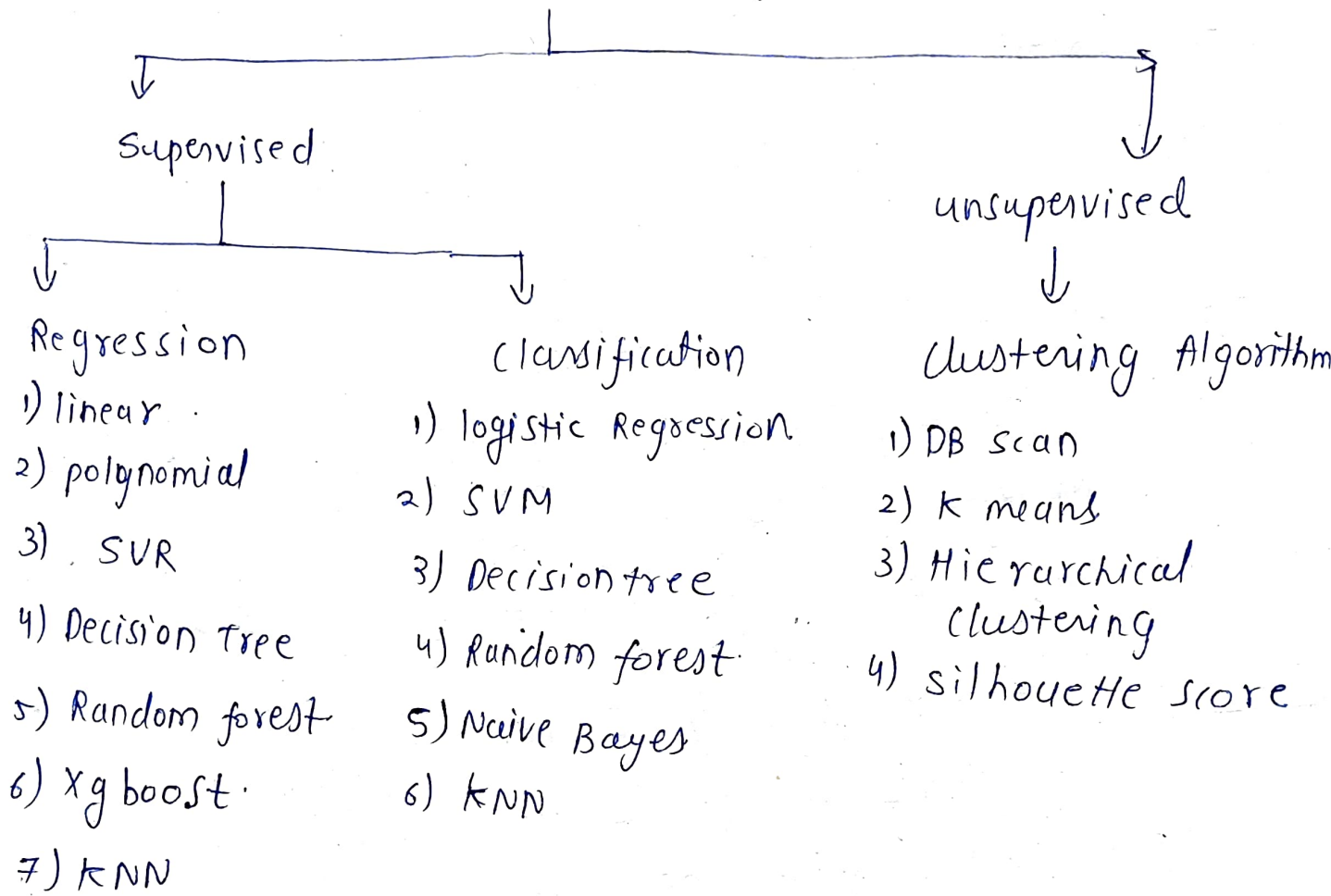


Machine learning



1) supervised \Rightarrow dataset \Rightarrow output is known

2) unsupervised \Rightarrow dataset \Rightarrow output is unknown.

① supervised Learning Examples

ex: 1

Degree	Experience	Salary
BE	7	50k
PHD	2	70k
ME	1	30k
M Tech	4	40k
—	—	—

Independent features:

Degree, Experience

Dependent feature:

Salary.

Since salary is continuous feature
 \therefore It is an example of Regression.

Ex: 2 House price prediction

\therefore price is continuous feature

\therefore Regression.

