

You have to use the designated spaces for your answers. No extra pages will be provided.

Problem 1: Regular Languages and DFAs (10 points)

Let $\Sigma = \{0, 1\}$.

$$L_1 = \{w \in \Sigma^* : w \text{ starts with odd number of 1's}\}$$

$$L_2 = \{w \in \Sigma^* : w \text{ starts and ends with same character}\}$$

- (a) Write down all strings in L_2 which are of length 3. (2 points)
- (b) Give the state diagram for a DFA that recognizes L_1 . (3 points)
- (c) Give the state diagram for a DFA that recognizes L_2 . (3 points)
- (d) Give the state diagram for a DFA that recognizes $L_1 \cap L_2$. (2 points)

(a)

(b)

(c)

(d)