

# The gamma rhythms

Instructor: Mark Kramer

# Today

Models of the gamma rhythms

# Gamma rhythms

30-80 Hz

## functions

### - cell-assembly formation / synchronization

[Womelsdorf et al. "Modulation of Neuronal Interactions Through Neuronal Synchronization." Science , 2007]

[Fernández-Ruiz et al., "Gamma Rhythm Communication between Entorhinal Cortex and Dentate Gyrus Neuronal Assemblies.", Science, 2021]

[Canolty et al., "High Gamma Power Is Phase-Locked to Theta Oscillations in Human Neocortex.", Science, 2006]

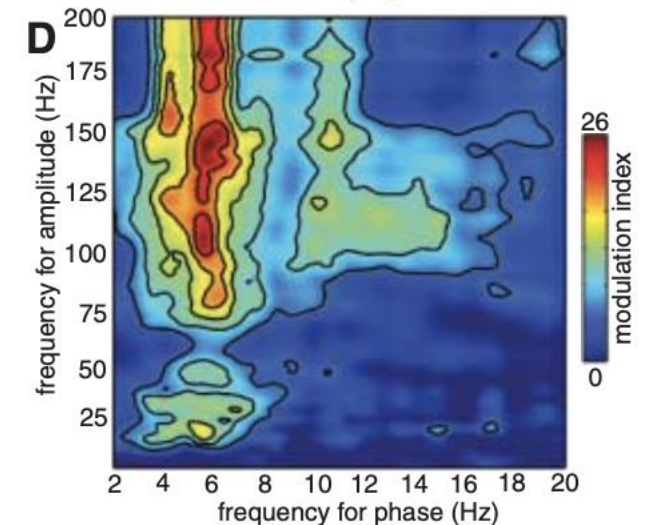
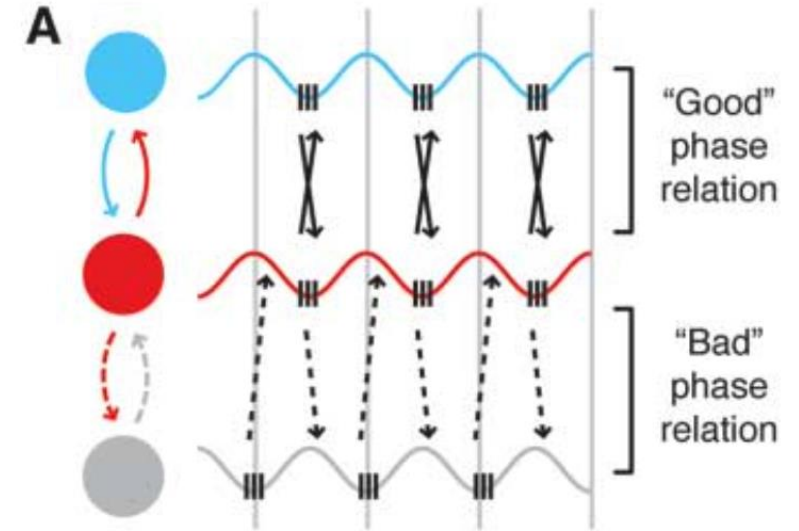
### - memory

[Lisman & Idiart. "Storage of  $7 \pm 2$  Short-Term Memories in Oscillatory Subcycles." Science, 1995]

[Lundqvist et al., "Gamma and Beta Bursts Underlie Working Memory." Neuron, 2016]

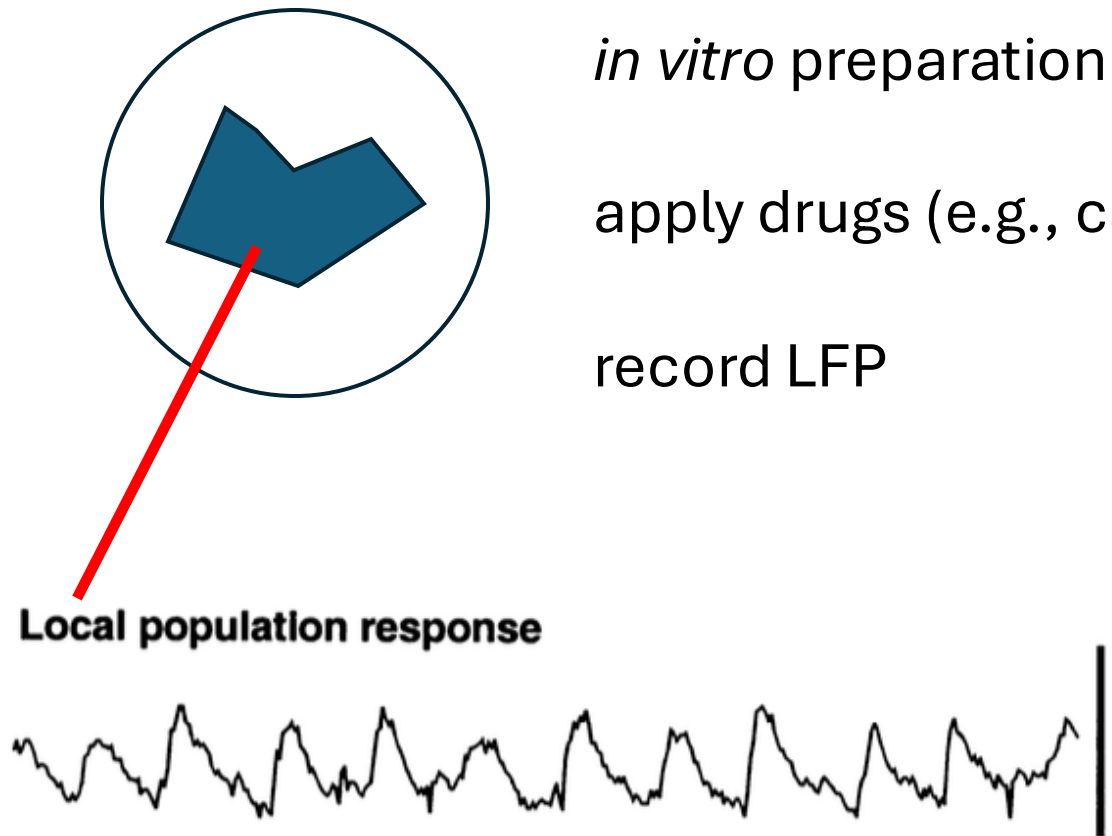
### - plasticity

[Hadler et al, "Gamma Oscillation Plasticity Is Mediated via Parvalbumin Interneurons." Science Advances, 2024]



