

2IMW30 - FOUNDATION OF DATA MINING  
Assignment 1a Report

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## EXERCISE 2

In this exercise, we are proving that if the Jaccard similarity of two sets is 0, then minhashing always gives a correct estimate of the Jaccard similarity.

If the Jaccard similarity of two sets is 0, then the intersection of the two sets is empty. This means there are no rows which the elements are both "1" in the characteristic matrix. Hence, when performing minhashing, there cannot be any row with the same values in 2 cells. Thus  $P(h(S_i) = h(S_j)) = 0$ , which is the same as the Jaccard similarity.

## EXERCISE 3

In this exercise, we show an example that the cyclic permutations are not enough to estimate the Jaccard similarity correctly.

Let's take a look at the example in table 1. We will perform a cyclic permutation to estimate the Jaccard similarity.

Table 1: Example

	S1	S2
a	1	0
b	1	1
c	0	0
d	0	1
e	1	1

In this example, we can see that the 2 sets have 2 common words, "b" and "e". In general,  $S1 \cap S2 = \{b, e\}$  and  $S1 \cup S2 = \{a, b, d, e\}$ . Thus the (correct) Jaccard similarity is  $|S1 \cap S2| / |S1 \cup S2| = 1/2$ .

Now we perform the cyclic permutation.

- a-b-c-d-e: The signature is 1 - 2.
- b-c-d-e-a: The signature is 1 - 1.
- c-d-e-a-b: The signature is 3 - 2.
- d-e-a-b-c: The signature is 2 - 1.
- e-a-b-c-d: The signature is 1 - 1.

We have 2 rows which contain the same values on 2 cells, and 5 rows in total. So the estimated Jaccard similarity is  $2/5$ , which is not correct. The reason is the 0 - 0 row, which makes the next rows to be counted twice while every row is counted only once in the total number of permutations.