Proposing a New Foundation of Attack Trees in Monoidal Categories

Harley Eades III

Computer and Information Sciences, Augusta University, Augusta, GA,
heades@augusta.edu

Abstract. TODO

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A Source Sink Graphs are Symmetric Monoidal