# Gamma rhythms

## Mechanisms (via experimental models)



*in vitro* preparation

apply drugs (e.g., carbachol to increase excitability)

record LFP

### Facts

- Block GABA<sub>A</sub> → eliminate gamma
- Block AMPA → eliminate gamma

involves ex & inh cells + synaptic interactions

# Gamma rhythms

## Mechanisms (via experimental models)

### More Facts

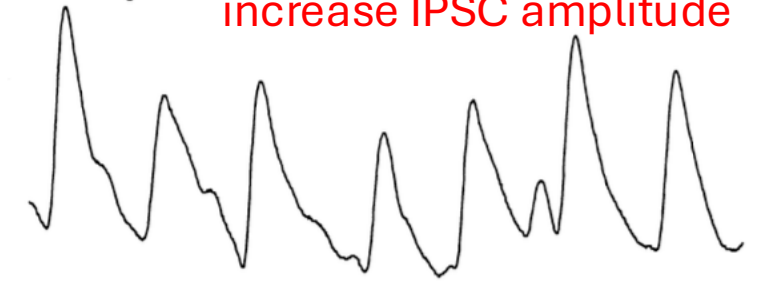
- rhythm frequency depends on GABA<sub>A</sub> kinetics (e.g., modulate with sedatives to alter period)
- pyramidal (ex) cells can fire sparsely
- basket (inh) cells fire on most cycles

Normal



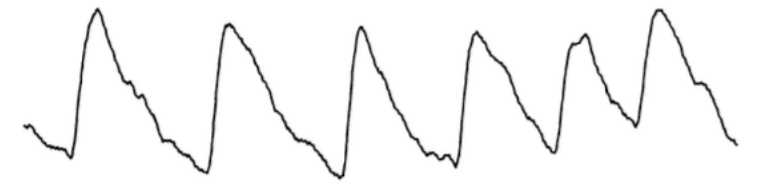
Diazepam

increase IPSC amplitude



Thiopental

increase IPSC decay kinetics



morphine

decrease IPSC amplitude



100 ms

# Gamma rhythms

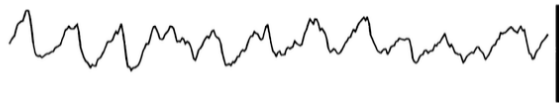
## Mechanisms (via experimental models)

