CSE331 Assignment 4

Section 1

Deadline: 18th December, 2022 11:59 pm

Total Marks: 30

[Submit your assignment here]

Q1: Answer each of the following questions for the context-free grammar G.

$$\begin{array}{c} R \to XRX \mid S \\ S \to \mathtt{a}T\mathtt{b} \mid \mathtt{b}T\mathtt{a} \\ T \to XTX \mid X \mid \varepsilon \\ X \to \mathtt{a} \mid \mathtt{b} \end{array}$$

- a) What are the variables of G?
- b) What are the terminals of G?
- c) Give three strings that are in L(G). [L(G) means the language recognized by the grammar G]
- d) Give three strings that are not in L(G).
- e) Convert the given CFG into an equivalent CFG in Chomsky Normal Form.

Q2: Write CFG that generate the following languages.

- a) {w | w contains even number of 0s but odd number of 1s}
- b) {w | w has equal number of 0s and 1s}
- c) {w | w has more 0s than 1s}
- d) {w | w is a palindrome}
- e) {w | w is not a palindrome}
- f) {w | w has exactly one more 0 than the number of 1s}

Q3: Convert the following CFG into CNF.

a) S, T, and U are the variables and 0 and # are the terminals.

$$\begin{array}{c} S \, \to \, TT \mid U \\ T \, \to \, \mathsf{0}T \mid T\mathsf{0} \mid \# \\ U \, \to \, \mathsf{0}U\mathsf{00} \mid \# \end{array}$$

b) A and B are the variables and 0 is the only terminal.

$$\begin{array}{l} A \,\rightarrow\, BAB \mid B \mid \varepsilon \\ B \,\rightarrow\, \mathsf{00} \mid \varepsilon \end{array}$$

c) R, S, and T are variables and a and b are two terminals.

$$\begin{split} R &\to S \mid T \\ S &\to \mathsf{a} S \mathsf{b} \mid \mathsf{a} \mathsf{b} \\ T &\to \mathsf{a} T \mathsf{b} \mathsf{b} \mid \mathsf{a} \mathsf{b} \mathsf{b} \end{split}$$

Q4: Consider the following CFG, G:

$$\begin{array}{c} S \, \to \, SS \mid T \\ T \, \to \, {\tt a}T{\tt b} \mid {\tt a}{\tt b} \end{array}$$

Show that G is ambiguous. Find a string of length 8 which will have only one leftmost derivation or parse tree.