Ex: 3 Flight fare prediction.

Since fare prediction will be a continuous feature

Therefore it is an example of regression.

Ex: 4 Predict Air quality Index.

Since AQI is continuous feature

Therefore Regression example

② classification (supervised learning).

No. of playing hours	No. of study hours	Exam Result
9	1	0
7	2	0
3	3	1
4	5	1
\vdots	\vdots	\vdots
\vdots	\vdots	\vdots
\vdots	\vdots	\vdots

Pass = 1

fail = 0

I.F \Rightarrow No. of playing hours and No. of study hours.

D.F \Rightarrow Exam Result.

Since Exam Result is categorical feature.
Therefore it is an example of classification.

Ex: 2 Algerian Forrest fire dataset.

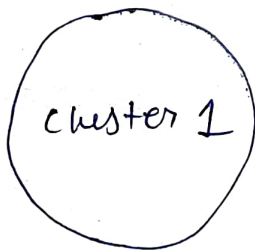
Since Dependent feature is categorical
Therefore classification example

③ unsupervised learning

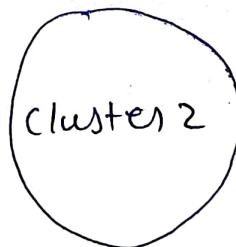
Dataset

Age	Salary	Spending (1-10) Score
24	70k	1
26	100k	9
⋮	⋮	⋮
21	20k	9
25	120k	2

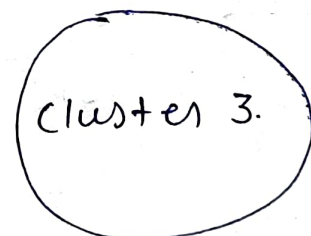
Prediction
↓
product
discount



→ Earn more
→ Spend more



→ Earn less
→ spend less



→ Earn less
→ spend more.

Above is customer segmentation example.

① simple Linear Regression:

It is used when we have one Independent variable and one dependant variable.

Ex: Training dataset

Height	Weight
6	29
5	55
4	66
6	72

Aim: To create a model which takes input as height and predicts weight.

Ex:

No. of Rooms	Price of house
2	20k
3	40k
4	60k

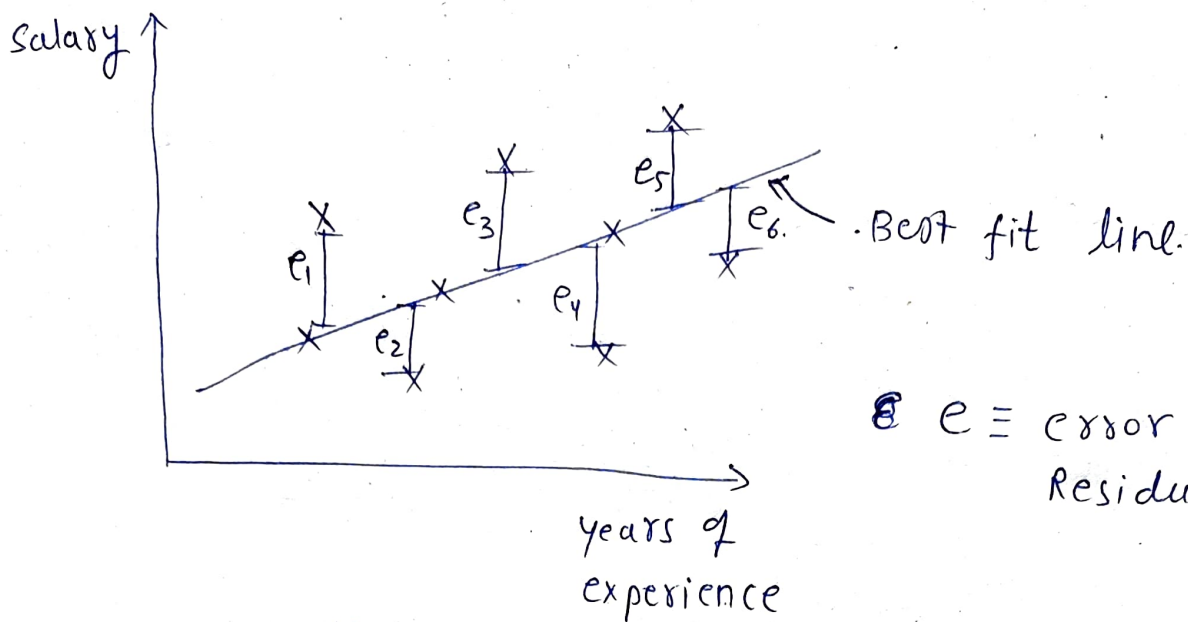
Aim:

model \Rightarrow I/P No. of rooms
└ predicts price of house

Ex:

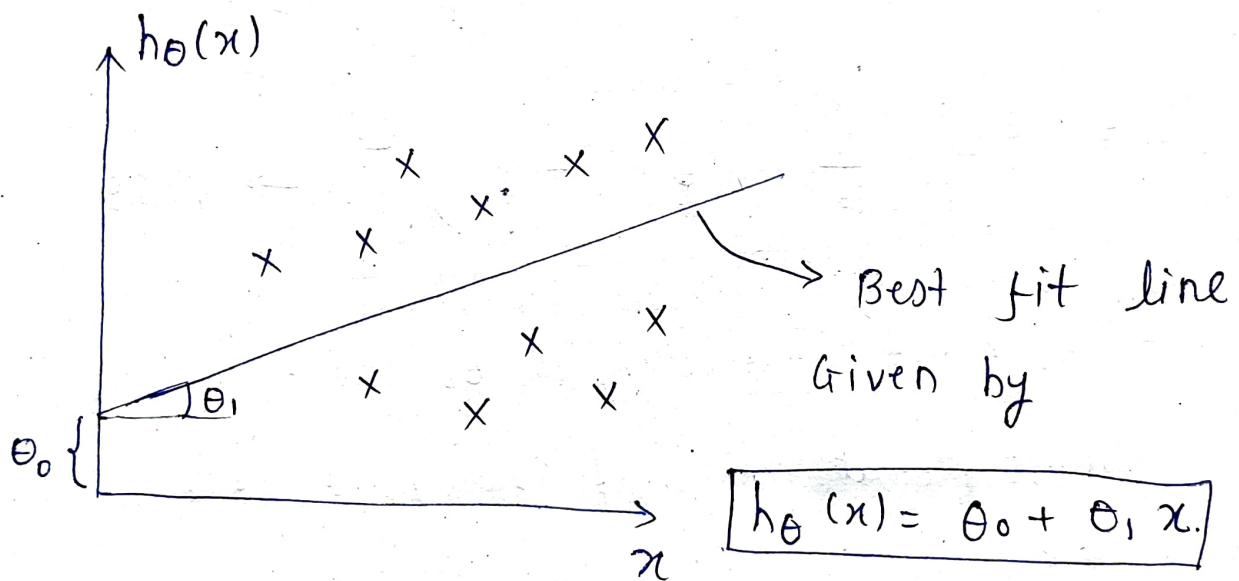
Years of Experience	Salary
2	10k
3	40k
5	70k

Aim: model \Rightarrow I/P years of Experience
└ predicts Salary



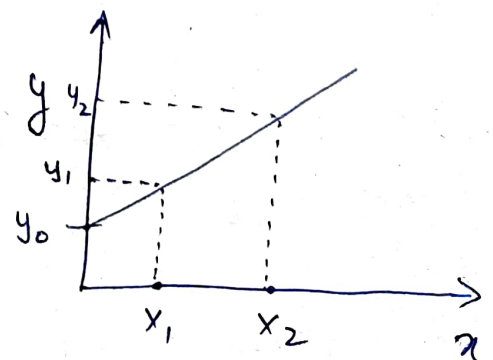
$e \equiv$ error or Residual.

We need to find Best fit line in such a way that \sum Error or Residuals is minimum.



where θ_0 is Intercept.
 θ_1 is slope.

To get best fit line
we change θ_0 and θ_1 .



$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{Intercept} = y_0$$

Cost Function

A cost function is an important parameter that determines how well a machine learning model performs for a given dataset. It calculates the difference between the expected value and predicted value and represents it as a single real number.

Cost function is a measure of how wrong the model is in estimating the relationship b/w input and output parameter.

$$J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m \left(h_{\theta} x^{(i)} - y^{(i)} \right)^2 \rightarrow \text{MSE}$$

Here $J(\theta_0, \theta_1)$ = cost function at θ_0 and θ_1 ,

m \equiv Total number of data points in dataset.

$y^{(i)}$ = actual value of dependent feature.

