L = { a q | q a prime number }

Deman picks pumping length p

I pick a where n>p & n is a prime

Deman has to pick y = a k where o k < p.

I choose i> 1 exact value is deferred

New string is y = a n+(i-1)k

eo pick i = n+1 y = a n+nk = a (k+1)

n (k+1) is definitely not a prime number.

L = $\{a^n b^m \mid n \neq m\}$ hard to do with pumping & L is a mess lut $L \cap a^* b^* = \{a^n b^n \mid n \geq 0\}$ and we know this is not regular

 $\Sigma = \{0,1,+,=\}$ $L = \{x+y=3 \mid x,y,g \in \{0,1\}^* \text{ & the equation is value}$ Demon picks p $I \text{ pick } 11\cdots 1 + 0 = 11\cdots 1$

Now deman has to pick you the leading block of 1' I can choose any i +1 to win.

L= {aibi | gcd(i,j)=1}. We will show I is not regular Demon chooses p I choose 9 > p+1 & such Hat gisa prime number. My chosen string is a b & I. Demon is forced to choose y = a O < K 5 p. Elle I pung "down" i.e. choose i=0 so now $xz=a^{2-\kappa}b^{2}$ Nok 9-K > (pH)-K > 0 in fact > 1 So gcd (g-K, 2) = 1 hence XZ & I. Thus I is not regular so L is not regular. Z = {a,b, c} = { x#cy / x, y e & (a+b)*, #a(x) = #6(y)} Deven chooses P I choose atcb Demon is forced to choose y = ak ox K = P I choose i= 2 xy2 Z = a + K c b = L. Z = {0,1} Given X & IN we define unary (x) = {1"/n ex} being (x) = { we = " | a witerpreted as a bivary number ex}. If binary (X) is regular does it mean unary (X) is regular?

No! Consider $X = \{2^n | n \ge 0\}$.

briany(x) = 0^*10^n unany(x) = $\{1^n | n = 2^m \text{ for some } m\}$.

Z = {a, b} { w ∈ Z = | #a(w) + #b(w)} I pick ap both Deman is forced to pick a y = a ; p > k > 0. I pick i = (p!/k)+1. xyiz = ap+(i+) k bp!+p = ap+p! bp!+p & L. However, this is a clever arithmetic trick. Here is a simpler way: { a b | n > 0 } is not regular. Ina"b" = {a"b" n=0} Hence I is not segular so L is not regular. If S SN we define many (\$) = {1" | neS} & binary (5) = { we {0,1}" | w read as a binary number eS}. If binary (S) is regular does many (S) have to be regular No! S = {\$2^n | n≥ 1} binary (s) = 100 so clearly regular. unary (S) is not regular Demon picks p I pick 12 Demon picks x, y, z s.t |xy| 5 p, 141>0 & xy z= 12p So k := |y| = p < 2p I Pick i= 2 xy2z= \$12+x 2° < 2°+k ≤ 2°+p < 2°+2° = 2°+1 so the new string is strictly between two Consecutive powers of 2 & hence connot be a power of 2.