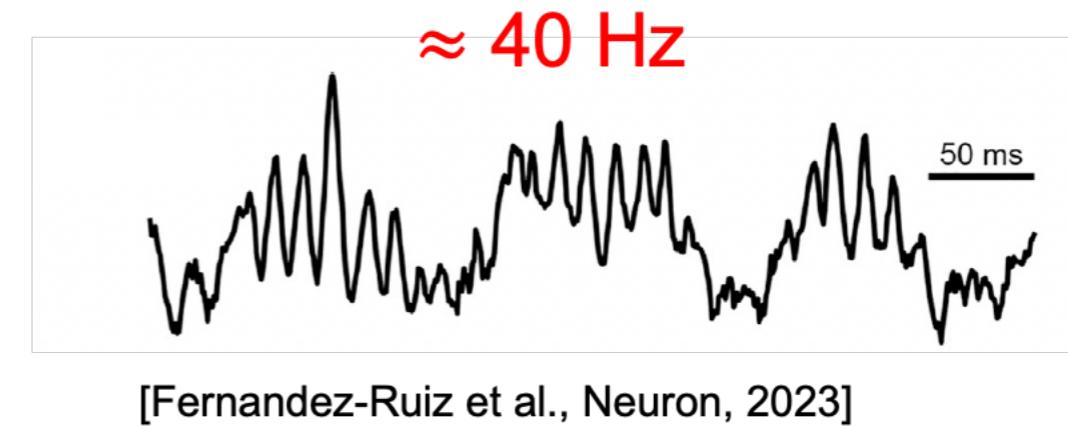
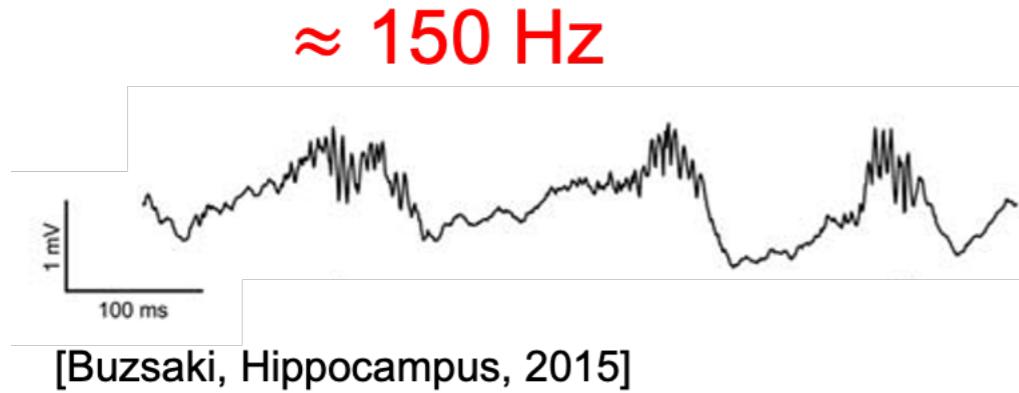
Note: Rhythms also appear in LFP, MEG, fMRI, ...



Observe: Different shapes. Different frequencies.

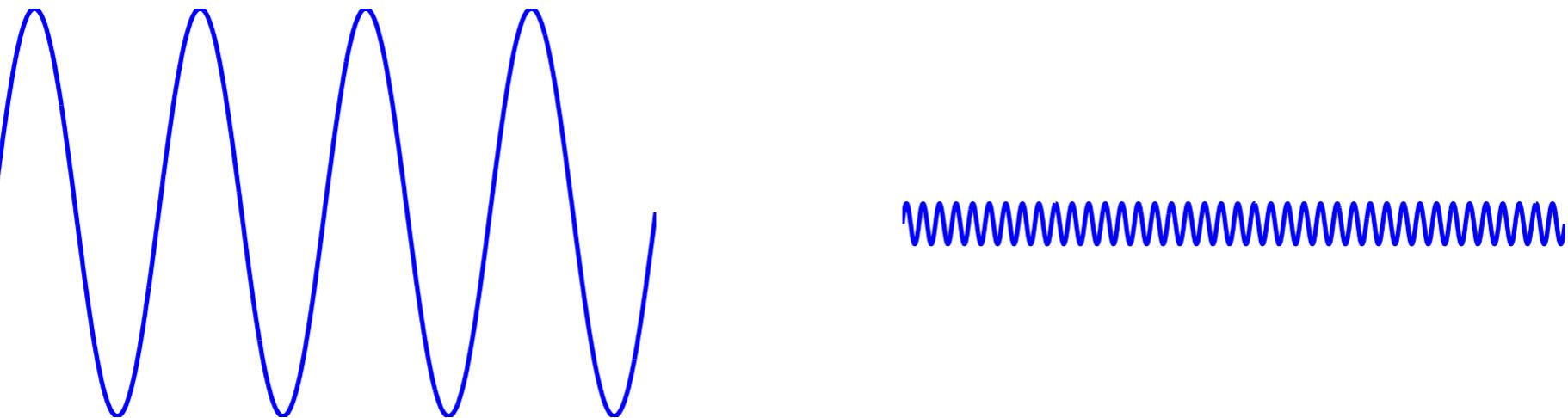
Brain rhythms

Fact: The brain can generate rhythmic activity.



Brain rhythms: “facts”

- Slower rhythms tend to be larger amplitude.

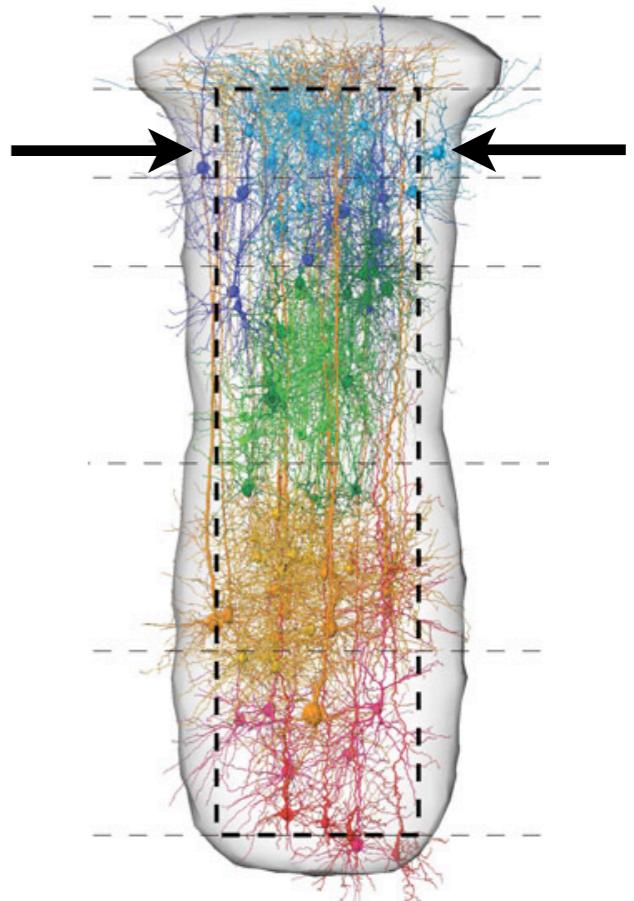


- The EEG \approx generated by coordinated synaptic transmembrane currents of many neurons.

Very complicated.

Not completely understood.

[Buzsáki et al. Nat Rev Neurosci (2012)]

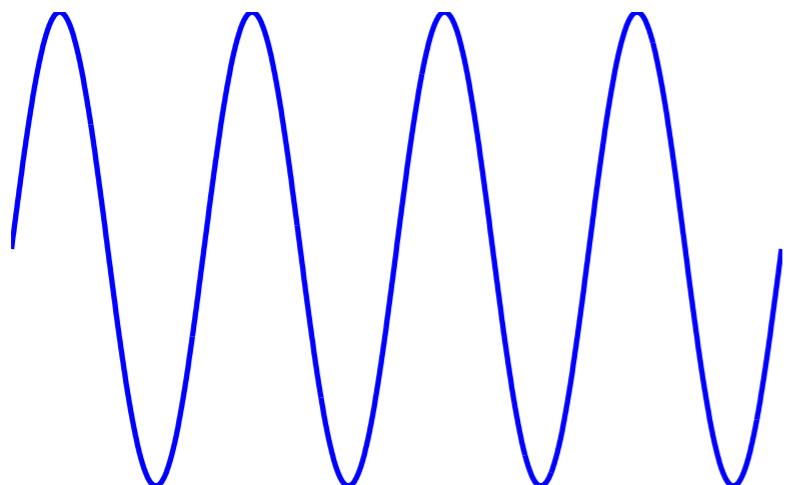


Brain rhythms: “facts”

Rhythms indicate cortical arousal

–Modulate the firing patterns of neurons.

Low frequency, high amplitude: low cortical arousal



Neural activities are . . . synchronized.

Groups of cells act in concert =
large EEG signal.

High frequency, low amplitude: high cortical arousal

Neural activities are . . . desynchronized.

Groups of cells involved in separate activities = small EEG signal.

Note: A healthy brain is a desynchronized brain.

Brain rhythms: characterization

Q: How do we characterize these rhythms?

To start, we can visualize and describe the rhythms.

Typical features:

Amplitude: Large or small ?

Frequency: Fast or slow ?

Shape: Sinusoidal, square, triangle, . . . ?

Duration: Long or short lasting ?