Local population response

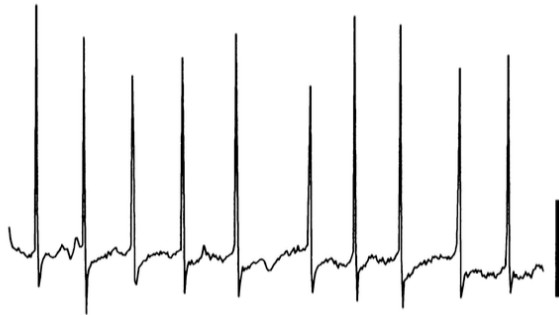


pyramidal (ex) cells don't spike

Excitatory neuron

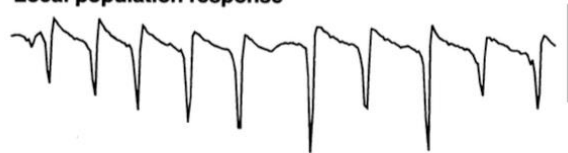


Interneuron



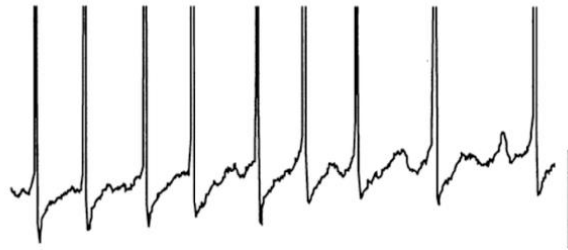
100 ms

Local population response

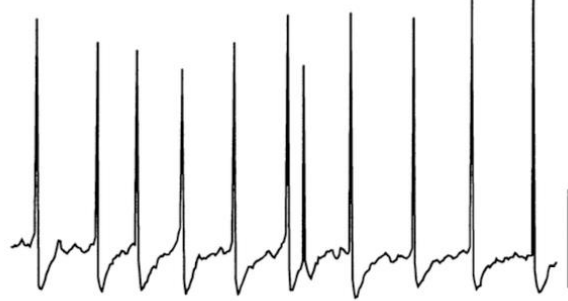


pyramidal (ex) cells always spike

Excitatory neuron



Interneuron



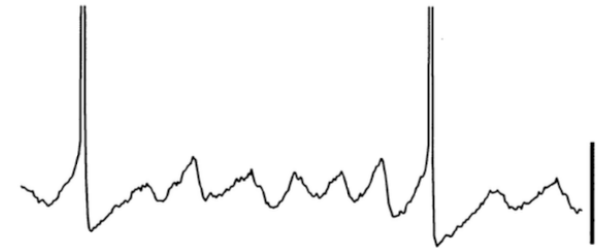
100 ms

Local population response

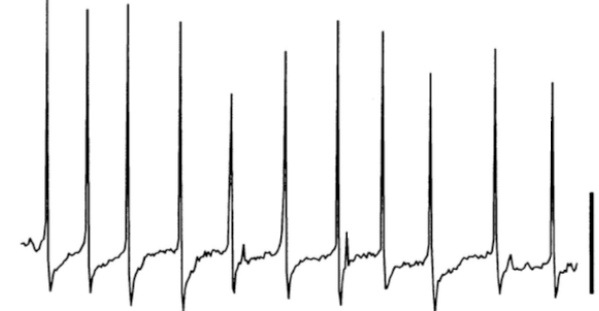


pyramidal (ex) cells sometimes spike

Excitatory neuron



Interneuron

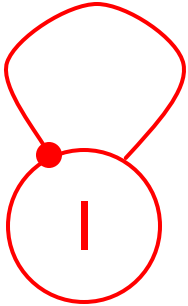


100 ms

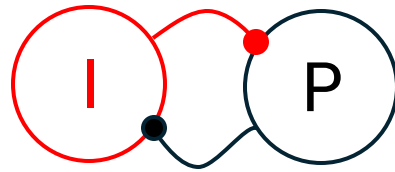
# Models

## Three types

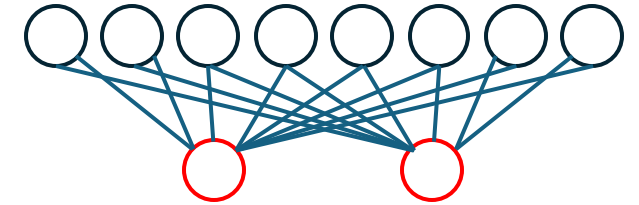
ING



PING



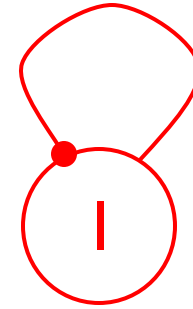
sparse  
PING



ING

Interneuron **N**etwork **G**amma

ING





# ING

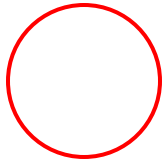
## Interneuron Network Gamma

### Experimental observations

- (1) Excitation (driven cells)
- (2) GABA<sub>A</sub> critical
- (3) Altering GABA<sub>A</sub> kinetics changes frequency

### Model

1 cell



Load with standard HH currents

$$\frac{dV}{dt} = I_{Na} + I_K + I_L + I_{inj}$$

To mimic (1)

make  $I_{inj}$  large → depolarize neuron → fast spiking

# ING

## Interneuron Network Gamma

### Experimental observations

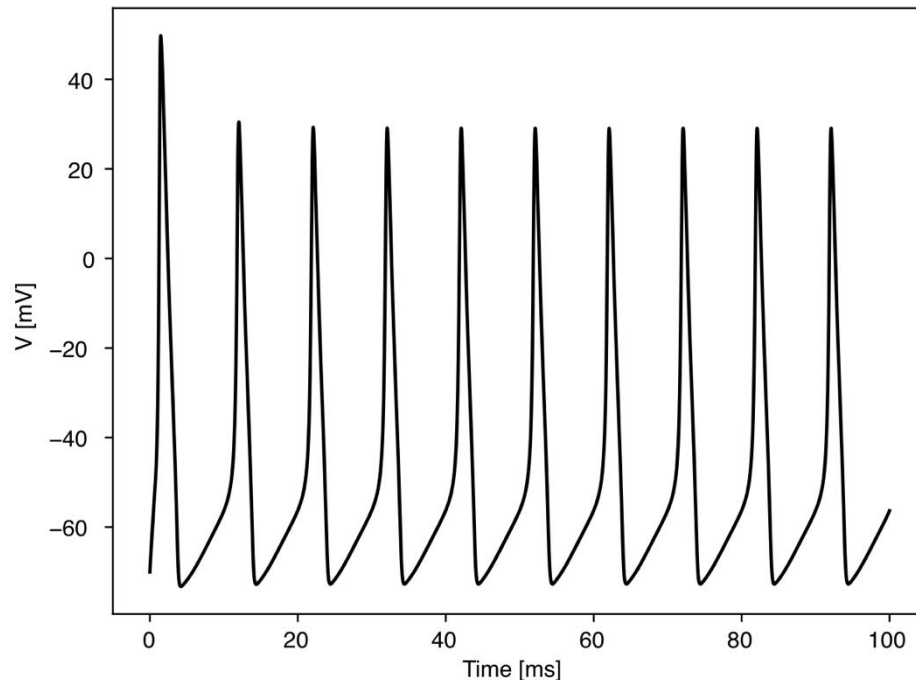
(1) Excitation (driven cells)

(2) GABA<sub>A</sub> critical

(3) Altering GABA<sub>A</sub> kinetics changes frequency

**To mimic (1)**      make  $I_{inj}$  large  $\rightarrow$  depolarize neuron  $\rightarrow$  fast spiking

Ex.  $I_{inj} = 30$



**Q.** What sets the timescale of spiking?

**A.** Dynamics of intrinsic currents (Na, K)

# ING

## Interneuron Network Gamma

### Experimental observations

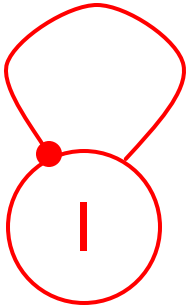
(1) Excitation (driven cells)

(2) GABA<sub>A</sub> critical

(3) Altering GABA<sub>A</sub> kinetics changes frequency

**To mimic (2)**

add an inhibitory synapse



**autapse** (presynaptic neuron = postsynaptic neuron)

**Q.** Realistic?

Then

$$\frac{dV}{dt} = I_{Na} + I_K + I_L + I_{inj} + I_{synapse}$$

# ING

## Interneuron Network Gamma

$$\frac{dV}{dt} = I_{Na} + I_K + I_L + I_{inj} + I_{synapse}$$

### Synaptic current

$$I_{synapse} = g_I s_I (E_I - V)$$

maximal  
conductance

inh. synapse gate

equilibrium voltage  
for inh. synapse (-80 mV)

neuron voltage

### Experimental observations

(1) Excitation (driven cells)

