$\begin{array}{c} costvar, \ c \\ termvar, \ x, \ y, \ z, \ f \\ baseAttackVar, \ b \\ index, \ i, \ j, \ k \\ A, \ B, \ C, \ E \\ & \mid \quad b \\ & \mid \quad A \odot B \\ & \mid \quad A \cup B \\ & \mid \quad A \multimap B \\ & \mid \quad A \multimap B \\ & \mid \quad (A) \end{array}$ 

## $\Gamma; \Delta \vdash T$

$$\frac{}{\varsigma;b\vdash b} \quad \text{T-VAR}$$
 
$$\frac{}{b;\cdot\vdash b} \quad \text{T-VARC}$$
 
$$\frac{\Gamma_1;\Delta_1\vdash T_1\quad \Gamma_2;\Delta_2\vdash T_2}{\Gamma_1,\Gamma_2;\Delta_1,\Delta_2\vdash T_1\odot T_2} \quad \text{T-PARA}$$
 
$$\frac{\Gamma_1;\Delta_1\vdash T_1\quad \Gamma_2;\Delta_2\vdash T_2}{\Gamma_1,\Gamma_2;\Delta_1,\Delta_2\vdash T_1\rhd T_2} \quad \text{T-SEQ}$$
 
$$\frac{\Gamma_1;\Delta_1\vdash T_1\quad \Gamma_2;\Delta_2\vdash T_2}{\Gamma_1,\Gamma_2;\Delta_1,\Delta_2\vdash T_1 \sqcup T_2} \quad \text{T-CHOICE}$$

 $\Theta; \Psi \vdash E$ 

$$\begin{array}{ccc} \overline{\cdot;E\vdash E} & \text{E\_VAR} \\ \hline & \overline{E;\cdot\vdash E} & \text{E\_VARC} \\ \hline & \frac{\Theta_1;\Psi_1\vdash E_1 & \Theta_2;\Psi_2\vdash E_2}{\Theta_1,\Theta_2;\Psi_1,\Psi_2\vdash E_1\odot E_2} & \text{E\_PARAI} \\ \hline & \frac{\Theta_1;\Psi_2\vdash E_1\odot E_2 & \Theta_2;\Psi_1,E_1,E_2,\Psi_3\vdash E_3}{\Theta_1,\Theta_2;\Psi_1,\Psi_2,\Psi_3\vdash E_3} & \text{E\_PARAE} \\ \hline & \frac{\Theta_1;\Psi_1\vdash E_1 & \Theta_2;\Psi_2\vdash E_2}{\Theta_1,\Theta_2;\Psi_1,\Psi_2\vdash E_1\rhd E_2} & \text{E\_SEQI} \\ \hline \end{array}$$

$$\frac{\Theta_{2};\Psi_{2} \vdash E_{1} \rhd E_{2} \quad \Theta_{1}, E_{1}, E_{2}, \Theta_{3}; \Psi_{2} \vdash E_{3}}{\Theta_{1}, \Theta_{2}, \Theta_{3}; \Psi_{1}, \Psi_{2} \vdash E_{3}} \quad \text{E_seqE}}{\frac{\Theta_{1}, \Psi_{1}, E_{1}, E_{2}, \Psi_{2} \vdash E}{\Theta; \Psi_{1}, E_{2}, E_{1}, \Psi_{2} \vdash E}} \quad \text{E_ex}}$$

$$\frac{\Theta_{1}; \Psi_{1} \vdash E_{1} \quad \Theta_{2}; \Psi_{2} \vdash E_{2}}{\Theta_{1}, \Theta_{2}; \Psi_{1}, \Psi_{2} \vdash E_{1} \sqcup E_{2}} \quad \text{E_choice}}{\frac{\Theta_{1}; \Psi_{1} \vdash E_{1} \quad \Theta_{2}; \Psi_{1} \vdash E_{2}}{\Theta; \Psi \vdash E_{1} \multimap E_{2}}} \quad \text{E_impI}}$$

$$\frac{\Theta_{1}; \Psi_{1} \vdash E_{1} \multimap E_{2} \quad \Theta_{2}; \Psi_{2} \vdash E_{1}}{\Theta_{1}, \Theta_{2}; \Psi_{1}, \Psi_{2} \vdash E_{2}} \quad \text{E_impE}}{\frac{\Theta_{1}; \Psi_{1} \vdash E_{1} \multimap E_{2} \quad \Theta_{2}; \Psi_{2} \vdash E_{1}}{\Theta; \Psi \vdash (T \sqcup T) \multimap T}} \quad \text{E_choiceCont}}$$

$$\frac{\Theta_{1}; \Psi \vdash T_{1} \sqcup T_{2}}{\Theta; \Psi \vdash (T_{1} \sqcup T_{2}) \bowtie (T_{2} \sqcup T_{1})} \quad \text{E_choiceSym}}{\frac{\Theta_{1}; \Psi \vdash (T_{1} \sqcup T_{2}) \sqcup T_{3}}{\Theta; \Psi \vdash ((T_{1} \sqcup T_{2}) \sqcup T_{3}) \multimap (T_{1} \sqcup (T_{2} \sqcup T_{3}))}} \quad \text{E_choiceAssoc}}$$

$$\frac{\Theta_{1}; \Psi \vdash T_{1} \circlearrowleft (T_{2} \trianglerighteq T_{3})}{\Theta; \Psi \vdash (T_{1} \circlearrowleft (T_{2} \sqcup T_{3})) \multimap ((T_{1} \circlearrowleft T_{2}) \sqcup (T_{1} \circlearrowleft T_{3}))} \quad \text{E_ldistPara}}$$

$$\frac{\Theta_{1}; \Psi \vdash T_{1} \circlearrowleft (T_{2} \sqcup T_{3})}{\Theta; \Psi \vdash (T_{1} \trianglerighteq (T_{2} \sqcup T_{3})) \multimap ((T_{1} \trianglerighteq T_{2}) \sqcup (T_{1} \trianglerighteq T_{3}))}} \quad \text{E_ldistPara}}$$

$$\frac{\Theta_{1}; \Psi \vdash T_{1} \trianglerighteq (T_{2} \sqcup T_{3})}{\Theta; \Psi \vdash (T_{1} \trianglerighteq (T_{2} \sqcup T_{3})) \multimap ((T_{1} \trianglerighteq T_{2}) \sqcup (T_{1} \trianglerighteq T_{3}))}} \quad \text{E_ldistSeq}}$$

Definition rules: 20 good 0 bad Definition rule clauses: 36 good 0 bad