$h_{\theta}(x)^i$ = predicted value of dependent feature.

The above cost function is called mean square error (MSE)

The aim is to minimise this mean square error i.e. the cost function.

Example $h_{\theta}(x) = \theta_0 + \theta_1 x$

consider $\theta_0 = 0$

lets have a dataset for $h_{\theta}(x) = \theta_1 x$

X	y
1	1
2	2
3	3

\Rightarrow Training dataset.

Here $y \Rightarrow$ dependent feature

$x \Rightarrow$ Independent feature.

X	y	$h_{\theta}(x)$ $\theta=0$	$h_{\theta}(x)$ $\theta=0.5$	$\frac{h_{\theta}x}{\theta=1}$	$h_{\theta}x$ $\theta=1.5$
1	1	0	0.5	1	1.5
2	2	0	1	2	3
3	3	0	1.5	3	4.5

at $\theta=0$

$$J(\theta_1) = \frac{1}{3} ((0-1)^2 + (0-2)^2 + (0-3)^2) = 4.67$$

at $\theta=0.5$

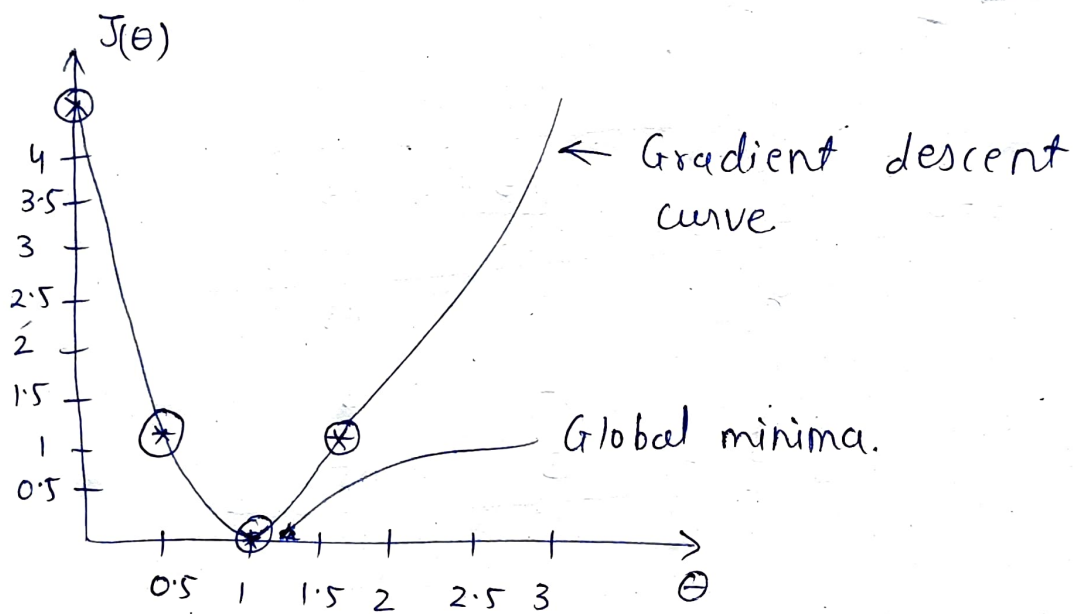
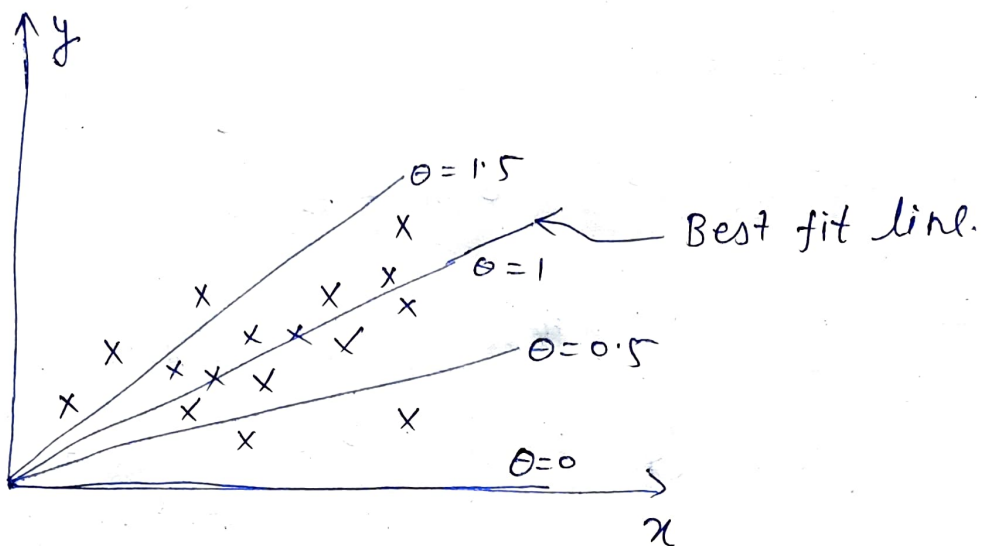
$$J(\theta_1) = \frac{1}{3} ((0.5-1)^2 + (1-2)^2 + (1.5-3)^2) = 1.16$$