(2) GABA<sub>A</sub> critical

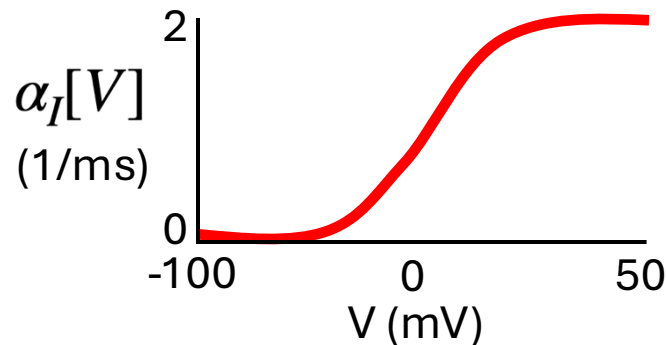
(3) Altering GABA<sub>A</sub> kinetics changes frequency

### Synaptic gate dynamics

$$\frac{ds_I}{dt} = \alpha_I[V](1 - s_I) - \beta_I[V]s_I$$

forward rate fxn

backward rate fxn



$$\beta_I[V] = \beta_I = \frac{1}{\tau_d}$$

constant

decay time  $\approx 10$  ms

# ING

## Interneuron Network Gamma

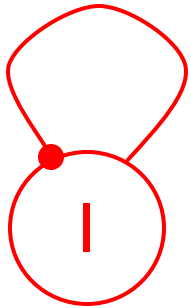
### Experimental observations

(1) Excitation (driven cells)

(2) GABA<sub>A</sub> critical

(3) Altering GABA<sub>A</sub> kinetics changes frequency

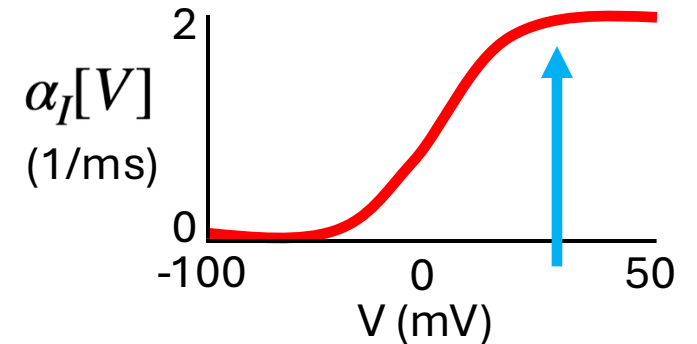
$$\frac{ds_I}{dt} = \alpha_I[V](1 - s_I) - \beta_I[V]s_I$$



**Q.** What happens?

- neuron spikes ( $V > 0$ )
- $\alpha_I[V] \rightarrow 2$
- $s_I \rightarrow 1$  (open)
- Chlorine ( $\text{Cl}^-$ ) flows in  $\rightarrow$  hyperpolarize cell (push to -80 mV)

Note:  $[\text{Cl}^-]_{\text{out}} \gg [\text{Cl}^-]_{\text{in}}$



# ING

## Interneuron Network Gamma

### Experimental observations

- (1) Excitation (driven cells)
- (2) GABA<sub>A</sub> critical
- (3) Altering GABA<sub>A</sub> kinetics changes frequency

### Model

$$C \frac{dV}{dt} = I_{\text{input}}(t) - \bar{g}_K n^4 (V - V_K) - \bar{g}_{\text{Na}} m^3 h (V - V_{\text{Na}}) - \bar{g}_L (V - V_L) - g_I s_I (V - E_I)$$

$$\frac{dn}{dt} = -\frac{n - n_{\infty}(V)}{\tau_n(V)}$$

$$\frac{dm}{dt} = -\frac{m - m_{\infty}(V)}{\tau_m(V)}$$

$$\frac{dh}{dt} = -\frac{h - h_{\infty}(V)}{\tau_h(V)}$$

$$\frac{ds_I}{dt} = \alpha_I[V](1 - s_I) - \beta_I[V]s_I$$

5 variables

5 differential equations

# ING

Interneuron Network Gamma

Experimental observations

(1) Excitation (driven cells)

(2) GABA<sub>A</sub> critical

(3) Altering GABA<sub>A</sub> kinetics changes frequency

Q. How does it work?

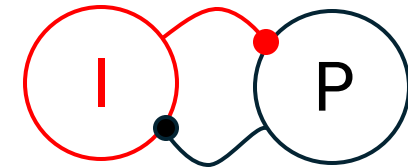
*Python*

# PING

START ZOOM

**P**yramidal **I**nterneuron **N**etwork **G**amma

PING





# PING

Using ING

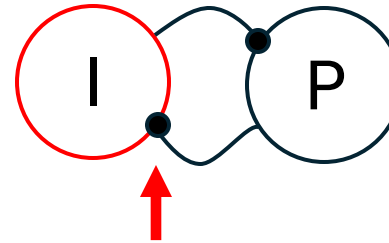
Experimental observations

- ✓ (1) Excitation (driven cells)
- ✓ (2) GABA<sub>A</sub> critical
- ✓ (3) Altering GABA<sub>A</sub> kinetics changes frequency
- ✗ (4) AMPA critical