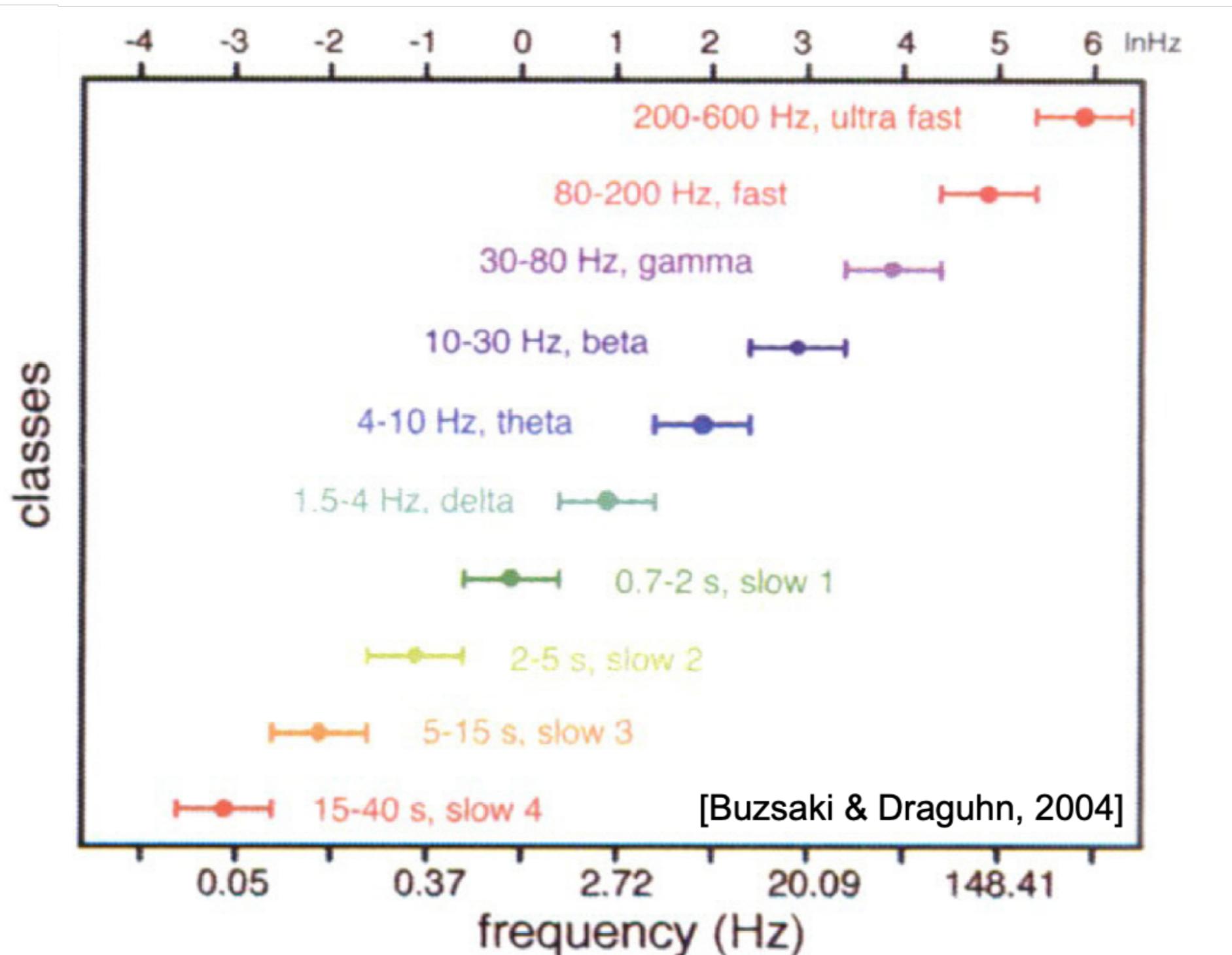
Our focus (usually) is frequency: How fast or slow is a rhythm?

Q: Why? Because different frequency rhythms are associated with different functions ...

Brain rhythms and functions

Many frequency bands, each associated with different functions.

Ex:

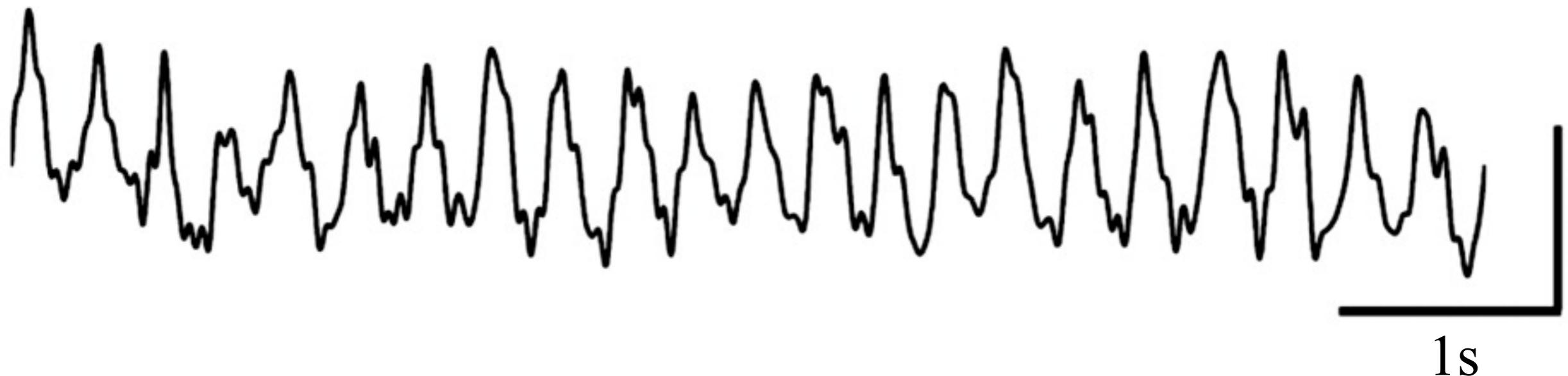


Let's look more carefully at some of these frequency bands . . .

Brain rhythms: theta

Theta: 4-8 Hz

Note: Theta frequency range different; the borders of ranges are not exact.



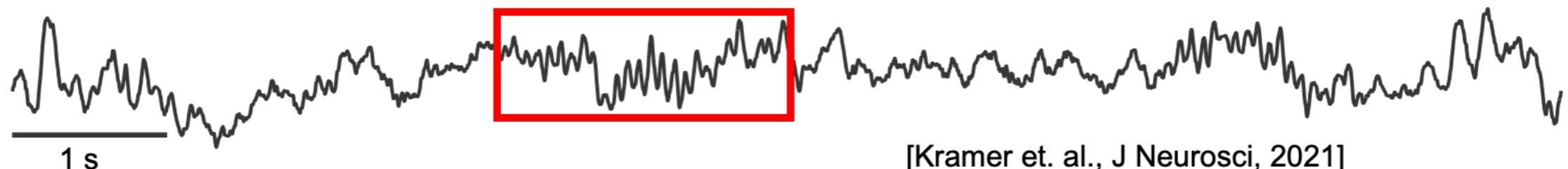
Function: Not completely understood.

In rats: learning and memory
location
motor behavior
sleep
emotional arousal
fear conditioning

Brain rhythms: alpha

Alpha: 8-12 Hz

Note: This band not in Slide #7 !



[Kramer et. al., J Neurosci, 2021]

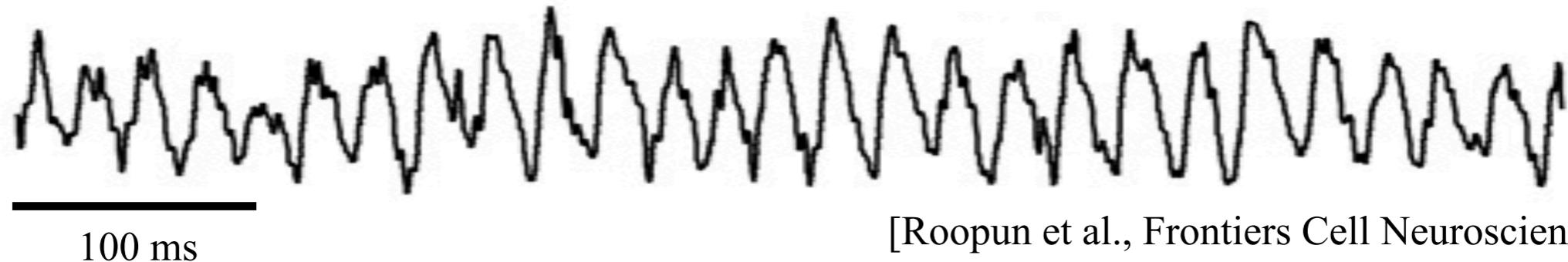
- The first EEG wave studies [Berger 1931]
- In EEG, strongest above occipital lobes when eyes closed at rest.

Function: “idling rhythm” - alert but still brain state
cortical operations in the absence of sensory inputs
disengagement of task-irrelevant brain areas

However, alpha also associated with attention,
sensory awareness.

