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Spatial Clustering Approach for Vessel Path Identification

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ABSTRACT This paper addresses the challenge of identifying the paths for vessels with operating routes of repetitive paths, semi-repetitive paths, and new paths. We propose a spatial clustering approach for labeling the vessel paths by using position information only. We develop a path clustering framework employing two methods: a distance-based path modeling and a likelihood estimation method. The former enhances the accuracy of path clustering through the integration of unsupervised machine learning techniques, while the latter focuses on likelihood-based path modeling and introduces segmentation for a more detailed analysis. The result findings highlight the superior performance and efficiency of the developed approach. The approach aims to offer valuable insights for route planning, ultimately contributing to improving the safety and operation practices in the maritime transportation.

INDEX TERMS Spatial clustering, vessel path identification, maritime transportation, average nearest neighbor distance, hierarchical clustering, likelihood estimation.

I. INTRODUCTION

A. BACKGROUND AND MOTIVATION

Maritime transportation is crucial for global trade, generating extensive vessel trajectory data that reveals intricate spatial and temporal navigation patterns. Understanding these patterns is vital for effective maritime traffic surveillance and management [15].

A *trajectory* refers to a sequence of consecutive geographical points, each representing a specific location at a given timestamp [23]. Trajectories, observed in various scenarios such as pedestrian movements, vehicular routes, and natural events like wildlife migrations or hurri-

cane, involve time-evolving position data. Trajectory mining aims to uncover significant patterns within datasets, enabling tasks like path classification, anomaly detection for accidents or traffic congestions, surveillance for suspicious activities, and prediction of vessel trajectories in different landscapes [9].

It is crucial to distinguish between 'trajectory' and 'path' when studying movement data. The term 'trajectory' typically denotes the movement of an object over time, while *path* refers to the specific route taken by the object. For instance, if an object travels from origin to destination, its trajectory is the sequence of geographical points

it passed through, while its path is the specific route taken, such as a sidewalk, street, highway, lane, railway, or waterway.

Additionally, the term *route* is synonymous with path or trajectory, as long as it shares the same origin and destination. Conversely, any difference in either the origin or destination represents another route.

Path clustering is the process of grouping paths into clusters based on their similarity.

Path clustering is a versatile technique that has found its niche in a wide range of practical applications. In the realm of navigation, path identification empowers systems to generate clear and detailed instructions for users seeking their way. Traffic analysis benefits from path clustering as it facilitates the identification of diverse traffic patterns, such as the smooth flow of traffic on highways and the congestion often encountered on city streets. Path identification proves equally valuable in route planning, enabling the optimization of routes for transportation systems, including public and maritime transportation services [24].

In the scope of maritime industry, path identification from Automatic Identification System (AIS) data is a challenging task due to the high spatial freedom and high frequency of ship navigation in sea areas. Thus, it is an imperative task to develop a path identification tool integrating with route planning systems for improving maritime safety and optimizing vessel routing. As data-driven approaches from AIS data continue to grow and evolve, path clustering will undoubtedly play an increasingly important role for understanding vessel behavior and supporting decision-making in maritime transportation [18].

B. AIMS AND CONTRIBUTIONS

This paper aims to address the challenge of identifying vessel paths in scenarios characterized by repetitive, semi-repetitive, and new paths. In general, the aims and contributions of the proposed approach in this paper can be outlined as follow:

- The proposed clustering approach of vessel paths only requires position information, specifically longitude and latitude.
- The clustering approach has a proven added value for clustering challenging unseen or undefined paths.
- The approach is robust and interpretable by applying a similarity measure that reduces the influence of noise or outliers and offers a clear interpretation of path clustering.
- The approach has a customized parameter to determine the number of path classes, thereby enhancing the flexibility and adaptability of the framework, allowing users to tailor it to their specific needs.
- The approach also has a method to study and analyze the patterns within specific segments of path.
- It is a data-driven solution that can be used as a valuable asset for informed decision-making in route planning and optimization, traffic management, and resource allocation.

The rest of this paper is organized as follows. Section II reviews the related work on vessel path identification. Section III describes our proposed spatial clustering approach in detail. The real-world vessel data of our case study is described in Section IV. Section V presents the results of our experimental evaluation. Section VI concludes the paper and discusses future work.