New model

+ include excitatory (pyramidal) cell

PING

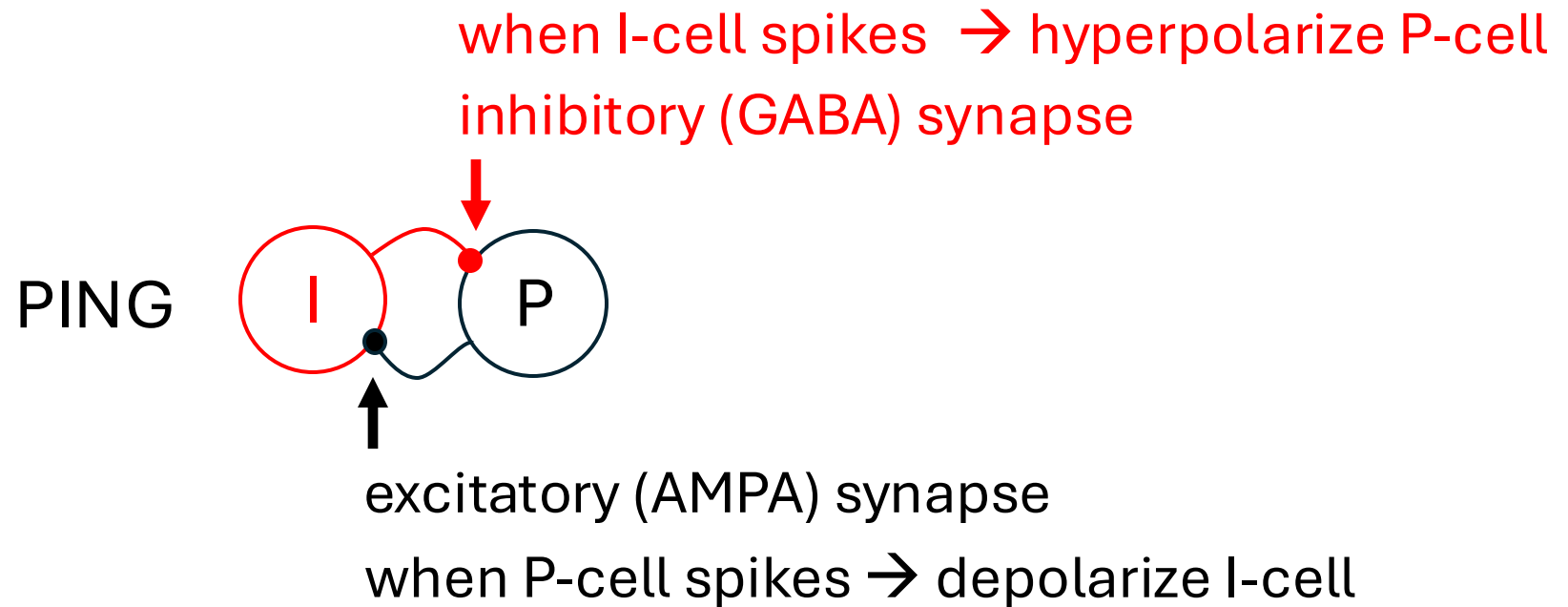


include AMPA synapse

Idea: cells collaborate to produce gamma

# PING

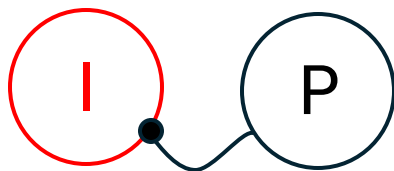
Connect cells with synapses



Build the model: HH + synapses

# PING

Include synapses



$$\frac{dV_I}{dt} = I_{Na} + I_K + I_L + I_{inj} + I_{synapse\ P \rightarrow I}$$

I-cell voltage

Synaptic current

$$I_{synapse\ P \rightarrow I} = g_P s_P (E_P - V_I)$$

maximal  
conductance

ex. synapse gate

equilibrium voltage  
for ex. synapse (0 mV)

I-cell voltage

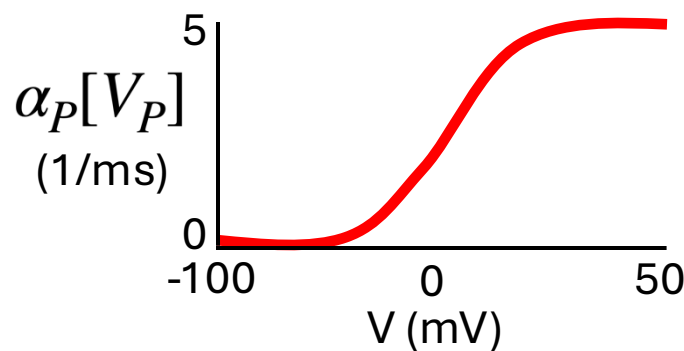
**post-synaptic** cell

Synaptic gate dynamics

$$\frac{ds_P}{dt} = \alpha_P[V_P](1 - s_P) - \beta_P[V_P]s_P$$

forward rate fxn, **pre-synaptic** V

backward rate fxn



$$\beta_P[V_P] = \beta_P = \frac{1}{\tau_d}$$

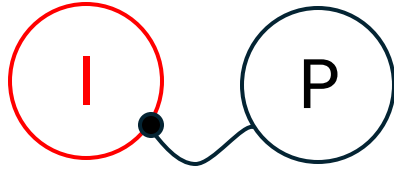
constant

decay time  $\approx 2$  ms

Note: faster than inh. synapse

# PING

Include synapses



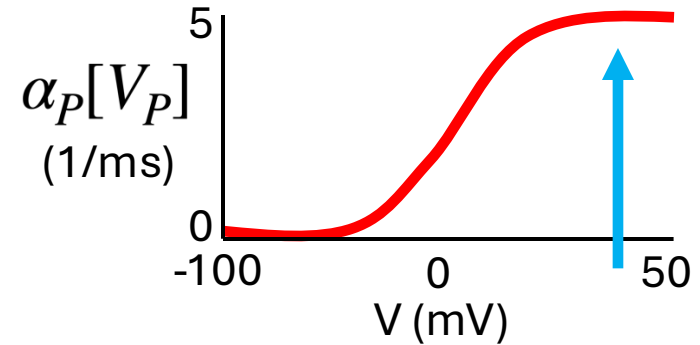
$$\frac{dV_I}{dt} = I_{Na} + I_K + I_L + I_{inj} + I_{synapse\ P \rightarrow I}$$

$$\frac{ds_P}{dt} = \alpha_P[V_P](1 - s_P) - \beta_P[V_P]s_P$$

**Q.** What happens?

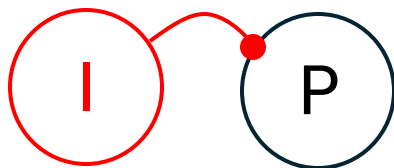
- P-cell spikes ( $V_P > 0$ )
- $\alpha_P[V_P] \rightarrow 5$
- $s_P \rightarrow 1$  (open)
- charge ( $\text{Na}^+$ ) flows in  $\rightarrow$  depolarize I-cell (push to 0 mV)