Brain rhythms: beta

Beta: 12-30 Hz



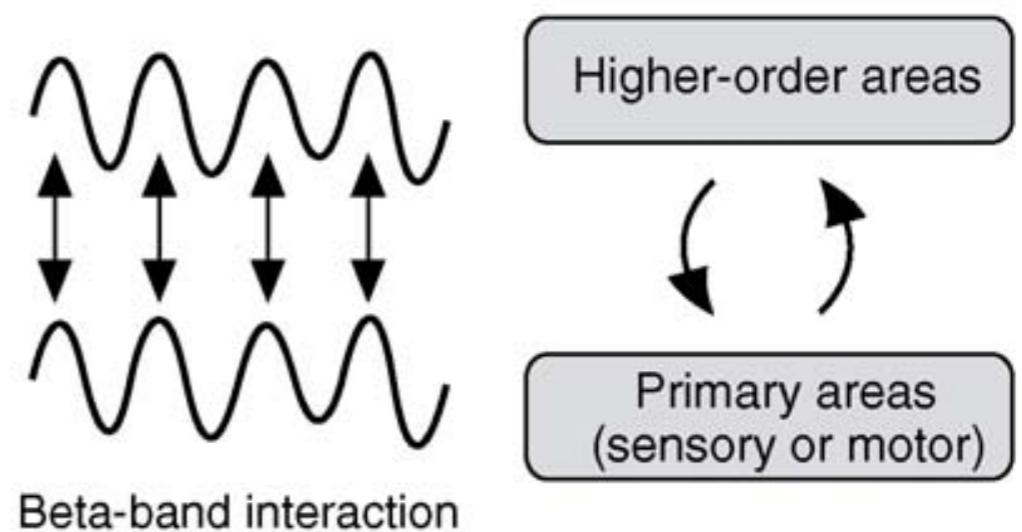
[Roopun et al., Frontiers Cell Neuroscience, 2008]

Function: Not fully understood.

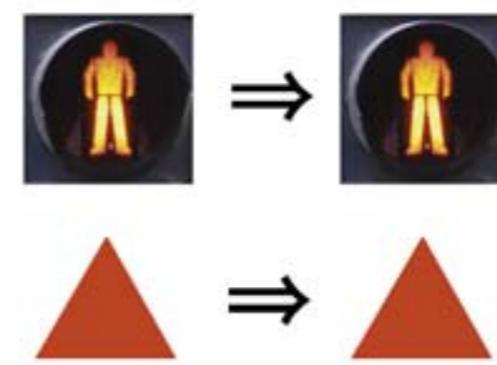
motor functions (e.g., steady-state contractions).

“Maintenance of the status quo”

“Couple” distant brain regions.



Beta-band interaction

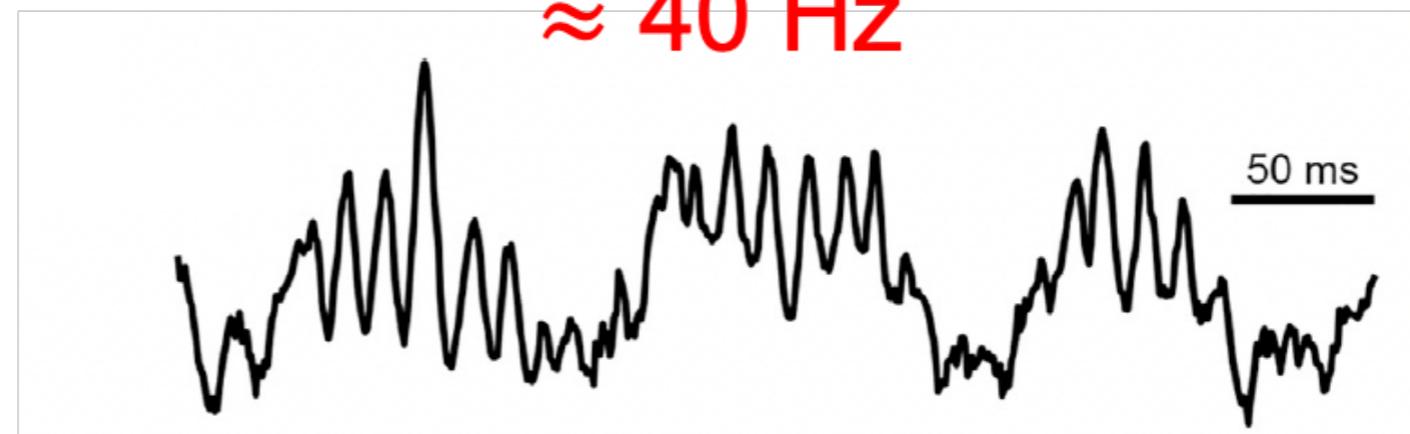


Intended
or expected
state transition

[Engel, Fries 2010]

Brain rhythms: gamma

Gamma: 30-50 Hz



[Fernandez-Ruiz et al., Neuron, 2023]

Function: Associated with a broad range of processes:
“binding”
attention
movement preparation
memory formation
conscious awareness

Note: Typically hard to see in EEG.

Q: Why?

Brain rhythms: Other bands

There are many other frequency bands . . .

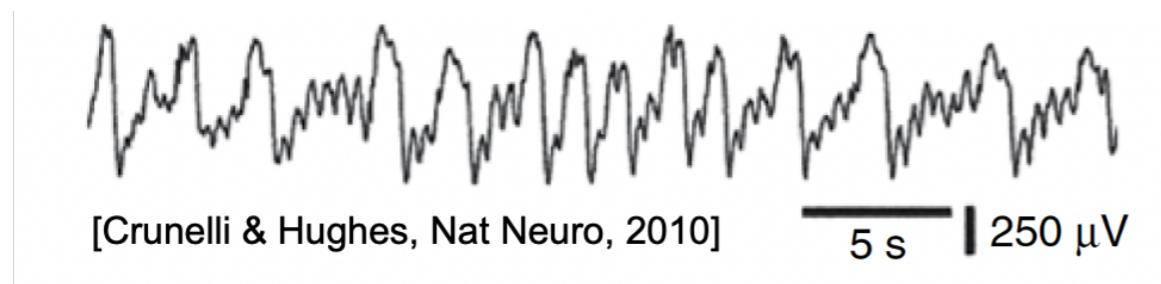
Slower

– **Delta:** 1-4 Hz

Sleep, learning, motivation

– **Slow cortical potential:** < 1 Hz

Emergence of consciousness?



Faster

– **High gamma:** 50-120 Hz

Coordination of neural activity

– **Ripples, HFO, UFO:** > 120 Hz

Replay of memories,
onset of seizures . . .



Brain rhythms in disease

Rhythms are sometimes associated with pathologies.

Ex: Seizure



[Martinet et al., Nat Comm, 2017]

Q: What rhythms do we see?

HFO Beta

Alpha

Theta

Delta

Q: How does the amplitude change?

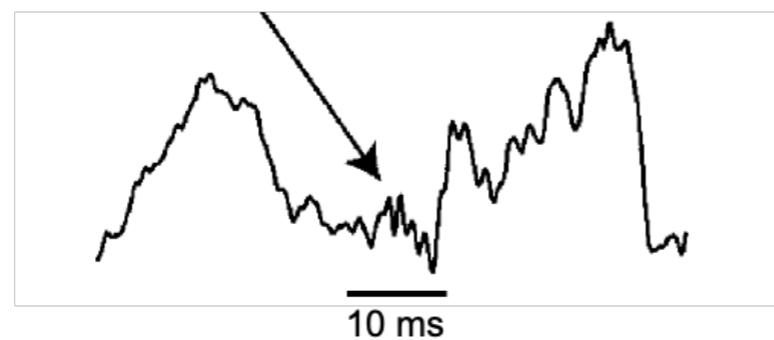
Note: Used the band labels, but “function” very different.

Brain rhythms in disease

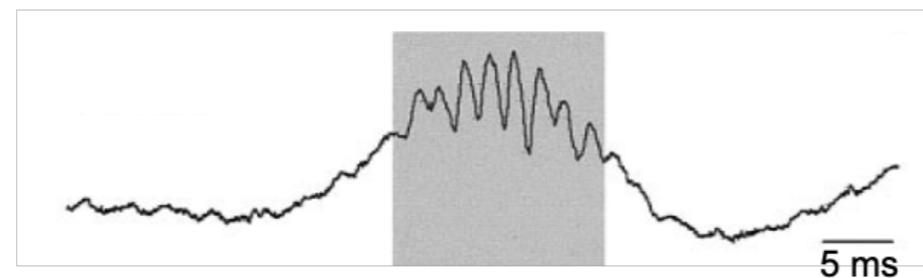
Rhythms are sometimes associated with pathologies.

Pathological ripples

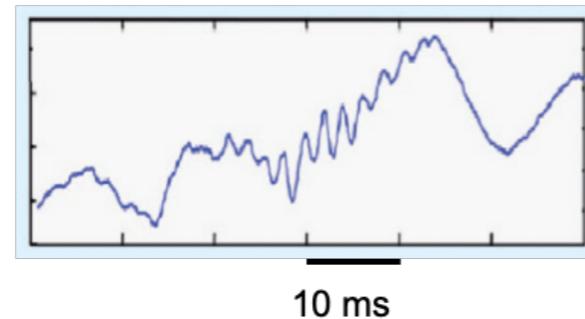
[Jacobs et al, 2012]



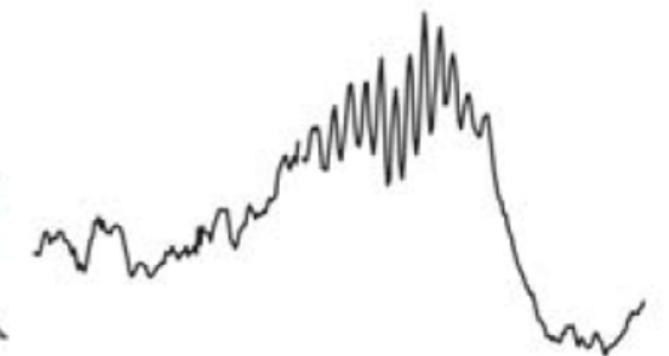
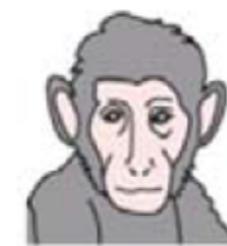
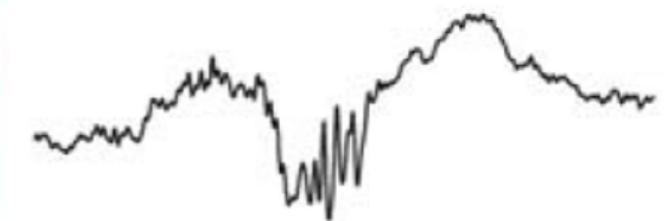
[Staba et al, 2002]



[Worell & Gotman, 2011]



Physiological ripples



[Buzsáki, Hippocampus, 2015]



Note: Used the band label, but “function” very different.