II. RELATED WORK

Path clustering can be done using a variety of different methods [20]. We will explore the related works of these various methods.

Clustering is gaining popularity for route extraction. Machine learning (ML) has recently been applied extensively for vessel path identification, learning patterns from historical data. The study presented in [14] introduced a framework, Traffic Route Extraction and Anomaly Detection (TREAD), which utilizes unsupervised learning for maritime route extraction. The primary emphasis is on anomaly detection and route

prediction, highlighting the crucial role of AIS data in enhancing maritime situational awareness. The work specifically addresses challenges related to intermittency and persistence in AIS data. Another method of route extraction was proposed in [19], transforming ship trajectories into ship trip semantic object (STSO) and utilizing graph theory for route extraction. The method proves robustness in extracting traffic routes for merchant ships but may have limitations for vessels with frequent navigation behavior changes, such as fishing vessels. While the approach in [22] adopts a dynamic time warping (DTW) distance as a similarity measure, and considering vessel course changes to analyze its trajectories. Experiments demonstrated its high accuracy in distinguishing and detecting similar vessel trajectories, outperforming existing methods in accuracy and cluster degree evaluation. Moreover, [3] presents a machine learning framework for maritime vessel trajectory analysis, incorporating clustering, classification, and outlier detection. It employs piecewise linear segmentation for compression and alignment kernels to integrate geographical domain knowledge, enhancing task performance. Results show reduced computation time without compromising accuracy.

Capobianco et al. [2] proposed a deep learning approach using recurrent neural networks, employing a Bidirectional Long Short-Term Memory (BiLSTM) layer as an encoder and a Unidirectional Long Short-Term Memory (LSTM) layer as a decoder, for vessel trajectory prediction. Their model outperforms baseline approaches, showcasing the effectiveness of sequence-to-sequence neural networks. In their study, Li et al. [11] presents an AIS data-based machine learning method for feature extraction and unsupervised route planning for Maritime Autonomous Surface Ships (MASS). The method uses Automatic and Adaptive Dynamic Time Warping (AADTW), Spectral Clustering with Affinity Feature (SCAF), and a route optimization algorithm based on dynamic program-

ming to extract features, obtain movement patterns, and plan routes. The proposed method outperforms existing methods by considering the impact of hidden factors and providing different routes for different types of MASS. The work in [10] systematically analyzes the performance of twelve ship trajectory prediction methods, including classical machine learning and emerging deep learning techniques. It compares twelve methods across three AIS datasets, representing different maritime traffic scenarios, and evaluates their effectiveness based on six indexes. The study concludes that traditional machine learning-based trajectory prediction methods struggle to meet the rising demands for accuracy and real-time performance, leading to increased interest in and promising results from deep learning-based approaches.

A maritime traffic route extraction approach based on multi-dimensional density-based spatial clustering of applications with noise (MD-DBSCAN) developed in [8]. The approach incorporates trajectory compression, similarity measures, and extraction of ship trajectories clusters. The approach demonstrating effectiveness in noise reduction and route extraction. The authors in [16] proposed a trajectory clustering method based on Hierarchical Density-Based Spatial Clustering of Applications with Noise (HDBSCAN) and Hausdorff distance to generate similarity matrix. The method adapts to shape characteristics and exhibits good clustering scalability and improved clustering results compared to DBSCAN, k-means, and spectral clustering algorithms.

Eljabu et al. proposed spatial clustering methods (SPTCLUST and SPTCLUST-II) in [5] and [4] respectively, for maritime traffic routes extraction from AIS data. The approach consists of data preprocessing, path finding, and route extraction without using traditional clustering algorithms. It achieved high F1-scores 97% and 99% for tankers and cargoes maritime traffic routes.

The study in [7] enhanced the DBSCAN

method by integrating the Mahalanobis distance metric for vessel behavior modeling. The proposed methodology includes clustering historical AIS data and detecting anomalies. The study showcases applicability to diverse water regions, contributing to situational awareness, collision prevention, and route planning.