Note:  $[\text{Na}^+]_{\text{out}} \gg [\text{Na}^+]_{\text{in}}$



# PING

Include synapses



$$\frac{dV_P}{dt} = I_{Na} + I_K + I_L + I_{inj} + I_{synapse\ I \rightarrow P}$$

P-cell voltage

Synaptic gate dynamics

Synaptic current

$$I_{synapse\ I \rightarrow P} = g_I s_I (E_I - V_P)$$

maximal  
conductance

inh. synapse gate

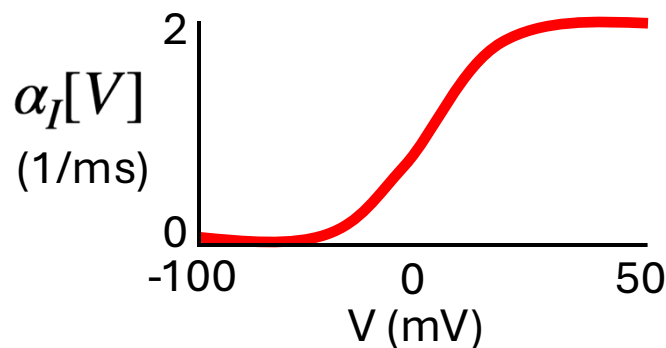
equilibrium voltage  
for inh. synapse (-80 mV)

P-cell voltage  
**post-synaptic cell**

$$\frac{ds_I}{dt} = \alpha_I[V_I](1 - s_I) - \beta_I[V_I]s_I$$

forward rate fxn, **pre-synaptic V**

backward rate fxn



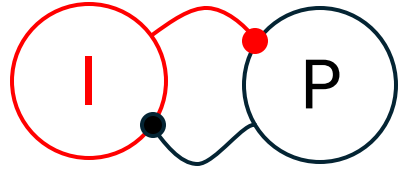
$$\beta_I[V] = \beta_I = \frac{1}{\tau_d}$$

constant

decay time  $\approx 10$  ms

# PING

Put it all together



10 variables

$$\frac{dV_P}{dt} = I_{Na} + I_K + I_L + I_{inj,P} + \overbrace{g_I S_I (E_I - V_P)}^{\text{inh. synaptic input}}$$

$$\left. \begin{aligned} \frac{dm_P}{dt} &= \\ \frac{dh_P}{dt} &= \\ \frac{dn_P}{dt} &= \end{aligned} \right\} HH$$

$$\frac{ds_P}{dt} = \alpha_P[V_P](1-s_P) - \beta_P[V_P]s_P \quad (\text{ex. gate dynamics}).$$

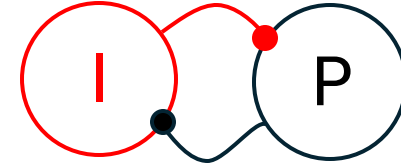
$$\frac{dV_I}{dt} = I_{Na} + I_K + I_L + I_{inj,I} + \underbrace{g_P S_P (E_P - V_I)}_{\text{ex. synaptic input}}$$

$$\left. \begin{aligned} \frac{dm_I}{dt} &= \\ \frac{dh_I}{dt} &= \\ \frac{dn_I}{dt} &= \end{aligned} \right\} HH$$

$$\frac{ds_I}{dt} = \alpha_I[V_I](1-s_I) - \beta_I[V_I]s_I \quad (\text{inh. gate dynamics})$$

# PING

Q. How does this generate a gamma rhythm?



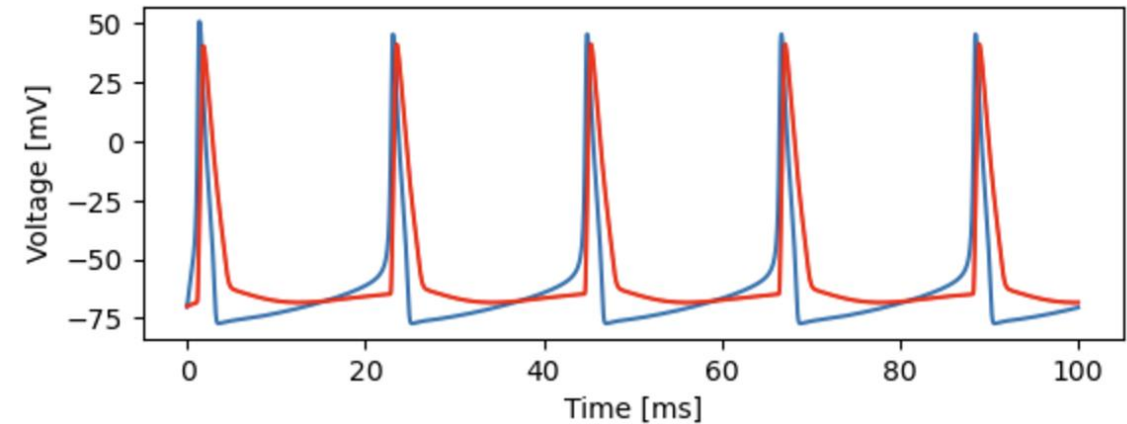
Assume P-cell has  $I_{inj,P}$  big enough to spike repeatedly in isolation

$t=0$       P-cell spikes       $\rightarrow$  excitation to I-cell       $\rightarrow$  I-cell spikes

$t \approx 0$       I-cell spikes       $\rightarrow$  inhibition to P-cell

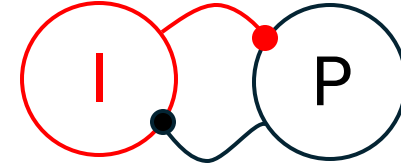
$t=25$       P-cell recovers       $\rightarrow$  P-cell spikes

Repeat ...