Brain rhythms are meaningless . . .

H: Brain rhythms are epiphenomena.

Large buildings: sway in the wind.

These oscillations are not performing a function, in fact they're unwanted.

Q: Is the same true in the brain?
Oscillations are an echo of some underlying function?

Q: Why so many oscillations?



Big questions

Q: Why do we observe rhythms in the brain?

- Functional role
- Epiphenomena

Q: What mechanisms support rhythms?

- Biological
- Dynamical

Q: Why do we observe different frequency bands, not a continuum?

Q: Why do rhythms interact?

- Mechanisms
- Functions
- Measures

We need answers to these questions.
Data analysis and models ...

Characterize brain rhythms

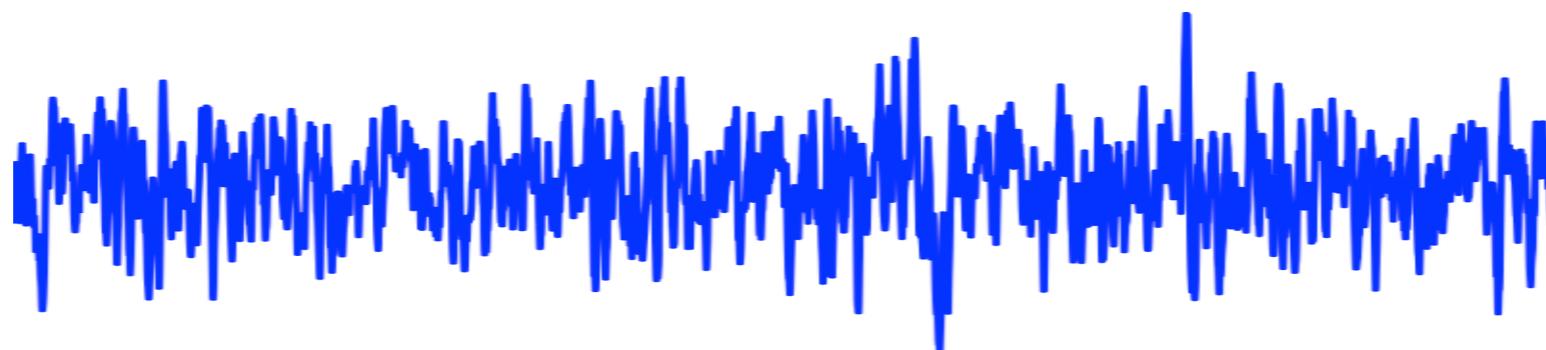
Many sophisticated tools to do so.

Today, consider two:

- Visual inspection
- Intuition for the spectrum

Idea:

Visual inspection: Plot the data. What do you see?



Spectrum: Break down the data into sinusoids . . .

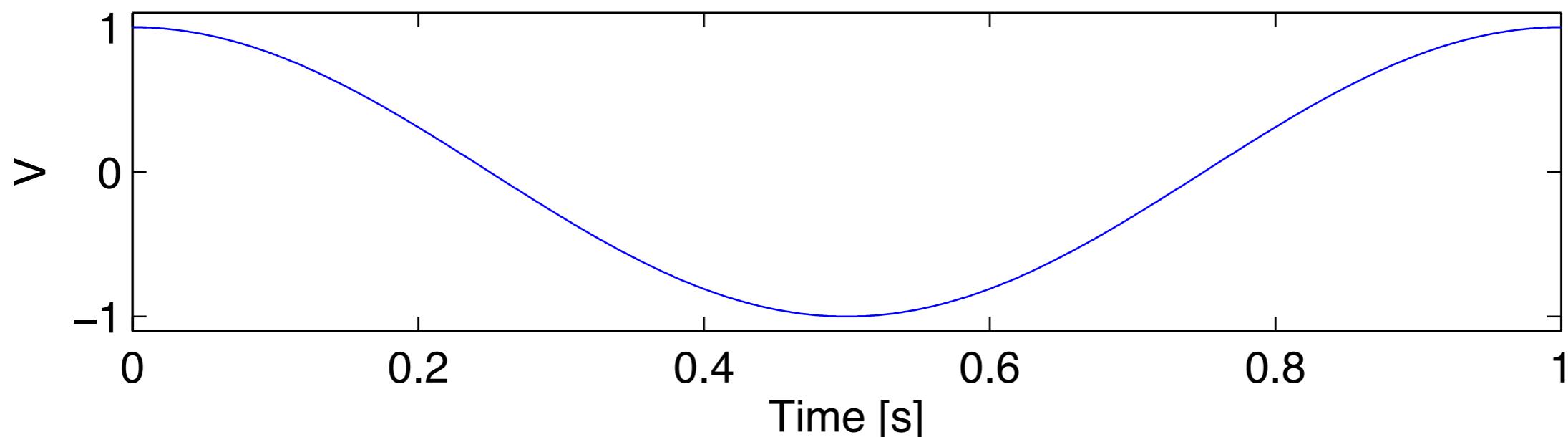
Remember: sinusoids . . .

$$V[t] = A \cos(2\pi f t)$$

Voltage as a function of time Amplitude Frequency [Hz] Time [s]

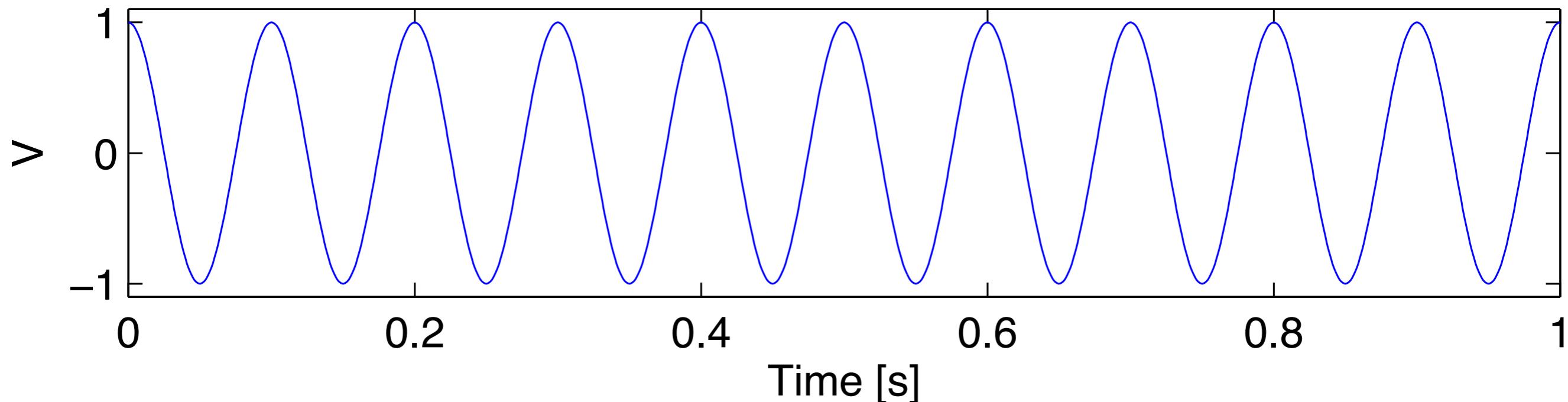
Ex. Consider: $f = 1$ Hz

Q: What does it look like?



Remember: sinusoids . . .

Q: What is the frequency of this sinusoid?



A: 10 cycles in 1 second, so 1 Hz.

Note: Visual inspection is often useful.

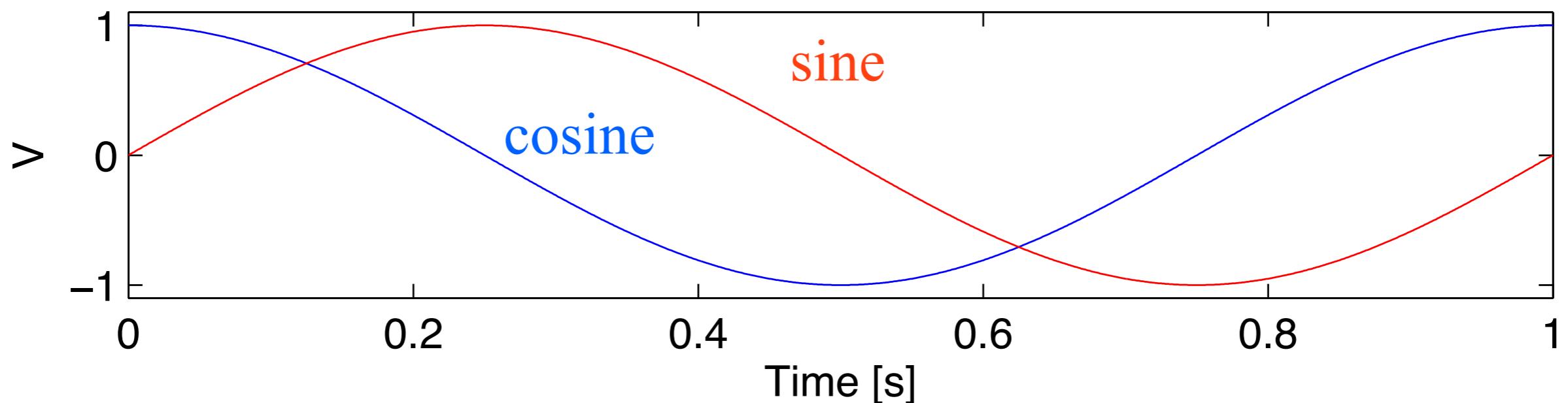
Remember: sinusoids . . .