Farahnakian et al. [6] conducted a comprehensive examination of clustering-based techniques, including k-means, DBSCAN, Affinity Propagation (AP), and the Gaussian Mixtures Model (GMM), for detecting abnormal vessel behaviors from AIS data. Results indicate that k-means is particularly effective in detecting dark ships and spiral vessel movements, crucial for enhancing maritime safety. Furthermore, the study [13] proposed two methods for trajectory outlier detection are proposed, with the first utilizing DBSCAN clustering and Hausdorff distance, and the second employing Support Vector Machine (SVM) classifier and the Generalized Sequence Pattern algorithm. Both models outperform the baselines, with the SVM approach demonstrating superior performance in the identification of traffic patterns and outliers.

The research paper [12] offers a detailed survey of visual analytics for vessel trajectory data. The authors discuss a variety of methods, including map-based visualization, timeline-based visualization, and interactive visualization.

The paper [21] comprehensively reviews various approaches for vessel trajectory predicting, including clustering algorithms and machine learning algorithms. It also discusses the challenges and future research directions, such as the uncertainty in the data, the dynamic environment, and the computational complexity. Among these challenges, which are subjects of ongoing research and require additional attention: navigating dynamic maritime environments poses a substantial challenge in accurately identifying vessel paths (I). Ensuring stability, explainability, and managing the computational cost of the model add further complexity (II). Additionally, addressing the need for flexibility,

scalability, and practical applicability is crucial for a comprehensive solution in the field of vessel path identification (III).

Motivated by these challenges, we aim to develop a framework that focuses on vessel path identification and potentially tackling such challenges faced in maritime transportation.

III. METHODOLOGY

The theoretical background and description of the underlying methodology of our proposed framework are covered within this section. The framework of vessel path identification is depicted in Figure 1.

1) Problem Formulation

The equations (1-3) serve as a mathematical representation to describe the clustering of vessel paths.

It is worth mentioning that the clustering process is conducted sequentially, point by point, while the labeling of path classes is performed to the entire voyage. Therefore, each voyage has a single label of path class.

$$Voyages \in Path\ Classes \quad (1)$$

$$Voyages = \{ts_1[p_1, \dots, p_n], \dots, ts_j[p_1, \dots, p_n]\} \quad (2)$$

$$Path\ Class\ Set = \{class_1, \dots, class_k\} \quad (3)$$

where:

Voyages: a collection of time series representing the voyage of the vessel taken through a path with a predicted clustered class.

ts_j: a time series of a voyage *j* a sequence of *n* data points, where each data point *p* represents the vessel position and is defined by a pair of coordinates, namely latitude and longitude.

n: a time duration of each voyage, it can be different from voyage to another.

j: a total number voyages.

Path Class Set: a set of *k* classes into which the path of voyages is being clustered.

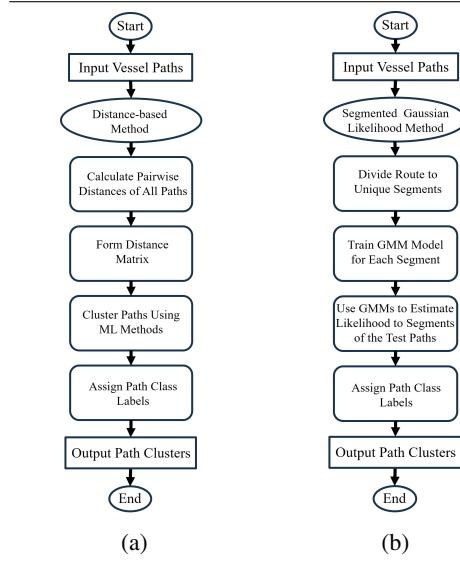


FIGURE 1: Framework of vessel path identification. (a) Flowchart of distance-based method. (b) Flowchart of segmented Gaussian likelihood method.

2) Distance-Based Method

The similarity between two paths is measured by the average nearest neighbor distance (ANND), as shown in Eq. (4).

$$ANND(i,j) = \frac{1}{n_i} \sum_{k=1}^{n_i} Distance(P_i^k, NN(P_j^k)) \quad (4)$$

where:

$ANND(i,j)$: is the average nearest neighbor distance between path i and path j , present in the distance matrix at row i and column j . It is a symmetric, meaning that $ANND(i,j)$ is the same as $ANND(j,i)$.

$Distance(P_i^k, NN(P_j^k))$: The distance between the k^{th} point in path i , denoted as P_i^k , and its corresponding nearest neighbor point in path j , indicated as $NN(P_j^k)$. n_i is the total number of points in path i .