at $\theta=1$

$$J(\theta_1) = \frac{1}{3} ((1-1)^2 + (2-2)^2 + (3-3)^2) = 0$$

at $\theta=1.5$

$$J(\theta_1) = \frac{1}{3} ((1.5-1)^2 + (3-2)^2 + (4.5-3)^2) = 1.16$$



Gradient descent is an optimization algorithm, which is used for optimizing the cost function or error in the model.

Gradient descent is an iterative approach where model gradually converges towards minimum value. and if model further iterates it produces little or zero change in Loss.

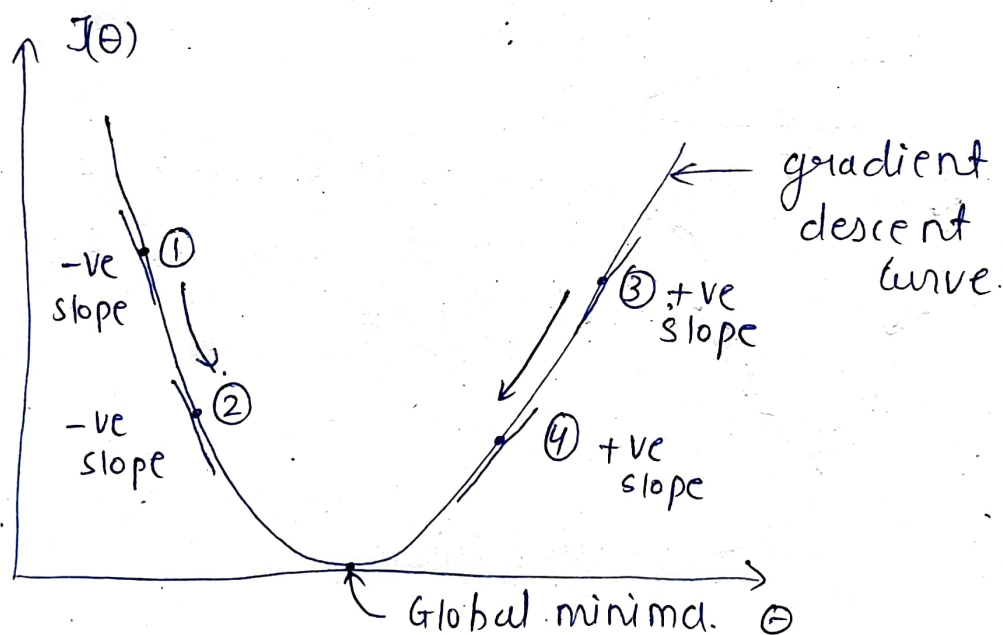
Convergence Algorithm.

Equation for gradient descent in Linear regression.

$$\theta_j = \theta_j - \alpha \frac{d J(\theta_j)}{d \theta_j}$$

Here $\alpha \equiv$ learning rate

$$\frac{d J(\theta_j)}{d \theta_j} = \text{slope of } J(\theta) \text{ and } \theta \text{ curve.}$$



at point 1 slope = (-ve)

$$\theta_j = \theta_j - \alpha (-k_1)$$

$$\theta_j = \theta_j + \alpha k_1$$

at point 2 slope = -ve

$$\theta_j = \theta_j - \alpha (-k_2)$$

$$= \theta_j + \alpha k_2$$

..... we are moving close to global minima.