In addition to cosine, there's also sine:

$$V[t] = B \sin(2\pi ft)$$

Voltage as a function of time Amplitude Frequency [Hz] Time [s]

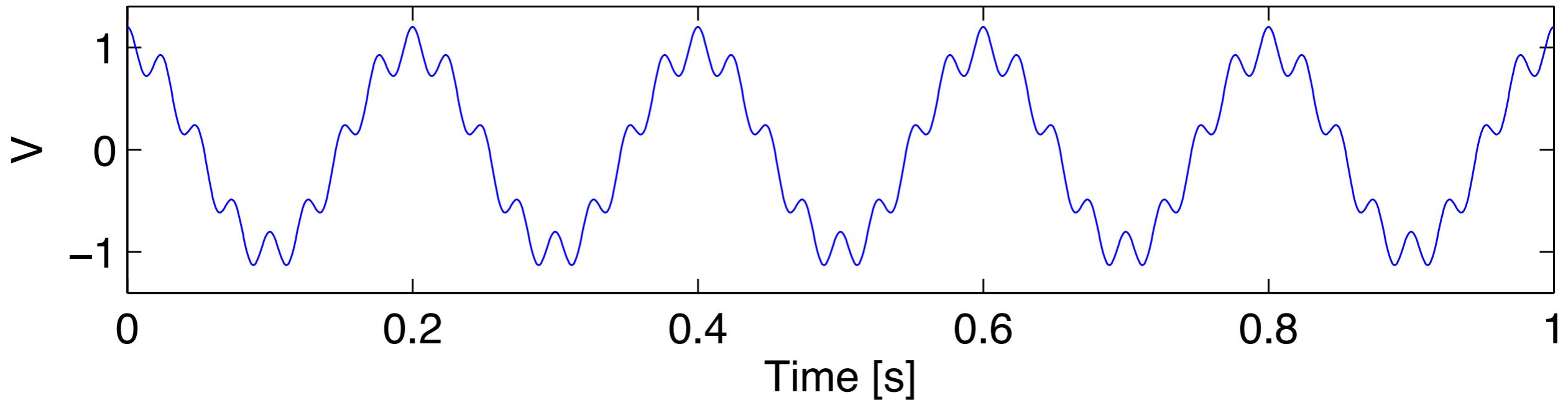
Ex. Consider: $f = 1$ Hz



Q: What's the difference?

Example: rhythmic signal

Consider the signal below:



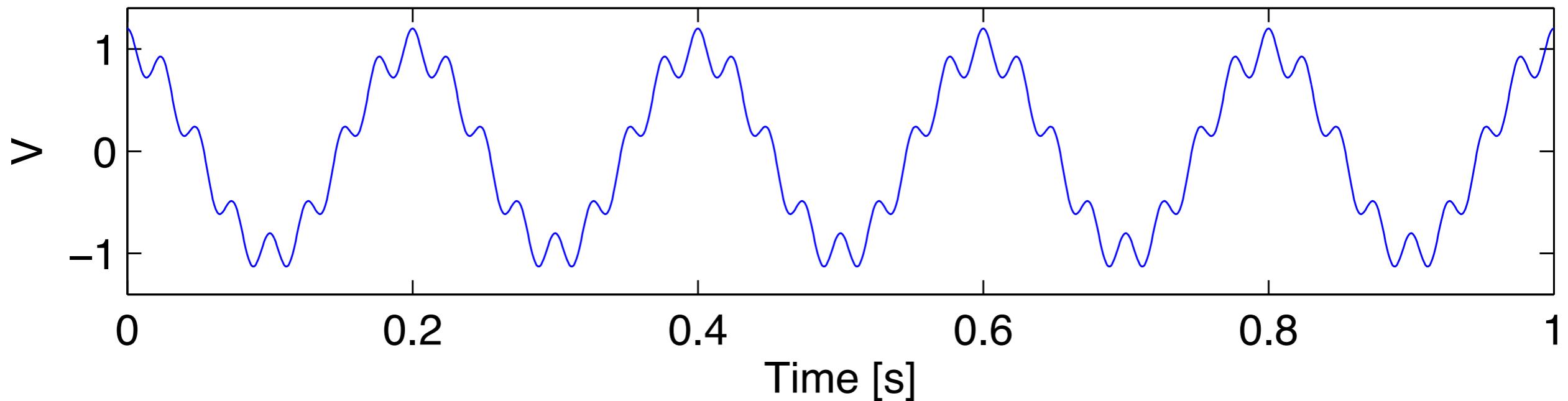
Q: What are the rhythms?

A: Apply visual inspection . . . Slow and fast
 5 Hz 40 Hz

Q: What has larger amplitude?

Example: rhythmic signal

So, we can represent this signal . . .



. . . as the sum of two sinusoids:

A slow, large amplitude sinusoid + a fast, small amplitude sinusoid

$$V[t] = A_1 \cos(2\pi f_1 t) + A_2 \cos(2\pi f_2 t)$$

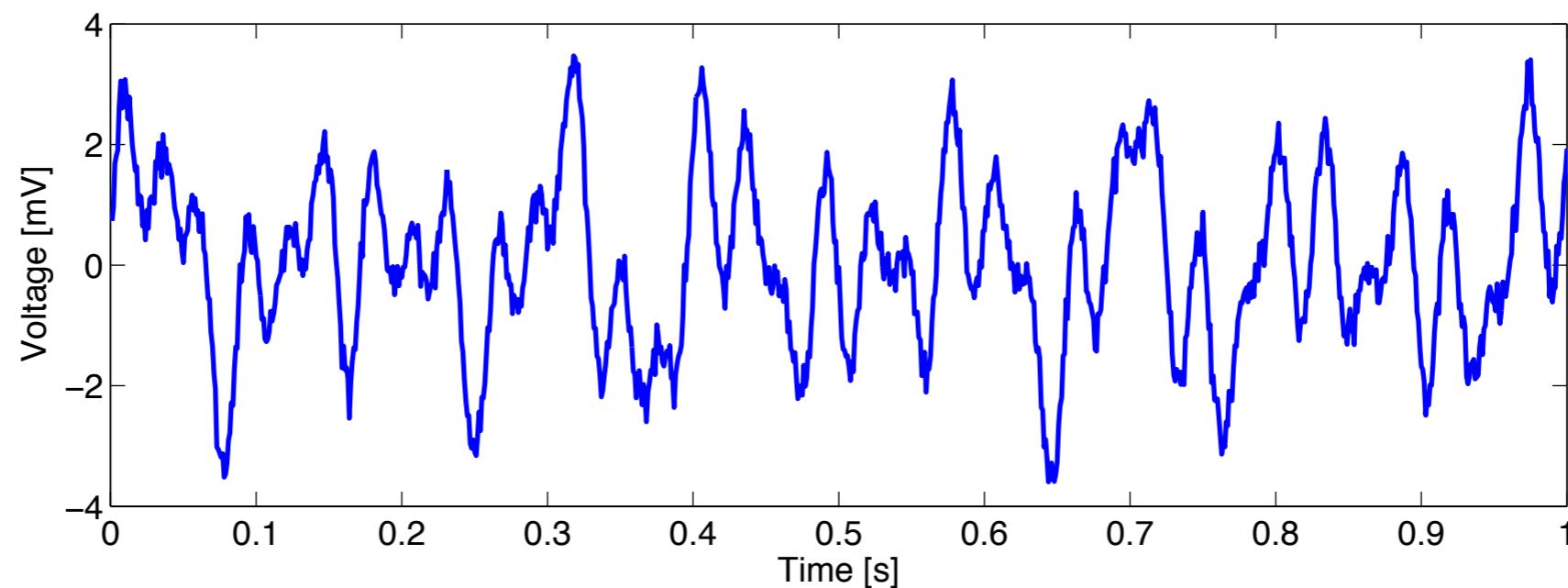
1.0 5 Hz 0.1 40 Hz

We get a simpler representation of the signal. That's the idea of the spectrum.