The measure $Distance$ is an Euclidean distance. However, for longer curved routes, Haversine or Great-circle distance is more suitable.

The ANND, as expressed in Eq. (4), is computed by averaging the distances between each point in one path and its nearest neighbor in the other path.

Then, the similarity value (i.e., ANND) of this pair of paths is stored as an element in the distance matrix.

A lower ANND indicates that the paths within a cluster are more similar. The distance matrix will have dimensions $(m \times m)$, where m is the number of paths.

For instance, the computed distance matrix for a set of 12 paths is illustrated in Figure 2.

After the construction of distance matrix, machine learning (ML) technique is applied for clustering the paths based on their corresponding values in distance matrix. The ML techniques that we used are k-means, Gaussian Mixture Model (GMM), and hierarchical clustering method.

	North_East	North_Middle	North_West	South	South_West	North_East	North_Middle	South	South_West	North_West	North_Middle
North_East	0	3.42	8.51	11.73	16.42	1.24	2.74	11.51	11.34	15.38	8.46
North_Middle	3.3	0	6.57	13.13	15.66	4.12	1.03	13.02	17.92	14.26	6.6
North_West	8.58	6.43	0	18.02	10.1	8.96	6.81	18.07	18.07	10.68	0.39
South	13.74	16.71	20.75	0	5.99	12.84	16.18	0.47	0.64	4.96	20.6
South_West	21.37	21.17	14.67	8.6	0	20.12	21.21	8.73	8.9	1.03	14.56
South_East	1.05	3.96	8.49	9.83	14.36	0	3.31	9.61	15.31	13.8	8.42
North_Middle_South	3.07	1.05	0	12.31	13.11	3.71	0	15.54	17.75	14.07	5.0
South_South	13.09	16.21	20.11	0.45	5.79	12.22	15.62	0	0.43	4.82	19.97
South_South_West	13.61	16.71	20.09	0.64	6.02	12.74	16.11	0.47	0	5.12	20.52
South_West_South	19.93	19.91	14.98	7.83	1.02	18.63	19.05	7.95	9.19	0	14.77
North_West_South	8.37	6.29	0.4	18.31	10.64	8.67	6.77	18.37	16.31	11.21	0
North_Middle_South	3.07	0.87	6.44	12.82	15.69	3.77	0.99	12.7	12.62	14.29	6.53

FIGURE 2: Part of distance matrix, it is for 12 paths.

3) Segmented Gaussian Likelihood Method

In addition to identifying the vessel's path, to better understand how the vessel changes its paths, we employ Gaussian distributions on several distinct segments of the vessel route. The process of this technique can be summarized as follows:

- Utilize a training dataset comprising vessel position information that should adequately represent all potential paths of the vessel route.
- Divide the route into different distinct segments.

- Train a single GMM model for each segment to find the Gaussian distributions of all segments of the route.
- Estimate likelihoods of the segments by using the trained GMM models with their corresponding segments of each vessel voyage in test dataset.
- Label the path classes based on the estimated likelihood at the unique segments of the route.

IV. CASE STUDY

In this section, we describe the case study, including the data collection, preprocessing and analysis.

A. DATA COLLECTION

In this study, we utilized a dataset that was collected from a ship named Cinderella II, which is a passenger ship operates in the Stockholm archipelago. The dataset spans over five months, from July to November 2022, and it comprises information of 124 voyages of this vessel, connecting between two main ports of Vaxholm in the east and Sodra in the west.

More information about Cinderella II can be found on [1]. For instance, the specifications of this vessel are 19 meters in length and 6.41 meters in breadth, boasts a gross tonnage of 68. Operating under the flag of Sweden, its maritime mobile service identity (MMSI) is 265513810. With a reported draught of 2.5 meters and a recorded average speed of 8.2 knots (4.2 m/s).



FIGURE 3: Image of the Cinderella II ship [1].

B. DATA PREPROCESSING AND ANALYSIS

In our approach, we emphasize on the significance of data representation. As a result, we

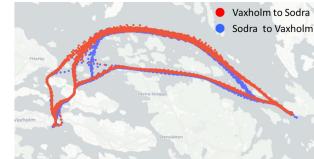
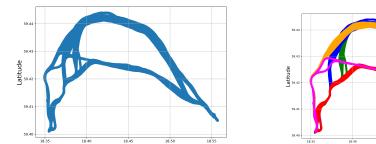


FIGURE 4: Map of vessel route.