# PING

Q. Consistent with experimental observations?



## Experimental observations

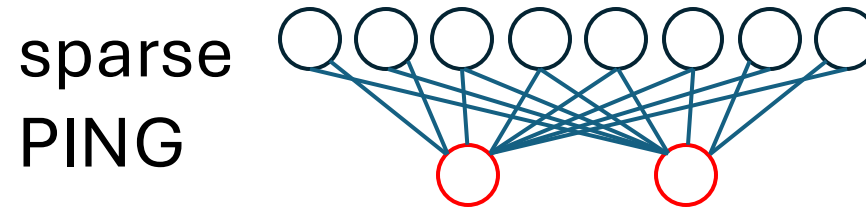
- ? (1) Excitation (driven cells)
- ? (2) GABA<sub>A</sub> critical
- ? (3) Altering GABA<sub>A</sub> kinetics changes frequency
- ? (4) AMPA critical

*Python Homework*



# Sparse PING

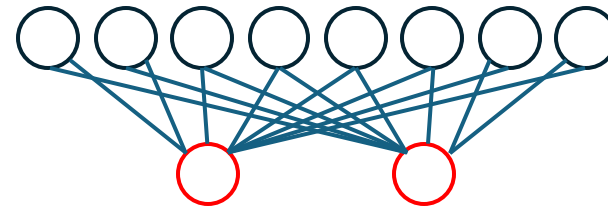
**S**parse **P**yramidal **I**nterneuron **N**etwork **G**amma



# Sparse PING

**Idea:** update the PING model to include a population of P&I cells.

**Ex.** 80 P cells & 20 I cells



Each includes HH equations

**P1**

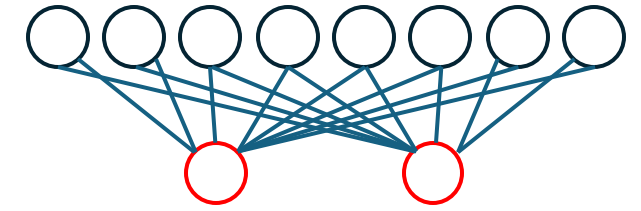
**P2**

**P3**

$C \frac{dV}{dt} = I_{\text{input}}(t) - \bar{g}_K n^4 (V - V_K) - \bar{g}_{Na} m^3 h (V - V_{Na}) - \bar{g}_L (V - V_L)$	$C \frac{dV}{dt} = I_{\text{input}}(t) - \bar{g}_K n^4 (V - V_K) - \bar{g}_{Na} m^3 h (V - V_{Na}) - \bar{g}_L (V - V_L)$	$C \frac{dV}{dt} = I_{\text{input}}(t) - \bar{g}_K n^4 (V - V_K) - \bar{g}_{Na} m^3 h (V - V_{Na}) - \bar{g}_L (V - V_L)$
$\frac{dn}{dt} = -\frac{n - n_{\infty}(V)}{\tau_n(V)}$	$\frac{dn}{dt} = -\frac{n - n_{\infty}(V)}{\tau_n(V)}$	$\frac{dn}{dt} = -\frac{n - n_{\infty}(V)}{\tau_n(V)}$
$\frac{dm}{dt} = -\frac{m - m_{\infty}(V)}{\tau_m(V)}$	$\frac{dm}{dt} = -\frac{m - m_{\infty}(V)}{\tau_m(V)}$	$\frac{dm}{dt} = -\frac{m - m_{\infty}(V)}{\tau_m(V)}$
$\frac{dh}{dt} = -\frac{h - h_{\infty}(V)}{\tau_h(V)}$	$\frac{dh}{dt} = -\frac{h - h_{\infty}(V)}{\tau_h(V)}$	$\frac{dh}{dt} = -\frac{h - h_{\infty}(V)}{\tau_h(V)}$

400 differential  
equations

# Sparse PING



Connect with synapses

Each P  $\rightarrow$  all I (with ex. synapses)

Each I  $\rightarrow$  all P (with inh. synapses)

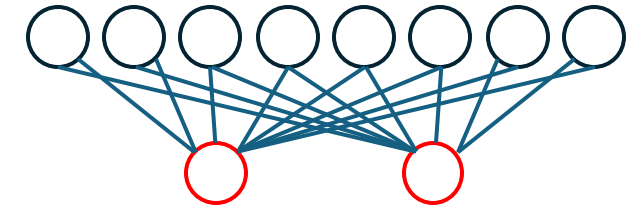
Then (for P1)

$$C \frac{dV}{dt} = I_{\text{input}}(t) - \bar{g}_K n^4 (V - V_K) - \bar{g}_{\text{Na}} m^3 h (V - V_{\text{Na}}) - \bar{g}_L (V - V_L) + I_{\text{syn } I1 \rightarrow P1} + I_{\text{syn } I2 \rightarrow P1} + \dots$$

many terms

$$\frac{ds_{I1}}{dt} = \dots, \frac{ds_{I2}}{dt} = \dots, \frac{ds_{I3}}{dt} = \dots$$

# Sparse PING

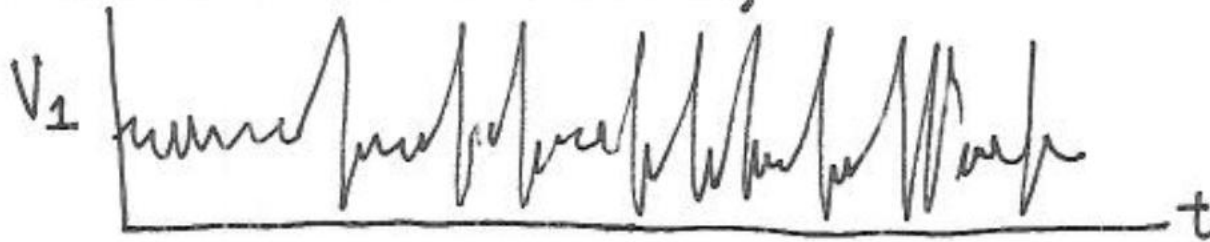


**Q.** How will the model work?

**Idea:**

- Give P cells enough depolarizing input to spike at high rate in isolation.
- Include noise in dynamics.