at point 3 slope = +ve

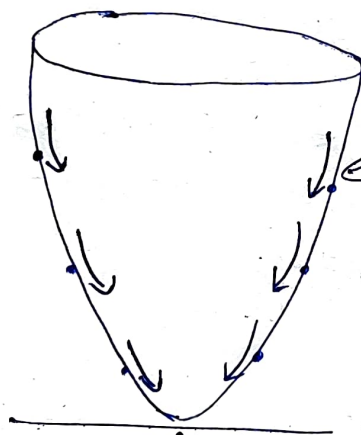
$$\begin{aligned}\theta_j &= \theta_j - \alpha(+k_3) \\ &= \theta_j - \alpha k_3\end{aligned}$$

at point 4 slope = +ve

$$\begin{aligned}\theta_j &= \theta_j - \alpha(+k_4) \\ &= \theta_j - \alpha k_4\end{aligned}$$

----- we are moving close to global minima.

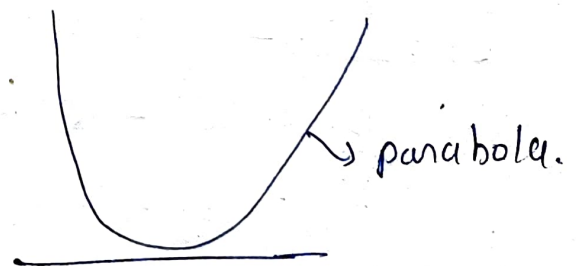
Note: If θ_0 and θ_1 both considered.

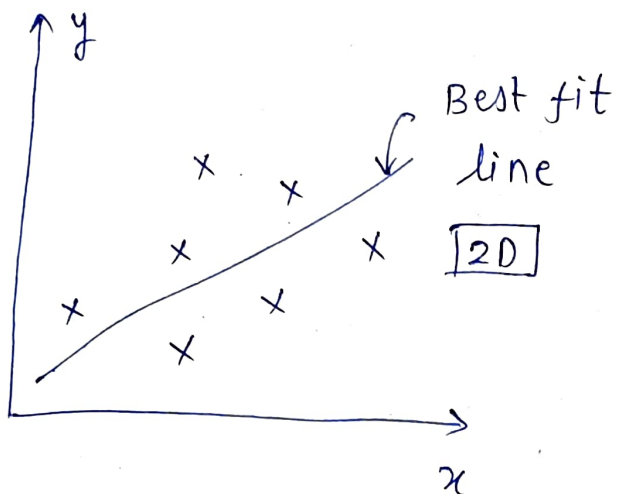


Gradient descent curve will be 3D object.

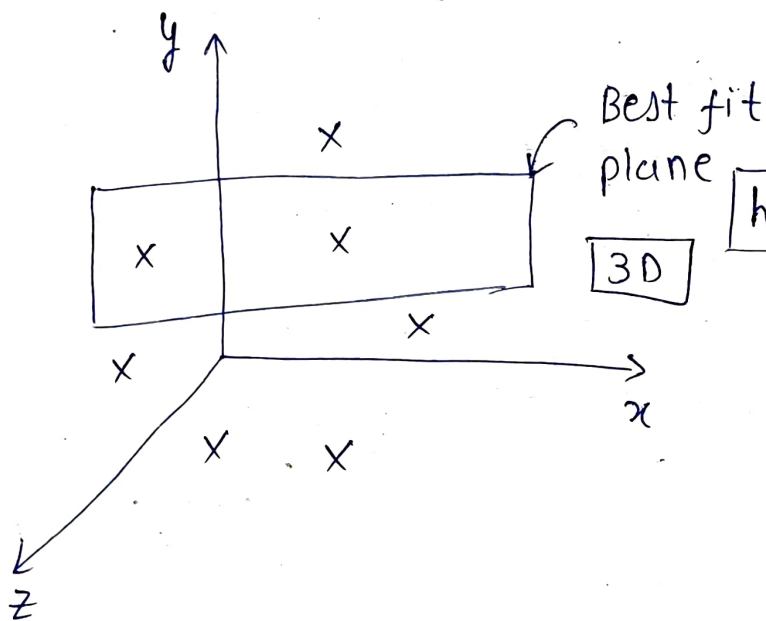
Global minima.

MSE \Rightarrow is reason we get gradient descent curve





$$h_{\theta}(x) = \theta_0 + \theta_1 x$$



$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x$$

* If there are more than 3 Dimensions then we get hyper plane.

Ex:
$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x + \theta_3 x$$

hyper plane.

Ex:

I.F. ₁	I.F. ₂	I.F. ₃	D.F.
No. of rooms	city	Room size	House price