(a) The vessel route. (b) Main classes of path

FIGURE 5: The vessel route before and after applying path identification

group the path points based on their timestamps of one second resolution with a resolution of one second, and store these grouped path points with distinctive Voyage IDs. Afterward, these paths are ready to be sent to the path clustering approach to determine the overall path class. Statistical analysis is conducted to figure out how the vessel paths are different in terms of fuel, time, distance and speed.

The histograms representing these quantities across various path classes can be observed in Figure 7. Notably, when vessel traverses the shorter southern paths, it employs slower speeds, effectively reducing fuel consumption without significantly impacting travel time.

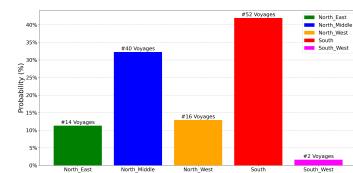


FIGURE 6: Distribution of voyages across the five path classes

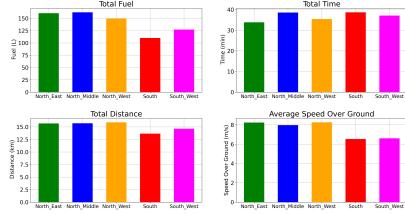


FIGURE 7: Average fuel and time, distance, and speed of five path classes

V. RESULTS AND DISCUSSION

In this section, we present the results of our spatial clustering approach for vessel path identification and discuss the implications of these findings. The approach involved the utilization of position information and various clustering techniques, specifically k-means, hierarchical clustering, and Gaussian distributions clustering with dataset contains 124 voyages.

A. EVALUATION OF PATH CLUSTERING

The results of vessel path identification are evaluated through visual illustration and tabulation using metrics such as confusion matrix, precision, recall, and F1-score [17].

The hits and messes of path clustering are presented by the confusion matrix.

For our results of path clustering, the confusion matrix is a one-vs-one type matrix. Then, the confusion matrix is converted into a one-vs-all type matrix (binary-class confusion matrix) as shown in Eq. (5), for calculating class-wise metrics like precision, recall, and F1-score.

	Pred. Pos.	Pred. Neg.
Act. Pos.	TP	FN
Act. Neg.	FP	TN

(5)

where True Positives (TP), False Positives (FP), True Negatives (TN), and False Negatives (FN) are determined by comparing the predicted (Pred.) and actual (Act.) path classes.

- Precision: the ratio of true positives to the total number of predicted positives.

- Recall: the ratio of true positives to the total number of actual positives in the data.
- F1-score: the harmonic mean of precision and recall.

The equations for precision, recall, and F1-score are shown in Eqs. (6), (7), and (8).

$$\text{Precision} = \frac{TP}{TP + FP} \quad (6)$$

$$\text{Recall} = \frac{TP}{TP + FN} \quad (7)$$

$$\text{F1-score} = 2 \times \frac{(Precision \times Recall)}{(Precision + Recall)} \quad (8)$$

B. DISCUSSION

Table 1 shows the results of applying k-means or Gaussian Mixture Model (GMM) models to identify the vessel paths from the distance matrix in the distance-based method of the path identification approach.

Notably, the paths with classes of North-West, South, and South-West demonstrated a F1-score of 1, indicating that the approach correctly identified all paths of these classes.

In contrast, the North-East and North-Middle paths exhibited lower F1 scores compared to other classes. The path class of North-Middle is the most challenging path to identify, since 6 paths of it have been clustered as North-East, as shown in Figure 9, which is the visualization for the approach results by using k-mean or GMM clustering models.

Figure 10 illustrates the probability distribution of misclustered paths with respect to latitude and longitude coordinates. It is obvious that these paths have nearly identical coordinates, which making them challenging paths to be clustering with k-means or GMM. This suggests that there is still room for improvement by using other ML clustering methods.

Table 2 presents the results of employing hierarchical clustering to the distance matrix in the distance-based method for clustering the vessel

paths. In the hierarchical clustering, there is a parameter called "Dendrogram Cut-off threshold" and its value should be selected depending on the number of path classes. Hence, as illustrated in Figure 11, this parameter is denoted by the Y-axis as a clustering height, and its value is set to 100 for clustering the vessel path into five classes.