Then, for some P-cell in isolation,

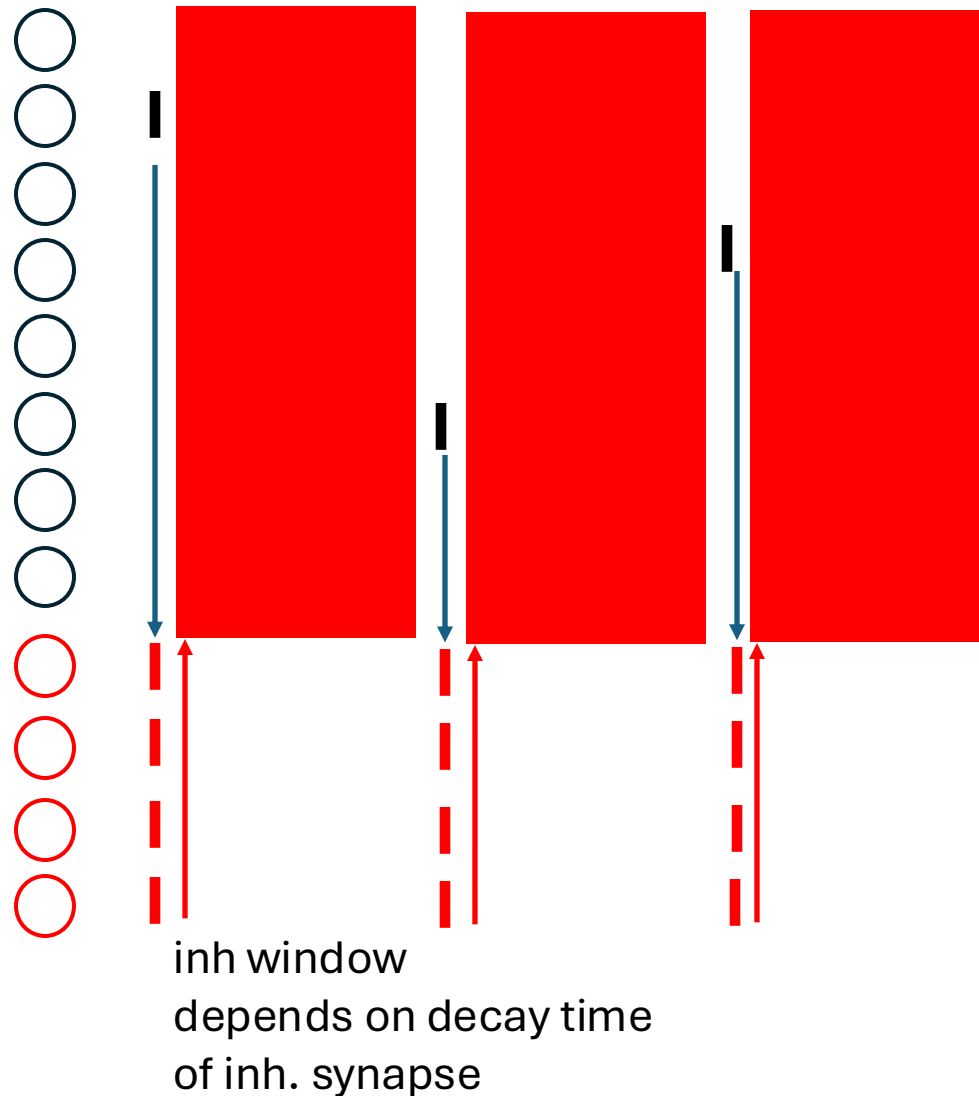


P-cell spikes.

Time between spikes  
varies due to noise.

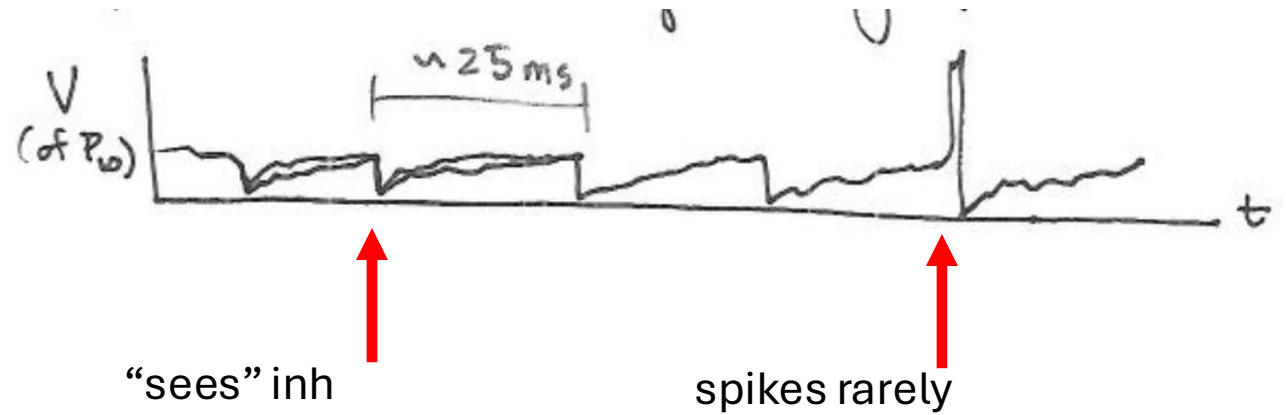
- Make synapses strong

# Sparse PING



Note: a different P-cell can spike on each cycle

Plot  $V$  for a P-cell



Each P-cell fires sparsely ... “sparse PING”

Match experimental observation

Cost: more complexity.