TURING MACHINE

9- tuple $M = (Q, \Sigma, \Gamma, +, U, \delta, s, t, r)$

Q: finite set of states

a finite set of input symbols

P: a finite set of tape symbols $U \in P \setminus \Sigma$ the blank symbol

+ G P \ E the end marker - left

8: Q× P→ Q× P× {4, R} transition function

SEQ Start state

a & Q accept state

rea reject stake

 $\delta(q,a)=(q',b,L)$ means if the machine seads a e is in state 2, it changes state to 2, crases the a swrites b and moves one step to the left.

TM's can move left or right on the tape You cannot overwrite the left end worker You cannot move left of to Once it enters a or r it never leaves

S(q,a) = (q', a, L) means you have the symbol unchanged.

A CONFIGURATION is a description & the machine at an instant of time

1011901 - HOW TO WRITE THE

CONFIGURATION AS

A STRING

uaqibo YIELDS uqaco

if 8 (2:, 6) = (2;, c, L)

Given M & input a the Start configuration is 90 w or 8 w an accept configuration is any configuration in which the state is a or ga, similarly for ran gr. An accept or reject configuration is called a halting configuration M accepts w if there is a finite sequence of configurations C1, C2, ··· Ck s.t. 1. C, is the start configuration & co 2. Each C: yields C:+1 3. Ck is an accepting configuration L(M) = { WE I * | Maccepts w} 3 outcomes are possible: accept, reject, log forever Lis Turing recognizable if F TM Ms.t Lis Turing decidable if ITM M s.t. L= L(M) & YWEZ* M halts on W. We say Lis computably enumerable on C E if L = L(M) for some TM
We say L is computable or decidable if Malways halts & L = L(M)Old krminology: recursively enumerable (RE) for CE & recursive for décidable.

Obviously any decidable language is recognizable (CE).

