# BUTTE COLLEGE COURSE OUTLINE

### I. CATALOG DESCRIPTION

# MATH 30 - Analytic Geometry and Calculus I

5 Unit(s)

**Prerequisite(s):** MATH 20 and MATH 26 or college-level pre-calculus

**Recommended Prep:** Four years of high school college-preparatory Mathematics and

Reading Level IV

**Transfer Status: CSU/UC** 

85 hours Lecture

A first course in differential and integral calculus of a single variable: functions, limits and continuity, techniques and applications of differentiation and integration, Fundamental Theorem of Calculus. Primarily for Science, Technology, Engineering & Math Majors. (C-ID MATH 210).

#### II. OBJECTIVES

Upon successful completion of this course, the student will be able to:

- A. Compute the limit of a function at a real number.
- B. Determine if a function is continuous at a real number.
- C. Find the derivative of a function as a limit.
- D. Find the equation of a tangent line to a function.
- E. Compute derivatives using differentiation formulas.
- F. Use differentiation to solve applications such as related rate problems and optimization problems.
- G. Use implicit differentiation.
- H. Graph functions using methods of calculus.
- I. Evaluate a definite integral as a limit.
- J. Evaluate integrals using the Fundamental Theorem of Calculus.
- K. Apply integration to find area.

#### III. COURSE CONTENT

## A. Unit Titles/Suggested Time Schedule

#### Lecture

| <u>Topics</u> |  | <u>Hours</u> |
|---------------|--|--------------|
|               | efinition and computation of limits using numerical, graphical, and gebraic approaches       | 8.00         |
| 2. Co         | ontinuity and differentiability of functions   | 3.00         |
| 3. De         | erivative as a limit   | 2.00         |
| 4. Int        | terpretation of the derivative as slope of tangent line and a rate of change                 | 6.00         |
|               | fferentiation formulas: constant rule, power rule, product rule, quotient le, and chain rule | 6.00         |
|               | erivatives of transcendental functions such as trigonometic, exponential, logarithmic        | 8.00         |
|               | aplicit differentiation with applications, and differentiation of inverse nctions            | 4.00         |
| 8. Hi         | gher-order derivatives   | 2.00         |
|               | raphing functions using first and second derivatives, concavity, and symptotes               | 5.00         |

| 10. Maximum and minimum values, and optimization | 10.00 |
|--|-------|
| 11. Mean Value Theorem                           | 1.00  |
| 12. Antiderivatives and Indefinite Integrals     | 6.00  |
| 13. Area under a curve                           | 6.00  |
| 14. Definite Integral and Riemann Sum            | 3.00  |
| 15. Properties of the Integral                   | 3.00  |
| 16. Fundamental Theorem of Calculus              | 4.00  |
| 17. Integration by substitution                  | 6.00  |
| 18. Indeterminate forms and L'Hopital's Rule     | 2.00  |
| Total Hours                                      | 85.00 |

#### IV. METHODS OF INSTRUCTION

- A. Lecture
- B. Collaborative Group Work
- C. Homework: Students are required to complete two hours of outside-of-class homework for each hour of lecture
- D. Discussion
- E. Board Work

#### V. METHODS OF EVALUATION

- A. Exams/Tests
- B. Quizzes
- C. Class Assignments and Class Response
- D. Daily Homework Assignments, where the student will demonstrate problem-solving skills

#### VI. EXAMPLES OF ASSIGNMENTS

- A. Reading Assignments
  - 1. Read the section in the textbook on The Derivative and be able to set up and evaluate the limit that represents the derivative of a given function.
  - 2. Read the section in the textbook on Antiderivatives and Indefinite Integration and be able to use basic integration rules to find an indefinite integral.

#### B. Writing Assignments

- 1. Graph the functions y = x, y = |x|, and  $y = x^{(1/3)}$ , compute the derivatives of each function at the point (0,0), and describe the differentiability of these functions at this point. Assume you are explaining this to a group of students hearing this for the first time and write a detailed explanation discussing your results and why they occurred.
- 2. If p(x) is a polynomial function, explain why p(x) has exactly one antiderivative whose graph contains the origin. Assume you are explaining this to a classmate having trouble and write a detailed explanation using a general polynomial as well as giving one specific example.

## C. Out-of-Class Assignments

- 1. Review the section in the textbook on Basic Differentiation and solve the problems assigned by the instructor, showing all steps.
- 2. Review the section in the textbook on The Fundamental Theorem of Calculus and solve the problems assigned by the instructor, showing each step.

## VII. RECOMMENDED MATERIALS OF INSTRUCTION

Textbooks:

A. Larson, R. & Edwards, B.H. <u>Calculus of a Single Variable</u>. 9th Edition. Brooks/Cole Cengage Learning, 2010.

Materials Other Than Textbooks:

A. Scientific Calculator or graphing calculator without symbolic algebra capabilities

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