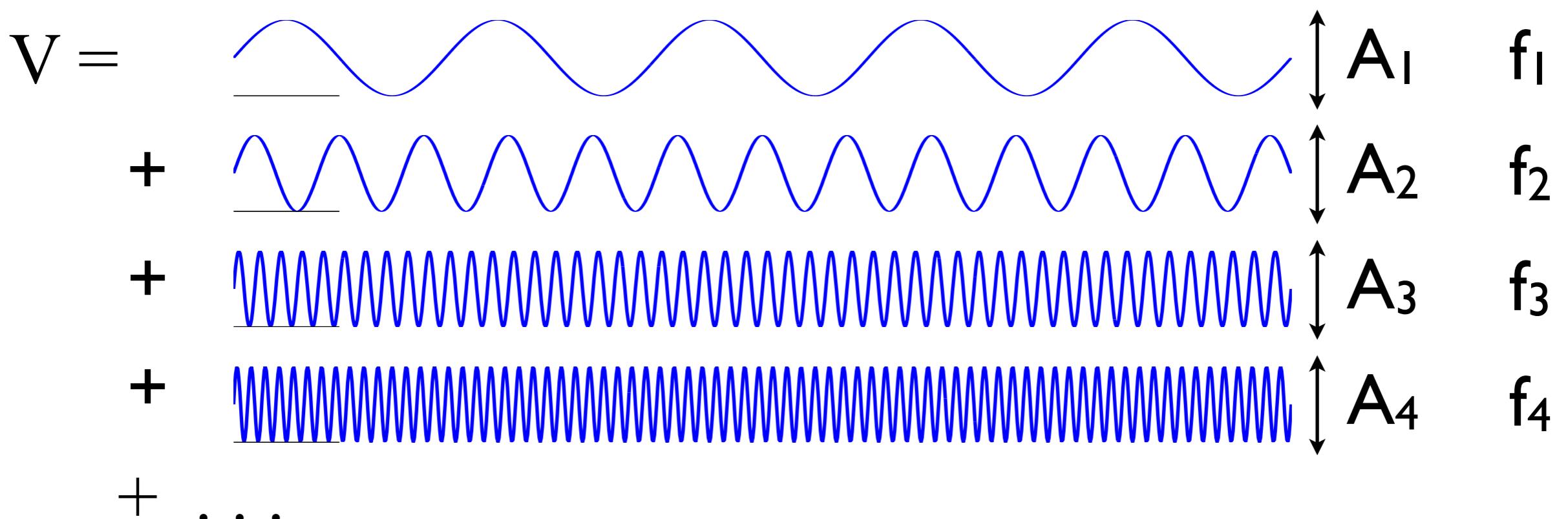
Idea: Spectrum

Consider:

$$V =$$



- Decompose signal into oscillations at different frequencies.



Represent V as a sum of sinusoids (e.g., part 7 Hz, part 10 Hz, . . .)

Idea: Spectrum

So, in equations:

$$V[t] = A_1 \cos(2\pi f_1 t) + B_1 \sin(2\pi f_1 t) + A_2 \cos(2\pi f_2 t) + B_2 \sin(2\pi f_2 t) + \dots$$

↑ ↑ ↑ ↑
amplitude frequency amplitude frequency

Or, more generally:

$$V[t] = \sum_j A_j \cos(2\pi f_j t) + B_j \sin(2\pi f_j t)$$

↑ ↑ →
 j amplitude oscillation at
sum over many frequencies frequency f_j

Note: A_j and B_j can be zero.
(some rhythms make no contribution to $V[t]$)

Note: A_j and B_j are large when f_j is a good match to the data.

Idea: Spectrum

Note: Think of sine & cosine as accounting for **phase**.

$$C_j \cos(2\pi f_j t + \phi_j)$$

↑ ↑ ↑
amplitude freq phase

Aside: $\cos(a + b) = \cos(a)\cos(b) - \sin(a)\sin(b)$

$$= C_j \cos(2\pi f_j t) \boxed{\cos(\phi_j)} - C_j \sin(2\pi f_j t) \boxed{\sin(\phi_j)}$$

A_j B_j

$$= \boxed{A_j} \cos(2\pi f_j t) + \boxed{B_j} \sin(2\pi f_j t)$$

Decompose $V[t]$ into sine/cosine or amplitude/phase.

Idea: Spectrum

Q: How do we find A_j and B_j ?

$$V[t] = \sum_j A_j \cos(2\pi f_j t) + B_j \sin(2\pi f_j t)$$

A: Consider A_j and use **orthogonality of sinusoids**.

$$\int_0^T \cos(2\pi f_j t) \cos(2\pi f_k t) dt = \begin{cases} 0 & \text{if } f_j \neq f_k \\ T/2 & \text{if } f_j = f_k \end{cases}$$

Choose T so f_j and f_k complete an integer number of cycles.

integrate over time

Choose T so f_j and f_k complete an integer number of cycles.

integrate over time

Idea: Spectrum

Python

Idea: Spectrum

Q: How do we find A_j and B_j ?

$$V[t] = \sum_j A_j \cos(2\pi f_j t) + B_j \sin(2\pi f_j t)$$

A: Consider A_j and use **orthogonality of sinusoids**.

$$\int_0^T \cos(2\pi f_j t) \sin(2\pi f_k t) dt = 0 \quad \text{for all } f_j, f_k$$


sine

Idea: Spectrum

Return to our original equation

$$V[t] = \sum_j A_j \cos(2\pi f_j t) + B_j \sin(2\pi f_j t)$$

Task: find A_j, B_j

Pick frequency f_k , multiply both sides by $\cos(2\pi f_k t)$, and integrate over time ...

$$\int_0^T V[t] \cos(2\pi f_k t) dt = \int_0^T \sum_j A_j \cos(2\pi f_j t) \cos(2\pi f_k t) dt$$
$$+ \int_0^T \sum_j B_j \sin(2\pi f_j t) \cos(2\pi f_k t) dt$$

Consider each integral ...

Idea: Spectrum

by orthogonality

$$\int_0^T \sum_j A_j \cos(2\pi f_j t) \cos(2\pi f_k t) dt = 0 \text{ if } f_j \neq f_k, \text{ or } T/2 \text{ if } f_j = f_k$$

$$\int_0^T \sum_j B_j \sin(2\pi f_j t) \cos(2\pi f_k t) dt = 0$$

$A_k T/2$ if $j = k$, 0 otherwise

$$\text{So } \int_0^T V[t] \cos(2\pi f_k t) dt = \int_0^T \sum_j A_j \cos(2\pi f_j t) \cos(2\pi f_k t) dt$$

$$+ \int_0^T \sum_j B_j \sin(2\pi f_j t) \cos(2\pi f_k t) dt$$

0

$$= A_k T/2$$

Idea: Spectrum

$$\int_0^T V[t] \cos(2\pi f_k t) dt = A_k T/2$$

Solve for A_k

$$A_k = \frac{2}{T} \int_0^T V[t] \cos(2\pi f_k t) dt$$

We've solved for amplitude A_k

Depends on observed data $V[t]$ multiplied by cosine we choose (f_k)

Idea: Spectrum

Return to our original equation

$$V[t] = \sum_j A_j \cos(2\pi f_j t) + B_j \sin(2\pi f_j t)$$

Q: How do we find A_j and B_j ?

A: Consider A_j and use **orthogonality of sinusoids**.

Similarly

$$A_k = \frac{2}{T} \int_0^T V[t] \cos(2\pi f_k t) dt$$

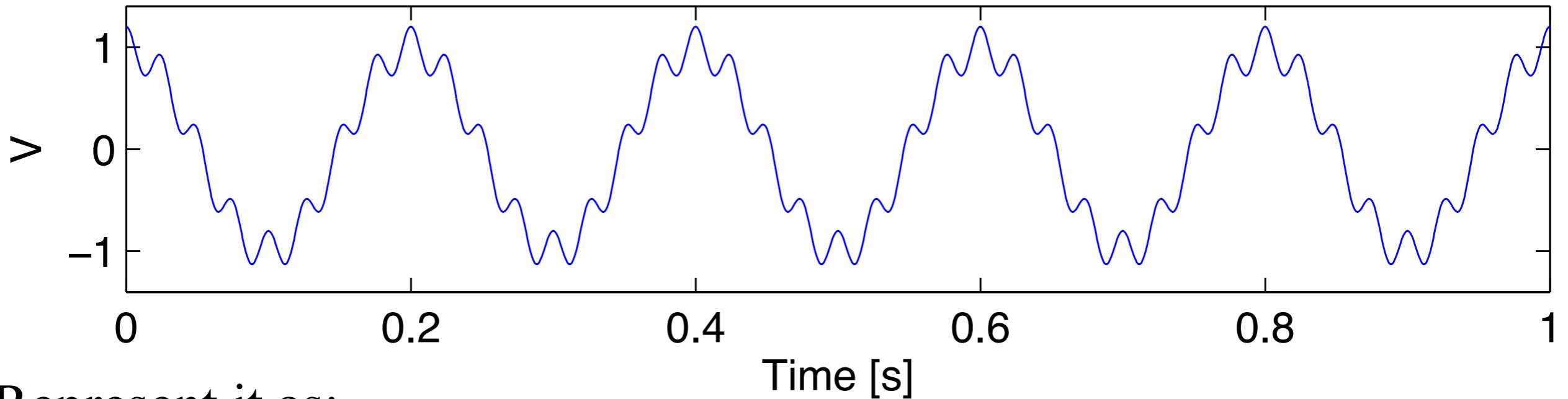
$$B_k = \frac{2}{T} \int_0^T V[t] \sin(2\pi f_k t) dt$$

Big idea: We can decompose $V[t]$ into a sum of sin/cos functions, and we have a strategy to find the amplitudes A_j, B_j

Example: rhythmic signal

Q: So what?