Remarkably, all path classes achieved an F1-score of 1, indicating that hierarchical clustering successfully identified all paths with high accuracy from the distance matrix using the distance-based method. This suggests that the choice of ML clustering technique with the distance matrix can influence the accuracy of path identification. Table 2 displays the outcomes of clustering, now by applying the segmented likelihood Gaussian method. This method achieved perfect precision, recall, and F1-score for all path classes.

Figures 12, 13, and 14 present visualizations for the segmented Gaussian likelihood method.

The accuracy in results by hierarchical and segmented Gaussian likelihood clustering for path classes indicating the efficacy of the developed approach of spatial clustering for vessel paths identification.

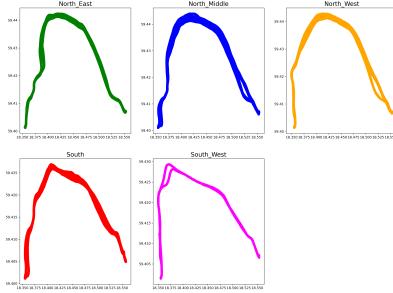


FIGURE 8: Individual Display of the Five Path Classes.

VI. CONCLUSION

The approach is able to identify the vessel paths with partially defined or unknown paths.

TABLE 1: Result of implementing k-means or GMM clustering to five path classes

(a) Precision, Recall, and F1-score

Paths	Precision	Recall	F1-score
North-East (NE)	0.7	1	0.824
North-Middle (NM)	1	0.85	0.919
North-West (NW)	1	1	1
South (S)	1	1	1
South-West (SW)	1	1	1

(b) Confusion Matrix

Actual	Predicted					Total
	NE	NM	NW	S	SW	
NE	14	0	0	0	0	14
NM	6	34	0	0	0	40
NW	0	0	16	0	0	16
S	0	0	0	52	0	52
SW	0	0	0	0	2	2
Total	20	34	16	52	2	124

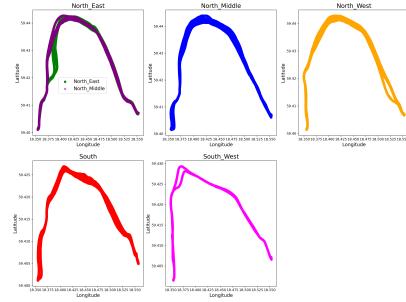


FIGURE 9: Results of k-means or GMM clustering to five path classes.

In the distance-based method, the hierarchical clustering used in the approach outperforms k-means and GMM clustering techniques.

The approach of hierarchical clustering includes a user-customized, a cut-off threshold, which allows desired control for the number of path classes, enhancing the flexibility and adaptability of the proposed approach.

In the distance-based method, adopting ANND as a measure of similarity makes path clustering less affected by noise or outliers and

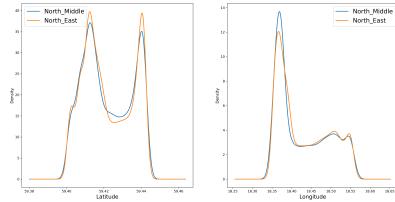


FIGURE 10: Probability distribution of location coordinates for misclustered paths by k-means or GMM.

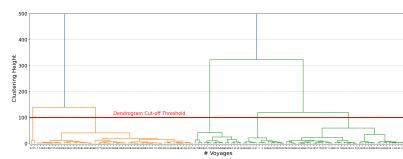


FIGURE 11: Results of hierarchical clustering to five path classes.

provides a more intuitive interpretation of path similarity, ultimately enhancing the robustness and interpretability of our approach.

The segmented Gaussian likelihood method is particularly useful for identifying and analyzing the vessel path alterations at different segments of the vessel route.

The proposed approach is computationally efficient and has the potential to be a valuable

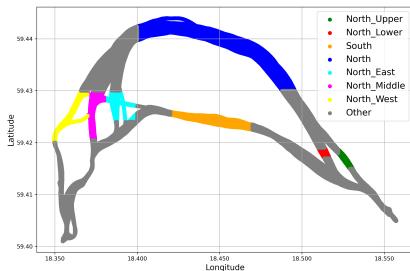


FIGURE 12: Distribution of the route into eight segments.