A: Represent $V[t]$ in a simpler way ... remember:



Represent it as:

$$V[t] = A_1 \cos(2\pi f_1 t) + A_2 \cos(2\pi f_2 t)$$

1.0 5 Hz 0.1 40 Hz

To represent $V[t]$ we need 4 numbers:

Amplitudes = {1, 0.1}

Frequencies = {5, 40} Hz

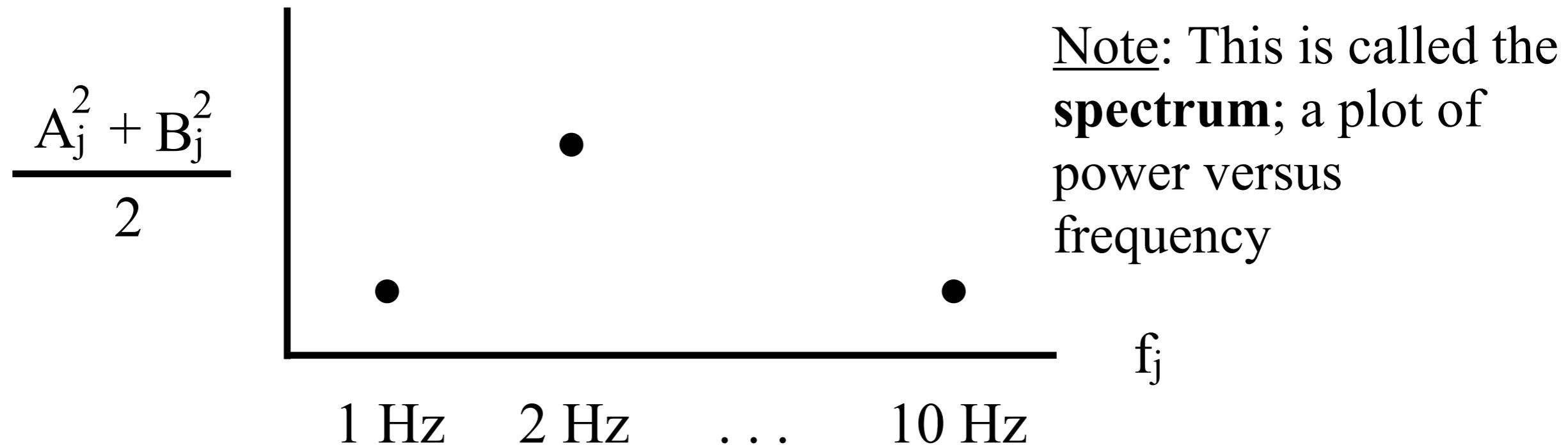
These 4 numbers completely summarize the data.

Plot: Spectrum

We can represent these amplitudes and frequencies graphically:

Plot: $\frac{A_j^2 + B_j^2}{2}$ versus f_j for each j

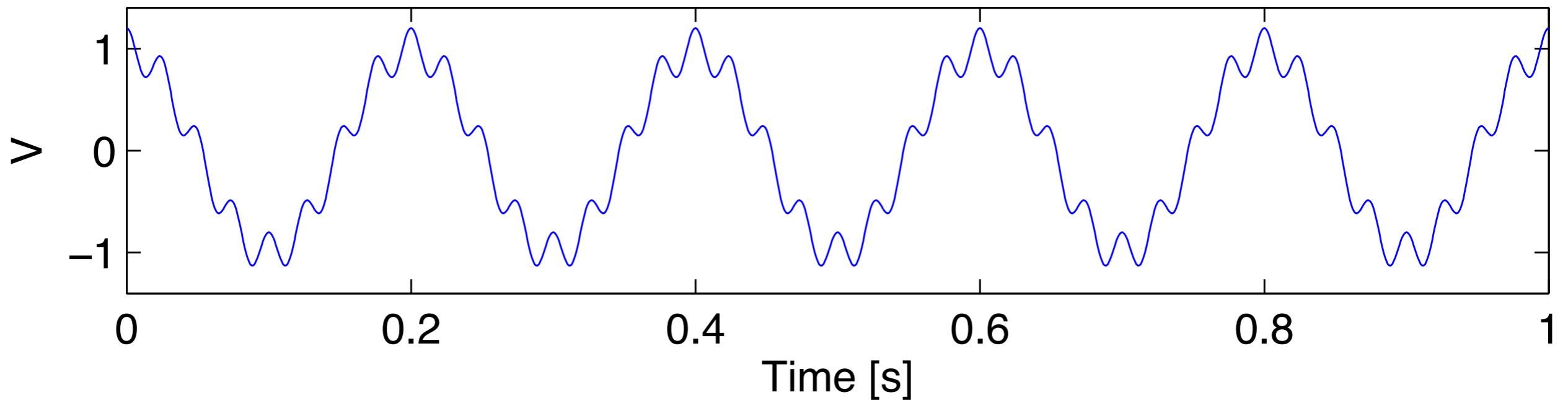
Note: The summed amplitudes squared.
Called the “power”



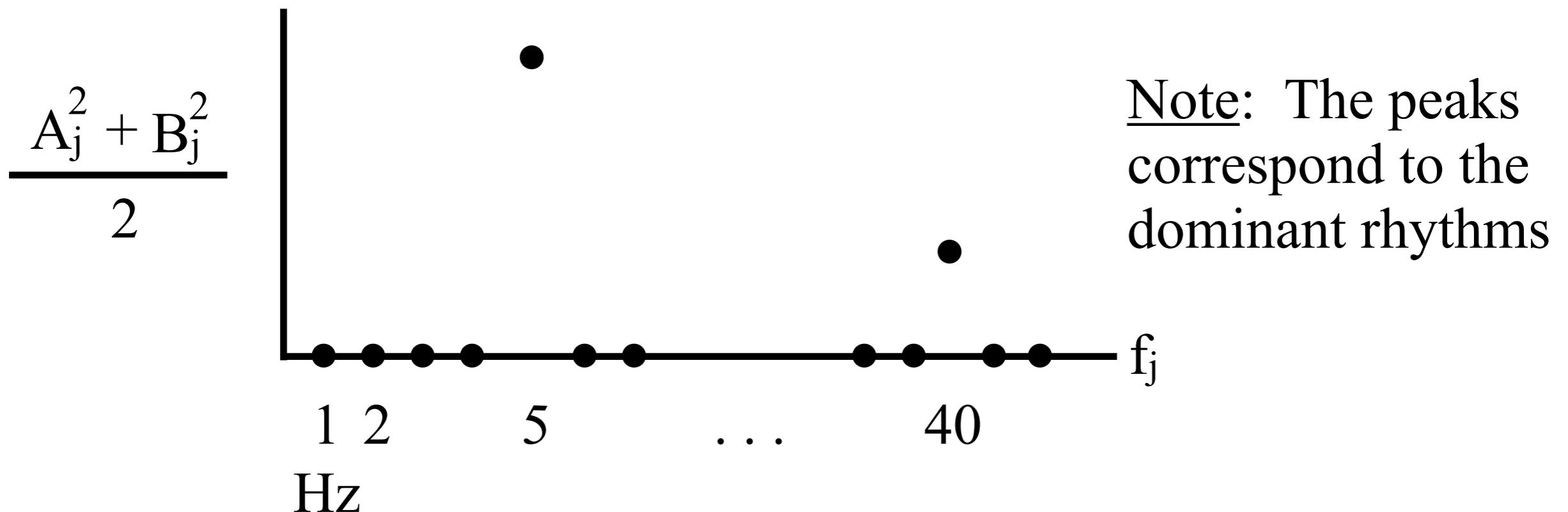
The peaks represent the dominant rhythms in the signal.

Example: rhythmic signal

Ex:



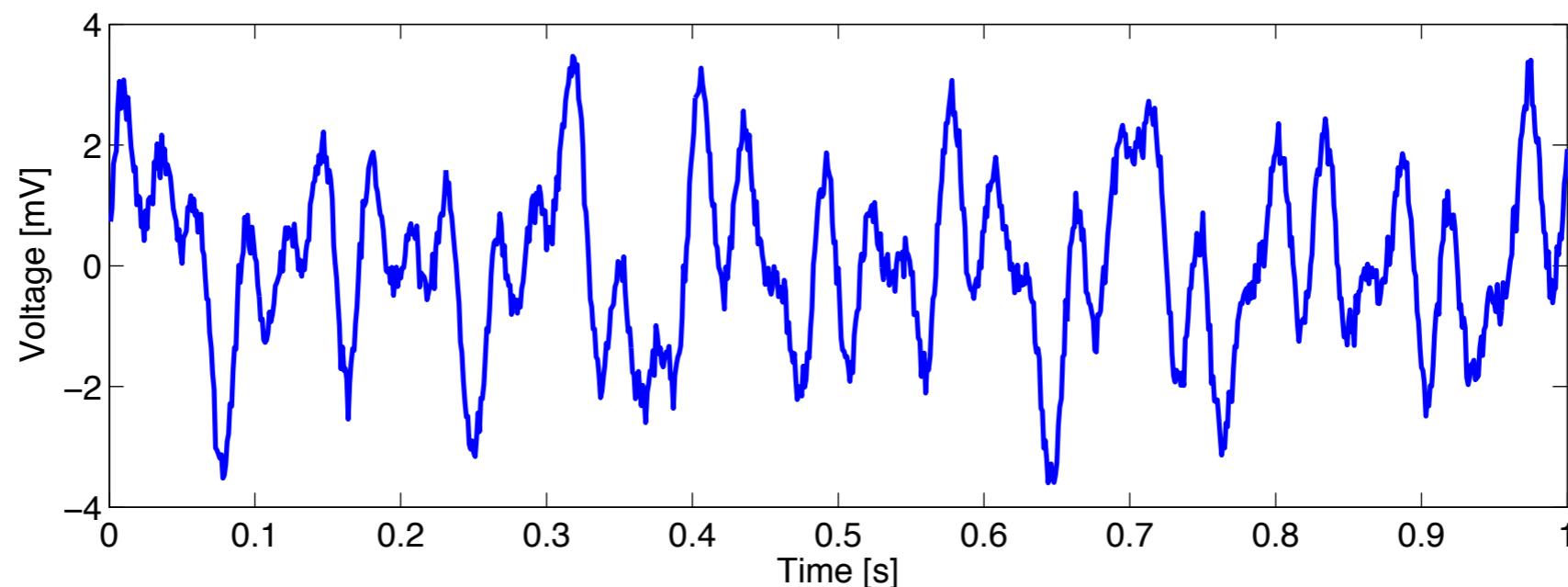
Plot the spectrum:



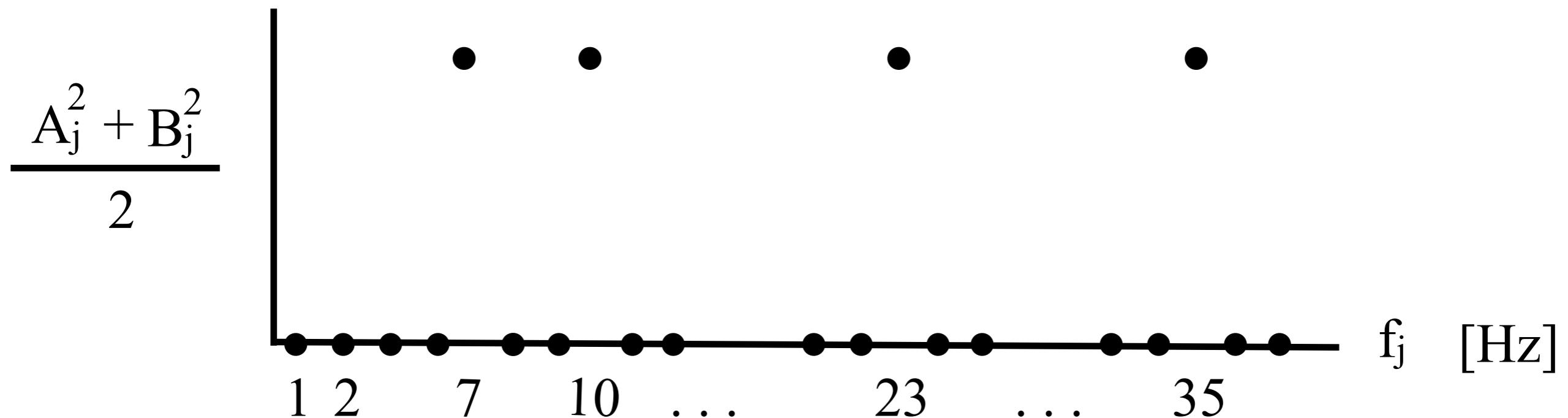
Example: rhythmic signal

Ex.

$V =$



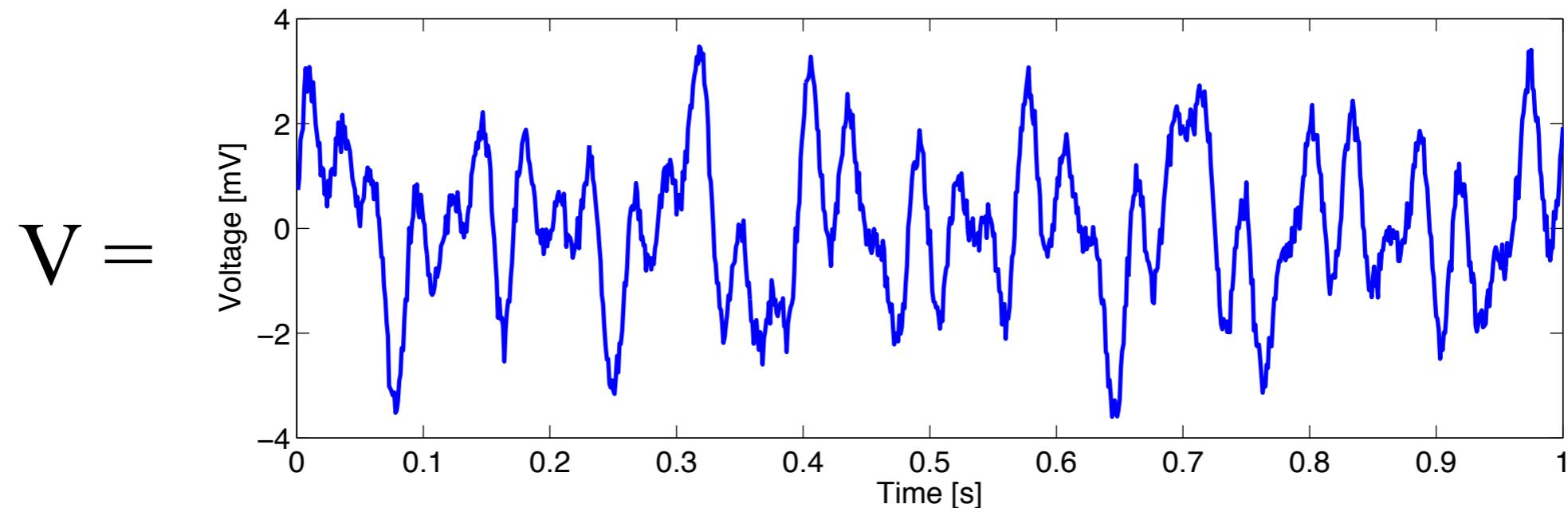
Note: It's complicated Plot the spectrum:



Q: What's happening here?

Example: rhythmic signal

So, by computing the power spectrum, we find the complicated signal:



We find it's the sum of 4 sinusoids at frequencies:

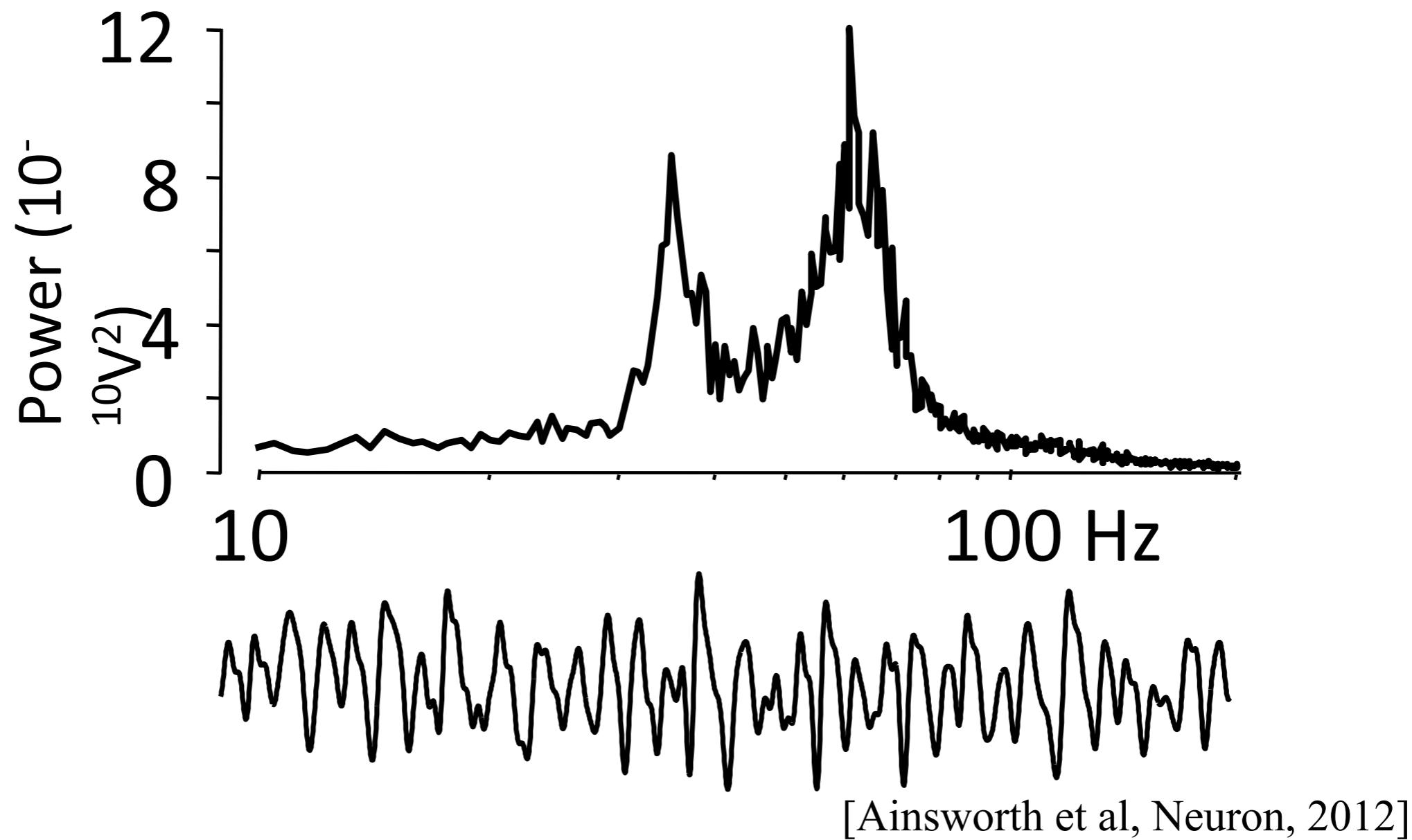
7 Hz, 10 Hz, 23 Hz, and 35 Hz

A much simpler representation of brain activity.

Example: Real world

Q: What does the power spectrum of real-world brain signals look like?

Ex. From a slice of rat cortex:



Q: What rhythms are dominant?

Next

Practical notions ...

A simple answer to one big rhythm question ...