TABLE 2: Result of implementing hierarchical clustering or segmented likelihood Gaussian clustering to five path classes

(a) Precision, Recall, and F1-score

Paths	Precision	Recall	F1-score
North-East (NE)	1	1	1
North-Middle (NM)	1	1	1
North-West (NW)	1	1	1
South (S)	1	1	1
South-West (SW)	1	1	1

(b) Confusion Matrix

Actual	Predicted					Total
	NE	NM	NW	S	SW	
NE	14	0	0	0	0	14
NM	0	34	0	0	0	34
NW	0	0	16	0	0	16
S	0	0	0	52	0	52
SW	0	0	0	0	2	2
Total	14	34	16	52	2	118

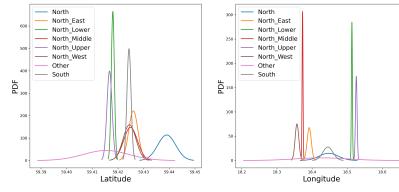


FIGURE 13: Probability distributions of location coordinates for the eight segments of the route.

tool for planning vessel paths. Accurate path identification can contribute to safer and more efficient maritime transportation practices, aiding in route planning, collision avoidance, and navigation optimization.

Nevertheless, the framework has some potential limitations, such as the segmented Gaussian likelihood method exhibiting sensitivity to segment definition which could affect its salable performance, particularly in complex maritime scenarios. Moreover, while the study case demonstrates that the framework is computationally efficient, it is essential to discuss any potential scalability issues, especially when dealing

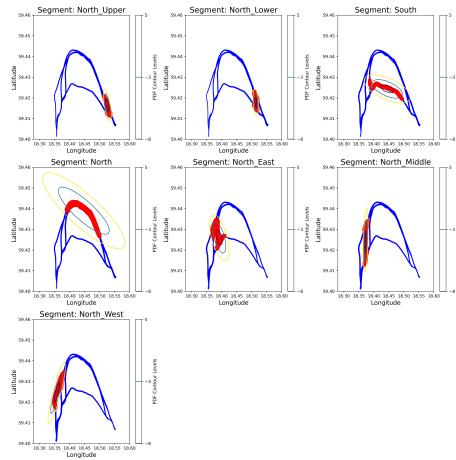


FIGURE 14: Gaussian distributions for seven segments of the route.

with large datasets, since the computational efficiency may vary depending on the dataset size and the nature of paths.

Further work could explore the scalability and real-world applicability of the proposed clustering approach, as well as its integration with related systems of maritime transportation.

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SUPPLEMENTARY MATERIALS

The source codes that are implemented on Python 3.9.7 to produce the results are available at: https://github.com/MohamedAbuella/Path_Clustering

REFERENCES

- [1] Marine Traffic. [Online]. Available: https://www.marinetraffic.com/en/ais/details/ships/shipid:322946/mmsi:265609540/imo:8619821/vessel:CINDERELLA_II, November 2023.
- [2] Samuele Capobianco, Leonardo M Millefiori, Nicola Forti, Paolo Braca, and Peter Willett. Deep learning methods for vessel trajectory prediction based on recurrent neural networks. *IEEE Transactions on Aerospace and Electronic Systems*, 57(6):4329–4346, 2021.
- [3] Gerben Klaas Dirks De Vries and Maarten Van Someren. Machine learning for vessel trajectories using compression, alignments and domain knowledge. *Expert Systems with Applications*, 39(18):13426–13439, 2012.
- [4] Lubna Eljabu, Mohammad Etemad, and Stan Matwin. Spatial clustering method of historical ais data for maritime traffic routes extraction. In *2022 IEEE International Conference on Big Data (Big Data)*, pages 893–902. IEEE, 2022.
- [5] Lubna Eljabu, Mohammad Etemad, and Stan Matwin. Spatial clustering model of vessel trajectory to extract sailing routes based on ais data. *International Journal of Computer and Systems Engineering*, 16(10):491–501, 2022.
- [6] Farshad Farahnakian, Florent Nicolas, Fahimeh Farahnakian, Paavo Nevalainen, Javad Sheikh, Jukka Heikkonen, and Csaba Raduly-Baka. A comprehensive study of clustering-based techniques for detecting abnormal vessel behavior. *Remote Sensing*, 15(6):1477, 2023.
- [7] Xuyang Han, Costas Armenakis, and Mojgan Jadidi. Modeling vessel behaviours by clustering ais data using optimized dbscan. *Sustainability*, 13(15):8162, 2021.
- [8] Changhai Huang, Xucun Qi, Jian Zheng, Runchao Zhu, and Jia Shen. A maritime traffic route extraction method based on density-based spatial clustering of applications with noise for multi-dimensional data. *Ocean Engineering*, 268:113036, 2023.
- [9] Jae-Gil Lee, Jiawei Han, and Kyu-Young Whang. Trajectory clustering: a partition-and-group framework. In *Proceedings of the 2007 ACM SIGMOD international conference on Management of data*, pages 593–604, 2007.
- [10] Huanhuan Li, Hang Jiao, and Zaili Yang. Ais data-driven ship trajectory prediction modelling and analysis based on machine learning and deep learning methods. *Transportation Research Part E: Logistics and Transportation Review*, 175:103152, 2023.
- [11] Huanhuan Li and Zaili Yang. Incorporation of ais data-based machine learning into unsupervised route planning for maritime autonomous surface ships. *Transportation Research Part E: Logistics and Transportation Review*, 176:103171, 2023.
- [12] Haiyan Liu, Xiaohui Chen, Yidi Wang, Bing Zhang, Yunpeng Chen, Ying Zhao, and Fangfang Zhou. Visualization and visual analysis of vessel trajectory data: A survey. *Visual Informatics*, 5(4):1–10, 2021.
- [13] Angelos Moaviniis, Anastasios Gounaris, and Ioannis Constantinou. Detection of anomalous trajectories for vehicle traffic data. In *Proceedings of the Workshops of the EDBT/ICDT 2023 Joint Conference, Ioannina, Greece*, 2023.
- [14] Giuliana Pallotta, Michele Vespe, and Karna Bryan. Vessel pattern knowledge discovery from ais data: A framework for anomaly detection and route prediction. *Entropy*, 15(6):2218–2245, 2013.
- [15] Enmei Tu, Guanghao Zhang, Lily Rachmawati, Eshan

- Rajabally, and Guang-Bin Huang. Exploiting ais data for intelligent maritime navigation: A comprehensive survey from data to methodology. *IEEE Transactions on Intelligent Transportation Systems*, 19(5):1559–1582, 2017.
- [16] Lianhui Wang, Pengfei Chen, Linying Chen, and Junmin Mou. Ship ais trajectory clustering: An hdbscan-based approach. *Journal of Marine Science and Engineering*, 9(6):566, 2021.
- [17] Ran Yan, Shuaian Wang, and Chuansheng Peng. An artificial intelligence model considering data imbalance for ship selection in port state control based on detention probabilities. *Journal of Computational Science*, 48:101257, 2021.
- [18] Ran Yan, Shuaian Wang, Lu Zhen, and Gilbert Laporte. Emerging approaches applied to maritime transport research: Past and future. *Communications in Transportation Research*, 1:100011, 2021.
- [19] Zhaojin Yan, Yijia Xiao, Liang Cheng, Rong He, Xiaoguang Ruan, Xiao Zhou, Manchun Li, and Ran Bin. Exploring ais data for intelligent maritime routes extraction. *Applied Ocean Research*, 101:102271, 2020.
- [20] Guan Yuan, Penghui Sun, Jie Zhao, Daxing Li, and Canwei Wang. A review of moving object trajectory clustering algorithms. *Artificial Intelligence Review*, 47:123–144, 2017.
- [21] Xiaocai Zhang, Xiuju Fu, Zhe Xiao, Haiyan Xu, and Zheng Qin. Vessel trajectory prediction in maritime transportation: Current approaches and beyond. *IEEE Transactions on Intelligent Transportation Systems*, 2022.
- [22] Liangbin Zhao and Guoyou Shi. A novel similarity measure for clustering vessel trajectories based on dynamic time warping. *The Journal of Navigation*, 72(2):290–306, 2019.
- [23] Yu Zheng. Trajectory data mining: an overview. *ACM Transactions on Intelligent Systems and Technology (TIST)*, 6(3):1–41, 2015.
- [24] Yu Zheng and Xiaofang Zhou. *Computing with spatial trajectories*. Springer Science & Business Media, 2011.